Modelling for the robust design of layered resonators for ultrasonic

particle manipulation

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Abstract: Several approaches have been described for the manipulation of particles within an

ultrasonic field. Of those based on standing waves, devices in which the critical dimension of

the resonant chamber is less than a wavelength are particularly well suited to microfluidic, or

"lab on a chip" applications. These might include pre-processing or fractionation of samples

prior to analysis, formation of monolayers for cell interaction studies, or the enhancement of

biosensor detection capability.

The small size of microfluidic resonators typically places tight tolerances on the positioning

of the acoustic node, and such systems are required to have high transduction efficiencies, for

reasons of power availability and temperature stability. Further, the expense of many

microfabrication methods precludes an iterative experimental approach to their development.

Hence, the ability to design sub-wavelength resonators that are efficient, robust and have the

appropriate acoustic energy distribution is extremely important.

This paper discusses one-dimensional modelling used in the design of ultrasonic resonators

for particle manipulation and gives example of their uses to predict and explain resonator

behaviour. Particular difficulties in designing quarter wave systems are highlighted, and

modelling is used to explain observed trends and predict performance of such resonators,

including their performance with different coupling layer materials.

Keywords: acoustic radiation force, layered resonators, robust design, particle manipulation

Introduction

Ultrasonic standing waves (USWs) can be used to trap and manipulate particles, and are

particularly well suited for the manipulation of micron-scale biological particles in devices of a

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microfluidic scale [1]. Several different approaches have been employed for the manipulation of particles using ultrasonic fields. For example, focussed ultrasound [2,3] or near-field effects [4] can be used to trap particles prior to analysis, particles can be moved by using two or more opposing transducers to modulate the standing wave field [5,6], or particles can be held and moved within USWs excited by plate waves coupled into the containing fluid [7,8]. However, the use of a simple planar layered resonator with a single transducer [9-11] offers the simplest approach to establishing a USW suitable for particle movement.

Planar USW systems may employ resonators that are larger than a wavelength and contain multiple pressure nodal planes [12,13], but for microfluidic scale devices, a resonant cavity with an axial dimension that is lower than the operating wavelength may be employed [14-16]. Such sub-wavelength resonators typically rely for their operation on precise positioning of the pressure node, to which particles will migrate. In these systems the ability to design a resonator that will operate with a good efficiency and have the required acoustic mode shapes is critical.

A variety of approaches to modelling resonators have been described (see for example [9,17,18]). This paper uses one dimensional models implementing impedance transfer relationships [11,19,20].

Layered resonators for particle manipulation

The structure of a typical planar resonator is shown in Fig. 1 and consists of a transducer which is, in general, bonded to a coupling layer (also known as a carrier layer or matching layer) that serves to isolate the adjacent fluid layer from the transducer. A standing wave is established in the fluid layer by a solid reflector layer.

Particles within the standing wave experience a force, which in most cases of interest acts towards a pressure node of the standing wave. The force on a particle of radius a at position x within the standing wave can be expressed as a function of the spatial gradients of the time averaged kinetic ($E_{kin}(x)$) and potential ($E_{pot}(x)$) energies [21]

$$F(x) = \frac{\partial}{\partial x} \left(\frac{4\pi a^3}{3} \left(\frac{3(\rho_p - \rho_f)}{(2\rho_p + \rho_f)} E_{kin}(x) - \left(1 - \frac{\beta_p}{\beta_f} \right) E_{pot}(x) \right) \right)$$
(1)

where β and ρ are the compressibility and the mass density of the fluid and the particle, indicated by subscripts f and p respectively. The wave number, k is equal to $2\pi/\lambda$ where λ is the wavelength of the standing wave.

The problem of modelling particle behaviour in the standing wave then becomes one of describing the variation of acoustic parameters through the acoustic field such that the energy parameters $E_{kin}(x)$ and $E_{pot}(x)$ can be calculated. The rest of the paper discusses the characterisation of the field itself in order to provide the behaviour required for the correct operation of the device (chiefly nodal position and energy density).

