

Foundations of Global Computing

A Personal Perspective

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Foundations of Global Computing

Resource Control

Programming Languages

Semantic Theories

Models for Concurrency

Global Ubiquitous Computing:

computation over a global network of mobile, bounded resources shared among mobile entities which move between highly dynamic, largely unknown, untrusted networks.

Difficulties:

Extreme dynamic reconfigurability; lack of coordination and trust; limited capabilities; partial knowledge . . .

Issues:

Protection and management of resources; privacy and confidentiality of data; . . .

Foundations of Global Computing

Petri Nets Based Models and Calculi

Resource Control

A distributed timed-arc Petri net (DTAPN) is a Petri net together with

- a interval time constraint on transitions, either discrete or continuous;
- a clock synchronisation equivalence Σ on places.

Tokens age, and transitions are enabled accordingly. Time elapses at the same speed on p and p' if $p \Sigma p'$.

Programming Languages

Globally Asynchronous, Locally Synchronous

Global Time: $\Sigma = P \times P$ Local Time: $\Sigma = \Delta_P$

A Separation Result: Reachability for safe LT nets is decidable, but undecidable for safe GT nets.

Semantic Theories

Models for Concurrency

ICATPN 2001, FST&TCS 2001

Foundations of Global Computing

Resource Control

- A categorical machinery which allows the derivation of LTSs from reduction systems.
- Bisimulation on such LTSs is a congruence, provided a general condition is met.

Programming Languages

Coinduction Principle Desiderata:

- Operational Corresp.: $p \searrow q$ iff $p \xrightarrow{\tau} q$
- Correctness: $p \approx q$ implies $p \cong q$
- Completeness: $p \cong q$ implies $p \approx q$

Semantic Theories

The intuition:

$$a \xrightarrow{\mathcal{C}} b \text{ iff } \mathcal{C}[a] \searrow b$$

Eg:

$$a \xrightarrow{-|\bar{a}} \mathbf{0} \quad M \xrightarrow{(\lambda x. -)N} M\{N/x\} \quad \mathbf{K}M \xrightarrow{-N} M$$

Models for Concurrency

Foundations of Global Computing

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Semantic Theories

The intuition:

$$a \xrightarrow{\mathcal{C}} b \text{ iff } \mathcal{C}[a] \searrow b$$

But: Must choose labels carefully not to mess up the bisimulation

Choose only 'minimal' redex-enabling contexts: GRPOs.

Relative pushouts in groupoidal categories:

EXPRESS 2002, FOSSACS 2003, NJC, TCS

Models for Concurrency

Foundations of Global Computing

Resource Control

Jeeg: concurrent OO with history-sensitive access control

- Java (no `synchronized()`, `wait()`, `notify()`, `notifyAll()`) for business code;
- Linear Time Temporal Logic for synchronisation code (method guards).

Programming Languages

```
public class MyClass {  
    sync {  
        m :  $\phi$ ;  
        ....  
    }  
    ...// Standard Java class def  
}
```

Semantic Theories

where `m` is a method identifier and ϕ , the guard, is an LTL formula. When `m` is invoked, the thread is kept on hold unless ϕ . When the condition is true, all waiting threads are awoken. `m` is implicitly synchronised.

JavaGRANDE 2002, WOODS 2003, Cone & Comp, OOPS 2004

Models for Concurrency

Foundations of Global Computing

Resource Control

Resources: Models, Types, Logics, Languages

➤ Access Control (Concur 2002, ESOP 2004)

Programming Languages

➤ Access Authorisation (FST&TCS 2002, Info&Co)

Semantic Theories

➤ Secrecy for Mobile Agents (ICALP 2003)

➤ Trust Management (SEFM 2003)

Models for Concurrency

➤ Bounds Control (ASIAN 2003)

Mobile Ambients

Both administrative domains and computational environments

➤ Subjective movements

$$\begin{aligned} n[\text{in } m.P \mid Q] \mid m[R] &\longrightarrow m[n[P \mid Q] \mid R] \\ m[n[\text{out } m.P \mid Q] \mid R] &\longrightarrow n[P \mid Q] \mid m[R] \end{aligned}$$

➤ Boundary dissolver

$$\text{open } n.P \mid n[Q] \longrightarrow P \mid Q.$$

➤ Process interaction

$$n[\langle M \rangle.P \mid (x).Q] \longrightarrow n[P \mid Q\{x := M\}],$$

Group Types for Mobility

Aim: *Resource Access Control*

- Detect and prevent unwanted access to resources.
- Focus on static approaches based on enforcing type disciplines.

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Groups: Sets of processes with common access rights.

Constraints like $k : \text{CanEnter}(n)$ are modelled as:

n belongs to group G

k may cross the border of ambients of group G .

