

University of Southampton Research Repository ePrints Soton

Copyright © and Moral Rights for this thesis are retained by the author and/or other copyright owners. A copy can be downloaded for personal non-commercial research or study, without prior permission or charge. This thesis cannot be reproduced or quoted extensively from without first obtaining permission in writing from the copyright holder/s. The content must not be changed in any way or sold commercially in any format or medium without the formal permission of the copyright holders.

When referring to this work, full bibliographic details including the author, title, awarding institution and date of the thesis must be given e.g.

AUTHOR (year of submission) "Full thesis title", University of Southampton, name of the University School or Department, PhD Thesis, pagination

Message Passing Case-study (Time Added Manually)

Table of Contents

Context c00	2
Context c01	2
Context c02	2
Context c03	3
Machine m00	4
Machine m01	6
Machine m02	9
Machine m03	11
Machine m04	14
Machine m05	17
Machine m06	20
Machine m07	25
Machine m08	30
Decomposed Machine Sender.....	35
Decomposed Machine Reciever	38
Decomposed Machine Channel	40

Message Passing Case-study (Time Added Manually)

Context c00

CONTEXT

c00

SETS

NET_MESSAGE

CONSTANTS

Data

ACK

FIN

Send_Message

last // Last sequence number of sendable message

DataTDL // Deadline duration to transfer Send_Message

AP_DATA // Application Data

AXIOMS

axm1 : partition(NET_MESSAGE, Data, {ACK}, {FIN})

axm2 : AP_DATA $\subseteq$ Data

axm3 : Send_Message $\in \mathbb{N} \rightarrow$ NET_MESSAGE

axm4 : ran(Send_Message) = Data $\cup$ {FIN}

axm5 : finite(Send_Message) $\wedge$ Send_Message $\neq \emptyset$

axm6 : last = card(Send_Message) - 1

axm7 : $\forall n. n \in \text{dom}(\text{Send_Message}) \Rightarrow 0 \cdot n \subseteq \text{dom}(\text{Send_Message})$

axm8 : $\text{dom}(\text{Send_Message}) = 0 \cdot \text{last}$

axm9 : $\forall m \cdot m \in \text{dom}(\text{Send_Message}) \wedge m \neq \text{last} \Rightarrow \text{Send_Message}(m) \neq \text{FIN}$

axm10 : Send_Message(last) = FIN

axm11 : $\forall n. n \in \mathbb{N} \wedge n < \text{last} \Rightarrow \text{Send_Message}(n) \in \text{Data}$

axm12 : DataTDL $\in \mathbb{N}$

axm13 : DataTDL > 0

axm14 : $\forall m, x, y. m \in \text{Send_Message} \wedge m = x \mapsto y \wedge y = \text{FIN} \Rightarrow x = \text{last}$

axm15 : $\forall x \cdot x \in \text{dom}(\text{Send_Message}) \Rightarrow x \in 0 \cdot \text{last}$

axm16 : $\forall x \cdot x \subseteq \mathbb{N} \wedge \text{finite}(x) \wedge x \neq \emptyset \Rightarrow \max(x) + 1 \notin x$

END

Context c01

CONTEXT

c01

EXTENDS

c00

CONSTANTS

PacketTDL

AXIOMS

axm1 : PacketTDL $\in \mathbb{N}$

axm2 : DataTDL $\geq (\text{last} + 1) * \text{PacketTDL}$

END

Context c02

CONTEXT

c02

EXTENDS

c01

CONSTANTS

MaxResend

ResendingDL

AXIOMS

axm1 : MaxResend > 1

axm5 : ResendingDL > 0

axm6 : PacketTDL $\geq (\text{MaxResend} + 1) * \text{ResendingDL}$

END

Context c03

CONTEXT

c03

EXTENDS

c02

CONSTANTS

ChannelDL

ReceiverDL

AXIOMS

axm1 : $\text{ChannelDL} \in \mathbb{N}$

axm2 : $\text{ResendingDL} > 2 * \text{ChannelDL}$

axm3 : $\text{ReceiverDL} \in \mathbb{N}$

axm4 : $\text{ReceiverDL} \geq \text{MaxResend} * \text{ResendingDL} + 2 * \text{ChannelDL}$

