

# Bridging Fault Test Method with Adaptive Power Management Awareness

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**Abstract**—A key design constraint of circuits used in handheld devices is the power consumption, mainly due to battery life limitations. Adaptive power management (APM) techniques aim to increase the battery life of such devices by adjusting the supply voltage and operating frequency, and thus the power consumption, according to the workload. Testing for resistive bridging defects in APM-enabled designs raises a number of challenges due to their complex analog behavior. Testing at more than one supply voltage setting can be employed to improve defect coverage in such systems, however, switching between several supply voltage settings has a detrimental impact on the overall cost of test. This paper proposes a multi-Vdd automatic test generation method which delivers 100% resistive bridging defect coverage and also a way of reducing the number of supply voltage settings required during test through test point insertion. The proposed techniques have been experimentally validated using a number of benchmark circuits.

**Index Terms**—Adaptive Power Management, Resistive Bridging Faults, Test Generation, Test Points

## I. INTRODUCTION

ENERGY-EFFICIENT design is becoming more important with technology scaling and with high performance requirements, especially for portable, battery-driven appliances. Several adaptive power management methods have been employed in a wide range of consumer electronics to optimize their power consumption. A popular adaptive power management technique is scaling the supply voltage and operating frequency according to the processing load [1], as implemented

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in several state-of-the-art processors [2] and [3]. Typically, a design with adaptive power management has a set of discrete supply voltage/frequency settings it can switch between depending on the current workload and power saving mode. Manufacturing test needs to ensure that such a design operates correctly over the entire set of supply voltage/frequency settings, while keeping the overall cost of test low.

Resistive bridges represent a major class of defects for deep submicron CMOS and have received increased attention. Research has investigated modeling [4], [5], [6], [7], [8], [9], [10], simulation [6], [9] and test generation [6], [11], [12], [13], [14] for resistive bridging faults (RBF). It has been shown in [8] that the fault coverage of a test set targeting resistive bridging faults can vary with the supply voltage used during test. This means that, depending on the operating Vdd setting, a given RBF may or may not affect the correct operation of the design. Consequently, to ensure high fault coverage for a design that needs to operate at a number of different Vdds, it may be necessary to perform testing at more than one Vdd to detect faults which manifest themselves only at particular Vdds. The first aim of this paper is to propose an automatic test generation method targeting multiple Vdd settings. The second aim of this work is to demonstrate a method of reducing the number of Vdd settings required during test without affecting the defect coverage.

The paper is organised as follows: Section II gives background information and summarizes the prior work on RBF testing. The motivation of multi-Vdd testing is discussed in Section III. In Section IV-A we present a deterministic test generation method targeting RBF at multiple Vdd settings and report the experimental validation results. A method to reduce the number of Vdd settings required during test by using test points is presented in Section V. Concluding remarks are given in Section VI.

## II. BACKGROUND AND PRIOR WORK

The main difficulty in RBF test generation arises from the fact that the bridging resistance is a continuous parameter which is not known in advance. A recent approach based on interval algebra [8], [9] allowed treating the whole continuum of bridge resistance values  $R_{sh}$  from  $0\Omega$  to  $\infty$  by handling a

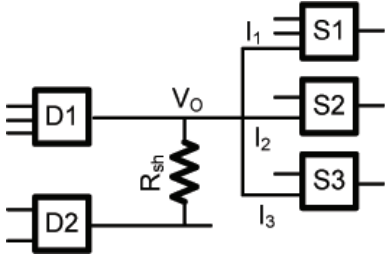


Fig. 1. Bridging fault example

finite number of discrete intervals. The key observation which enables this method is that a resistive bridge changes the voltages on the bridged lines from 0V (logic-0) or Vdd (logic-1) to some intermediate values, which will be different for different  $R_{sh}$  values. The logic behavior of the physical defect can be expressed in terms of the logic values perceived by the gate inputs driven by the bridged nets based on their specific input threshold voltage.

A typical bridging fault scenario is illustrated in Fig. 1. D1 and D2 are the gates driving the bridged nets, while S1, S2 and S3 are successor gates, i.e. gates having inputs driven by one of the bridged nets. The resistive bridge affects the logic behavior only when the two bridged nets are driven at opposite logic values. For example, let us consider the case when the output of D1 is driven high and the output of D2 is driven low. The dependence of the voltage level on the output of D1 ( $V_O$ ) on the equivalent resistance of the physical bridge is shown in Fig. 2. The deviation of  $V_O$  from the ideal voltage level (Vdd) is highest for small values of  $R_{sh}$  and decreases for larger values of  $R_{sh}$ . To translate this analog behavior into the digital domain, the input threshold voltage levels  $V_{th1}$ ,  $V_{th2}$  and  $V_{th3}$  of the successor gates S1, S2 and S3 have been added to the  $V_O$  plot. For each value of the bridging resistance  $R_{sh}$ , the logic values read by inputs  $I_1$ ,  $I_2$  and  $I_3$  can be determined by comparing  $V_O$  with the input threshold voltage of the corresponding input. These values are shown in the second part of Fig. 2. Crosses are used to mark the faulty logic values and ticks to mark the correct ones. It can be seen that, for bridges with  $R_{sh} > R_3$ , the logic behavior at the fault site is fault-free (all inputs read the correct value), while for bridges with  $R_{sh}$  between 0 and  $R_3$ , one or more of the successor inputs are reading a faulty logic value. The  $R_{sh}$  value corresponding to  $R_3$  is normally referred to as ‘‘critical resistance’’ as it represents the crossing point between faulty and correct logic behavior. Methods for determining the critical resistance have been presented in several publications [6], [9].

A number of bridging resistance intervals can be identified based on the corresponding logic behavior. For example, bridges with  $R_{sh} \in [0, R_1]$  exhibit the same faulty behavior in the digital domain (all successor inputs read the faulty logic value), similarly, for bridges with  $R_{sh} \in [R_1, R_2]$ , successor gates S2 and S3 read the faulty value, while S1 reads the

