

# Temporal Constraints for Concurrent Object Synchronisation

WOOD, Warsaw 12.04.03

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# What does Inheritance do, after all?

```
class Buffer {  
    void put(Object v) { ...; }  
    void get() { ...; }  
    ...  
}  
  
class Lock {  
    ...  
    void lock() { ...; }  
    void unlock() { ...; }  
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```

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Influence `Buffer` inheriting behaviour from `Lock`.

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Do you expect a Buffer which is locked/unlocked via Lock?



# Objects and Concurrency

Objects: A fundamental, state-of-the-art concept for engineering complex software systems. (Design Patterns, Refactoring, ...)

Concurrency: A fundamental technology to meet today's demands on software functionalities. (Internet, Mobile and Embedded Devices, Software Agents, ...)

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The plan

- Explain the phenomenon via examples;
- Illustrate the driving lines of the main existing approaches;
- Design and implementation of the programming language Jeeg.



# Concurrency and Interference

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The solutions:

- Operational Mechanisms: Semaphores and Locks, ...
- Linguistic Constructs: Critical Regions and Monitors, ...
- Alternative Models: Message Passing, Resource-Based, ...

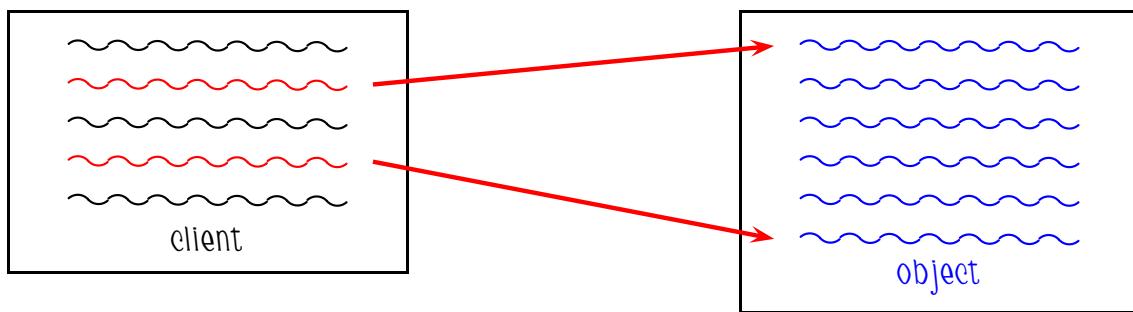
Their relevance: In the end the problem **is** in the concurrency model

# The Java Concurrency Model

```
public class Buffer {  
    protected Object[] buf;  
    protected int MAX, current = 0;  
  
    Buffer(int max) {  
        MAX = max;  
        buf = new Object[MAX];  
    }  
    public synchronized Object get() throws Exception {  
        while (current <= 0) wait();  
        Object ret = buf[--current];  
        notifyAll();  
        return ret;  
    }  
    public synchronized void put(Object v) throws Exception {  
        while (current >= MAX) wait();  
        buf[current++] = v;  
        notifyAll();  
    }  
}
```

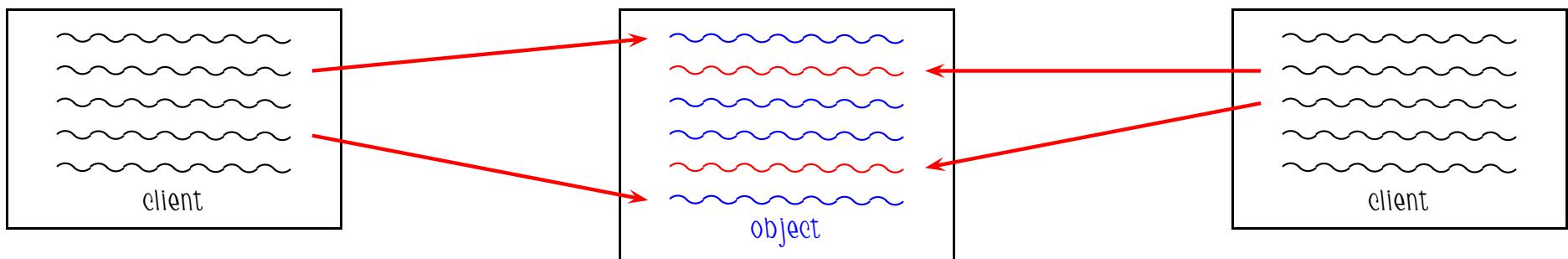


# Business and Synchronisation Code



In sequential programming, clients can be asked to behave well. E.g., don't get unless you have put. (Synchronisation code and Business code.)

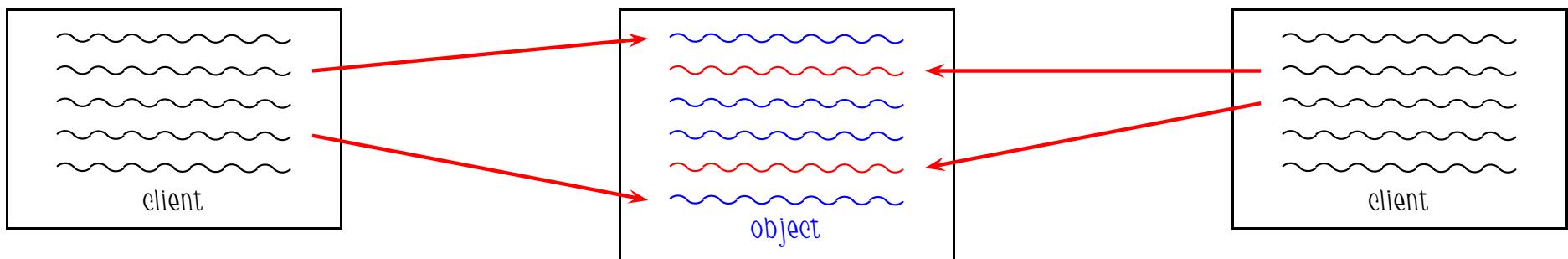
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Concurrent object oriented programs in common programming languages consist of business code inextricably interwoven with synchronisation code.

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```
class Buffer {  
    ...  
    void put(Object el) {  
        if ("buffer not full") ...  
    }  
    Object get() {  
        if ("buffer not empty") ...  
    }  
}
```



