

# Foundations of Global Computing

A Personal Perspective

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# Foundations of Global Computing

Resource Control

Programming Languages

Semantic Theories

Models for Concurrency

## Global Ubiquitous Computing:

computation over a global network of mobile, bounded resources shared among mobile entities which move between highly dynamic, largely unknown, untrusted networks.

## Difficulties:

Extreme dynamic reconfigurability; lack of coordination and trust; limited capabilities; partial knowledge ...

## Issues:

Protection and management of resources; privacy and confidentiality of data; ...

# Foundations of Global Computing

## Petri Nets Based Models and Calculi

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A distributed timed-arc Petri net (DTAPN) is a Petri net together with

- a interval time constraint on transitions, either discrete or continuous;
- a clock synchronisation equivalence  $\Sigma$  on places.

Tokens age, and transitions are enabled accordingly. Time elapses at the same speed on  $p$  and  $p'$  if  $p \Sigma p'$ .

## Globally Asynchronous, Locally Synchronous

Global Time:  $\Sigma = P \times P$  Local Time:  $\Sigma = \Delta_P$

A Separation Result: Reachability for safe LT nets is decidable, but undecidable for safe GT nets.

ICATPN 2001, FST&TCS 2001

# Foundations of Global Computing

Resource Control

- A categorical machinery which allows the derivation of LTSs from reduction systems.
- Bisimulation on such LTSs is a congruence, provided a general condition is met.

Programming Languages

Coinduction Principle Desiderata:

- Operational Corresp.:  $p \searrow q$  iff  $p \xrightarrow{\tau} q$
- Correctness:  $p \approx q$  implies  $p \cong q$
- Completeness:  $p \cong q$  implies  $p \approx q$

The intuition:

$$a \xrightarrow{\mathcal{C}} b \text{ iff } \mathcal{C}[a] \searrow b$$

Eg:

$$a \xrightarrow{-|\bar{a}} 0 \quad M \xrightarrow{(\lambda x.-)^N} M\{N/x\} \quad \mathbf{K}M \xrightarrow{-N} M$$

Models for Concurrency

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Semantic Theories

The intuition:

$$a \xrightarrow{\mathcal{C}} b \text{ iff } \mathcal{C}[a] \searrow b$$

But: Must choose labels carefully not to mess up the bisimulation

Choose only 'minimal' redex-enabling contexts: GRPOs.

Relative pushouts in groupoidal categories:

EXPRESS 2002, FOSSACS 2003, NJC, TCS

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Models for Concurrency

# Foundations of Global Computing

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Programming Languages

Semantic Theories

Models for Concurrency

Jeeg: concurrent OO with history-sensitive access control

- ▶ Java (no `synchronized()`, `wait()`, `notify()`, `notifyAll()`) for business code;
- ▶ Linear Time Temporal Logic for synchronisation code (method guards).

```
public class MyClass {  
    sync {  
        m :  $\phi$ ;  
        ...  
    }  
    ...// Standard Java class def  
}
```

where `m` is a method identifier and  $\phi$ , the guard, is an LTL formula. When `m` is invoked, the thread is kept on hold unless  $\phi$ . When the condition is true, all waiting threads are awoken. `m` is implicitly synchronised.

JavaGRANDE 2002, WOODS 2003, Cone & Comp, OOPS 2004

# Foundations of Global Computing

Resource Control

Resources: Models, Types, Logics, Languages

Programming Languages

Semantic Theories

Models for Concurrency

- Access Control (Coneur 2002, ESOP 2004)
- Access Authorisation (FST&TCS 2002, Info&Co)
- Secrecy for Mobile Agents (ICALP 2003)
- Trust Management (SEFM 2003)
- Bounds Control (ASIAN 2003)

# Mobile Ambients

Both administrative domains and computational environments

- Subjective movements

$$n[ \text{ in } m.P \mid Q ] \mid m[ R ] \longrightarrow m[ n[ P \mid Q ] \mid R ]$$

$$m[ n[ \text{ out } m.P \mid Q ] \mid R ] \longrightarrow n[ P \mid Q ] \mid m[ R ]$$

- Boundary dissolver

$$\text{open } n.P \mid n[ Q ] \longrightarrow P \mid Q.$$

- Process interaction

$$n[ \langle M \rangle.P \mid (x).Q ] \longrightarrow n[ P \mid Q\{x := M\} ],$$

# Group Types for Mobility

Aim: *Resource Access Control*

- ▶ Detect and prevent unwanted access to resources.
- ▶ Focus on static approaches based on enforcing type disciplines.

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Groups: Sets of processes with common access rights.

Constraints like  $k : \text{CanEnter}(n)$  are modelled as:

$n$  belongs to group G

$k$  may cross the border of ambients of group G.