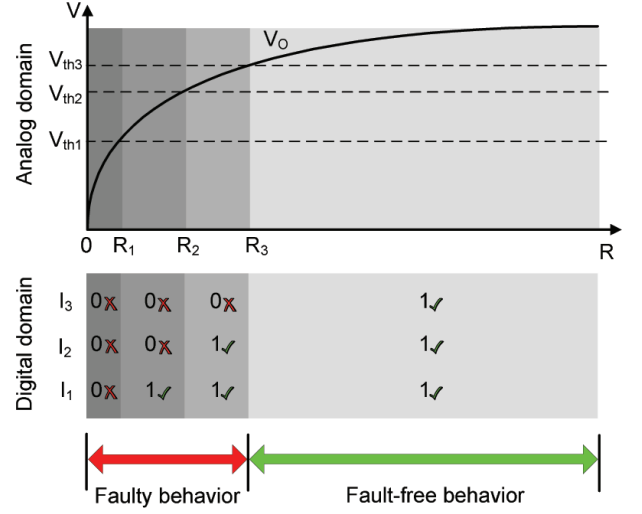


Fig. 2. Bridging fault behavior

correct value, and finally, for bridges with  $R_{sh} \in [R_2, R_3]$  only S3 reads a faulty value while the other two successor gates read the correct logic value. Consequently, each interval  $[R_i, R_{i+1}]$  corresponds to a distinct logic behavior occurring at the bridging fault site. The logic behavior at the fault site can be captured using a data structure which will be further referred to as logic state configuration (LSC). An LSC consists of the logic values at the inputs of the driving gates and the logic values detected by the inputs of the successor gates. LSCs capturing faulty logic behavior can be looked at as logic fault models. An LSC is said to be non-redundant, if there is at least one test pattern which can justify the net values specified by the LSC and also make the faulty behavior observable at the primary outputs. An LSC for which no such test pattern exists is referred to as a redundant LSC. This means that redundant LSCs cannot occur during the functional operation of the circuit, and consequently only non-redundant LSCs have to be targeted during test generation in order to ensure correct operation of the circuit. The union of the resistance intervals corresponding to non-redundant LSCs forms the Global Analogue Detectability Interval (G-ADI) [9]. Basically, G-ADI represents the entire range of detectable physical defects. Given a test set  $TS$ , the Covered Analogue Detectability Interval (C-ADI) represents the range of physical defects detected by  $TS$ . The C-ADI for a bridging defect is the union of one or more disjoint resistance intervals, the union of intervals corresponding to non-redundant LSCs [4], [8], [9], [13]. Throughout this paper, the quality of a test set is estimated by measuring how much of the G-ADI has been covered by the C-ADI. When the C-ADI of test set  $TS$  is identical to the G-ADI of fault  $f$ ,  $TS$  is said to achieve full fault coverage for  $f$ .

Several test generation methods for resistive bridging faults have been proposed [6], [11], [14] and more recently [12], [13].

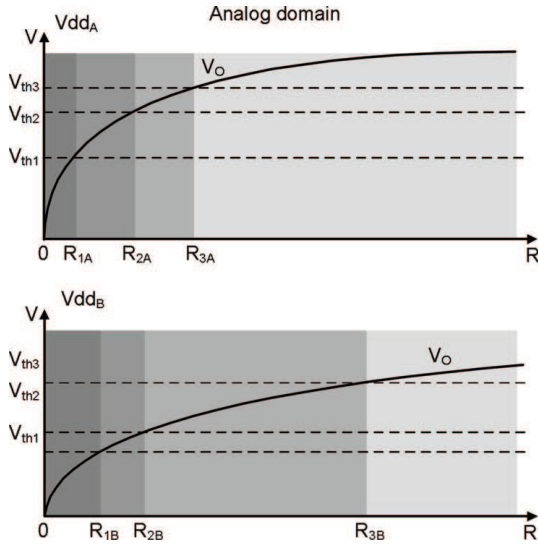


Fig. 3. Effect of supply voltage on bridging fault behavior: Analog domain

The method presented in [11] is to guarantee the application of all possible values at the bridge site without detailed electrical analysis. In [12], the effect of a bridge on a node with fanout is modeled as a multiple line stuck-at fault. The study in [6], identifies only the largest resistance interval and determines the corresponding test pattern. In contrast to [6], the sectioning approach from [14] considers all the sections (resistance intervals)  $[R_i, R_{i+1}]$ . For each section, the corresponding LSC (and associated faulty logical behavior) is identified. This avoids the need for dealing with the resistance intervals and improves the test quality compared with [6], but the number of considered faults grows.

In [13], the authors combined the advantages of the interval based [6] and the sectioning approach [14] into a more efficient test generation procedure by targeting the section with the highest boundaries first. Interval based fault simulation is then used to identify all other sections covered by the test pattern. It should be noted that all test generation methods described above [6], [11], [12], [13], [14] are intended for a fixed supply voltage setting, i.e. all tests are applied at the same supply voltage. In the next section we explain why it is sometimes necessary to use more than one Vdd setting during test to ensure full bridging defect coverage for adaptive power management enabled designs.

### III. MOTIVATION OF MULTI-VDD TESTING

This section provides an analysis of the effect of varying supply voltage on bridging fault behavior, which provides the starting point for the work presented in this paper. Figures 3, 4 and 5 show the relation between the voltage on the output of gate D1 (Fig. 1) and the bridging resistance for two different supply voltages  $Vdd_A$  and  $Vdd_B$ . The diagrams in Fig. 4 show how the analog behavior at the fault site translates

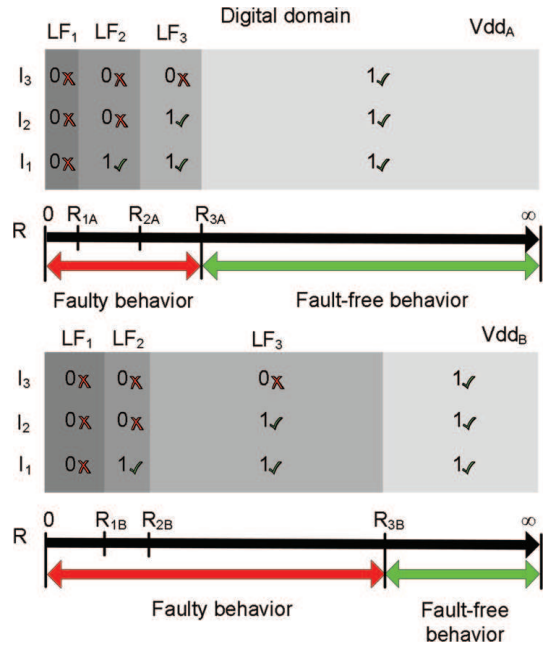


Fig. 4. Effect of supply voltage on bridging fault behavior: Digital domain

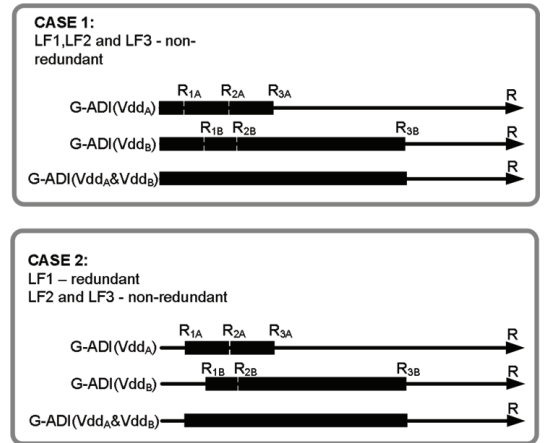


Fig. 5. Effect of supply voltage on bridging fault behavior: Observable bridging resistance ranges

