

Analysis of a strike-slip fault network using high resolution multibeam bathymetry, offshore NW Devon U.K.

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1. Introduction

The analysis of fault networks is vital to understanding the brittle deformation of the earth's crust as faults rarely occur individually and without associated deformation. Therefore, the major aim of this paper is to assess the changes in geometry, fault displacement and topology within a strike-slip fault network at different scales, hence, investigating the role of small and large faults. It will also demonstrate the use of high resolution multibeam bathymetry data as a tool to map and analyse an offshore strike-slip fault network.

22 Initial work on fault populations includes the application of power-law distributions to
 23 fault populations. This has been particularly useful for describing fault growth by
 24 looking at the distribution of fault displacement and fault trace lengths (Cartwright et
 25 al., 1995; Gupta and Scholz, 2000; Soliva and Schultz, 2008; Xu et al., 2010).
 26 Geometric and kinematic studies of fault populations have also contributed by
 27 adding to the understanding of fault segmentation, growth and propagation (e.g.
 28 Peacock & Sanderson 1991, 1994; Cartwright et al., 1995; Childs et al., 2003;
 29 Taylor et al., 2004; Bull et al., 2006; Baudon and Cartwright, 2008). Other work has
 30 investigated the importance and contribution of small scale faulting to the overall
 31 extension of an area (e.g. Walsh et al., 1991; Marrett and Allmendinger, 1992, Putz-
 32 Perrier and Sanderson 2008a, 2010) and their role in block rotations (e.g. Peacock
 33 et al., 1998).
 34 This work suggests that fault systems evolve by individual faults increasing in both
 35 length and displacement, and that they become more linked with increasing finite
 36 strain (Ferrill et al., 1999; Walsh et al., 2001). This has been further supported by
 37 studies which show that fault populations evolve into longer and simpler systems
 38 with strain becoming localized within a fault system (e.g. Cowie et al., 1995; Nicol et
 39 al., 1997; Cowie et al., 2005; Moriya et al., 2005; Soliva and Schultz, 2008).
 40 The use of high resolution reflection seismology has helped investigate
 41 displacement rate patterns within fault networks, both temporally and spatially,
 42 adding further to our understanding of fault movement, interaction and linkage
 43 within fault networks (Taylor et al., 2004; Mouslopoulou et al., 2009; Nicol et al.,
 44 2010). More recently Nixon et al. (2011) use aerial photography combined with field
 45 data to map a strike-slip fault network at Westward Ho!, north Devon. This
 46 demonstrated a spatial variation in fault pattern, displacement distribution and

kinematic behaviour, hence, illustrating the heterogeneity of deformation within a fault network.

This paper seeks to further this study by combining the techniques used in Nixon et al. (2011) with multibeam bathymetry data to map and describe a strike-slip fault network offshore Hartland Point, north Devon (Fig. 1). It will determine the overall fault trends and kinematic behaviour of the network, investigating the possible affects of changing resolution on the geometry, topology, connectivity, and strain distribution within the network. This is then compared and correlated with onshore strike-slip networks at Hartland Quay and Westward Ho!.

2. Geological Setting

The strike-slip faults in north Devon cut Upper Carboniferous mudstones, siltstones and sandstones of the Crackington, Westward Ho!, Bideford and Bude Formations (Fig. 1) (Higgs et al., 1990). These form part of the Culm Basin that was later inverted at the end of the Carboniferous period during Variscan deformation, which produced ~E-W trending upright folds throughout the region (Sanderson, 1979; 1984).

The strike-slip faults comprise NE-trending left-lateral faults and NW-trending right-lateral faults that are related to approximately N-S compression. The precise age of the strike-slip faults may not be determined stratigraphically, but field evidence shows that they do post-date the late Variscan folding (Higgs et al., 1990). Hence, it is thought that these faults formed in either: **1)** a late Variscan right-lateral shear zone that occurred during the Late Paleozoic (Arthaud and Matte, 1977; Badham, 1982) caused by oblique NW-SE convergence between the African and European

plates (Coward and McClay, 1983; Sanderson, 1984; Barnes and Andrews, 1986; Holdsworth, 1989); or **2**) during late Cretaceous-Tertiary N-S shortening (Lake and Karner, 1987; Chadwick, 1993; Peacock and Sanderson, 1998) caused by the northward collision of the African plate into the Eurasian plate and/or Atlantic ridge-push forces as Britain drifted from the American plate (Underhill and Patterson, 1998).

Some strike-slip faults in north Cornwall and Devon are known to be reactivated (Kim et al., 2001). For example, the Sticklepath-Lustleigh fault zone (Fig. 1) is thought to have formed in the late Variscan event as a NW-trending right-lateral fault zone before undergoing left-lateral reactivation in the late Cretaceous-Tertiary (Holloway and Chadwick, 1986). The faults at Hartland do not show signs of multiphase movement or reactivation and, hence, their precise age is not important for this study. What is important is that the upright folding, steeply dipping bedding and strike-slip nature of the faults allow accurate measurements of displacements from mapped offsets of folds and stratigraphy.

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3. Mapping Methods

The strike-slip fault network was mapped from high resolution multibeam bathymetry data of the offshore region to the north and west of Hartland Point (Fig. 1). These data were collected as part of the UK Civil Hydrography Programme with the data being collected in 2007 and 2008 by two vessels: MV Meridian using a Reson 7125 400 kHz multibeam, and MV Jetstream using a Kongsberg Maritime EM3002D multibeam. The data are of high quality and image features at the coast

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94 in water depths of only –1.0 m chart datum. This coverage was achieved by
95 surveying at high tide and utilising the large tidal range in the Bristol Channel.
96 The multibeam bathymetry data were imported into ArcGIS for analysis and
97 interpretation, and a geo-referenced 3D image with a pixel resolution of 0.5 m was
98 created. Interpretation was completed using Hillshade images which accentuated
99 bedding and fault traces. The degree of slope was also calculated from the
100 multibeam data, and this combined with measurement of the strike of identified
101 bedding planes, allowed determination of the strike and dip of bedding.
102 The multibeam bathymetry (Fig. 2) revealed a submerged platform of bedrock
103 extending ~2.5 km from the shore line which provided a much more extensive area
104 of faulting to be mapped (~16 km²), than that exposed at low tide on the wave-cut
105 platforms. The high quality of the multibeam data allowed direct correlation of
106 bedding and faults with features mapped onshore on wave-cut platforms (Fig. 2).
107 However there are localised sand pockets offshore which prevents correlation in
108 some of the more sheltered coves such as the areas between Dyers Lookout and
109 Damehole Point and adjacent to Upright Cliff.
110 The faults were digitized along with cut-offs of marker beds that allowed the
111 calculation of multiple, lateral separations along fault traces. Each fault was then
112 segmented along its trace-length at each measured offset point and an average
113 displacement determined for each fault segment. Offsets are difficult to measure at
114 intersections between two faults, hence, fault segments that share an intersection
115 point with another fault were attributed the same displacement value as the
116 measured offset point at the other end of the segment. This means that all the
117 faults comprising the network are divided into segments and that each is associated

118 with a value of displacement. The extracted fault segment data was the primary
119 structural data that was used for further analysis.

120 The mapped fault network was correlated with onshore field mapping at Hartland
121 Quay (a well studied and easily accessible part of the coastline with numerous and
122 well exposed fold hinge lines and faults), where further 3D structural data was
123 collected including bedding, fault orientations and slickenside measurements where
124 possible.

126 **4. Mapping Results**

127 ***4.1 Folds and bedding attitudes***

128 The multibeam bathymetry images an extensive submerged platform of bedrock
129 with a general E-W trend of moderately to steeply dipping and folded bedding. This
130 matches the attitude of bedding seen in onshore cliffs and wave cut platforms (Fig.
131 3a). Onshore mapping from Hartland Quay shows that the bedding has been
132 intensively folded, with chevron folds varying in wave-lengths from 15-80 m (Fig. 4).
133 This folding has been studied in detail from the cliff outcrops (e.g. Tanner, 1992;
134 Davison et al., 2004) and can also be seen offshore. Throughout the submerged
135 platform many marker beds that can be traced around fold hinges (Fig. 3).
136 Stereographic projections of poles to bedding show that the folds trend
137 approximately E-W related to N-S compression (Fig. 5). The profile planes from
138 both onshore and offshore bedding data correlate with each other (Fig. 5) indicating
139 that the strike and dip measurements of bedding taken from the multibeam
140 bathymetry data are accurate. However, there is a bias in the dip data from

offshore due to the more limited availability of exposed bedding surfaces needed for slope calculations as the dip increases.

4.2 Relationship between faults and folding

Mapping from the multibeam bathymetry indicates there are two distinct sets of faults based on their trend and lateral separation. The NW-trending have consistent right-lateral separations and NE-trending faults have left-lateral separations (Fig. 2). The relationship between the mapped faults and folding indicates that the faults post-date the folding, as the faults cut and offset both layering and fold axial traces (Fig. 3b).

The fault sets mapped from the bathymetry can be traced onshore (Fig. 3c) and correlate with onshore observations at Hartland Quay, where there are many examples of NW-trending right-lateral faults and NE-trending left-lateral faults (Fig. 4). Folds at Hartland Quay are also cross-cut by the faults, with fold hinges defining piercement points on both fault sets that show a dominant component of strike-slip offset (Figs. 4 and 6). Furthermore, structural measurements taken from Hartland Quay show that the fault planes are sub-vertical and have sub-horizontal slickensides (Fig. 5a).