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    }  
}
```

Add a method `freeze`.

Chances are that the `synchronisation code` in `Buffer` must be totally rewritten for that.

All approaches to the anomaly so far consist of *disentangling* business and synchronisation code. None is very successful.

# Partitioning of States

**State Partition:** Introduce an explicit partition of the object's state, and explicit enabling conditions for methods.

**Example.** In the case of `Buffer`, choose `empty`, `partial`, `full` and the declarations:

`put: requires not full`

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**Example.** In the case of `Buffer`, choose `empty`, `partial`, `full` and the declarations:

`put: requires not full`

`get: requires not empty`

Then

```
Object get() {  
    ...  
    if ("buffer is now empty") become empty;  
    else become partial;  
    return res;  
}
```

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Consider adding `get2` which retrieves two elements at once. Then, the partition `empty` and `full` is not enough anymore.

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Consider adding `get2` which retrieves **TWO** elements at once. Then, the partition `empty` and `full` is not enough anymore.

Need to distinguish those states where there is exactly one element: `single`.

Correspondingly, refine it to be:

`get2`: requires not `empty` or `single`

```
Object get() {    ...
  if ("buffer is now empty") become empty;
  else if ("buffer is singleton") become single;
  else become partial;
  return res;
}
```



# History-Sensitivity of Acceptable States

When methods' enabling depends on the `history` of objects, we have a form of the anomaly so-called `history-sensitive`.

For instance, a method `withdraw` available only after a method `authenticate` has been completed.

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To exemplify, we want to add to `Buffer` a method `gget` enabled only if the last method invoked of `Buffer` was other than `get`.

# History Buffer

```
public class HistoryBuffer extends Buffer {  
    boolean afterGet = false;  
    public HistoryBuffer(int max) super(max);  
    public synchronized Object gget() throws Exception {  
        while ( current <= 0 || afterGet ) wait();  
        Object ret = buf[--current]; afterGet = false;  
        notifyAll();  
        return ret;  
    }  
    public synchronized Object get() throws Exception {  
        while (current <= 0) wait();  
        Object ret = buf[--current]; afterGet = true;  
        notifyAll();  
        return ret;  
    }  
    public synchronized void put(Object v) throws Exception {  
        while (current>=MAX) wait();  
        buf[current++] = v; afterGet = false;  
        notifyAll();  
    }  
}
```



# History Buffer, again

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        while ( current <= 0 || afterGet) wait();  
        afterGet = false;  
        return super.get();  
    }  
    public synchronized Object get() throws Exception {  
        Object o = super.get();  
        afterGet = true;  
        return o;  
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# Modification of Acceptable States

Anomaly when **mix-in classes** are used to add behaviour to object via multiple inheritance.

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class Lock {  
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Trying to influence the enabling conditions of a class, by inheritance.

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Of course, this does no much towards having a lockable buffer, in any language I know of.

**Question:** Is the Inheritance Anomaly **nonsense** or a **genuine** problem?  
If you look at it from the **OO** standpoint, it is genuine.



Jeeg tackles the (History-Sensitive) Inheritance Anomaly. It is:

- an aspect-oriented superimposition of two separate languages
  - Java (no synchronized(), wait(), notify(), and notifyAll() for business code);
  - Linear Time Temporal Logic for synchronisation code (method guards).

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```
public class MyClass {
  sync {
    m :  $\phi$ ;
    ....
  }
  ...// Standard Java class definition
}
```

`m` is a method id and  $\phi$ , the `guard`, is a formula in a given `constraint` language. When `m` is invoked, the thread is `kept on hold` unless  $\phi$ . When the condition is true, all `waiting` threads are `awaken`. `m` is implicitly `synchronized`.

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If  $\phi$  is a boolean expression, this is just a `declarative` version of Java concurrency.



# The logic

Logic: a trade-off between expressiveness and efficiency: its formulae must be verified at every method invocation!

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Linear temporal logic (past tense)

$$\phi ::= \text{AP} \mid !\phi \mid \phi \sqcap \phi \mid \text{Previous } \phi \mid \phi \text{ Since } \phi$$

AP are pure boolean expressions with no:

- side-effects,
- references to objects.
- method invocations,
- and it only refers to private/protected fields of the class it belongs to.

Derived connectives:

$$\phi \&& \psi \triangleq !(!\phi \sqcap !\psi); \quad \text{Sometime } \phi \triangleq \text{true Since } \phi; \quad \text{Always } \phi \triangleq !\text{Sometime } !\phi.$$

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This yield a rather expressive language CL, yet easy to implement.