For instance, the system:

$$k[\text{in } n \mid l[\text{out } k]] \mid n[-]$$

is well-typed under assumptions of the form:

$$k : \text{amb}[K, \text{cross}(N)]$$
$$l : \text{amb}[L, \text{cross}(K)]$$
$$n : \text{amb}[N, \dots]$$

# Indirect Border Crossing

Trojan Horses: The system

Odysseus[ **in** Horse.out Horse.Destroy ] | Horse[ **in** Troy ] | Troy[ Trojans ]

is well-typed under assumptions:

Odysseus : amb[Achaean, cross(Toy)]

Horse : amb[Toy, cross(City)]

Troy : amb[City, -]

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Troy : amb[City, -]

However, the system may evolve to

Troy[ Trojans | Horse[ - ] | Odysseus[ Destroy ] ]

where Odysseus got inside Troy's Walls taking by surprise the Trojans.

# Types

Groups:  $\mathbf{G}, \mathbf{H}, \dots$

Sets of groups:  $\mathcal{P}, \mathcal{S}, \dots$   $\mathcal{U}$  The universal set of groups

Ambients types:

$A ::= \text{amb}[\mathbf{G}, \mathbf{M}]$  amb of group  $\mathbf{G}$ , with mobility type  $\mathbf{M}$

Process types:

$\Pi ::= \text{proc}[\mathbf{G}, \mathbf{M}]$  process that can be enclosed in an ambient of group  $\mathbf{G}$ ,  
may drive to ambients whose groups are in  $\mathbf{M}$

Capability types:

$K ::= \text{cap}[\mathbf{G}, \mathbf{M}]$  capability that can appear in an ambient of group  $\mathbf{G}$ ,  
may drive it to ambients whose groups are in  $\mathbf{M}$

Mobility types:

$\mathbf{M} ::= \text{mob}[\mathcal{P}]$  mobility specs: where processes are allowed to reside

# Access Control Properties

Mobility properties:

- If  $\Gamma \vdash n[\text{in } m.P \mid Q] \mid m[R] : \Pi$ , then

$$\Gamma \vdash m : \text{amb}[\mathbf{M}, \_] \quad \text{and} \quad \Gamma \vdash n : \text{amb}[\_, \text{mob}[\mathcal{P}]]$$

with  $\mathbf{M} \in \mathcal{P}$ .

- If  $\Gamma \vdash m[n[\text{out } m.P \mid Q] \mid R] : \Pi$ , then

$$\Gamma \vdash m : \text{amb}[\mathbf{M}, \text{mob}[\mathcal{P}_m]] \text{ and } \Gamma \vdash n : \text{amb}[\mathbf{N}, \text{mob}[\mathcal{P}_n]]$$

with  $\mathbf{M} \in \mathcal{P}_n$  and  $\mathcal{P}_m \subseteq \mathcal{P}_n$ .

# Detecting Odysseus' intentions

Now, in order to assign a type to

Odysseus[ in Horse.out Horse.Destroy ] | Horse[ in Troy ] | Troy[ Trojans ]

we need assumptions of the form:

Odysseus : amb[Achaean, mob[{Ground, Toy, City}]]

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representing that Odysseus is an **Achaean** intentioned to move into a **City**!

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On the other hand, under assumptions of the form

Odysseus : amb[Achaean, mob[{Ground, Toy}]]

the **Trojans** should not fear any attack from Odysseus.

# Dependent Types for Access Control

Dependent Mobility Types: ( $\mathcal{P}$  and  $\mathcal{C}$  are sets of names, not groups.)

$A ::= \text{amb}[\text{hasFathers}(\mathcal{P}), \text{hasChildren}(\mathcal{C})]$

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Dependent types allow personalised services and dynamic access control.

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- Names have several possible types, depending on the *actual* communications occurred.
- The set of names *exchanged* over a channel must be tracked. Luckily, The set of possible types for a name has a *maximum* and a *minimum* element.

# Secrecy in Mobile Ambients

Names  $\approx$  Cryptokeys: Carrying messages inside **private** ambients preserves message **integrity** and **privacy**. Or, does it?

$$(vn)(a[ n[ \text{out } a.\text{in } b.\langle M \rangle ] ] \mid b[ \text{open } n.(x)P ] )$$

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How to provide stronger protection?

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It actually offers no guarantees for software agents, as ***n*** must be revealed along the move, and servers may peek inside.

How to provide stronger protection?

A new **crypto-primitive**: subjective access control using co-capabilities + data encryption to preserve secrecy of data while agents move autonomously

$$n[ \text{seal } k.P \mid Q ] \rightarrow n\{ P \mid Q \}_k$$

sealed under *k*  
crypto-key

Effects:

- blocks message exchanges and encrypts their contents;
- the sealed ambient cannot communicate, but it may move.

