

Iterative detection and decoding for hard-decision forwarding aided cooperative spatial multiplexing

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Abstract—In this paper, ¹ the optimal decoding strategy for cooperative spatial multiplexing (CSM) aided systems is derived. In CSM systems, the multiple relay stations (RSs), which compose a virtual antenna array (VAA), independently decode the packets received from the mobile stations (MS) and forward them to the base station (BS). When the BS decodes the signal forwarded from the RSs, the potential decoding errors encountered at the RSs will result in erroneous forwarding, but their effects are mitigated by the proposed solution. Our simulation results show that when the direct link has a significantly higher signal-to-noise ratio than the relay link, the proposed decoding algorithm achieves an approximately 3 dB better performance than conventional CSM, which does not consider the deleterious effects of erroneous forwarding from the RSs.

I. INTRODUCTION

Multiple-input multiple-output (MIMO) systems [1] are capable of dramatically increasing the channel capacity, which grows linearly with the number of transmit or receive antennas, whichever is lower [2], [3]. However, the mobile stations (MSs) have a limited-size and hence they are typically equipped with a single antenna, which erodes the achievable capacity gain of MIMO systems. To mitigate this problem, virtual antenna arrays (VAAs) based on cooperative and relay station (RS)-aided communications have been studied [4]–[6], [9]–[11]. In the uplink (UL) of VAA-aided systems, the source information is first transmitted from the MS to multiple RSs, and then the RSs simultaneously retransmit the received packet to the base station (BS) having multiple receive antennas. By composing a virtual MIMO channel between the multiple RSs and the BS, substantial diversity and multiplexing gains can be achieved. Furthermore, since the RSs are typically far apart, the signals transmitted from the RSs experience independent fading, which ensures a higher diversity gain. By using VAAs based on multiple RSs, the effects of shadow fading can also be mitigated. The RSs may be constituted by the MSs, which are currently not engaged in active communication with the BS, but fixed RSs may also be installed.

Similar to collocated antenna arrays, various MIMO transmission modes can be applied to the VAAs, such as for example, space-time coding (STC) [4]–[6] designed for attaining a high diversity gain. By contrast, cooperative spatial multiplexing (CSM) [7], [8] was contrived to maximise the achievable throughput in multiple RS aided VAAs [6], [9]–[11]. In the CSM transmission mode, the UL packet received at the RSs

in a high-rate serial transmission mode is divided into several lower-rate substreams, which are simultaneously transmitted in parallel from the RSs to the BS. More specifically, each RS independently decodes the entire UL packet based on its own received signal, but it forwards only a part of the entire packet using an error-resilient mode without reducing the overall throughput. Compared to classic relaying systems, the CSM arrangement is capable of reducing the required temporal and spectral resources as a benefit of parallel—rather than individual serial—transmission from multiple RSs. Consequently, by employing CSM, rather than a single RS-aided scheme using for example multiple time-slots, the effective throughput can be increased.

In this paper, a novel CSM scheme is proposed. It is typically assumed that RSs perfectly decode the packets received from the source. However, in practice, decoding errors may occur at the RSs and hence the erroneous packets are forwarded from the RSs to the destination, which may substantially affect the attainable end-to-end performance. To circumvent this problem, we develop an efficient decoding algorithm for the destination node (i.e. for the BS in the UL), which is capable of mitigating the associated error propagation. In the proposed algorithm, the decoding errors encountered at the RSs are taken into account, when iterative MIMO detection/decoding [13] is performed at the BS. More explicitly, the decoding errors of a RS can be corrected at the BS with the aid of the side information, which is generated from the substreams received from other RSs as well as from the signal directly received from the source node.

This paper is organized as follows. Section II describes the system model of multiple RS aided CSM communication. In Section III, the proposed decoding algorithm is derived, while Section IV provides our simulation results. In Section V, our conclusions are presented

II. SYSTEM MODEL

Both the MS and the RSs are assumed to have a single antenna², while the BS has N_B receive antennas. We assume that N_R RSs support the UL communication, which results in a $(N_B \times N_R)$ -dimensional virtual MIMO channel matrix between the RSs and BS. In the first time-slot (TS), the MS

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²In this paper, the proposed algorithm is derived under assumption that the MS and RSs adopt a single antenna. However, the proposed algorithm can be readily extended to the scenario of having multiple antennas at the MS and RSs.