# An Object's History

A generic computation  $\pi$  from  $o$ 's perspective.

$$h_0^0 \cdots h_{j_0}^0 o.\mathbf{m}_1 h_0^1 \cdots h_{j_1}^1 o.\mathbf{m}_2 h_0^2 \cdots h_{j_2}^2 \cdots$$

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Here only the part of  $h_{j_k}^k$  containing the values of private/protected, non-reference variables of  $o$ , say  $\sigma_k$ , can affect evaluation. Therefore, we take

$$\mathcal{H}_o(\pi) \equiv \sigma_0 \xrightarrow{m_1} \sigma_1 \xrightarrow{m_2} \sigma_2 \xrightarrow{m_3} \sigma_3 \dots$$

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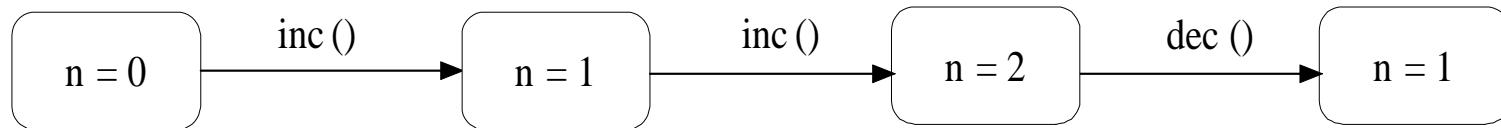
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We think of  $H_o(\pi)$  as

$$\mathcal{H}_o \equiv \sigma_0 \sigma_1 \sigma_2 \sigma_3 \cdots$$

where  $\sigma_i$  binds the special identifier **event** to (a value representing method)  $m_i$ .

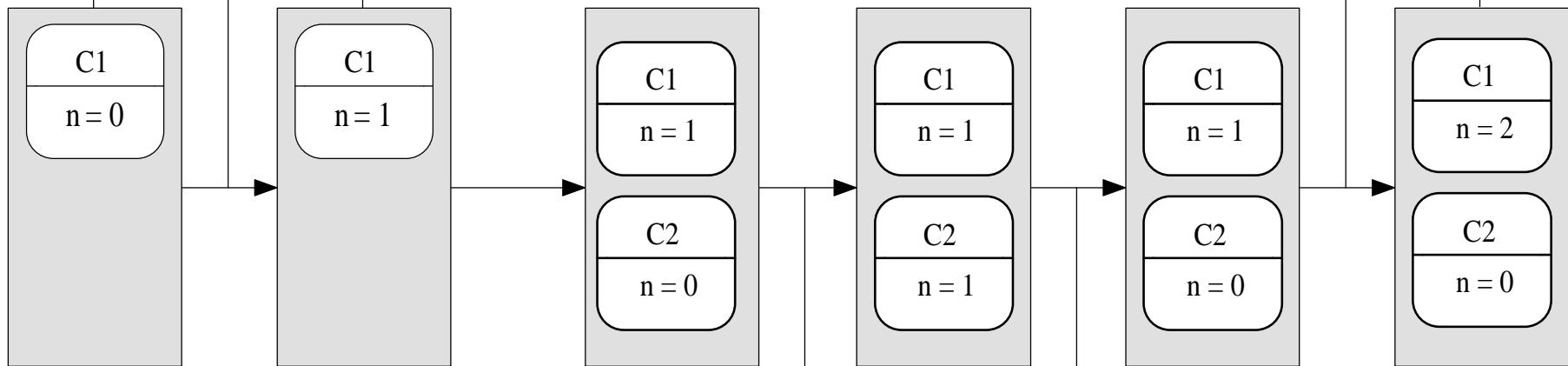
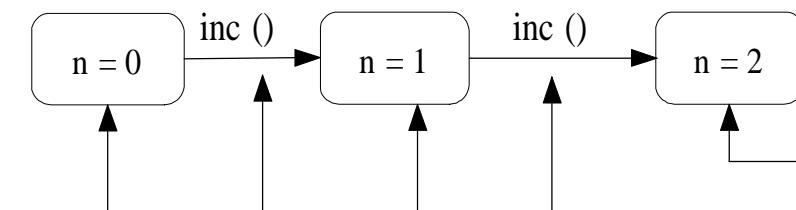


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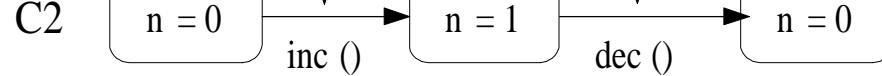
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# Concurrent Objects' Histories

C1



C2



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# Interpretation of Formulae on Object Histories

Let  $\Sigma$  denote  $\mathcal{H}_o(\pi)$ . For all indexes  $k$  in  $\Sigma$ , we define  $\Sigma_k \models \phi$ , that is  $\phi$  holds at time  $k$ , by structural induction on  $\phi$  as follows.

$$\Sigma_k \models p \quad \text{iff} \quad \sigma_k \models p \quad (p \text{ is true at } \sigma_k)$$

$$\Sigma_k \models !\phi \quad \text{iff} \quad \text{not } \Sigma_k \models \phi$$

$$\Sigma_k \models \phi \parallel \psi \quad \text{iff} \quad \Sigma_k \models \phi \text{ or } \Sigma_k \models \psi$$

$$\Sigma_k \models \text{Previous } \phi \quad \text{iff} \quad k > 0 \text{ and } \Sigma_{k-1} \models \phi$$

$$\Sigma_k \models \phi \text{ Since } \psi \quad \text{iff} \quad \Sigma_j \models \psi \text{ for some } j \leq k,$$

$$\text{and } \Sigma_i \models \phi \text{ for all } j < i \leq k$$

Finally, we convene that  $\Sigma \models \phi$  iff  $\Sigma_0 \models \phi$ .