into the digital domain. In this example, three distinct logic faults LF1, LF2 and LF3 could be identified for each Vdd setting. However, because the voltage level on the output of D1 does not scale linearly with the input threshold voltages of S1, S2 and S3 when changing the supply voltage (this has been validated through SPICE simulations), the resistance intervals corresponding to LF1, LF2 and LF3 differ from one supply voltage setting to another. This means that a test pattern targeting a particular logic fault will detect different ranges of physical defects when applied at different supply voltage settings. For example, at  $Vdd_A$ , a test pattern targeting LF3 will detect bridges with  $R_{sh} \in [R_{2A}, R_{3A}]$ , while at  $Vdd_B$  it will detect a much wider range of physical

bridges ( $R_{sh} \in [R_{2B}, R_{3B}]$ ). Analysing this from a different perspective, a bridge with  $R_{sh} = R_{3B}$  will cause a logic fault at  $Vdd_B$  but not at  $Vdd_A$ . To demonstrate the need for using multiple Vdd settings during test we use the following two scenarios. In Case 1 (Fig. 5) all three logic faults LF1, LF2 and LF3 are non-redundant. Fig. 5 shows the ranges of bridging resistance corresponding to faulty logic behavior for the two Vdd settings (basically the G-ADI sets corresponding to the two Vdd settings). Previous work on test generation for bridging faults [13] has used the concept of G-ADI assuming a fixed Vdd scenario. We have extended the concept of G-ADI to capture the dependence of the bridging fault behavior on the supply voltage by defining the multi-Vdd G-ADI as the union of Vdd specific G-ADIs for a given design.

$$G-ADI = \bigcup G-ADI(Vdd_i)$$

The overall G-ADI consists of the union of the two Vdd specific G-ADI sets. It can be seen that  $G-ADI(Vdd_A)$  represents about 45% of the overall G-ADI while  $G-ADI(Vdd_B)$  fully covers the overall G-ADI. This means that a test set detecting LF1, LF2 and LF3 will achieve full bridging defect coverage when applied at  $Vdd_B$ . In Case 2 from Fig. 5, only LF2 and LF3 are non-redundant, which means that there is no test pattern which can detect LF1. In this case,  $G-ADI(Vdd_A)$  represents about 30% of the overall G-ADI while  $G-ADI(Vdd_B)$  represents about 90% of the overall G-ADI. This means that full bridging fault coverage cannot be achieved using a single Vdd setting.

From the previous analysis it can be concluded that to achieve full G-ADI coverage in a variable Vdd system, it may be necessary to apply tests at several Vdd settings. Instead of repeating the same test at all Vdd settings, which would lead to long testing times and consequently would increase the manufacturing cost, it would be desirable to be able to determine for each Vdd settings only the test patterns which effectively contribute to the overall defect coverage. A methodology for achieving this is presented in Section IV-A.

Although in this work we are considering equal probabilities for defects with different resistance values, the real life occurrence distribution of bridge resistance may make some resistance values unlikely to be found on a fabricated circuit. The impact of a real life distribution on multi-Vdd testing of RBFs is addressed in Fig. 6. It shows the distribution of defects which cannot be detected at 0.8V Vdd (which would be a preferred Vdd for a 1.2V process according to [4], [8]). The distribution in Fig. 6 is based on seven of the medium and large size ISCAS benchmarks. The random spread of these defects across the resistance range suggests that to ensure high defect coverage it will be necessary to test at more than one Vdd, even if the defect occurrence distribution corresponding to a particular manufacturing process is concentrated around a certain resistance range.

Switching between different Vdd settings during test is not a trivial task, and therefore a large number of Vdd settings required during test can have a detrimental effect on the overall

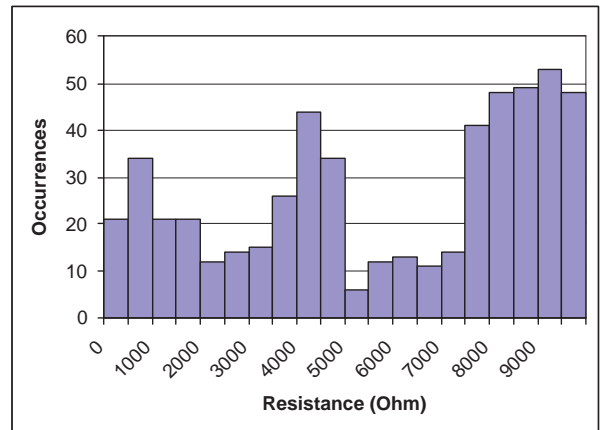


Fig. 6. The distribution of resistance values that cannot be detected at 0.8V Vdd

cost of test. Consequently it would be desirable to keep the number of Vdd settings required during test to a minimum. By analysing the scenario described in Case 2 (Fig. 5), it can be seen that full bridging defect coverage could be achieved using a single Vdd setting ( $Vdd_B$ ), if the logic fault corresponding to the resistance interval  $[R_{1A}, R_{1B}]$ , LF1 in this case, would become detectable, i.e. non-redundant. Based on this observation, we propose a test point insertion methodology which aims to increase the defect coverage at specific Vdd settings by exposing resistance intervals corresponding to redundant logic faults, which consequently reduces the total number of Vdd settings during test. The proposed test point insertion methodology is presented in Section V.

#### IV. PROPOSED MULTI-VDD TEST GENERATION

The proposed multi-Vdd test generation flow is shown in Fig. 7. The multi-Vdd test generation flow starts from the placed and routed design to generate a realistic list of bridges and computes a number of Vdd-specific test sets which provide 100% bridging defect coverage.

##### A. Methodology

The proposed test generation flow starts by generating the bridge list by coupling capacitance extraction on the placed and routed design, where each pair of nets that are capacitively coupled are considered a likely bridge. The multi-Vdd test generation procedure, detailed in Fig. 8, generates Vdd-specific test sets for the given bridge list and synthesised netlist. An optional post processing step, explained later in this section, can be performed to further reduce the overall number of test patterns.

