

1 **Large-Eddy Simulation of Heat Transfer from a Single Cube**
2 **Mounted on a Very Rough Wall**

3 **V.B.L. Boppana · Z-T Xie · I.P. Castro**

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6 **Abstract** The local thermal effects in the wake of a single cube with a strong heated
7 rear face, representing a large building in an urban area, are studied using large-eddy
8 simulations (LES) for various degrees of heating, which are characterized by the lo-
9 cal Richardson number, Ri . New wall models are implemented for momentum and
10 temperature and comparison of the flow and thermal fields with the wind-tunnel data
11 of Richards et al. (Journal of Wind Engineering and Industrial Aerodynamics, 2006,
12 94, 621-636) shows fair agreement. Buoyancy effects are quite evident at low Ri and
13 a significant increase in the turbulence levels is observed for such flows. Apart from
14 the comparisons with experiments, further analysis included the estimation of the
15 thermal boundary-layer thickness and heat transfer coefficient for all Ri . For suffi-
16 ciently strong heating, the heat transfer coefficient at the leeward face is found to be
17 higher than the roof surface. This suggests that, beyond a certain Ri value, buoyancy
18 forces from the former surface dominate the strong streamwise convection of the lat-
19 ter. Quadrant analysis along the shear layer behind the cube showed that the strength
20 of sweeps that contribute to momentum flux is considerably enhanced by heating.
21 The contribution of different quadrants to the heat flux is found to be very different
22 to that of the momentum flux for lower Ri .

23 **Keywords** Heat flux · Rough wall · Single cube · Wall model

24 **1 Introduction**

25 Rapid increase in urbanization over the last few decades has given rise to several
26 challenging problems in the field of Urban meteorology. One of the challenges is un-
27 derstanding and modelling the thermal effects in urban flows. These can arise because

V. B. L. Boppana · Zheng-Tong Xie · Ian P. Castro
School of Engineering Sciences
University of Southampton
Tel: +44(0)23 8059 2320
Fax: +44(0)23 8059 3058
E-mail: V.B.Boppana@soton.ac.uk

28 the background atmosphere is non-neutral or because of localized surface heating of
29 buildings in the urban canopy. This paper focusses on the latter.

30 There have been various investigations of thermal effects using wind-tunnel and/or
31 field experiments or numerical computations. Several of the latter have used Reynolds
32 Averaged Navier-Stokes (RANS) and large-eddy simulations (LES) of two-dimensional
33 (2-D) canyons in neutral atmospheres. These have shown that local differential heat-
34 ing within the urban canopy has various effects on the canyon flow and pollutant
35 dispersion (Sini et al., 1996; Kim and Baik, 1999; Li et al., 2010; Cheng and Liu,
36 2011; Cai, 2012; Park et al., 2012). In these studies, it was observed that buoyancy
37 forces due to ground or leeward wall heating strengthen the intensity of the circula-
38 tion within the canyon, resulting in increases in the vertical exchange rates of passive
39 pollutants. In a three-dimensional (3-D) RANS study by Dimitrova et al. (2009) on
40 a geometry that resembles an urban area in Lisbon, Portugal, it was observed that
41 the airflow within the canyon was significantly altered by the solar heating of the
42 building surfaces. These computations clearly indicated that surface heating has sig-
43 nificant impact on the flow inside the canyons. However, some field studies (Louka
44 et al., 2002; Offerle et al., 2007; Idczak et al., 2007) suggest that the buoyancy effects
45 on the canyon flow are not as significant as those suggested by the computations. This
46 could be attributed either to inadequate numerical representation of flow or thermal
47 physics near the wall or too simplified a model geometry, although it should be noted
48 that point measurements in the field are inevitably very limited. A few field stud-
49 ies also suggest, firstly, that large horizontal thermal gradients exist in the vicinity
50 of walls heated by solar radiation (Louka et al., 2002) and, secondly, that the heat
51 transfer is very intermittent within the wall boundary layer of a leeward-heated wall
52 (Nottrott et al., 2011). This implies that grid resolution in the computations has to be
53 very fine, or that sophisticated near-wall models need to be developed.

54 Therefore, with the broader aim of simulating canopy stability effects in urban
55 areas and obtaining accurate estimates of the heat flux from building walls by resolv-
56 ing the thermal boundary layer, we first simulated dispersion from a passive scalar
57 area source in an array of roughness elements using LES (Boppana et al., 2010). This
58 is analogous to dispersion from surface heat sources when the resulting temperature
59 differences are sufficiently small that they do not influence the flow dynamics. These
60 simulations showed good agreement with the wind-tunnel experiments of Pascheke
61 et al. (2008). Our next step was then to use LES to simulate the buoyancy effects
62 in urban flows – i.e. when temperature differences *do* influence the flow dynamics
63 – and this paper presents the results. A wind-tunnel study by Richards et al. (2006),
64 in which the leeward face of a cube was heated, was considered to be appropriate
65 for validation of our numerical methodology. Hereafter, ‘experiments’ refer to this
66 wind-tunnel study unless specified otherwise.

67 The numerical details of the computational study are outlined in Sect. 2. In Sect. 3,
68 results of computations from the heated cube are compared with the experiments and
69 some details on the thermal boundary-layer thickness, heat transfer coefficient and
70 quadrant analysis of momentum and heat fluxes are presented. Finally, conclusions
71 are given in Sect. 4.

2 Numerical Details and Settings

2.1 Governing equations and boundary conditions

The filtered continuity and Navier–Stokes equations governing unsteady incompressible flow are

$$\frac{\partial u_i}{\partial x_i} = 0, \quad (1a)$$

$$\text{and } \frac{\partial u_i}{\partial t} + \frac{\partial u_i u_j}{\partial x_j} = -\frac{\partial}{\partial x_i} \left(\frac{p}{\rho} \right) + \frac{\partial}{\partial x_j} \left(\frac{\tau_{ij}}{\rho} + \nu \frac{\partial u_i}{\partial x_j} \right) + f \delta_{i3}. \quad (1b)$$

The resolved-scale velocity and pressure are respectively given by u_i and p with u , v and w the streamwise, lateral and vertical velocity components respectively. $f \delta_{i3}$ is the body force due to thermal buoyancy and is estimated using the Boussinesq approximation; ρ and ν are the density and kinematic viscosity of the fluid; τ_{ij} is the subgrid-scale (SGS) Reynolds stress and was handled using the Smagorinsky model in conjunction with a Lilly damping function near the walls. We set Smagorinsky's constant $C_s = 0.1$.

At the inlet, the inflow method proposed by Xie and Castro (2008) was used as the boundary condition. In the lateral (y) direction, a periodic boundary condition was employed and at the outlet, a zero normal gradient for u , v and w with a mass balance correction was imposed. Stress free conditions were imposed at the top of the domain. The boundary condition for the bottom surface is treated with a rough-wall model, with details given in Sect. 2.3.

The filtered governing equation for temperature is

$$\frac{\partial \theta}{\partial t} + \frac{\partial u_j \theta}{\partial x_j} = \frac{\partial}{\partial x_j} \left((k_s + k_m) \frac{\partial \theta}{\partial x_j} \right), \quad (2)$$

where θ is the resolved-scale temperature. k_s is the subgrid turbulent diffusivity and is given by ν_s / Pr_s , where ν_s is the subgrid viscosity and Pr_s is the subgrid Prandtl number whose value was set to 0.9. k_m is the molecular diffusivity and is defined as ν / Pr_m . The gradient (normal to the boundary) of the temperature was set to zero at the top of the domain and at the outlet.

A finite volume approach was followed to discretize the flow and temperature equations. The monotone advection and reconstruction scheme (?) with a blending factor of 0.9 was used for the spatial convective terms and the central difference scheme is used for spatial diffusive terms of (1) and (2). A second-order backward implicit scheme was used for discretizing the time-dependent term. The initial and average durations of the simulations were approximately 120 and $200L_x/u_{\text{ref}}$ respectively, where L_x is the streamwise domain length and u_{ref} is the time- and spatially-averaged streamwise velocity at the top of the domain. Tests showed that this was sufficient to produce statistically converged data. All the computations were carried out using ? version 4.14.

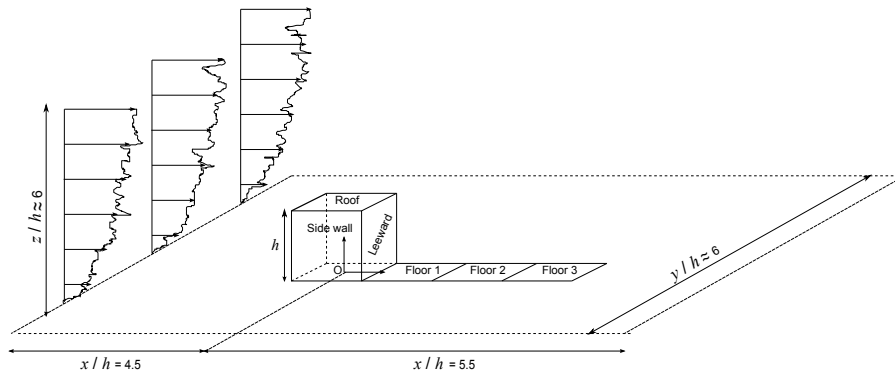


Fig. 1 Sketch of 3-D view of the computational domain with a single cube. The heated surfaces are shown.