# Buffer in JEEG

```
public class Buffer {  
    sync {  
        put : current < MAX;  
        get : current > 0;  
    }  
    protected Object[] buf;  
    protected int MAX, current = 0;  
    Buffer(int max) {  
        MAX = max; buf = new Object[MAX];  
    }  
  
    public Object get() throws Exception {  
        Object ret = buf[--current];  
        return ret;  
    }  
  
    public void put(Object v) throws Exception {  
        buf[current++] = v;  
    }  
}
```



# History Buffer in JEEG

```
public class HistoryBuffer extends Buffer {  
    sync {  
        gget: Previous (event != get) && current > 0;  
    }  
  
    public HistoryBuffer(int max) {  
        super(max);  
    }  
  
    public Object gget() throws Exception {  
        Object ret = buf[--current];  
        return ret;  
    }  
}
```



# Lockable Buffer in JEEG

```
public interface Lock {  
    public void lock();  
    public void unlock();  
}  
  
public class LockBuf extends Buffer implements Lock {  
    sync {  
        get    : super.getConstr && !Previous (event == lock);  
        put    : super.putConstr && !Previous (event == lock);  
        lock   : !Previous (event == lock);  
        unlock : true;  
    }  
  
    public LockBuf(int max) { super(max); }  
    public void lock() { }  
    public void unlock() { }  
}
```



# Expressiveness of JEEG

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Nicely, Jeeg allows for a "quantitative" analysis.

**Expressiveness of LTL:** A set of state sequences  $X$  is the set of all  $\Sigma$ s that satisfy a given  $\phi$  if and only if  $X$  is a star-free regular language. (Zuck [1986])

Star-free Regular Languages:

$$re ::= \epsilon \mid a \mid re \cdot re \mid re + re \mid \neg r \quad ( \mid re^*)$$



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State for C:  $p \in A_C \subset AP$ ; Sequence of states:  $P \in A_C^*$ . ( $\Sigma \models P$  iff  $\Sigma_k \models P_k$ )

**Theorem (CHARACTERIZING CL).** For  $\phi$  a formula on C,  $X = \{\Sigma \mid \Sigma \models \phi\}$  iff there exists  $re$  on  $A_C$  such that  $\Sigma \in X$  iff  $\Sigma \models P$  for some  $P \in re$ .

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**Special case:** Only atomic propositions of the kind event == m.

Then CL would capture precisely those sequences of events which are star-free regular languages (i.e., enforce synchronisation policies so expressible).



# Examples

HistoryBuffer: the temporal constraint

Previous event  $\neq$  get

can be expressed by the following star-free regular expressions.

$$\neg(A^* \cdot \text{get}) \quad \text{where } A^* \triangleq \epsilon + \neg\epsilon.$$

The temporal constraint

Sometime  $m \triangleq$  true Since  $m$ .

corresponds to

$$A^* \cdot m \cdot A^*.$$

# Limitations of LTL: No Counting

```
public class SharedResource {  
    sync {  
        request: true;  
        release: true;  
    }  
    public void request() { ... }  
    public void release() { ... }  
    ...  
}
```

Define a class **SeizableResource** which allows **exclusive access** to the shared resource:  
An additional method **exclusiveRequest** must be provided.

Clearly, this leads to identify a pattern of events such as:

$M ::= \epsilon \mid \text{request } M \text{ release } \mid MM \mid \dots$

It is well known that this language is not regular. Methods **request** and **release** will have to be redefined. The **anomaly** surfaces again here.

# Runtime Evaluation of CL Expressions

Given a finite trace  $\Sigma$  and a LTL formula  $\phi$ , does  $\Sigma \models \phi$ ?

Traditionally: build a Buchi automata to ‘model-check’ sequences. Dealing with past tense operators gives us an advantage: an ‘online’ algorithm.

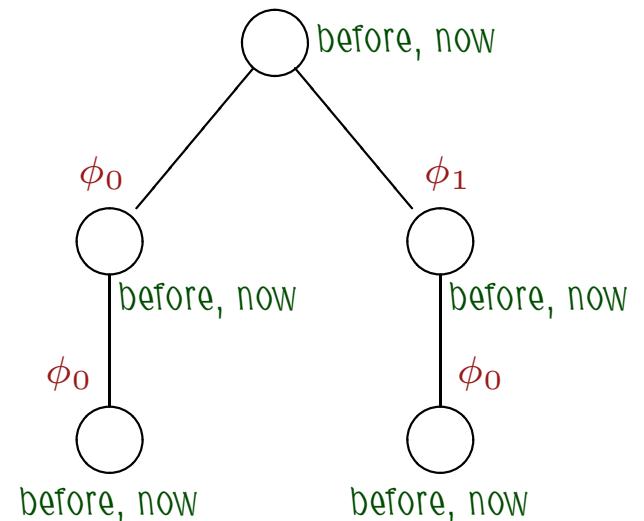
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- Build the **syntax tree** of the formula;
- Associate variables **before** and **now** to every node, initially set to **false**;
- Visit the tree depth-first and simultaneously assign  $\phi.\text{before} := \phi.\text{now}$  and  $\phi.\text{now}$  as follows.