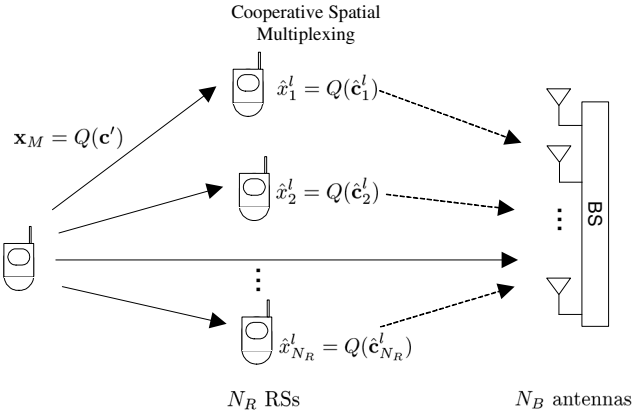


Fig. 1. Cooperative spatial multiplexing systems.

encodes the UL information bit stream into a codeword \mathbf{c}' , which contains L_c coded bits. The codeword \mathbf{c}' is then mapped to the symbol stream \mathbf{x}_M hosted by the $(L_x \times 1)$ -element symbol vector. Then, \mathbf{x}_M is transmitted from the MS to the RSs, as shown in Fig. 1. The signal received at the n th RS during the l th channel use becomes

$$y_{R,n}^l = h_{R,n} x_M^l + v_{R,n}^l, \quad n = 1, 2, \dots, N_R, \quad l = 1, 2, \dots, L_x, \quad (1)$$

where x_M^l is the l th element of \mathbf{x}_M and $y_{R,n}^l$ is the corresponding received signal. Furthermore, $h_{R,n}$ represents the complex-valued channel coefficient and $v_{R,n}^l$ indicates the independent zero-mean complex Gaussian noise having a variance of $\sigma_v^2/2$ per dimension.

We note that during the first TS, the BS also receives the symbol stream \mathbf{x}_M , which is directly transmitted from the MS, even though the direct link between the MS and BS typically has a lower signal-to-noise ratio (SNR) than the relay link. The signal received at the m th antenna of the BS can be written as

$$y_{B,m}^l = h_{B,m} x_M^l + v_{B,m}^l, \quad m = 1, 2, \dots, N_B, \quad l = 1, 2, \dots, L_x, \quad (2)$$

where $h_{B,m}$ denotes the complex-valued channel coefficient and $v_{B,m}^l$ indicates the independent zero-mean complex Gaussian noise having a variance of $\sigma_v^2/2$ per dimension.

Exploiting the signal received from the MS, each RS estimates the codeword \mathbf{c}' by performing channel decoding. The estimate of \mathbf{c}' at the n th RS is denoted as $\hat{\mathbf{c}}'_n$. Then, $\hat{\mathbf{c}}'_n$ is forwarded to the interleaver $\Pi_R(\cdot)$ in order to obtain $\hat{\mathbf{c}}_n = \Pi_R(\hat{\mathbf{c}}'_n)$. If the received packet is perfectly decoded at each RS, we have $\hat{\mathbf{c}}_1 = \hat{\mathbf{c}}_2 = \dots = \hat{\mathbf{c}}_{N_R} = \mathbf{c}$, where $\mathbf{c} = \Pi_R(\mathbf{c}')$. For the sake of benefitting from spatial multiplexing aided transmissions, the interleaved codeword $\hat{\mathbf{c}}_n$ is divided into N_R reduced-length substreams $\{\hat{\mathbf{c}}_{n,1}, \hat{\mathbf{c}}_{n,2}, \dots, \hat{\mathbf{c}}_{n,N_R}\}$, where $\hat{\mathbf{c}}_{n,k}$ indicates the k th (L_c/N_R) -length substream of $\hat{\mathbf{c}}_n$. Given the N_R substreams, the n th RS only transmits the n th substream $\hat{\mathbf{c}}_{n,n}$ to the BS. More specifically, N_R RSs transmit