104 2.2 Settings

105 In the wind-tunnel experiments, the cube height (h) was 0.19 m; the cube was made
 106 of plaster of Paris and an aluminium plate of 2 mm thickness was fitted on its leeward
 107 face. This plate was heated from inside using a ceramic radiant heater that was
 108 powered by an autotransformer. The leeward face thus had neither constant temper-
 109 ature nor constant heat flux. This imposed some difficulty in specifying the exact
 110 heat boundary condition in our computations. However, temperature was measured
 111 at two points approximately equi-distant either side of the centre point on the leeward
 112 face in the experiments. The average of these measurements is given in Table
 113 1 of Richards et al. (2006) and this value was specified as the uniform temperature
 114 on the leeward face in the present computations. In the experiments, thermocouples
 115 were also mounted on the top surface, defined hereafter as the ‘roof’, and two stream-
 116 wise faces (also called ‘side’ faces) of the cube, and on the bottom floor behind the
 117 cube. The measured values were again specified as uniform temperature boundary
 118 conditions in the computations (see later). Unlike the roof and side faces, it is not
 119 clear from Richards et al. (2006) at what location the temperature was measured on
 120 the bottom floor. We have assumed that the temperature on the floor decreases with
 121 increasing distance from the leeward face. Therefore, as an approximation of this,
 122 different surface temperatures were specified uniformly in the three regions of size
 123 $h \times h$ shown in Fig. 1; the values are tabulated in Table 1. In the experiments there
 124 were no roughness elements positioned in the surrounding region of the cube; to simu-
 125 late this, the third square region denoted by ‘floor 3’ in Fig. 1 and a region of size
 126 $2h \times 4h$, positioned so that its upstream edge was a distance of about h ahead of the
 127 cube’s front face, had no roughness elements and so was smooth. The remaining re-
 128 gion of the bottom surface of the domain was treated as rough. Except for the heated
 129 regions on the bottom wall, an adiabatic boundary condition was specified on the
 130 remaining surface. Possible implications of these various assumptions are discussed
 131 in due course. In all computations, the reference temperature θ_{ref} was 293 K. The
 132 Reynolds number based on the cube height and the streamwise velocity at that height
 133 was approximately 6000.

Surface	θ_{wall} (K)
Leeward	445
Roof	319
Side wall	307
Floor 1	321
Floor 2	307
Floor 3	300

Table 1 Specified temperature on different surfaces.

Ri	g
0.00	9.81
-0.02	0.38
-0.24	3.50
-0.66	9.81
-2.00	29.02

Table 2 Variation of g with Ri .

134 The domain size for these computations was $10h \times 6.2h \times 6h$ because this proved
135 sufficient in previous related studies (e.g. Lim et al., 2009). Except for the uniform
136 resolution of $h/19$ in the x and y directions on the cube surface, the rest of the do-
137 main had non-uniform spacing that followed a geometric progression. In the x and
138 y directions, the resolution was of size $h/19$ near the cube and expanded to a reso-
139 lution of $h/7$ at the boundaries, such that the mesh expansion ratio did not exceed
140 1.04. In the vertical direction, the resolution decreased from $h/35$ at the cube height
141 to $h/7$ at $z/h \approx 0$, such that the mesh expansion ratio was 1.13; the resolution again
142 decreased from the cube height to the domain top ($h/7$) with a mesh expansion ra-
143 tio of 1.02. The resolution has to be relatively coarse at the bottom wall because the
144 rough-wall model requires the first wall grid to lie within the (notional) logarithmic
145 layer i.e. $30 < z_1^+ < 200$ (where $z_1^+ = u_\tau z_1 / \nu$, u_τ is the wall friction velocity and z_1
146 is the distance from the wall to the centre of the first grid).

147 In order to understand the local thermal effects on the flow, experiments were
148 conducted for various Ri , defined as

$$149 \quad Ri = \frac{\beta g h (\theta_{\text{ref}} - \theta_{\text{wall}})}{u_{\text{ref}}^2}. \quad (3)$$

150 Here β is the coefficient of thermal expansion, g is the acceleration due to gravity
151 and θ_{wall} is the mean wall temperature on the leeward face.¹ In order to maintain
152 consistency in comparisons for different cases of Ri , θ_{wall} and θ_{ref} were fixed and g
was changed accordingly; the resulting values are shown in Table 2.

153 2.3 More details on wall boundary conditions

154 2.3.1 Rough-wall momentum model

155 In the experiments, sharp edged roughness elements (almost similar to vertical flat
156 plates) comprising two different heights ($h/2.375$ and $h/3.8$) were arranged in the
157 form of an aligned array on the bottom floor of the wind tunnel. Such an arrangement
158 crudely represents the urban roughness. In the current computations, the turbulence
159 created by these roughness elements was represented by a rough-wall model devel-
160 oped by Xie et al. (2004). This model is based on the principle of injecting energy

¹ Note that in the experiments, the reference velocity for Ri was taken as the mean velocity at $(x/h, y/h, z/h) = (-1.5, 0, 1.25)$, rather than our u_{ref} .

161 into the resolved velocity field. According to this model, the local wall shear stress is
 162 given by

$$\frac{\tau_{zx}}{u_*^2} = \frac{1}{U_a} \left[\langle u \rangle + (u - \langle u \rangle) \left(\beta_0 + \beta_1 \frac{|u - \langle u \rangle|}{u_*} + \beta_2 \frac{|u - \langle u \rangle|^2}{u_*^2} + \dots + \beta_l \frac{|u - \langle u \rangle|^l}{u_*^l} \right) \right], \quad (4)$$

163 where $\langle \cdot \rangle$ represents averaging in the horizontal plane, u is the streamwise velocity
 164 at the first grid point from the wall, U_a is the mean streamwise velocity at the same
 165 location, u_* is the friction velocity and β_k (where $k = 0, 1 \dots l$) is the damping factor
 166 that ranges between 0 and 1. The value of β_k can be obtained from the similarity laws
 167 or measurements. A similar relation can be written for instantaneous shear stress in
 168 the spanwise direction (τ_{zy}). Unlike Xie et al. (2004), who estimated the value of
 169 β_2 from wind-tunnel near-wall data, such data are not known from the experiments
 170 of Richards et al. (2006) and therefore the choice of β_k remains an issue. However,
 171 we tested various values of β_1 by assuming that the contribution from other β terms
 172 are small. $\beta_1 = 0.01$ seemed to be reasonable (with $\beta_0 = 0$), as values larger than
 173 this yielded steep gradients in the turbulent kinetic energy near the wall and smaller
 174 values did not yield sufficient turbulence to represent adequately the ‘very’ rough
 175 wall.

176 2.3.2 Smooth-wall momentum model

177 The logarithmic law is commonly employed to incorporate the near-wall shear stress
 178 if the near-wall grid lies in the logarithmic region. But such an approximation does
 179 not yield accurate skin-friction coefficients, especially in complex flow regions. In
 180 an attempt to address such issues, Cabot and Moin (1999) developed a wall model
 181 that includes solving boundary-layer equations on an embedded finer mesh between
 182 the wall and the near-wall grid, thereby improving the near-wall modelling. Such a
 183 method was implemented successfully on various complex problems such as boundary-
 184 layer flows past an aerofoil trailing edge (Wang and Moin, 2002) and backward fac-
 185 ing step flow (Rani et al., 2009). A brief description of this method is given here;
 186 for more details, refer to Wang and Moin (2002). The wall shear stress is obtained
 187 by solving the following turbulent boundary-layer equations for the two tangential
 188 velocity components on an embedded mesh between the wall and the first grid point.

$$\frac{\partial}{\partial x_n} (v + v_t) \frac{\partial u_i}{\partial x_n} = F_i, \quad (5)$$

$$189 \quad \text{where } F_i = \frac{1}{\rho} \frac{\partial p}{\partial x_i} - f \delta_{i3} + \frac{\partial u_i}{\partial t} + \frac{\partial}{\partial x_j} u_i u_j, \quad (6)$$

190 for given $n \in \mathbf{J}$, $\forall i \in \mathbf{J} \setminus \{n\}$, $\forall j \in \mathbf{J}$ where $\mathbf{J} = \{1, 2, 3\}$.

191 Here n denotes the wall-normal direction. Wang and Moin (2002) computed the eddy
 192 viscosity v_t using the mixing-length model with near-wall damping, so that

$$\frac{v_t}{\nu} = \kappa z_w^+ (1 - e^{-z_w^+/A})^2 \quad (7)$$

193 where z_w^+ is the distance to the wall in wall units, $A = 19$ and κ is the model coefficient.
 194 If the transient and convective terms are ignored in Eq. 6, Eq. 5 reduces to an
 195 ordinary differential equation, which upon integration from the wall to the first grid
 196 point yields the following.

$$\tau_{wi} = \mu \left. \frac{\partial u_i}{\partial x_n} \right|_{x_n=0} = \frac{\rho}{\eta \int_0^\eta \frac{dx_n}{\nu + \nu_t}} \left\{ u_{\eta_i} - F_i \int_0^\eta \frac{x_n}{\nu + \nu_t} dx_n \right\}, \quad (8)$$

197 where η is the first wall-normal grid point.