Thus, the mapped offshore and onshore faults are strike-slip based on the fact that:

- 1) They form two separate fault sets in map view that have consistent and opposite lateral separations, forming NW-trending right-lateral faults and NE-trending left-lateral faults (Fig. 2);
- 2) Both sets are steeply dipping with shallowly plunging slickensides (Fig. 5a);
- 3) They laterally offset fold hinges and limbs in the same direction (Figs. 3b and 4);

165 4) Fold hinge lines form piercement points with a dominant strike-slip
166 displacement (Fig. 6a).

167 ***4.3 Spatial distribution and relative proportions of fault sets***

168 The strike-slip fault network is dominated by NW-trending right-lateral faults as seen
169 in the (length x displacement) weighted rose diagram (Fig. 2b). These make up
170 80% of the overall trace-length with the largest right-lateral faults showing
171 displacements of up to 146 m. Left-lateral faults are less numerous and much
172 smaller, forming conjugate intersections with right-lateral faults (Fig. 7).

173 The larger right-lateral faults have long traces (up to 2.6 km) that approximately
174 divide the stratigraphy into elongated NW-trending blocks. Within these blocks are
175 many smaller right-lateral and left-lateral faults. Many of these are isolated, but
176 some are connected to each other by small left-lateral faults. Within the fault
177 blocks there is a slight anticlockwise rotation of stratigraphy and, combined with the
178 right-lateral dominance, this suggests that the strike-slip fault network is acting in a
179 domino fashion controlled by the larger right-lateral faults (c.f. Nixon et al., 2011).

181 **5. Displacement and Scaling**

182 The ability to map displacements along the lengths of the fault traces allows the
183 fault network to be displayed at different scales. Figure 8 shows a series of maps of
184 the network produced by clipping the fault segments at different displacements,
185 ranging from 0.5-50 m (Fig. 8). This is referred to as a 'displacement cut-off' and is
186 similar to the approach used by Watterson et al. (1996) to analyse the scaling
187 properties of faults in the South Yorkshire coalfield. Rather than giving a maximum

188 displacement/throw to a whole fault trace this technique is applied to each fault
189 segment, which provides a more accurate representation of resolution as it
190 preserves the spatial location of the faults and clips trace lengths by removal of the
191 low displacement segments at fault tips (c.f. Pickering et al. 1997).

192 Different attributes can be measured at each resolution clipping (i.e. trace-length,
193 fault density, fault set percentages, strain etc.), which is particularly useful for
194 analysing the distribution of each attribute across different sizes of fault within the
195 network. Using 10 m as a displacement cut-off value allows a direct comparison of
196 small and large fault segments and helps assess their role within the fault network,
197 with small fault segments and large fault segments having <10 m displacement and
198 ≥ 10 m displacement, respectively. The value of 10 m is used as it corresponds
199 with the approximate limit of resolution in many 3-D seismic reflection surveys.

200 ***5.1 Effects of scale on the spatial arrangement of the fault*** 201 ***network***

202 At high displacement cut-offs (i.e. Figs 8a and 8b) the network is dominated by a
203 few, long, isolated right-lateral faults, but at lower cut-offs the system appears more
204 connected with smaller conjugate left-lateral faults connecting the larger right-lateral
205 faults (Figs 8c, d, and e). This is reflected in the trace-length percentages for each
206 fault set with left-lateral faults increasing from 7% to 20% with the inclusion of faults
207 with less than 10 m displacement (Fig. 9c).

208 The larger fault segments form boundaries to NW-trending elongated blocks of
209 stratigraphy with small fault segments infilling the spaces in between, increasing
210 fault density from 1.8 to 5.9 km⁻¹ (1 km⁻¹ represents 1 km of fault trace per square
211 km). Consequently, at high displacement cut-offs coherent and “unfaulted” regions

appear between a series of widely spaced right-lateral faults when in reality there is deformation at a smaller scale within the blocks.

It is apparent that the small fault segments are either infilling faults, small left-lateral faults, or tips of larger faults. These are responsible for the increase in fault density and have a significant effect on the distribution of trace-length. A plot of trace-length density vs displacement cut-off (Fig. 9a) shows the distribution of fault trace-length across different fault sizes. The majority of trace-length is taken up by smaller fault segments with the larger-displacement (>10 m) fault segments only making up 30% of the trace-length. This is a further reflection of the increased deformation within the fault blocks with the inclusion of smaller fault segments.

There are few conjugate intersections between fault segments with >10 m displacement, with the formation of strike-slip relays (Peacock & Sanderson 1995) being the main source of fault interaction, whereas splays and abutting faults become more frequent with the inclusion of smaller fault segments. Hence, the fault network appears less connected at high displacement cut-offs.

This analysis shows that the spatial arrangement of the fault network varies with scale, with the appearance of left-lateral faults at higher resolutions. Watterson et al. (1996) observe a somewhat similar pattern for multiple sets of normal faults in the southern Yorkshire coal fields, with one fault set being cut out at high-throw cut-offs. This suggests that this variation with scale is common where one fault set is dominant.

5.2 Strain distribution

The displacements calculated for each fault segment were used in a tensor analysis of strain, which provides an estimate of the maximum extension and its orientation.

236 This involves the calculation of a Lagrangian strain tensor from the cross-product of
 237 the unit normal and displacement vectors of each fault segment. Peacock and
 238 Sanderson (1993) apply this to faults sampled along a line, using a weighting factor
 239 to correct for the orientation bias of such samples. The same approach is valid for
 240 sampling on a plane, where (displacement x segment length) / unit area replace the
 241 displacement / unit length in a line sample. The weight (w) is determined from the
 242 angle between the fault normal and the plane. As we are dealing with sub-vertical
 243 strike slip faults, both the fault normal and displacement vector lie close to the sub-
 244 horizontal plane of the sample and the weighting factor can be ignored (i.e. $w \rightarrow 1$).
 245 The eigenvectors and eigenvalues of the strain tensor provide estimates of the
 246 orientation and magnitude of the principal strains. For a more detailed methodology
 247 see Nixon et al. (2011).
 248 The strain analysis shows that the area has an overall maximum extension of
 249 ~4.2% in a WNW-ESE orientation, with the large fault segments and small fault
 250 segments accommodating extensions of 3.5% and 0.7%, respectively (Table 1).
 251 The plot of percentage extension vs displacement cut-off shows the distribution of
 252 strain for different fault sizes within the network (Fig. 9b). Even though most of the
 253 fault trace length is taken up by smaller fault segments, 86% of the overall
 254 extension is accumulated on fault segments with ≥ 10 m displacement and ~45%
 255 by fault segments with > 40 m displacement.
 256 There is a small variation in maximum horizontal extension direction from N113°E
 257 for large faults to N107°E for small faults (Table 1). Although small, and
 258 undoubtedly within the errors of the determination of the principal strain axes, this
 259 sense of rotation is consistent with the domino behaviour of the system. The overall
 260 orientation of maximum extension is N112°E (see Table 1) which is weighted more

261 towards the large fault segments of the fault network. This indicates that the
 262 mechanical behaviour of the fault network is mainly controlled by the larger fault
 263 segments within the network.

264 Overall, the majority of strain throughout the strike-slip network is accommodated by
 265 the large fault segments. Putz-Perrier and Sanderson (2008) show similar
 266 distributions of strain for normal faults at Kimmeridge Bay with large faults
 267 accommodating 65% of the overall strain, suggesting localization of strain onto the
 268 larger faults. This has also been seen in numerical and physical modelling (Cowie
 269 et al., 1995; Ackermann et al., 2001; Mansfield and Cartwright, 2001).

270 Although strain is localized onto the larger fault segments, the smaller fault
 271 segments are still significant, accommodating 14% of the overall extension. This is
 272 due to the high trace-length of small fault segments. Thus, our work on strike-slip
 273 faults systems (this paper; Nixon et al., 2011) supports similar work by Putz-Perrier
 274 & Sanderson (2008a,b, 2010) on normal faults, and establishes by direct
 275 measurement the relative contribution to deformation made by faults with different
 276 displacements. This is an important factor in understanding extension estimates
 277 from seismic data as the faults that are too small to be resolved seismically may
 278 contribute significantly to the total strain, as was originally suggested by
 279 extrapolation assuming power-law scaling (e.g. Walsh et al., 1991, Marrett and
 280 Allmindinger, 1992, Jackson and Sanderson 1992; Pickering et al., 1996).

281 Pickering et al. (1997) recognise that fault lengths and throws of normal fault tips
 282 are often not seismically resolved. Therefore, estimates of sub-seismic strain using
 283 displacement scaling of fault populations will still underestimate sub-seismic strain
 284 as they do not take into account any additional contribution from fault tips, linkage
 285 zones and associated damage. By using fault segments rather than individual

faults, this study incorporates the effects of fault tips and linkage zones, with that of small faults, in evaluating their role in accommodating extension within a basin.

6. Topology

The fault network was analysed in terms of a system of fault branches between tips (I-nodes) or intersections (X- or Y-nodes) (Fig. 10). Manzocchi (2002) uses this system to estimate connectivity by looking at the relative proportions of I-, Y- and X-nodes for fracture networks. Like fracture networks, fault networks become connected through a combination of crossing fault intersections (X-nodes), and abutments and splays of fault tips (Y-nodes). Hence, for this study the combined percentage of X- and the Y-nodes was used to represent the connectivity of the fault network. This is then taken further by analysing how the percentage and nature of connecting nodes within the fault network changes with resolution.