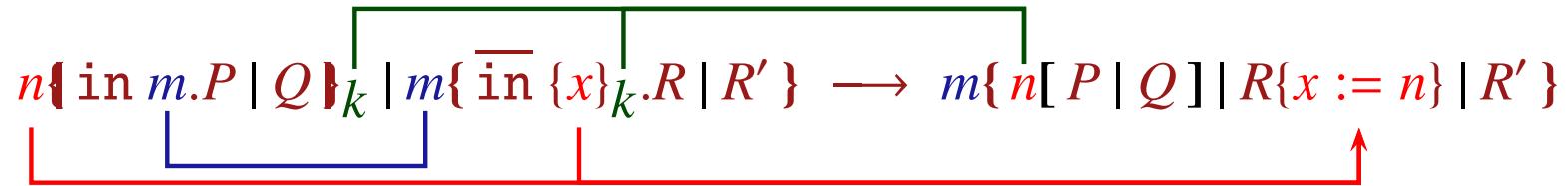
# Sealed Ambients

- The mechanism to resume to a fully operational state is associated to movements and co-capabilities containing keys

$$n\{ \text{in } m.P \mid Q \}_k \mid m\{ \overline{\text{in }} \{x\}_k.R \mid R' \} \longrightarrow m\{ n[P \mid Q] \mid R\{x := n\} \mid R' \}$$

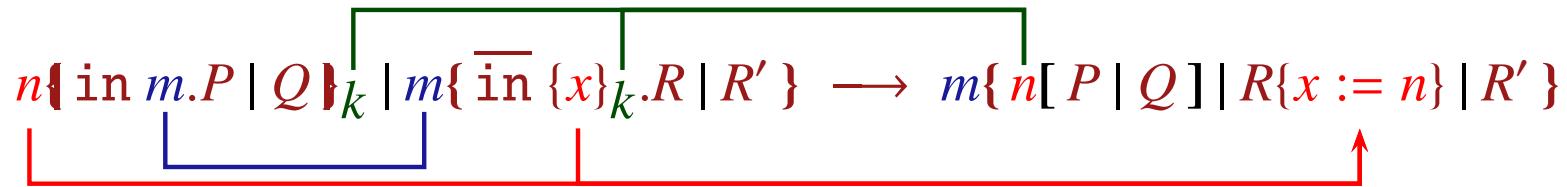
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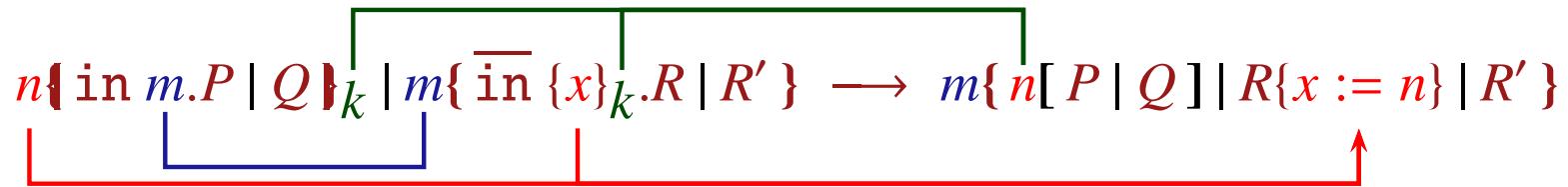
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Example:

$$(\nu k)a[ n[ \text{seal } k.\text{out } a.\text{in } b.\langle M \rangle^\hat{\wedge} ] ] \mid b[ \overline{\text{in }} \{x\}_k.(y)^x.P ]$$

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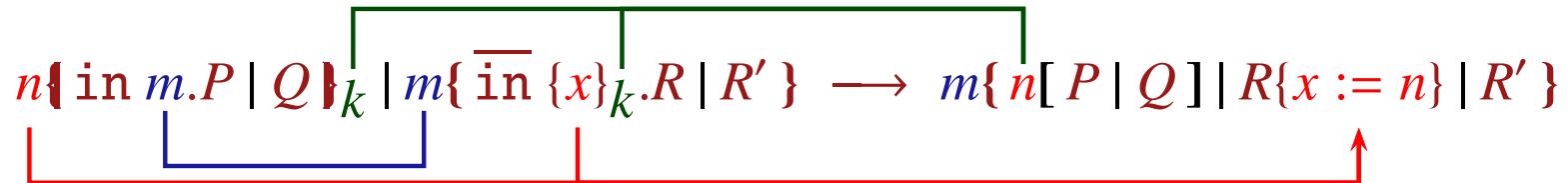
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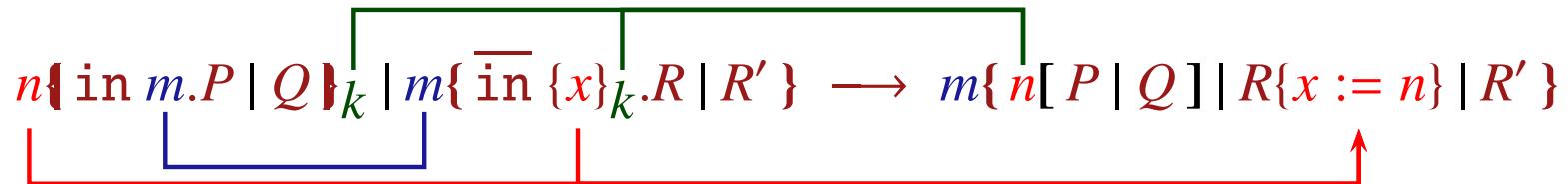
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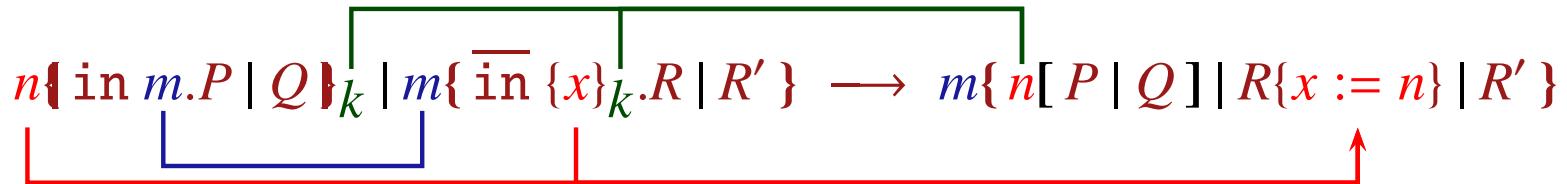
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# Secrecy and Adversaries