198 In the current computations, the wall shear-stress components were calculated
 199 using Eq. 8. ν_t was obtained from the mixing-length model given by Eq. 7 in which
 200 κ was set to a constant value of 0.4. Similar to Wang and Moin (2002), the local
 201 friction velocity u_τ at each timestep was obtained from the previous timestep using
 202 the term $[(\tau_{w1}/\rho)^2 + (\tau_{w2}/\rho)^2]^{1/4}$.

203 2.3.3 Smooth-wall temperature model

204 Similar to the momentum wall model above, a wall model for the temperature can be
 205 derived from the temperature transport equation given by Eq. 2. Ignoring the transient
 206 and convection terms and integrating the diffusion term twice gives the wall heat flux
 207 q_w as

$$q_w = \frac{\mu}{Pr_m} \left. \frac{\partial \theta}{\partial x_n} \right|_{x_n=0} = \frac{\rho c_p}{\eta \int_0^\eta \frac{dx_n}{k_t + k_m}} (\theta_\eta - \theta_{\text{wall}}), \quad (9)$$

208 where c_p is the specific heat capacity, θ_η and θ_{wall} are the temperatures at the near-
 209 wall grid point and the wall, respectively. Such a wall model was also derived and
 210 implemented by Rani et al. (2009). In the current computations, $Pr_t (= \mu_t/k_t)$ was set
 211 to a constant value of 0.9 and the heat transfer coefficient specified at the wall was
 212 given by Eq. 9.

213 In order to assess the performance of the above mentioned temperature and mo-
 214 mentum (Sect. 2.3.2) wall models for the smooth wall, they were initially imple-
 215 mented on flow past four staggered cubes with a passive scalar on the bottom wall
 216 surface. The details on geometry and boundary conditions are given in Boppana et al.
 217 (2010). The resulting time and spatial average scalar and streamwise velocity profiles
 218 were then compared with fine resolution LES (this is close to direct numerical simu-
 219 lations at the wall) and coarse resolution ($h/16$) with the standard logarithmic law at
 220 the wall. With the above smooth wall models, although 6% improvement is observed
 221 at the bottom wall streamwise velocity, approximately 34% improvement is observed
 222 in the near-wall scalar. Therefore, in the current set of large-eddy simulations, these
 223 smooth wall models are used on the cube and heated floor surfaces.

224 3 Results

225 As mentioned in Sect. 2.2, for the flow past a heated cube on a very rough wall, the
 226 thermal effects were investigated for $Ri = 0, -0.02, -0.24, -0.66$ and -2.0 . This

range of Ri includes forced and mixed convection in the flow around the cube. The approach flow is maintained similar to experiments and its modelling details are given in the Appendix. The flow and thermal fields behind the cube are compared with the experiments in Sect. 3.1 and further analysis on these fields is presented in Sect. 3.2.

3.1 Comparisons with experiments

Results are shown with the experimental data mostly for $Ri = -0.66$; where necessary, the results for other Ri cases will be explained. The normalized time-averaged streamwise velocity, kinetic energy and temperature profiles behind the cube and at two different spanwise locations are shown in Figs. 2, 3 and 5 respectively.

The streamwise velocities obtained from LES are found to be in fair agreement with experiments for both $Ri = 0$ and -0.66 . However, a notable observation is that the computed velocities above the cube height are lower than the experimental data at all locations. The measured velocity profile at $x/h = -3.5$ follows approximately a power-law behaviour and the experimental data slightly exceeds the power-law values in the region $0.6 < z/h < 1.6$. This could partly explain the differences seen in Fig. 2. It is observed that below the cube height, heating enhanced the magnitude of the streamwise velocity, especially beyond the recirculation region ($x/h = 1.5$).

Figure 3 shows that the turbulent kinetic energy from simulations is also in fair agreement with the experiments. Heating causes a notable increase in the kinetic energy, especially for $z/h < 1$. Above the cube height, the LES shows higher kinetic energy than experiments at all downstream locations. This could be due to slightly larger TKE than the experiments at the inlet for $z/h < 2$ (not shown here). Contours of the normalized TKE and mean velocity vector field behind the cube and at the symmetry plane (i.e. $y/h = 0$) are shown in the Fig. 4 for four different cases of heating. The figure clearly shows the increase in TKE with the decrease in Ri , and this behaviour is not limited to the wake of the cube but extends towards the shear layer and above, especially for $Ri = -2$. In the cube wake, increasing buoyancy clearly leads to increase in velocity vector magnitude.

The simulations for $Ri = -0.66$ in Fig. 5 show lower values of normalized temperatures than the experiments at all downstream locations except at $x/h = 0.55$. The difference between simulation and experiment is large only below the cube height. It cannot be entirely attributed to the small differences in the flow field between simulations and experiments, for reasons explained below. The figure also shows the temperatures that were obtained by not using the temperature and momentum wall models described in Sect. 2.3. Clearly, the temperature estimation is improved with these wall models and so they were used in all the subsequent computations.

It was mentioned in Sect. 2.2 that the heating in the experiments had neither constant heat flux nor constant temperature on the leeward face of the cube; the total input heat flux was also not measured. This imposes a challenge in making appropriate comparisons of simulated temperature field with the experiments. However, with only marginal differences seen in the velocity field, we can assume that the total heat flux must be the same far downstream of the cube in both LES and wind-tunnel experiments (and of course equal to the total input heat flux at the various heated sur-

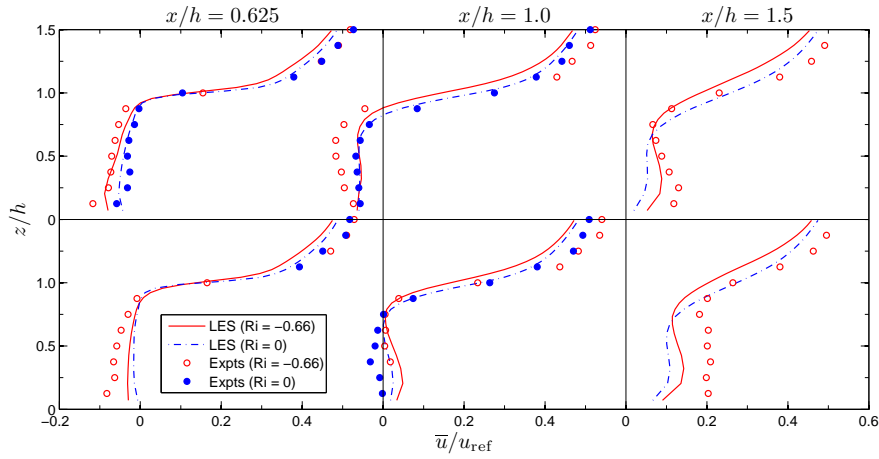


Fig. 2 Normalized mean streamwise velocity profiles at different downstream locations behind the cube for $Ri = 0$ and -0.66 : Top row at $y/h = 0$, bottom row - average of data at $y/h = \pm 0.25$.

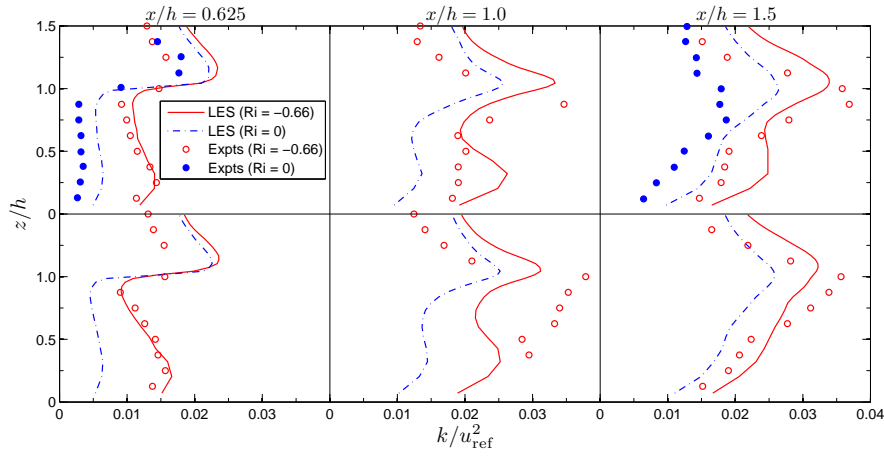


Fig. 3 Normalized mean turbulent kinetic energy profiles at different downstream locations behind the cube for $Ri = 0$ and -0.66 : Top row at $y/h = 0$, bottom row - average of data at $y/h = \pm 0.25$.

270 faces). Since the data available from the experiments were insufficient to allow direct
 271 estimation of this total heat flux, we attempted to match the temperature profiles in
 272 the wake of the cube in order to estimate the total heat flux in the experiments.

