# Imperfect Digital Fibre Optic Link Based Cooperative Distributed Antennas with Fractional Frequency Reuse in Multicell Multiuser Networks

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Abstract— The achievable throughput of the entire cellular area is investigated, when employing fractional frequency reuse techniques in conjunction with realistically modelled imperfect optical fibre aided distributed antenna systems (DAS) operating in a multicell multiuser scenario. Given a fixed total transmit power, a substantial improvement of the cell-edge area's throughput can be achieved without reducing the cell-centre's throughput. The cell-edge's throughput supported in the worst-case direction is significantly enhanced by the cooperative linear transmit processing technique advocated. Explicitly, a cell-edge throughput of  $\eta = 5$  bits/s/Hz may be maintained for an imperfect optical fibre model, regardless of the specific geographic distribution of the users.

## I. INTRODUCTION

The classic Unity Frequency Reuse (UFR) pattern may be applied by wireless systems in order to maximize the attainable area spectral efficiency at the cost of increasing the Co-channel Interference (CCI) level, hence the UFR typically exhibits a low throughput at the cell-edge. As a remedy, the Fractional Frequency Reuse (FFR) [1] philosophy may be invoked, which reduced the CCI at the cell-edge at the cost of a reduced area-spectral-efficiency. Hence the FFR scheme is capable of improving the cell-edge Signal-to-Interference-plus-Noise-Ratio (SINR) [2]. As a result, FFR has also been adopted in the Third Generation Partnership Project's (3GPP) Long Term Evolution (LTE) initiative [3] and in the Worldwide interoperability for Microwave Access (WiMAX) [4] system.

By contrast, a DAS improves the cell-edge throughput by placing the Remote Antennas (RA) more close to the cell-edge terminals, hence naturally reducing the pathloss [5]. However, the reduced pathloss will increase the interference imposed on the cell-edge terminals served by the neighbouring RAs. In practice only those MSs can be granted a high throughput, which roam in the vicinity of the RA. When the MS is roaming near the angle halfway between two adjacent RAs [6] [7], its

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For the practical application of DASs, the connection between the BS and RAs may be a coaxial cable, optical fibre or a Radio Rrequency (RF) link [10] [11]. The Radio over Fibre (RoF) [12] and Digital Fibre Optical (DFO) link [13] based transmission technique may also be used for the BS to RA links, which is more reliable than a wireless backhaul, albeit it is also more costly. In contrast to the RoF family [14], the DFO link is immune to the sideband cancellation phenomenon, which occurs in the RoF system [15] [16] and it is capable of avoiding both the inter-modulation distortions of the optical fibre as well as the nonlinearity imposed by the optical components, but this is typically achieved at an increased complexity and cost [13]. Additionally, optical multilevel signalling transmission techniques [17] [18] may be applied for the DFO link, which are capable of reducing the complexity of the optical receiver at the RA. Hence in this study we opted for the DFO link. As a further benefit, DFO techniques also allow us to preprocess the DownLink (DL) transmit signal for all the users in the central BS, before it is transmitted to the mobile station (MS). Hence the DFO backhaul may also support the extension of BS cooperation techniques [19] to DASs. Furthermore, when aiming for supporting Gigabit-transmissions, which is the goal of LTE-Advanced (LTE Release 10) [20], these highrate systems may suffer from the effects of both the dispersion and nonlinearty imposed by the optical fibre links of the DASs [21]. Hence jointly considering the effects of DFO link and wireless links becomes important, when analyzing the performance of DAS systems designed for LTE-Advanced applications.

Against this background, in this paper we quantify the

attainable throughput across the entire cellular coverage area in a multicell, multiuser scenario, when employing cooperative techniques beneficially combined both with realistically modelled imperfect optical fibre aided DASs as well as with FFR. More explicity, we introduced the Split-Step Fourier (SSF) method [22] to analyse how the dispersion and nonlinearity of the optical fibre link affect the throughput of the cell-edge area.

- Although the dispersion of the optical signalling pulse may be viewed as an undesirable imperfection of a pure optical fibre system, ironically, it might result in beneficial throughput enhancements in the cell-edge area of the non-cooperative RA aided FFR system. This is because the dispersion-induced attenuation of the optical signalling pulses may be capable of mitigating the IRI in the multicell, multiuser scenario. However, we will demonstrate that due to the worst-case direction problem caused by the IRI, the non-cooperative RA aided FFR system may not always lead to an improved attainable throughput in the entire cell-edge area.
- 2) We will also demonstrate that employing a single omnidirectional transmit antenna at each RA and a single receive antenna at each MS, but jointly designing the Transmit PreProcessing (TPP) matrix of all the cooperative RAs combined with FFR is capable of achieving an increased throughput for the entire cell-edge area, regardless of the specific geographic distribution of the users. Furthermore, even though conventional cooperative signal processing techniques are unable to directly mitigate the optical fibre receiver's self-inflicted noise, the proposed cooperative RA-aided FFR system exhibits a higher attainable throughput than conventional noncooperative FFR aided systems, especially in the worstcase direction.

Our results not included here for reasons of space economy suggest that the IRI experienced in the local cell dominates the interference experienced in the DFO link aided DAS combined with FFR. We also found that the DAS combined with FFR requires a reduced transmit power at each RA, which naturally limits the IRI imposed by the cells using the same frequency band in a tier-two cell. Hence, the IRI inflicted by the tier-two cells will be neglected to simplify our analysis in the multicell multiuser scenario considered.

Our paper is organised as follows. In Section II we introduce the multicell multiuser topology considered, describe the imperfect optical fibre model. In Section III, we outline the received signal model of the non-cooperative DAS with FFR system (Section III-A), introduce several cooperative linear processing techniques (Section III-B) and present our link level results recorded for a range of practical modulation and coding schemes (Section III-C) followed by our performance evaluations in Section IV. Finally, we conclude our discourse in Section V.



Fig. 1. The toplogy of two tiers of nineteen cells relying on a FFR and DAS arrangement, where  $N_r = 6$  RAs are employed. The structure of the cells in tier two is the same as the ones in tier one.

