



Design Consideration and Implementation of Analog Adaptive Filters for Sensor Response Correction

M. Jafaripناه, B. M. Al-Hashimi and N. M. White

University of Southampton
{mj01r,bmah,nmw}@ecs.soton.ac.uk

Abstract : *This paper considers the design issues relating to the practical implementation of analog adaptive filters to the area of sensor compensation, of which there is little reported work in the literature. Recently, we have demonstrated the effectiveness of analog adaptive techniques in sensor response correction through simulation [1]. The case is illustrated by showing how the response of a load cell can be improved to speed up the process of measurement. The load cell is a sensor with an oscillatory output in which the measurand contributes to the response parameters. Thus, a compensation filter needs to track variation in measurand whereas a simple, fixed filter is only valid at one specific load value. To allow a practical implementation of the adaptive techniques, a novel piecewise linearization technique is proposed in order to vary a floating voltage-controlled resistor in a linear manner over a wide range. Practical results are presented, thus demonstrating the feasibility of the proposed techniques.*

Keywords : Analog Adaptive Filter, Sensor, Load Cell, Response correction.

Introduction

Load cells are used in a variety of industrial weighing applications such as vending machines and checkweighing systems. Since information processing and control systems cannot function correctly if they receive inaccurate input data, compensation of the imperfections of sensors is one of the most important aspects of sensor research. Influence of unwanted signals, non ideal frequency response, parameter drift, non-linearity, and cross-sensitivity are the five major defects in primary sensors [3]. In the new generation of sensors, called intelligent or smart sensors, the influence of these imperfections has been dramatically reduced by using signal processing techniques, which have resulted from advances in the field of digital systems.

Some sensors such as load cells have an oscillatory output, which needs time to settle down. Dynamic measurement refers to the ascertainment of the final value

of a sensor signal while its output is still in oscillation. It is therefore necessary to determine the value of the measurand in the fastest time possible. One example of processing that can be done on the sensor output signal is filtering to achieve response correction. Several methods have been reported addressing this problem. Software techniques for sensor compensation are reviewed in [2]. Digital adaptive techniques have been used in [13] for load cell response correction. An artificial neural network has been proposed for dynamic measurement which needs a learning phase [14]. Other methods such as employing a Kalman filter [6] and estimation with recursive least square (RLS) procedure [10] have also been applied for dynamic weighing systems. Almost all the above reported methods are based on digital signal processing techniques, which need analog-to-digital converters and powerful signal processors.

Although digital techniques have been used efficiently, the aim of this paper is to investigate the possibility of using analog adaptive techniques for sensor response correction. The potential benefits of analog adaptive techniques compared to digital methods include higher signal processing speeds, lower power dissipations, and smaller integrated circuit areas. It should be noted that most applications of analog adaptive techniques have focused on communications and digital magnetic storage [4] and there has been little or no work on application of analog adaptive techniques to intelligent sensors which is the main focus of this paper. In [1], we have developed models for the sensor and compensation filter. These models are discussed briefly in sections 2 and 3. In section 4, for practical implementation of the models, a new piecewise linearization method is proposed and also experimental results are presented.

2. Sensor Response Correction

The primary sensor is considered as a system with transfer function $G(s)$. The general principle for eliminating the transient time is shown in Fig.1. A filter having the reciprocal characteristic of the sensor is cascaded with it. Therefore, the transfer function of the

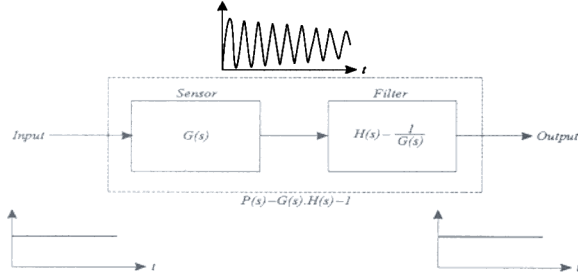


Figure 1: General principle of load cell response correction

whole system is “unity” which means that any changes in the input transfer to the output without any distortion.