For instance, the system:

$$k[\text{in } n \mid l[\text{out } k]] \mid n[-]$$

is *well-typed* under assumptions of the form:

$$k : \text{amb}[\mathbf{K}, \text{cross}(\mathbf{N})]$$
$$l : \text{amb}[\mathbf{L}, \text{cross}(\mathbf{K})]$$
$$n : \text{amb}[\mathbf{N}, \dots]$$

Indirect Border Crossing

Trojan Horses: The system

$\text{Odysseus}[\text{in Horse.out Horse.Destroy}] \mid \text{Horse}[\text{in Troy}] \mid \text{Troy}[\text{Trojans}]$

is well-typed under assumptions:

$\text{Odysseus} : \text{amb}[\text{Achaean}, \text{cross}(\text{Toy})]$

$\text{Horse} : \text{amb}[\text{Toy}, \text{cross}(\text{City})]$

$\text{Troy} : \text{amb}[\text{City}, _]$

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$\text{Troy} : \text{amb}[\text{City}, _]$

However, the system may evolve to

$\text{Troy}[\text{Trojans} \mid \text{Horse}[_] \mid \text{Odysseus}[\text{Destroy}]]$

where Odysseus got inside **Troy's Walls** taking by surprise the *Trojans*.

Types

Groups: $\mathbf{G}, \mathbf{H}, \dots$

Sets of groups: $\mathcal{P}, \mathcal{I}, \dots$ \mathcal{U} The universal set of groups

Ambients types:

$\mathbf{A} ::= \text{amb}[\mathbf{G}, \mathbf{M}]$ amb of group \mathbf{G} , with mobility type \mathbf{M}

Process types:

$\Pi ::= \text{proc}[\mathbf{G}, \mathbf{M}]$ process that can be enclosed in an ambient of group \mathbf{G} , may drive to ambients whose groups are in \mathbf{M}

Capability types:

$\mathbf{K} ::= \text{cap}[\mathbf{G}, \mathbf{M}]$ capability that can appear in an ambient of group \mathbf{G} , may drive it to ambients whose groups are in \mathbf{M}

Mobility types:

$\mathbf{M} ::= \text{mob}[\mathcal{P}]$ mobility specs: where processes are allowed to reside

Access Control Properties

Mobility properties:

➤ If $\Gamma \vdash n[\text{in } m.P \mid Q] \mid m[R] : \Pi$, then

$$\Gamma \vdash m : \text{amb}[\mathbf{M}, _] \quad \text{and} \quad \Gamma \vdash n : \text{amb}[_, \text{mob}[\mathcal{P}]]$$

with $\mathbf{M} \in \mathcal{P}$.

➤ If $\Gamma \vdash m[n[\text{out } m.P \mid Q] \mid R] : \Pi$, then

$$\Gamma \vdash m : \text{amb}[\mathbf{M}, \text{mob}[\mathcal{P}_m]] \quad \text{and} \quad \Gamma \vdash n : \text{amb}[\mathbf{N}, \text{mob}[\mathcal{P}_n]]$$

with $\mathbf{M} \in \mathcal{P}_n$ and $\mathcal{P}_m \subseteq \mathcal{P}_n$.

Detecting Odysseus' intentions

Now, in order to assign a type to

`Odysseus[in Horse.out Horse.Destroy] | Horse[in Troy] | Troy[Trojans]`

we need assumptions of the form:

`Odysseus : amb[Achaean, mob[{Ground, Toy, City}]]`

`Horse : amb[Toy, mob[{Ground, City}]]`

`Troy : amb[City, _]`

representing that `Odysseus` is an **Achaean** intended to move into a **City**!

Detecting Odysseus' intentions

Now, in order to assign a type to

Odysseus[**in** *Horse*.**out** *Horse*.*Destroy*] | *Horse*[**in** *Troy*] | *Troy*[*Trojans*]

we need assumptions of the form:

Odysseus : amb[**Achaean**, mob[{**Ground**, **Toy**, **City**}]]

Horse : amb[**Toy**, mob[{**Ground**, **City**}]]

Troy : amb[**City**, _]

representing that *Odysseus* is an **Achaean** intentioned to move into a **City**!

On the other hand, under assumptions of the form

Odysseus : amb[**Achaean**, mob[{**Ground**, **Toy**}]]

the *Trojans* should not fear any attack from *Odysseus*.