## II. SYSTEM DESCRIPTION AND OPTICAL FIBRE MODELLING

#### A. Multicell Multiuser System Topology

The multicell multiuser scenario based on the FFR scheme is illustrated in Fig. 1, which consists of two tiers of nineteen hexagonal cells [23] surrounding the central BS  $B_0$ , where  $B_0$  is assumed to be at the origin. We assume symmetry, where every cell has the same system configuration and focus our attention on cell  $B_0$  of Fig. 1 without any loss of generality. The frequency partitioning strategy of the total available bandwidth F is characterized by  $F_c \cap F_e = \emptyset$ , where  $F_c$  and  $F_e$  represent the cell-centre's frequency band and the cell-edge's frequency band, respectively.  $F_e$  is divided into three orthogonal frequency bands  $F_i, i \in [1, 3]$ , exclusively used at the cell-edge of one of the three adjacent cells.

To simplify the structure, we assume that the number of active MSs  $N_m$  and RAs  $N_r$  is the same  $(N_m = N_r)$ , which implies that each RA may support a single MS. The users are assumed to be randomly distributed in the cell-edge area, and a total of  $N_m$  MSs are roaming at any point  $Z_i$ , as described by the polar coordinates of  $[\theta_{Zi}, L_{Zi}], i \in [1, N_m]$ . A total of  $N_r$  RAs are employed in each cell described by its polar coordinates denoted by  $[\theta_{Ri}, L_{Ri}] = [2\pi(i-1)/N_r, d], i \in [1, N_r]$ . Likewise, the BSs in tier-one are described by their polar coordinates of  $[\theta_{Bj}, L_{Bj}] = [2\pi(j-1)/6, \sqrt{3}R], j \in [1, 6]$  and the polar coordinates of the BSs in tier-two may also be readily obtained from the underlying simple geometry. Fig. 2 shows a single optical fibre link spanning from the BS to the RA.

## B. Imperfect Optical Fibre Model

In order to investigate the system topology introduced above, we assume that the links from BS  $B_0$  of Fig. 1 to the RAs are constituted by a realistic imperfect optical fibre,



Fig. 2. System architecture of the DFO link, showing a single optical fibre link spanning from the BS to the RA. The transmitted baseband data is used to modulate a stream of optical Gaussian pulses, where an ideal optical modulator is assumed, therefore it does not impose any chirp on the optical pulse. Then the Gaussian optical signalling pulses are transmitted through the optical fibre, which imposes both linear and nonlinear distortions. At the RA, after an ideal photo-detector, the optical signalling pulses are converted back to the corresponding baseband electronic signals.

rather than simply assuming a perfect optical fibre. The phase rotation imposed by the optical fibre link on the modulated signal constellation diagram is supposed to be compensated, hence in this paper we only considered the fibre-induced imperfections imposed on the modulated signal's amplitude. Hence, the signal received at the RA i after passing through the realistically modelled optical fibre may be written as:

$$s_i = A_L x_i + n_f, \tag{1}$$

where  $A_L$ ,  $x_i$  and  $n_f \sim C\mathcal{N}(0, \sigma_f^2)$  represent the received amplitude of the optical pulse after passing through the optical fibre having a total length of L, the transmitted signal and the complex-valued Additive White Gaussian Noise (AWGN), respectively. Furthermore, the so-called *pulse-broadening* (PB) effect caused by dispersion [24] may not impose a significant performance limitation in pure optical fibre links, since the inter-pulse-interference may be negligible for the transmission of the baseband signal through the DFO link. However, the PB additionally imposes an attenuation of the optical signalling pulse, which may affect the attainable throughput of the cell-edge area, when considering our DFO link aided DAS combined with FFR in a multicell, multiuser scenario.

To elaborate on our optical fibre model a little further, the parameter  $A_L$  takes into account the fibre's attenuation, its dispersion and the fibre's nonlinearity characterized by the generalized Nonlinear Schrödinger (NLS) equation [22] expressed in the form of:

$$\frac{\partial A}{\partial z} = \underbrace{\left(\frac{\beta_3}{6}\frac{\partial^3}{\partial t^3} - \frac{i\beta_2}{2}\frac{\partial^2}{\partial t^2} - \frac{\alpha}{2}\right)}_{\widehat{D}}A \\ + \underbrace{i\xi\left(|A|^2 + \frac{i}{\omega_0}\frac{1}{A}\frac{\partial}{\partial t}\left(|A|^2A\right) - T_R\frac{\partial|A|^2}{\partial t}\right)}_{\widehat{N}}A, \quad (2)$$

where A(z,t) is the Gaussian signalling pulse envelope as a function of both the time t and the propagation distance z. The term  $\widehat{D}$  characterizes the dispersion and fibre loss effects, while  $\widehat{N}$  characterizes the nonlinearity effects, as the pulse propagates along the optical fibre. Still considering Eq (2), in the term  $\widehat{D}$ ,  $\alpha$  represents the fibre attenuation,  $\beta_2$  is the groupvelocity dispersion (GVD) parameter, and  $\beta_3$  is the third-order dispersion coefficient, which becomes significant for ultranarrow signalling pulses, as detailed in [24]. Considering the term  $\hat{N}$  in Eq (2),  $\xi$  describes the fibre's nonlinearity,  $\omega_0$  is the angular frequency of the carrier wave and  $T_R$  is related to the slope of the Raman gain spectrum, as detailed in [22]. In the case of having a pulse width of  $T_0 > 5$ ps which is typical for telecommunication fibres [22], the first term of  $\hat{D}$  and the last two terms of  $\hat{N}$  may be neglected [22]. These simplifications allow us to focus our attention on the nonlinearity and dispersion effects in this paper, hence the

$$\frac{\partial A}{\partial z} = \left(-i\frac{\beta_2}{2}\frac{\partial^2}{\partial t^2} + i\xi|A|^2\right)A = \left(\widehat{D'} + \widehat{N'}\right)A, \quad (3)$$

where the terms  $\widehat{D'}$  and  $\widehat{N'}$  are the simplified forms of the dispersion character  $\widehat{D}$  and of the nonlinear character  $\widehat{N}$  in Eq (2).

fibre loss parameter is assumed to be  $\alpha = 0$ . Then Eq (2) may

be further simplified to:

More explicity, the general formula of Eq (2) or its simplified form in Eq (3) describes the pulse propagation problem [22], but in this form it is not directly suitable for analyzing how the throughput of the wireless link is affected by the parameters of the imperfect optical fibre backhaul. The more practical SSF may be applied for analyzing the solutions of the NLS equation [22], which has been considered for modelling the optical-fibre communication systems [25]. Hence we employ the SSF method for jointly analyzing the attainable throughput of the DFO link. The SSF method delivers an approximate numerical solution, where the dispersive and nonlinear effects observed in Eq (3) may be separated into independent phenomena over a small segment-length lstretching from z to (z + l) in Eq (3), yielding:

$$A(z+l,t) \approx F_T^{-1} \left\{ exp\left[ l\widehat{D'}(-i\omega) \right] F_T\left[ exp(l\widehat{N'})A(z,t) \right] \right\},$$
(4)

where  $F_T$  and  $F_T^{-1}$  denotes the Fourier-transform and inverse Fourier-transform operation, respectively. Firstly, the exponential nonlinearity-related term exp(lN') of Eq (4) may be taken into account directly in the time domain. Secondly, before characterizing the dispersive effects, we take the Fouriertransform of the term exp(lN')A(z,t), since the exponential dispersion-related term  $exp(l\widehat{D'})$  may be evaluated in the frequency domain. The Fourier-transform of the dispersion character D' is obtained by replacing the operator  $\partial/\partial T$  by  $-i\omega$  in Eq (3). Then, following the inverse Fourier-transform of Eq (4), we obtain the time domain representation of the received signal after propagating through the *l*-length fibre. The total optical fibre length satisfies L = ml, which suggests that the whole fibre length is decomposed into m consecutive llength segments. Hence the optical pulse propagating through an L-length fibre may be obtained by evaluating Eq. (4) in mconsecutive steps, yielding a solution denoted as  $A_L$ .

## III. RECEIVED SIGNAL OF DFO AIDED DAS WITH FFR Systems

### A. DFO aided Non-Cooperative DAS with FFR system

Focusing our attention on the cell  $B_0$  of Fig. 1, when noncooperative DASs are employed, the transmit power  $P_B$  of the BS and the transmit power  $P_R$  of each RA should obey the total transmit power constraint of  $P_B + N_r P_R = P$ , where Pis the full power at the BS of the traditional UFR and FFR scheme.

1) Received Signal in the Cell-Centre Area: The interference at any MS located at point  $Z_i$  in the cell-centre area is imposed by the direct wireless links of BSs  $\{1, \ldots, N_b\}$ , with  $N_b$  being the number of BSs, which we refer to as the Inter-BS-Interference (IBI). Hence, the received signal may be written as:

$$y_{c} = \sqrt{P_{B}}\psi_{B0}h_{B0}x_{0} + \sum_{j=1}^{N_{b}}\sqrt{P_{B}}\psi_{Bj}h_{Bj}x_{j} + n, \quad (5)$$

where  $\psi_{Bj}$ ,  $h_{Bj}$ ,  $j \in [0, N_b]$  and  $n \sim C\mathcal{N}(0, \sigma_0^2)$  represent the combined pathloss plus shadowing based large-scale signal attenuation, small-scale fast Rayleigh fading and the complexvalued AWGN, respectively. More explicitly, we jointly consider both the pathloss and the lognormal shadowing component, which is formulated as:  $\psi_{Bj} = [\rho 10^{\varsigma(\sigma_s)/10}]^{1/2}$ ,  $j \in [0, N_b]$ , where  $\rho$  denotes the pathloss that obeys a predefined pathloss model [26], while  $\varsigma$  denotes a real valued Gaussian random variable having a standard deviation of  $\sigma_s = 8$ dB [26]. Hence,  $G_{Bj} = \psi_{Bj} |h_{Bj}|$  denotes the equivalent channel gain, while the SINR of any of the MSs near the cell-centre is given by:

$$\gamma_c = \frac{G_{B0}^2 P_B}{2\sigma_0^2 + \sum_{j=1}^{N_b} G_{Bj}^2 P_B}.$$
(6)

2) Received Signal in the Cell-Edge Area: When considering the cell-edge area, we assume that the links spanning from the BS  $B_0$  of Fig. 1 to the RAs are constituted by a realistic imperfect optical fibre, while the last-mile connection from the RAs to the MS relies on the wireless link. The signal received at the RA *i* after passing through the realistically modelled optical fibre is introduced in Section II-B.

The noise-contaminated, faded signal  $s_i, i \in [1, N_r]$  denoted in Eq (1) at the wireless channel's input is normalised by a power-scaling factor and then forwarded through the wireless channel to the destination, namely to the MS roaming in the cell-edge area, where the power-scaling factor  $\chi$  is employed in order to maintain a constant transmit power at the RAs. As a result, the signal received by MS *i* at any point  $Z_i$  in the cell-edge area in the absence of any cooperative techniques, may be written as

$$y_{ei} = \sqrt{P_R} \psi_{Ri} h_{Ri} \chi s_i + \sum_{k=1, k \neq i}^{N_r} \sqrt{P_R} \psi_{Rk} h_{Rk} \chi s_k + n.(7)$$

Let  $A = \chi A_L$  and  $N_f = 2\sigma_f^2 \chi^2$  denote the equivalent optical fibre-induced amplitude attenuation and the equivalent power spectral density of the optical fibre noise, respectively. The details of the parameters  $s_i$  and  $A_L$  are introduced in

Section II-B. Then, the SINR at any MS roaming in the celledge area is:

$$\gamma_{ei} = \frac{G_{Ri}^2 A^2 P_R}{2\sigma_0^2 + \sum_{i=1}^{N_r} G_{Ri}^2 N_f P_R + \sum_{k=1, k \neq i}^{N_r} G_{Rk}^2 A^2 P_R},$$
(8)

where  $G_{Ri} = \psi_{Ri} |h_{Ri}|$  denotes the equivalent channel gain.

3) Idealistic Received Signal in the Cell-Edge Area: We assume the employment of perfect adaptive beamforming, where each MS is served with the aid of a narrow beam. We also assume that the MSs would be served only by the nearest RAs and that their reception is not contaminated by the other RAs, hence no IRI is received by the MSs roaming in the cell-edge area. Hence their reception is only contaminated by the noise  $N_f$  imposed at the optical fibre receiver. Then the interference-free upper bound of the SINR can be rewritten from Eq (8) as:

$$\gamma_u = \frac{G_{Ri}^2 A^2 P_R}{2\sigma_0^2 + G_{Ri}^2 N_f P_R}.$$
(9)

4) Benchmarker Systems: Finally, when the classic UFR technique is employed, the received signal model is described by Eq (5), but bearing in mind that the full power P is transmitted by each BS instead of  $P_B$ . When the FFR technique is employed, similarly to the classic UFR, the signal received in the cell-centre area is also described by Eq (5). On the other hand, the signal received in the cell-edge area both from the serving BS and from the cells using the same frequency band in tier-two obeys Eq (5).