The response of a load cell can change for different measurands. For example, the characteristic of a load cell changes when a load is applied to it because the mass of the load contributes to the inertial parameters of the system. Therefore the transfer function of the filter should change accordingly. In other words, a fixed filter can be used only for one specific load value.

Previous work has shown that the load cell can be modelled as a 2^{nd} order system [13].

$$(m + m_0) \cdot \frac{d^2 y(t)}{dt^2} + c \cdot \frac{dy(t)}{dt} + k \cdot y(t) = F(t) \quad (1)$$

Where m is the mass being weighed, m_0 is the effective mass of the sensor, c is the damping factor, k is the spring constant, and $F(t)$ is the force function. The Laplace transfer function of this sensor is

$$G(s) = \frac{Y(s)}{F(s)} = \frac{\frac{1}{m+m_0}}{s^2 + \frac{c}{m+m_0}s + \frac{k}{m+m_0}} = \frac{A}{s^2 + \frac{\omega_0}{Q}s + \omega_0^2} \quad (2)$$

This shows that m affects all inertial parameters of the sensor such as gain factor, A , quality factor, Q , and natural frequency, ω_0 .

Eq. 2 yields a pair of complex conjugate poles $a \pm jb$ where

$$a = -\frac{c}{2(m + m_0)} \quad (3)$$

and

$$b = \sqrt{\frac{k}{(m + m_0)} - \frac{c^2}{4(m + m_0)^2}} \quad (4)$$

Thus the zeros of the adaptive filter, which are the poles of the sensor can be obtained.

In general, assume w is defined as a vector that contains all of the parameters of adaptive filter i.e.

$$w = [w_1 \ w_2 \ w_3 \ \dots]^T \quad (5)$$

The elements of w can be calculated for different values of the measurand. To emphasise that w depends on m , it can be written as $w(m)$. m is unknown in the first instance when a new measurement begins. Therefore the parameters of the adaptive filter can not be set to appropriate values in order that the filter behaves as an inverse system. Hence, an adaptive rule is required to modify the parameters of the adaptive

filter according to the value of measurand. This rule is a crucial element but there is not a straightforward solution for it. Usually, in classic adaptive techniques, an adaptive algorithm, such as least mean squares (LMS) method, updates w to minimize a cost function. However, Eq.(2) shows that, for a load cell, the suitable filter has a pair of conjugate zeros, $z_{1,2} = a \pm jb$, which, a and b can be considered as the parameters of adaptive filter and the relationship between them and load can be modelled as in Eqs.(3) and (4). The real-time measurement operation is shown in Fig.2.

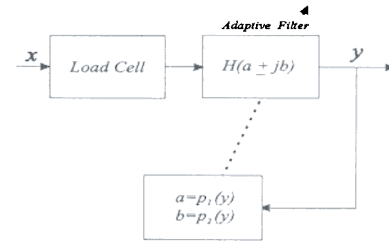


Figure 2: Block diagram of adaptive load cell response correction

In this block diagram m has been substituted with y , the output of the whole system, which is proportional to m . Initially the zeros of the filter are set to arbitrary values. Then the output y is calculated. This new value of y is used to calculate the zeros of the filter once again. Repeating these steps results in a rapid approach to obtain the steady state value of y .

So far the zeros of the 2^{nd} order compensation filter have been examined. In order that the analog filter can be realised, it is necessary to add at least two poles to the filter. The values of these poles can be determined practically. For simulation purposes, these poles are selected by trial and error so that the output of the filter quickly reaches its steady-state value with minimum oscillation. The transfer function of the compensation filter is

$$H(s) = \frac{(m + m_0)}{10^{-5}} \cdot \frac{s^2 + \frac{c}{m+m_0}s + \frac{k}{m+m_0}}{s^2 + 600s + 10^5} \quad (6)$$

The transfer functions of the load cell (Eq. 2) and its compensation filter (Eq. 6) are biquadratic functions. There now exists a wealth of theoretical and experimental information on the design of fixed or non-adaptive analog biquads [5]. The problem is how to make a biquad adaptive and it is necessary to have only one filter component to track changes in m without any influence on the other parameters such as damping factor, c , and the spring coefficient, k .