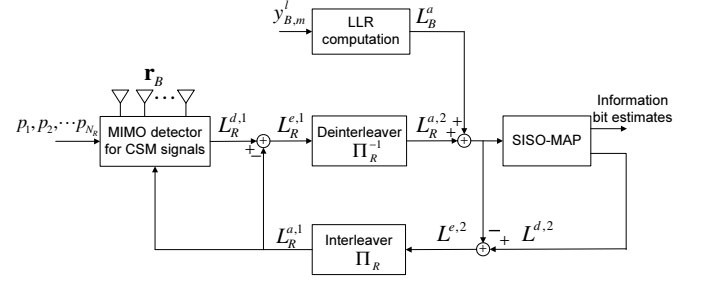


Fig. 2. Block diagram of the proposed decoding scheme.

N_R substreams in parallel so that the entire codeword of \mathbf{c} is received at the BS during the second TS.

The substream $\hat{\mathbf{c}}_{n,n}$ of the n th RS can be expressed as $\hat{\mathbf{c}}_{n,n} = \{\hat{\mathbf{c}}_{n,1}^l, \hat{\mathbf{c}}_{n,2}^l, \dots, \hat{\mathbf{c}}_{n,N_R}^l\}$, where $\hat{\mathbf{c}}_n^l$ is the coded bit vector associated with the symbol \hat{x}_n^l , which is transmitted from the n th RS during the l th channel use. Here, L_s denotes the number of channel uses during the second TS. The overall received signal at the BS during the l th channel use of the second TS can be expressed as³

$$\mathbf{r}_B = \mathbf{G} \hat{\mathbf{x}}_R + \mathbf{v}_B, \quad (3)$$

where \mathbf{r}_B represents the $(N_B \times 1)$ -element complex-valued received signal vector, while $\hat{\mathbf{x}}_R = [\hat{x}_1^l, \hat{x}_2^l, \dots, \hat{x}_{N_R}^l]^T$ indicates the symbol vector transmitted across the RSs during the l th channel use. Furthermore, \mathbf{G} denotes the $(N_B \times N_R)$ -element complex-valued channel matrix, where $[\mathbf{G}]_{mn}$ indicates the channel coefficient between the n th RS and the m th receive antenna of the BS. Still considering (3), \mathbf{v}_B denotes the $(N_B \times 1)$ -element noise vector of independent zero-mean complex Gaussian entries having a variance of $\sigma_v^2/2$ per dimension. It is worth noting that the received signal model of (3) is reminiscent of the vertically encoded MIMO system of [12], [14], which transmits a segment of a single codeword from each transmit antenna.

By applying the now classic iterative detection and decoding (IDD) algorithm to the received signal \mathbf{r}_B [12], [14], the BS decodes the UL packet \mathbf{c}' . As shown in Fig. 2, the directly detected signal $y_{B,m}^l$ of (2) can also be exploited in order to improve the attainable performance. When decoding \mathbf{c}' , it is generally assumed that the RSs forwarded perfectly decoded data. However, in practical relaying systems, decoding errors may occur at the RSs, which causes error propagation at the BS. In order to mitigate error propagation, an efficient decoding algorithm will be proposed in the forthcoming section, which considers potentially erroneous signal transmission from the RSs. The proposed algorithm is derived by extending the decoding algorithm of [15] to CSM systems.

