

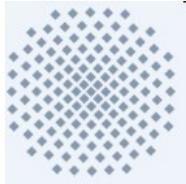


Interactive Realtime Multimedia Applications
on Service Oriented Infrastructures



QoS Provisioning and Orchestrating Processes within an SOA

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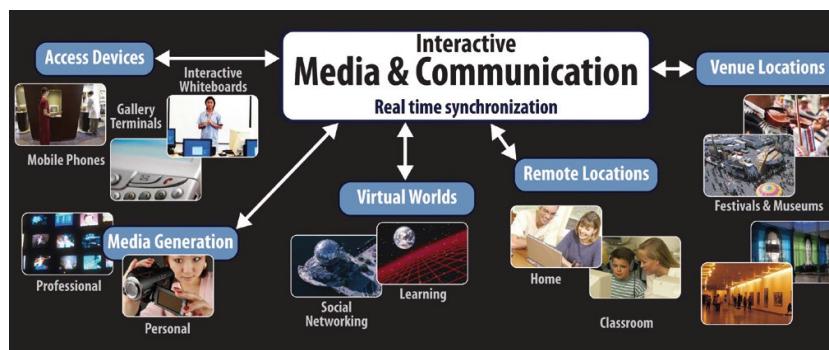
University Stuttgart



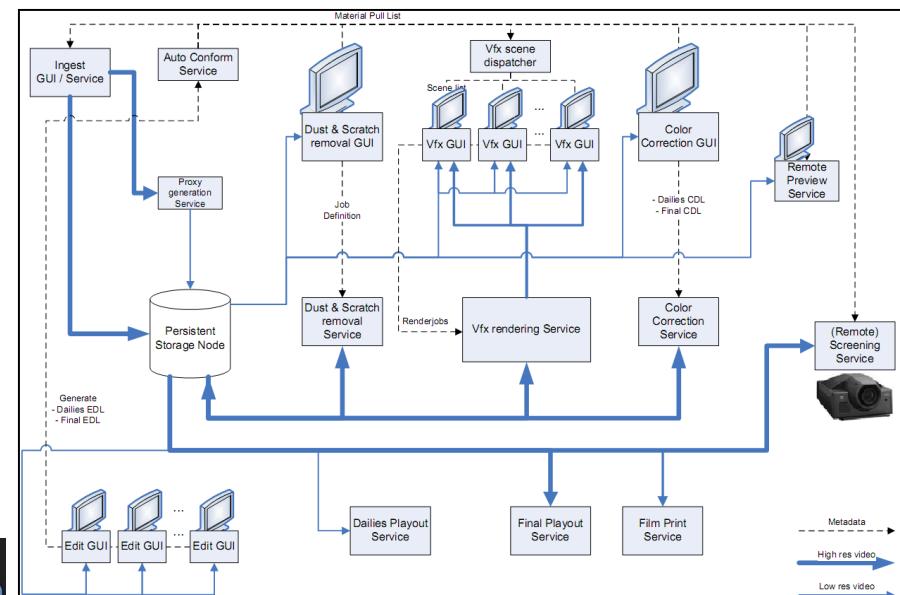
- Design, develop and validate a Service Orientated Infrastructure which will allow the adoption of interactive real-time applications, and especially multimedia applications



Augmented Reality



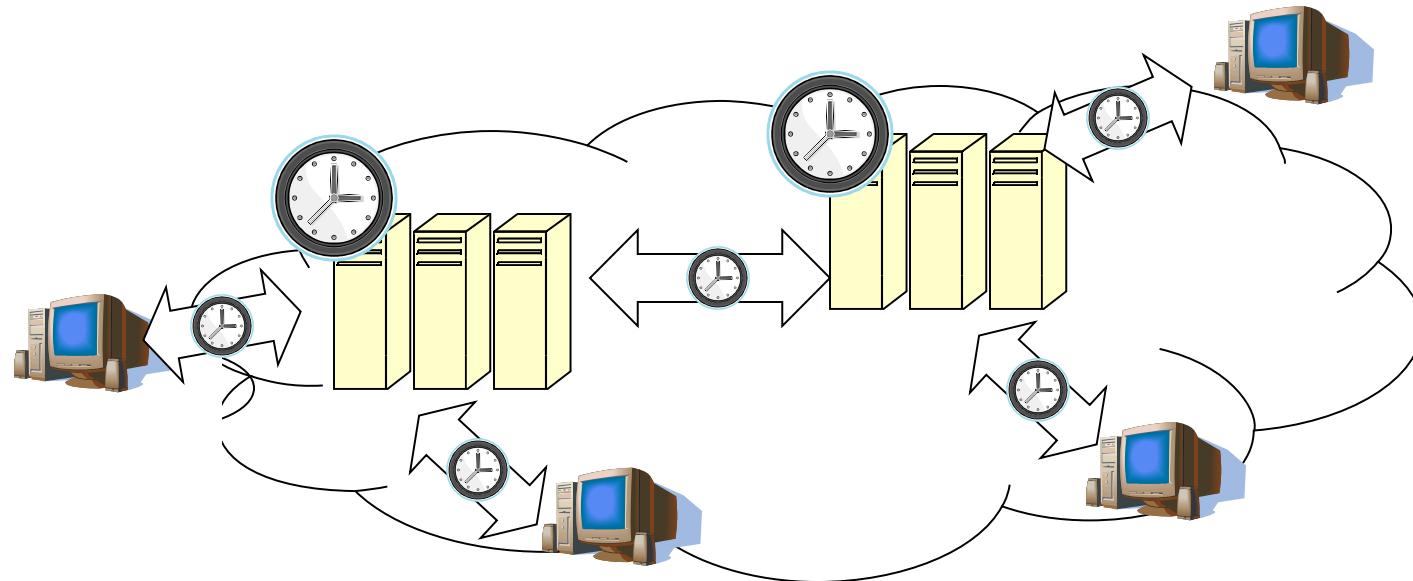
Social networking, education



Film post production

Intuition: think of distributed Amazon EC2 and S3 with guaranteed workflow and guaranteed realtime QoS

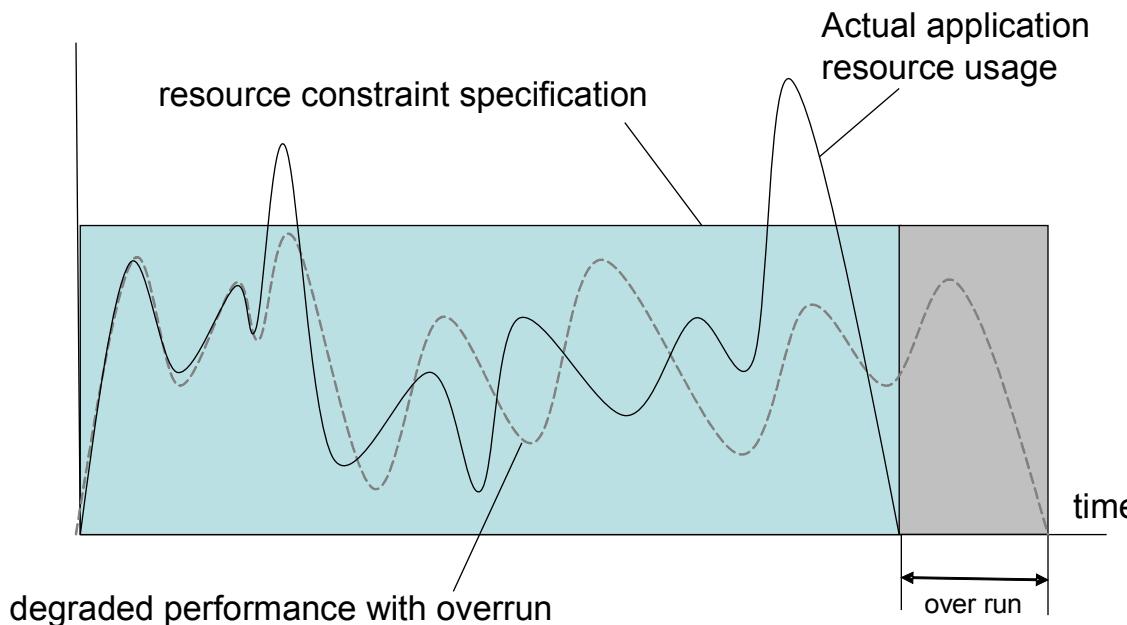
- Guaranteed virtual resource QoS:
processor, RAM, storage, bandwidth, latency, jitter, ...
- Guaranteed reservations:
resources will be available during reservation time frame
- QoS is monitored and verifiable during runtime