3. Overview of Sensor and Compensation Filter Models

In [1], we have shown that how biquadratic filters can be used effectively to model the behaviour of the sensor and compensation filter. For instance, compensation filter model is depicted in Fig.3. To make this biquad adaptive, as described in the block diagram of Fig.2, the filter's zeros have to be changed by the output of the biquad. It is possible to use a voltage-controlled

resistor in the compensation filter instead of R_8 which models $(m + m_0)$ in Eq.(6). R_8 has to be split into a fixed resistor equal to m_0 and an additional resistor proportional to m . Since m is the mass being weighed, in the sensor model it is equivalent to stimulating voltage (V_i) and in the compensation filter model it should be directly proportional to filter output voltage.

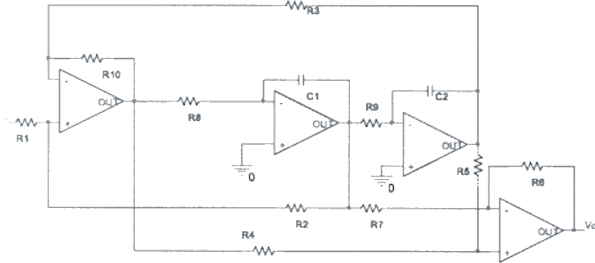


Figure 3: Compensation filter model

For simulation purposes, the analog behavioural modeling facility in PSpice can be used. This is achieved by using the G component (a voltage-controlled current source) and "TABLE", which allows the user to enter different resistors for different voltages.

From experimental data for a particular load cell [14] the damping factor c , spring constant k , and the effective mass of the load cell m_0 , are 3.5, 2700 Pa, and 0.5 kg, respectively. These numbers are used to determine the components values in the models.

To demonstrate the effectiveness of the models, the simulation result for one sample load value ($m = 0.1kg$) is shown in Fig.4. For step excitation, the input voltage of the load cell model should be a step function whose amplitude is proportional to m .

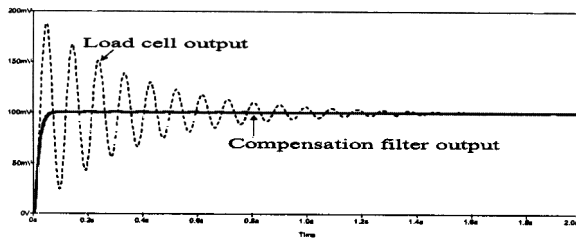


Figure 4: Simulation result of adaptive compensation for $m = 0.1kg$

4. Practical Implementation

In the sensor and compensation models, there is a floating linear Voltage-Controlled Resistor (VCR) which must be directly proportional to the controlling voltage over a wide range because this resistor is equivalent to $(m_0 + m)$. In PSpice simulation [1], this VCR was modelled using a voltage-controlled current source whose voltage values and resistors were set by a theoretical table format, hence there was no restrictions. In practice, however, such component does not exist. The challenging part of the practical implementation of the sensor and compensation filter models is the realization of such a

VCR. The properties of this VCR can be summarised as follows:

- Resistor should be floating (none of its terminals is connected to ground or power supply).
- Resistor should be linear (linear relationship between voltage and current).
- Relationship between resistance and controlling voltage should be linear over a wide range, enhancing its practical application.

4.1. Voltage-Controlled Resistor

Junction Field Effect Transistors (JFET) have long been used as voltage-controlled resistors [7, 11, 9, 8]. The channel resistance of the JFET can be controlled by applying a variable voltage between its gate and source. There are, however, two major problems:

1. Voltage across the channel should be small. In other words, for large V_{DS} , the channel is a non-linear resistor.
2. Channel resistance is inversely proportional to gate voltage.