III. PROPOSED DECODING ALGORITHM

The bit error probability (BEP) within the decoded packet $\hat{\mathbf{c}}_n$, which is the interleaved version of the channel decoder's

³For notational convenience, we omit the channel use index throughout the paper, when it does not cause any confusion.

output at the n th RS, is denoted as $p_n (< 1/2)$, i.e. $p_n = d(\hat{\mathbf{c}}_n, \mathbf{c})/L_c$, where $d(\cdot, \cdot)$ represents the Hamming distance between two vectors. Furthermore, we denote the coded bit vector associated with the l th symbol vector $\hat{\mathbf{x}}_R$ as $\hat{\mathbf{c}}^l = \{\hat{c}_1^l, \hat{c}_2^l, \dots, \hat{c}_{N_R}^l\}$. We note that the elements of $\hat{\mathbf{x}}_R$ are independently transmitted from the different RSs and \hat{c}_n^l is the estimated coded bit stream at the n th RS. Then, $\hat{\mathbf{c}}^l$ can be written as

$$\hat{\mathbf{c}}^l = \mathbf{c}^l \oplus \Delta \mathbf{c}^l, \quad (4)$$

where \mathbf{c}^l denotes the corresponding exact coded bits, while $\Delta \mathbf{c}^l \in \{0, 1\}^K$ represents the K -element vector of decoding errors in $\hat{\mathbf{c}}^l$. Here, \oplus denotes the element-wise XOR operation, while K denotes the size of $\hat{\mathbf{c}}^l$, namely the number of coded bits associated with the symbol vector $\hat{\mathbf{x}}_R$. Furthermore, the k th bit of $\hat{\mathbf{c}}^l$ can be expressed as $\hat{c}_k = c_k \oplus \Delta c_k$, where c_k and Δc_k indicate the k th elements of \mathbf{c}^l and $\Delta \mathbf{c}^l$, respectively. We express the probability of Δc_k as

$$p(\Delta c_k) = \begin{cases} 1 - q_k, & \text{if } \Delta c_k = 0 \\ q_k, & \text{if } \Delta c_k = 1 \end{cases}, \quad (5)$$

where q_k is equal to one of the N_R RS BEPs $\{p_1, p_2, \dots, p_{N_R}\}$. More specifically, if \hat{c}_k is the coded bit transmitted from the n th RS, its error probability becomes p_n , i.e., $q_k = p_n$.

The signal directly received from the MS does not contain the RS's decision error hosted by $\Delta \mathbf{c}^l$ and hence the conventional channel decoder is applied to $y_{B,m}^l$ of (2) without any modification. Therefore, we only have to modify the MIMO detection block of the CSM signals of (3) seen in Fig. 2 by considering the decoding error vector $\Delta \mathbf{c}^l$. The log-likelihood ratio (LLR) of c_k is formulated as

$$L_R^{d,1}(c_k) = \log \frac{\sum_{\{\mathbf{c}^l, \Delta \mathbf{c}^l\}: c_k=1} e^{-\|\mathbf{r}_B - \mathbf{G}\tilde{\mathbf{x}}_R\|^2/\sigma^2} p(\mathbf{c}^l, \Delta \mathbf{c}^l)}{\sum_{\{\mathbf{c}^l, \Delta \mathbf{c}^l\}: c_k=0} e^{-\|\mathbf{r}_B - \mathbf{G}\tilde{\mathbf{x}}_R\|^2/\sigma^2} p(\mathbf{c}^l, \Delta \mathbf{c}^l)}, \quad (6)$$

where $\tilde{\mathbf{x}}_R$ is a trial of $\hat{\mathbf{x}}_R$ corresponding to $\{\mathbf{c}^l, \Delta \mathbf{c}^l\}$ and $p(\mathbf{c}^l, \Delta \mathbf{c}^l)$ is the joint probability of \mathbf{c}^l and $\Delta \mathbf{c}^l$. Furthermore, $\|\cdot\|$ represents the Frobenius matrix norm. With the aid of the random interleaver $\Pi_R(\cdot)$ at the RSs, the elements of \mathbf{c}^l and $\Delta \mathbf{c}^l$ can be assumed to be mutually independent, respectively, and hence the joint probability $p(\mathbf{c}^l, \Delta \mathbf{c}^l)$ is written as

$$p(\mathbf{c}^l, \Delta \mathbf{c}^l) = \prod_{i=1}^K p(\Delta c_i) p(c_i). \quad (7)$$

