

# A Formal Method for Modeling, Verification and Synthesis of Embedded Reactive Systems

Ruiter Braga Caldas

*Universidade Federal do Amazonas*

*Av. Rodrigo Otávio, nº 6.200, Coroado, Manaus-Brazil.*

*ruiter@dcc.ufam.edu.br*

Raimundo da Silva Barreto

*Universidade Federal do Amazonas*

*Av. Rodrigo Otávio, nº 6.200, Coroado, Manaus-Brazil.*

*rbarreto@dcc.ufam.edu.br*

Lucas Cordeiro

*Universidade Federal do Amazonas*

*Av. Rodrigo Otávio, nº 6.200, Coroado, Manaus-Brazil.*

*lucascordeiro@ufam.edu.br*

Sérgio Campos

*Universidade Federal de Minas Gerais*

*Av. Antônio Carlos, 662, Pampulha, BeloHorizonte-Brazil.*

*scampo@dcc.ufmg.br*

## ABSTRACT

Embedded reactive systems are now invisible and everywhere, and are adopted, for instance, to monitor and control critical tasks in cars, airplanes, traffic, and industrial plants. However, the increasing amount of new functionalities being moved to software leads to difficulties in verifying the design correctness. In this context, we propose a novel design method called *BARE Model*, which is a formal abstraction to design, verify and synthesize software in embedded reactive applications. The method consists in designing the application using an extension of the well-known finite state machine, called X-machine. We thus propose to translate this model to a tabular data structure, which is a kind of state transition table augmented with memory input, memory output, and condition (or guard). This tabular structure may be automatically translated to the input of the NuSMV model checker in order to verify the system's properties. We also propose a runtime environment to execute the system (expressed as a tabular data structure) in a specific platform. In this way, we can convert the high-level specification into executable code that runs on a target platform. To show the practical usability of our proposed method, we experimented it with the Envirottrack case study. The experiment shows that the proposed method is able to not only model the system, but also to verify safety and liveness properties, and synthesize executable code of real-world applications.

## KEYWORDS

Formal Methods, Model Checking, Embedded Systems.

## 1. INTRODUCTION

Reactive systems are those that maintain an ongoing interaction with its environment rather than to compute some final value and terminate [17]. In this way, reactive systems have to react to stimuli produced by the environment. When these systems perform a specific function and is part of a larger system they are called embedded reactive systems. We advocate that embedded reactive systems are now invisible and everywhere. They are used to monitor and control important functions in cars, airplanes, industrial plants, bank accounts, and even patients in the hospital. If we consider critical applications, where an error can lead to a catastrophe (for instance, loss of human life), the control quality assurance plays an important role to ensure that risks are minimized and kept under control. However, in order to achieve this goal, rigorous methods and techniques must be used to develop and verify those system.

Embedded reactive systems are usually defined by a data acquisition stage, application of an algorithm, followed by output of a result. The development process of these systems needs to ensure that the behaviour of the software is well controlled, even in the presence of unusual combinations of external stimuli and failures. In this context, Finite States Machine (FSM) can be used to capture the system's behaviour in a high-level of abstraction and to make it possible to reason about the system's properties via model checking [2]. In reactive systems, for example, the application is usually built by combining different FSMs, but this combination lacks the ability to model non-trivial data structures that arise from real-world applications [7]. In order to alleviate this problem, X-machine extends the FSM by introducing memory concepts, and functions that operate on input symbols and memory values. This work makes two major novel contributions. First, we propose the use of the formal model *BARE*<sup>1</sup> as the model to design embedded reactive applications. This model is used to describe the behaviour at a high-level of abstraction using the X-machines formalism so that we can transform it into a tabular model and later upload it into the target platform to be executed by a specific runtime environment. From the tabular model, a specific "system model" maybe generated and some properties (e.g., safety and liveness) can be verified using a model checker to ensure the correctness of the application; in particular, this work adopted the NuSMV model checker. Second, X-machines are static mathematical models, which do not support the notion of *events* and *conditions*. Consequently, we modified and added these two new elements into the original model of the X-machine. In this case, events are fired whenever a change occurs in the values of the variables under observation. Conditions are logical expressions dependent on events, which are composed by memory variables and are linked by logical connectors. As a result of this modification, our proposed method may be effective in the modeling, verification and synthesis of real-world embedded reactive applications.