There have been some published papers that address linearizing the relationship between the current and voltage of the JFET (the first problem) [7, 12, 8, 11]. However, extensive literature search has shown that there is very little or no work in the area of producing a resistor that varies with input voltage in a linear manner. In this section, these two problems are addressed and a novel linearization technique is proposed to solve the second one.

The relationship between drain current, I_D , and drain-source voltage, V_{DS} , of a JFET in the triode or ohmic region ($V_{DS} < (V_{GS} - V_{GS(off)})$) is

$$I_D = \frac{2I_{DSS}}{V_P^2} [(V_P - V_{GS})V_{DS} - 0.5V_{DS}^2] \quad (7)$$

which shows a nonlinear relationship between I_D and V_{DS} (a nonlinear resistance). For small values of V_{DS} , the square term in Eq.(7) can be ignored and in this case the drain-source resistance can be considered as a linear resistance, which in practice limits the voltage across the resistance to several hundred millivolts. Although it is possible to linearize this resistance over a wider range [7, 12, 8, 11], however, since in the analog adaptive filter model, the voltage across VCR is very small, $(V_{DS})^2$ in Eq.(7) can be ignored without significant impact. In this case, for V_{GS} less than $V_{GS(off)}$, the channel resistance becomes:

$$R_{DS} = \frac{R_{DS(on)}}{(1 - \frac{V_{GS}}{V_P})} \quad (8)$$

Where $R_{DS(on)} = \frac{V_P}{2I_{DSS}}$ is the minimum resistance for $V_{GS} = 0$. Eq.(8) shows that R_{DS} is inversely proportional to controlling voltage, V_{GS} . Eq.(8) can be rewritten as

$$R_{DS} = R_{DS(on)} \cdot [1 + (\frac{V_{GS}}{V_P}) - \frac{1}{2} \cdot (\frac{V_{GS}}{V_P})^2 + \frac{1}{6} \cdot (\frac{V_{GS}}{V_P})^3 + \dots] \quad (9)$$

Eq.(9) can be approximated as a linear equation if $\frac{1}{2} \cdot (\frac{V_{GS}}{V_P})^2 \ll (\frac{V_{GS}}{V_P})$. This restriction is equivalent to $m \ll m_0$, which means that the mass being weighed should be much less than the effective mass of the sensor. However, in practice, typically m can be several order of magnitude bigger than m_0 . To increase the capability of the compensation filter over a wider range, we propose to introduce a nonlinear amplifier between the output of the filter, which is controlling voltage (V_C), and the gate of JFET (Fig.5).

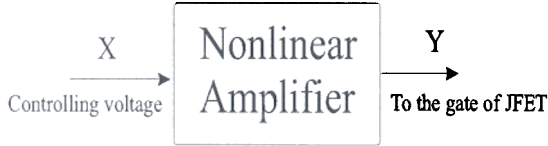


Figure 5: Nonlinear amplifier which provides the gate voltage from V_C

The nonlinear relation between output, Y , and input, X , of this amplifier can be obtained as follow. The VCR needs to change linearly with V_C , i.e.

$$R_{VCR} = R_0(1 + \alpha \cdot V_C) = R_0(1 + \alpha \cdot X) \quad (10)$$

where α is a proportional constant. The relationship between R_{DS} of the JFET with its V_{GS} is given in Eq.(8) and it is required that this resistance changes linearly with V_C . In other words, Eqs.(8) and (10) should be equal

$$\frac{R_{DS(on)}}{(1 - \frac{Y}{V_P})} = R_0(1 + \alpha \cdot X) \quad (11)$$

The value of R_0 is not important, and it is assumed $R_0 = R_{DS(on)}$. By manipulating Eq.(11), the input-output relationship of the nonlinear amplifier is

$$Y = \frac{V_P \cdot \alpha \cdot X}{1 + \alpha \cdot X} \quad (12)$$

One possible implementation of Eq.(12) is shown in Fig.6, which realize piecewise linear approximation of this equation.