Questions for modelling and verification

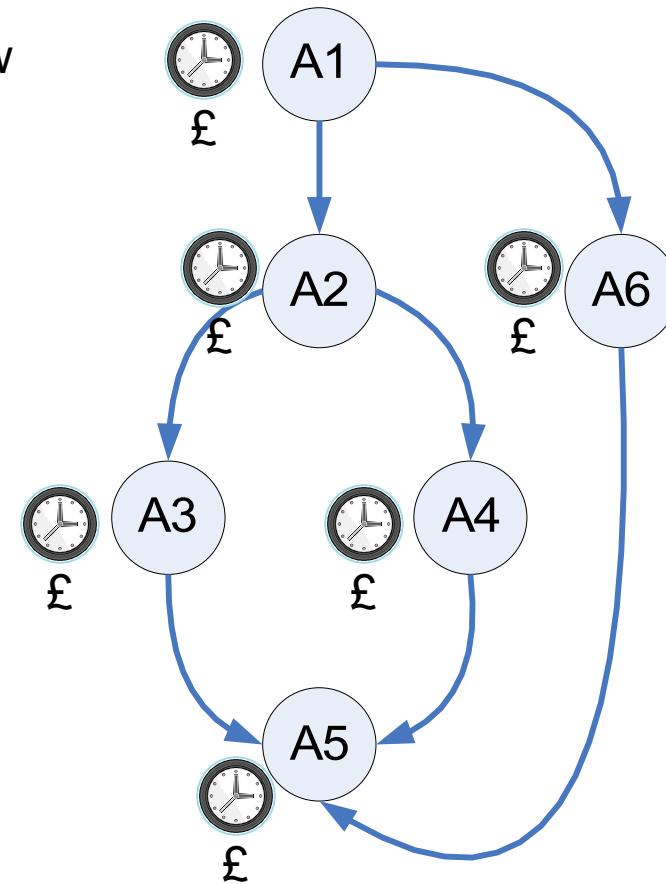
Before developing application into IRMOS service
Estimate performance characteristics

Why bother?
not possible to increase resources or time interval during execution



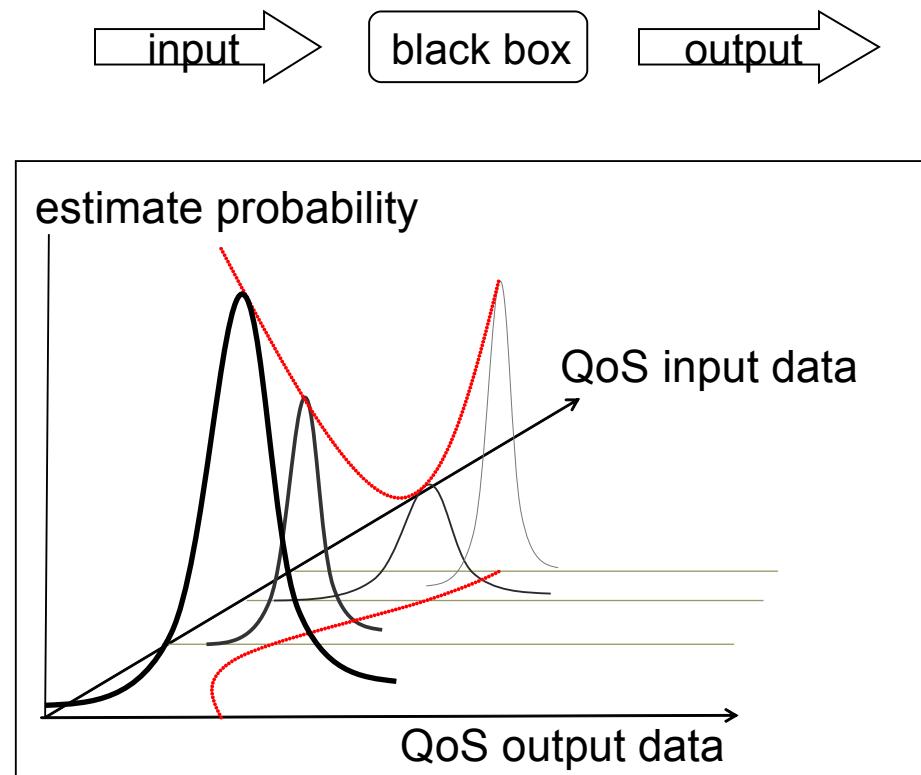
Before developing application

- Time frame reservations required for workflow and components
- Application workflow choreography; verified with respect to
 - resource contention,
 - resource utility,
 - causal dependencies,
 - deadlock,
 - livelock, etc,

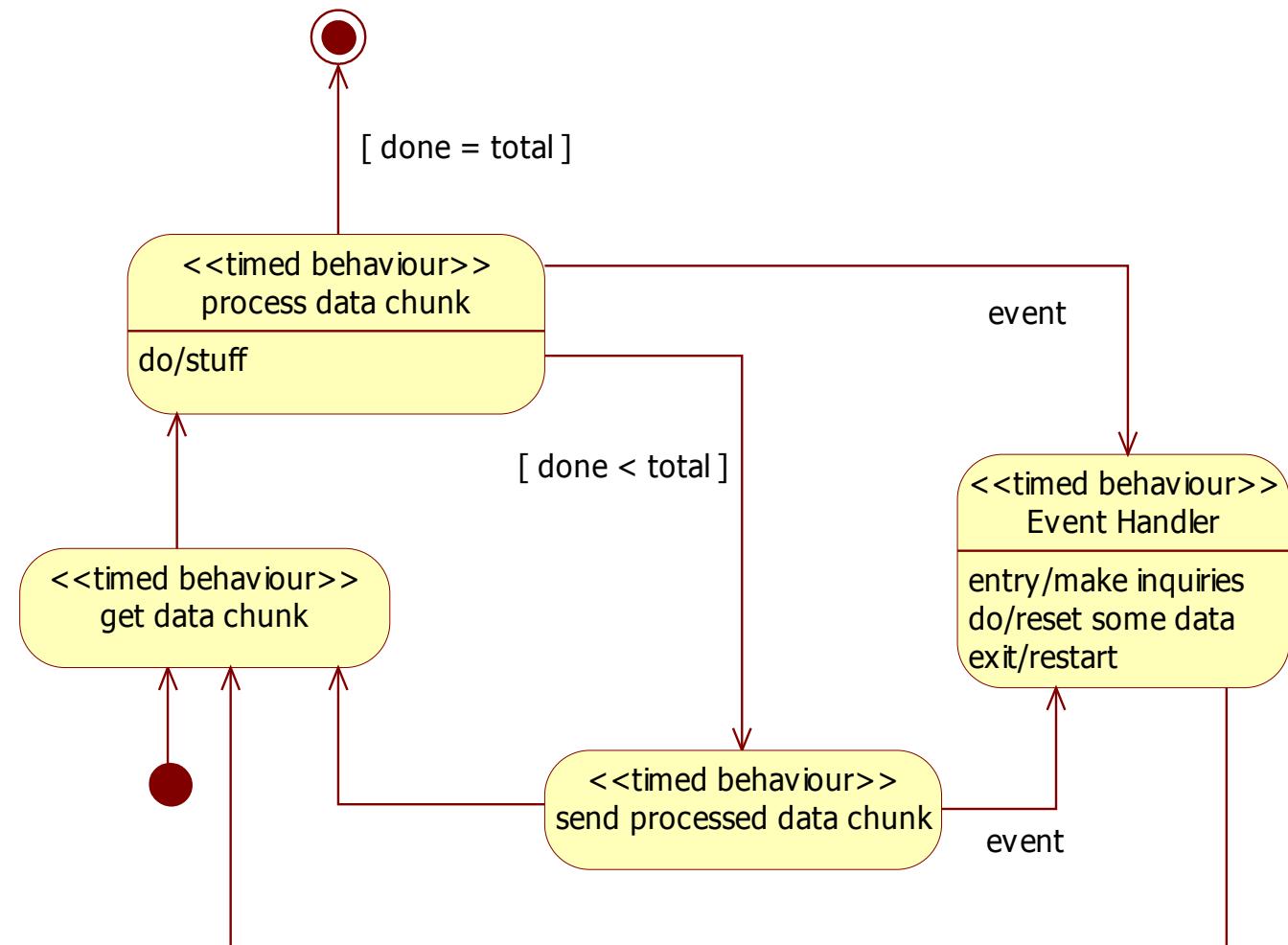


Black Box Process Component Performance

- Stochastic correlations from benchmarking and partial knowledge of algorithms.