## 2. X-MACHINE

X-machine is a mathematical device that is capable of modeling both data-flow and control-flow of a system. It employs a diagrammatic approach to model the control-flow by extending the expressive power of FSM. X-machine has been proposed independently by the mathematician Eilenberg [6] and used by other researchers as a specification language for dynamic systems [7]. In an X-machine model, transitions between states are no longer performed through simple input symbols, but by the application of functions. Functions ( $\phi$ ) receive input symbols ( $\sigma$ ) and memory values ( $m$ ) and produce output symbols ( $\gamma$ ) and may modify memory values. In contrast to FSM, X-machines are capable of modeling non-trivial data structures by employing a memory, which is attached to the X-machine. Consequently, in the X-machine model, transitions are associated to functions, or relations, that act on a data structure. One of these subclasses proposed by Laycock [14] is the *Stream X-machine* in which the inputs and outputs are performed through a data stream. In the formal description, a deterministic Stream X-machine, denoted by  $\text{XM} = (\Sigma, \Gamma, Q, M, \Phi, F, q_0, m_0)$ , is a eight tuple such that: (i)  $\Sigma$  is the input alphabet; (ii)  $\Gamma$  is the output alphabet; (iii)  $Q$  is the finite set of states; (iv)  $M$  is the (possibly) infinite set of values of variables in memory; (v)  $\Phi$  is a machine type of  $M$  comprising a finite set of partial functions  $\phi$  that map a memory and an input to a new memory and an output; (vi)  $F$  is a partial function of the next state, given a state and a function of the type  $\Phi$ , it denotes

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1 Available at <http://www.dcc.ufam.edu.br/ruiter/index.php/br/projetos>

the next state.  $F$  normally is described as a diagram of state,  $F : Q \times \Phi \rightarrow Q$ ; (vii)  $q_0$  is the initial state; and (viii)  $m_0$  is the initial values of variables in memory. Section 4 shows an example of modeling with X-Machine.

### 3. THE PROPOSED METHOD

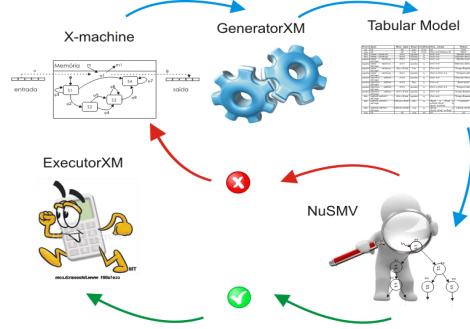


Figure 1. Overview of Bare Model

Figure 1 shows the proposed development cycle of embedded reactive applications. We start by modeling the system using an extension of the X-Machine model that deals with embedded reactive systems; this extension is called *BARE* model. Considering that the *BARE* model is not executable, after the modeling phase we call the *GeneratorXM* which aims to transform the *BARE* model to a tabular model. The tabular model may be executed by a runtime environment, in this method called *ExecutorXM*. The proposed method also provides means to verify formally the properties of the system. Therefore, it is possible to translate from the tabular model to a specific input of a model-checker, in this case, we adopt the NuSMV model-checker. The main parts of the proposed method are described in the following subsections.