axm5 : $\text{ReceiverDL} \geq \text{PacketTDL}$

END

Machine m00

MACHINE

m00 // *Deadline(Start_Transferring, Transferring $\vee$ Error, DataTDL)*

SEES

c00

VARIABLES

transferred0 // *Whole transfered Message*

Transferred // *Flag*

Start_Transferring // *Flag*

Error // *Flag*

time

Start_TransferringT

INVARIANTS

inv1 : transferred0 $\subseteq$ Send_Message

inv2 : Start_Transferring $\in$ BOOL

inv3 : Transferred $\in$ BOOL

inv4 : Error $\in$ BOOL

inv5 : time $\in$ $\mathbb{N}$

inv6 : Start_TransferringT $\in$ $\mathbb{N}$

inv7 : dom(Send_Message) = 0 .. last

inv8 : last $\geq$ 0

EVENTS

INITIALISATION $\triangleq$

STATUS

ordinary

BEGIN

act1 : transferred0 := $\emptyset$

act2 : Transferred := FALSE

act3 : Start_Transferring := FALSE

act4 : Error := FALSE

act5 : time := 0

act6 : Start_TransferringT := 0

END

Start_Transferring $\triangleq$

STATUS

ordinary

WHEN

grd1 : Start_Transferring = FALSE

THEN

act1 : Start_Transferring := TRUE

act2 : Start_TransferringT := time

END

Transferred $\triangleq$

STATUS

ordinary

WHEN

grd1 : Transferred = FALSE

grd2 : Start_Transferring = TRUE

grd3 : Error = FALSE

THEN

act1 : Transferred := TRUE

act2 : transferred0 := Send_Message

END

Error $\triangleq$

STATUS

ordinary

WHEN

grd1 : Start_Transferring = TRUE

grd2 : Transferred = FALSE

grd3 : Error = FALSE

THEN

act1 : Error := TRUE

Message Passing Case-study (Time Added Manually)

END

Tick_Tock $\triangleq$
STATUS

ordinary

ANY

tick

WHERE

grd1 : tick $\in \mathbb{N}$

grd2 : tick > 0

grd3 : Start_Transferring = TRUE $\wedge$ Transferred = FALSE $\wedge$ Error = FALSE $\Rightarrow$ time + tick $\leq$ Start_TransferringT + DataTDL

THEN

act1 : time := time + tick

END

END

Machine m01

MACHINE

m01 // *Deadline(Start_Transferring, Transferring(last) ∨ Error, DataTDL)*

REFINES

m00

SEES

c00

VARIABLES

transferred // *Whole transfered Message*

Transferring // *Flag*

Error // *Flag*

time

TransferringT

Start_Transferring

Start_TransferringT

INVARIANTS

inv1 : transferred $\subseteq$ Send_Message

inv2 : Start_Transferring $\in$ BOOL

inv3 : Transferring $\subseteq$ dom(Send_Message)

inv4 : Error $\in$ BOOL

inv5 : time $\in \mathbb{N}$

inv6 : TransferringT $\in$ Transferring $\rightarrow \mathbb{N}$

inv7 : Start_TransferringT $\in \mathbb{N}$

inv8 : $\forall n \cdot n \in \text{Transferring} \wedge n > 0 \Rightarrow n-1 \in \text{Transferring}$

inv9 : $\forall n \cdot n \in \text{Transferring} \Rightarrow 0 \cdot n \subseteq \text{Transferring}$

inv10 : Transferring = dom(transferred)

inv11 : Transferring $\neq \emptyset \Rightarrow \text{Start_Transferring} = \text{TRUE}$

inv12 : last $\in$ Transferring $\Leftrightarrow$ Transferred = TRUE

inv13 : last $> 0 \wedge$ last $- 1 \in$ Transferring $\Rightarrow$ transferred $\cup \{\text{last} \mapsto \text{FIN}\} = \text{Send_Message}$

inv14 : last = 0 $\wedge$ last $\notin$ Transferring $\Rightarrow$ transferred $\cup \{\text{last} \mapsto \text{FIN}\} = \text{Send_Message}$