Simple two-layer model

Background theory

An approach to the characterisation of the underlying properties of resonators is to begin by looking at the modal solutions of a two layer system consisting of a fluid layer with a rigid boundary coupled with a reflector layer with a pressure-release boundary [20]. Such a model is not, in itself, sufficient to understand the behaviour of a resonator such as that shown in Fig. 1. However it can act as a starting point, suggesting layer properties able to provide the required nodal behaviour. Additional layers can then be added and their parameters adjusted in a fuller model to maintain, or fine-tune resonator response. The two-layer approach simplifies to solving

$$k_f t_f = \tan^{-1} \left(\frac{r_f \left(r_r^2 + r_0^2 \tan^2 \left(k_r t_r \right) \right)}{r_r \tan \left(k_r t_r \right) \left(r_r^2 - r_0^2 \right)} \right)$$
 (2)

where t_r and t_f are the thicknesses of the reflector and fluid layers respectively, k is the wave number and r_f and r_0 are the acoustic impedances of the fluid and reflector layers respectively. A given ratio of the thicknesses of the two layers (i.e a fixed design) is represented by a straight line passing through 0,0 on the graph in Fig. 2, which shows the first 4 solutions of equation (2), plotted as the ratio of thickness to wavelength of the fluid layer to the ratio of thickness to wavelength of the reflector layer.

A fluid layer having two perfectly rigid boundaries would have modal solutions corresponding to horizontal lines at $t_f/\lambda_f = 0.5$, 1, etc. where λ_f is the ultrasonic wavelength in the fluid layer. Similarly, a reflector bounded by two pressure release surfaces would show half wave resonances as vertical lines corresponding to $t_r/\lambda_r = 0.5$, 1, etc. There is, however, no modal solution at (0.5, 0.5) on the graph, but region C shows how the modes of the coupled system split when adjacent layers would have coincident resonances if isolated. The parameter in Fig. 2 that indicates the position of the pressure node within the fluid layer is t_f/λ_f . In order to place a node centrally, in this two layer model, a reflector thickness of a quarter wavelength is required,

i.e. t_r/λ_r =0.25, as shown in area A of Fig. 2. It can also be seen from area A that the solid line representing the solution to equation (2) is relatively flat in that region, indicating that the position of the node should be stable with regards to the reflector layer thickness. Even with the combination of a half wavelength fluid layer and a quarter wavelength reflector layer, the influences of the coupling layer and transducer need to be considered, and Fig. 3a shows how the frequency of maximum energy density in the fluid layer, and hence the position of the node within the fluid layer, varies as a function of coupling layer thickness. With the parameters used in this system (taken from [11]) the variation in frequency is relatively small, and selection of a quarter wavelength coupling gives the most stable frequency, but a relatively low value of peak energy. The material used for the coupling layer is investigated in more detail later.

The highest values of energy density occur either side of the points at which the coupling layer equals half wavelength multiples, but with a significant dip for the half wavelength coupling layer itself. This dip, however, becomes less pronounced at lower Q factors. If the Q factors are reduced from 200 and 500 for the coupling and fluid layers respectively (Fig 3a) to 50 for both (Fig 3b), the frequency variation of the peak remains similar, but the peak energy density characteristics change significantly. These Q factors seem low, but their values represent observed losses throughout the resonant device and will in general be much lower than material Q factors [9]. A similar observation is made later for quarter-wavelength fluid layer systems where coupling layer materials have been investigated.

Modelling of quarter wavelength devices

The need for robust design of resonators becomes particularly important when dealing with quarter wavelength devices. A quarter wavelength resonance is observed when the fluid layer is at a quarter wavelength and the reflector layer is a half wavelength thick, in the region marked *B* in Fig. 2. Such a system may be used to force particles against, or close to, a solid surface as shown in Fig. 4 which is designed to enhance particle capture on an immunosensor surface.

A simple simulation suggests that for fixed values of coupling layer and reflector thickness, simply varying the fluid layer thickness should enable the pressure node to be positioned at, or close to, the reflector layer. This can be seen from the simulations of a silicon/Pyrex resonator shown in Fig. 5, which use the parameters shown in Table 1.