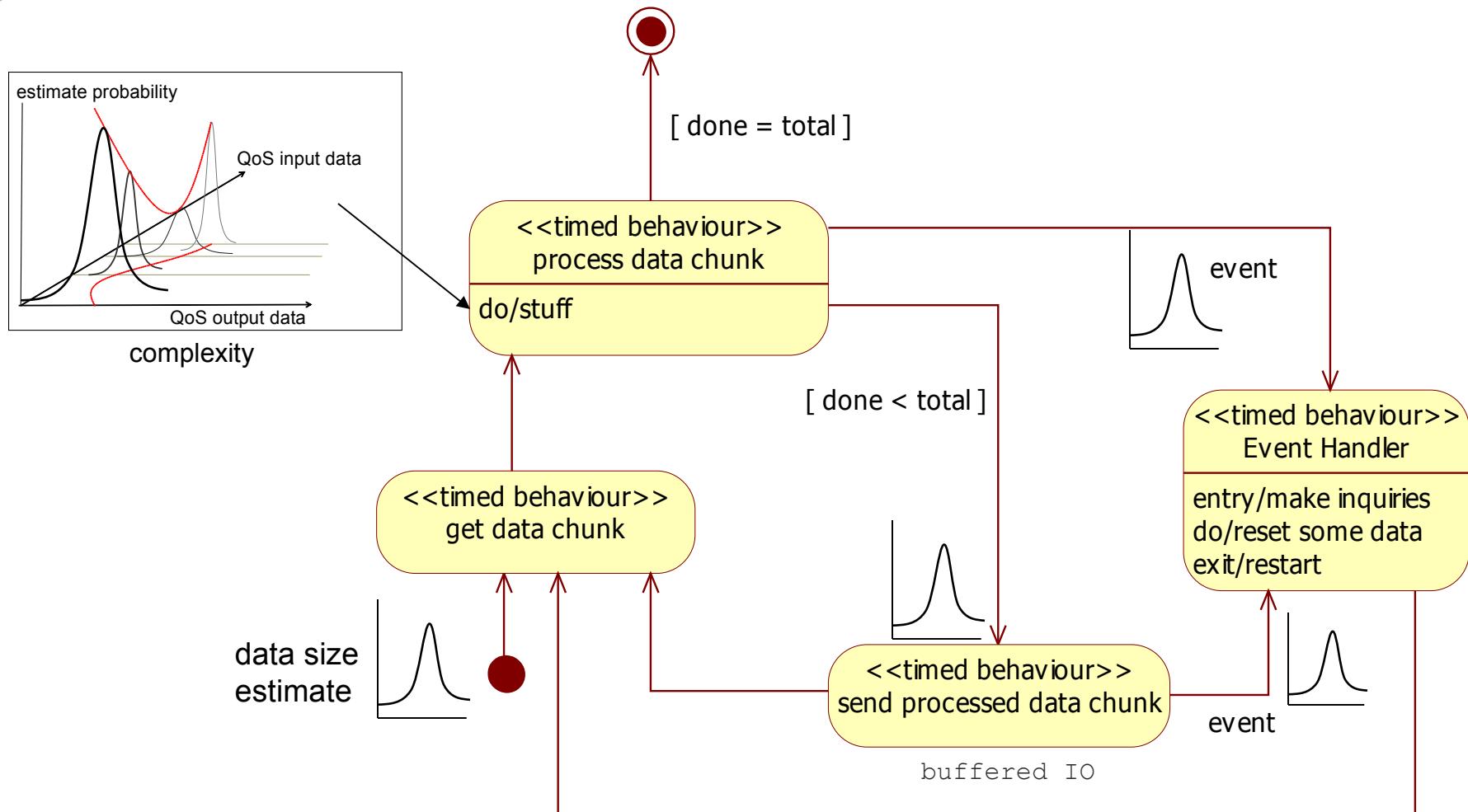


Streaming Real Time Processes



State machine pattern for streaming data

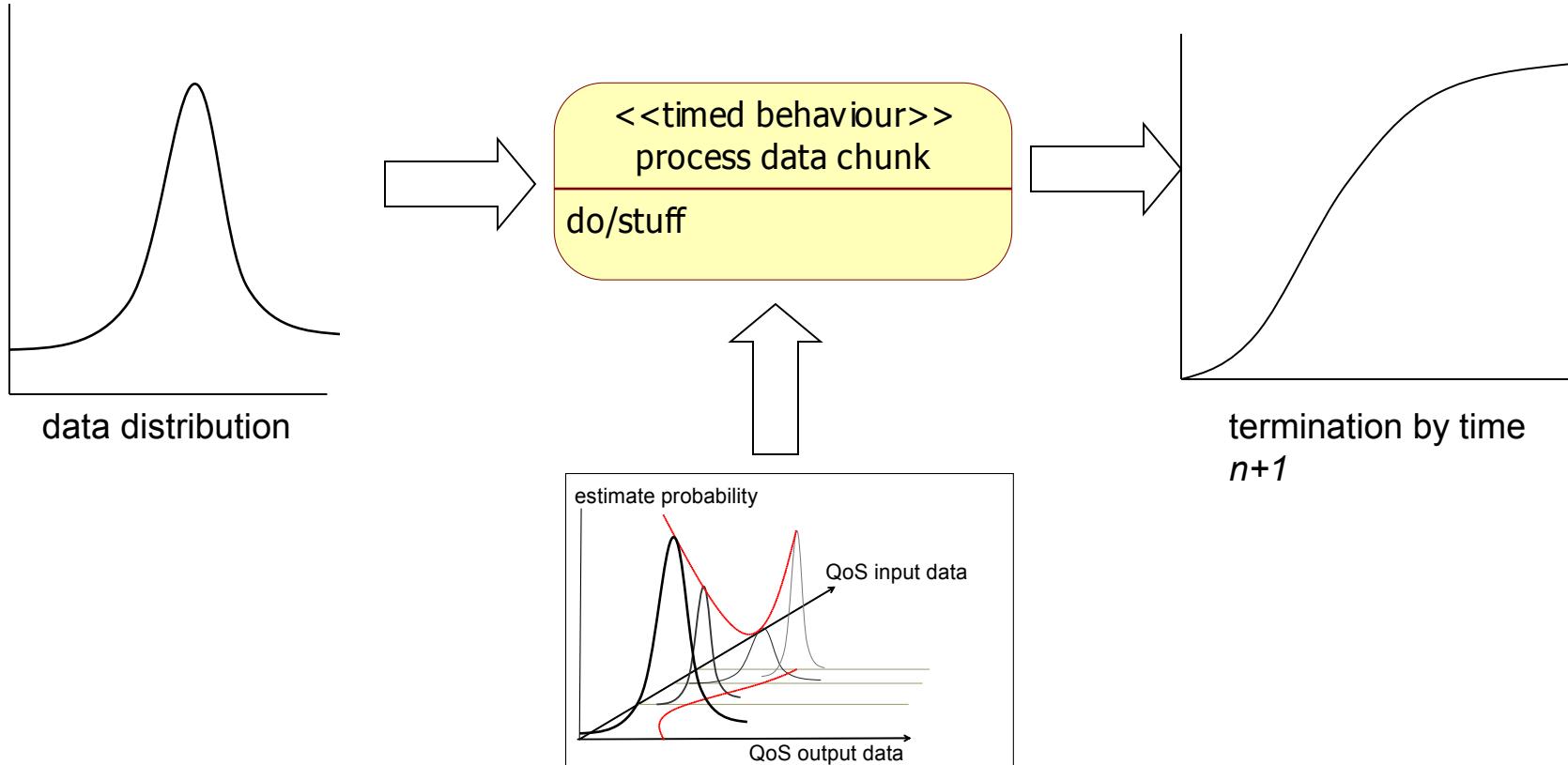
Streaming Real Time Processes



Stochastic interaction events and data

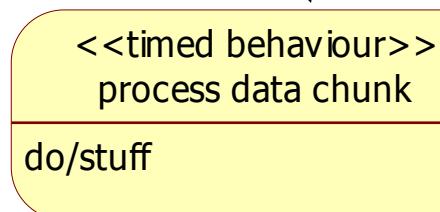
Termination Estimate

- Given stochastic complexity and input data
- If executing at time n what's probability of still running at $n+1$?

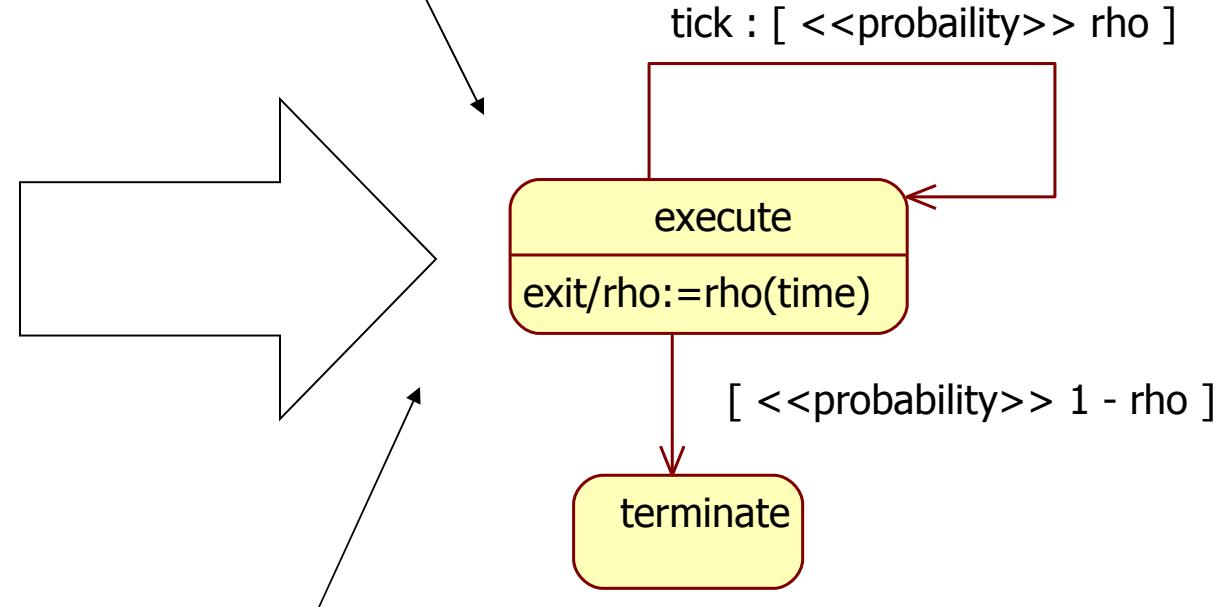


Discrete time stochastic automaton

Replace this



with this



- has standard semantics
- formally verify properties with stochastic model checkers
- can synchronise on stochastic events