The test generation algorithm starts by identifying for each bridge the resistance intervals corresponding to faulty logic behaviour (at least one of the inputs fed by the bridged nets

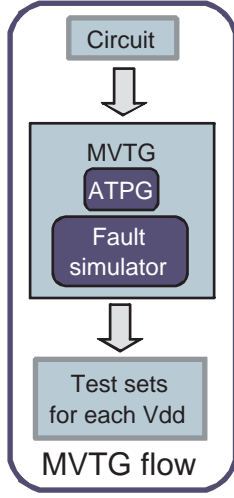


Fig. 7. Flow for the test generation algorithm

reads an incorrect logic value) for each Vdd setting (lines 1-6). This is achieved by determining the voltage levels on the bridged nets through SPICE simulations and comparing them with the threshold voltages of the inputs fed by them. One simulation is done for each possible input assignment to the gates that drive the bridged nets. To speed-up the process, the SPICE simulation results are stored into a database, such that for subsequent bridges with the same type of driving gates, the time-consuming SPICE simulations are replaced with fast database look-ups. The logic behaviour corresponding to each resistance interval is captured using logic state configuration (LSC) data structures, as explained in Sections II and III. An LSC holds the Boolean values at the inputs of the gates driving the bridge and the Boolean values seen by the inputs fed by the bridged nets. The tuple consisting of an LSC, its corresponding Vdd setting  $v$  and resistance interval  $ri$  will be further referred to as a Logic Fault Set (LFS), with the following semantic: a test pattern detecting the faulty behaviour described by  $lsc$  covers the resistance interval  $ri$  when applied at Vdd setting  $v$ .

The algorithm continues by computing for every bridge  $b$  the test patterns for resistance intervals that are not yet covered (lines 9-17). All generated test patterns are included in a set of candidate test-patterns for  $b$  by adding the corresponding LFS to  $c\_LFS(b)$ . The resulting set of test patterns comprises all possible ways of covering the detectable resistance intervals corresponding to the bridge  $b$ . This test set is minimised using an integer linear programming formulation of a minimum set covering problem (select\_LFSs on line 18). The result  $TS\_LFS$  is the minimum set of test patterns that covers all detectable bridge resistance (the scope of G-ADI). The selected test set ( $TS\_LFS$ ) is fault simulated using all remaining bridges and the resistance intervals corresponding to detected LFSs are marked as covered, so they are not targeted anymore in subsequent iterations (lines 20-25). For fault simulation we

**Input:** netlist, Vdd settings  $V = \{v\}$ , Bridges  $B = \{b\}$

**Output:** Multi-Vdd tests with 100% defect coverage

```

1: for all Bridge  $b \in B$  do
2:   for all  $v \in V$  do
3:     compute all  $(lsc, ri)$  for  $(b, v)$ 
4:     //  $ri$  abbreviates Resistance Interval
5:      $LFS(b) := LFS(b) \cup \{(lsc, v, ri)\}$ 
6:   end for
7: end for
8: while  $(B \neq \emptyset)$  do
9:   Get a bridge  $b$  from  $B$ 
10:  for all  $lfs \in LFS(b)$  do
11:    if  $(lfs$  not covered) then
12:       $ATPG(b, LSC(lfs))$ 
13:      if  $(ATPG$  found a test pattern  $tp$ ) then
14:         $TP(lfs) := tp$ 
15:        mark  $lfs$  as covered in  $c\_LFS(b)$ 
16:      end if
17:    end if
18:  end for
19:   $TS\_LFS := select\_LFSs(c\_LFS(b))$ 
20:   $B := B \setminus \{b\}$ 
21:  for all LFS  $\overline{lfs} \in TS\_LFS$  do
22:     $v := V(\overline{lfs})$ 
23:     $tp := TP(\overline{lfs})$ 
24:     $TestSet(v) := TestSet(v) \cup \{tp\}$ 
25:    fault simulate on  $\overline{b} \in B$  and mark all detected LFS
26:    as covered in  $c\_LFS(\overline{b})$ 
27:  end for
28: end while
  
```

Fig. 8. Multi-Vdd Test Generation (MVTG)

have used a method similar to the one employed in [9].

An optional post-processing step can be employed to further reduce the size of the multi-Vdd test set size obtained as described earlier. Initially, each test pattern is fault-simulated using the entire bridge list to compute its individual defect coverage. The test set is then sorted in descending order of the test pattern defect coverage. The test patterns in the ordered test set are fault simulated again, this time dropping resistance intervals as soon as they are detected. If for a particular test pattern ( $tp$ ) no resistance interval was dropped,  $tp$  is removed from the test set as it does not contribute to the overall defect coverage since all resistance intervals targeted by  $tp$  had been already detected by the previous test patterns in the ordered test set.

## B. Experimental results

The proposed multi-Vdd test generation method has been implemented as a tool chain (Fig. 7) consisting of an automatic test generator and a fault simulator and has been validated experimentally using a number of ISCAS 85 and ISCAS 89

TABLE I  
MULTI-VDD TEST GENERATION RESULTS

| Design | RBF # | Vdd 0.8V | Vdd 1.0V | Vdd 1.2V | Sum #tp | CPU time | ATPG % | Sim/RBF |
|--------|-------|----------|----------|----------|---------|----------|--------|---------|
|        |       | #tp TS 1 | #tp TS 2 | #tp TS 3 |         |          |        |         |
| c1355  | 80    | 39       |          |          | 39      | 21       | 71     | 557     |
| c1908  | 98    | 57       |          |          | 57      | 13       | 58     | 296     |
| c2670  | 104   | 67       |          |          | 67      | 27       | 41     | 269     |
| c3540  | 363   | 184      | 6        | 1        | 191     | 340      | 62     | 568     |
| c7552  | 577   | 281      |          | 1        | 282     | 1049     | 66     | 552     |
| s838   | 34    | 26       | 2        |          | 28      | 6        | 54     | 243     |
| s1488  | 435   | 144      | 2        |          | 146     | 193      | 10     | 265     |
| s5378  | 305   | 214      |          |          | 214     | 308      | 32     | 914     |
| s9234  | 223   | 132      | 2        |          | 134     | 130      | 43     | 1068    |
| s13207 | 358   | 192      | 5        | 1        | 198     | 2454     | 53     | 1291    |
| s15850 | 943   | 324      | 4        | 5        | 333     | 11835    | 42     | 417     |
| s35932 | 1170  | 547      | 50       | 63       | 660     | 11233    | 53     | 263     |

TABLE II  
MULTI-VDD TEST-SETS DEFECT COVERAGE

| Design | TS 1            | TS 1&2          | TS 1&3          | TS 1&2&3        |
|--------|-----------------|-----------------|-----------------|-----------------|
|        | defect coverage | defect coverage | defect coverage | defect coverage |
| c1355  | 100.0           |                 |                 |                 |
| c1908  | 100.0           |                 |                 |                 |
| c2670  | 100.0           |                 |                 |                 |
| c3540  | 99.20           | 99.96           |                 | 100.0           |
| c7552  | 99.95           |                 | 100.0           |                 |
| s838   | 95.04           | 100.0           |                 |                 |
| s1488  | 99.98           | 100.0           |                 |                 |
| s5378  | 100.0           |                 |                 |                 |
| s9234  | 99.87           | 100.0           |                 |                 |
| s13207 | 99.57           | 99.92           |                 | 100.0           |
| s15850 | 99.84           | 99.94           |                 | 100.0           |
| s35932 | 93.95           | 98.48           |                 | 100.0           |

benchmark circuits. The sequential circuits were treated as combinational by assuming full scan-chains and only non-feedback bridges have been targeted.

