A Distributed Calculus for Role-Based Access Control

Daniele Gorla

joint work with C. Braghin and V. Sassone

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Contents

- the *RBAC96* model
- a *formal framework* for concurrent systems running under a RBAC policy: an extension of the π-calculus
- a *type system* ensuring that the specified policy is respected during computations
- a *bisimulation* to reason on systems' behaviours
- some useful applications of the theory:
  - finding the *'minimal' schema* to run a given system
  - *refining a system* to be run under a given schema
  - *minimize the number of users* in a given system.

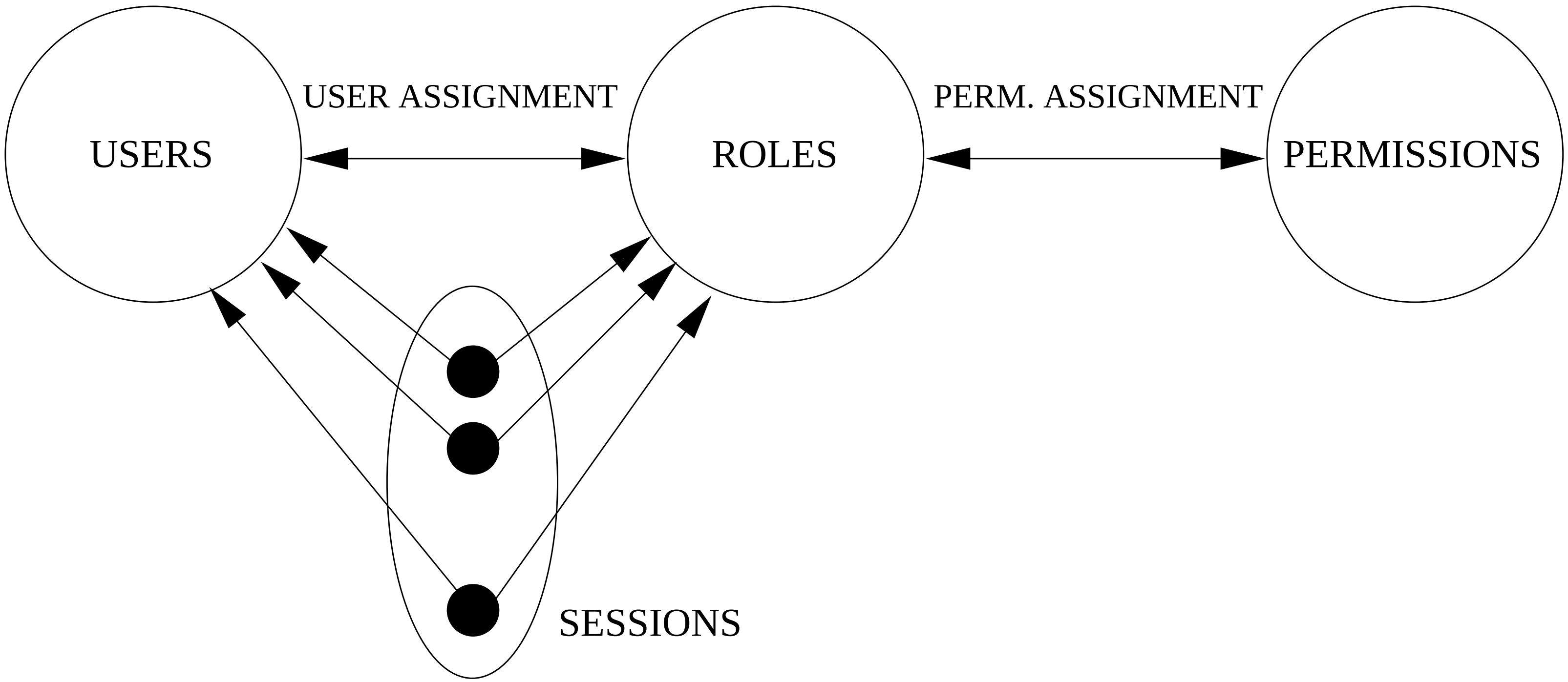
Access Control Models

“Techniques used to define or restrict the rights of individuals or application programs to obtain data from, or place data onto, a storage device"
(American National Standard, Telecom Glossary)

3 well-known models:

- *Discretionary access control*
- *Mandatory access control*
- *Rôle-based access control*

The Basic RBAC model



RBAC

Role-Based Access Control is attracting increasing attention because:

- it reduces complexity and cost of security administration;
- permission's management is less error-prone;
- it is flexible (rôle's hierarchy, separation of duty, etc.);
- it is *least privilege*-oriented.

Our work

Formalize the behaviour of concurrent and distributed systems under security policies defined in a RBAC fashion.