273 Let q be the total (input) heat flux obtained from LES with the constant tempera-
 274 ture boundary conditions (detailed earlier). Normalizing the mean temperature using
 275 this heat flux yields profiles shown in Fig. 6. Since the heat flux in the experiments is
 276 unknown, several trials have shown that the total heat flux in the experiments could
 277 be $q_{\text{est}} = 1.8q$. This is because, reasonable agreement between experiments and computa-
 278 tions can be seen in Fig. 6 when the former is normalized with q_{est} . Therefore, an

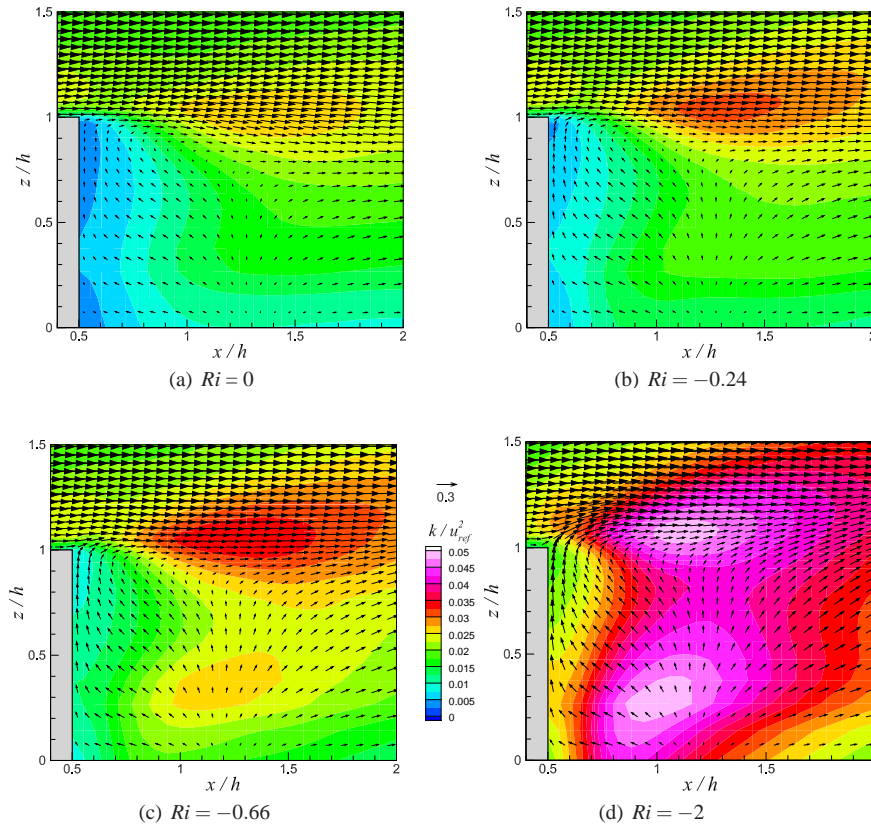


Fig. 4 Contours of the normalized TKE and mean velocity vectors in the wake of the cube.

279 LES was performed in order to check the sensitivity of the type of heat boundary con-
 280 dition and q_{est} on the flux normalized temperature profiles. The resulting normalized
 281 temperature profiles shown in Fig. 6 confirms the reasonableness of the estimate of
 282 q_{est} for the experimental heat flux and insensitivity to the type of heat boundary con-
 283 dition. In order to assess the importance of heating the floor surfaces shown in Fig. 1,
 284 additional computations were done by heating *only* the leeward face of the cube. In
 285 the resulting normalized temperature profiles (not shown here), the near-wall temper-
 286 atures were found to be severely under-predicted, thereby justifying the bottom floor
 287 heating in the current set of computations .

288 Figure 7 shows the contours of the flux-normalized mean temperature for differ-
 289 ent Ri at $z/h = 0.5$. There are two striking features in this figure. Firstly, with decrease
 290 in Ri the normalized temperatures in the vicinity of the leeward face decrease. This
 291 is because of the strong updrafts due to buoyancy (also seen in Fig. 4), especially
 292 close to the leeward face. Secondly, the strong updraft at lower Ri decreases the heat
 293 transport in the streamwise direction. It can be seen in the figure that the stream-

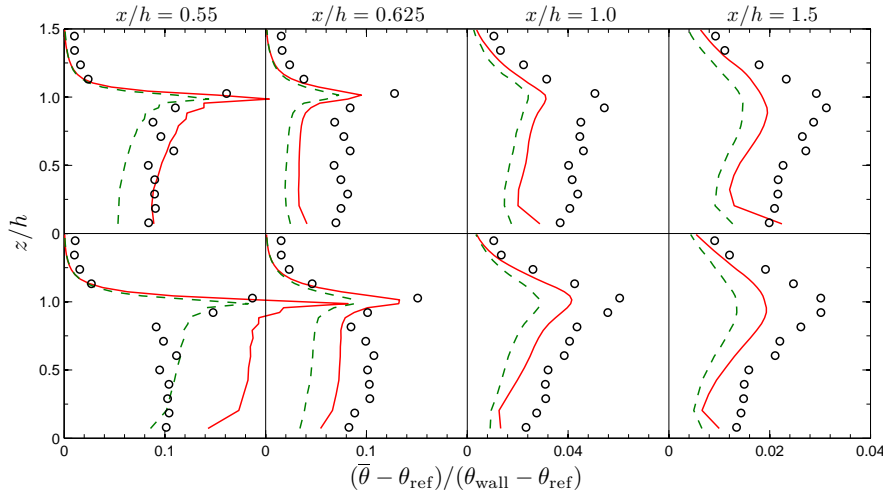


Fig. 5 Normalized mean temperature profiles for $Ri = -0.66$ at different downstream locations behind the cube; solid lines - LES (with wall models given in Sect. 2.3), dashed lines - LES (with standard wall models), symbols - experiments; top row at $y/h = 0$, bottom row - average of data at $y/h = \pm 0.4$.

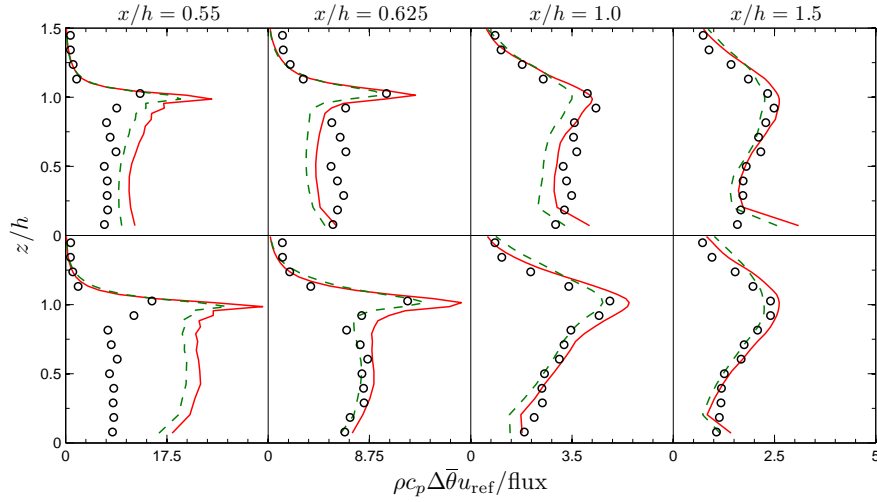


Fig. 6 Flux-normalized mean temperature profiles for $Ri = -0.66$ at different downstream locations behind the cube; $\Delta\theta = (\bar{\theta} - \theta_{\text{ref}})$; solid lines - LES (flux = q), dashed lines - LES (flux = q_{est}), symbols - experiments (flux = q_{est}); top row at $y/h = 0$, bottom row - average of data at $y/h = \pm 0.4$.

294 wise convection of heat is much stronger at $Ri = -0.02$, thereby suggesting that, for
 295 weakly unstable flows, heat is predominantly convected downstream.