The benchmark circuits were synthesised using an ST cell library of  $0.12\mu\text{m}$ . Three Vdd settings were used during the experiment,  $0.8\text{V}$ ,  $1.0\text{V}$  and  $1.2\text{V}$ . In Table I and Table III we show the test-set sizes generated and the CPU time for the algorithm in Fig. 8 and the optional test set post-processing step respectively. Table I shows the results of running the Multi-Vdd Test Generation program (Fig. 8). The left-most column shows the benchmark circuits, where an initial ‘‘c’’ means that the circuit is combinational and an ‘‘s’’ means that the circuit is sequential. The second column from the left shows for each design, how many non-feedback bridges have been identified from the circuit layout. The ‘‘extractRC’’ tool from Cadence was used to get the pairs of nets that are capacitively coupled. These pairs of nets are the most likely bridge locations. Feedback bridges were identified and removed. The next three main columns, marked with ‘‘Vdd 0.8V’’, ‘‘Vdd 1.0V’’ and ‘‘Vdd 1.2V’’, show the test pattern count in the corresponding test-set - TS 1, TS 2 and TS 3 respectively. The sixth column shows the total number of test-patterns necessary to achieve 100% defect coverage. The column that is marked with ‘‘CPU time’’ shows the CPU time required to achieve these results, in seconds. Our implementation uses a SAT solver based ATPG engine [15]. The second column from the right shows the fraction of time spent inside the ATPG engine (line 11 of Fig. 8). We believe this fraction can be significantly reduced if access to a more efficient commercial ATPG engine is available. The right-most column gives the average number of simulations per bridge that would have been required if we did not have a pre-compiled database of bridge simulation data.

In Table II we have evaluated the test-sets that are

defined in Table I. Column two until five show the incremental defect coverage of applying the test-sets in order. This defect coverage is defined as follows:  $DC = \sum_B \text{detected resistance} / \sum_B \text{detectable resistance}$ , where  $\sum_B$  signifies the sum over all the RBFs. Column two is the defect coverage of only applying TS 1 (for  $0.8\text{V}$  Vdd). Column three is the defect coverage achieved by applying TS 1 at  $0.8\text{V}$  and TS 2 at  $1.0\text{V}$ . In the same way, column four is the defect coverage of TS 1 and TS 3 (where TS 3 is applied at  $1.2\text{V}$ ). The last column shows the defect coverage achieved by applying all test-sets at their respective Vdd settings.

As can be seen from Table I, for some circuits, 100% defect coverage can be achieved using a single Vdd during test. However, for other circuits, such as s35932, achieving full defect coverage requires testing at more than one Vdd setting.

Table III shows the results of applying the optional post processing step to the test-sets in Table I. The columns that are marked with # show the final number of test patterns in the test set for the respective Vdd settings. The complimentary %-columns give the relative reduction in test patterns in the respective test sets. So for circuit s15850, the outcome of the post-processing was 235 test patterns for Vdd  $0.8\text{V}$ , which is 27% less than before the post-processing (see Table I, column 3). In the fifth main column is the relative reduction in the total number of test patterns. The last column shows the relative difference in CPU time. So again, for circuit s15850, it took 4.58 times longer to include the post-processing compared to column 7 of Table I. Table III demonstrates that it is possible to achieve up to 27% reduction in test set size at the expense of increased CPU time.

An additional experiment was made using Synopsys TetraMAX and Multi-Vdd Test Generation (Fig. 8) as a combined test generation flow. First, a test-set targeting bridging faults is generated with TetraMAX, using the same bridge list as in the

TABLE III  
TEST-SET SIZE REDUCTIONS USING THE POST-PROCESSING STEP ON THE TEST SETS FROM TABLE I

| Design | 0.8V |    | 1.0V |    | 1.2V |    | Tot. | CPU  |
|--------|------|----|------|----|------|----|------|------|
|        | #    | %  | #    | %  | #    | %  | %    | time |
| c1355  | 32   | 18 |      |    |      |    | 18   | 95   |
| c1908  | 47   | 18 |      |    |      |    | 18   | 238  |
| c2670  | 57   | 15 |      |    |      |    | 15   | 393  |
| c3540  | 151  | 18 | 6    | 0  | 1    | 0  | 17   | 419  |
| c7552  | 229  | 19 |      |    | 1    | 0  | 18   | 528  |
| s838   | 22   | 15 | 2    | 0  |      |    | 14   | 67   |
| s1488  | 121  | 16 | 2    | 0  |      |    | 16   | 608  |
| s5378  | 175  | 18 |      |    |      |    | 18   | 585  |
| s9234  | 109  | 17 | 2    | 0  |      |    | 17   | 390  |
| s13207 | 158  | 18 | 3    | 40 | 1    | 0  | 18   | 342  |
| s15850 | 235  | 27 | 4    | 0  | 3    | 40 | 27   | 458  |
| s35932 | 459  | 16 | 43   | 14 | 51   | 19 | 16   | 900  |

TABLE IV  
RESULTS OF USING TETRAMAX AND MVTG AS A COMBINED TEST GENERATION FLOW

| Design | TMAX |     | MVTG top-up |          |          | Tot. | CPU   |
|--------|------|-----|-------------|----------|----------|------|-------|
|        | DC   | #tp | 0.8V #tp    | 1.0V #tp | 1.2V #tp |      |       |
| c1355  | 83   | 33  | 32          |          |          | 65   | 18    |
| c1908  | 98   | 42  | 27          |          |          | 69   | 11    |
| c2670  | 90   | 27  | 50          |          |          | 77   | 36    |
| c3540  | 96   | 72  | 126         | 6        | 1        | 205  | 239   |
| c7552  | 95   | 44  | 198         |          | 1        | 243  | 789   |
| s838   | 88   | 17  | 17          | 2        |          | 36   | 2     |
| s1488  | 96   | 82  | 82          | 2        |          | 166  | 123   |
| s5378  | 95   | 60  | 123         |          |          | 183  | 214   |
| s9234  | 89   | 48  | 92          | 2        |          | 142  | 105   |
| s13207 | 95   | 60  | 89          | 5        | 1        | 155  | 1625  |
| s15850 | 98   | 56  | 144         | 4        | 5        | 209  | 1954  |
| s35932 | 96   | 33  | 89          | 36       | 66       | 224  | 11511 |

experiment of Table I. Then the TetraMAX test-set was fault simulated at Vdd 0.8V (since higher resistive bridging fault coverage is achieved at a lower Vdd). The defect coverage achieved and the number of test patterns in the TetraMAX test-set is given in the second main column of Table IV. Subsequently, MVTG is used on the bridges that were not fully covered by the TetraMAX test-set, to supply the remaining defect coverage up to 100%. The sizes of the test sets generated by the MVTG top-up run are given in the third column for each Vdd setting. In the fourth column of Table IV, marked "Tot." we show the total test pattern count. The last column is the CPU time (in seconds) for simulating the TetraMAX test-set and running MVTG to top-up the test-set.