The percentages of different node (Table 2) show that the fault network offshore Hartland Point is dominated by I-nodes (isolated tips). Connecting nodes make up just 21.2% of all nodes with the majority being Y-nodes. Two different types of Y-node can be identified: **1)** Synthetic Y-nodes where two faults with the same motion sense intersect resulting from a fault linkage or splay; and **2)** Antithetic Y-nodes where two faults with the opposite motion sense intersect as a result of one fault abutting another. The latter make up over 50% of all connecting nodes which emphasizes the importance of conjugate fault sets when considering the connectivity of a fault network.

The plot of connecting node % vs displacement cut-off shows that the percentage of fault branches ending at Y-shaped or X-shaped nodes approximately halves with

the exclusion of the small fault segments (Fig. 11). This is quite significant considering that there are no connecting nodes present for fault segments at displacement cut-offs of greater than 25 m, resulting in the network appearing very unconnected at low resolutions. Furthermore, the nature of interacting Y- and X-nodes varies with scale. Synthetic Y-nodes (or splays) are dominant for faults with >5 m displacement, whereas for faults with <5 m displacement, antithetic Y-nodes dominate and crossing X-nodes are occasionally developed. This pattern suggests that larger faults are more likely to form linkage and splays, due to fault growth, and that low displacements are usually needed for crossing X-shaped fault intersections to be preserved.

Overall the offshore network at Hartland is poorly connected, but the connectivity of the strike-slip network increases with increasing resolution, particularly with the inclusion of faults smaller than the seismic resolution cut-off. This, combined with an increase in fault density from 1.8 to 5.9 km⁻¹, indicates that the connectivity of the fault network is very dependant on small fault segments. Pickering et al. (1997) found similar results when modeling the connectivity of normal fault tips, highlighting the importance of underestimating the connectivity of fault networks due to the limited resolution of seismic data.

7. Discussion and Comparison with Westward Ho!

Analysis of the offshore strike-slip fault network at Hartland shows that the distribution of different attributes varies with displacement. This has highlighted three main points: 1) small faults, fault tips and linkage zones contribute the majority of the overall trace-length; 2) strain is localized onto individual large displacement

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334 fault segments; 3) at low displacement cut-offs the fault network appears more
335 connected with the inclusion of small faults, fault tips and linkage zones. To show
336 that these observations are applicable to other fault networks, the same scaling
337 analysis has been applied to an onshore strike-slip fault network at Westward Ho!
338 previously described by Nixon et al. (2011).

339 **7.1 Westward Ho!**

340 The fault sets at Westward Ho! have orientations that match those found offshore
341 from Hartland Point (NW-trending right-lateral faults and NE-trending left-lateral
342 faults), and they also post-date folding. The network has large faults that divide the
343 rock-mass into elongated blocks with small faults accommodating deformation
344 within each block, not unlike the offshore network. There is much heterogeneity
345 within the fault network at Westward Ho!, with fault set dominance changing
346 throughout (Nixon et al., 2011), however the geometric and lithological similarities
347 with the offshore fault network make Westward Ho! a good comparison. Three
348 contrasting small areas of intense deformation from within the fault network at
349 Westward Ho! were chosen for comparison (Fig. 12):

350 **Left-lateral area** – This has the highest strain value of the three areas with an
351 overall maximum extension of ~26.8% and an orientation of N068°E resulting from
352 the left-lateral dominance of the fault network (Nixon et al., 2011). The majority of
353 the trace-length, 71%, is taken up by small fault segments (Table 1). However,
354 94% of the overall extension is accommodated by the larger fault segments, which
355 is the largest proportion in comparison with the other two onshore areas.

356 **Damage Area** – This is a region of more internal deformation lying between large
357 left-lateral faults (Fig. 12) and has an overall maximum extension of ~24.3% with an

orientation of N077°E. The trace-length density is almost double the trace-length density of the left lateral area (Table 1) and small fault segments, make up 79% of overall trace-length (Table 1). Hence, the small fault segments are much more significant than in the left-lateral area and accommodate 14% of the overall extension.

Right-lateral area – This has the lowest strain value of the three areas with an overall maximum extension of ~15.7% and an orientation of N112°E. Again the majority of the trace-length is taken up by the small fault segments with only 12% being taken up by the large-fault segments (Table 1). The distribution of strain shows a similar pattern with 77% being localized onto the large fault segments, however, this is much less than both the left-lateral and damage areas (Table 1).

7.2 Strain

Overall the three areas at Westward Ho! accommodate much higher strains and fault densities in comparison with the offshore network at Hartland (Table 1). This is not an effect of resolution as it is consistent for all displacement cut-offs (Fig. 13), instead this indicates that the areas at Westward Ho! are more intensely deformed. The linear-log plots (Fig. 13) show that the three onshore areas have a similar pattern of trace-length and strain distribution to the fault network offshore. Most of the fault trace-length is taken up by small displacement (<10 m) fault segments and the majority of the strain is still accommodated by large displacement (≥10 m) fault segments, again supporting the idea of strain localization onto larger faults.

The distributions of strain for the three onshore areas at Westward Ho! show that more strain is localized onto the larger fault segments with an increase in strain (Table 1). This is reflected in the linear-log plot of strain vs displacement cut-off

(Fig. 13b) as an increase in gradient at higher displacements and suggests that as strain increases strain becomes localized onto higher displacement fault segments. This is consistent with the observations of Nicol et al. (1997) who show that, with increasing strain, networks have faults with higher displacement rates. Whilst strain localization appears to increase with increasing strain for the three areas at Westward Ho!, the fault network offshore from Hartland Point does not fit this observation. Even though the offshore network accommodates much lower strains than the onshore areas at Westward Ho!, 85% of the strain is localized onto the large fault segments, which is a higher proportion than the right-lateral area and similar to the damage area (Table 1). This is due to the increased deformation seen at Westward Ho! as indicated by the high strains and fault densities (Table 1, Fig. 13). Strain is localized to areas of intense deformation, not just individual fault planes, and accommodated by internal deformation within fault blocks and associated damage zones. Hence, in areas of localized deformation less strain is localized on the larger fault segments due to increased amounts of internal deformation between large faults. Pickering et al. (1996) found similar affects for normal faults by fitting to power-law distributions of the form

$$N \propto (\text{displacement})^{-D},$$

where the D-value is termed the power-law exponent. They found that for a D-value of 0.5 almost all the extension is taken up by faults with heaves greater than 20 m, whereas for a D-value of 0.9 their contribution decreases to less than half. As an increase in the D-value of a fault population reflects a higher degree of small-

scale faulting, this supports the idea that for areas with increased amounts of internal deformation less strain is localized onto the larger faults. The significance of small faults within areas of internal deformation is also reflected in the strain orientations with the damage area accommodating less rotation in comparison to the left-lateral area. This is opposite to the conclusions of Peacock et al. (1998) who proposed that small faults added to the overall rotation of an area. This difference is due to the nature of internal deformation, with the majority of small faults in this study being antithetic and conjugate to the bounding faults. Although the small fault segments have an increased significance in areas with increased deformation the majority of strain is still accommodated by the larger fault segments, indicating that the kinematic behaviour of the fault network is controlled by the large faults.

7.3 Connectivity

The connecting node percentage (X- and Y-nodes) for the left-lateral, damage and right-lateral areas at Westward Ho! are 45.5%, 73.5% and 37.5%, respectively (Table 2). The majority of connecting nodes are antithetic Y-nodes, which agrees with the offshore fault network and further emphasizes the importance of conjugate fault sets when considering connectivity. The percentages for all connecting nodes are much higher than the offshore network indicating that the three areas at Westward Ho! are better connected. The damage area is also the most connected, mainly due to its increased fault density.

A ternary plot of I-, Y-, and X-node proportions illustrates the connectivity changes of a fault network with increasing resolution. In general, the networks become better connected away from the I-node corner of the triangle (Fig. 14), but see

Manzocchi (2002) for a more detailed discussion of this in terms of percolation theory. Overall the proportion of connecting nodes within each fault network, from both Westward Ho! and Hartland Point, increases with increasing resolution. The right-lateral area has a similar connectivity pathway to the network at Hartland Point. They both follow the I-Y margin of the ternary diagram and only have a small contribution of connecting X-nodes, even at high resolutions. The left-lateral and damage areas also follow the I-Y line on the ternary diagram. However, they are influenced much more by the presence of connecting X-nodes and are more connected at higher resolutions.

All the fault networks experience a significant increase in the proportion of X- and Y-nodes once faults with less than 12 m displacement are included (Fig. 14). However, the fault networks at Westward Ho! are also better connected than at Hartland Point suggesting that fault networks become more connected with increasing strain (Table 2 and Fig.14). Furthermore, the damage area is much more connected than the right and left-lateral areas indicating that damage zones and areas with increased internal deformation are better connected. These areas often have increased numbers of smaller faults further supporting the idea that connectivity is reliant on small faults.

This indicates that even though the connectivity of fault networks is primarily dependant on the length, density and orientation of the faults and their spatial correlation (Berkowitz et al., 2000), strain and the nature of its localization also plays an important role. Fault networks appear to be better connected when strain is localized to an area, creating damage zones of intense deformation and high fault densities, rather than when strain is localized onto individual faults forming longer and simpler systems. This also suggests that connectivity increases with increased

amounts of deformation. Micarelli et al. (2006) show similar results with the connectivity of fracture networks being higher in intensely deformed damage zones than in weakly deformed damage zones around normal fault planes.