This circuit has n different gains for different intervals ($V_{ref(i-1)} < |Y| < V_{ref(i)}$):

$$A_{v(i)} = -\frac{R_1 || R_2 \dots || R_i}{R} \quad \text{for } i = 1, 2, \dots, n \quad (13)$$

To calculate the gains, Eq.(12) can be approximated by n straight lines, as shown in Fig.7, for $n = 3$.

The breaking points of this curve are $V_{GS(i)} = Y(i) = V_{ref(i)}$ (for $i = 1, 2, \dots, n$). Corresponding inputs of the nonlinear amplifier, $X(i)$, can be calculated from Eq.(12). This approximation is equivalent to n piece of straight lines and hence needs an amplifier with n different gains. Slopes of the piecewise lines, $k(i)$, are equal to the gains of amplifier, $A_{v(i)}$

$$k(i) = \frac{\Delta Y(i)}{\Delta X(i)} = \frac{Y(i) - Y(i-1)}{X(i) - X(i-1)} = A_{v(i)} \quad \text{for } i = 1, 2, \dots, n \quad (14)$$

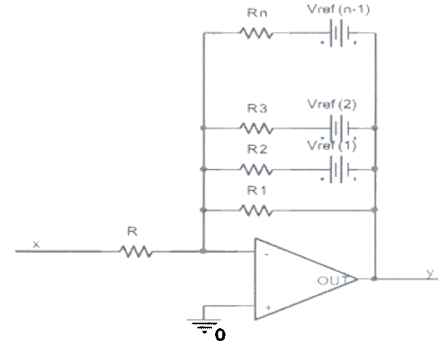


Figure 6: Implementation of the proposed piecewise linear approximation technique

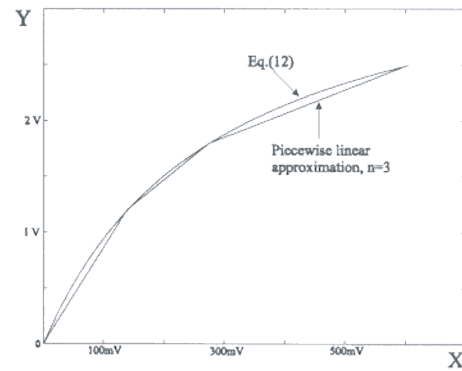


Figure 7: Piecewise linear approximation of Eq.(12)

Where $Y(0) = X(0) = 0$.

Having used this piecewise linear amplifier to provide the gate voltage, Fig.8 shows R_{DS} of the JFET with changing V_C . To indicate the effectiveness of the proposed technique, the ideal linear case and nonlinear case are also depicted. This figure shows that R_{DS} can be controlled linearly over a wide range (more than three times $R_{DS(on)}$). In other words, the adaptive compensation filter can be used for the values of m as large as $3m_0$.