Please note in Table IV, that Synopsys TetraMAX generates test-sets that may yield defect coverage as low as 83% at Vdd

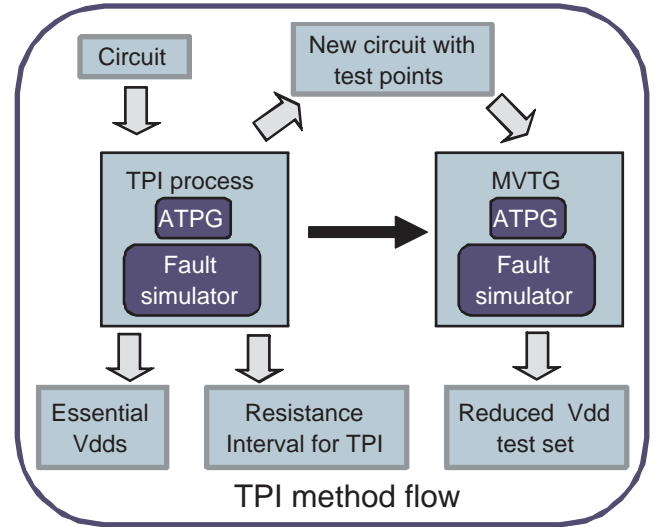


Fig. 9. Flows for the proposed TPI scheme

= 0.8V. TetraMAX uses a heuristic that combines the victim-aggressor bridge fault model with a scheme to drive one of the bridged nodes with maximum strength and the other node with minimum strength. This way, the likelihood of detecting a bridge defect is maximised, even though TetraMAX does not take the defect resistance value into account.

## V. REDUCING THE NUMBER OF TEST VDDs

The flow for reducing the number of Vdd settings during test is shown in Fig. 9, it consists of two phases: test point identification and insertion, during which phase the method identifies the Vdd settings which can be eliminated during test, and test generation on the modified circuit.

### A. Methodology

As shown in Section IV-A, different test sets need to be applied at several Vdd settings to ensure 100% defect coverage for multi-Vdd designs. Switching between supply voltage settings during test is not a trivial task and increases the cost of test, mainly due to the switching time overheads. Consequently, it is desirable to keep the number of the test voltage settings to a minimum. Previously, test point insertion (TPI) has been used for increasing the defect coverage [16] and test compaction [17]. In this section, we show how TPI can be used to reduce the number of different Vdd settings required during test without affecting the defect coverage. The proposed flow is shown in Fig. 9. For this purpose, we introduce the concept of "essential" test Vdd. A test Vdd is said to be essential if there is at least one bridge for which the highest resistance value causing faulty behavior can be detected at this Vdd. This means that any of the resistance intervals targeted at non-essential test Vdds by the test generation algorithm presented in the previous section can be detected at one of

- 1: Compute set of Essential Test Vdds ( $V_{ess}$ )
- 2: Compute set of NRINEV
- 3: **for all**  $NRINEV$  **do**
- 4: LSC Selection( $NRINEV, V_{ess}$ )
- 5: Determine a preliminary set of test points at the defect site boundary for detecting the selected LSCs
- 6: **end for**
- 7: Minimize set of observation points
- 8: Control Point Minimization ()
- 9: Generate Essential Vdd Test Sets for the modified netlist
- 10: **return** ( $netlist, Test Sets$ )

Fig. 10. Test Point Insertion

the essential test Vdds, subject to suitable controllability and observability at the bridge site. Test point insertion can be used to provide the controllability and observability required at the bridge site. Fig. 10 outlines the method for achieving this goal. The key steps of this method are further detailed in Fig. 12, 13, 14 and 15.

The algorithm starts by computing the set of essential test Vdds for the given voltage settings and bridge list. To achieve this, for each bridge  $B$ , the algorithm determines the highest detectable bridge resistance value across all available Vdd settings and marks the Vdd setting corresponding to the highest resistance value as essential Vdd. In line 2, the algorithm determines for each bridge the set of resistance intervals which cause faulty behaviour at a non-essential Vdd, but are fully or partially undetectable at any of the essential Vdds due to lack of suitable controllability or observability. These resistance intervals are referred to as Non Redundant Interval at Non-Essential Voltage (NRINEV). Next, in lines 3 to 6, for each NRINEV, the algorithm determines a set of test points needed to make the resistance interval detectable at an essential Vdd setting. For this purpose, a set of LSC which fully cover the NRINEV interval is identified. Since in most cases, more than one set of LSCs can be used to cover the same NRINEV, the algorithm selects the LSC set which is likely to require the least number of test points to become detectable. The LSC selection algorithm used for this purpose is detailed in the following section. Once all NRINEV intervals have been covered, in lines 7 and 8 an attempt is made to reduce the number of required test points by identifying test points which can be shared among two or more selected LSCs. The algorithm then inserts the resulting set of test points into the original netlist and invokes MVTG (Fig. 8) to generate the test sets corresponding to the set of essential Vdds.

1) *LSC selection*: LSC selection aims to determine a set of LSC covering a given NRINEV which is likely to require the least number of test points. The algorithm, illustrated in Fig. 12, uses signal probabilities to quantify the effort required to control the logic values required by a LSC on the corresponding nets. In our experiments, signal probabilities

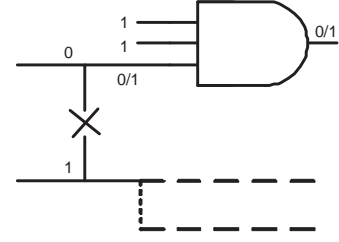


Fig. 11. Observability calculation

were determined by simulating 5000 pseudorandom patterns, however other analytical methods for estimating signal probability could be used for this purpose just as well. The algorithm continues by identifying all LSCs which expose resistance intervals fully or partially overlapping with the target NRINEV interval. A probabilistic estimate of the controllability and observability (PECO) is computed for each candidate LSC (steps 3 to 5) as follows:

$$PECO(LSC) = C(LSC) \cdot O(LSC) \quad (1)$$

where  $C(LSC)$  is a probabilistic measure of the LSC controllability and  $O(LSC)$  is a probabilistic measure of the observability of the defect at the outputs of the gates fed by the bridge.