Table 1. Quarter wave simulation parameters

	Coupling	Fluid	Reflector
	5.25e-4		
Density (kg m ⁻³)	2.34e+3	1.00e+3	2.20e+3
Speed of Sound (m s ⁻¹)	8.43e+3	1.50e+3	5.43e+3

However the gradient of the solution line in region B of Fig. 2 suggests that the nodal position is likely to be extremely sensitive to reflector layer thickness

Martin et al. [22] investigated the acoustics of such a system with the aim of forcing spores onto an antibody coated surface using a 3 MHz USW. The device was tested in batch and flowthrough modes and it was found that the efficacy of capture was critically dependent on the reflector layer thickness. When a 980 µm thick reflector was used, there was almost no capture of the BG spores. Capture increased with a 1000 µm reflector, peaked with a thickness of about 1100 µm and fell away significantly with a reflector thickness of 1300 µm. This was explained by 1D simulations of the acoustic pressure for different reflector thicknesses, as shown in Fig. 6(a). With a reflector thickness of 980 μm, the pressure node is in the fluid, away from the reflector boundary, so particles are forced away from the antigen surface. With a 1000 µm reflector, the node is just in the reflector, so particles will be forced to the surface. A 1200 µm reflector places the node well into the reflector, but also brings a pressure antinode into the fluid, causing many particles to be forced to the opposite boundary. Hence there is an optimum positioning of the node that is dependent on the reflector thickness and a significant decrease in capture efficiency on each side of this thickness. When flow and particle tracking were added to the acoustic model [23] it was possible to predict the nature of the dependence of particle capture on reflector depth, as shown in Fig. 6(b).

Selecting operating points from 2D plots

There are other applications in which it is required to place a pressure node close to, but not on, a boundary with a solid layer. Such a "near quarter-wave" resonator has been designed for

concentrating particles prior to analysis [24] and is shown schematically in Fig. 7.

In this case the aim was to move particles to within 20 μ m of the reflector layer in a 180 μ m cavity. In order to achieve this, multiple simulations were completed to predict the sensitivity of the energy density and nodal position to relevant geometric parameters. An example is shown in Fig. 8 in which these parameters are plotted against reflector and coupling layer thickness. For each geometric design, the acoustic energy within the fluid layer is determined over a small range of frequencies in order to isolate the fluid quarter wavelength mode. Acoustic energy density and corresponding position of the pressure minimum are recorded for the frequency where energy density is seen to peak.

The parameters used in the simulations are shown in the Table 2, with the values of Q-factor inferred by matching modelled and experimentally derived electrical input impedance spectra for:

- 1. the isolated transducer,
- 2. the transducer, glue and coupling layers,
- 3. the full system.

Table 2. Concentrator simulation parameters

Layer	Thickness	Density	Sonic velocity (m/s)	Q-factor
	(µm)	(kg/m^3)		Q-1actor
Glue	10	1080	2640	2
Macor coupling	800-1800	2540	5510	100
Fluid	180	1000	1480	50
Reflector	1200-	2470	5600	100
	1550			

In Fig. 8 the white diagonal bar across plot (a) suggests that both reflector and coupling layer thicknesses are important parameters to consider when designing to maximise acoustic energy density and therefore radiation force. Similarly, plot (b) indicates how the design influences the position of the pressure minimum within the fluid layer and how the thicknesses chosen can result in the pressure node moving from within the fluid layer a small distance from the reflector layer (grey) and into the reflector such that particles are pushed up to the reflector surface

(white). The irregularity of the contour representing a single wavelength is due to a coincidence of the coupled transducer/matching layer resonance and the half wavelength resonance of the reflector. Pressure amplitude plots for the two points ('o' $t_r = 1350 \mu m$ and $t_c = 1200 \mu m$, and '+' $t_r = 1350 \mu m$ and $t_c = 1300 \mu m$) marked in Fig. 8 are shown in Fig. 9.

It can be seen that point '+' corresponds to a higher energy in the coupling layer, although the pressure profile in the fluid layer is similar. However from Fig. 8 point 'o' is far more robust in terms of nodal position, despite having a lower energy.