Dependent Types for Access Control

Dependent Mobility Types: (\mathcal{P} and \mathcal{C} are sets of names, not groups.)

$$A ::= \text{amb}[\text{hasFathers}(\mathcal{P}), \text{hasChildren}(\mathcal{C})]$$

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Dependent types allow personalised services and dynamic access control.

$$\text{HorseServer} \triangleq !(x)(\nu \text{Horse} : \text{amb}[_ , \text{hasChildren}\{x\}])\text{Horse}[\text{out Troy.in Troy.0}]$$

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- Names have several possible types, depending on the *actual* communications occurred.
- The set of names *exchanged* over a channel must be tracked. Luckily, The set of possible types for a name has a *maximum* and a *minimum* element.

Secrecy in Mobile Ambients

Names \approx Cryptokeys: Carrying messages inside *private* ambients preserves message *integrity* and *privacy*. Or, does it?

$$(\nu n)(a[n[\text{out } a.\text{in } b.\langle M \rangle]] \mid b[\text{open } n.(x)P])$$

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It actually offers no guarantees for software agents, as *n* must be revealed along the move, and servers may peek inside.

How to provide stronger protection?

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It actually offers no guarantees for software agents, as *n* must be revealed along the move, and servers may peek inside.

How to provide stronger protection?

A new crypto-primitive: subjective access control using co-capabilities + data encryption to preserve secrecy of data while agents move autonomously

$$n[\text{seal } k.P | Q] \longrightarrow n[P | Q]_k$$

sealed under *k*

crypto-key

Effects:

- blocks message exchanges and encrypts their contents;
- the sealed ambient cannot communicate, but it may move.

Sealed Ambients

- The mechanism to resume to a fully operational state is associated to movements and co-capabilities containing keys

$$n\{\text{in } m.P \mid Q\}_k \mid m\{\overline{\text{in}} \{x\}_k.R \mid R'\} \longrightarrow m\{n[P \mid Q] \mid R\{x := n\} \mid R'\}$$

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Example:

$$(\nu k)a[n[\text{seal } k.\text{out } a.\text{in } b.\langle M \rangle^{\hat{}}]] \mid b[\overline{\text{in}} \{x\}_k.(y)^x.P]$$

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Secrecy and Adversaries

Intuitively:

A process preserves the secrecy of a piece of data M if it does not publish M , or anything that would permit the computation of M .

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S-Adversary: A context $A(-)$ which initially knows names and capabilities in S .

Revealing Names: P may reveal n to S if there exists an S -adversary $A(-)$ and a name $c \in S$ such that:

$$A(P) \Longrightarrow C(c[\langle n \rangle^\wedge \mid Q]) \quad (c \text{ free})$$

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Typing System: Secrecy is captured by a type system \vdash which may classify processes as **untrusted** $\Gamma \vdash P : \text{Un}$, and data as **public** $a : \text{Public}$ if it can be exchanged with untrusted process.

Secrecy Theorem: Well-typed processes do not reveal their secrets publicly. Formally, if $\Gamma \vdash P : \text{Un}$ and $\Gamma \not\vdash s : \text{Public}$, then P preserves the secrecy of s from all public channels, i.e. from $\{a \mid \Gamma \vdash a : \text{Public}\}$. (Payload s won't be entrusted to a public a .)

Between Theory and Practice

That's all good, but ...

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... one cannot type the Internet

The gap between theory and practice matters in practice.

All this only works as long as you **trust** the certified types, or are willing to **typecheck** migrating code yourself (**bytecode verification**, **PCC**, ...), ...

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All this only works as long as you **trust** the certified types, or are willing to **typecheck** migrating code yourself (**bytecode verification**, **PCC**, ...), ...

- **Verification** (relates to type checking/inference)
- **Certificates** (groups as certified roles)
- **Trust**: In UbiComp, **security** must work be coupled with **trust management**.

Which is hard, because of **delegation** and **dynamic policies**

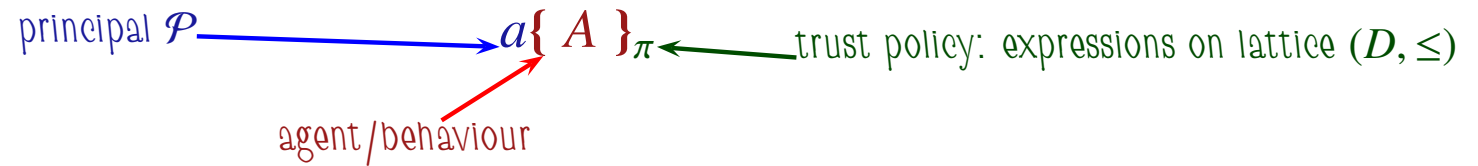
Trust Management

Focus on Trust Evolution and Delegation in Dynamic Networks

$$a\{A\}_{\pi}$$

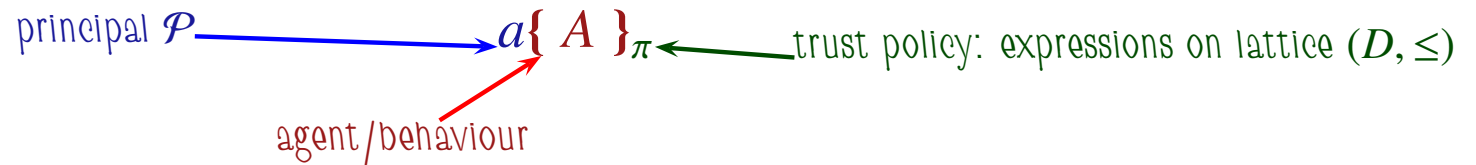
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Trust Based Services:

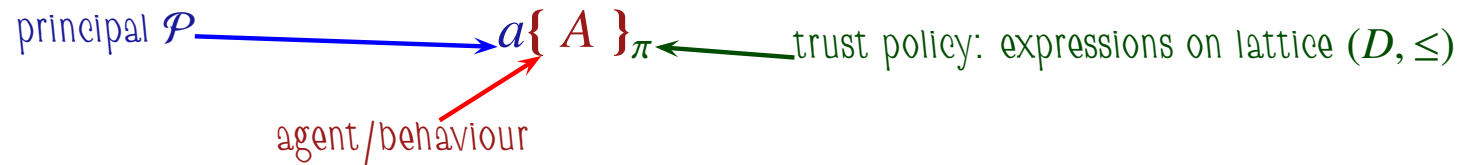
$$a\{ b.\ell\langle v \rangle . A \}_- \mid b\{ \ell(x) . \Sigma_t B_t \}_{\pi} \longrightarrow a\{ A \}_- \mid b\{ B_{\pi(a)}\{x := v\} \}_{\pi}$$

Trust Evolution:

$$a\{ \zeta . A \mid B \}_{\pi} \longrightarrow a\{ A \mid B \}_{\zeta(\pi)}$$

Trust Management

Focus on Trust Evolution and Delegation in Dynamic Networks



Trust Based Services:

$$a\{b.\ell\langle v \rangle.A\}_\pi \mid b\{\ell(x).\Sigma_t B_t\}_\pi \longrightarrow a\{A\}_\pi \mid b\{B_{\pi(a)}\{x := v\}\}_\pi$$

Trust Evolution:

$$a\{\zeta.A \mid B\}_\pi \longrightarrow a\{A \mid B\}_{\zeta(\pi)}$$

Policies and Expressions:

$\pi ::= \lceil p \rceil$	delegation	$\tau ::= t \in D$	value/var
$\lambda x : P. \tau$	abstraction	$\pi(p)$	policy value
$\text{op}(\pi_1, \dots, \pi_n)$	lattice op	$e \mapsto \tau; \tau$	choice
$p ::= a \in \mathcal{P}, x : P$	principal/vars	$e ::= \tau \text{ emp } \tau, p \text{ eq } p$	comparisons
		$e \text{ bop } e$	boolean op

Understanding Delegation

Example:

$a :$ $p \mapsto \text{trusted};$

$q \mapsto \ulcorner b \urcorner(q);$

$z \mapsto \ulcorner p \urcorner(z);$

$b :$ $p \mapsto \ulcorner a \urcorner(p);$

$q \mapsto \text{untrusted};$

$z \mapsto \ulcorner a \urcorner(z);$

Understanding Delegation

Example:

$a : p \mapsto \text{trusted};$

$q \mapsto \lceil b \rceil(q);$

$z \mapsto \lceil p \rceil(z);$

$b : p \mapsto \lceil a \rceil(p);$

$q \mapsto \text{untrusted};$

$z \mapsto \lceil a \rceil(z);$

Delegation, formally: Global trust as a fixpoint.

$\pi : (\mathcal{P} \rightarrow \mathcal{P} \rightarrow D) \rightarrow (\mathcal{P} \rightarrow D)$

Local Policy

$\Xi : (\mathcal{P} \rightarrow \mathcal{P} \rightarrow D) \rightarrow (\mathcal{P} \rightarrow \mathcal{P} \rightarrow D)$

Collected Policies

Global Trust: $\text{fix}(\Xi) : \mathcal{P} \rightarrow \mathcal{P} \rightarrow D.$ But, is this good enough?

Understanding Delegation

Example:

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$q \mapsto \lceil b \rceil(q);$

$z \mapsto \lceil p \rceil(z);$

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Collected Policies

Global Trust: $\text{fix}(\Xi) : \mathcal{P} \rightarrow \mathcal{P} \rightarrow D.$ But, is this good enough?