$$C(LSC) = \prod_{i=1}^n (Prob(i)) \quad (2)$$

where  $n$  is the cumulated number of inputs of the two gates driving the bridged nets and  $Prob(i)$  is the probability of logic value required by the LSC on input  $i$ .

$$O(LSC) = \sum_{i=1}^m (f(X)) \quad (3)$$

where  $m$  is the number of gates fed by the bridged nets which propagate the faulty value to their outputs and  $f(X)$  is the probability that the fault effect is propagated through gate  $X$ , computed as follows:

$$f(X) = \frac{\sum_{j=1}^k \prod_{i=1}^l SP_{i,j}}{2^l} \quad (4)$$

where  $k$  is the number of input combinations which propagate the fault effect to the output of successor gate  $X$ ,  $l$  is the number of inputs of gate  $X$  which are not fed by the bridge, and  $SP_{i,j}$  is the probability of having the value corresponding to input combination  $j$  on input  $i$ . For example, for a 3-input AND gate fed by the bridge (as shown in Fig. 11) there is one input configuration which will propagate the fault (0/1) to its output out of the 4 possible combinations on the two inputs which are not fed by the bridge. Assuming the "1" probabilities of the inputs which are not driven by the bridge to be 0.4 and 0.7 respectively, the probability of this gate propagating



**Input:** NRINEV interval

Essential Vdd settings  $V_{ess}$

**Output:** Set of LSCs covering NRINEV with minimum number of required test points

- 1: Compute signal probabilities on all nets
- 2: Generate a list of LSC candidates sets which cover partially or completely the NRINEV at  $V_{ess}$
- 3: **for all** LSC candidates **do**
- 4:   Compute PECO(LSC)
- 5: **end for**
- 6: Determine the set of LSC covering NRINEV with maximum overall PECO
- 7: **return** LSC selection

Fig. 12. LSC Selection

the fault to its output is  $\frac{0.4+0.7}{4} = 0.07$ . In this way  $O(LSC)$  provides a probabilistic estimate to help compare various LSCs and favour the one which is likely to require lesser number of observation points.

PECO(LSC) is then used as weight in a set covering linear programming formulation to determine the LSC set covering NRINEV which is likely to require the fewest number of test points.

At this point, the selected LSCs can be made controllable and observable by inserting appropriate test points at the defect site boundary.

2) *Preliminary test point insertion at the defect site boundary:* The method proposed for determining the preliminary set of test points at the defect site boundary for a given LSC is shown in Fig. 13. The algorithm starts by checking whether the driving gates' input assignments required by the LSC can be satisfied. If the required input assignments can be satisfied, it means there is at least one test pattern which activates the fault. Otherwise the algorithm attempts to determine a set of control points necessary for activating the fault (lines 2-15). This is achieved by using incremental bit-flipping on the driving gates' input assignments until a satisfiable combination is found. The input nets corresponding to the bit-flips in the LSC represent control point candidates and are added to the Exclusive Control Point Candidate list (ECL). At this point (step 17), the algorithm attempts to generate a test pattern which detects LSC and returns on successful generation of a test pattern. If a test pattern detecting the LSC could not be found, it means that although the fault can be activated, it is not observable at the primary outputs. At this point, the following two scenarios are possible: the faulty behavior can be observed at the output of at least one of the successor gates, or, the faulty behavior does not propagate through any of the successor gates. In order to differentiate between these two issues, a stimulus is generated for fault activation. This stimulus is applied to the circuit and all the successor gates are checked to see if the faulty behavior is observable at the

output of any of these gates. If the fault is observable at the output of these gates, then the algorithm structurally traverses the circuit and marks all the nets that observes the faulty behavior as potential observation point candidates (step 22). If the fault effect is not observable at the output of any of the successor gates, the algorithm uses the logic values on all the nets, set by the stimulus generated in step 20 of the algorithm, and identifies the successor gate which observes the faulty value and requires the least number of control points in order to propagate it to its output. The nets corresponding to these control points are then added to ECL. In lines 28 to 34 the algorithm repeats steps 17 to 23 to mark all the nets that observe the faulty values for later observation point minimization, if a test pattern cannot detect the defect even after inserting control points for observability.

3) *Test points minimization:* The TPI algorithm (Fig. 10) minimizes the number of observation points, after processing all the NRINEV intervals. The optimum set of observation points will be the minimum set cover of the nets marked as observation point candidates in lines 22 and 33 of Fig. 13. This is similar to the method proposed in [18].

The TPI algorithm calls control point minimization algorithm in step 8 of Fig. 10, to reduce the number of control points in the modified circuit. This is achieved by finding pairs of control point candidate nets which can be replaced by a single control point while still achieving the required controllability. The algorithm (shown in Fig. 14) starts by determining the fan-in cone (FIC) sets for each net added to the ECL set in lines 9 and 26 of Fig. 13.  $FIC(ec)$  consists of all nets in the fan-in logic cone of  $ec$ , starting from the primary inputs. Basically,  $FIC(ec)$  contains all nets which may affect the logic value on  $ec$ . Next, the algorithm finds the Common Nets (CN) for the FIC of all possible pairs of nets in ECL, i.e.,  $CN(ec_i, ec_j)$  holds the nets which appear in both  $FIC(ec_i)$  and  $FIC(ec_j)$ . For every set of common nets  $CN(ec_i, ec_j)$ , the algorithm attempts to determine a list of valid candidates (VC) shown in line 8, where every valid candidate is able to provide the required controllability on  $(ec_i$  and  $ec_j)$ , thus reducing two control points to one. These valid candidates are generated by algorithm shown in Fig. 15 (Find Valid CP Candidates) for every pair of control points in ECL. The algorithm then determines the minimum set of control points as a minimum set cover for all VC sets. The resulting set of control points are then inserted in the netlist.