296 The above comparisons with experiments suggest that our LES of the flow and
 297 thermal fields are reasonably good. Further analysis of the heat transport processes
 298 was performed to better understand the variations with different Ri . This was all based

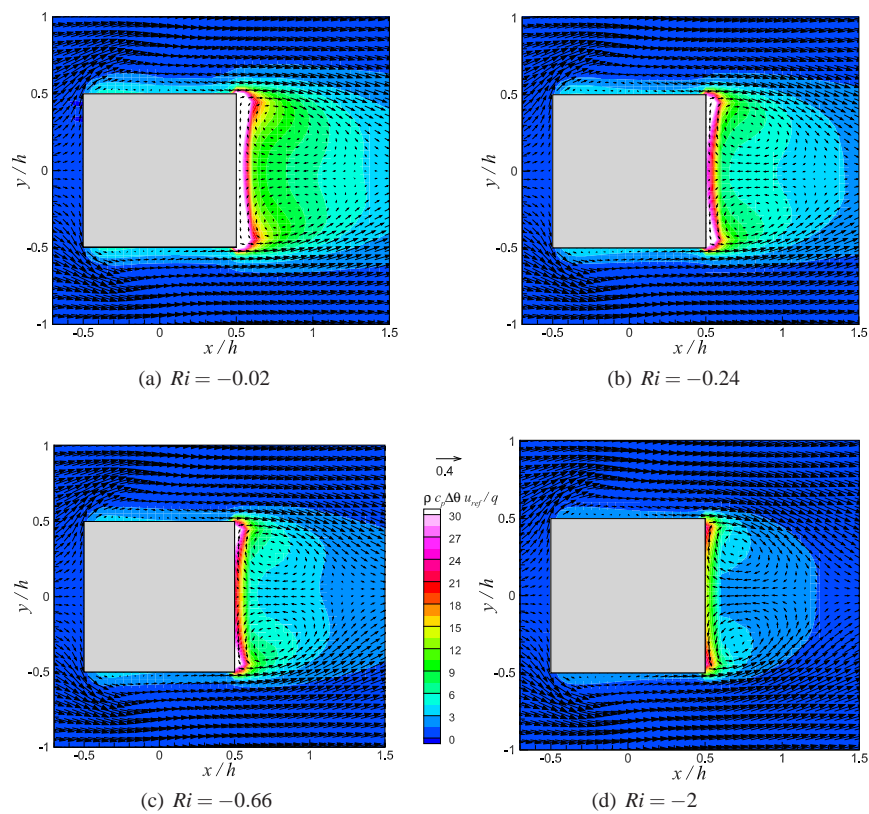


Fig. 7 Contours of the flux-normalized mean temperature and normalized mean velocity vectors at $z/h = 0.5$.

299 on data from the computations with fixed temperature boundary conditions and is
 300 presented and discussed below.

301 3.2 Further analysis

302 3.2.1 Fluxes

In order to understand how the vertical distribution of heat fluxes vary with Ri , each of its components i.e. advective, turbulent and diffusive fluxes are calculated. These

are defined as:

$$A_f \equiv \text{advective heat flux} = \rho c_p \left\{ \frac{1}{L_x L_y} \int_0^x \int_0^y \tilde{\theta} \tilde{w} dx dy + \left(\frac{1}{L_x L_y} \int_0^x \int_0^y \bar{\theta} dx dy \right) \left(\frac{1}{L_x L_y} \int_0^x \int_0^y \bar{w} dx dy \right) \right\}, \quad (10a)$$

$$T_f \equiv \text{turbulent heat flux} = \frac{\rho c_p}{L_x L_y} \int_0^x \int_0^y \overline{\theta' w'} dx dy, \quad (10b)$$

$$D_f \equiv \text{diffusive heat flux} = \frac{\rho c_p}{L_x L_y} \int_0^x \int_0^y (k_s + k_m) \frac{\partial \bar{\theta}}{\partial z} dx dy. \quad (10c)$$

303 Note that A_f and T_f are resolved quantities, and the k_s term in D_f is the subgrid-scale
 304 modelled contribution of the total turbulent heat flux. The tilde variables are the de-
 305 viations from the spatial mean of the time-average values, primed variables are the
 306 fluctuations from the respective time-averaged values and overbar denotes the time
 307 average. L_x and L_y are the respective domain lengths in the streamwise and span-
 308 wise directions. (Note, however, that to avoid the influence of the zero-gradient outlet
 309 boundary condition, we used an integration domain a little shorter than L_x .) The first
 310 term in the advective flux is called the dispersive flux and the contribution from the
 311 second term is found to be very small and hence is not shown in Fig. 8. The disper-
 312 sive, turbulent and diffusive heat flux components shown in Fig. 8 are normalized
 313 by the total downwind convective heat flux obtained far downstream of the cube. It
 314 is observed that decreasing Ri leads to an increase in vertical dispersive flux and its
 315 maximum value gradually shifts towards the cube height. Due to the strong buoyancy
 316 effects at $Ri = -0.66$ and -2.0 , the dispersive flux at the cube height is positive,
 317 in contrast to the negative values at $Ri = -0.02$ and -0.24 . Below the cube height,
 318 the vertical turbulent flux values are very small and differ only marginally for all Ri ,
 319 suggesting that the fluctuations of the vertical velocity and temperature difference are
 320 poorly correlated. It can be observed that the maximum value of the turbulent heat
 321 flux decreases gradually and slightly shifts above the cube height with decrease in
 322 Ri , again due to the stronger buoyancy effects at lower Ri . Due to a reasonably good
 323 mesh resolution, the diffusive heat flux contribution for all Ri is found to be small
 324 compared to the other fluxes.

325 3.2.2 Thermal boundary-layer thickness

326 In the field study of Louka et al. (2002), it was observed that a large horizontal ther-
 327 mal gradient (at the vertical wall of the building) extends up to approximately 0.2 m
 328 from the wall and has a greater intensity at 0.02 m from the wall; the mean building
 329 height was 21 m. Their measurements thus suggest that the thermal boundary layer
 330 is relatively very thin. However, it would be quite challenging to determine its pre-
 331 cise thickness both in the field and in wind-tunnel models. We therefore estimate the

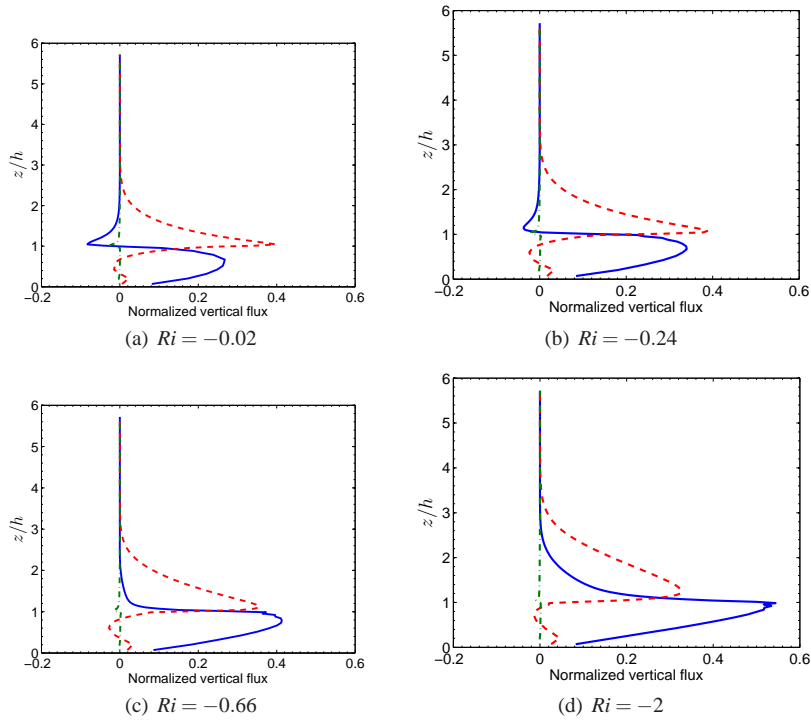


Fig. 8 Normalized vertical heat flux profiles for different Ri . Solid line: dispersive flux component of A_f , Dashed line: T_f , Dash-dot line: D_f .

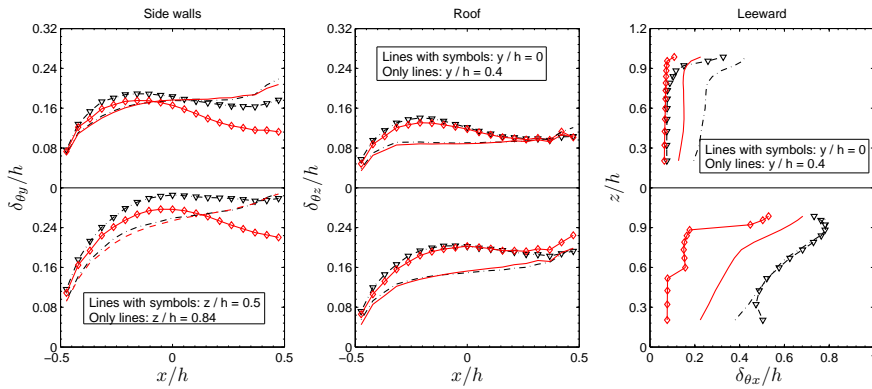


Fig. 9 Variation of thermal boundary-layer thickness at different locations. $Ri = -0.24$: dash-dot lines with and without triangles, $Ri = -2$: solid lines with and without diamonds. $\vartheta = 0.05$ and 0.025 for top and bottom rows respectively.

332 thermal boundary-layer thickness ($\delta_{\theta_{x_i}}$) in this section for various Ri and on differ-
 333 ent surfaces of the cube, where $\delta_{\theta_{x_i}}$ is defined as the distance from the wall where
 334 $(\bar{\theta} - \theta_{\text{ref}})/(\theta_{\text{wall}} - \theta_{\text{ref}}) = \vartheta$. The thickness therefore depends on the threshold value,
 335 ϑ , and for comparison purposes, the threshold values chosen are 0.05 and 0.025.
 336 With this definition, $\delta_{\theta_{x_i}}$ was estimated at different locations and for different Ri . For
 337 brevity purpose, only the data that corresponds to $Ri = -0.24$ and -2.0 are shown
 338 in Fig. 9. At $z/h = 0.5$ and 0.84 the ‘side’ wall data correspond to the average values
 339 from two sides of the cube. Similarly the data at $y/h = 0.4$ correspond to the average
 340 of values at $y/h = 0.4$ and -0.4 . Details of the thermal thickness variations on each
 341 surface are explained below.