8. Summary and Conclusions

Multibeam bathymetry has been used to identify and map an extensive area of a strike-slip fault network offshore from Hartland Point, north Devon. The fault network comprises NW trending right-lateral faults and NE trending left-lateral faults and behaves in a right-lateral domino fashion. The spatial arrangement, topology, and distribution of strain and trace-length of the fault network vary with resolution:

- 1) Small (<10 m) displacement fault segments infill fault blocks, bounded by large displacement (10-150 m) faults, and make up most of the trace-length.
- 2) Strain is localized onto the large-displacement fault segments with ≥ 10 m displacement that bound the fault blocks.
- 3) The kinematic behaviour of the fault network is controlled by rotation between the large faults.
- 4) Fault networks appear less connected at lower resolutions as the connectivity of the fault network is very dependant on the presence of small fault segments.

Comparison with onshore field examples from Westward Ho! confirms these points with similar distributions of strain and fault trace-length. Furthermore, combining the two datasets suggests that strain localization and connectivity are influenced by both the overall strain and amount of internal deformation:

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- 477 **5)** More strain is localized onto the larger-displacement fault segments,
478 however, small fault segments can make an important contribution to strain
479 in areas with large amounts of internal deformation (damage zones).
480 **6)** Connectivity of a fault network increases with increasing strain as well as
481 with increasing resolution.
482 **7)** Damage zones and areas with internal deformation are better connected due
483 to increased contributions of small fault segments and high fault densities.
484 **8)** Fault networks are better connected when strain is localized to an area rather
485 than when strain is localized onto individual faults.

486 The comparison with the onshore fault networks at Westward Ho! confirms that the
487 observations from the analysis of the offshore fault network at Hartland are
488 applicable to other fault networks. The techniques and methods developed for this
489 study have helped to further the analysis of fault networks. The application of high
490 resolution multibeam bathymetry imagery has allowed expansion and uncovering of
491 an extensive fault network. This combined with analysis of fault patterns, topology
492 and distribution of resulting strains highlights the importance of resolution when
493 investigating crustal deformation, particularly when considering faults smaller than
494 the seismic resolution cut-off.
495

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500 multibeam bathymetry data (HI 1158: Bristol Channel - Barnstable Bay), and staff at
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502 photography was provided by the Channel Coastal Observatory.

503

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Figure Captions

Fig. 1 Location map with the main geological units. The grey area represents the interpreted offshore region.

Fig. 2 a) Interpreted multibeam bathymetry image from offshore Hartland Point showing the extent of the mapped fault network. Inset are the locations of the images in Fig. 3. b) Length-weighted rose diagram indicating the main fault trends.

Fig. 3 Multibeam bathymetry images with applied hillshade effect showing the quality of the imagery and the onshore-offshore correlation: a) An aerial photograph image (onshore) of strata and fold structures (grey) that can be traced into the offshore bathymetry survey (colour); b) An image of the seabed c. 2.5 km offshore showing an anticline that is cut by right and left-lateral

661 faults showing offsets in the same direction on both limbs; c) An offshore
 662 bathymetry image (colour) with faults, strata and foldstructures which can be
 663 traced onto an onshore aerial photograph (grey).

664 Fig. 4 Fault map of a wave-cut platform at Hartland Quay showing lateral
 665 offsets of fold axial traces. Points A-A' and B-B' represent the piercement
 666 points shown in the field photographs in Figure 6a and b, respectively.

667 Fig. 5 Equal-area stereographic projections: a) fault and bed data from
 668 Hartland Quay, the dotted lines represent right-lateral faults and solid lines
 669 represent left-lateral faults; b) offshore bedding data measured from the
 670 multibeam bathymetry.

671 Fig. 6 Interpretation of field photographs from Hartland Quay showing folds
 672 cut by strike-slip faults, a) Small fold with steeper N-dipping and shallower S-
 673 dipping limb, with hinge in same bed forming a piercement offset of 8.4 m
 674 right-laterally (A-A'). b) Large fold with hinge in same bed offset ~48 m right-
 675 laterally (B-B').

676 Fig. 7 A plot of displacement against azimuth for the fault segment data
 677 offshore from Hartland Point.

678 Fig. 8 Displacement maps of fault segments offshore Hartland Point. Each
 679 map has a different displacement cut-off representing different resolutions: a)
 680 50 m, b) 20 m, c) 10 m, d) 3 m and e) 0.5 m.

681 Fig. 9 Linear-log plots of fault data from offshore Hartland Point showing the
 682 distribution of trace-length (a) and % extension (b) vs displacement cut-off. c)

Indicates the proportion of trace-length taken up by right-lateral (black) and left-lateral (grey) faults.

Fig. 10 a) Schematic diagram illustrating a system with fault branches and nodes. b) A ternary plot of I-, Y-, and X-node proportions illustrating the connectivity of the schematic fault network. In general, fault networks become better connected away from the I-node corner of the triangle, see Manzocchi (2002) for a more detailed discussion of this in terms of percolation theory.

Fig. 11 Linear-log plot of connecting node % vs displacement cut-off.

Fig. 12 Fault map of the wave-cut platform at Westward Ho! showing the localities of the left-lateral, damage and right-lateral areas, respectively. Modified from Nixon et al. (2011).

Fig. 13 Linear-log plots of fault data from the left-lateral, damage and right-lateral areas. a) trace-length density vs displacement cut-off and b) % extension vs displacement cut-off. The data for the offshore network is also included for comparison (grey).

Fig. 14 Ternary diagram of I-, Y- and X-Node percentages showing the connectivity pathways from 50 m resolution to full resolution of the fault networks from offshore Hartland Point and onshore Westward Ho!.

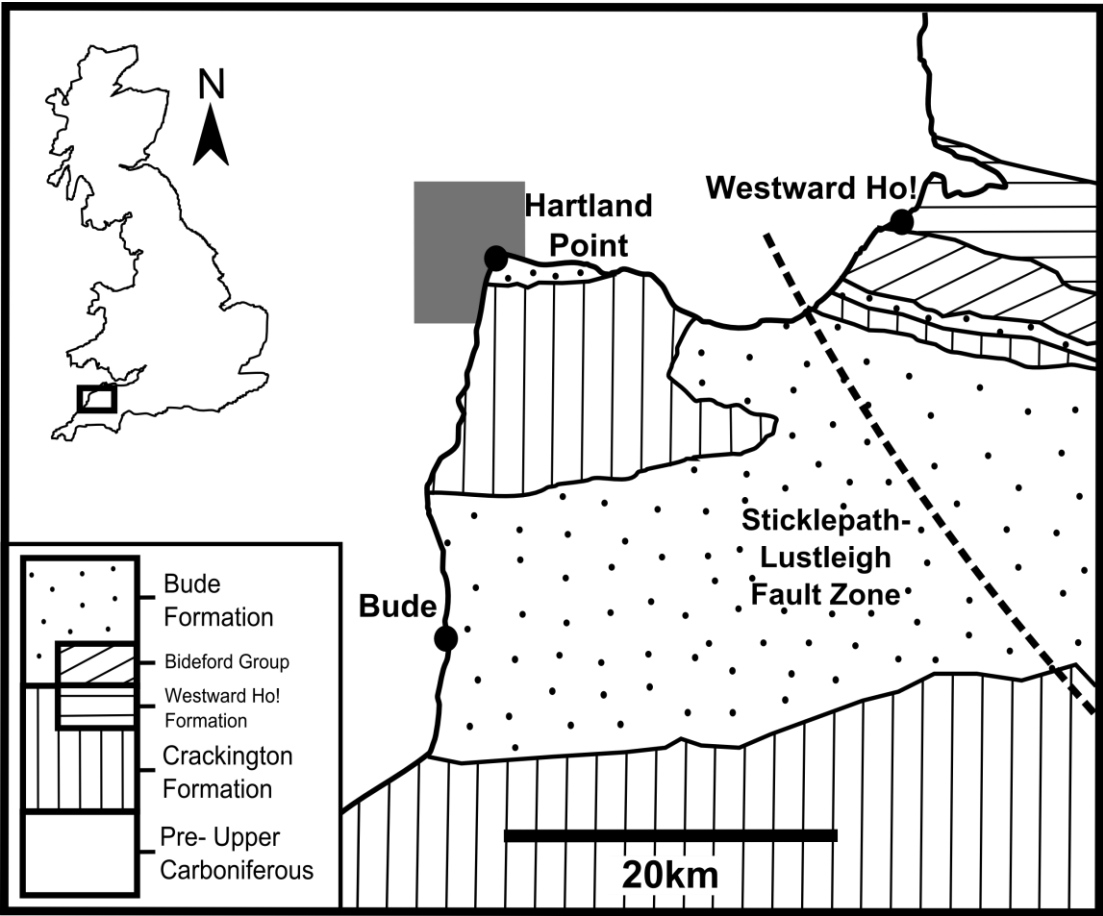
Table 1. Structural characteristics and distribution of strain and trace-length within the fault networks offshore Hartland Point and onshore Westward Ho!