Just as the damping in the system alters the characteristics between Fig. 3a and Fig. 3b, this system is also sensitive to changes in Q factors. Fig. 10 is a repeat of the simulation shown in Fig. 8 but with a significantly higher reflector Q factor. The nodal position (lower figure in each case) as a function of layer thicknesses remains robust to layer thicknesses and is similar in both figures. Not surprisingly the magnitude of the energy density in the fluid layer (upper figure) changes significantly between the simulations. Further, the form of the energy density surface has changed. In the more highly damped system of Fig. 8, the maximum energy density lies close to the irregular single wavelength contour, while for the higher Q Fig. 10, the maximum energy lies either side of this contour in a manner similar to the coupled resonances described in [11]. Hence the position of the node in these systems appears to be relatively robust to the damping factors.

Fig. 11 shows a prototype quarter wave concentrator in which $t_r = 1440 \,\mu m$ and $t_c = 1040 \,\mu m$. This device provided a factor of 4 concentration with one micron diameter particles and the nodal position was as predicted by modelling using high Q factors, although the damping and hence energy density characteristics proved to be closer to those shown in Fig. 8 on experimental evaluation.

Effect of Varying the Coupling Layer Material

As discussed previously, the coupling layer material can have an effect on the nodal positions, and the amount of energy stored within the fluid layer. Practical considerations are also important in designing particle manipulators, such as bio-compatibility, ease of manufacture, and cost, so it is useful to know what range of materials can be used and how they affect the performance. The device shown in Fig. 11 has a coupling layer manufactured from

Macor, a machinable ceramic, similar to glass. Devices with coupling layers made from other materials were also constructed. The materials investigated were aluminium and brass. It is known that the coupling layer material influences the acoustic energy density and the maximum radiation force experienced by a particle. This is highly relevant to quarter-wavelength systems as the success of a resonator typically relies on maximising the acoustic energy density. In the case of a quarter wave device, the quarter wave mode is a lot less energetic than a typical half wave device and maximizing the efficiency to avoid heating effects in the other layers requires careful design. Quarter wave devices are much less efficient than half wave devices because of the reliance on a reflector layer resonance where much of the acoustic energy is dissipated.

Initial simulations were used to design near quarter-wavelength resonators operating around 2MHz for each coupling layer material. The acoustic pressure profiles within these devices are similar to that shown in Fig.9 where a half-wavelength resonance is seen in the reflector layer above the fluid chamber. This resonance imposes a node at the fluid/reflector boundary and for certain fluid depths will result in a quarter-wavelength "resonance" in the fluid layer. This mode forces suspended particles up to this surface.

For the experimental devices a transducer with a resonance close to the operating frequency of the assembled chamber was used (Ferroperm PZ26, 1mm thick). To give comparable acoustic pressure profiles in the fluid layer, the model was used to select coupling layer and fluid layer thickness dimensions. In each case the fluid layer thickness was chosen to be 0.18mm and coupling layer thicknesses of 1.0, 1.4, and 1.2 were selected for brass, aluminium and Macor, respectively. Table 3 contains the measured thickness dimensions and acoustic properties used in the initial modelling.

Although the modelling suggests good results for the pressure profile, the model requires calibrating with experimental data to provide absolute values for the acoustic parameters. This is done by taking acoustic energy density measurements for the different chambers and then adjusting the model parameters such as material Q factors, to get the best match. Acoustic energy density measurements are taken between 1.96 and 2.1 MHz at 10 kHz intervals. These measurements are made by levitating a polystyrene particle and recording the threshold voltage where the particles begin to sediment, similar to the method described by Martin *et al.* [22]. For the particles, fluid (water) and frequency used, this threshold voltage corresponds to a pressure amplitude of 33kPa. During experiments, the position of the node is difficult to measure

accurately but is reasonably consistent with predictions of the pressure profile such as that shown in Fig. 9. As the acoustic pressure amplitude is proportional to the transducer voltage, the pressure amplitude P_0 resulting from a 10 V_{pkpk} voltage is recorded and converted to an energy density measurement using (3):

$$\langle \bar{\varepsilon} \rangle = \frac{1}{4} P_0^2 \beta_w, \tag{3}$$

where $\langle \overline{\varepsilon} \rangle$ is the acoustic energy density and β_w is the bulk modulus of water, with the results presented in Fig. 12.