inv15 : last $\in$ Transferring $\Rightarrow$ transferred0 = transferred

inv16 : $0 \notin \text{Transferring} \Rightarrow \text{Transferring} = \emptyset$

inv17 : $\forall x, y \cdot x \in \mathbb{N} \rightarrow \text{NET_MESSAGE} \wedge y \subseteq x \wedge \text{dom}(x) = \text{dom}(y) \Rightarrow x = y$

inv18 : $\forall n \cdot n \in \text{Transferring} \wedge n+1 \notin \text{Transferring} \Rightarrow 0 \cdot n = \text{Transferring}$

EVENTS

INITIALISATION $\triangleq$

STATUS

ordinary

BEGIN

act1 : transferred $:= \emptyset$

act2 : Transferring $:= \emptyset$

act3 : Error $:= \text{FALSE}$

act4 : time $:= 0$

act5 : TransferringT $:= \emptyset$

act6 : Start_Transferring $:= \text{FALSE}$

act7 : Start_TransferringT $:= 0$

END

Start_Transferring $\triangleq$

extended

STATUS

ordinary

REFINES

Start_Transferring

WHEN

grd1 : Start_Transferring = FALSE

THEN

act1 : Start_Transferring $:= \text{TRUE}$

act2 : Start_TransferringT $:= \text{time}$

END

Transferring $\triangleq$

STATUS

ordinary

ANY

Message Passing Case-study (Time Added Manually)

```
m
x
y
WHERE
  grd1 : Start_Transferring = TRUE
  grd2 : m ∈ Send_Message
  grd3 : m = x ↦ y
  grd4 : x ∉ Transferring
  grd5 : x = 0 ⇒ Transferring = ∅
  grd6 : x > 0 ⇒ x-1 ∈ Transferring
  grd7 : Error = FALSE
  grd8 : x < last
THEN
  act1 : Transferring := Transferring ∪ {x}
  act2 : transferred := transferred ∪ {m}
  act3 : TransferringT(x) := time
END

TransferringLast ≜
  STATUS
  ordinary
REFINES
  Transferred
ANY
  m
  x
  y
WHERE
  grd1 : Start_Transferring = TRUE
  grd2 : m ∈ Send_Message
  grd3 : x = last
  grd4 : m = x ↦ y
  grd5 : x ∉ Transferring
  grd6 : x > 0 ⇒ x-1 ∈ Transferring
  grd7 : Error = FALSE
THEN
  act1 : Transferring := Transferring ∪ {x}
  act2 : transferred := transferred ∪ {m}
  act3 : TransferringT(x) := time
END

Error ≜
  STATUS
  ordinary
REFINES
  Error
WHEN
  grd1 : Start_Transferring = TRUE
  grd2 : last ∉ Transferring
  grd3 : Error = FALSE
THEN
  act1 : Error := TRUE
END

Tick_Tock ≜
  STATUS
  ordinary
REFINES
  Tick_Tock
ANY
  tick
WHERE
  grd1 : tick ∈ ℕ
  grd2 : tick > 0
  grd3 : Start_Transferring = TRUE ∧ last ∉ Transferring ∧ Error = FALSE ⇒ time + tick ≤ Start_TransferringT + DataTDL
THEN
  act1 : time := time + tick
END
```

END

Machine m02

MACHINE

m02 *// Deadline(Start_Transferring, Transferring(0)∨Error, PacketTDL)*
 // ∀ x · x < last / Deadline(Transferring(x), Transferring(x+1)∨Error, PacketTDL)

REFINES

m01

SEES

c01

VARIABLES

transferred *// Whole transfered Message*
Transferring *// Flag*
Error *// Flag*
time
TransferringT
Start_Transferring
Start_TransferringT