	Offshore Hartland Point			Left-lateral - Westward Ho!			Damage - Westward Ho!			Right-lateral - Westward Ho!		
	Overall	Small fault segments (<10 m)	Large fault segments (>=10 m)	Overall	Small fault segments (<10 m)	Large fault segments (>=10 m)	Overall	Small fault segments (<10 m)	Large fault segments (>=10 m)	Overall	Small fault segments (<10 m)	Large fault segments (>=10 m)
Trace-length	-	70%	30%	-	71%	29%	-	79%	21%	-	88%	12%
% extension	4.2	0.7	3.5	26.8	1.6	25.2	24.3	3.4	20.8	15.7	3.5	12.2
Proportion of Strain	-	14%	86%	-	6%	94%	-	14%	86%	-	23%	77%
Orientation of maximum extension (θ)	N112°E	N107°E	N113°E	N068°E	N089°E	N067°E	N077°E	N093°E	N074°E	N112°E	N107°E	N114°E
Fault Density (km ⁻¹)	5.9	-	-	39.5	-	-	80.4	-	-	45.1	-	-

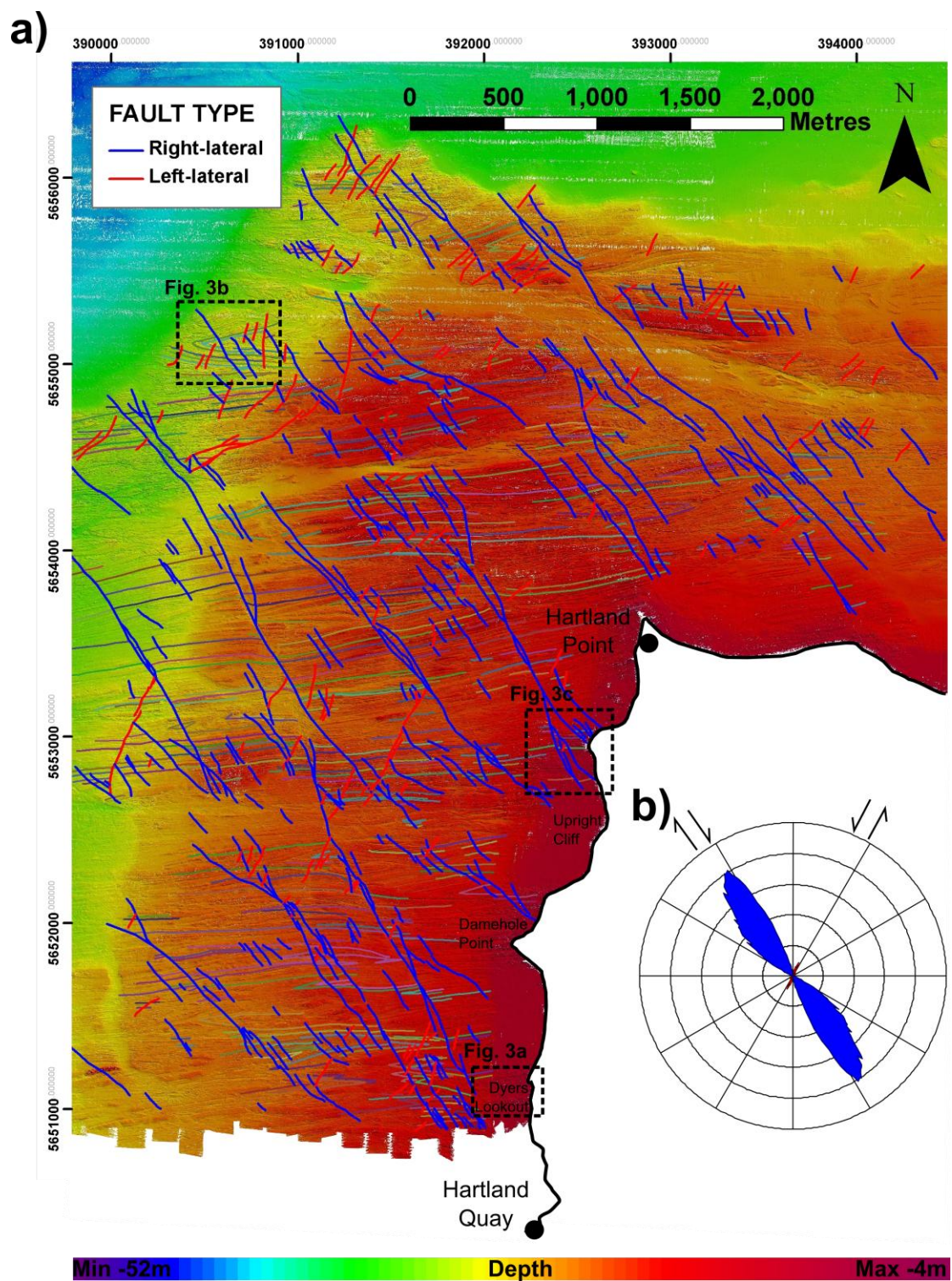
Table 2. Nodal percentages of the fault networks from offshore Hartland Point and onshore Westward Ho!

	I-Node %	Y-Node %		X-Node %
		Synthetic	Antithetic	
Offshore Hartland Point	78.8	6.5	11.5	3.2
Left-lateral - Westward Ho!	54.5	6.4	25.7	13.4
Damage - Westward Ho!	26.5	18.8	42.7	12.0
Right-lateral - Westward Ho!	63.5	15.2	19.2	2.1

Figure

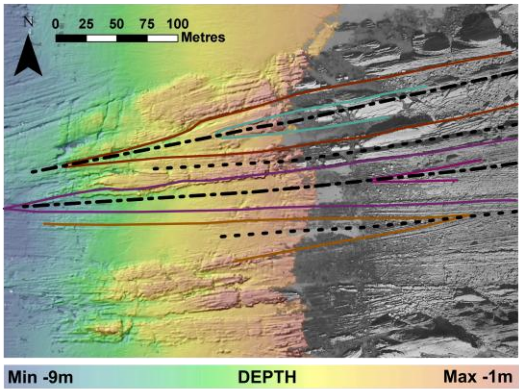


Figure

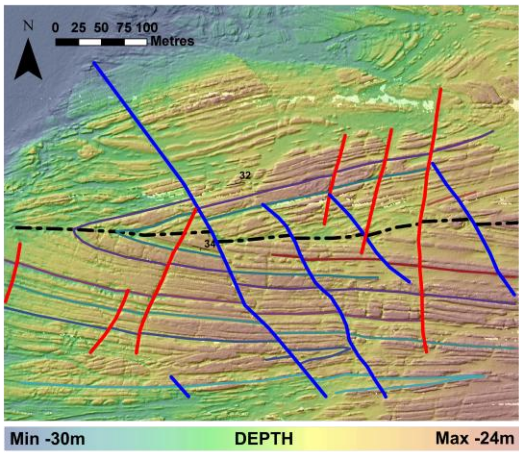


Figure

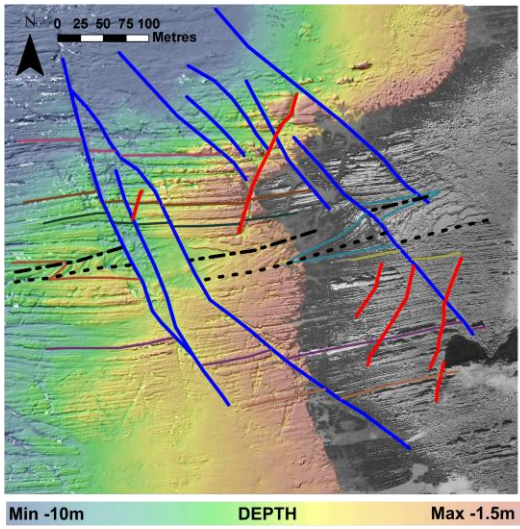
a)



b)

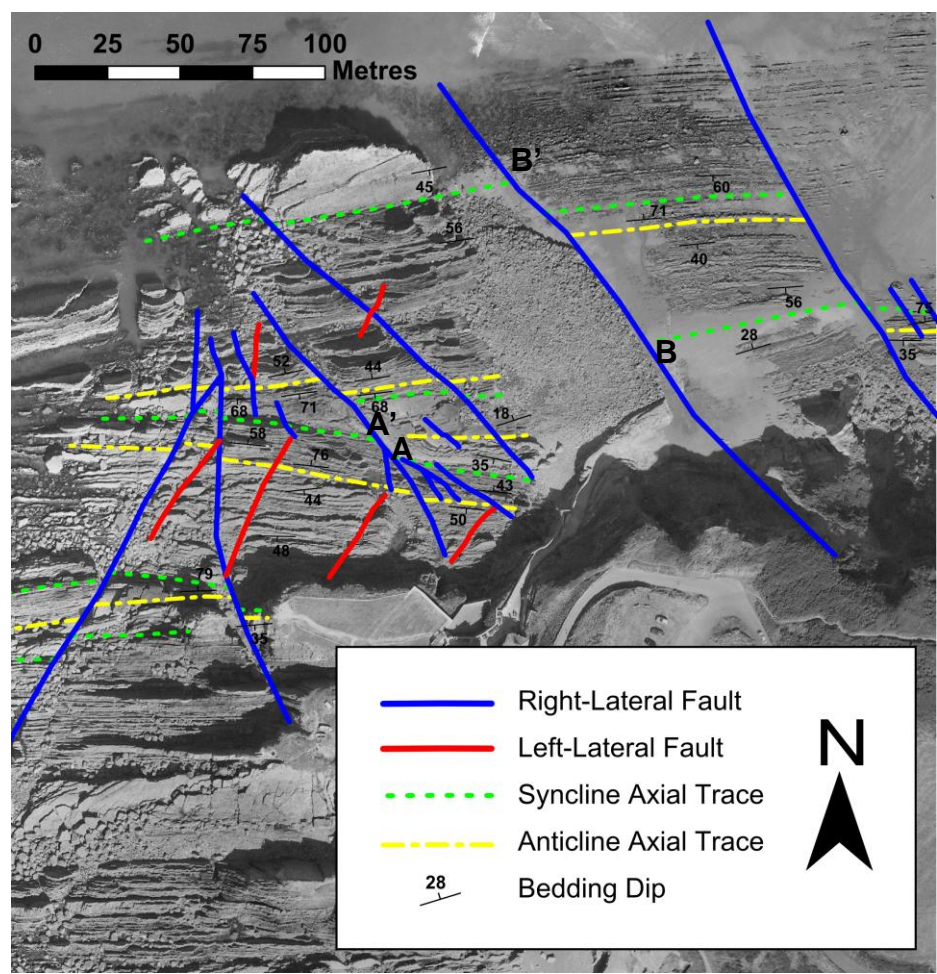


c)