rho(n) for known complexity

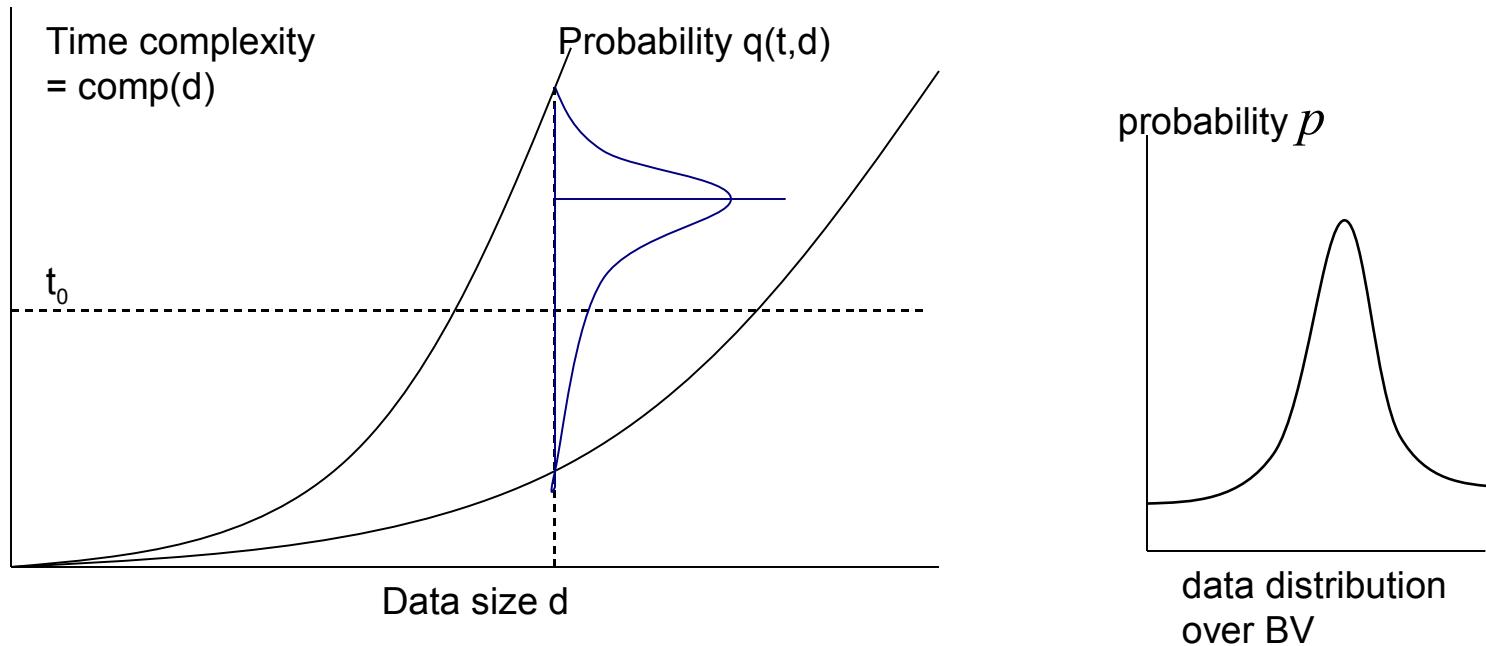
- Data is Borel measurable space BV
- Data estimates are probability measure p over BV
- Time to execute black box is $f(v)$ for v in BV
- Define

$$T(f, t) = \{v \in BV \mid f(v) > t\}$$

- If executing at time t , probability of still executing at $t+d$

$$\begin{aligned}
 \text{rho}(t + d) &= \frac{\int_{v \in T(f, t+d)} p(v) dv}{\int_{v \in T(f, t)} p(v) dv} = \frac{p(T(f, t + d))}{p(T(f, t))} \\
 &= \frac{\text{probability of complexity greater than } t+d}{\text{probability of complexity greater than } t}
 \end{aligned}$$