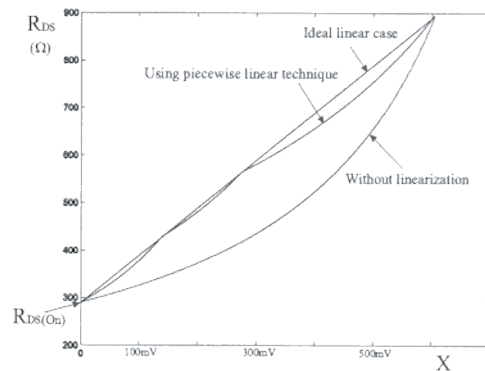


Figure 8: Linearization of R_{DS} using the proposed piecewise linear technique

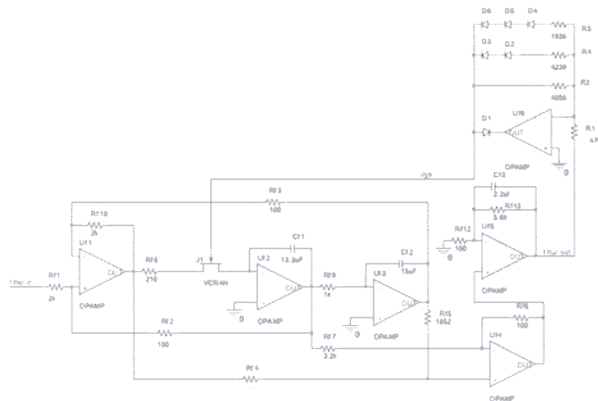


Figure 9: Complete practical analog adaptive compensation filter

4.2. Experimental Results

The complete analog adaptive compensation filter using a JFET as the VCR and piecewise linear amplifier to provide gate voltage is shown in Fig.9. The voltage references in Fig.6 have been implemented with cascade of single diodes.

For practical testing, a square wave excitation voltage was applied to the sensor circuit, and according to the amplitude of the excitation voltage, the sensor VCR (R_s) was changed manually. Figs.10 and 11 show two sample inputs and outputs of the adaptive filter. The input amplitudes are 100 mV and 330 mV, which are equivalent to $m = 0.1kg$ and $0.33kg$. Clearly the practical results show that analog adaptive biquad filter (Fig.9), can be used to correct the response of the load cell. It should be noted that there is good correlation between simulation and experimental results (Figs.4 and 10). To indicate the effectiveness of using an adaptive filter, a fixed filter was also used for compensation. When the excitation voltage is 330 mV, the gate of JFET is connected to ground (i.e. only fixed $R_{DS(on)}$ is in the filter circuit) and the input and output of the filter are depicted in Fig.12, which shows that the fixed filter is unable to perform the response correction.

5. Concluding Remarks

This paper has shown that it is possible to perform effective response compensation of sensors using analog adaptive filter techniques. This has been demonstrated with a reference to a load cell sensor. It has been shown that the state-variable biquadratic filter provides an accurate and flexible sensor and adaptive compensation filter models. Simulation and experimental results, showing the viability of the proposed technique, were presented. The practical prototype consisted of a novel piecewise linearization technique for floating voltage-controlled resistor. We are currently developing switched-current techniques that allow the integrated fabrication of the analog adaptive filter with digital CMOS compatible process. Switched-current circuits have capability to work at low supply voltages which is an interesting advantage specially for