Employing (7), the likelihood function of (6) is formulated as

$$\begin{aligned} & \sum_{\{\mathbf{c}^l, \Delta \mathbf{c}^l\}: c_k=1} e^{-\|\mathbf{r}_B - \mathbf{G}\tilde{\mathbf{x}}_R\|^2/\sigma^2} p(\mathbf{c}^l, \Delta \mathbf{c}^l) \\ &= \sum_{\{\mathbf{c}^l, \Delta \mathbf{c}^l\}: c_k=1} d(\tilde{\mathbf{x}}_R) \prod_{i=1}^K p(\Delta c_i) p(c_i), \end{aligned} \quad (8)$$

where $d(\tilde{\mathbf{x}}_R) = e^{-\|\mathbf{r}_B - \mathbf{G}\tilde{\mathbf{x}}_R\|^2/\sigma^2}$. Then, as in [15], we divide (8) into four terms with respect to the values of c_1 as well as Δc_1 and combine them in order to obtain

$$\begin{aligned} & \sum_{\{\mathbf{c}^l, \Delta \mathbf{c}^l\}: c_k=1} d(\tilde{\mathbf{x}}_R) p(\mathbf{c}^l, \Delta \mathbf{c}^l) \\ &= \sum_{\{\mathbf{c}_2^l, \Delta \mathbf{c}_2^l, \hat{c}_1\}: c_k=1, \hat{c}_1=0} d(\tilde{\mathbf{x}}_R) \{(1 - q_1) p(c_1 = 0) \\ &+ q_1 p(c_1 = 1)\} \prod_{i=2}^K p(\Delta c_i) p(c_i) \\ &+ \sum_{\{\mathbf{c}_2^l, \Delta \mathbf{c}_2^l, \hat{c}_1\}: c_k=1, \hat{c}_1=1} d(\tilde{\mathbf{x}}_R) \{q_1 p(c_1 = 0) \\ &+ (1 - q_1) p(c_1 = 1)\} \prod_{i=2}^K p(\Delta c_i) p(c_i), \end{aligned} \quad (9)$$

where we have $\mathbf{c}_i^l = \{c_i, c_{i+1}, \dots, c_K\}$ and $\Delta \mathbf{c}_i^l = \{\Delta c_i, \Delta c_{i+1}, \dots, \Delta c_K\}$. By using the a-priori probability of \hat{c}_i

$$p(\hat{c}_i) = \begin{cases} (1 - q_i) p(c_i = 0) + q_i p(c_i = 1), & \text{if } \hat{c}_i = 0 \\ q_i p(c_i = 0) + (1 - q_i) p(c_i = 1), & \text{if } \hat{c}_i = 1 \end{cases}, \quad (10)$$

we rewrite (9) as

$$\begin{aligned} & \sum_{\{\mathbf{c}^l, \Delta \mathbf{c}^l\}: c_k=1} d(\tilde{\mathbf{x}}_R) p(\mathbf{c}^l, \Delta \mathbf{c}^l) \\ &= \sum_{\{\mathbf{c}_2^l, \Delta \mathbf{c}_2^l, \hat{c}_1\}: c_k=1} d(\tilde{\mathbf{x}}_R) p(\hat{c}_1) \prod_{i=2}^K p(\Delta c_i) p(c_i). \end{aligned} \quad (11)$$

Similar operations to (9) and (11) can be applied to the other coded bits $\{c_2, c_3, \dots, c_K\}$ except for c_k in order to obtain

$$\begin{aligned} & \sum_{\{\mathbf{c}^l, \Delta \mathbf{c}^l\}: c_k=1} d(\tilde{\mathbf{x}}_R) p(\mathbf{c}^l, \Delta \mathbf{c}^l) \\ &= p(c_k = 1) \left\{ (1 - q_k) \sum_{\hat{\mathbf{c}}^l: \hat{c}_k=1} d(\tilde{\mathbf{x}}_R) \prod_{i=1, i \neq k}^K p(\hat{c}_i) \right. \\ &+ q_k \sum_{\hat{\mathbf{c}}^l: \hat{c}_k=0} d(\tilde{\mathbf{x}}_R) \prod_{i=1, i \neq k}^K p(\hat{c}_i) \left. \right\}. \end{aligned} \quad (12)$$

The likelihood function for $c_k = 0$ can also be simplified by applying similar operations to those of (9), (11) and (12), yielding (13). Upon excluding the a-priori part, the extrinsic information is expressed as (14).