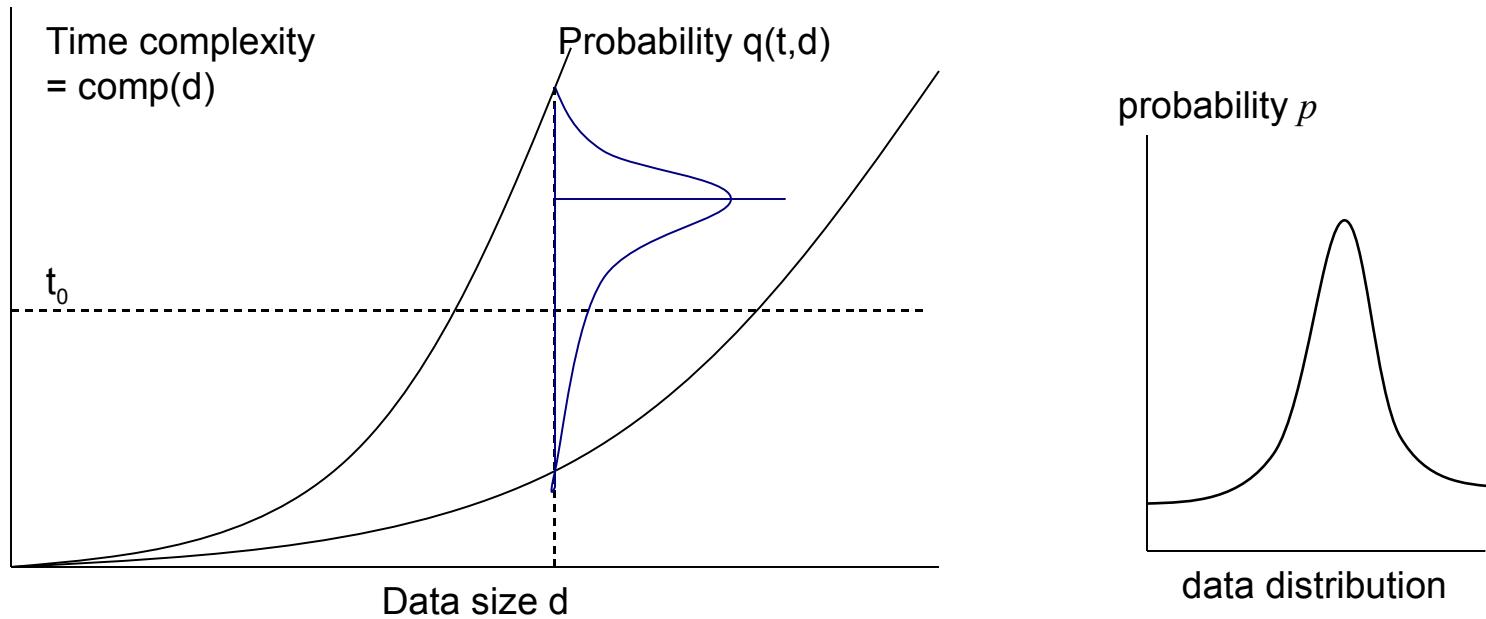
Estimated Complexity Discrete Time



$$\Pr(\text{comp}(d) > t \mid \text{input size is } d) = \sum_{t > t_0} q(t,d)$$

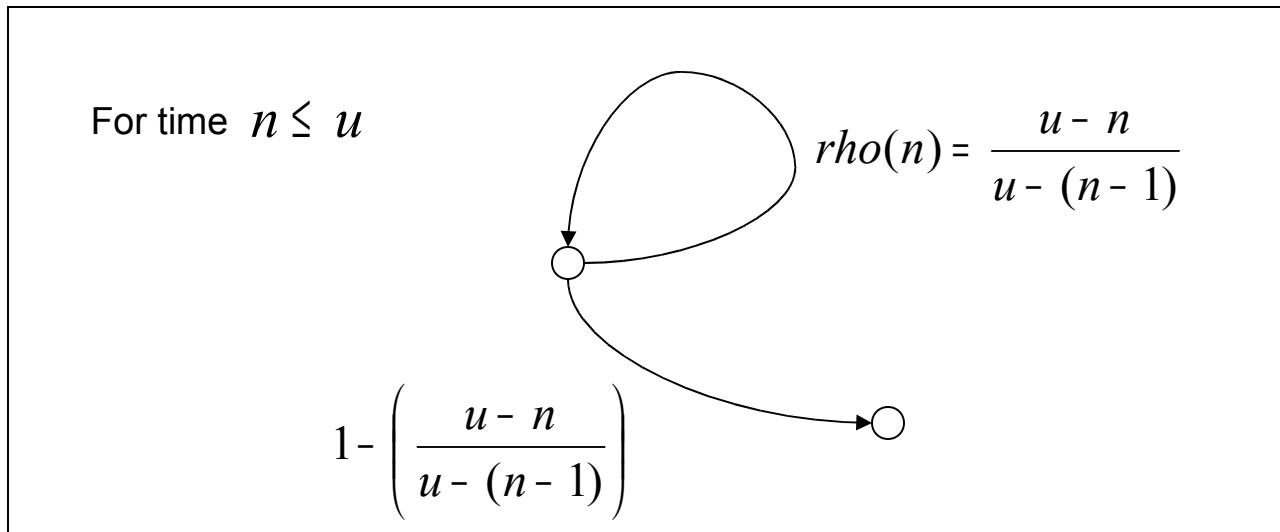
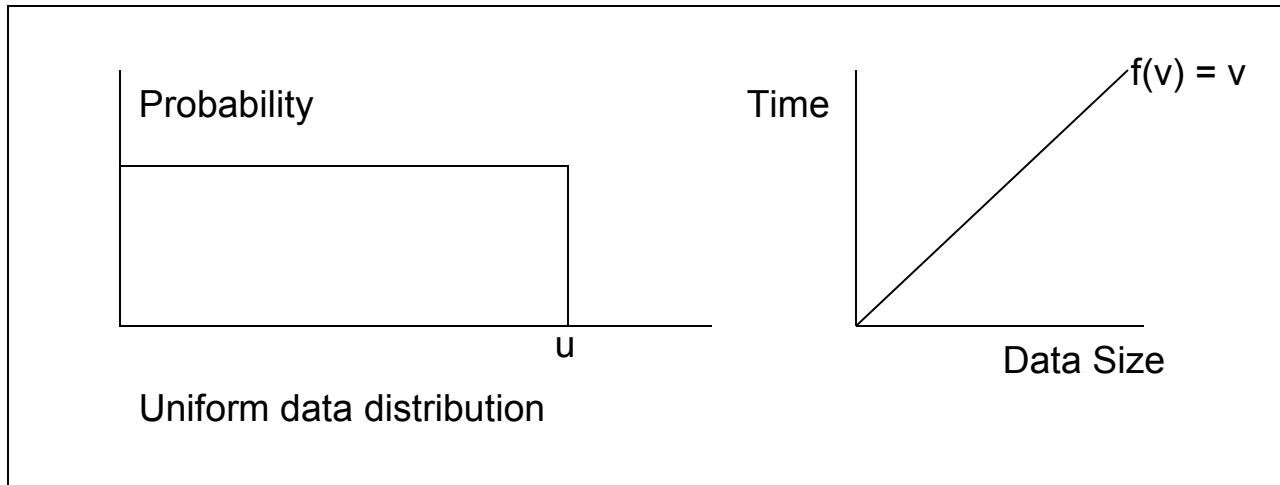
$$\Pr\{d \in BV \mid \text{comp}(d) > t\} = \int_{d \in BV} \left(\sum_{t > t_0} q(t,d) \right) dp$$

Estimated Complexity Discrete Time



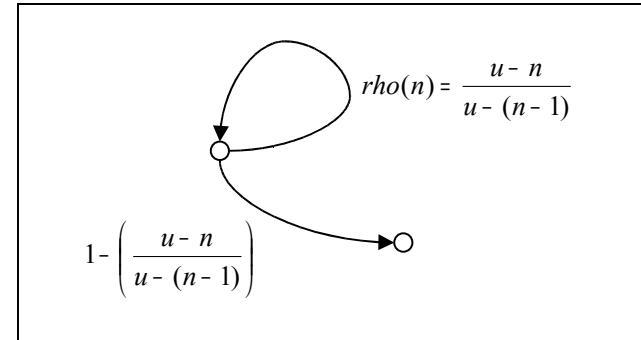
$$\rho(n) = \frac{\int_{d \in BV} \left(\sum_{t > n} q(t, d) \right) dp}{\int_{d \in BV} \left(\sum_{t > n-1} q(t, d) \right) dp}$$

rho(n) for uniform distribution linear complexity



Uniform plus linear termination estimate

Probability of terminating at time n

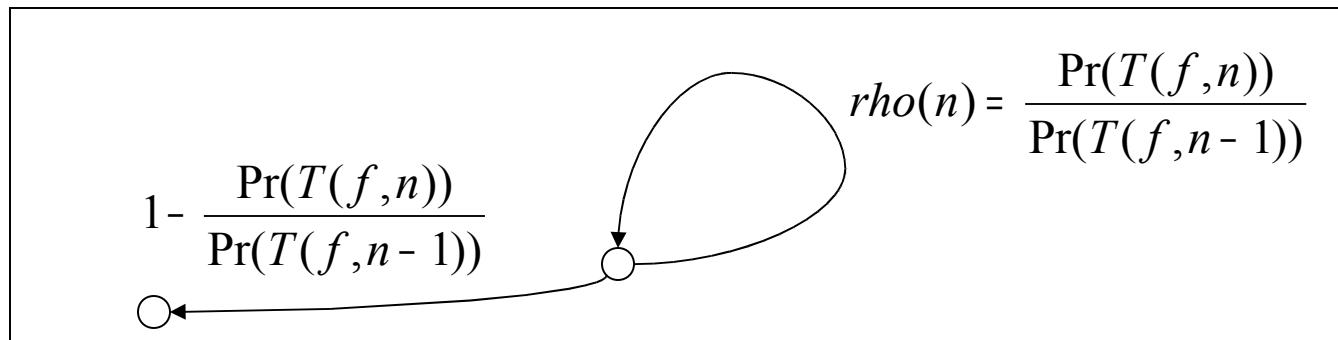


$$= rho(0) \cdots rho(n-2) rho(n-1) (1 - rho(n))$$

$$= \left(\frac{u-1}{u-0} \right) \left(\frac{u-2}{u-1} \right) \left(\frac{u-3}{u-2} \right) \cdots \left(\frac{u-(n-2)}{u-(n-3)} \right) \left(\frac{u-(n-1)}{u-(n-2)} \right) \left(1 - \frac{u-n}{u-(n-1)} \right)$$

$$= \left(\frac{u-(n-1)}{u} \right) \left(1 - \frac{u-n}{u-(n-1)} \right) = \frac{1}{u}$$

Exact complexity termination estimate



Estimate that automaton terminates at time $n =$

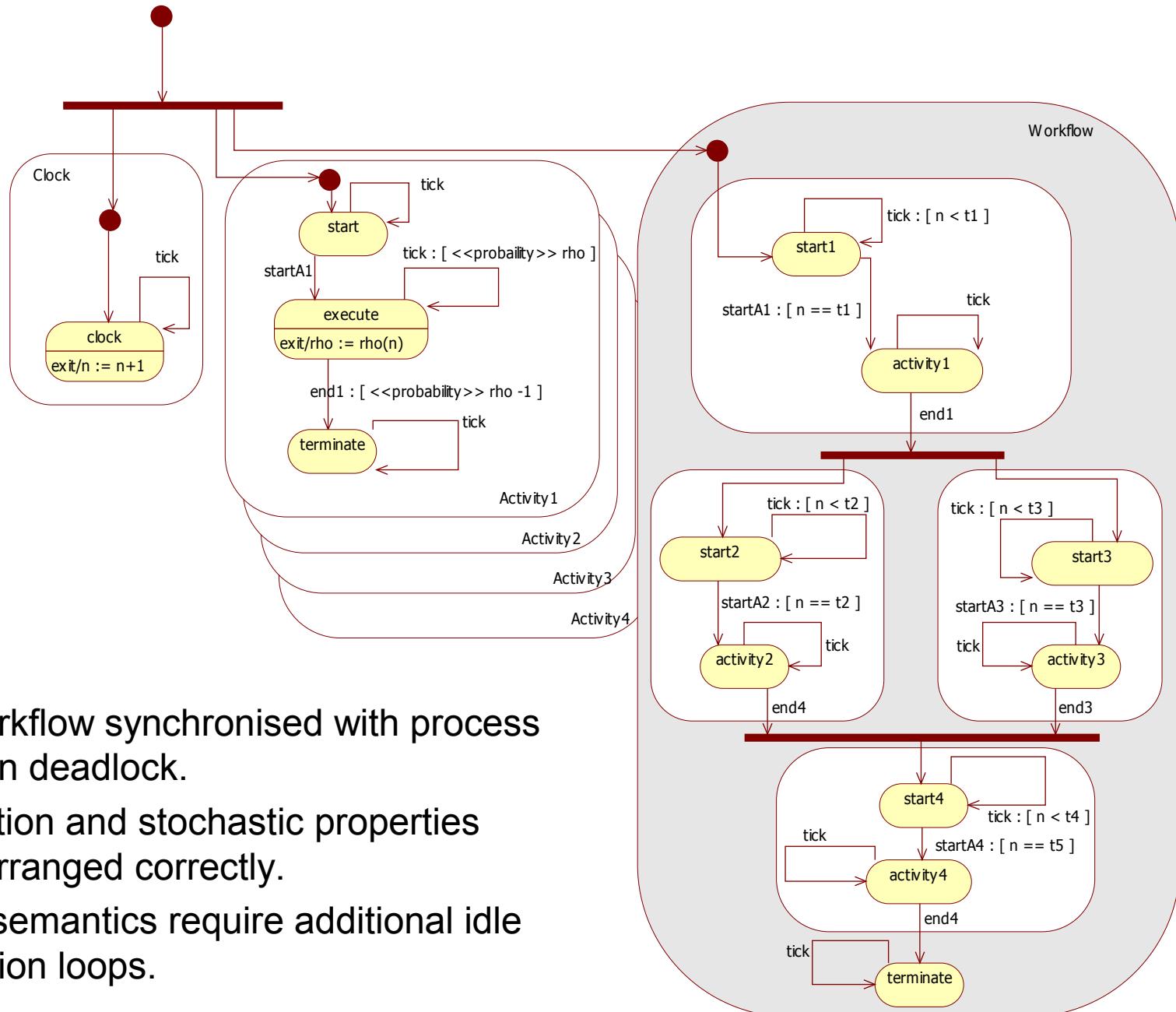
$$\Pr(T(f,0)) \left(\frac{\Pr(T(f,1))}{\Pr(T(f,0))} \right) \left(\frac{\Pr(T(f,2))}{\Pr(T(f,1))} \right) \left(\frac{\Pr(T(f,3))}{\Pr(T(f,2))} \right) \dots$$