This is similar to

- the types developed in Dπ and KLAIM to implement discretionary access control
- the types developed for Boxed Ambients to implement mandatory access control

The starting point: π-calculus

Concurrent processes communicating on *channels*.

$$\textsc{Processes:}\quad P,Q \;::=\; a(x).P \;\mid\; u\langle v\rangle.P \;\mid\; [u=v]P \;\mid\; (\nu a\!:\!R)P \;\mid\; \mathbf{nil} \;\mid\; P|Q \;\mid\; !P$$

The Syntax of our Calculus

Concurrent processes communicating on *channels*.

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$$\textsc{User Sessions:}\qquad r\{\!|P|\!\}_\rho$$

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Channels are allocated to users to enable a distibuted implementation

Dynamic Semantics

It is given in the form of a *reduction relation*

Communication:

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$$r\{\!|\mathbf{role}\;R.P|\!\}_\rho$$

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$$r\{\!|\mathbf{yield}\, R.P|\!\}_\rho \longmapsto r\{\!|P|\!\}_{\rho-\{R\}}$$

RBAC schema

- Permissions are *capabilities* that enable process actions. Thus, $\mathcal{A} \triangleq \{R^{\uparrow}, R^{?}, R^{!}\}_{R \in \mathcal{R}}$ is the set of permissions.

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- In our framework, the *RBAC schema* is a pair of finite relations $(\mathcal{U} \,;\, \mathcal{P})$, such that

$$\mathcal{U} \subseteq_{\text{fin}} (\mathcal{N}_u \cup \mathcal{C}) \times \mathcal{R} \qquad\qquad \mathcal{P} \subseteq_{\text{fin}} \mathcal{R} \times \mathcal{A}$$

An Example

A banking scenario:

- two users, the client r and the bank s
- cashiers are modelled as channels $c_1, \ldots, c_n$ of user s
- the rôles available are `client` and `cashier`.

$$r\{\!|\, \textbf{role}\ \texttt{client}.enqueue^s\langle r\rangle.dequeue(z).z\langle req_1\rangle.\cdots.z\langle req_k\rangle.z\langle stop\rangle.\textbf{yield}\ \texttt{client}\,|\!\}_\rho \quad \|$$

$$s\{\!|\,(\nu\, free)(!enqueue(x).free(y).dequeue^x\langle y\rangle \quad | \quad \Pi_{i=1}^n free^s\langle c_i^s\rangle \quad |$$

$$\Pi_{i=1}^n\ !c_i(x).(\ [x = withdrw\_req]\ <\textsf{handle withdraw request}> \ |$$

$$[x = dep\_req]\ <\textsf{handle deposit request}> \ | \ \ldots \ |$$

$$[x = stop]free^s\langle c_i^s\rangle)\ )\,|\!\}_{\rho'}$$

Static Semantics - Types

- The syntax of types:

$$
\begin{array}{lrcl}
\textit{Types} & T & ::= & UT \quad | \quad C \\
\textit{User Types} & UT & ::= & \rho[a_1 : R_1(T_1), \ldots, a_n : R_n(T_n)] \\
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- A typing environment is a mapping from user names and variables to user types that respects the assignments in $\mathcal{U}$

Static Semantics - The Type System

An example: performing input actions.

(T-INPUT)

$$\frac{\Gamma \vdash a : R(T) \qquad R^{?} \in \mathcal{P}(\rho) \qquad \Gamma, x \mapsto T; \rho \vdash_r^{\mathcal{P}} P}{\Gamma; \rho \vdash_r^{\mathcal{P}} a(x).P}$$

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Type Safety: Let A be a well-typed system for $(\mathcal{U}; \mathcal{P})$. Then, whenever $A \equiv (\nu\, \widetilde{a^r : R})(A' \parallel r\{\!|b(x).P|\!\}_\rho)$, it holds that

- either $b^r : S \in \widetilde{a^r : R}$ and $S^{?} \in \mathcal{P}(\rho)$,
- or $b^r \notin \widetilde{a^r}$ and $S^{?} \in \mathcal{P}(\rho)$, where $\{S\} = \mathcal{U}(b^r)$

The Example Again

- The banking scenario again:
  - now each available operation is modelled as a different channel ($wdrw$ = withdraw, opn = open account, cc = credit card request)
  - the communication among different channels requires different rôles
  - $\mathcal{P}$ is such that $\{(\texttt{rich\_client}, \texttt{cc}^{!}), (\texttt{rich}, \texttt{rich\_client}^{\uparrow})\} \subseteq \mathcal{P}$.