These plots show that the acoustic energy density peaks at frequencies where resonant modes are encountered. Predicted energy density is also shown, where the input parameters to the model have been modified to improve the match with both impedance and energy density measurements. Notably the Q factors have been adjusted to 300, 100 and 100 for brass, aluminium and Macor, respectively. Similarly, the Q factors in the fluid and reflector are low at ~30 and ~100, respectively. In the case of brass, two peaks can be seen although the model suggests that the peak around 1.98MHz is a combined transducer and coupling layer resonance. This mode appears to be particularly energetic and may be reinforced, for example, by structural modes.

To compare each material more directly, the model was used to simulate the effect of varying coupling layer thickness whilst applying identical reflector and fluid layer properties. Fig. 13 shows the predicted peak energy density for a range of coupling layer thicknesses as a

Table 3. Dimensions of experimental samples. Properties of materials taken from [25].

Coupling layer	thickness (mm)		Fluid layer thickness (mm)		Densit y	Sonic velocity	Acoustic impedan
material	Design	Measured	Design	Measu red	(kg/m ³	(m/s)	ce (MRayl)
Brass	1.00	1.08	0.18	0.17	8640	4700	40.6
Aluminiu m	1.40	1.42	0.18	0.175	2700	6420	17.3
Macor	1.20	1.17	0.18	0.19	2540	5510	14.0

fraction of wavelength (t_m/λ) and where the transducer voltage is a constant 10 Vpkpk. Note that Fig. 13 is generated by locating the frequency at which the quarter-wavelength mode (reflector resonance) occurs and omits any other resonant modes close to this frequency. It therefore does not include the high energy resonance seen at 1.98MHz in the experimental results for the brass coupling material.

In general, the energy density is comparable for the materials considered, although the material does have a limited impact in the maximum energy density achievable. Peaks suggest that for all the materials tested a coupling layer thickness of just under $n.t_m/2\lambda$ (n = 1, 2 only shown) results in a higher acoustic energy. The trade-off in this case is that the acoustic node moves away from the surface and further into the fluid layer at these dimensions as shown in Fig. 13c. As the transducer is operating close to a half-wavelength, the peaks also coincide with a wavelength resonance in the transducer and coupling layer combined where if this structure were isolated from the fluid and reflector would have a pressure node located on the coupling layer surface. The close proximity of this coupled resonance to the quarter-wavelength mode may therefore be responsible for the change in energy density and movement of the node towards the coupling layer surface. Also, for an increase in n the energy density decreases, probably due to greater losses within a progressively thicker coupling layer.

The observations made in Fig. 13 are similar to those in Fig. 3b for a half-wavelength system. This suggests that the design of the coupling layer and transducer can be decoupled from the fluid and reflector layer to some extent. For example, the position of the nodal plane(s) within a fluid chamber depends on the controlled design of the fluid and reflector design and aided by Fig. 2. Although the coupling layer and transducer will influence the node position and energy density, they have a small effect relative to fluid/reflector design and considering the wide range of coupling layer/transducer designs which could feasibly drive the system.

Conclusions

One-dimensional acoustic modelling has helped identify specific parameters which influence the robust design of resonators for particle manipulation. The nodal position and energy density are typically important factors in resonator performance, and the choice of layer dimensions and material properties influence these factors significantly. For example, the careful selection of Q factors for the various materials and layers used to construct these resonators may be used to help relax dimensional tolerances. It appears that the influence of the coupling layer on the

performance of both half and quarter-wavelength resonances is related, with the proximity of the coupling layer/transducer mode impacting upon the characteristics of fluid/reflector modes.

It has also been shown that the behaviour of quarter-wavelength modes can be more fully understood based on a comparison of modelled and experimental data. Using experimental data to refine the simulation input parameters it is possible to predict the acoustic energy density to well within the correct order of magnitude. This is important, for example, for bio-sensing applications where the location of the pressure node and strength of the field influences significantly the feasibility of such devices. The choice of material used to couple between the transducer and fluid manipulation chamber determines to a limited extent the maximum energy density achievable, although coupling layer thickness appears to have a greater impact. Therefore a range of materials can be used for the construction of the coupling layer.