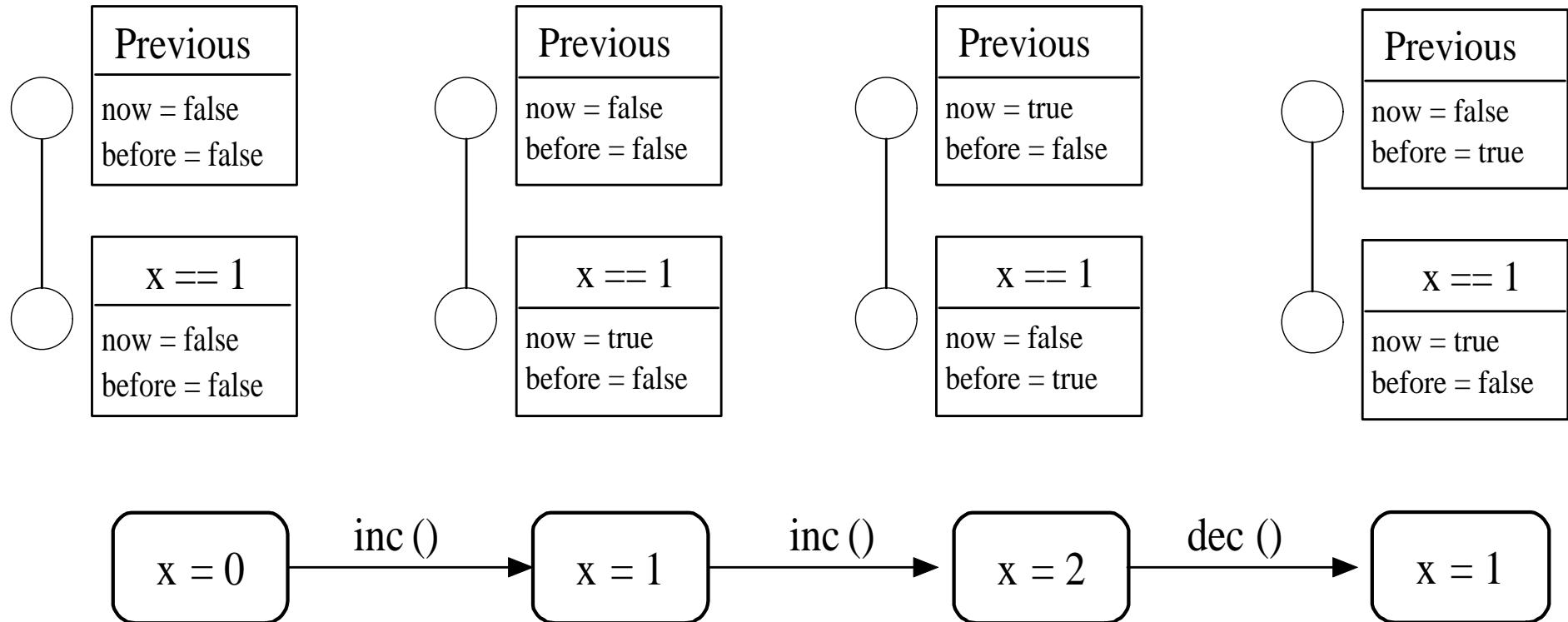
previous	now := $\phi_0.\text{before}$
since	now := $\phi_1.\text{now}$ or (before and $\phi_0.\text{now}$ )
or	now := $\phi_0.\text{now}$ or $\phi_1.\text{now}$
not	now := not $\phi_0.\text{now}$
AP	now := eval( $\phi$ )



# An Example

**Example:** Let us consider the evaluation of the temporal formula

Previous( $x == 1$ )