#### 3.1. The BARE model

The *BARE* model extends the X-Machine model specifically to deal with embedded reactive systems. In this context, we consider that all applications are composed by three main components: (1) *Sensor*, which is responsible for providing data to the application. This data generation can be time-triggered or event-triggered; (2) *Transformer*, which is responsible for implementing each application requirement; and (3) *Communicator*, which is responsible for all aspects related to send data to other devices. We propose to adopt X-machines for both Sensors and Communicators and consequently connecting them as an unique component. In this paper, however, we focus mainly on the transformer component, which is targeted to embedded reactive applications and is developed in a domain-specific basis. All three parts are further placed together into a single application for execution on a embedded platform. The *BARE* model extends the X-Machine model in the following way:  $BM = (T, \Sigma, \Gamma, \Lambda, Q', M, E, C, \Phi, F, q_0, m_0)$  where:

- $T$  is a set of basic data types.
- $\Sigma$  is the input alphabet, which is called *monitored variables*.
- $\Gamma$  is a set of output alphabet. This definition is the same as the X-Machine.  $\Gamma$  is called *controlled variables*.
- $\Lambda$  is a set of internal alphabet or *internal variables*.

- $Q' = Q \cup \{Init, Start, Halt\}$ , is the set of states. The purpose of the states *Init*, *Start*, *Halt* is to perform initial configuration (state *Init*) or initialization (state *Start*), and indicate when the application terminates (state *Halt*). We propose that the first state to be executed in any application is always the state *Init*, and after the state *Start*.
- $M$  is the set of values of variables in memory. This definition is the same as the X-Machine.
- $E$  is the set of Events. Events may be fired whenever a change occurs in the value of the variables (monitored, controlled, internal).
- $C$  is the set of Conditions. Conditions are logical expressions that rely on events. They are composed by variables from memory and linked by logical connectors.
- $\Phi$  is a finite set of partial functions  $\varphi$ , that transforms an input alphabet and a value of memory into an output alphabet and a new value of memory, enabled by a condition when an event occurs.  $\varphi : \Sigma \times M \times C \rightarrow \Gamma \times M$ .
- $F$  is a partial function of the next state, given a state and a function of the type  $\Phi$ , it denotes the next state.  $F$  normally is described as a diagram of state,  $F : Q \times \Phi \rightarrow Q$ .
- $q_0 \in Q'$  is the *Init* state. This definition is the same as the X-Machine.
- $m_0 \in M$  is the initial values of variables in memory. This definition is the same as the X-Machine.

### 3.2. Mapping the BARE Model to the Tabular Model

The *BARE* model is a specification model and, therefore, it is not executable. The next step on the proposed method is to transform the *BARE* model into a tabular model. This tabular structure is constructed with the aim to transform a specification model to a executable model, in such a way to make it easy to execute the application on the target platform. This kind of tabular model has been used for several years as a tool for software specification [3, 9, 11], with the aim of making systems more readable and understandable. The transformation from the *BARE* model to the tabular model is performed automatically by a specific tool called *GeneratorXM*. The columns of the application table are filled in with the information obtained directly from the *BARE* model. The resulting table is composed by the following columns: **(i)** *Source* represents the initial states of the transitions. The *Source* column should contain all states including the states *Init*, *Start*, *Halt*. The transitions between states are controlled by events. As  $s_j = F(s_i, \varphi_i)$ . In this case, this column should contain all  $s_i \in Q'$ ; **(ii)** *Input* contains the input event to be considered in the transition between states. As  $\langle \gamma_k, m_{k+1} \rangle = \varphi_k(\sigma_k, m_k, c_k)$ , the *Input* column should contain all  $\sigma_k \in \Sigma$ . **(iii)** *Mem\_input* are internal variables values that will be considered in the condition to enable state transitions. As  $\langle \gamma_k, m_{k+1} \rangle = \varphi_k(\sigma_k, m_k, c_k)$ , the column should contain all  $c_k \in C$ ; **(iv)** *Target* is the target state of transitions. As  $s_j = F(s_i, \varphi_i)$ . In this case, the *Target* column should contain all  $s_j \in Q'$ ; **(v)** *Condition* is the condition to be evaluated in order to enable the transition from the *current* state to the *target* state. The conditions are synchronized by the input events. As  $\langle \gamma_k, m_{k+1} \rangle = \varphi_k(\sigma_k, m_k, c_k)$ , the *Condition* column should contain all  $c_k \in C$ ; **(vi)** *Mem\_output* are internal variable values of the machine that will be updated if the transition is taken when the condition  $c_k$  is satisfied. As  $\langle \gamma_k, m_{k+1} \rangle = \varphi_k(\sigma_k, m_k, c_k)$ , the column *Mem\_output* should contain all  $m_{k+1} \in M$ ; **(vii)** *Output* is the value produced as a result of the transition between states. The output may trigger some other event or produce some output data. As  $\langle \gamma_k, m_{k+1} \rangle = \varphi_k(\sigma_k, m_k, c_k)$ , the *Output* column should contain all  $\gamma_k \in \Gamma$ .