Intuitively:

A process preserves the secrecy of a piece of data  $M$  if it does not publish  $M$ , or anything that would permit the computation of  $M$ .

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$S$ -Adversary: A context  $\mathbf{A}(-)$  which initially knows names and capabilities in  $S$ .

Revealing Names:  $P$  may reveal  $n$  to  $S$  if there exists an  $S$ -adversary  $\mathbf{A}(-)$  and a name  $c \in S$  such that:

$$\mathbf{A}(P) \Rightarrow \mathbf{C}(c[\langle n \rangle^\hat{\wedge} \mid Q]) \quad (\text{ } c \text{ free})$$

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Typing System: Secrecy is captured by a type system  $\vdash$  which may classify processes as untrusted  $\Gamma \vdash P : \mathbf{Un}$ , and data as public  $a : \mathbf{Public}$  if it can be exchanged with untrusted process.

Secrecy Theorem: Well-typed processes do not reveal their secrets publicly. Formally, if  $\Gamma \vdash P : \mathbf{Un}$  and  $\Gamma \not\vdash s : \mathbf{Public}$ , then  $P$  preserves the secrecy of  $s$  from all public channels, i.e. from  $\{a \mid \Gamma \vdash a : \mathbf{Public}\}$ . (Payload  $s$  won't be entrusted to a public  $a$ .)

# Between Theory and Practice

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All this only works as long as you trust the certified types, or are willing to typecheck migrating code yourself (bytecode verification, PCC, ...), ...

- Verification (relates to type checking/inference)
- Certificates (groups as certified roles)
- Trust: In UbiComp, security must work be coupled with trust management.

Which is hard, because of delegation and dynamic policies

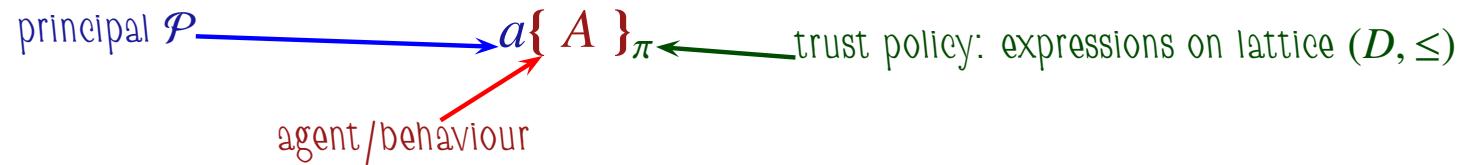
# Trust Management

Focus on Trust Evolution and Delegation in Dynamic Networks

$$a\{ A \}_{\pi}$$

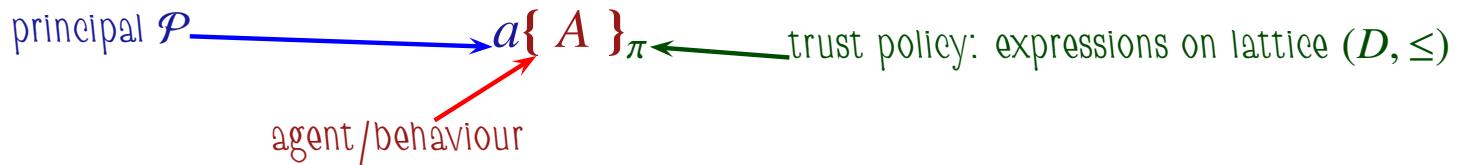
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Trust Based Services:

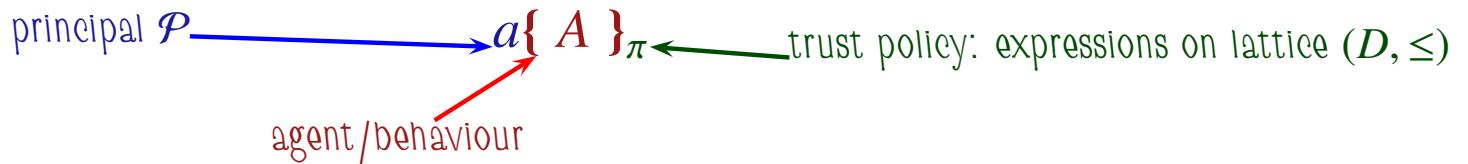
$$a\{ b.\ell(v).A \}_- \mid b\{ \ell(x).\Sigma_t B_t \}_\pi \rightarrow a\{ A \}_- \mid b\{ B_{\pi(a)}\{x := v\} \}_\pi$$