$$\dots \left(\frac{\Pr(T(f,n-2))}{\Pr(T(f,n-3))} \right) \left(\frac{\Pr(T(f,n-1))}{\Pr(T(f,n-2))} \right) \left(1 - \frac{\Pr(T(f,n))}{\Pr(T(f,n-1))} \right)$$

$$= \Pr(f(d) > n - 1 \mid d \in BV) - \Pr(f(d) > n \mid d \in BV)$$

$$= \Pr(n \geq f(d) > n - 1 \mid d \in BV)$$

Elementary timed workflow



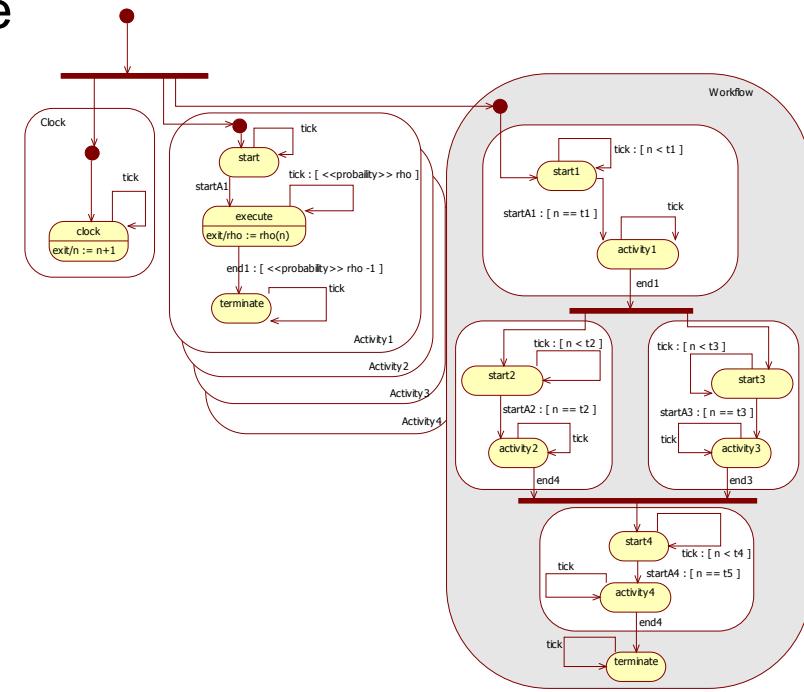
Arbitrary Workflow synchronised with process and clock can deadlock.

Synchronisation and stochastic properties have to be arranged correctly.

PRISM tool semantics require additional idle and termination loops.

Correct Workflow Semantics

- For any DAG workflow with consistent time frames
- For any black box process with given stochastic complexity and data
- There is a timed non-stochastic workflow automaton that
 - is deadlock free in composition with processes and clock
 - imposes correct causal dependencies between processes
- Extends to cyclic graphs by extending timed finite automata for black box processes
- Workflow can also be extended to allow for failure, cancellation and restarts among processes.



```

module Activity

[tick]      (x=idle) -> (x'= idle);
[startA]    (x=idle) -> (x' = go);
[]          (x=go) -> rho_iterate0:(x'=add_one_to_count)
              + (1 - rho_iterate0):(x'=terminate);
[]          (x=add_one_to_count) ->
              (x'=exec) & (count0'=incrmnt_count0);
[run]       (x=exec) -> (x'=return);
[tick]      (x=return) -> (x'=go);
[end]       (x=terminate) -> (x'=stop);
[tick]      (x=stop) -> (x'=stop);

endmodule

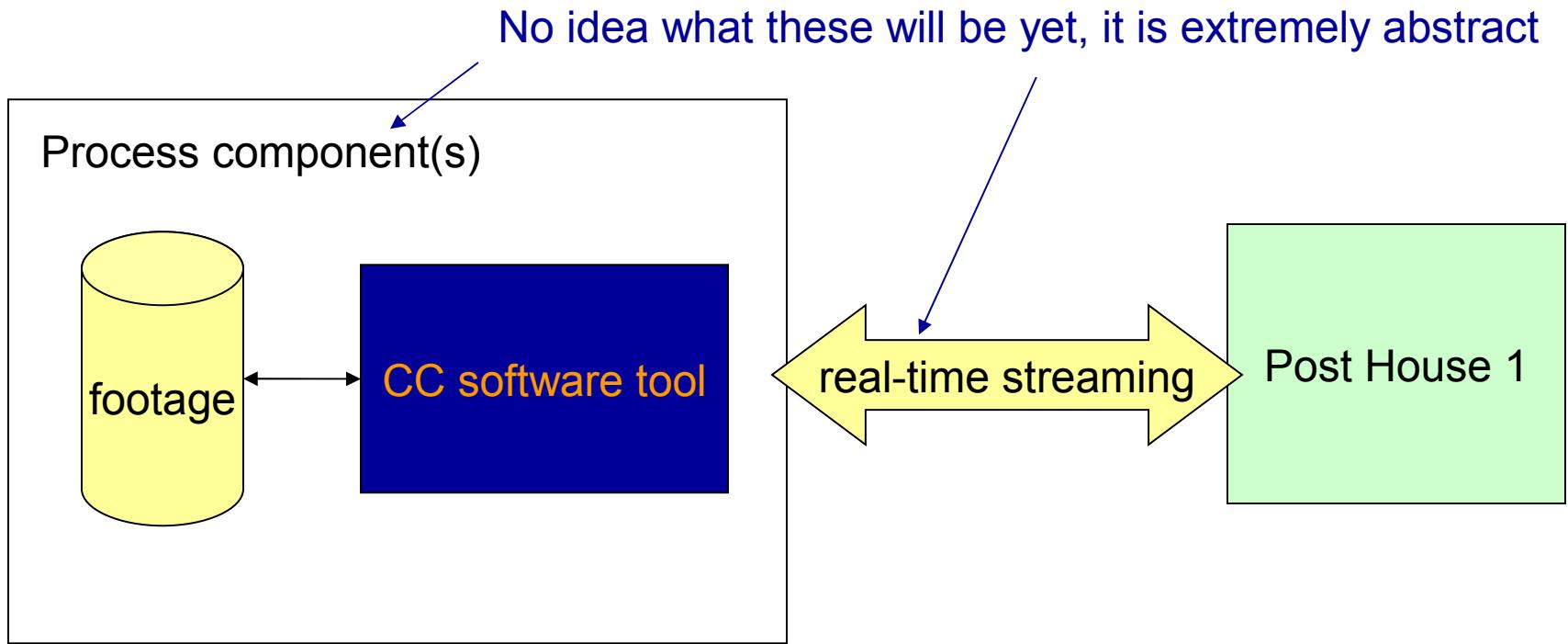
```

```

formula rho_itr0 = rho0*(1- count0/interval0) +
                  rho1*count0/interval0;
formula rho_iterate0 =
  ((count0 >= 0) & (count0 <= interval0)) ? rho_itr0 : rho1;