$p : \text{trusted}$

$q : \text{untrusted}$

$z : ???$

Cannot confuse don't trust with don't know: the value of $\lceil p \rceil(z)$ could become available later.

Need to account for uncertain knowledge of $\lceil p \rceil(z) \in D.$

Trust Structures



Thm. (D, \leq, \sqsubseteq) yields an adequate semantics $\llbracket - \rrbracket : \text{Policies} \rightarrow \text{Env} \rightarrow (\mathcal{P} \rightarrow \mathcal{P} \rightarrow D)$.
 The trust structure is derived canonically from (D, \leq) . The fixpoint is computed with respect to \sqsubseteq .

$$\llbracket \pi_{p_1}, \dots, \pi_{p_n} \rrbracket_{\sigma} = \text{fix}_{\sqsubseteq}(\lambda m. \lambda p. (\llbracket \pi_p \rrbracket_{\sigma m}))$$

Ongoing work:

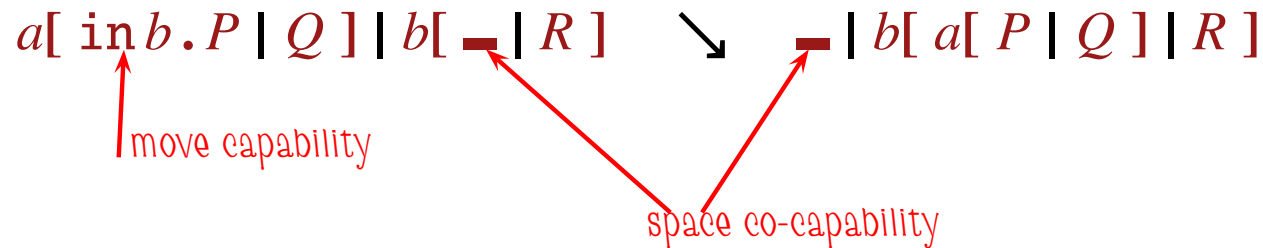
- Approximate the fixpoint in the presence of partial information.
- Use Kripke style semantics to capture trust evolution in time.
- Static safety guarantees: processes do not undermine their site policies.

Dimensions, Capacities, Mobility

Central Notion: Resource Usage

Focus: Capacity Bounds Awareness.

- Bounded Capacity Ambients
- Fine control of capacity.
- Space as a linear co-capability.



Computation takes space, dynamically, and we'd like to model it.

A Calculus of Bounded Capacities: Movement

Fundamentals: Space Conscious Movement

$$\begin{array}{lcl} a[\text{in } b.P \mid Q] \mid b[_ \mid R] & \searrow & _ \mid b[a[P \mid Q] \mid R] \\ _ \mid b[a[\text{out } b.P \mid Q] \mid R] & \searrow & a[P \mid Q] \mid b[_ \mid R] \end{array}$$

A Calculus of Bounded Capacities: Movement

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Example: Travelling needs but consumes no space.

$$\begin{array}{lcl} a[\text{in } b.\text{in } c.\text{out } c.\text{out } b.0] \mid b[_ \mid c[_]] & & \\ \searrow \searrow _ \mid b[_ \mid c[a[\text{out } c.\text{out } b.0]]] & & \\ \searrow \searrow a[0] \mid b[_ \mid c[_]] & & \end{array}$$

A Calculus of Bounded Capacities: Sizes

Fundamentals: Space Conscious Movement

► But the **size** of travellers matters!

$$\begin{array}{lcl}
 a^k[\text{in } b.P \mid Q] \mid b[\overbrace{- \mid \dots \mid -}^{k \text{ times}} \mid R] & \searrow & \overbrace{- \mid \dots \mid -}^{k \text{ times}} \mid b[a^k[P \mid Q] \mid R] \\
 \underbrace{- \mid \dots \mid -}_{k \text{ times}} \mid b[a^k[\text{out } b.P \mid Q] \mid R] & \searrow & a^k[P \mid Q] \mid b[\underbrace{- \mid \dots \mid -}_{k \text{ times}} \mid R]
 \end{array}$$

A Calculus of Bounded Capacities: Sizes

Fundamentals: Space Conscious Movement

► But the **size** of travellers matters!

$$\begin{array}{ccc}
 a^k[\text{in } b.P \mid Q] \mid b[\overbrace{- \mid \dots \mid -}^{k \text{ times}} \mid R] & \searrow & \overbrace{- \mid \dots \mid -}^{k \text{ times}} \mid b[a^k[P \mid Q] \mid R] \\
 \underbrace{- \mid \dots \mid -}_{k \text{ times}} \mid b[a^k[\text{out } b.P \mid Q] \mid R] & \searrow & a^k[P \mid Q] \mid b[\underbrace{- \mid \dots \mid -}_{k \text{ times}} \mid R]
 \end{array}$$

What is the a^k ? A type annotation measuring the size of P .