- 342 1. Side walls: The δ_{θ_y} variation along the side wall is shown at two different heights.
 343 At the cube’s mid-height, it can be observed that δ_{θ_y}/h decreases with decrease
 344 in Ri . This is due to the increase in buoyancy at lower Ri . The larger thermal
 345 boundary-layer thickness at $Ri = -0.24$ also indicates that the lateral dispersion
 346 of temperature is larger. This is also seen in Fig. 7. Towards the top of the cube i.e
 347 at $z/h = 0.84$, δ_{θ_y} is almost the same for all Ri due to stronger streamwise velocity
 348 at that height. The presence of the recirculation region on the side walls, whose
 349 size decreases with decreasing Ri , might be responsible for the slight bulging
 350 behaviour of δ_{θ_y} in the range $-0.5 \leq x/h \leq 0$ at $z/h = 0.5$. Such bulging behaviour
 351 is very clear with $\vartheta = 0.025$. It is to be noted that by decreasing ϑ from 0.05 to
 352 0.025, the thermal boundary-layer thickness increased approximately by $0.1h$.
 353 This indicates the sensitivity of the thermal thickness to the threshold value.
- 354 2. Roof: The thermal thickness on the roof is smaller than on the sidewalls due to
 355 a larger streamwise velocity above the boundary layer on the roof. Because of
 356 the presence of a thin recirculation region which extends up to $x/h = 0$ from the
 357 leading edge and whose length is almost same for all Ri , the thermal thickness is
 358 larger at $y/h = 0$ than it is at $y/h = 0.4$. The sensitivity of the thermal thickness to
 359 ϑ is found to be similar to that of side walls.
- 360 3. Leeward: The thermal thickness for $z/h < 0.2$ is not shown here as it is influ-
 361 enced by the floor heating. Due to stronger vertical convection at lower Ri , a clear
 362 trend of decreasing thermal boundary-layer thickness with decreasing Ri can be
 363 observed. For $\vartheta = 0.05$ and 0.025 , δ_{θ_x}/h is larger at $y/h = 0.4$ than it is at the
 364 symmetry plane. The downstream convection of heat at $y/h = 0$ is affected by
 365 the two counter rotating vortices on either side of the symmetry plane. There-
 366 fore δ_{θ_x}/h is smaller at $y/h = 0$ than at $y/h = 0.4$ and this is also very evident in
 367 Fig. 7. With decrease in ϑ to 0.025 , δ_{θ_x}/h increased by almost a factor of two,
 368 indicating the sensitivity of the thickness to the threshold value. It also suggests
 369 the presence of steeper horizontal thermal gradients, as observed in the field stud-
 370 ies of Louka et al. (2002). Because of the wake flow behind the cube, the thermal
 371 boundary-layer thickness is greater on the rear wall than on the sidewalls and roof
 372 surfaces.
- 373 4. Windward: In order to estimate the thermal boundary-layer thickness on the wind-
 374 ward face, an additional computation that includes some heating on the windward
 375 face was done for $Ri = -0.66$. This implies that the whole cube is heated, but
 376 with different temperatures on each face (the sidewalls and windward face had

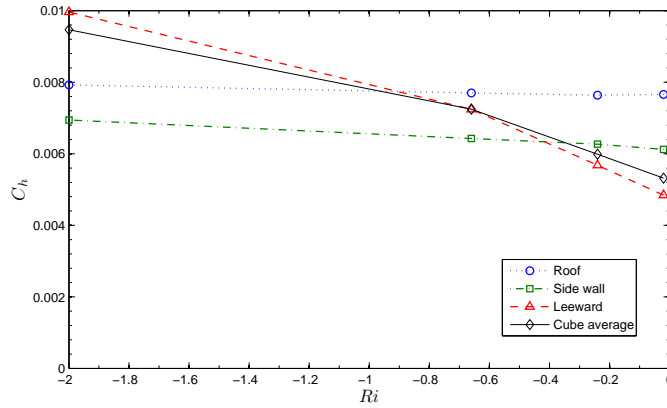


Fig. 10 Heat transfer coefficient at cube surfaces.

377 the same temperature in this case). The thermal boundary layer is found to be
 378 thinner than $0.1h$ for $\vartheta = 0.025$ and not measurable (i.e. thinner than the distance
 379 to the first grid point away from the wall) for $\vartheta = 0.05$. These relatively very thin
 380 boundary layers (compared to those on the other surfaces) are almost certainly
 381 caused by flow impingement on the windward surface.

3.2.3 Heat transfer coefficient

383 The convective heat transfer coefficient (C_h) is an important parameter in urban mi-
 384 croscale modelling. It's applications include assessment of energy performance of
 385 buildings, estimation of convective moisture transfer from building surfaces etc. There-
 386 fore, it would be useful to know the variation of C_h for different heated surfaces of
 387 the cube and also for different Ri . Here, it is defined as

$$C_h = \frac{q_{\text{wall}}}{\rho c_p u_b (\theta_{\text{wall}} - \theta_{\text{ref}})}. \quad (11)$$

388 where q_{wall} is the heat flux from each heated surface and u_b is the bulk velocity of
 389 the mean flow. Recall that θ_{wall} varied on each heated surface (Table 1). We observe
 390 in Fig. 10 that, except for the leeward wall at $Ri = -2$, the heat transfer coefficient
 391 at the roof surface is larger than sidewalls and leeward wall; this must be a result
 392 of strong streamwise convection. For the same reason, the values of C_h are almost
 393 constant for all Ri on the roof surface. A marginal increase in C_h can be seen at
 394 $Ri = -2$ on side walls. On the leeward wall, C_h is smaller than the roof and sidewalls
 395 for $Ri = -0.02$ and -0.24 . But for $Ri = -0.66$, C_h for leeward wall is larger than
 396 on the sidewalls but smaller than on the roof. This suggests that the buoyancy effects
 397 are smaller than the streamwise convection on the roof surface, but larger than the
 398 sidewalls. For $Ri = -2$, in contrast, C_h on the leeward wall is larger than on the roof,
 399 indicating that the buoyancy effects are now dominant than the streamwise convection
 400 on the roof.

401 The weighted average of the heat transfer coefficient at the heated surfaces of the
 402 cube is also shown in the same figure for each Ri . The average heat transfer coefficient
 403 for $Ri = -0.02$ is found to be approximately half of that observed in the wind-tunnel
 404 experiments by Meinders and Hanjalić (1999). In the COSMO (Comprehensive Out-
 405 door Scale MOdel) field experiments by Kanda and Moriizumi (2009), the value of
 406 C_h is estimated to be between 0.01 and 0.02 which is approximately 2 to 4 times
 407 larger than the current computations. These differences could be a result of all or
 408 some of the following: (i) both these experimental studies consisted of flow past an
 409 array of aligned cubes whereas the current LES computes flow past a single cube; (ii)
 410 the domain height in our LES is nearly three times larger than in the Meinders and
 411 Hanjalić (1999) (channel) experiments, which implies a higher bulk velocity; (iii) to
 412 obtain the values of C_h in the COSMO field experiments, surface radiative tempera-
 413 ture was used (at $z/h = 3$), which is different from the local surface temperature. It
 414 could also be possible that Ri was very large in the COSMO experiments.

415 3.2.4 Quadrant analysis

416 A simple statistical tool that measures the contribution of different kinds of events
 417 arising from the large-scale coherent structures is ‘quadrant analysis’. This technique
 418 has been used extensively in vegetation canopies and a detailed review by Finnigan
 419 (2000) shows that sweeps contribute more to the momentum flux as well as the heat
 420 flux within and just above the canopy. In the case of urban roughness, studies (e.g
 421 Rotach, 1993; Castro et al., 2006) also showed that momentum transfer close to and
 422 within the canopy is dominated by sweep events. Quadrant analysis by Christen et al.
 423 (2007) showed that the turbulent momentum and heat fluxes are predominantly by
 424 sweeps in most regions of the urban street canyon and closer to roofs whereas ejec-
 425 tions were found to be slightly dominating at higher measurement locations. In con-
 426 trast, Shiau and Hsieh (2002) found that for a shallow (low-slope) trapezium-shaped
 427 body in a wind tunnel, ejections were stronger than sweeps at $z/h = 1.2$.