### 3.3. Formal Verification of Tabular Model

The technique chosen to verify the system is model checking [12], and the model checker adopted is the NuSMV [4]. The input language of the NuSMV model checker is a finite state machine (FSM), which makes it easier the translation from the *BARE* model. The model must describe the transition relation of the states through valid transition relations of the machine. The construction of the system's model from the *Bare* model will be carried out through a tabular model, which contains all the needed elements to extract the

transition system. The mapping of the tabular model to the system's model is thus done automatically by the *GeneratorXM*, which is based on the following algorithm:

1. Construction of the elements of the VAR section.
  - (a) The variables in memory are selected from the set  $M$  of the *BARE* model. If needed, types are required explicitly from the user.
  - (b) All events, either input or output, are declared as boolean type. The events come from the sets  $\Sigma$  and  $\Gamma$  of the *BARE* model.
  - (c) All states, except for the states *Init* and *Start*, are declared in a variable called *states*. This variable has enumerated type with all states of the system. These states come from the set  $Q'$  of the *BARE* model.
2. Construction of the elements of the ASSIGN section.
  - (a) All variables are assigned to its initial value. When needed, these values are required explicitly from the user.
  - (b) The variable *states* is assigned to the *target value* of the transition "start" of the tabular model.
3. Construction of the transition between states through the CASE expression.
  - (a) For each line of the tabular model, we construct an expression to the next state of the system as follows:  $\text{states} = V_i[1] \& V_i[5] : V_i[4]$ , where  $V_i[j]$  means  $j^{\text{th}}$  column of the line  $i$ .

### 3.4. ExecutorXM: The Runtime Environment for the BARE model

The application consists in an array of monitored variables  $m = [m_1, \dots, m_l]$ , an array of internal variables  $i = [i_1, \dots, i_m]$ , an array of controlled variables  $c = [c_1, \dots, c_n]$ , and a finite directed graph  $G = (V, A)$ , where the following conditions are satisfied: **(1)** There is only one vertex called "Init" ( $I \sqsubseteq V$ ); there is only one vertex called "Start" ( $S \sqsubseteq V$ ); there is only one vertex called "Halt" ( $H \sqsubseteq V$ ); and any vertex  $v$  is in the path from  $S$  to  $H$ ; **(2)** Each arc  $a$  not incident in  $H$  is associated with a quantifier-free formula of type  $P_a(m, i)$  and an assignment  $i \leftarrow f_a(m, i)$ ; Each arc  $a$  incident in  $H$  is associated with a quantifier-free formula of type  $P_a(m, i)$  and an assignment  $c \leftarrow f_a(m, i)$ ; where  $P_a$  means *test predicate* associated with arc  $a$ , and  $P_a(m, i)$  is called *test formula* associated with arc  $a$ ; **(3)** For each vertex  $v \neq H$ , let  $a_1, a_2, \dots, a_r$  be all arc leaving  $v$  and let  $P_{a1}, P_{a2}, \dots, P_{ar}$  the test predicates associated with arcs  $a_1, a_2, \dots, a_r$ , respectively. Thus, for all  $m$  and  $i$ , one and only one of the  $P_{a1}(m, i), P_{a2}(m, i), \dots, P_{ar}(m, i)$  is *true*. After the construction of the graph, the application execution occur in accordance with the following algorithm:

1. Execution starts on vertex *Init* ( $I$ ) and next the control is given to the vertex *Start* ( $S$ ).
2. Let  $j = 0$ ,  $v^j = S$  and  $i^j$  the internal variables.
3. If  $v^j = H$ , then execution ends, otherwise go to step 4.
4. Let  $a_k$  the arc in which  $v^j$  is the source vertex, and the test formula associated with the arc is *true*, that is,  $P_{ak}(m, i^j) = \text{true}$ . Let  $v^{j+1}$  be the target vertex of  $a_k$ . Thus, the control moves, through  $a_k$ , to the vertex  $v^{j+1}$  and one of the following assignments is executed:
  - $i^{j+1} \leftarrow f_{ak}(m, i^j)$ , if  $v^{j+1} \neq H$ ;
  - $c \leftarrow f_{ak}(m, i^j)$ , if  $v^{j+1} = H$ ;
5. Let  $j=j+1$ , go to step 3.

One platform adopted for execution of the runtime environment was the LEGO Mindstorm Robot [15]. The *ExecutorXM* was implemented in the LUA language [10]. This implementation is composed by two main

functions: *Executor* and *ReadCurrent*. The *Executor* is the main function. It receives a file with the application in the tabular format, always starts by state “init”, and executes up to state “halt” is reached. *ReadCurrent* receives as input the current state and returns all lines of the application that has this as source state. All such lines are evaluated in order to capture all input events of column “Input” and put in a list of monitored events. When an event occur, the next step is to find out what condition is true. We consider that just one condition will be true in each event. After that, the event in the column “Output” is executed. Later, “Mem\_Output” is updated, in such a way that internal variables are updated, and the next current state is defined by column “Target”.

## 4. THE ENVIROTRACK CASE STUDY

This section describes the main characteristics of the *EnviroTrack* case study [1], and shows results of the application of the proposed method in the modeling, verification and synthesis.

### 4.1. Problem Specification

*EnviroTrack* aims to detect and track moving targets in a network of sensors. One sensor node can be in one of the following states: *free*, *follower*, *member* or *leader*. Initially a node is in the *free* state. A node *free* becomes *member* when it detects a target. A node *free* becomes a node *follower* if it has not detected any target, but it is in the neighbourhood of a member and received a *heartbeat* that a target was detected. The sensor node in *free* state does not respond to time event and leader election event. A node *leader* is a node that was *member* and was elected for this purpose. All *members* send their location to the *leader*, which performs a fusion of the positions for estimation on the position of the target object. If the node *leader* loses the detection of the intruder, it passes to the state of *follower* and other node *member* must be elected as *leader*. The *members* send specific signals (*heartbeat*) so that the *free* nodes that are in their neighbourhood may become a *follower*. The *follower* has a timer, and if it has not detected a target in a timeout, it returns to be *free* state. Figure 2 shows a high-level model of the *EnviroTrack* application.

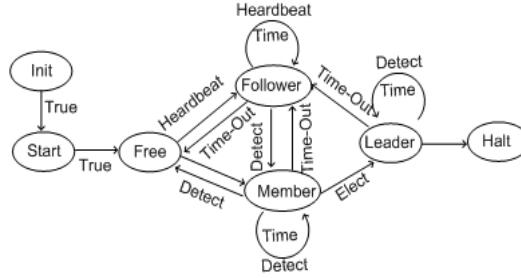


Figure 2. Envirotrack application

### 4.2. EnviroTrack's BARE Model

The *BARE* model of the EnviroTrack case study is defined by the following tuple:  $BM = (T, \Sigma, \Gamma, \Lambda, Q', M, E, C, \Phi, F, q_0, m_0)$ , where:

- 1)  $T = (\text{Int}, \text{Bool}, \text{Temp} = [0, 10000])$ ;
- 2)  $\Sigma = \{\text{mSound}=\{\text{Bool}\}, \text{mIntruder}=\{\text{Bool}\}, \text{mElect}=\{\text{Bool}\}, \text{mTemp}=\{\text{Temp}\}, \text{mX}=\{\text{Int}\}, \text{mY}=\{\text{Int}\}\}$ ;
- 3)  $\Gamma = \{\text{cSound}=\{\text{Bool}\}, \text{cPosX}=\{\text{Int}\}, \text{cPosY}=\{\text{Int}\}\}$ ;
- 4)  $\Lambda = \{\text{iX}=\{\text{Int}\}, \text{iY}=\{\text{Int}\}, \text{iCurr}=\{\text{Temp}\}, \text{iTotal}=\{\text{Temp}\}\}$ ;
- 5)  $Q' = \{\text{Free}, \text{Follower}, \text{Member}, \text{Leader}, \text{Init}, \text{Start}, \text{Halt}\}$ ;

- 6)  $M = (mSound, mIntruder, mElect, mX, mY, mTemp, iCurr, iTot, iX, iY, cSound, cPosX, cPosY);$
- 7)  $E = \{e1=mSound \sqcap e2=mIntruder \sqcap e3=mElect \sqcap e4=mTemp\};$
- 8)  $C = \{ \{c0=True\}, \{c1=e1\}, \{c2=e2\}, \{c3=e3\}, \{c4=iCurr > iTot \sqcap e4\}, \{c5=iCurr \leq iTot \sqcap e4\}, \{c6=iCurr \leq iTot \sqcap e2\} \};$
- 9)  $\Phi : \varphi_0 = (\_, \_, c0, \_, \_); \varphi_1 = (mSound, iCurr, c1, iCurr=0, "Heartbeat"); \varphi_2 = (mIntruder, iCurr, c2, iCurr=0, "Intruder"); \varphi_3 = (mElect, iCurr, c3, iCurr=0, "Elect"); \varphi_4 = (mTemp, \_, c4, \_, "Timeout"); \varphi_5 = (mTemp, (iCurr, iTot), c5, iCurr=iCurr+1, "Timing"); \varphi_6 = ((mX, mY), (iX, iY, iCurr, iTot), c6, (iX=iX+mX, iY=iY+mY), "Collecting"); \varphi_7 = (\_, (iX, iY), c3, (cPosX=iX, cPosY=iY), (cPosX, cPosY));$
- 10)  $F: (Init, \varphi_0, Start); (Start, \varphi_0, Free); (Free, \varphi_1, Follower); (Free, \varphi_2, Member); (Follower, \varphi_1, Follower); (Follower, \varphi_2, Member); (Follower, \varphi_4, Free); (Follower, \varphi_5, Follower); (Member, \varphi_2, Member); (Member, \varphi_3, Leader); (Member, \varphi_5, Member); (Member, \varphi_4, Follower); (Leader, \varphi_4, Follower); (Leader, \varphi_5, Leader); (Leader, \varphi_6, Leader); (Leader, \varphi_7, Halt).$
- 11)  $qo = \{\text{Init}\}.$
- 12)  $mo = (mSound=False, mIntruder=False, mElect=False, mX=0, mY=0, mTemp=False, iCurr=0, iTot=10, iX=0, iY=0, cPosX=0, cPosY=0, cSound=False).$