Notation. We use $\overbrace{-}^k$ as a shorthand for $\overbrace{- \mid \dots \mid -}^{k \text{ times}}$.

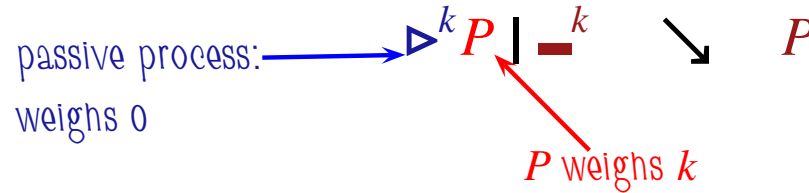
A Calculus of Bounded Capacities: Spawning

Fundamentals: Space Conscious Process Activation

$$\triangleright^k P \mid \text{---}^k \searrow P$$

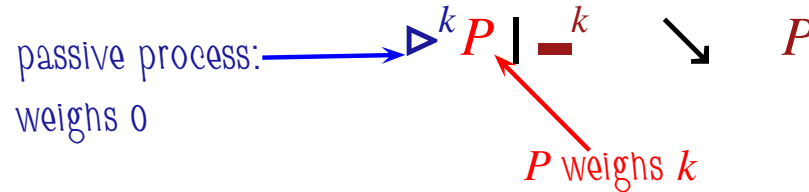
A Calculus of Bounded Capacities: Spawning

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A Calculus of Bounded Capacities: Spawning

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Example: Replication: $!^k \triangleq !\triangleright^k$

$$!\triangleright^k P \mid _^k \searrow !\triangleright^k P \mid P$$

Types ensure only 0-weighted processes are replicable: One must use spawning, so that replication needs space proportional to the process' weight.

A Calculus of Bounded Capacities: Transfer

Fundamentals: Space Acquisition and Release

$$\text{put}^{\checkmark} a . P \mid _ \mid a^k [\text{get}^{\wedge} . Q \mid R] \quad \searrow \quad P \mid a^{k+1} [Q \mid _ \mid R]$$

$$a^{k+1} [\text{put} . P \mid _ \mid S] \mid b^h [\text{get} a . Q \mid R] \quad \searrow \quad a^k [P \mid S] \mid b^{h+1} [Q \mid _ \mid R]$$

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Example: A Memory Module

$$\text{memMod} \triangleq \text{mem} [_^{256MB} \mid !\text{put} \mid !\text{get free}]$$

$$\text{malloc} \triangleq \text{m} [!\text{get mem} . \text{free} [\text{out m} . \text{get m} . \text{put}] \mid !\text{put}]$$

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$$\text{memMod} \mid \text{malloc} \searrow^{256MB} \text{mem} [!\text{put} \mid !\text{get free}] \mid \text{m} [_^{256MB} \mid \dots] \searrow^{2 \times 256MB}$$

$$\text{mem} [!\text{put} \mid !\text{get free}] \mid \text{malloc} \mid \text{free}^{256MB} [_ \mid \text{put}] \searrow^{256MB} \text{memMod} \mid \text{malloc} \mid \dots$$

A System of Capacity Types

Capacity Types: ϕ, \dots are pairs of nats $[n, N]$, with $n \leq N$.

Effect Types \mathcal{E}, \dots are pairs of nats (d, i) , representing dees and ines.

Exchange Types: $\chi ::= \text{Shh} \mid \text{Amb}\langle\sigma, \chi\rangle \mid \text{Cap}\langle\mathcal{E}, \chi\rangle$

Process and Ambient and Capability Types:

$a : \text{Amb}\langle\phi, \chi\rangle$ a has no less than ϕ_m and no more than ϕ_M spaces

$P : \text{Proc}\langle k, \mathcal{E}, \chi\rangle$ P weighs k and produces the effect \mathcal{E} on ambients

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Thm: Subject Reduction: Well-typed processes preserve space.

If $\Gamma \vdash P : \text{Proc}\langle k, \mathcal{E}, \chi\rangle$ and $P \searrow Q$ then $\Gamma \vdash Q : \text{Proc}\langle k, \mathcal{E}', \chi\rangle$ for some $\mathcal{E}' \triangleleft \mathcal{E}$.