Trust Evolution:

$$a\{ \zeta.A \mid B \}_\pi \rightarrow a\{ A \mid B \}_{\zeta(\pi)}$$

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Trust Based Services:

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Policies and Expressions:

$\pi ::=$	$\lceil p \rceil$	delegation	$\tau ::=$	$t \in D$	value/var
	$\lambda x : P. \tau$	abstraction		$\pi(p)$	policy value
	$op(\pi_1, \dots, \pi_n)$	lattice op		$e \mapsto \tau; \tau$	choice
$p ::=$	$a \in \mathcal{P}, x : P$	principal/vars	$e ::=$	$\tau \text{ cmp } \tau, p \text{ eq } p$	comparisons
				$e \text{ bop } e$	boolean op

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# Understanding Delegation

Example:

$a : p \mapsto \text{trusted};$

$q \mapsto \lceil b \rceil(q);$

$z \mapsto \lceil p \rceil(z);$

$b : p \mapsto \lceil a \rceil(p);$

$q \mapsto \text{untrusted};$

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$z \mapsto \lceil p \rceil(z);$	$z \mapsto \lceil a \rceil(z);$

Delegation, formally: Global trust as a fixpoint.

$$\pi : (\mathcal{P} \rightarrow \mathcal{P} \rightarrow D) \rightarrow (\mathcal{P} \rightarrow D) \quad \text{Local Policy}$$

$$\Xi : (\mathcal{P} \rightarrow \mathcal{P} \rightarrow D) \rightarrow (\mathcal{P} \rightarrow \mathcal{P} \rightarrow D) \quad \text{Collected Policies}$$

Global Trust:  $\text{fix}(\Xi) : \mathcal{P} \rightarrow \mathcal{P} \rightarrow D$ . But, is this good enough?

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$p : \text{trusted}$	$q : \text{untrusted}$	$z : ???$
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Cannot confuse don't trust with don't know: the value of  $\lceil p \rceil(z)$  could become available later.

Need to account for uncertain knowledge of  $\lceil p \rceil(z) \in D$ .

# Trust Structures



Thm.  $(D, \leq, \sqsubseteq)$  yields an adequate semantics  $\llbracket - \rrbracket : \text{Policies} \rightarrow \text{Env} \rightarrow (\mathcal{P} \rightarrow \mathcal{P} \rightarrow D)$ . The trust structure is derived canonically from  $(D, \leq)$ . The fixpoint is computed with respect to  $\sqsubseteq$ .

$$\llbracket \pi_{p_1}, \dots, \pi_{p_n} \rrbracket_{\sigma} = \text{fix}_{\sqsubseteq}(\lambda m. \lambda p. \llbracket \pi_p \rrbracket_{\sigma m})$$

Ongoing work:

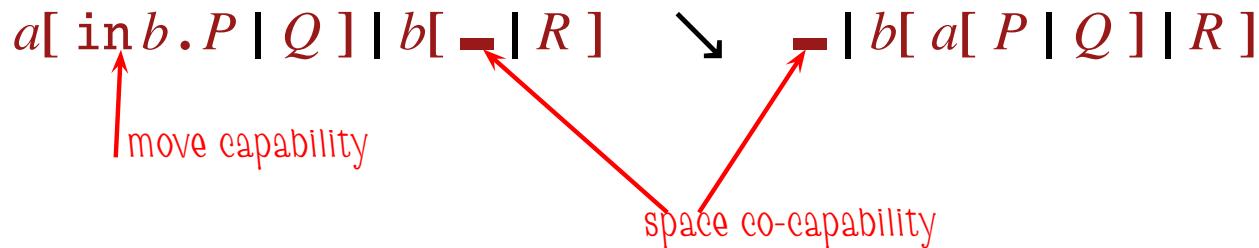
- ▶ Approximate the fixpoint in the presence of partial information.
- ▶ Use Kripke style semantics to capture trust evolution in time.
- ▶ Static safety guarantees: processes do not undermine their site policies.

# Dimensions, Capacities, Mobility

Central Notion: Resource Usage

Focus: Capacity Bounds Awareness.

- ▶ Bounded Capacity Ambients
- ▶ Fine control of capacity.
- ▶ Space as a linear co-capability.



Computation takes space, dynamically, and we'd like to model it.

# A Calculus of Bounded Capacities: Movement

## Fundamentals: Space Conscious Movement

$$\begin{array}{ccc} a[\text{ in } b.P \mid Q] \mid b[\text{ - } \mid R] & \searrow & \text{ - } \mid b[a[P \mid Q] \mid R] \\ \text{ - } \mid b[a[\text{ out } b.P \mid Q] \mid R] & \searrow & a[P \mid Q] \mid b[\text{ - } \mid R] \end{array}$$

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Example: Travelling needs but consumes no space.

$$\begin{array}{c} a[\text{ in } b.\text{in } c.\text{out } c.\text{out } b.0] \mid b[\_ \mid c[\_]] \\ \searrow \searrow \_ \mid b[\_ \mid c[a[\text{ out } c.\text{out } b.0]]] \\ \searrow \searrow a[0] \mid b[\_ \mid c[\_]] \end{array}$$