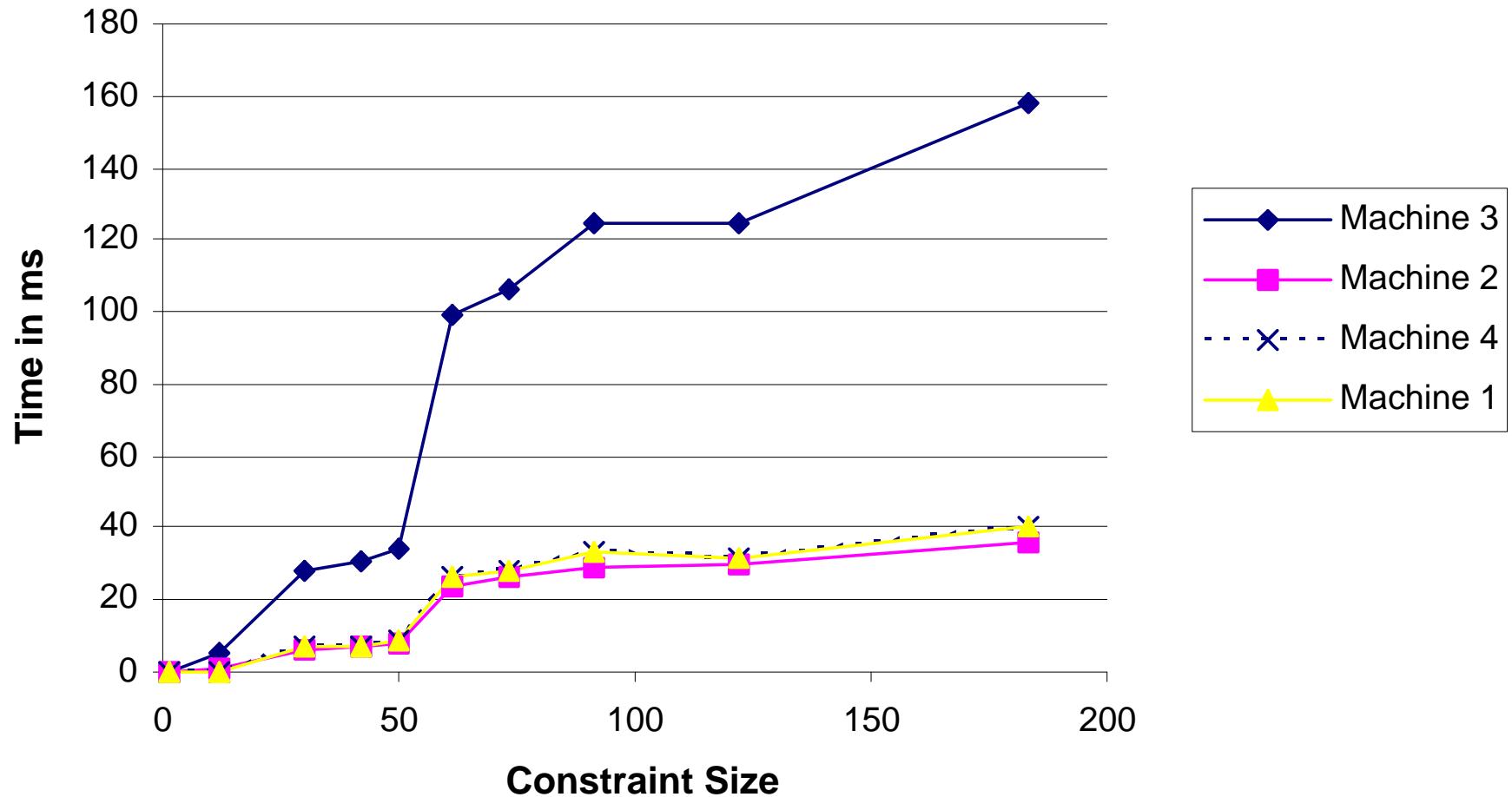
# The Synchronisation Manager

Formulae must be evaluated after `every` method execution. This is done by a synchronization manager via **Method Call Interception**. It

- takes control at method call and `checks` (not `evaluates`) the constraint for the method.
- If it holds, control goes to the method code; otherwise the synchronization manager performs a `wait()`, putting the object to `sleep`.
- After the method execution, control `shifts back` to the manager, which now `re-evaluates` the synchronization constraints.
- After updating the formulae logic value, the manager issues a `notifyAll()` statement. Blocked methods may then attempt to proceed again.

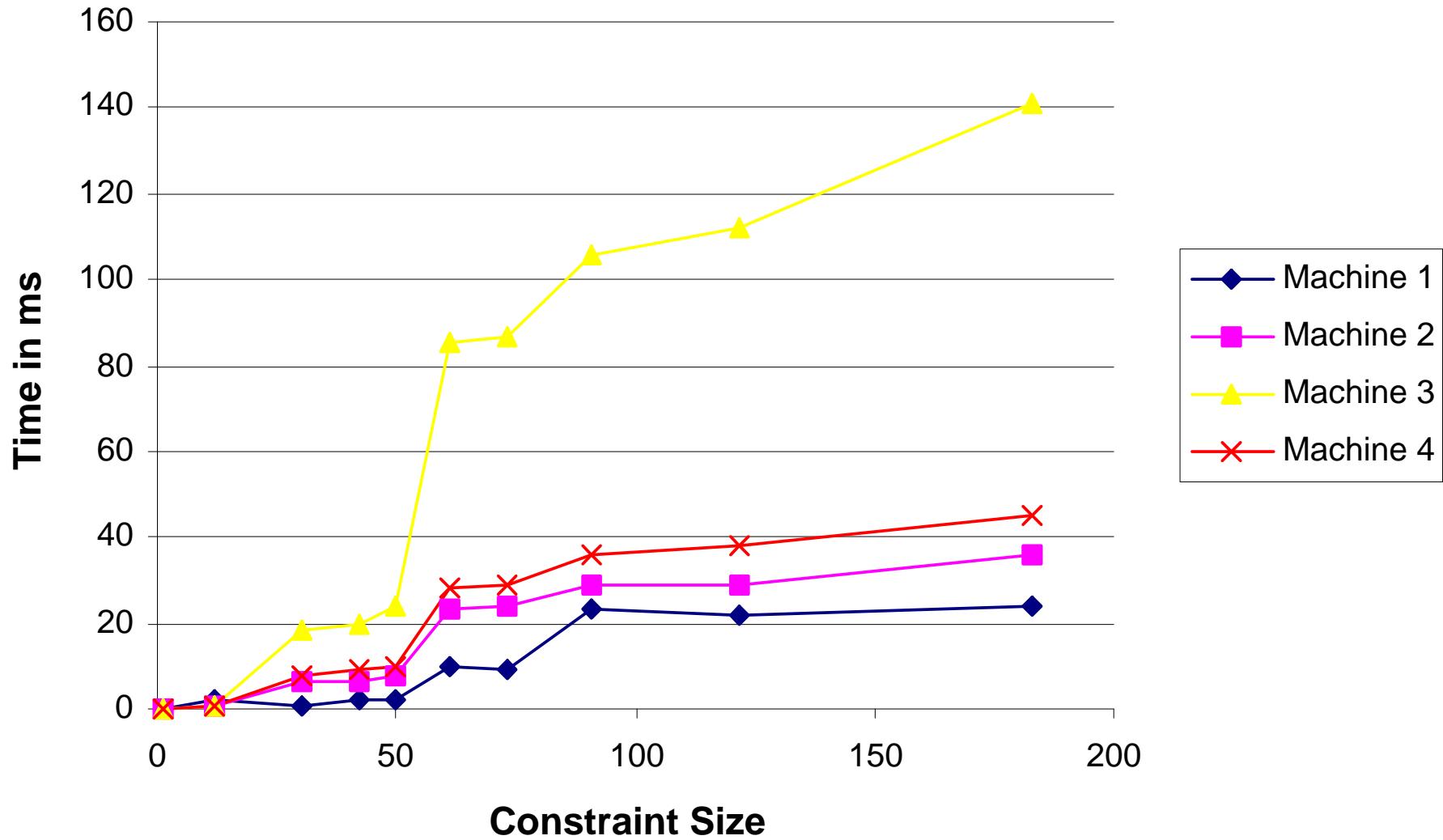
To have access to `private/protected fields`, the synchronization manager an **inner class** of the object it manages.