To find which kind of events dominate in the current simulations where the lee-
 ward wall of the cube was strongly heated, quadrant analysis was carried out on both
 momentum and heat transport. The natural classification of quadrant events is used
 and is given below.

$$\begin{aligned}
 \text{Ejection(E)} : & \quad u' < 0, w' > 0; \quad \theta' > 0, w' > 0 \\
 \text{Sweep(S)} : & \quad u' > 0, w' < 0; \quad \theta' < 0, w' < 0 \\
 \text{Outward interaction(O)} : & \quad u' > 0, w' > 0; \quad \theta' < 0, w' > 0 \\
 \text{Inward interaction(I)} : & \quad u' < 0, w' < 0; \quad \theta' > 0, w' < 0
 \end{aligned}$$

The primed quantities (i.e. u', w', θ') denote fluctuations from the respective time-
 mean values. Analogous to the momentum flux, the removal of hot air from the cube
 wake to the flow above is called an ‘ejection (E)’ and the in-rush of cold air upstream
 of the cube to its wake is called a ‘sweep (S)’. The momentum and heat fluxes corre-

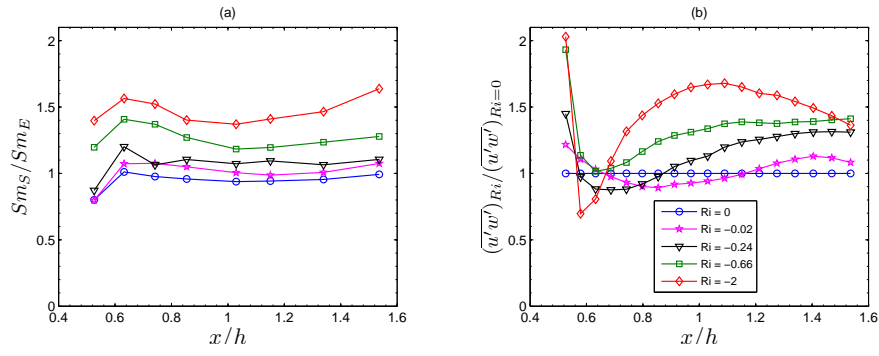


Fig. 11 Momentum flux along the shear layer behind the cube. (a) Ratio of strength of sweeps to ejections; (b) Variation of momentum flux with respect to neutral case. Legend in (b) refers to (a) also.

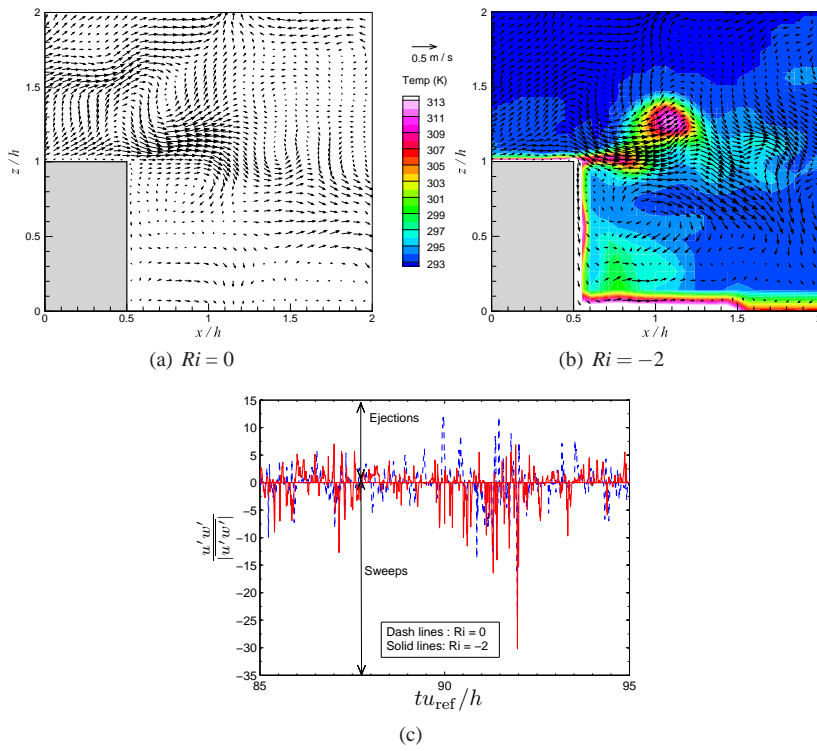


Fig. 12 The vector field of instantaneous velocity fluctuations (a & b) and contour of the instantaneous temperature (b) and in the wake of the cube at $y/h = 0$. (c) Time series of normalized shear-stress corresponding to the ejection and sweep events at $(x/h, z/h) = (1.54, 1.01)$. For clarity the sign of shear stress for ejections is reversed.

sponding to different quadrant events are given by

$$(\overline{u'w'})_Q = \frac{1}{T} \int_T u'(t)w'(t)I_Q(t) dt \quad (12a)$$

$$(\overline{\theta'w'})_Q = \frac{1}{T} \int_T \theta'(t)w'(t)I_Q(t) dt \quad (12b)$$

where Q denotes the quadrant event i.e. ‘S’, ‘W’, ‘O’ and ‘I’. $I_Q(t)$ is an indicator function and is given by

$$I_Q(t) = \begin{cases} 1 & \text{if } (u', w') \text{ is in quadrant } Q \\ & \text{if } (\theta', w') \text{ is in quadrant } Q \\ 0 & \text{otherwise} \end{cases}$$

The event frequency and the stress and heat flux fractions contributed by the individual events are then given by

$$F_Q = \frac{1}{T} \int_T I_Q(t) dt, \quad (13a)$$

$$Sm_Q = \frac{(\overline{u'w'})_Q}{\overline{u'w'}}, \quad (13b)$$

$$Sh_Q = \frac{(\overline{\theta'w'})_Q}{\overline{\theta'w'}} \quad (13c)$$

428 Momentum flux contributions from the four quadrant events are shown along the
 429 shear layer and at the symmetry plane i.e. $(y/h, z/h) = (0, 1)$ in Fig. 11a. It is ob-
 430 served that sweep (‘S’) and ejection (‘E’) events occur more frequently than outward
 431 (‘O’) or inward (‘I’) interaction events in the case of momentum transport. With de-
 432 crease in Ri , a gradual increase in the frequency of ‘O’ and ‘I’ events is observed,
 433 but these are still dominated by the frequency of ‘S’ and ‘E’ events. Although ‘E’
 434 events occur more frequently than ‘S’ events, the latter contributes more to the mo-
 435 mentum flux. Also, this contribution increases with decrease in Ri and this can be
 436 seen in Fig. 11a. This could be due to the displacement of cold, denser air flowing
 437 from upstream by the thermal plume emanating from the leeward face. The former
 438 is then subjected to stronger fluctuations in the downward direction thereby yielding
 439 stronger sweeps. This can be seen in Fig. 12b and for comparison purposes the neutral
 440 case is shown in Fig. 12a. Although, this figure pertains to one specific time instant, a
 441 snapshot of the time series for $Ri = 0$ and -2 , shown in Fig. 12c, confirms that heating
 442 enhances the sweep strength considerably in the shear layer. To clarify the behaviour
 443 of the momentum flux along the shear layer with decrease in Ri , it is normalized with
 444 respect to the neutral case data and this is shown in Fig. 11b. It is evident that heating
 445 increases the normalized momentum flux, but in a non-monotonic way.

446 Unlike momentum, the frequency of the events that correspond to ‘S’ and ‘E’ in
 447 the heat flux transport dominate ‘O’ and ‘I’ events only for $Ri = -0.02$ and -0.24 . For
 448 lower Ri this behaviour changes and, as an example, the frequency distribution of the
 449 events, F_Q , is shown for $Ri = -2$ in Fig. 13c. In comparison with F_Q for momentum in

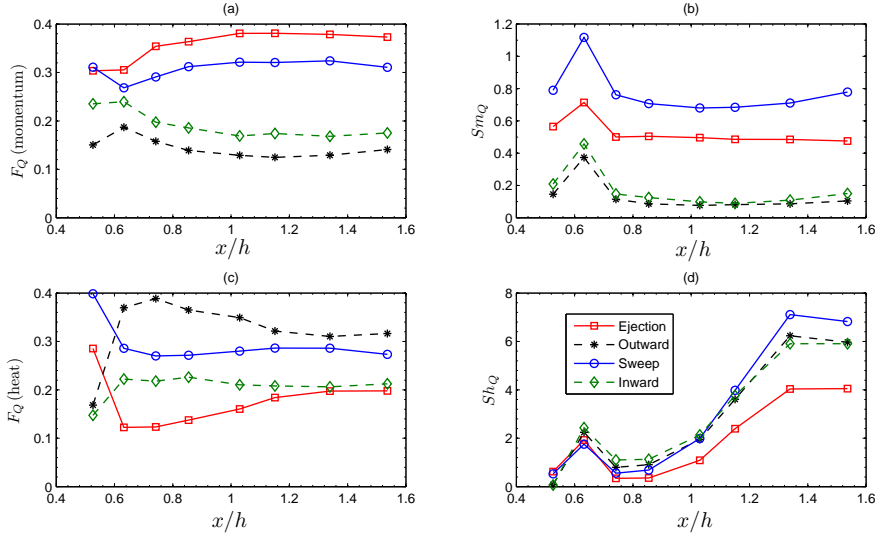


Fig. 13 The frequency (a, c) and flux fractions (b, d) of momentum and heat along the shear layer for $Ri = -2$. Note that the signs of stress fractions of outward and inward interactions for momentum and heat in (b) and (d) are reversed for better comparison with the ejection and sweep events.