In [15], only a single RS having multiple antennas was employed for network-coding aided relaying systems. Therefore, the error rate q_k is constant over the elements of $\hat{\mathbf{c}}^l$. However, in CSM systems employing multiple RSs, each RS independently decodes the received packet, a part of which is forwarded from each RS to the BS. Therefore, the parallel spatial substreams received at the BS have different BEPs p_n . In (14), it is seen that the extrinsic information of a coded bit is computed by using its specific error rate q_k . Furthermore, when $p(\hat{c}_i)$ is computed in (10), each coded bit's error probability q_i is exploited. In order to employ the proposed decoding algorithm, the BEP information of $\{p_1, p_2, \dots, p_{N_R}\}$ should be forwarded to the BS. However,

$$L_R^{d,1}(c_k) = \log \frac{p(c_k = 1)}{p(c_k = 0)} + \log \frac{(1 - q_k) \sum_{\hat{c}^l: \hat{c}_k=1} d(\tilde{\mathbf{x}}_R) \prod_{i=1, i \neq k}^K p(\hat{c}_i) + q_k \sum_{\hat{c}^l: \hat{c}_k=0} d(\tilde{\mathbf{x}}_R) \prod_{i=1, i \neq k}^K p(\hat{c}_i)}{(1 - q_k) \sum_{\hat{c}^l: \hat{c}_k=0} d(\tilde{\mathbf{x}}_R) \prod_{i=1, i \neq k}^K p(\hat{c}_i) + q_k \sum_{\hat{c}^l: \hat{c}_k=1} d(\tilde{\mathbf{x}}_R) \prod_{i=1, i \neq k}^K p(\hat{c}_i)}. \quad (13)$$

$$L_R^{e,1}(c_k) = \log \frac{(1 - q_k) \sum_{\hat{c}^l: \hat{c}_k=1} d(\tilde{\mathbf{x}}_R) \prod_{i=1, i \neq k}^K p(\hat{c}_i) + q_k \sum_{\hat{c}^l: \hat{c}_k=0} d(\tilde{\mathbf{x}}_R) \prod_{i=1, i \neq k}^K p(\hat{c}_i)}{(1 - q_k) \sum_{\hat{c}^l: \hat{c}_k=0} d(\tilde{\mathbf{x}}_R) \prod_{i=1, i \neq k}^K p(\hat{c}_i) + q_k \sum_{\hat{c}^l: \hat{c}_k=1} d(\tilde{\mathbf{x}}_R) \prod_{i=1, i \neq k}^K p(\hat{c}_i)}. \quad (14)$$

if the length L_c of the codeword is sufficiently high, the side-information transmission overhead of the BEP information is expected to be modest.

IV. SIMULATION RESULTS

In order to evaluate the performance of the proposed decoding algorithm, we have performed computer simulations. We employed a turbo code having the rate $R = 1/2$ and length of 1024, which is constituted by two recursive systematic convolutional (RSC) codes with the octal generators (7,5). Furthermore, QPSK signaling and the exact log-MAP channel decoding algorithm are used. The number of inner decoding iterations in the turbo channel decoder was set to five. In the IDD of the MIMO receiver, all possible symbol combinations are considered in the computation of (14), and the number of outer MIMO detection/decoding iterations was selected to be four.