### B. DFO aided Cooperative DAS with FFR

In a multicell, multiuser scenario cooperative DAS techniques may be used, in order to provide a high throughput for the MSs roaming near the cell-edge area, especially for mitigating the worst-case direction problem caused by IRI. To simplify the entire system, only a single omni-directional antenna is applied for each RA. Nonetheless, when jointly designing the TPP matrix **T**, the  $N_R$  cooperative RAs operate in a concerted action as a virtual multiple-input and singleoutput (MISO) or virtual multiple-input and multi-output (MIMO) system. On the other hand, only a single receiver antenna is applied at the MS. We will show that the proposed system architecture is capable of substantially enhancing the throughput achievable in the cell-edge area with the advent of our cooperative TPP aided FFR scheme.

**Notation**: the lower case boldface letters and the upper case boldface letters represent column vectors and matrices, respectively. The superscript  $(\cdot)^T$  and the  $(\cdot)^H$  denotes the transposition and the conjugate transpose respectively.

1) Received Signal-to-Interference-plus-Noise-Ratio: The principle of cooperative DAS schemes is essentially the same as that of cooperative BSs [8], where the transmit signal destined for the MSs is spread over all the  $N_r$  cooperative RAs. In the multicell multiuser scenario there are  $N_m$  MSs roaming in the cell-edge area of Fig 1, which are simultaneously supported by the  $N_r$  RAs ( $N_r = N_m$ ). Provided that the different propagation delays of all the  $N_r$  RA links

measured with respect to all the served  $N_m$  MSs can be precompensated, the vector of received signal can be written as:

$$\mathbf{y} = \mathbf{H}\mathbf{T}\mathbf{x} + \mathbf{n},\tag{10}$$

where  $\mathbf{y}_{N_m \times 1}$  and  $\mathbf{n}_{N_m \times 1}$  denote the received signal vector and the circularly symmetric complex Gaussian noise vector. Furthermore,  $\mathbf{x} = [x_1, x_2, \cdots, x_{N_m}]_{1 \times N_m}^T$ ,  $x_i$  is defined as the signal transmitted from RA *i* to MS *i*. More explicitly,  $x_i = \chi_i s_i$ ,  $i \in [1, N_r]$  represents the signal passing through the realistic 'lossy' optical fibre, where  $\chi_i$  and  $s_i$  is the same as that defined in Section III-A.2. If the central BS has an estimate of the channel matrix  $\mathbf{H} = [\mathbf{h}_1^T, \mathbf{h}_2^T, \cdots, \mathbf{h}_{N_m}^T]_{N_m \times N_r}^T$ , we can design a transmit matrix  $\mathbf{T}$  for mitigating the IRI, where  $\mathbf{T} = [\mathbf{t}_1, \mathbf{t}_2, \cdots, \mathbf{t}_{N_m}]_{N_r \times N_m}$  is uniquely and unambiguously determined by  $\mathbf{H}$ . We also have a dedicated TPP matrix  $\mathbf{T}$ , which obeys the per RA power constraint of:

$$\mathbf{T}_{i,\forall} \mathbf{T}_{i,\forall}^{H} \le \frac{P - P_B}{N_r},\tag{11}$$

where  $\mathbf{T}_{i,\forall}$  is the row vector of the matrix  $\mathbf{T}$ .

Furthermore,  $\mathbf{h}_i = [\psi_1 h_1, \psi_2 h_2, \cdots, \psi_{N_r} h_{N_r}]_{1 \times N_r}, i \in [1, N_m]$ , represents the channel of all the  $N_m$  RA to MS i links, which takes into account both the large-scale signal attenuation and the small-scale fast Rayleigh fading channel, where  $\psi_i$  and  $h_i$  is the same as that defined in Section III-A.2. Hence, a unified discrete-time model for the signal received by MS i may be formulated based on Eq (10) as:

$$y_{i} = \|\mathbf{h}_{i}\mathbf{t}_{i}\|_{x_{i}} + \sum_{k \neq i} \|\mathbf{h}_{i}\mathbf{t}_{k}\|_{x_{k}} + n_{i}.$$
 (12)

When we have  $k \neq i$ ,  $x_k$  is the IRI imposed by the transmit signal intended for MS k, but received at MS i. Hence, the DFO links' SINR encountered at MS i in the cell-edge area may be written as:

$$\gamma_{i} = A^{2} \mathbf{h}_{i} \mathbf{t}_{i} \mathbf{t}_{i}^{H} \mathbf{h}_{i}^{H} \times [2\sigma_{0}^{2} + \underbrace{N_{f} \mathbf{h}_{i} \mathbf{t}_{i} \mathbf{t}_{i}^{H} \mathbf{h}_{i}^{H}}_{IRI_{2}} + \underbrace{(A^{2} + N_{f}) \mathbf{h}_{i} (\sum_{k \neq i} \mathbf{t}_{k} \mathbf{t}_{k}^{H}) \mathbf{h}_{i}^{H}}_{IRI_{1}}]^{-1},$$
(13)

where A and  $N_f$  represent the equivalent optical fibre attenuation factor and the equivalent power spectral density of the optical fibre' noise, respectively, as defined in Section III-A.2. It can be seen from Eq (13), that for MS *i*, the IRI is composed of two terms. Specifically, the term  $IRI_1$  of Eq (13) is the desired signal of MS  $k \neq i$  that is also contaminated by the optical fibre link's noise  $N_f$ , which can be mitigated by appropriately designing the corresponding TPP matrix. The other term, namely  $IRI_2$  of Eq (13), is the optical fibre link's noise contaminating the desired signal of MS *i*, which is the self-inflicted noise, hence the TPP matrix is unable to mitigate it.