Table 1: Envirotrack Table Application

Source	Input	Mem_in	Target	Cond.	Mem_out	Output
init	<i>nil</i>	<i>nil</i>	start	<i>T</i>	<i>nil</i>	"Init"
start	<i>nil</i>	<i>nil</i>	free	<i>T</i>	<i>iCurr=0;iTotal=10</i>	"Start"
free	<i>mSound</i>	<i>iCurr</i>	follower	<i>c1</i>	<i>iCurr=0</i>	"Heartbeat"
free	<i>mIntruder</i>	<i>iCurr</i>	member	<i>c2</i>	<i>iCurr=0</i>	"Intruder"
follower	<i>mSound</i>	<i>iCurr</i>	follower	<i>c1</i>	<i>iCurr=0</i>	"Heartbeat"
follower	<i>mIntruder</i>	<i>iCurr</i>	member	<i>c2</i>	<i>iCurr=0</i>	"Intruder"
follower	<i>mTime</i>	<i>iCurr,iTotal</i>	free	<i>c4</i>	<i>iCurr=0</i>	"Timeout"
follower	<i>mTime</i>	<i>iCurr</i>	follower	<i>c5</i>	<i>Icurr = iCurr+1</i>	"Timing"
member	<i>mIntruder</i>	<i>iCurr</i>	member	<i>c2</i>	<i>Icurr = 0</i>	"Intruder"
member	<i>mElect</i>	<i>iCurr</i>	leader	<i>c3</i>	<i>Corr = 0</i>	"Elect"
member	<i>mTime</i>	<i>iCurr</i>	member	<i>c5</i>	<i>Icurr = iCurr+1</i>	"Timing"
member	<i>mTime</i>	<i>iCurr,iTotal</i>	follower	<i>c4</i>	<i>Icurr = 0</i>	"Timeout"
leader	$(mX,mY) \sqcap mTime$	<i>iCurr,iTotal</i>	follower	<i>c4</i>	<i>Icurr = 0</i>	"Timeout"
leader	$(mX,mY) \sqcap mTime$	<i>(iX,iY)</i>	leader	<i>c5</i>	<i>IXY = mY</i>	"Collecting"
leader	$(mX,mY) \sqcap mTime$	<i>(iX,iY)</i>	Halt	<i>c6</i>	<i>PosXY = iX,iY</i>	<i>(cPosX,cPosY)</i>
halt	<i>nil</i>	<i>nil</i>	halt	<i>nil</i>	<i>nil</i>	<i>nil</i>

The tabular model of the *Envirotrack* application is shown in Table 1.

### 4.3. EnviroTrack's Formal Verification

The proposed method is able to verify reachability/safety/liveness properties by adopting the NuSMV model checker. Figure 3 show the input to the NuSMV automatically generated by the *GeneratorXM*. As presented before, the specifications to be checked as provided by the user. In the case of this figure, it was checked the following properties: (1) all execution eventually reach the "halt" state ((AG EF states = halt)); (2) Whenever there is a intrusion detection, the node switches to a member state (AG mPresence = 1  $\rightarrow$  states = member); (3)To become a leader node it has to be a member and be elected (event touch) (AG (states = member & mTouch = 1)  $\rightarrow$  AX states = leader). All these properties was verified by NuSMV and the result was true.

```

MODULE main
VAR
iCurr : 0..11;
iTTotal : 1..10;
mSound: boolean;
mPresence: boolean;
mTouch: boolean;
mTime: boolean;
states: {halt,free,follower,member,leader} ;
ASSIGN
init (iCurr):= 0;
init (iTTotal):= 5;
init(states) := free ;
next(states) := case
    states = free & mSound : follower;
    states = free & mPresence : member;
    states = follower & mSound : follower;
    states = follower & mPresence : member;
    states = follower & iCurr>iTotal & mTime : free;
    states = follower & iCurr<=iTTotal & mTime : follower;
    states = member & mPresence : member;
    states = member & mTouch : leader;
    states = member & iCurr<=iTTotal & mTime:member;
    states = member & iCurr>iTotal & mTime:follower;
    states = leader & iCurr<=iTTotal & mTime : follower;
    states = leader & iCurr>iTotal & mTime:leader;
    states = leader & mTouch:halt;
    1 : states ;
    esac;
next(iCurr) := case
    states = free & mSound : 0;
    states = free & mPresence : 0;
    states = follower & mSound : 0;
    states = follower & mPresence : 0;
    states = follower & iCurr<=iTTotal & mTime : iCurr+1;
    states = member & mPresence : 0;
    states = member & mTouch : 0;
    states = member & iCurr<=iTTotal & mTime : iCurr+1;
    states = leader & iCurr<=iTTotal & mTime : iCurr+1;
    1 :iCurr ;
    esac;
next(iTotal) := case
    1 :iTTotal ;
    esac;
SPEC AG EF states = halt
SPEC AG mPresence = 1 -> states = member
SPEC AG (states=member & mTouch=1) -> AX states=leader