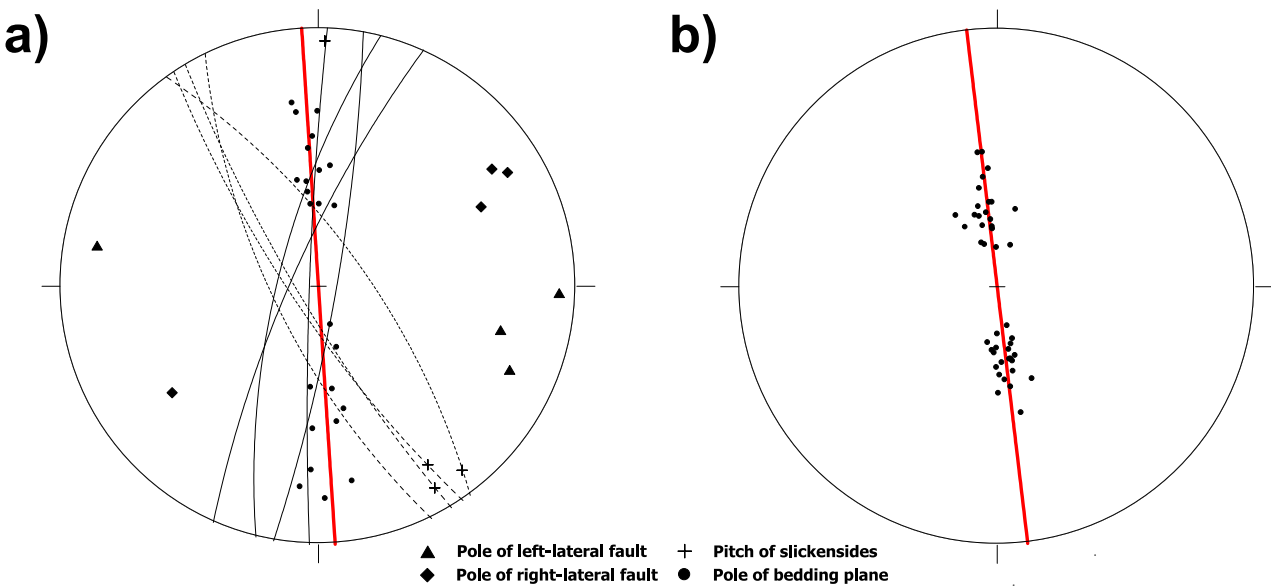


- Right-Lateral Fault
- Left-Lateral Fault
- - - Syncline Axial Trace
- - - Anticline Axial Trace
- 28 Bedding Dip

Figure

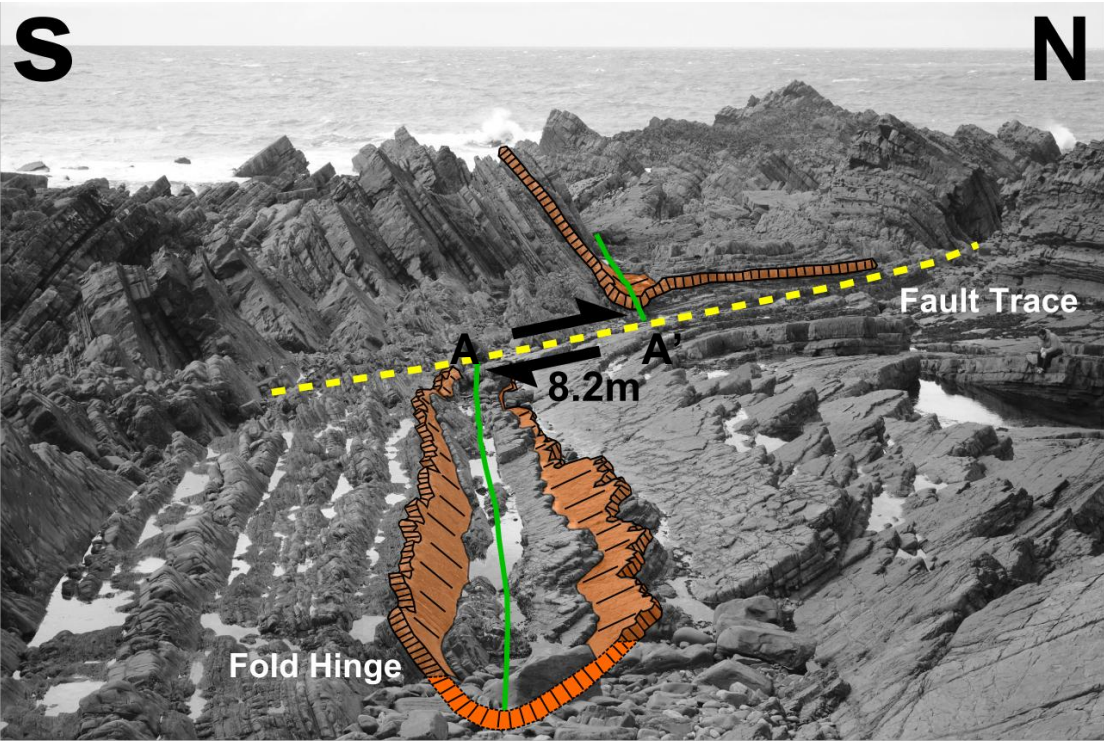


Figure

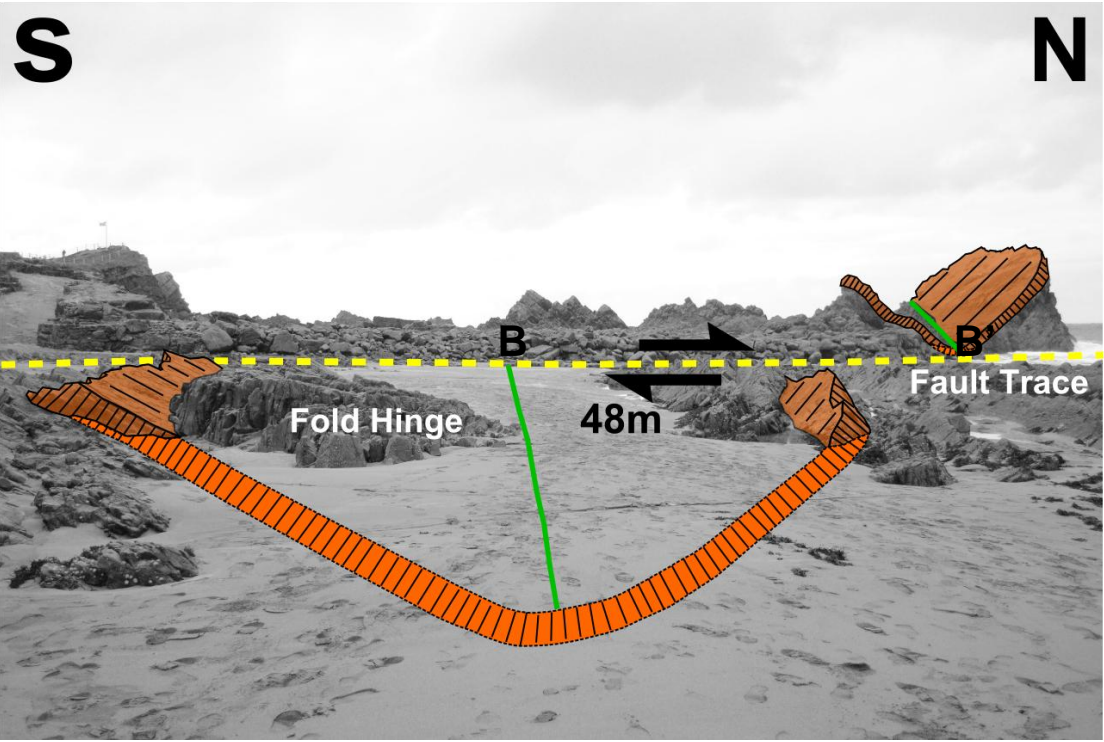


Figure

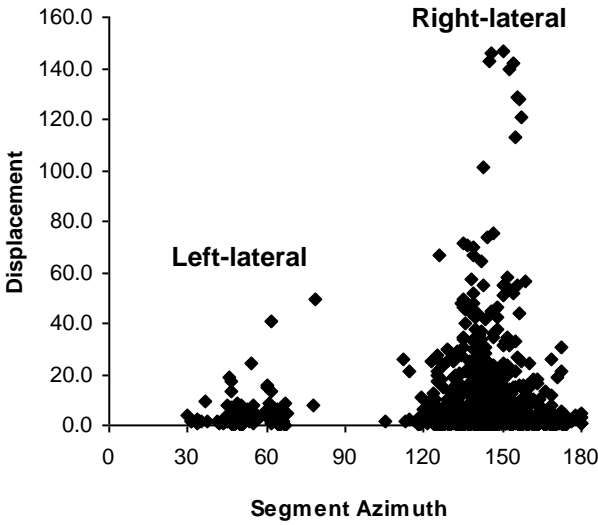
a)