2) Linear Transmit Processing: Again, we assume that there is only a single transmit antenna at each RA and a single receive antenna at each MS, hence our system is fully described by the number of RAs  $N_r$  and by the number of MSs  $N_m$  served. Hence our design is based on the  $(N_m \times N_r)$ - element channel matrix  $\mathbf{H}$  associated with the central BS and the TPP facilitates a low-complexity matched-filter-based receiver design at each MS. Our linear TPP matrix  $\mathbf{T}$  may be written as:

$$\mathbf{T} = \mathbf{G} \cdot \mathbf{W},\tag{14}$$

where  $\mathbf{W}_{N_m \times N_m}$  is a diagonal matrix representing the power [8] allocated for each RA and  $\mathbf{G}_{N_r \times N_m}$  is the linear TPP matrix jointly designed on the basis of **H**. The TPP matrix **G** can be calculated with the aid of different linear preprocessing algorithms. In this paper we consider the minimum mean square error (MMSE) beamformer [27] and the eigenbeamformer (egBF) [28] as our design example.

The classic MMSE beamforming technique strikes an attractive tradeoff between the achievable interference cancellation and noise enhancement, hence it is attractive for practical applications. The TPP weight matrix  $\mathbf{G}_{MMSE} = \mathbf{H}^{H}(\mathbf{H}\mathbf{H}^{H} + \frac{2\sigma_{0}^{2}}{P_{R}}\mathbf{I})^{-1}$ , which is entirely based on the channel matrix  $\mathbf{H}$ , remains unaffected by the transmit signal. The employment of the TPP matrix  $\mathbf{G}_{MMSE}$  mitigates the  $IRI_{1}$  component in Eq (13), eliminating the interference inflicted on the desired signal.

In cooperative egBF, the TPP matrix  $\mathbf{G}_{BF} = [\mathbf{g}_1, \mathbf{g}_2, \cdots, \mathbf{g}_{N_m}]$  is used, where  $\mathbf{g}_i, i \in [1, N_m]$  is the right-hand-side singular vector of  $\mathbf{H}$ , which only achieves a power gain, while the mitigation of the term  $IRI_1$  in Eq (13) is dependent on the instantaneous geographic distribution of the users. Hence the mitigation of the  $IRI_1$  cannot always be achieved by appropriately selecting the direction of the transmitted beam, unless we employ an idealistic infinitesimally narrow beam for each MS. The associated performance will be characterized in Section IV-E.

However, in contrast to the  $IRI_1$ , the link's self-noise imposed by the optical fibre receiver's noise contribution, namely the  $IRI_2$  terms of Eq (13) cannot be mitigated by the TPP matrix employed, regardless, whether the cooperative MMSE or the cooperative egBF is used. In fact, the selfinterference may even be boosted, when the desired signal of MS *i* is amplified.

#### C. System Throughput

Let us now demonstrate how these SINR expressions may be mapped to the ultimate system performance metric formulated in terms of the achievable throughput  $\eta$ . The throughput may be characterised by the maximum *successfully transmitted* information rate, which is referred to as the system's *goodput*:

$$\eta(\gamma) = R_M R_C [1 - P_{bl}(b, \gamma)], \tag{15}$$

where  $\gamma$  may represent either  $\gamma_c$  of Eq (6) or  $\gamma_{ei}$  of Eq (8) or  $\gamma_u$  of Eq (9),  $R_M$  denotes the 'rate' i.e. the throughput of the modulation scheme, while  $R_C$  is that of the channel code. Still referring to Eq (15),  $P_{bl}(b, \gamma)$  represents the BLock Error Ratio (BLER) corresponding to the particular Modulation and Coding Scheme (MCS) employed. In this paper, we assume that Bit Interleaved Coded Modulation (BICM) [29] is employed, which relies on Gray mapped Mary Quadrature Amplitude Modulation (QAM) [30], where we have  $M = 2^b$  and b = 2, 4, 6 represents the number of bits per QAM symbol. Hence the modem's throughput is  $R_M = b$ . In our paper, we employ  $2^b$ -ary QAM combined with Rate Compatible Punctured Codes (RCPC) [31] having six selected MCSs, namely Mode  $[1, \ldots, 6]$  of  $[R_M, R_C] =$ [(2, 1/2), (2, 3/4), (4, 1/2), (4, 3/4), (6, 2/3), (6, 6/7)].

In practice, obtaining the BLER curves for all the MCSs by simulation is time-consuming, especially in our multicell multiuser system-level evaluations. Let us hence circumvent this time-consuming process with the aid of a more efficient semi-analytical process. We commence by briefly highlighting the derivation of the BLER  $P_{bl}(b, \gamma)$  of a 2<sup>b</sup>-ary QAM aided BICM scheme based on the BLER  $P_{bl}(b = 1, \gamma_0)$  of a BPSK modulated BICM scheme transmitting over an AWGN channel, where only  $P_{bl}(b = 1, \gamma_0)$  is evaluated by simulation. To this effect, we first define the appropriate base-line SINR  $\gamma_0$  as that of a binary BPSK scheme, at which we have the same BLER as an arbitrary b-bit/symbol modem, which would typically require an SINR of  $\gamma > \gamma_0$ , i.e. where we have  $P_{bl}(b,\gamma) = P_{bl}(b=1,\gamma_0)$ . We note that the above-mentioned BLER equality holds only, when the mutual information per bit output by the demodulator obeys the relation of  $I(b, \gamma) =$  $I(b = 1, \gamma_0)$ . This is because I serves as the input of the channel decoder, and as long as I remains the same, the ultimate BLER also remains the same. Hence, the mutual information I per bit may be expressed as [29]:

$$I(b,\gamma) = 1 - \frac{2^{-b}}{b} \sum_{i=1}^{b} \mathbb{E}_{w} \times \left\{ \ln \left[ 1 + \sum_{j=1, j \neq i}^{b} \exp \left( -\frac{|u_{j} - u_{i} + w|^{2} - |w|^{2}}{1/\gamma} \right) \right] \right\},$$
(16)