While 1D models are able to provide very useful, and in the case of nodal position accurate, predictions of device behaviour, the influences of lateral field variations are also of significance [26]. These variations are the main limitation on the performance of the concentrator described here [24]

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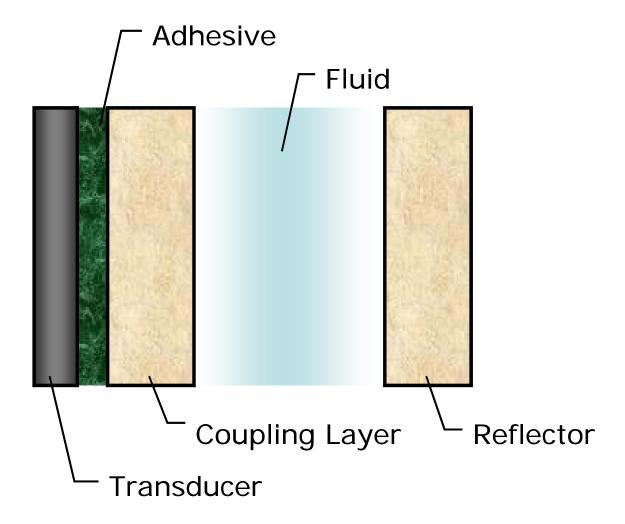


Fig. 1. Typical structure of a planar layered resonator

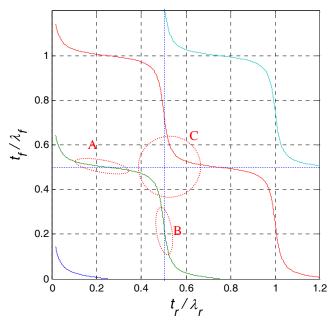


Fig. 2. The first four solutions of equation (2), based on [20]. Parameters t_r and t_f are the thicknesses of the reflector and fluid layers respectively and λ_r and λ_f are ultrasonic wavelengths in those layers

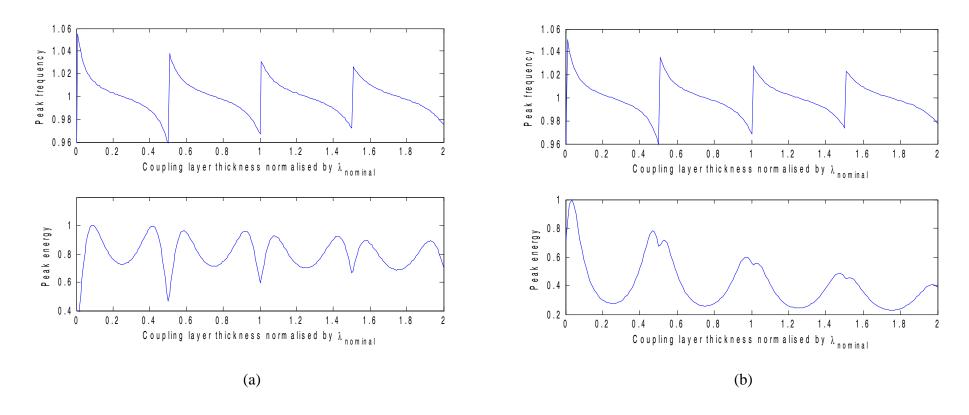


Fig. 3. Variation of the frequency and energy density of the most energetic resonance as coupling thickness layer varies. (a) Parameters based on simulations in [11], and normalised against the nominal resonance frequency. (b) With lower Q factors in coupling and fluid layers.

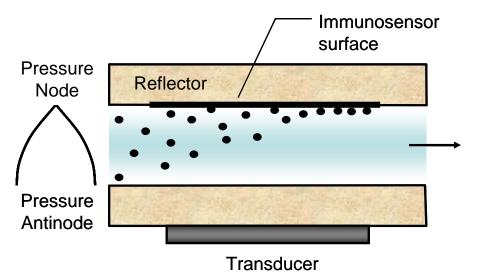


Fig. 4. Schematic representation of a quarter wavelength resonator forcing particles up against a solid surface with an immunosensor coating.