# Benchmarks: Object Creation



Object creation triggers the creation of data structures for formulas

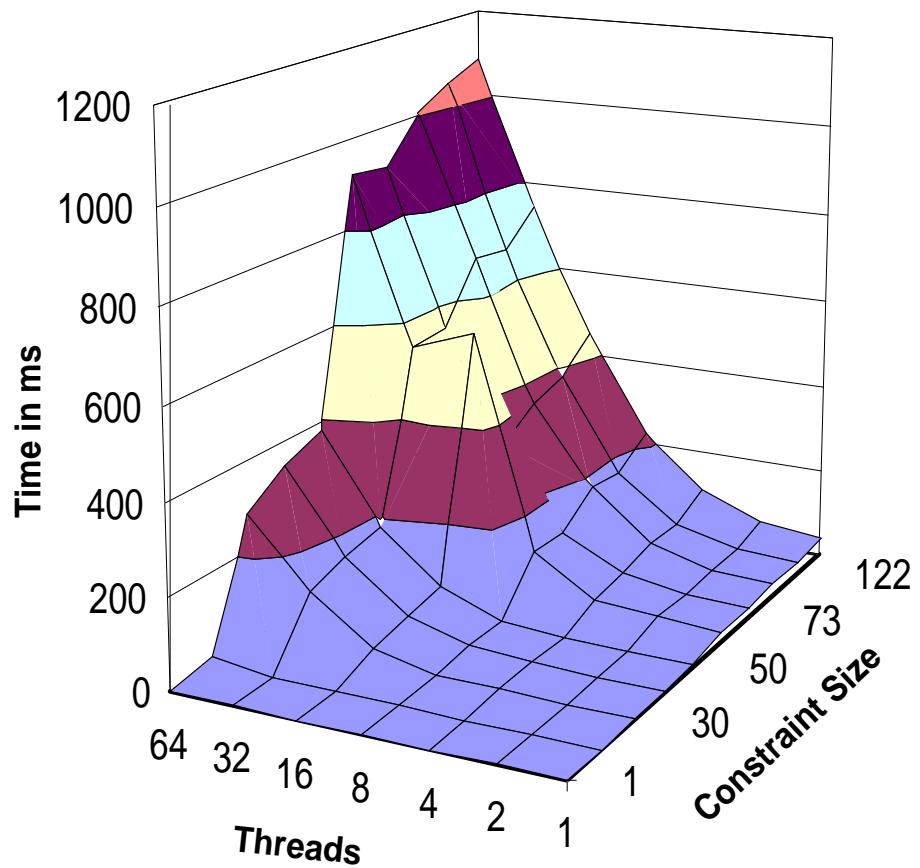
# Benchmarks: Method Call



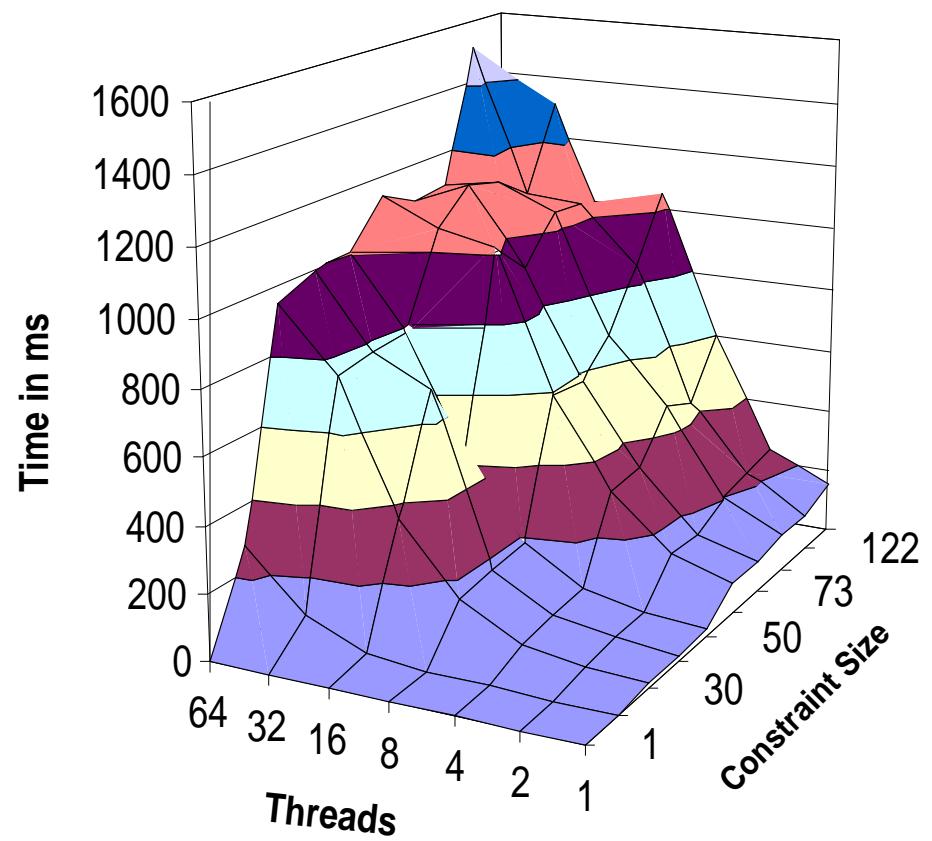
Method calls trigger the evaluation of formulas