where  $w \sim \mathcal{CN}(0, 1/2\gamma)$  is the complex-valued zero-mean Gaussian noise process and  $u \in \mathcal{A}$  represents the constellation points in the QAM alphabet, with the *i*th bit A being represented by  $u_i, i \in [1, b]$ . When fixing the mutual information per bit as  $I(b,\gamma) = I(b = 1,\gamma_0)$ , we may find the base*line* SINR  $\gamma_0$  for b = 1, where this BPSK modulated scheme achieves the same per-bit mutual information (MI) I as a higher-throughput  $2^{b}$ -ary QAM-aided BICM scheme. More explicitly, the MI per pit  $I(b = 1, \gamma_0)$  is a monotonically increasing function of  $\gamma_0$ , its unique inverse exists. Hence this *base-line* SINR  $\gamma_0$  may be expressed as the inverse-function  $\gamma_0 = I^{-1}[b=1, I(b, \gamma)]$ . This reveals the relation between  $\gamma$ and  $\gamma_0$ , allowing us to find the BLER  $P_{bl}(b,\gamma)$  of a  $2^b$ -ary QAM-aided BICM scheme from that of the simulated BLER of a BPSK modulated BICM scheme, i.e. from  $P_{bl}(b=1,\gamma_0)$ , which may be formulated as:

$$P_{bl}(b,\gamma) = P_{bl}\left\{b = 1, I^{-1}[b = 1, I(b,\gamma)]\right\}.$$
 (17)

As a result, the BLER  $P_{bl}(b, \gamma)$  of the above MCSs may be obtained with the aid of Eq (17), where  $P_{bl}(b = 1, \gamma_0)$  is obtained from the Monte-Carlo simulation of a BPSK modulated BICM scheme employing the above-mentioned RCPC having constituent code-rates of  $R_C = [1/2, 3/4, 2/3, 6/7]$  in an AWGN channel. Finally, the associated effective throughput

TABLE I PROPAGATION REGIMES

Curve	$P_0$	$T_0$	l	$L_D$	$L_N$
1	10mW	10ps	5m	5km	50km
2	160mW	10ps	5m	5km	3km
3	10 mW	10ps	10m	5km	50km
4	10 mW	20ps	5m	20km	50km
5	10 mW	50 ps	5m	125km	50 km

 $\eta(\gamma)$  of Eq (15) expressed in terms of 'bits/s/Hz' may be obtained by assuming a Nyquist roll-off factor of zero. Owing to space limitations, the detailed link-level simulation results are not explicitly shown here.

#### **IV. PERFORMANCE EVALUATION**

#### A. Simulation Assumptions

The system topology considered is illustrated in Fig. 1, where each hexagonal cell has a radius of R, and the distance between the two adjacent BSs is  $D = \sqrt{3}R$ , e.g.  $\overline{B_2B_3} = \sqrt{3}R$ . We considered the Urban-Macro propagation scenario of [26], where we have D = 3km and the distance-dependent pathloss expressed in dB is  $34.5 + 35 \log_{10}(d_0)$ , with  $d_0$  being the distance between any transmitter and receiver in meters. We assume furthermore that the total transmitter power is P = 46dBm and the noise power at the MS is -174dBm/Hz, when an operating in bandwidth of 10 MHz is considered [26]. Moreover, the optical fibre link's normalised Signal-to-Noise-Ratio (SNR) is assumed to be 50dB and the length of the optical fibre is assumed to be five times the distance between the BS and RA, where we have L = 5d, and d is the line-of-sight distance. We opted for  $d = 0.7R, \forall i$ .

The cell-centre area's radius r may be defined as the maximum radius, where a throughput of at least  $\eta = 2bits/s/Hz$ may be maintained in a conventional cellular system employing the classic UFR technique, but beyond this coverageradius it drops below  $\eta = 2bits/s/Hz$ . When employing DASs in a FFR-based cellular system, the transmit power of the BS should be sufficiently high to ensure that the average throughput maintained at a distance of r remains exactly as high as that of the classic UFR technique, while the rest of the power is evenly allocated to the RAs. Hence, when considering the  $N_r = 6$  RAs operating in a non-cooperative DAS aided FFR scenario, the resultant power sharing regime of all the transmitters obeys  $P_B = 2P/5$ , while for the relay we have  $P_R = P/10$ . By contrast, when considering the  $N_r = 6$  RAs operating in a cooperative DAS assisted FFR scenario, the power constraint of Eq (11) is applied. Finally, the ultimate throughput is obtained by averaging the SINR over 4000 simulation runs, and then substituting it into Eq (15) and Eq (17).

## B. Propagation Regimes in the DFO Link

Before detailing our results, the propagation scenario encountered has to be introduced. When the pulses propagate



Fig. 3. Throughput comparison of the traditional UFR system, FFR system and of the  $N_r = 6$  non-cooperative DAS aided FFR system in two-tier scenarios along the  $\theta_{best}$  and  $\theta_{worst}$  directions recorded for characterizing the nonlinear effects of the optical fibre and the accuracy of the SSF Method.



Fig. 4. Throughput comparison of the traditional UFR system, FFR system and of the  $N_r = 6$  non-cooperative DAS aided FFR system along the  $\theta_{best}$ and  $\theta_{worst}$  directions for characterizing the dispersion effects of the optical fibre.

along the optical fibre, both the nonlinearity and the dispersion depend on the peak power  $P_0$  and on the initial width  $T_0$ of the incident pulse. The critical fibre-lengths  $L_N$  and  $L_D$ quantify the length of fibre over which either the nonlinear, or the dispersive effects become dominant during the signalling pulse's propagation. The relations between  $L_N$  and  $P_0$ ,  $L_D$ and  $T_0$  are calculated as follows [22]:

$$L_N = \frac{1}{\xi P_0}, L_D = \frac{T_0^2}{|\beta_2|}.$$
(18)

The typical values of the GVD parameter  $\beta_2$  and the nonlinearity parameter  $\xi$  at a wavelength of  $1.55\mu m$  are [22]  $|\beta_2| \approx 20 p s^2 / km$  and  $\xi \approx 2 W^{-1} km^{-1}$  for standard telecommunication fibres. For a given optical fibre length of L, we have:





Fig. 5. Throughput contours for the  $N_r = 6$  and  $N_r = 12$  non-cooperative DAS aided FFR system.

- if  $L \ll L_N$  and  $L \ll L_D$ , neither the nonlinear nor the dispersive effects impose a significant performance degradation during the pulse's propagation.
- if  $L \ll L_N$  and  $L \sim L_D$ , the nonlinear effects may be ignored and the dispersion will play the dominant role.
- for  $L \sim L_N$  and  $L \ll L_D$ , the dispersion is negligible compared to the nonlinear distortion.
- for  $L \sim L_N$  and  $L \sim L_D$ , both of the nonlinear and dispersion effects are non-negligible.