The algorithm shown in Fig. 15 starts by creating a copy of the netlist without any control points, but with the optimized observation points at their respective locations. For every pair of control point candidates  $(ec_A$  and  $ec_B)$  the algorithm inserts all control points necessary to detect LSC(A) (using information stored in ECL), with the exception of  $ec_A$  and  $ec_B$ , where LSC(A) is the LSC corresponding to  $ec_A$ . It then tries all the common nets  $CN(ec_A, ec_B)$ , one-by-one and attempts to generate a stimulus using both types of control

**Input:** LSC Candidate

```

Bridge  $b$ 
1: for all Gates driving the bridge do
2:   if LSC input assignment not satisfiable then
3:     CPCCount = 1;
4:     SATISFIED = FALSE;
5:     while NOT SATISFIED do
6:       for all LSCIA = LSC input assignment with CP-
         Count bit-flips do
7:         if LSCIA is satisfiable then
8:           SATISFIED = TRUE;
9:           add nets corresponding to bit-flips in LSCIA
             to ECL
10:          BREAK;
11:         end if
12:       end for
13:       CPCCount = CPCCount + 1
14:     end while
15:   end if
16: end for
17: if LSC non-redundant then
18:   return (success)
19: end if
20: Generate a stimulus to activate the fault
21: if Fault is observable at the output of the gates fed by the
     bridge then
22:   Mark all the nets which observe the fault effect as OP
     candidates
23: else
24:   Use the logic values set by the stimulus at the inputs of
     the gate
25:   Identify a gate, from all the gates which see a fault, that
     require min. no. of CPs to propagate the fault
26:   add control point candidates to ECL
27: end if
28: if LSC non-redundant then
29:   return (success)
30: end if
31: Generate a stimulus to activate the fault
32: if Fault is observable at the output of the gates fed by the
     bridge then
33:   Mark all the nets which observe the fault effect as OP
     candidates
34: end if

```

Fig. 13. Preliminary test point identification at the defect site boundary

```

1: for all NRINEV do
2:   for all  $ec \in ECL$  do
3:     Compute FIC( $ec$ )
4:   end for
5: end for
6: for all pair ( $ec_i, ec_j$ ) where  $ec_i, ec_j \in ECL$  do
7:    $CN(ec_i, ec_j) = FIC(ec_i) \cap FIC(ec_j)$ 
8:    $VC(ec_i, ec_j) = \text{Find Valid CP Candidates } (CN(ec_i, ec_j))$ 
9: end for
10: Find minimum number of CPs as a minimum set cover on
      $\{VC(ec_i, ec_j)\}$ 
11: Insert CPs into netlist

```

Fig. 14. Control Point Minimization

**Input:**  $ec_A, ec_B, CN(ec_A, ec_B), LSC(A), LSC(B)$

```

1: Create a copy of the original circuit
2: Insert all the CPs required by LSC(A) with the exception
   of  $ec_A, ec_B$ 
3: for all  $cn \in CN(ec_A, ec_B)$  do
4:   for all  $cptype \in CP-0, CP-1$  do
5:     Insert a control point ( $cptype$ ) at  $cn$ 
6:     if LSC(A) is non-redundant then
7:        $FVC = FVC \cup \{cn\}$ 
8:     end if
9:   end for
10: end for
11: if  $FVC \neq \emptyset$  then
12:   Insert all the CPs required by LSC(B) with the exception
     of  $ec_A, ec_B$ 
13:   for all  $fvc \in FVC$  do
14:     Insert a control point of type  $cptype(fvc)$ 
15:     if LSC(B) is non-redundant then
16:        $VC = VC \cup fvc$ 
17:     end if
18:   end for
19: end if
20: return VC

```

Fig. 15. Find Valid CP Candidates

points CP-1 and CP-0. For all candidates that detect LSC(A) a tuple consisting of the net, fanout and CP-type is placed in *First Valid Candidates, FVC*. The algorithm then moves to LSC(B) and repeats the above procedure but this time it uses the members of *FVC* instead of common nets' members. It then adds all those members of *FVC* which are able to detect LSC(B) to *Valid Candidates, VC* list and returns the list to the calling Algorithm (Fig. 14).

## B. Experimental Results

The TPI algorithm (Fig. 10) has been validated using a similar experimental set up as discussed in Section IV-B. The only difference is that instead of extracting the bridge list using

TABLE V  
RESULTS OF TEST POINT INSERTION ALGORITHM

| Design | Total Bridges | Vdd(s)<br>bf TPI | Vdd(s)<br>af TPI | CP(s) | OP(s) |
|--------|---------------|------------------|------------------|-------|-------|
| c1355  | 6,566         | 0.8v, 1.2v       | 0.8v             | 6     | 0     |
| c1908  | 7,986         | All*             | 0.8v, 1.2v       | 2     | 1     |
| c2670  | 10,000        | All              | 0.8v, 1.2v       | 19    | 0     |
| c3540  | 10,000        | All              | 0.8v, 1.0v       | 6     | 1     |
| c7552  | 9,998         | 0.8v, 1.2v       | 0.8v             | 0     | 1     |
| s344   | 469           | All              | 0.8v             | 5     | 0     |
| s382   | 1,146         | All              | 0.8v, 1.2v       | 7     | 2     |
| s386   | 1,625         | All              | 0.8v, 1.0v       | 9     | 1     |
| s838   | 5,737         | All              | 0.8v, 1.0v       | 26    | 11    |
| s5378  | 9,933         | All              | 0.8v, 1.0v       | 5     | 1     |
| s9234  | 10,000        | All              | All              | 0     | 0     |
| s13207 | 10,000        | All              | 0.8v, 1.0v       | 3     | 0     |
| s15850 | 10,000        | All              | 0.8v, 1.0v       | 3     | 0     |

\*All = 0.8v, 1.0v, 1.2v

a layout tool, in this case, an exhaustive bridge list is generated by considering all possible pairs of nets in the netlist, up to a maximum of 10,000 pairs. This is done to increase the total number of bridges, and therefore create more challenging test cases for all the circuits. The test point insertion flow on the layout extracted bridge list required only a very small number of test points, only 3 out of 12 circuits required test points. The experimental data is available at [19] to enable comparison with this work. The total number of bridges for each circuit is shown in the second column of Table V.

The total number of bridges considered for each circuit, along with the number of test Vdd(s) used for detecting all the defects both before and after inserting test points in the circuit, are shown in Table V. As it can be seen, by using the proposed test point insertion method, the number of test Vdds are reduced from three to one, or three to two for almost all circuits without affecting the defect coverage. It is only for s9234 where the number of Vdd settings required during test could not be reduced, this is because it has bridges with highest critical resistance at all three test voltages, i.e., they are all essential. The number of control and observation points added in each circuit are shown next, in Table V. It should be noted that total number of test points (including OPs and CPs) are ten or less for almost all the circuits, and that it is only in the cases of c2670 and s838 that more test points are used.

## VI. CONCLUSION

Low power consumption and low cost manufacturing test are key constraints in today's competitive microelectronics industry. This paper has demonstrated that the employment of adaptive power management presents a number of challenges that need to be addressed to achieve high test quality at low cost. The paper has addressed these challenges through a multi-Vdd test generation method which delivers full bridging fault

coverage across multiple Vdd settings and a test point insertion method which can be employed to reduce the number of Vdd settings required during test without affecting the test quality. Although only non-feedback bridges have been considered in this work, we believe the same concepts are equally applicable for feedback-bridging testing and we are planning to address this in our future work.

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