```

Figure 3. Model of the System for the EnviroTrack Case Study

## 5. RELATED WORK

Kasten and Romer [13] proposed a new abstraction to manage the event-triggered programming. They use a state machine program model, called Object State Model (OSM), which is based on Harel's StateCharts [8] and uses an external compiler to produce C code. They use an empirical state machine with a textual language to specify the machine architecture. In our work, however, we employ a formal state machine bypassing the combinatorial state explosion with an easier diagrammatic approach for modeling systems control. Levis and Culler [16] propose Maté, a byte-code interpreter to run on motes as a virtual machine. Maté executes only the virtual machine instructions and a regular sensor application should be converted to the virtual machine instructions before execution. The advantage is that a sender node does not need to send the network programming module, because the virtual machine is already running on the receiver node, under the TinyOS. Our solution, however, does not make use of an operating system. Dunkels et al [5] propose a programming abstraction called *Protothreads* for event-driven sensor network. Protothreads uses a type of continuation, called local continuation, to reduce the complexity of applications and they require only one stack to execute, doing rewind to switch context. The main limitation of protothreads is that the automatic variable has a local scope and it is not saved across context switches, because the stack is rewound at the end of each procedure. In our work, however, we employ a very simple continuation mechanism within a tabular fashion, and the memory is the only shared common space.

## 6. CONCLUSIONS

In this paper, we propose a new way for designing, verifying, and implementing reactive embedded systems. These systems are characterized by a tight integration of computation and control with the sensing and actuation physical components. In this context, we propose an interactive method that adopts a formal modeling method, followed by a verification process, and a runtime environment that can execute the formal specification into a real embedded platform. Most part of this method is automated and thus the proposed method can avoid an ad-hoc design process. We named this process as *BARE Development Model*. The BARE model starts by modeling the specification using an abstract model called X-machine, where data and control are described in a graphical structure of the abstract finite state machine. The construction of a X-

machine is performed by a tool called *GeneratorXM*, which translates the X-machine to a tabular model, which is then loaded into the specific execution platform. The platform that we used to carry out the experiments is based on the LEGO Mindstorm NXT, which has some sensors and actuators in the kit so that it simplifies the execution of the model into a real hardware. The tabular model is directly executed in the *ExecutorXM*, which is the runtime environment that can execute the formal specification into a real platform. The *ExecutorXM* was implemented in the Lua language.

One contribution of this work is the definition of a dynamic execution model for X-Machines, in this case the tabular model. As presented, X-Machines are abstract mathematical entities used to model specifications and system characteristics. However, at the best of our present knowledge, there is no mapping of the abstract model to an executable model. Another important contribution of this work is the automatic generation of the “system model” from the tabular model. Such model is specified in the input language of the NuSMV model checker tool. Consequently, we are able to verify some properties of the model using properties specified in CTL temporal logic.

From our experiments, we also noted that the tabular model is a suitable way to carry out the dynamic reconfiguration since each line of the table is considered as independent of each other. Thus, lines can be sent or deleted in order to aggregate new functionalities or even change the original applicability of the application. As a future work, we intend to investigate the dynamic reconfiguration in the context of embedded reactive applications.

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