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$$\not\vdash r\{\!|\mathbf{role}\ \mathtt{client}.enqueue^{s}\langle r\rangle.dequeue(z).z\langle creditcard\_req\rangle.cc^{s}\langle signature\rangle.z\langle stop\rangle|\!\}_{\{\mathtt{user}\}}$$

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LTS Semantics

- The labels of the LTS are derived from those of the π-calculus:

$$\mu \quad ::= \quad \tau \quad | \quad a^r n \quad | \quad a^r n : R \quad | \quad \overline{a}^r n \quad | \quad \overline{a}^r n : R$$

- the LTS relates *configurations*, i.e. pairs $(\mathcal{U}\,;\mathcal{P}) \triangleright A$ made up of a RBAC schema $(\mathcal{U}\,;\mathcal{P})$ and a system A.
- Example:

$$\text{(LTS-F-INPUT)} \quad \frac{\mathcal{U}(a^r) = \{R\} \qquad R^? \in \mathcal{P}(\rho) \qquad n \notin dom(\mathcal{U})}{(\mathcal{U}\,;\mathcal{P}) \triangleright r\{\!|a(x).P|\!\}_\rho \xrightarrow{a^r n:S} (\mathcal{U} \uplus \{n : S\}; \mathcal{P}) \triangleright r\{\!|\, P[{}^{n}\!/\!{}_{x}] \,|\!\}_\rho}$$

Bisimulation Equivalence

- We can define a standard bisimulation over the LTS
- (Bisimulation) It is a binary symmetric relation $\mathcal{S}$ between configurations such that, if $(D, E) \in \mathcal{S}$ and $D \xrightarrow{\mu} D'$, there exists a configuration E' such that $E \stackrel{\hat{\mu}}{\Longrightarrow} E'$ and $(D', E') \in \mathcal{S}$. *Bisimilarity*, $\approx$, is the largest bisimulation.
- the bisimulation is adequate with respect to a standardly defined (typed) barbed congruence.

Some Algebraic Laws

- if an action is not enabled, then the process cannot evolve:

$$r\{\!|\alpha.P|\!\}_\rho \approx \mathbf{0} \qquad \text{if } \mathcal{P}(\rho) \text{ does not enable } \alpha$$

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- the user performing an output action is irrelevant; the only relevant aspect is the set of permissions activated when performing the action:

$$r\{\!|b^s\langle n\rangle.\mathbf{nil}|\!\}_\rho \approx t\{\!|b^s\langle n\rangle.\mathbf{nil}|\!\}_\rho$$

Finding the “Minimal” Schema

- Goal: to look for a ‘minimal’ schema to execute a given system A while mantaining its behaviour w.r.t. $(\mathcal{U}\,;\mathcal{P})$
- Algorithm:
  - fix a *metrics* (number of rôles in the schema, permissions associated to each rôle, etc.)
  - define the set $CONF_A = \{(\mathcal{U}';\mathcal{P}') \triangleright A : (\mathcal{U}';\mathcal{P}')$ is a RBAC schema$\}$ of configurations for A
  - partition $CONF_A$ w.r.t. $\approx$ and consider the equivalence class containing $(\mathcal{U}\,;\mathcal{P}) \triangleright A$
  - choose the minimal schema according to the chosen metrics

Refining Systems

- Goal: to add rôle activations/deactivations within a system in such a way that the resulting system can be executed under a given schema $(\mathcal{U}\,;\mathcal{P})$
- we want a rôle to be active only when needed
- the refining procedure replaces any input/output prefix α occurring in session $r\{\!|\cdots|\!\}_\rho$ with the sequence of prefixes **role** $\vec{R}.\alpha.$**yield** $\vec{R}$ where $\vec{R}$ is formed by rôles assigned to r, activable when having activated ρ and enabling the execution of α
- the refining procedure adapts the type system
- Improvement: we can give an algorithm to minimize the number of these actions added

Relocating Activities

- Goal: to transfer a process from one user to another without changing the overall system behaviour, in order to minimize the number of users in a system
- it is possible to infer axiomatically judgments of the form:

$$(\mathcal{U}\,;\mathcal{P})\ \triangleright\ r\{\!|P|\!\}_\rho\ \approx\ (\mathcal{U}\,;\mathcal{P})\ \triangleright\ s\{\!|P|\!\}_\rho$$

  This judgment says that the process P can be executed by r and s without affecting the overall system behaviour.

- Thus, the session $r\{\!|P|\!\}_\rho$ can be removed. If no other session of r is left in the system, then r is a useless user and is erased.

Conclusion

- We have defined a formal framework for reasoning about concurrent systems running under an RBAC schema;
- a number of papers deal with the specification and verification of RBAC schema;
- Future Works:
  - extend the framework to deal with more complex RBAC models;
  - prove that bisimilarity is complete for barbed congruence;

`http://www.dsi.uniroma1.it/~gorla/publications.htm`