All the elements of the MIMO channel matrices are assumed to be independent and identically distributed (i.i.d.) zero-mean complex Gaussian random variables having a variance of $1/2$ per dimension, which are constant in a TS. The SNR is defined as the ratio of the average power per information bit arriving at the receiver to the spectral density of the noise. For simplicity, the SNRs of the MS-RS and RS-BS links are assumed to be same and are denoted as γ_R . The SNR of the direct link from the MS to the BS is denoted as γ_{MB} . It is also assumed that the relay channel has the same or a higher SNR compared to the direct channel (i.e. $\gamma_R \geq \gamma_{MB}$) and we denote the ratio between these SNRs as $\gamma_\Delta (> 1)$.

In Figs. 3-5, where the codeword error ratio (CER) performance of various decoders is characterized, the *perfect CSM* denotes the idealized CSM scheme that transmits the perfectly decoded packets from the VAA, which do not suffer from decoding errors at the RSs. By contrast, the *conventional CSM* refers to the specific CSM scheme, which does not consider the potential presence of decoding errors at the RSs. Therefore, the BS assumes that perfectly decoded packets were transmitted from the RSs, regardless whether the forwarded packets actually contain hard-decision errors. In *Decoder 1*, namely the proposed scheme, the BS performs decoding by exploiting the algorithm described in Section III, while perfect knowledge of the BEP q_k is assumed. By contrast, in *Decoder 2* each RS estimates the BEP q_k with the aid of the algorithm described in [15], which is then forwarded to the BS. The ‘*SDF using the Gaussian model*’ represents the soft-decision forwarding aided CSM system, where the expectation values

of the decoded symbols are transmitted from the RSs in order to minimize the mean square error of the forwarded signal, while the soft-valued errors between the transmitted symbols and the exact values are assumed to be Gaussian random variables [16].

Fig. 3 illustrates the achievable CER performance of CSM systems using $N_R = 2$, $N_B = 2$, and $\gamma_\Delta = 6$ dB. It is seen that *Decoder 1* and *Decoder 2* perform similarly, even though *Decoder 2* does not assume the perfect knowledge of the BEP q_k . Furthermore, both *Decoder 1* and *Decoder 2* outperform the ‘*SDF using the Gaussian model*’ as well as the ‘*conventional CSM*’. In Fig. 4, the performance of CSM systems using $N_R = 2$, $N_B = 2$, and $\gamma_\Delta = 18$ dB is shown. In this scenario, the direct link has a much lower SNR than the relay link and hence the beneficial effect of the signal directly transmitted from the MS is almost negligible. In Fig. 4, it is observed that at $\text{CER}=10^{-2}$, *Decoder 1* provides an approximately 2.8 dB SNR gain compared to the ‘*SDF using the Gaussian model*’. Since the direct link is weak in this scenario, the accurate modeling of the relayed signal beneficially affects the achievable decoding performance at the BS. More specifically, the proposed algorithm of Section III employs a more accurate error model than the ‘*SDF using the Gaussian model*’ and hence it provides a substantial performance improvement, even though it exploits a simple hard-decision based forwarding scheme, rather than a soft-decision forwarding aided relaying scheme.

In Fig. 5, the performance of the $N_R = 4$, $N_B = 4$ and $\gamma_\Delta = 18$ dB scenario is characterised. Similar to Figs. 3-4, the proposed *Decoders* perform significantly better than the *conventional CSM*. Furthermore, they achieve an approximately 3.2 dB SNR gain over the ‘*SDF using the Gaussian model*’.

V. CONCLUSION

In this paper, the optimal decoding algorithm designed for hard-decision forwarding aided CSM systems has been derived. Since multiple RSs independently decode their received packets, which are forwarded to the BS, each RS may have a different decoding error rate. Therefore, in contrast to the decoding algorithm of [15], which employs a single RS in the network-coding aided relaying system, the different BEP of each spatial stream is taken into account in order to create the optimal decoding algorithm for CSM systems. In the proposed algorithm, the erroneous forwarded signals can be corrected with the aid of the $(N_R - 1)$ other spatial layer’s signals as well as using the signal directly received from the MS. Our