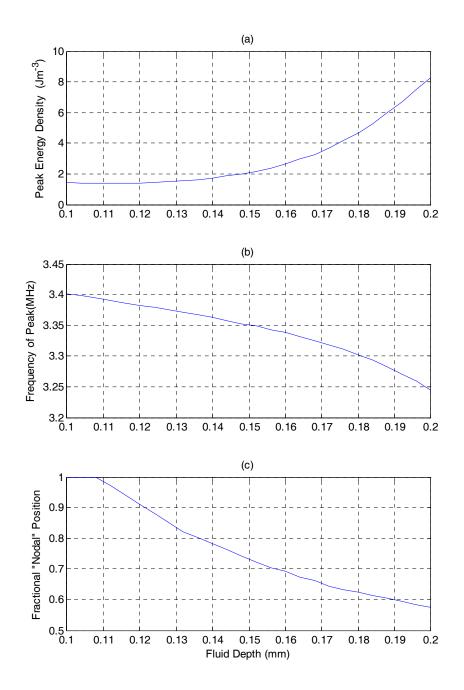


Fig. 5. Simulated values of peak energy density, peak frequency and nodal position for silicon microfabricated quarter wavelength resonator

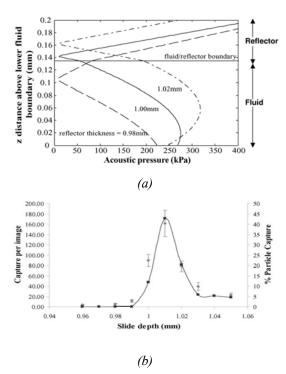


Fig. 6. Acoustic simulation of the pressure profile across the chamber used by Martin et al. [22] for different reflector thicknesses (a), and simulations of particle capture (line) compared with experimental data (b). Reproduced from [22] with permission from Elsevier.

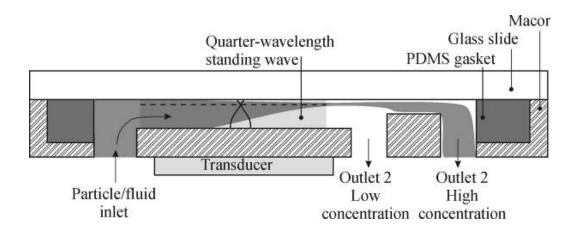


Fig. 7. Schematic representation of a "near quarter-wave" concentrator.

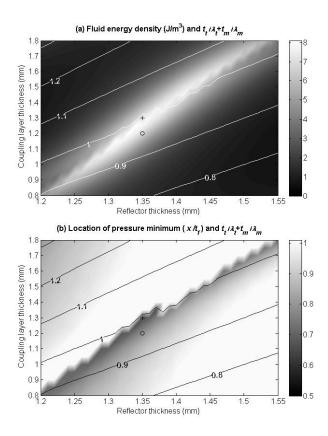


Fig. 8. Acoustic energy density in the fluid layer (upper) and fractional position of pressure minimum (lower) with contours representing the coupled transducer and coupling layer thickness in wavelengths.

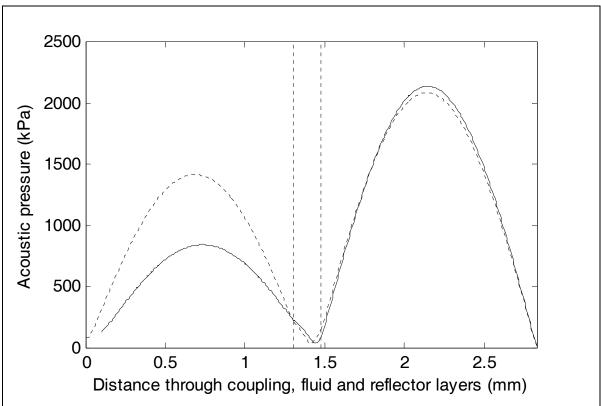


Fig. 9. Acoustic pressure profile for the two potential design points marked in Fig. 9 - 'o' (solid) and '+' (dotted).