INVARIANTS

inv1 : Start_Transferring=TRUE ∧ 0 ∉ Transferring ∧ Error=FALSE
 ⇒time≤Start_TransferringT+ PacketTDL
inv2 : 0 ∈ Transferring ∧ Error=FALSE ⇒TransferringT(0)≤Start_TransferringT+ PacketTDL
inv3 : ∀ x · x < last ∧ x ∈ Transferring ∧ x+1 ∉ Transferring ∧ Error=FALSE
 ⇒time≤TransferringT(x)+ PacketTDL
inv4 : ∀ y · y ∈ Transferring ∧ Error = FALSE
 ⇒TransferringT(y)≤Start_TransferringT+(y+1)*PacketTDL
inv5 : Start_TransferringT ≤ time

EVENTS

INITIALISATION ≜

extended

STATUS

ordinary

BEGIN

act1 : transferred := ∅
act2 : Transferring := ∅
act3 : Error := FALSE
act4 : time := 0
act5 : TransferringT := ∅
act6 : Start_Transferring := FALSE
act7 : Start_TransferringT := 0

END

Start_Transferring ≜

extended

STATUS

ordinary

REFINES

Start_Transferring

WHEN

grd1 : Start_Transferring = FALSE

THEN

act1 : Start_Transferring := TRUE
act2 : Start_TransferringT := time

END

Transferring ≜

STATUS

ordinary

REFINES

Transferring
TransferringLast

ANY

m
x
y

WHERE

Message Passing Case-study (Time Added Manually)

```
    grd1 : Start_Transferring = TRUE
    grd2 : m ∈ Send_Message
    grd3 : m = x ↦ y
    grd4 : x ∉ Transferring
    grd5 : x = 0 ⇒ Transferring = ∅
    grd6 : x > 0 ⇒ x-1 ∈ Transferring
    grd7 : Error = FALSE
THEN
    act1 : Transferring := Transferring ∪ {x}
    act2 : transfered := transfered ∪ {m}
    act3 : TransferringT(x) := time
END

Error ≜
    extended
        STATUS
        ordinary
REFINES
    Error
WHEN
    grd1 : Start_Transferring = TRUE
    grd2 : last ∉ Transferring
    grd3 : Error = FALSE
THEN
    act1 : Error := TRUE
END

Tick_Tock ≜
    STATUS
    ordinary
REFINES
    Tick_Tock
ANY
    tick
WHERE
    grd1 : tick ∈ ℕ
    grd2 : tick > 0
    grd3 : Start_Transferring = TRUE ∧ 0 ∉ Transferring ∧ Error = FALSE ⇒ time + tick ≤ Start_TransferringT + PacketTDL
    grd4 : ∀ x · x < last ∧ x ∈ Transferring ∧ x+1 ∉ Transferring ∧ Error = FALSE ⇒ time + tick ≤ TransferringT(x) + PacketTDL
THEN
    act1 : time := time + tick
END

END
```

Machine m03

MACHINE

```

// Deadline(Start_Transferring, Sending(0), 0)
m03 //  $\forall x \cdot x < \text{last} \mid \text{Deadline}(\text{Sending}(x), \text{Transferred}(x) \vee \text{Error}, \text{PacketTDL})$ 
//  $\forall x \cdot x = \text{last} \mid \text{Deadline}(\text{Transferred}(x), \text{Sending}(x+1) \vee \text{Error}, 0)$ 

```

REFINES

m02

SEES

c01

VARIABLES

```

Transferring // Flag
TransferringT // Flag
Sending // Flag
Error // Flag
transferred
sent2 // sent packets
time // time
SendingT // time of sending