# A Calculus of Bounded Capacities: Sizes

Fundamentals: Space Conscious Movement

► But the size of travellers matters!

$$\begin{array}{ccc} a^k [ \text{in } b.P \mid Q ] \mid b[ \underbrace{- \mid \dots \mid -}_{k \text{ times}} \mid R ] & \xrightarrow{} & \underbrace{- \mid \dots \mid -}_{k \text{ times}} \mid b[ a^k [ P \mid Q ] \mid R ] \\ \underbrace{- \mid \dots \mid -}_{k \text{ times}} \mid b[ a^k [ \text{out } b.P \mid Q ] \mid R ] & \xrightarrow{} & a^k [ P \mid Q ] \mid b[ \underbrace{- \mid \dots \mid -}_{k \text{ times}} \mid R ] \end{array}$$

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What is the  $a^k$ ? A type annotation measuring the size of  $P$ .

Notation. We use  $\underline{-}^k$  as a shorthand for  $\underbrace{- \mid \dots \mid -}_{k \text{ times}}$ .

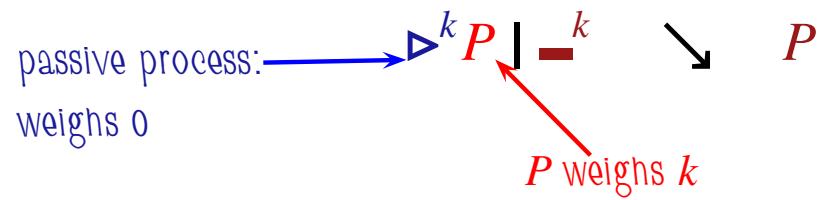
# A Calculus of Bounded Capacities: Spawning

Fundamentals: Space Conscious Process Activation

$$\triangleright^k P \mid \_^k \quad \searrow \quad P$$

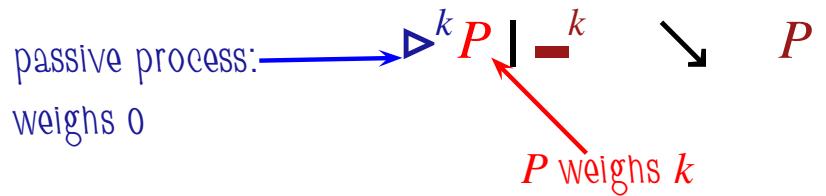
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## Fundamentals: Space Conscious Process Activation



# A Calculus of Bounded Capacities: Spawning

Fundamentals: Space Conscious Process Activation



Example: Replication:  $!^k \triangleq \triangleright^k$

$$!^k P \mid \_^k \quad \downarrow \quad !\triangleright^k P \mid P$$

Types ensure only 0-weighted processes are replicable: One must use spawning, so that replication needs space proportional to the process' weight.

# A Calculus of Bounded Capacities: Transfer

Fundamentals: Space Acquisition and Release

$$\text{put}^{\checkmark} a.P \mid \text{---} \mid a^k[\text{get}^{\hat{a}}.Q \mid R] \quad \searrow \quad P \mid a^{k+1}[Q \mid \text{---} \mid R]$$

$$a^{k+1}[\text{put}.P \mid \text{---} \mid S] \mid b^h[\text{get} a.Q \mid R] \quad \searrow \quad a^k[P \mid S] \mid b^{h+1}[Q \mid \text{---} \mid R]$$

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## Example: A Memory Module

$$\text{memMod} \triangleq \text{mem}[\text{---}^{256MB} \parallel \text{!put} \parallel \text{!get free}]$$

$$\text{malloc} \triangleq m[\text{!get mem.free}[\text{out m.get m.put}] \parallel \text{!put}]$$

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$$\text{memMod} \mid \text{malloc} \xrightarrow{256MB} \text{mem}[!\text{put} \mid !\text{get free}] \mid m[-^{256MB} \mid \dots] \xrightarrow{2 \times 256MB}$$

$$\text{mem}[!\text{put} \mid !\text{get free}] \mid \text{malloc} \mid \text{free}^{256MB}[- \mid \text{put}] \xrightarrow{256MB} \text{memMod} \mid \text{malloc} \mid \dots$$

# A System of Capacity Types

Capacity Types:  $\phi, \dots$  are pairs of nats  $[n, N]$ , with  $n \leq N$ .

Effect Types  $\mathcal{E}, \dots$  are pairs of nats  $(d, i)$ , representing dees and ines.

Exchange Types:  $\chi ::= \text{Shh} \mid \text{Amb}\langle\sigma, \chi\rangle \mid \text{Cap}\langle\mathcal{E}, \chi\rangle$

Process and Ambient and Capability Types:

$a : \text{Amb}\langle\phi, \chi\rangle$   $a$  has no less than  $\phi_m$  and no more than  $\phi_M$  spaces

$P : \text{Proc}\langle k, \mathcal{E}, \chi\rangle$   $P$  weighs  $k$  and produces the effect  $\mathcal{E}$  on ambients

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Thm: Subject Reduction: Well-typed processes preserve space.