```

Colour Correction Conceptual Model

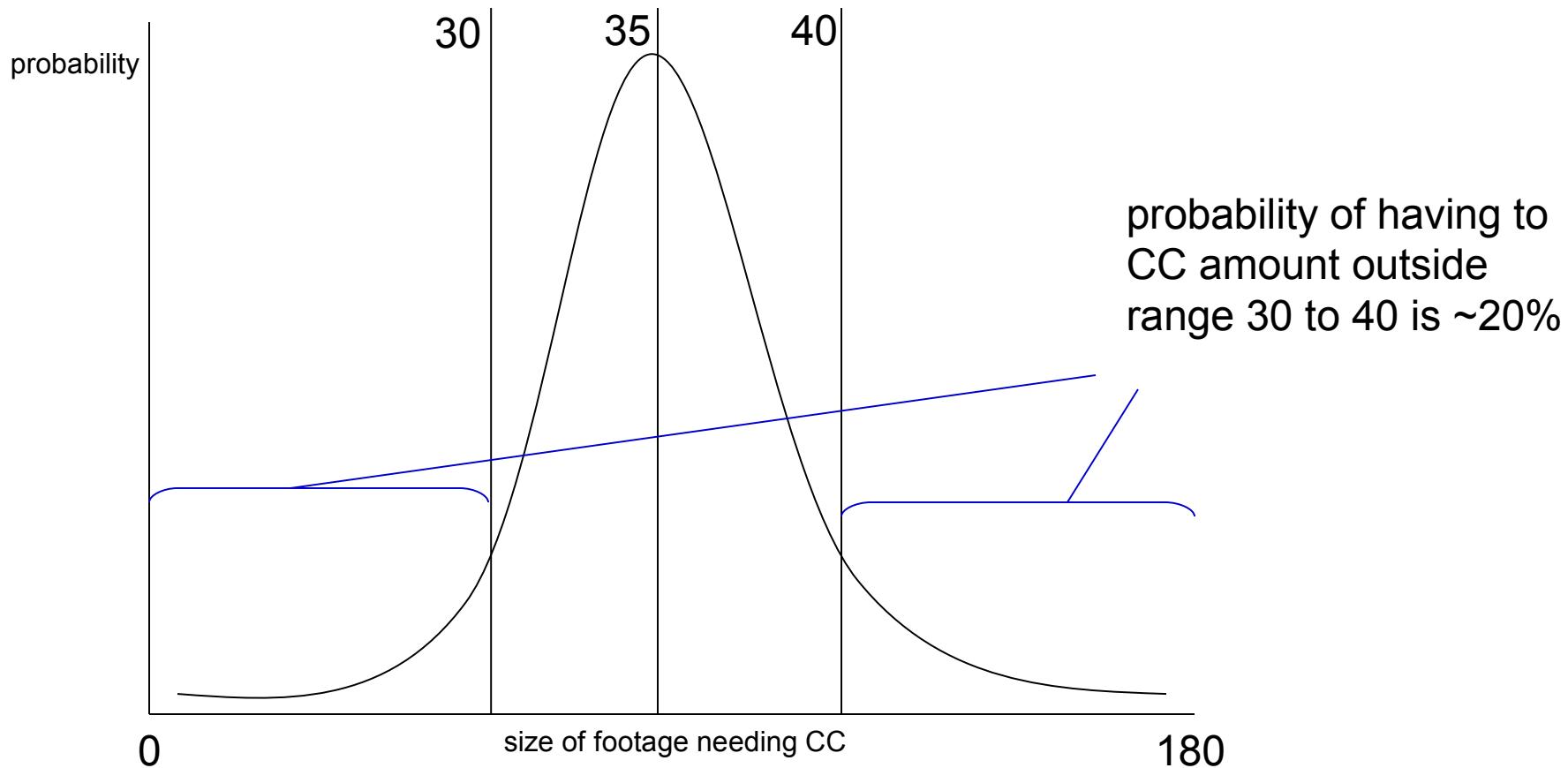


Conceptual level so we don't know

- What type of buffering exists
- How data is transcoded for data link
- How data link is shared
- How data link is managed

But we can make a model that gives predictions!

Stochastic Data



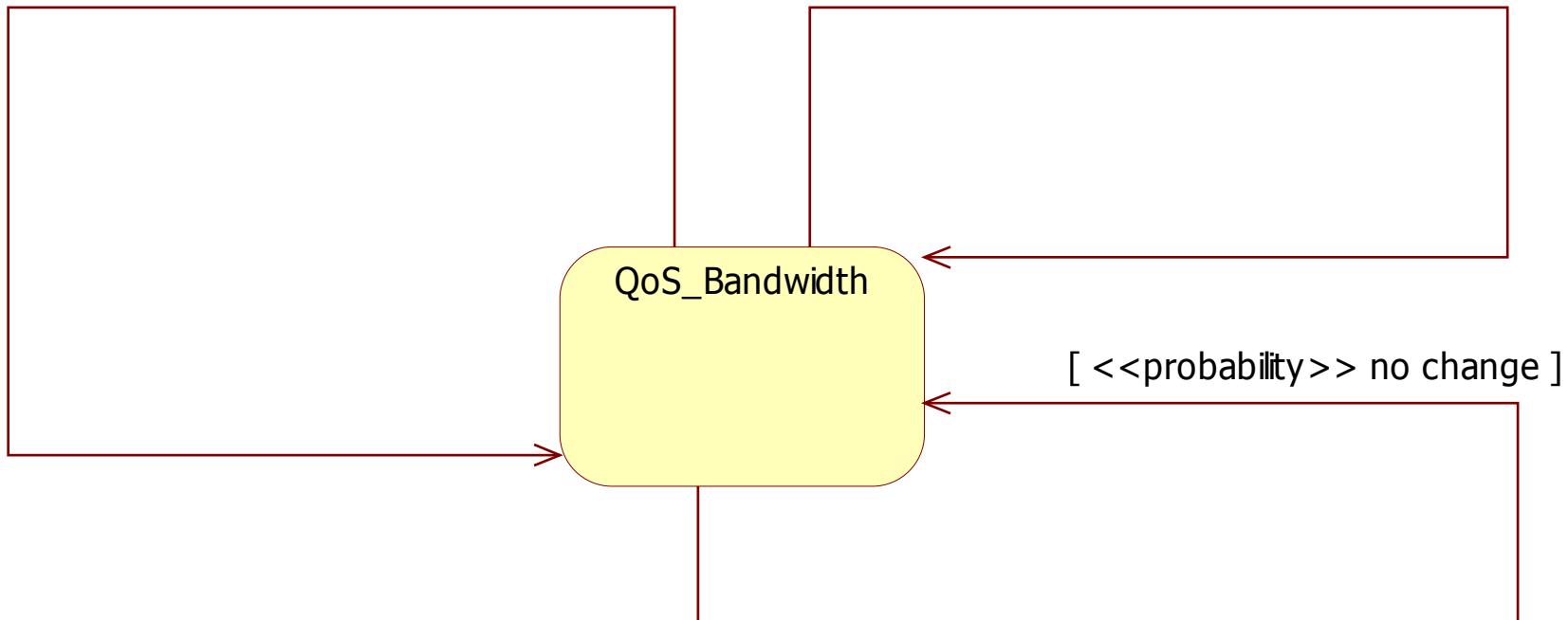
Black box complexity is linear

If bandwidth is 'too low' for continuous period (say 1 minute) rewind is necessary