In this paper, according to the Urban-Macro cell scenario introduced in Section IV-A, we assume the set of  $P_0$  and





Fig. 7. The enhancement of throughput  $\Delta \eta$  contours for the  $N_r = 6$  cooperative DAS aided FFR systems, comparing with non-cooperative DAS aided FFR.

Fig. 6. Throughput comparison of the traditional UFR system, FFR system and the  $N_r = 6$  cooperative DAS aided FFR system along the best direction with 5 sets of optical parameters in Table I multicell multiuser scenario. The legends are shared between the top and bottom graphs.

 $T_0$  values shown in Table I in order to investigate how the nonlinear and dispersion effects of the optical fibre influence the attainable throughput of the wireless channel in the cell-edge area.

## C. Throughput of Cell-centre Area

The attainable throughput of both of the non-cooperative DAS combined with FFR system (Fig. 3 and 4) and the cooperative DAS combined with FFR (Fig. 6 in the cell-centre area rely on the same SINR of Eq (6) introduced in Section III-A. Hence, both of them have the same throughput performance. Explicitly, upon assigning a transmit power of  $P_B = 2P/5$  in the cell-centre area, the throughput of the non-cooperative DAS combined with FFR system and that of cooperative DAS combined with FFR become similar to that of the traditional UFR and FFR systems, provided that the latter two systems assign the full transmit power to the BS.

#### D. Cell-edge Area of Non-cooperative DAS with FFR

Fig. 3 and Fig. 4 compare the throughput of the classic UFR system, of the traditional FFR system and of the non-cooperative RA-aided FFR assisted systems using  $N_r = 6$ ,  $N_m = 6$  in the best and the worst direction in a two-tier scenario. The four sets of optical fibre parameters shown in Table I were used.

1) Throughput along Best Direction: By contrast, when the cell-edge area is considered, observe in Fig. 3 and Fig. 4 that the throughput of the conventional UFR scheme becomes lower than  $\eta = 2$  bits/s/Hz, while that of the conventional FFR scheme is in the range of  $\eta \in [1,3]$  bits/s/Hz. When the non-cooperative RA-aided FFR-assisted system is employed in conjunction with  $N_r = 6$  RAs, a throughput in the range of  $\eta \in [3,5]$  bits/s/Hz is achieved along the best direction.

More explicity, when using the parameters of Table I, Curves 1 - 5 in Fig. 3 and Fig. 4, suggest that:

- Nonlinear Effect of the DFO Link: The comparison of Curve 1 ( $P_0 = 10$  mW) and Curve 2 ( $P_0 = 160$  mW) in Fig. 3 shows how the power assigned to the optical pulses affects the throughput of the wireless link, which was demonstrated by setting  $P_0 = 10 \text{mW}$  and 160 mWof peak power for the optical signalling pulse. Again, the corresponding optical parameters are shown in Table I. Observe by comparing Curves 1 and 2 of Fig. 3 that assigning a  $P_0 = 160 \text{mW}$  power to the optical pulse makes the nonlinearity-induced impairments dominant, which will broaden the spectrum of the optical pulse in the frequency domain. The nonlinearity indirectly results in an increased attenuation for the optical pulses, but this cannot be compensated by an increased transmit power, hence this leads to a boost of the IRI. As a net-result, the system suffers from an approximate throughput loss of 1 bits/s/Hz in the cell-edge area along the best direction.
- Accuracy of SSF Method: Comparing Curve 3 to Curve 1 of Fig. 3, the former is associated with a longer segment *l* used by the SSF method, which reduces the analysis complexity. However, as a result, the predicted throughput is reduced by about 1 bits/s/Hz. By contrast, a shorter

segment l results in a more accurate of the SSF model at the cost of a higher offline analysis complexity. But selecting the probable segment length will strongly affect the results of simulation, which is important for whom doing the relative research. For a typical urban cell size our Monte-Carlo simulation results suggest that l = 5mis an appropriate compromise, which may be trusted as the real attainable throughput of our DFO aided DAS combined with FFR system.

Dispersion Effect of the DFO Link: Fig. 4 demonstrates by increasing the width of the optical signalling pulse from  $T_0 = 10$  ps to 20 ps and 50 ps for Curves 4 and 5, how this affects the throughput of the wireless link, when the non-cooperative RA-aided FFR-assisted system is employed in conjunction with  $N_r = 6$  RAs. Again, when using the optical parameters shown in Table I and setting a peak power of  $P_0 = 10$  mW, the nonlinear effects of the optical fibre become negligible. Comparing Curve 4 ( $T_0 = 20$ ps) and 5 ( $T_0 = 50$ ps) to Curve 1 ( $T_0 = 10$ ps) of Fig. 4, the throughput at the cell-edge remains in the range of  $\eta \in [4, 5]$  bits/s/Hz, but when the optical pulse width is increased, according to Table I from  $T_0 = 10$  ps to 20ps and 50ps, the attainable throughput of the celledge area is reduced. The reason for this observation is that wide pulses are typically broadened to a lesser relative degree along the optical fibre, which also leads to a reduced attenuation both at the optical receiver of the serving RA as well as at the interfering RAs.

2) Throughput along Worst Direction: When considering the worst direction in both Fig. 3 and Fig. 4, regardless of the specific choice of the five parameter sets of Table I, we only achieve a throughput of about  $\eta = 1$  bits/s/Hz. This is due to the above-mentioned worst-case direction problem [6], which becomes the limiting factor in the case of the conventional non-cooperative RA-aided FFR assisted system.

3) Comparison of the Entire Cell's Throughput: Fig. 5 demonstrates the attainable throughput across the entire cell for the different configurations of our non-cooperative RA-aided FFR assisted system associated with Curve 1 of Table I. More explicity, the cell-centre area's throughput contours recorded in Fig. 5 for both configurations are similar. However, the throughput distribution of the  $N_r = 6$  RA-aided configuration recorded for the cell-edge area tends to be more 'patchy', while that of the  $N_r = 12$  RA-assisted configuration tends to cover the entire outer ring more evenly. As a result, the general conclusion emerging for the comparison of these two configurations is that the optimum positioning of DASs should take into account the expected user-distribution and user-load. However, the "worst-case direction" problem persists in both of these two configurations.