If  $\Gamma \vdash P : \text{Proc}\langle k, \mathcal{E}, \chi\rangle$  and  $P \searrow Q$  then  $\Gamma \vdash Q : \text{Proc}\langle k, \mathcal{E}', \chi\rangle$  for some  $\mathcal{E}' \leq \mathcal{E}$ .

# Future Work

- What: Third-Party Resources: Models, Languages and Techniques
  - Resource-Aware Computation: resource bounds negotiation & enforcement
  - Resource Usage: calculi & logics for quantitative analysis
  - Resource Safety: languages for security & trust policies; general resource logics
  - Resource Trust: history-based: theory and infrastructures

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- ▶ How: Integrated approach: Behavioural, Execution, Abstract Models.
- ▶ Who: Communities involved:
  - EU FET Global Computing
  - UKCRC Great Challenges: Science for Global Ubiquitous Computing
  - EPSRC UK eScience & UK UbiNet

# Contexts as Labels

The intuition:

$$a \xrightarrow{\mathcal{C}} b \text{ iff } \mathcal{C}[a] \searrow b$$

For instance:

$$a \xrightarrow{-|\bar{a}} 0$$

$$M \xrightarrow{(\lambda x. -)N} M\{N/x\}$$

$$KM \xrightarrow{-N} M$$

Yep, but not quite:

- Too many labels not desirable:
  - Useless combinatorial explosion:  $\lambda x. xx \xrightarrow{-MN} MMN$
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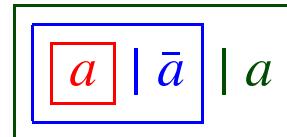
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Choose only 'minimal' redex-enabling contexts

► Case analysis of basic situations: Sewell. Abstract approach: Leifer-Milner



# A Categorical Approach

Lawvere theory on  $\Sigma$

- ▶ the natural numbers for objects
- ▶ a morphism  $t: m \rightarrow n$ , for  $t$  a  $n$ -tuple of  $m$ -holed terms.
- ▶ Composition is substitution of terms into holes.

E.G. for  $\Sigma$  the signature for arithmetics:

- ▶ term  $(-_1 \times x) + -_2$  is an arrow  $2 \rightarrow 1$  (two holes yielding one term)
- ▶  $\langle 3, 2 \times y \rangle$  is an arrow  $0 \rightarrow 2$  (a pair of terms with no holes).
- ▶ Their composition is the term  $(3 \times x) + (2 \times y)$ , an arrow of type  $0 \rightarrow 1$ .

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A generalisation from term rewriting systems to categories.

- ▶ A category  $\mathbb{C}$  with distinguished object  $0$ .
- ▶ A set of reaction rules  $\mathcal{R} \subseteq \bigcup_{C \in \mathbb{C}} \mathbb{C}(0, C) \times \mathbb{C}(0, C)$ .
- ▶ A set  $\mathbb{D}$  of arrows of  $\mathbb{C}$  called the reactive contexts.  
Assume that  $d_0 \cdot d_1 \in \mathbb{D}$  implies  $d_0$  and  $d_1 \in \mathbb{D}$ .

The reaction relation is defined as

$$a \longrightarrow b \quad \text{iff} \quad a = d \cdot l, \quad b = d \cdot r, \quad d \in \mathbb{D} \text{ and } \langle l, r \rangle \in \mathcal{R}.$$