Future Work

- What: Third-Party Resources: Models, Languages and Techniques
 - Resource-Aware Computation: resource bounds negotiation & enforcement
 - Resource Usage: calculi & logics for quantitative analysis
 - Resource Safety: languages for security & trust policies; general resource logics
 - Resource Trust: history-based: theory and infrastructures

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- Who: **Communities involved:**
 - EU FET Global Computing
 - UKCRC Great Challenges: Science for Global Ubiquitous Computing
 - EPSRC UK eScience & UK UbiNet

Contexts as Labels

The intuition:

$$a \xrightarrow{\mathcal{C}} b \text{ iff } \mathcal{C}[a] \searrow b$$

For instance:

$$a \xrightarrow{-|\bar{a}} \mathbf{0}$$

$$M \xrightarrow{(\lambda x. -)N} M\{N/x\}$$

$$\mathbf{K}M \xrightarrow{-N} M$$

Yep, but not quite:

➤ Too many labels not desirable:

➤ Useless combinatorial explosion: $\lambda x. xx \xrightarrow{-MN} MMN$

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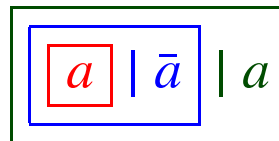
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Choose only 'minimal' redex-enabling contexts

➤ Case analysis of basic situations: Sewell. Abstract approach: Leifer-Milner



A Categorical Approach

Lawvere theory on Σ

- the natural numbers for objects
- a morphism $t: m \rightarrow n$, for t a n -tuple of m -holed terms.
- Composition is substitution of terms into holes.

E.G. for Σ the signature for arithmetics:

- term $(-_1 \times x) + -_2$ is an arrow $2 \rightarrow 1$ (two holes yielding one term)
- $\langle 3, 2 \times y \rangle$ is an arrow $0 \rightarrow 2$ (a pair of terms with no holes).
- Their composition is the term $(3 \times x) + (2 \times y)$, an arrow of type $0 \rightarrow 1$.

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A generalisation from term rewriting systems to categories.

- A category \mathbb{C} with distinguished object 0 .
- A set of reaction rules $\mathcal{R} \subseteq \bigcup_{C \in \mathbb{C}} \mathbb{C}(0, C) \times \mathbb{C}(0, C)$.
- A set \mathbb{D} of arrows of \mathbb{C} called the reactive contexts.

Assume that $d_0 . d_1 \in \mathbb{D}$ implies d_0 and $d_1 \in \mathbb{D}$.

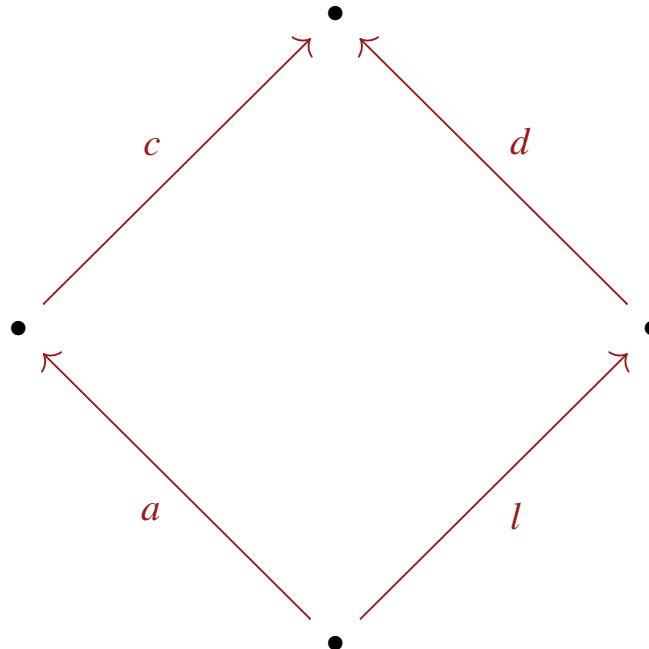
The reaction relation is defined as

$$a \longrightarrow b \quad \text{iff} \quad a = d . l, \quad b = d . r, \quad d \in \mathbb{D} \quad \text{and} \quad \langle l, r \rangle \in \mathcal{R}.$$