## E. Cell-edge Area of Cooperative DAS with FFR

Fig. 6 compares the throughput of the classic UFR based arrangement and of the traditional FFR aided system, as well as of the cooperative RA-aided FFR assisted system using  $N_r = 6$ , which was evaluated along both the best and worst angular directions respectively and employing the five sets

of parameters seen in Table I for the optical fibre link. We consider supporting  $N_m = 6$  MSs roaming in the cell-edge area, where MS *i* is close to the RA *i*. The  $N_m$  MSs are served simultaneously by the  $N_r$  cooperative RAs and they are randomly distributed around the point  $Z_i$ ,  $i = 1, \ldots, N_m$  of Fig. 1, where  $Z_i$  belongs to the corresponding  $60^\circ$ -sector surrounding RA *i*. The MSs are allowed to randomly cross the cell-edge area, but only once, in order to investigate the histogram of the attainable throughput for the  $N_m$  MSs.

1) Throughput along Best Direction: When the cell-edge area is considered, observe the upper figure in Fig. 6 that the throughput of the conventional UFR scheme becomes lower than  $\eta = 2$  bits/s/Hz, while that of the conventional FFR scheme is in the range of  $\eta \in [1,3]$  bits/s/Hz. When the cooperative RA-aided FFR-assisted system using the parameters associated with Curves 1, 4 and 5 of Table I is considered, observe in Fig. 6 that linear TPP achieves a throughput of  $\eta = 5$  bits/s/Hz, which is similar to the throughput upper bound of the RA-aided FFR-assisted system. Hence, when the nonlinearity effects can be ignored, the dispersion does not overly affect the throughput of the wireless channel.

Comparing Curve 2 and Curve 1 in Fig. 6, when using a peak power of  $P_0 = 160$  mW for the signalling pulses, the MMSE TPP techniques achieve a slightly higher throughput than 4 bits/s/Hz. Since the term  $IRI_1$  in Eq (13) is mitigated by the MMSE TPP, the throughput reduction is imposed by the further attenuation of the received optical signalling pulses inflicted by the fibre's nonlinearity. When employing the parameters associated with Curve 3 with a segment length of l = 10m for the SSF method, a throughput reduction of  $\Delta \eta = 1$  bits/s/Hz is encountered.

Observe in Fig. 6 that the throughput of cooperative egBF is between that of the linear TPP techniques and of the traditional UFR system, and it is not always higher than that of the conventional FFR scheme. The reason for this phenomenon is that the performance of the cooperative egBF is also dependent on the geographic distribution of the  $N_m$  users. Hence the served MS may suffer from an increased interference, which imposes an increased throughput erosion in comparison to the conventional FFR scheme.

2) Throughput along Worst direction: It is demonstrated in the lower figure of Fig. 6 that the cooperative RA-aided FFR assisted system does not suffer from the worst-case angular direction problem and hence the linear TPP techniques achieve a throughput of  $\eta = 5$  bits/s/Hz, which is the upper bound of the RA-aided FFR-assisted system. The other curves exhibit the same throughput performance as that shown in the upper figure of Fig. 6. The cooperative egBF does not solve the worst-case angular direction problem, hence its throughput is lower than that of the traditional FFR.

#### F. Enhancement of Throughput Across the Entire Cell

In order to observe the attainable throughput improvement  $\Delta \eta$  achieved by the cooperative RA aided FFR assisted systems over their non-cooperative counterparts across the entire cell, the resultant throughput contour profile associated with Curve 1 of Table I is portrayed in Fig. 7. We configured the cooperative techniques for enhancing the attainable

throughput in the cell-edge area, hence in the cell-centre area we have  $\Delta \eta = 0$ . In the cell-edge area, when considering the cooperative MMSE arrangement for example, there is a significant throughput improvement in the worst-case angular direction, since we have  $\Delta \eta = 4$ bits/s/Hz in the direction  $\theta_{worst}$ . By contrast, when the MS is roaming close to the RA, the throughput improvement achieved by the cooperative MMSE technique remains limited. When however the MS is roaming far from the RA, the benefits of the cooperative techniques become more pronounced.

## V. CONCLUSIONS

The achievable throughput of a DFO aided DAS relying on FFR and a realistic optical fibre backhaul was investigated in practical multicell, multiuser scenarios. Our work demonstrated that the non-cooperative DAS aided FFR system is capable of gleaning some benefits from the imperfections of the optical fibre, because the dispersion of the optical signalling pulse might indirectly increase the attainable throughput of the cell-edge area. More explicity, when applying the configurations of  $N_r = 6$  and  $N_r = 12$ , the geographic throughput distribution becomes different, which may be beneficially exploited for supporting different geographic users-distributions. Correspondingly, the cooperative RA-aided FFR relying on the linear TPP techniques <sup>1</sup> advocated is capable of efficiently mitigating the IRI in the worst-case direction. As a result, the system may be capable of supporting a throughput of  $\eta = 5$  bits/s/Hz, regardless of the specific geographic userdistribution encountered. Furthermore, the cooperative RAaided FFR system may become tolerant to the dipsersion of the optical pulse, but sensitive to the fibre-induced nonlinearity, if the optical pulse has a high power.

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<sup>1</sup>Indeed, efficient TPP requires efficient feedback control, which involves an accurate and frequent channel estimation, quantisation and feedback process, where sophisticated signal processing improvements may result in an increased throughput. The overhead associated with this cooperative transmission, or closed-loop design in general, is constituted by the Dopplerdependent channel-sounding pilot overhead and the feedback quantisation overhead, where the latter potentially depends not only on the quantisation method performed, but also on the specific cooperative structure employed, i.e. on whether centralised or distributed cooperation is used.

Regarding the effect of the numbers of RAs, an intuitive observation is that the more cooperative RAs, the more overhead will be incurred. However, no simple quantitative relationship may be established. Furthermore, since the amount of overhead imposed may offset the potential gain achieved, we have to strike an attractive tradeoff, as discussed in [32]. The rate of change of the channel will indeed significantly decrease the resultant performance gains, since the feedback may become more outdated and the preprocessing matrix will be subject to strong mismatch. Hence, closed-loop designs in general may not be suitable for high-velocity applications, where in addition to an increased normalized feedback delay, the channel estimation becomes more challenging in the downlink.

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