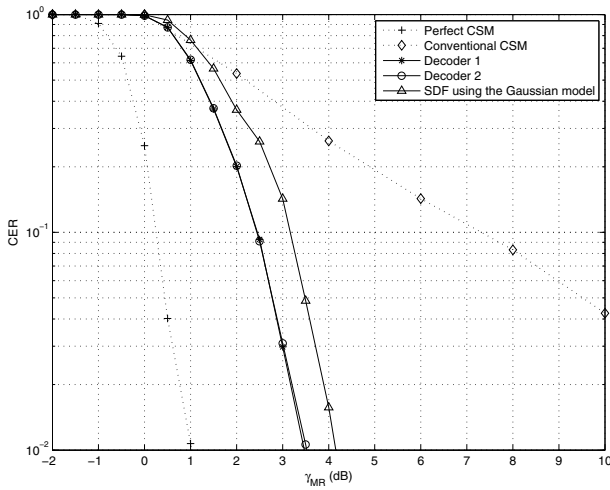


Fig. 3. CER versus SNR performance over a frequency-flat channel using $N_R = 2$, $N_B = 2$, $\gamma_{\Delta} = 6$ dB.

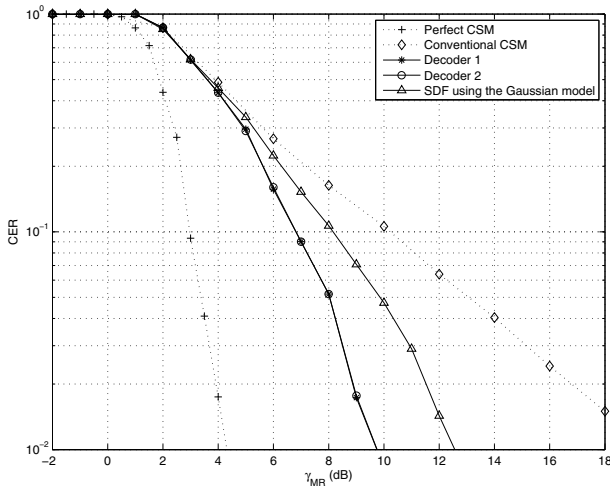


Fig. 4. CER versus SNR performance over a frequency-flat channel using $N_R = 2$, $N_B = 2$, $\gamma_{\Delta} = 18$ dB.

simulation results show that the proposed decoding algorithm designed for CSM systems provide substantial performance gains compared to the previously proposed algorithms, since the errors of the forwarded signals are taken into account with the aid of an accurate hard-valued error model. In order to achieve further improvements, the corresponding soft-decision forwarding strategy can be considered in our future work. By forwarding the soft-valued signals, which would more accurately indicate their reliability, the overall performance of CSM systems can be improved, provided that an accurate error model is employed.

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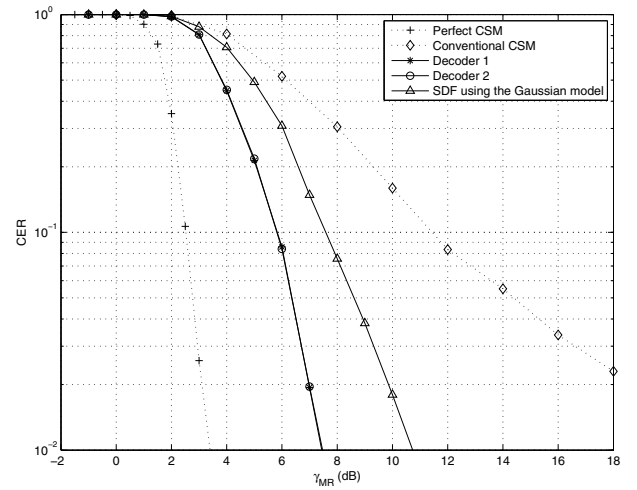


Fig. 5. CER versus SNR performance over a frequency-flat channel using $N_R = 4$, $N_B = 4$, $\gamma_{\Delta} = 18$ dB.

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