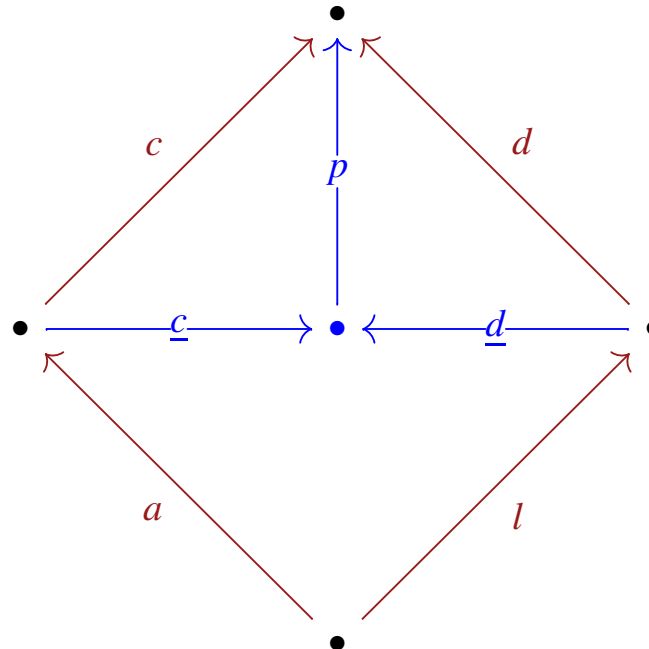
(G)RPOs

Suppose that \mathbb{C} is a (bi)category and consider a redex square



$(G)RPOs$

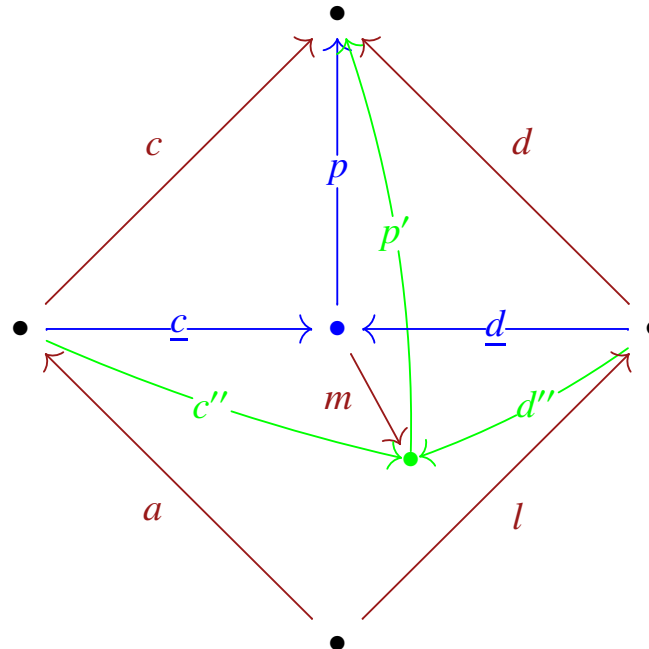
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- a relative pushout (RPO) is a tuple $\langle \underline{c}, \underline{d}, p \rangle$ which satisfies the universal property that:

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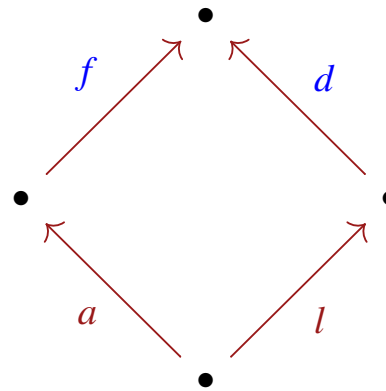


- a relative pushout (RPO) is a tuple $\langle \underline{c}, \underline{d}, p \rangle$ which satisfies the universal property that:
- for any other such $\langle c', d', p' \rangle$ there exists a unique mediating morphism m .

Deriving LTS

The LTS *derived* from the reactive system has:

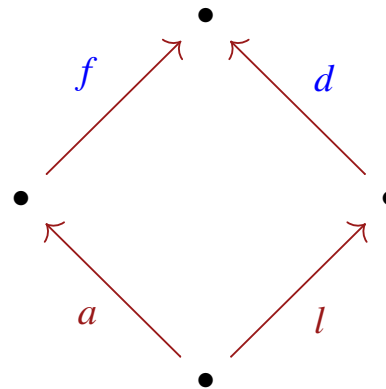
- Nodes: $a : O \rightarrow N$
- Transitions: $a \xrightarrow{f} dr$ iff for $\langle l, r \rangle \in \mathcal{R}$ and $d \in \mathbb{D}$, $\langle f, d, \text{id} \rangle$ is a relative pushout of the square



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- Thm. If all *redex squares* like the above have (G)RPOs then the bisimulation on the derived LTS is a *congruence*.

[Leifer-Milner 00, Sassone-Sobocinski 02]

Applying (G)RPOs

- Milner (2001) worked out RPOs for a graphical formalism called bigraphs.
- Sassone and Sobocinski (2002) introduced GRPOs to handle calculi with non-trivial structural congruences.
- Jensen and Milner (2003) derived (essentially) the usual π labelled bisimulation on asynchronous π using RPOs.
- Sassone and Sobocinski (2003) worked out an easy encoding of Milner's pre-category approach into the G-world.
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So far, the price of the initial 2-categorical investment seems worth paying...

Future Work

- Extend to more complicated process calculi with complex structural congruences (e.g. replication); Apply to specific graph rewriting systems.