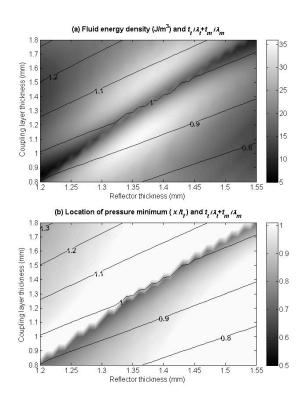
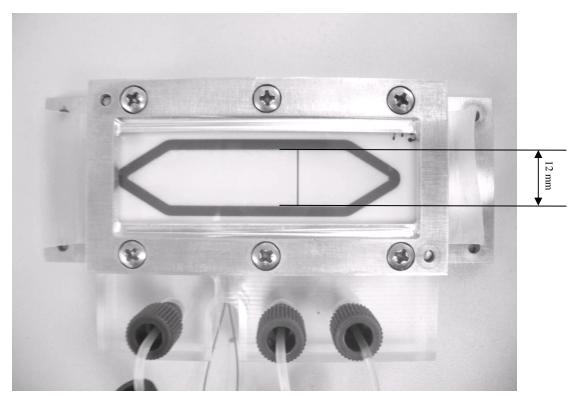


Fig. 10. Acoustic energy density in the fluid layer (upper) and fractional position of pressure minimum (lower) with contours representing the coupled transducer and coupling layer thickness in wavelengths but with higher Q factors in the layers than used in Fig. 9



 $\textbf{Fig. 11.} \ \ Prototype \ quarter-wavelength \ concentrator$

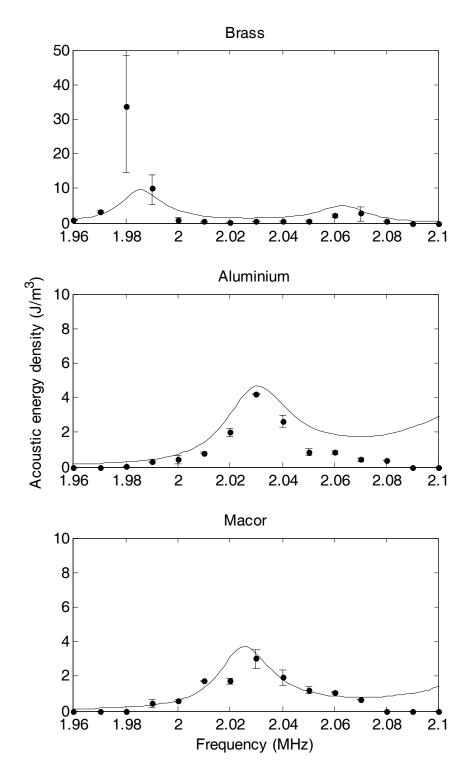


Fig. 12. Comparison between measured (pointes with error bars) and modelled (solid lines) acoustic energy density.

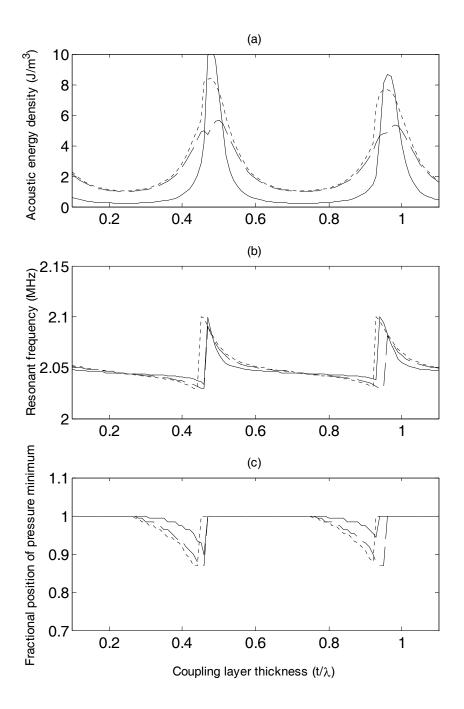


Fig. 13. Predicted peak acoustic energy density in the fluid layer for a range of coupling layer thicknesses for brass (solid), aluminium (dashed) and Macor (dotted). Showing (a) acoustic energy density, (b) the quarter-wavelength excitation frequency and (c) the fractional position of the pressure minimum within the fluid chamber.