```

INVARIANTS

```

inv1 : Sending  $\subseteq \text{dom}(\text{Send\_Message})$  // Type
inv2 : finite(Sending)
inv3 : sent2  $\subseteq \text{Send\_Message}$  // Type
inv4 : SendingT  $\in \text{Sending} \rightarrow \mathbb{N}$  // Type
inv5 :  $0 \in \text{Sending} \Leftrightarrow \text{Start\_Transferring} = \text{TRUE}$  // gluing invariant
inv6 :  $0 \in \text{Sending} \Rightarrow \text{SendingT}(0) = \text{Start\_TransferringT}$  // gluing invariant
inv7 :  $\forall n \cdot n \in \text{Sending} \wedge n > 0 \Rightarrow n-1 \in \text{Transferring}$ 
inv8 : Transferring  $\subseteq \text{Sending}$ 
inv9 :  $\forall n \cdot n \in \text{Sending} \wedge n > 0 \Rightarrow n-1 \in \text{Sending}$ 
inv10 :  $\forall n \cdot n \in \text{Sending} \Rightarrow 0 \dots n \subseteq \text{Sending}$ 
inv11 :  $\forall n \cdot n \in \text{Sending} \wedge n+1 \notin \text{Sending} \Rightarrow 0 \dots n = \text{Sending}$ 
inv13 :  $\forall x \cdot x > 0 \wedge x \in \text{Sending} \Rightarrow \text{TransferringT}(x-1) = \text{SendingT}(x)$ 
inv14 :  $\forall x \cdot x \in \text{Transferring} \Rightarrow x \in \text{Sending}$ 
inv15 :  $\forall x \cdot x < \text{last} \wedge x \in \text{Transferring} \wedge x+1 \notin \text{Sending} \wedge \text{Error} = \text{FALSE}$ 
//  $\Rightarrow \text{time} \leq \text{TransferringT}(x)+0$ 
inv16 :  $\forall x \cdot x \in \text{Transferring} \Rightarrow \text{TransferringT}(x) \leq \text{time}$ 
inv17 :  $\text{dom}(\text{sent2}) = \text{Sending}$ 
inv18 :  $0 \notin \text{Sending} \Rightarrow \text{Sending} = \emptyset$ 
inv19 :  $\forall x \cdot x \in \text{dom}(\text{TransferringT}) \Rightarrow \text{time} \geq \text{TransferringT}(x)$ 

```

EVENTS

INITIALISATION $\triangleq$

STATUS

ordinary

BEGIN

```

act1 : Sending :=  $\emptyset$ 
act2 : Error := FALSE
act3 : transferred :=  $\emptyset$ 
act4 : sent2 :=  $\emptyset$ 
act5 : time := 0
act6 : SendingT :=  $\emptyset$ 
act7 : Transferring :=  $\emptyset$ 
act8 : TransferringT :=  $\emptyset$ 

```

END

Start_Transferring $\triangleq$

STATUS

ordinary

REFINES

Start_Transferring

ANY

```

m
x
y

```

WHERE

grd1 : $m \in \text{Send_Message}$

Message Passing Case-study (Time Added Manually)

```
    grd2 : m = x  $\mapsto$  y
    grd3 : x  $\notin$  Sending
    grd4 : x=0
    grd5 : Error = FALSE
THEN
    act1 : Sending := Sending  $\cup$  {x}
    act2 : sent2 := sent2  $\cup$  {m}
    act3 : SendingT(x) := time
END

Sending  $\triangleq$ 
    STATUS
    ordinary
ANY
    m
    x
    y
WHERE
    grd1 : m  $\in$  Send_Message
    grd2 : m = x  $\mapsto$  y
    grd3 : x  $\notin$  Sending
    grd4 : x = 0  $\Rightarrow$  Transferring =  $\emptyset$ 
    grd5 : x > 0  $\wedge$  x-1  $\in$  Transferring
    grd6 : Error = FALSE
THEN
    act1 : Sending := Sending  $\cup$  {x}
    act2 : sent2 := sent2  $\cup$  {m}
    act3 : SendingT(x) := time
END

Transferring  $\triangleq$ 
    STATUS
    ordinary
REFINES
    Transferring
ANY
    m
    x
    y
WHERE
    grd1 : m  $\in$  Send_Message
    grd2 : m = x  $\mapsto$  y
    grd3 : x  $\notin$  Transferring
    grd4 : x  $\in$  Sending
    grd5 : Error = FALSE
THEN
    act1 : Transferring := Transferring  $\cup$  {x}
    act2 : transfered := transfered  $\cup$  {m}
    act3 : TransferringT(x) := time
END

Error  $\triangleq$ 
    STATUS
    ordinary
REFINES
    Error
ANY
    x
WHERE
    grd1 : x  $\in$  Sending
    grd2 : x  $\notin$  Transferring
    grd3 : Error = FALSE
THEN
    act1 : Error := TRUE
END

Tick_Tock  $\triangleq$ 
    STATUS
    ordinary
```