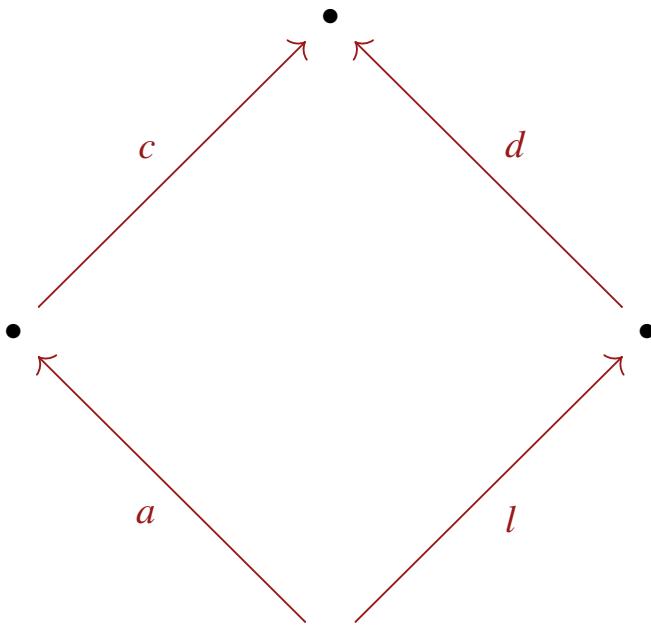


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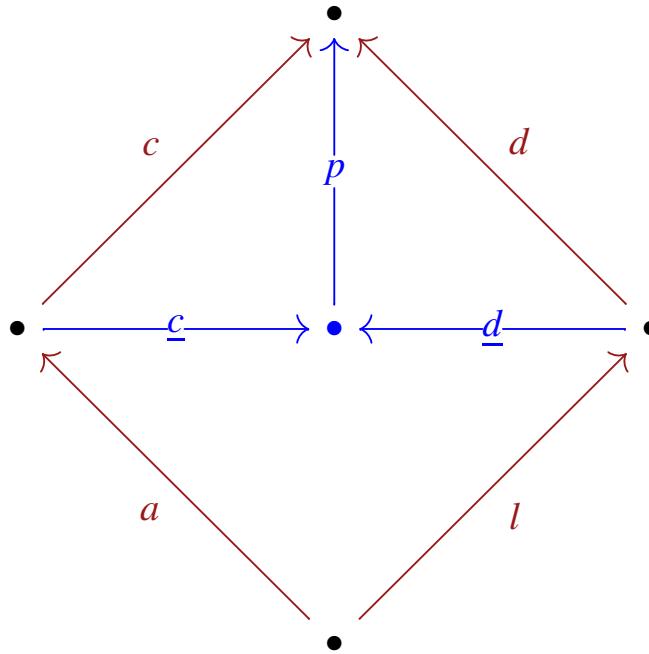
# (G)RPOS

Suppose that  $\mathbb{C}$  is a (bi)category and consider a redex square



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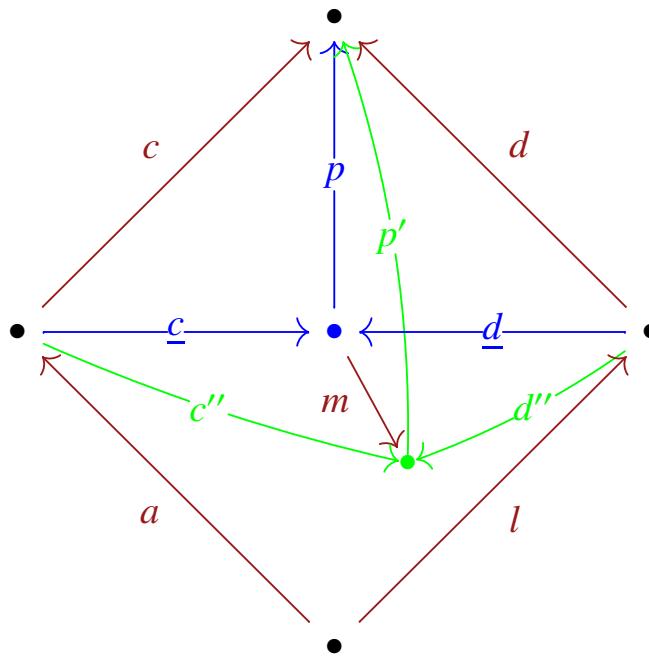
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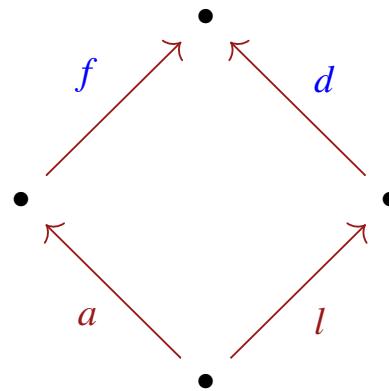


- ▶ a relative pushout (RPO) is a tuple  $\langle \underline{c}, \underline{d}, p \rangle$  which satisfies the universal property that:
- ▶ for any other such  $\langle c', d', p' \rangle$  there exists a unique mediating morphism  $m$ .

# Deriving LTS

The LTS derived from the reactive system has:

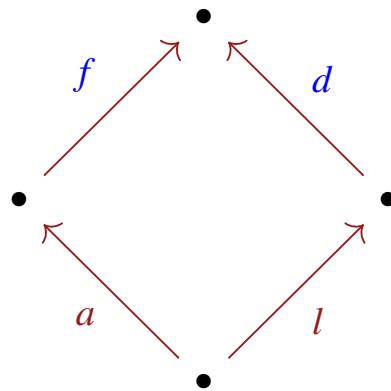
- ▶ Nodes:  $a : O \rightarrow N$
- ▶ Transitions:  $a \xrightarrow{f} dr$  iff for  $\langle l, r \rangle \in \mathcal{R}$  and  $d \in \mathbb{D}$ ,  $\langle f, d, \text{id} \rangle$  is a relative pushout of the square



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- ▶ Thm. If all redex squares like the above have (G)RPOS then the bisimulation on the derived LTS is a congruence.  
[Leifer-Milner 00, Sassone-Sobociński 02]

# Applying (G)RPOS

- Milner (2001) worked out RPOS for a graphical formalism called bigraphs.
- Sassone and Sobociński (2002) introduced GRPOS to handle calculi with non-trivial structural congruences.
- Jensen and Milner (2003) derived (essentially) the usual  $\pi$  labelled bisimulation on asynchronous  $\pi$  using RPOS.
- Sassone and Sobociński (2003) worked out an easy encoding of Milner's pre-category approach into the G-world.
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So far, the price of the initial 2-categorical investment seems worth paying...

## Future Work

- Extend to more complicated process calculi with complex structural congruences (e.g. replication); Apply to specific graph rewriting systems.