QoS model of streaming data link

[<<probability>>down a bit] / subtract a bit

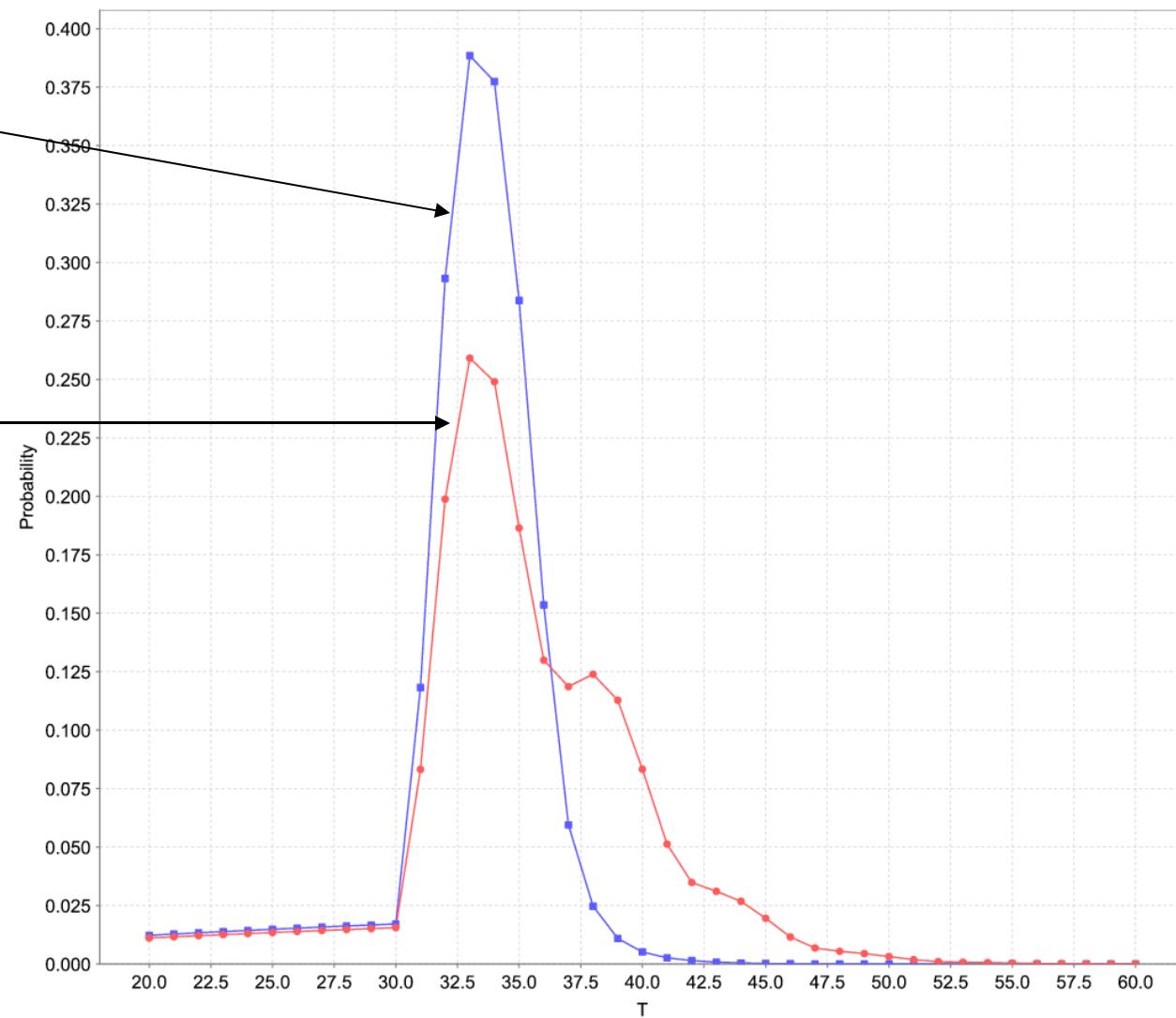
[<<probability>> up] / add a bit



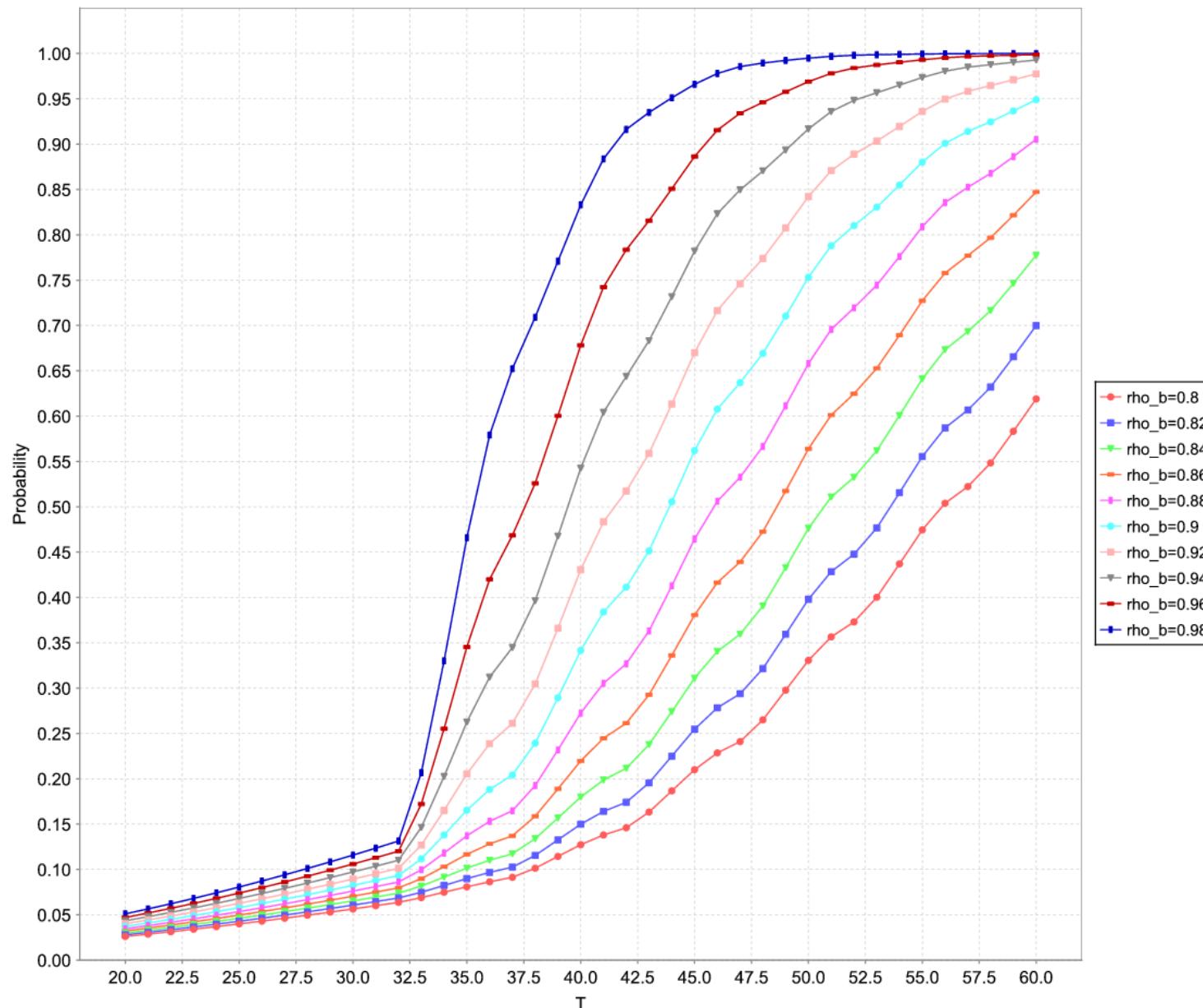
Predictions

If bandwidth
OK 100% of
time

If bandwidth
OK for 98% of
time



Predictions



□ Process terms

- $[t_0 < t < t_1] \rightarrow P$ if clock is in given range then do P
- $[?t < n : r=r'] P$ if clock t is less than n set r to r' then do P
- $\rho_1 \cdot P_1 + \dots + \rho_n \cdot P_n$ there is probability ρ_i that will do P_i
- $e \bullet P$ first do e next do P
- $P + Q$ do exactly one of P or Q depending on which is enabled
- $P \parallel Q$ interleave P and Q
- $P \parallel_S Q$ synchronous interleaving on event set S

Timed Black Box Process Term

$$\begin{aligned}
 \Pr(a) &= \Omega \cdot \Pr(a) + \text{start}_a \cdot \text{run}(a) + \text{cancel}_a \cdot \text{fail}_a \cdot 0 \\
 \text{run}(a) &= [t_0^a \leq t \leq t_1^a] \rightarrow (\rho_a \Omega \cdot \text{run}(a) + (1 - \rho_a) \cdot \text{done}_a \cdot 0) \\
 &\quad + ([t > t_1^a] \rightarrow \text{fail}_a \cdot 0) \\
 &\quad + (\text{cancel}_a \cdot \text{fail}_a \cdot 0) \\
 \text{Clock}_0 &= [: t = 0] \text{Clock} \\
 \text{Clock} &= [: t = t + 1] \Omega \cdot \text{Clock}
 \end{aligned}$$

Iterative Black Box Processes

$$\begin{aligned}
 \mathsf{Pr}(a) &= \Omega \cdot \mathsf{Pr}(a) + \mathsf{start}_a \cdot \mathsf{getrs}(a) + \mathsf{cancel}_a \cdot \mathsf{fail}_a \cdot 0 \\
 \mathsf{getrs}(a) &= ([r_a = \mathsf{f}] \rightarrow \Omega \cdot \mathsf{getrs}(a)) + ([r_a = \mathsf{t}] \rightarrow [: r_a = \mathsf{f}] \mathsf{rn}_a \cdot \mathsf{run}(a)) \\
 \mathsf{run}(a) &= [t_0^a \leq t \leq t_1^a] \rightarrow (\rho_a \Omega \cdot \mathsf{run}(a) + (1 - \rho_a) \cdot [: r_a = \mathsf{t}] \mathsf{done}_a \cdot \mathsf{iter}(a)) \\
 &\quad + ([t > t_1^a] \rightarrow [: r_a = \mathsf{t}] \mathsf{fail}_a \cdot 0) \\
 &\quad + (\mathsf{cancel}_a \cdot [: r_a = \mathsf{t}] \mathsf{fail}_a \cdot 0) \\
 \mathsf{iter}(a) &= (\mathsf{exp}(a) \mapsto \mathsf{Pr}(a)) \parallel_{\mathcal{S}_y} \prod_{a' \in \mathsf{nxt}(a, G)} (\mathsf{exp}(a') \mapsto \mathsf{start}_{a'} \cdot 0)
 \end{aligned}$$