Message Passing Case-study (Time Added Manually)

REFINES

Tick_Tock

ANY

tick

WHERE

grd1 : $\text{tick} \in \mathbb{N}$

grd2 : $\text{tick} > 0$

grd3 : $\forall x \cdot x \in \text{Sending} \wedge x \notin \text{Transferring} \wedge \text{Error} = \text{FALSE}$
 $\Rightarrow \text{time} + \text{tick} \leq \text{SendingT}(x) + \text{PacketTDL}$

grd4 : $\forall x \cdot x < \text{last} \wedge x \in \text{Transferring} \wedge x+1 \notin \text{Sending} \wedge \text{Error} = \text{FALSE}$
 $\Rightarrow \text{time} + \text{tick} \leq \text{TransferringT}(x) + 0$

THEN

act1 : $\text{time} := \text{time} + \text{tick}$

END

END

Machine m04

MACHINE

```

// Deadline(Start_Transferring, Sending03(0 ↦ 0), 0)
//  $\forall x \cdot x \leq \text{last} \mid \text{Deadline}(\text{Sending03}(x \mapsto 0), \text{Transferring03}(x \mapsto 0) \vee \text{ResendingProcess}(x \mapsto 1), \text{ResendingDL})$ 
//  $\forall x_0, x_1 \cdot x_1 < \text{MaxResend} \mid \text{Deadline}(\text{ResendingProcess}(x_0 \mapsto x_1), \text{Transferring03}(x_0 \mapsto x_1) \vee \text{ResendingProcess}(x_0 \mapsto x_1 + 1), \text{ResendingDL})$ 
m0 //  $\forall x_0 \cdot x_0 \leq \text{last} \mid \text{Deadline}(\text{ResendingProcess}(x_0 \mapsto \text{MaxResend}), \text{Transferring03}(x_0 \mapsto \text{MaxResend}) \vee \text{Error}, \text{ResendingDL})$ 
4 //  $\forall x_0, x_1 \cdot x_0 < \text{last} \mid \text{Deadline}(\text{Transferring03}(x_0 \mapsto x_1), \text{Sending03}(x_0 + 1 \mapsto 0) \vee \text{Error}, 0)$ 
//  $\forall x_0, x_1 \cdot x_1 = 0 \mid \text{Delay}(\text{Sending03}(x_0 \mapsto x_1), \text{ResendingProcess}(x_0 \mapsto x_1 + 1), \text{ResendingDL})$ 
//  $\forall x_0, x_1 \cdot x_1 > 0 \wedge x_1 < \text{MaxResend} \mid \text{Delay}(\text{ResendingProcess}(x_0 \mapsto x_1), \text{ResendingProcess}(x_0 \mapsto x_1 + 1), \text{ResendingDL})$ 
//  $\forall x_0, x_1 \cdot x_1 = \text{MaxResend} \mid \text{Delay}(\text{ResendingProcess}(x_0 \mapsto x_1), \text{Error}, \text{ResendingDL})$ 

```

REFINES

m03

SEES

c02

VARIABLES

```

Sending03      // Flag
Error          // Flag
Transferring03 // Flag
transferred
sent2          // sent packets
time
Sending03T
Transferring03T // time
ResendingProcess // Flag
ResendingProcessT // time