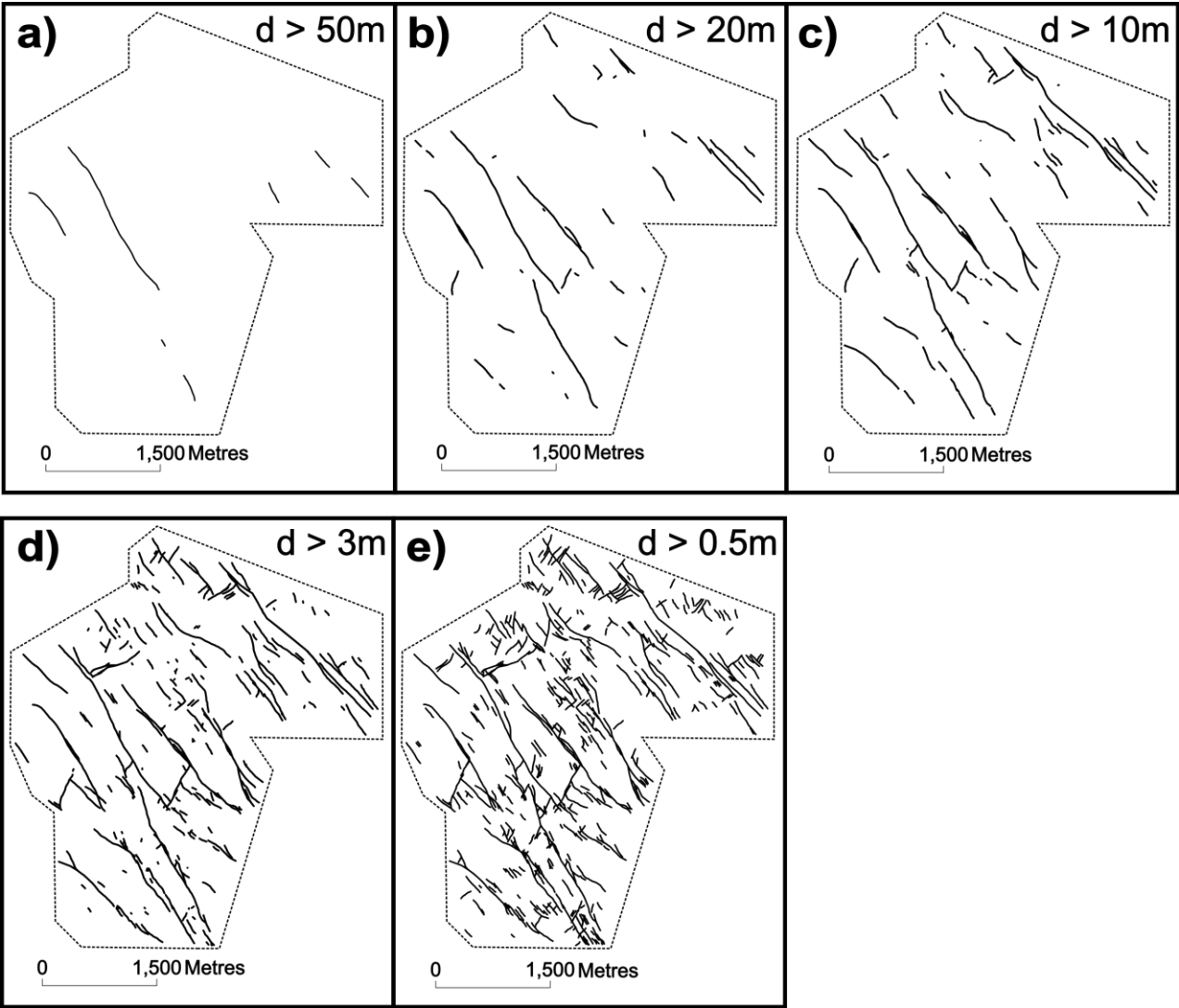
b)



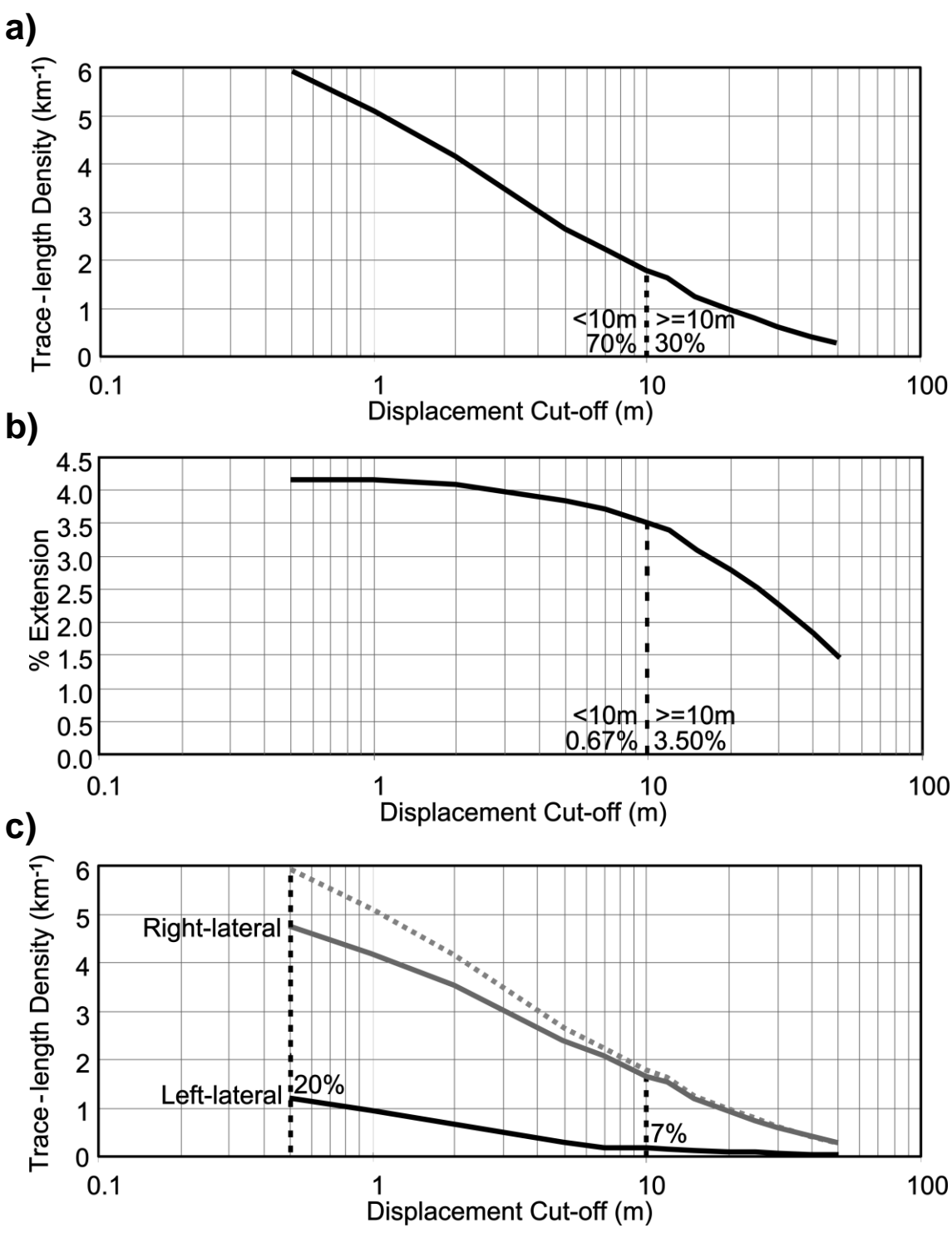
Figure



Figure

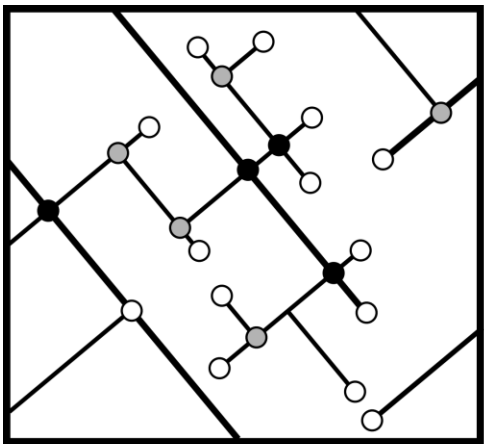


Figure



Figure

a)

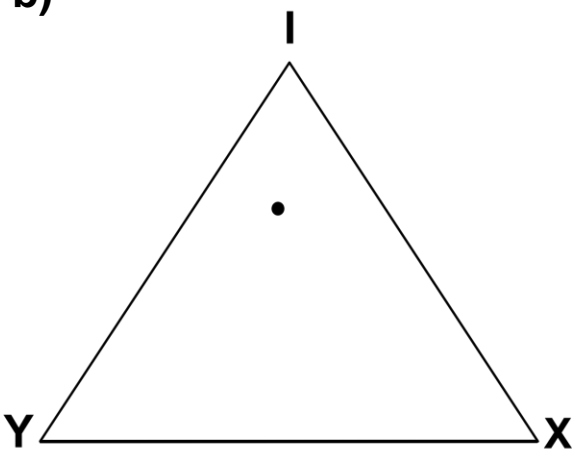


○ = I-Type Node
(n = 14)