450 Fig. 13a where the frequencies of ‘E’ and ‘O’ are the highest and lowest respectively,
 451 the F_Q of heat in Fig. 13c shows the opposite behaviour. As expected, the heat flux
 452 fraction of the ‘E’ events (Sh_E) is higher in the vicinity of the leeward wall. The larger
 453 values of Sh_S for $x/h > 1$ in Fig. 13d could indicate a strong in-rush of cold air into
 454 the shear layer. Unlike the momentum flux distribution in Fig. 13b, where the ‘O’ and
 455 ‘I’ events are weaker than the ‘E’ and ‘S’ events all along the shear layer, Fig. 13d
 456 shows that the strengths of ‘O’ and ‘I’ lie between those of ‘E’ and ‘S’ events for
 457 $x/h > 1$; for $x/h < 1$ the strengths of ‘O’ and ‘I’ events are found to be larger. All this
 458 suggests that the contributions to net heat flux from the different quadrants are very
 459 different to those of shear stress.

460 The normalized vertical turbulent heat flux variations along the shear layer for
 461 various Ri are shown in Fig. 14. We observe that with increase in heating, the normal-
 462 ized turbulent heat flux decreases and reaches a constant value as the distance
 463 from the leeward face increases. This decrease is caused by an increase in the heat
 464 flux contribution from the ‘O’ and ‘I’ quadrant events with decrease in Ri .

465 The above observations are valid within the *very* thin shear layer at the cube
 466 height. Corresponding quadrant analysis was also done at $(x, y, z) \approx (0.75x_R, 0, z_{TKE_m})$,
 467 where x_R is the recirculation length and z_{TKE_m} is the height at which turbulent kinetic
 468 energy is maximum; both these values vary with Ri . This analysis showed that the
 469 strength of ejections dominates that of sweeps, but only marginally for momentum
 470 transport. This is in contrast to the above observation made for the shear layer re-
 471 gion. However, in the case of heat flux, sweeps continued to dominate ejections, with
 472 increasing strength for decreasing Ri . The above quadrant analysis gives a general
 473 overview of the kind of events that arise in thin shear layer region behind the cube,

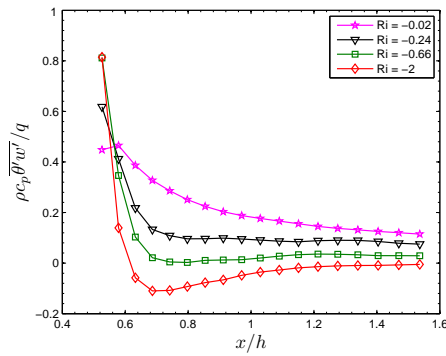


Fig. 14 Variation of normalized turbulent heat flux along the shear layer.

474 with strong leeward wall heating. The findings are found to be similar to those ob-
 475 served in field and wind-tunnel studies mentioned earlier, particularly for momentum.

476 4 Conclusions

477 The heat transfer from a single building with strong heating on its leeward surface
 478 and surrounded by an urban roughness array has been studied using LES for various
 479 degrees of thermal forcing ranging from neutral to weakly unstable to highly unsta-
 480 ble flows around the building. The (neutrally stable) turbulent atmospheric boundary
 481 layer consists of a constant shear-stress region up to half of the boundary-layer depth.
 482 It is quite challenging, both in the wind tunnel as well as in numerical simulations,
 483 to generate such a deep surface layer. But with the inflow boundary condition devel-
 484 oped by Xie and Castro (2008), it is possible to generate such an approach flow in
 485 the LES. Three sets of wall models are used: (i) a rough-wall model to represent an
 486 aligned array of roughness elements on the floor of the wind tunnel; (ii) a momentum
 487 wall model, and (iii) a temperature wall model to improve the flow and temperature
 488 estimation near the smooth wall surfaces on a relatively coarse mesh. The resulting
 489 flow and thermal fields showed fair agreement with the wind-tunnel experiments.
 490 The buoyancy effects are found to be significant in the wake of the cube, especially
 491 at lower Ri . At higher Ri , the heat emitted from the cube is found to be concentrated
 492 at the leeward wall and convected downwind.

493 The thermal boundary-layer thickness and heat transfer coefficient are estimated
 494 for each heated surface of the cube and for all Ri . It is observed that the thermal
 495 boundary layers on the side and leeward walls become thinner with a decrease in Ri .
 496 However, compared to the side walls and roof surface, the thermal boundary layer on
 497 the leeward wall is found to be larger because of the weak streamwise convection. Ir-
 498 respective of the variation in Ri , the stronger streamwise convection on the top of the
 499 cube yielded a thinner boundary layer compared to the other surfaces. For the same
 500 reason, the heat transfer coefficient is found to be largest on the roof surface, except
 501 for $Ri = -2$ where the buoyancy effects resulted in the largest heat transfer coefficient
 502 at the leeward wall. This suggests that, at such low Ri , buoyancy dominates the effects

503 of the strong shear layer normally present at roof level. These details should be use-
504 ful in the development or improvement of empirical models of heat transfer around
505 buildings in urban areas. The quadrant analysis performed along the shear layer be-
506 hind the cube showed that the momentum flux is mostly due to stronger sweeps and
507 that heating increases the sweep strength considerably (relative to ejections). In the
508 case of heat, the quadrant analysis showed a similar behaviour to momentum only for
509 relatively high $Ri = -0.02$ and -0.24 . Unlike the momentum flux, the frequency and
510 strength of the heat flux from the outward and inward interaction quadrants are not
511 small. This suggests that at lower Ri the contribution of these events to the heat flux
512 is very different to that for the momentum flux.

513 Whilst this investigation has focussed on the flow and thermal fields in the wake
514 of a single heated building, partly because of the availability of a corresponding ex-
515 perimental dataset, extension to arrays of urban-like roughness elements with heating
516 analogous to, for example, the incidence of solar radiation will clearly be important.
517 This will be the subject of future work, in which we hope to explore the integrated
518 effects of surface heating on momentum transfer and turbulence in urban-like areas.

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524 support and Stefano Duranti for helping us to implement the wall models in Star-CD.

525 **A Appendix: Modelling the approach flow in a channel**

526 In the experiments, the model scale of the cube was 1:100. A turbulent atmospheric boundary layer was
527 simulated such that the turbulent energy and shear stress were both essentially constant to a height equal to
528 one half of the boundary-layer height. In the computations, it is crucial to maintain the approach flow used
529 in the experiments but it is equally challenging to create and maintain a developed boundary-layer profile
530 with the necessary constant turbulent energy and shear stress in a deep surface layer over an axial fetch
531 significantly larger than the cube dimension. Initial computations were performed with a bottom rough
532 wall and without the cube, to check that the required flow did not change significantly with an upwind
533 fetch.

534 The computational domain size of the channel flow was $18h \times 9h \times 6h$. A height of $6h$ was deemed
535 sufficient, since that is similar to the boundary-layer thickness in the experiments. The inlet velocity profile
536 in the experiments followed a power-law and the same was specified in the computations. Reynolds normal
537 stress components were specified at the inlet such that the turbulent kinetic energy (TKE) agreed with that
538 of the experiments. The Reynolds shear stress specified at the inlet had a constant value in the surface
539 layer with a decreasing linear profile above. Cyclic boundary conditions were employed in the spanwise
540 direction. The bottom rough wall was represented by the rough-wall model described in Sect. 2.3.1. Stress
541 free conditions were specified on the top surface and, at the outlet, the axial gradient of the velocity field
542 was set to zero followed by a mass balance correction. The resulting profiles of time-averaged normalized
543 streamwise velocity and TKE are shown in Fig. 15. It can be seen that the streamwise velocity increases
544 only marginally with increasing downstream distance. However, the turbulent kinetic energy profiles at
545 various downstream locations indicate that the flow is developing, although very slowly (especially when
546 compared to RANS computations not shown here). The sharp peaks in the kinetic energy at the second
547 wall grid point in Fig. 15b could be due to the injection of energy into the resolved velocity field at the

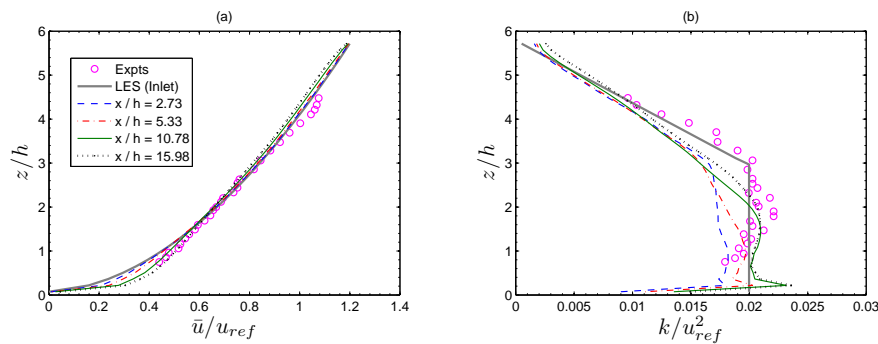


Fig. 15 (a) Normalized mean streamwise velocity and (b) turbulent kinetic energy profiles at various downstream locations.

548 wall surface by the rough-wall model. Despite these small imperfections, it is clear that an approach flow
 549 similar to the experiments can be adequately represented with the inflow and rough-wall models.

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