# Benchmarks: Details of Method Call

Machine 2



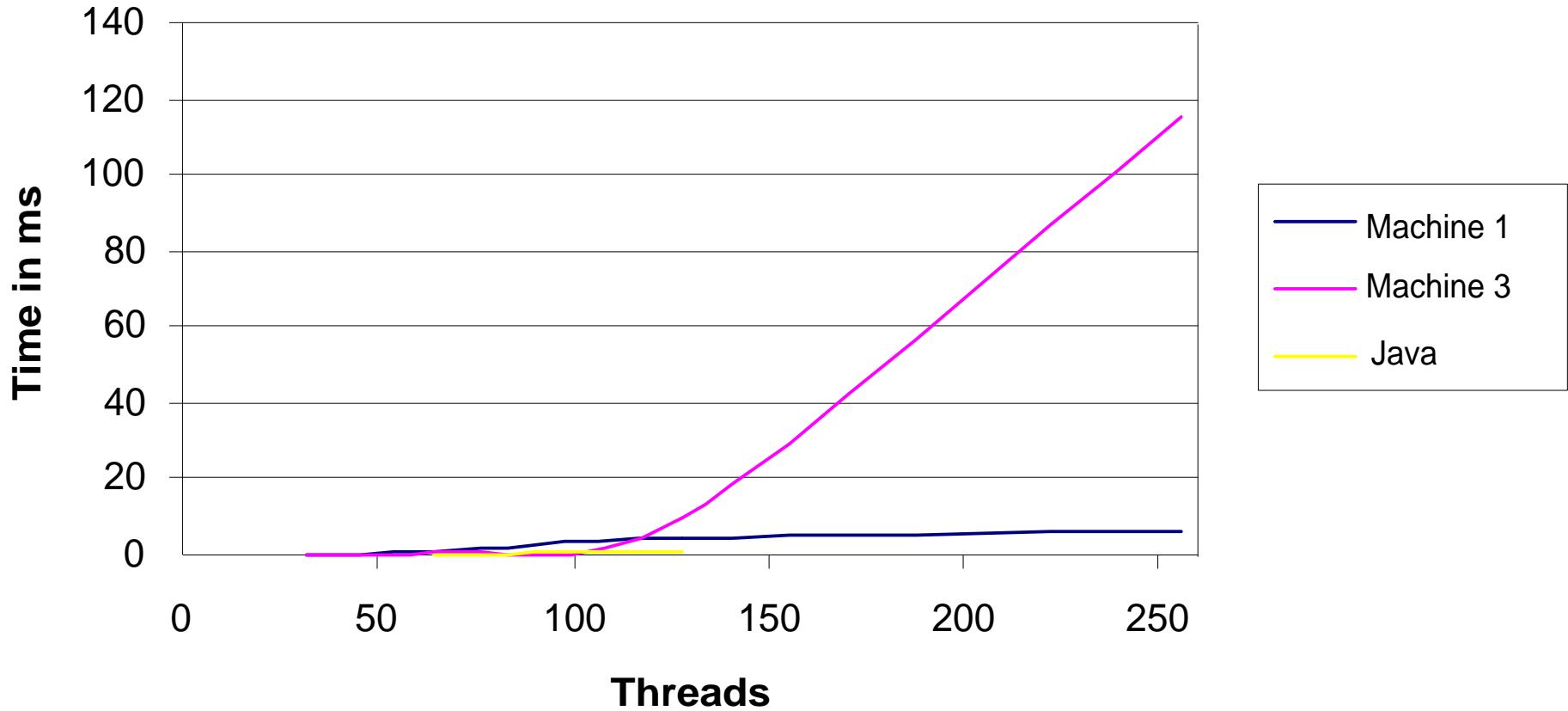
Machine 3



Formulae evaluation triggers mutual exclusion protocols



# Benchmarks: Comparison



However, synchronisation must be performed also in Java!

# Performance Evaluation

Testing shows that:

- Under low-load (below 70 threads) even complex synchronization constraints yield little performance overhead.
- Low-end machines face worse scalability problems due object locking: The slower the evaluation algorithm, the longer a large number of threads are kept waiting.

# Conclusion

Jeeg

- Synchronization constraints written in LTL and specified in a aspect-oriented, declarative manner.
- CL is helpful in treating the inheritance anomaly.
- Characterisation of CL in terms of regular languages
- Efficiently implementable (available at <http://www.brics.dk/~milicia/Jeeg>).

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## Future Work:

- Quantified linear temporal logic (QLTL) or monadic second order logic (MSOL), 'second order' variations of LTL of greater expressiveness.
- optimizing the LTL evaluation procedure by using ad-hoc static-analysis techniques.