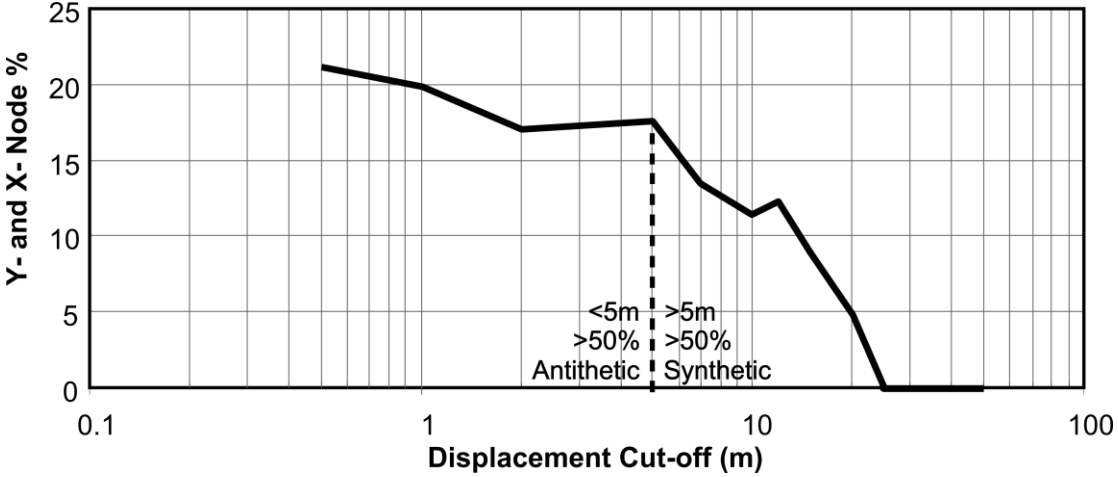
● = Y-Type Node
(n = 5)

● = X-Type Node
(n = 4)

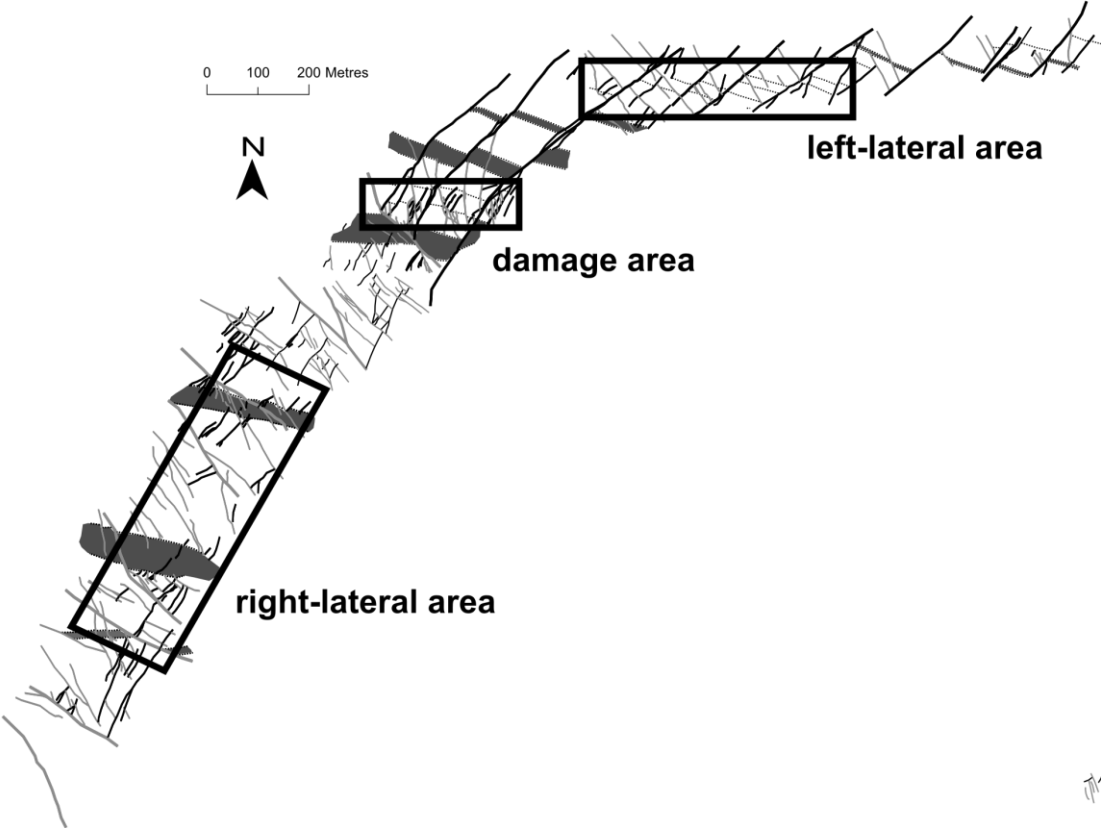
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Figure

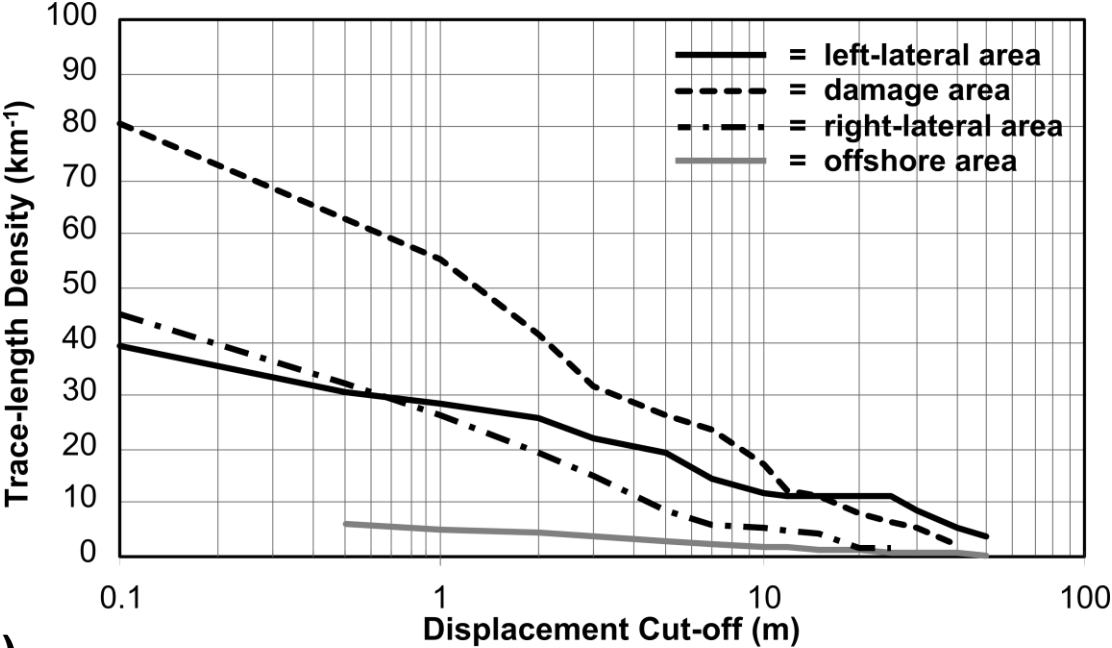


Figure

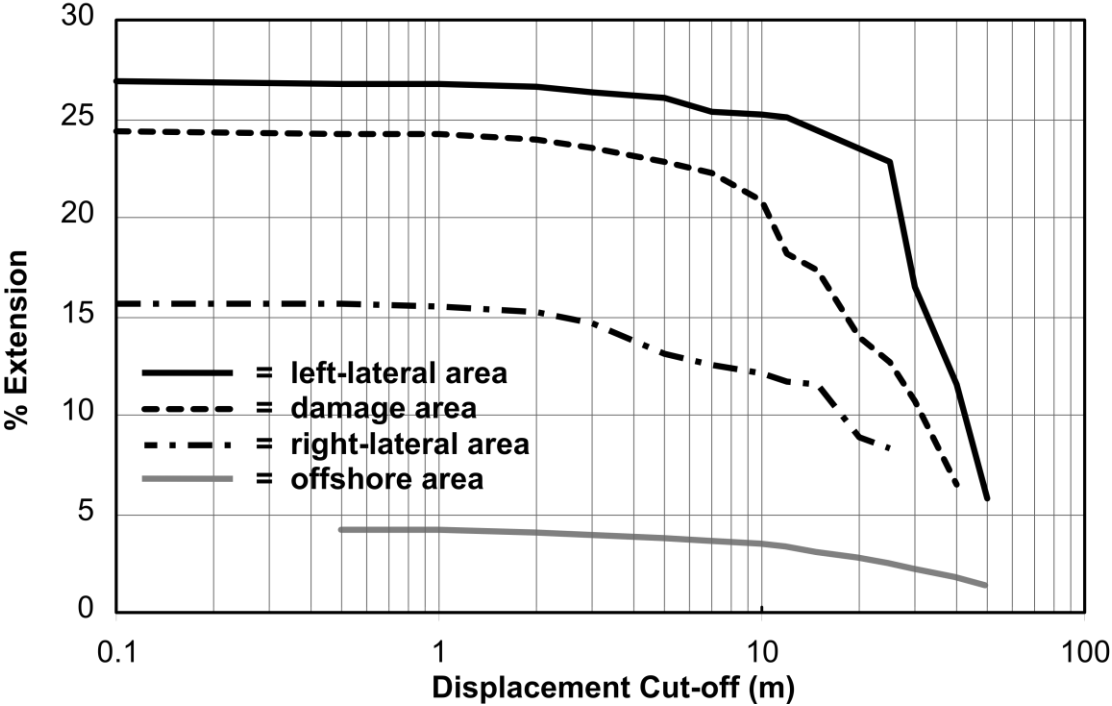


Figure

a)



b)



Figure