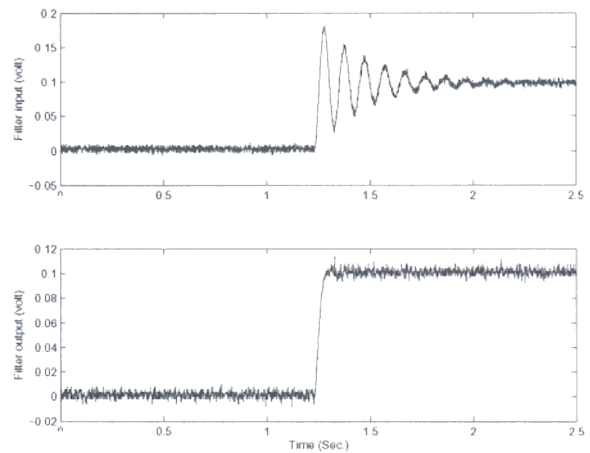


Figure 10: Input and output of the adaptive filter with $m = 0.1kg$

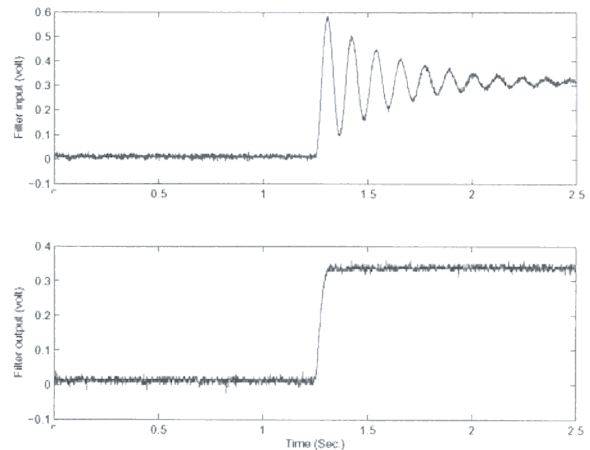


Figure 11: Input and output of the adaptive filter with $m = 0.33kg$

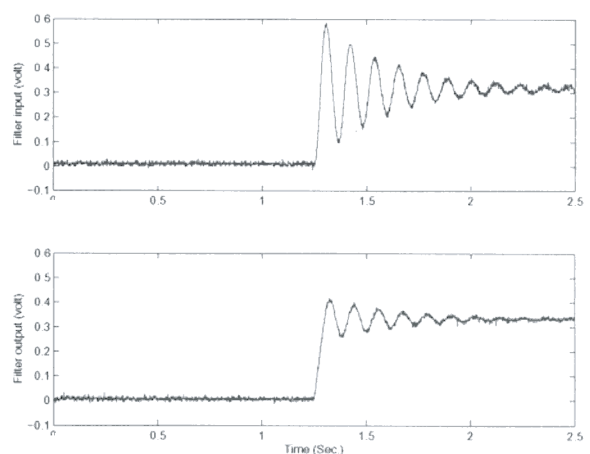


Figure 12: Input and output of the non-adaptive filter with $m = 0.33kg$

system-on chip applications.

Acknowledgments

The authors wish to thank the Iranian Ministry of Science, Research and Technology for the first author studentship support.

References

- [1] M. Jafaripanah B. M. Al-Hashimi and N. M. White. Load cell response correction using analog adaptive techniques. pages IV752–IV755, IEEE International Symposium on Circuits and Systems (ISCAS), Bangkok, Thailand, May 2003.
- [2] J E Brignell. Software techniques for sensor compensation. *Sensors and Actuators A*, 25-27:29–35, 1991.
- [3] J E Brignell and N M White. *Intelligent Sensor Systems*. Institute of Physics Publishing Ltd, 1994.
- [4] A. Carusone and D. A. Johns. Analogue adaptive filters: Past and present. *IEE Proceedings on Circuits, Devices, and Systems*, 47(1):82–90, February 2000.
- [5] W.-K. Chen. *Passive and active filters*. John Wiley and sons, Inc., 1986.
- [6] M. Halimic and W. Balachandran. Kalman filter for dynamic weighing system. pages 787–791, IEEE International Symposium on industrial electronics, July 1995.
- [7] K. Nay and A. Budak. A voltage-controlled resistance with wide dynamic range and low distortion. *IEEE Transaction On Circuits and Systems*, CAS-30(10):770–772, October 1983.
- [8] R. Senani and D. R. Bhaskar. A simple configuration for realizing voltage-controlled impedances. *IEEE Transaction On Circuits and Systems-I: Fundamental Theory and Application*, 39(1):52–59, January 1992.
- [9] R. Senani and D. R. Bhaskar. Versatile voltage-controlled impedance configuration. *IEE Proc.-Circuits Devices systems*, 141(5):414–416, October 1994.
- [10] W-Q. Shu. Dynamic weighing under nonzero initial condition. *IEEE Transaction on Instrumentation and measurement*, 42(4):806–811, August 1993.
- [11] Siliconix, AN105. *FETS as voltage-controlled resistor*, March 1997.
- [12] N. Tadic. A floating, negative-resistance voltage-controlled resistor. pages 437–442, IEEE Instrumentation and Measurement technology Conference, Budapest, Hungary, May 2001.
- [13] W J Shi N M White and J E Brignell. Adaptive filters in load cell response correction. *Sensors and Actuators A*, A 37-38:280–285, 1993.
- [14] S M T Alhoseyni Almodarresi Yasin and N M White. The application of artificial neural network to intelligent weighing systems. *IEE proceedings-Science, Measurement and Technology*, 146:265–269, November 1999.