```

INVARIANTS

```

inv1 : ResendingProcess ∈ Sending ↔ 1 · MaxResend // Type
inv2 : ResendingProcessT ∈ ResendingProcess → ℕ // Type
inv3 : Sending03 ∈ Sending → {0} // Type
inv4 : Sending03T ∈ Sending03 → ℕ // Type
inv5 :  $\forall x \cdot x \in \text{dom}(\text{SendingT}) \Rightarrow \text{Sending03T}(x \mapsto 0) = \text{SendingT}(x)$  // gluing
inv6 : Transferring03 ∈ Transferring → 0 · MaxResend // Type
inv7 : Transferring03T ∈ Transferring03 → ℕ // Type
inv8 :  $\forall x, y \cdot x \in \text{dom}(\text{TransferringT}) \wedge x \mapsto y \in \text{dom}(\text{Transferring03T}) \Rightarrow \text{Transferring03T}(x \mapsto y) = \text{TransferringT}(x)$  // gluing
inv9 :  $\forall x, y \cdot x \mapsto y \in \text{ResendingProcess} \wedge y > 1 \Rightarrow x \mapsto y - 1 \in \text{ResendingProcess}$ 
inv10 :  $\forall x \cdot x \mapsto 1 \in \text{ResendingProcess} \Rightarrow x \mapsto 0 \in \text{Sending03}$ 
inv11 :  $\forall x_0, x_1 \cdot x_1 < \text{MaxResend} \wedge x_0 \mapsto x_1 \in \text{ResendingProcess} \wedge x_0 \mapsto x_1 \notin \text{Transferring03} \wedge x_0 \mapsto x_1 + 1 \notin \text{ResendingProcess}$ 
            $\Rightarrow \text{time} \leq \text{ResendingProcessT}(x_0 \mapsto x_1) + \text{ResendingDL}$ 
inv12 :  $\forall x_0 \cdot x_0 \mapsto \text{MaxResend} \in \text{ResendingProcess} \wedge x_0 \mapsto \text{MaxResend} \notin \text{Transferring03} \wedge \text{Error} = \text{FALSE}$ 
            $\Rightarrow \text{time} \leq \text{ResendingProcessT}(x_0 \mapsto \text{MaxResend}) + \text{ResendingDL}$ 
inv13 :  $\forall x \cdot x \mapsto 0 \in \text{Sending03} \wedge x \mapsto 0 \notin \text{Transferring03} \wedge x \mapsto 1 \notin \text{ResendingProcess}$ 
            $\Rightarrow \text{time} \leq \text{Sending03T}(x \mapsto 0) + \text{ResendingDL}$ 
inv14 :  $\forall x_0, x_1 \cdot x_0 \mapsto x_1 \in \text{ResendingProcess} \Rightarrow 1 \cdot x_1 \subseteq \text{ran}(\{x_0\} \triangleleft \text{ResendingProcess})$ 
inv15 :  $\forall x_0, x_1 \cdot x_0 \mapsto x_1 \in \text{ResendingProcess} \Rightarrow \text{ResendingProcessT}(x_0 \mapsto x_1) \leq \text{Sending03T}(x_0 \mapsto 0) + (x_1) * \text{ResendingDL}$ 
inv16 :  $\text{dom}(\text{ResendingProcess}) \subseteq \text{dom}(\text{Sending03})$ 

```

EVENTS

INITIALISATION $\triangleq$

STATUS

ordinary

BEGIN

```

act1 : Sending03 := ∅
act2 : Error := FALSE
act3 : Transferring03 := ∅
act4 : transferred := ∅
act5 : sent2 := ∅
act6 : time := 0

```

Message Passing Case-study (Time Added Manually)

```
act7 : Sending03T :=  $\emptyset$ 
act8 : Transferring03T :=  $\emptyset$ 
act9 : ResendingProcess :=  $\emptyset$ 
act10 : ResendingProcessT :=  $\emptyset$ 
END

Sending03  $\triangleq$ 
  STATUS
  ordinary
REFINES
  Sending
  Start_Transferring
ANY
  m
  x
  y
WHERE
  grd1 : m  $\in$  Send_Message
  grd2 : m = x  $\mapsto$  y
  grd3 : x  $\mapsto$  0  $\notin$  Sending03
  grd4 : x = 0  $\Rightarrow$  Transferring03 =  $\emptyset$ 
  grd5 : x > 0  $\Rightarrow$  x-1  $\in$  dom(Transferring03)
  grd6 : Error = FALSE
THEN
  act1 : Sending03 := Sending03  $\cup$  {x  $\mapsto$  0}
  act2 : sent2 := sent2  $\cup$  {m}
  act3 : Sending03T(x  $\mapsto$  0) := time
END

ResendingProcess  $\triangleq$ 
  STATUS
  ordinary
ANY
  x0
  x1
WHERE
  grd1 : x0  $\mapsto$  x1-1  $\in$  Sending03  $\cup$  ResendingProcess
  grd2 : x0  $\notin$  dom(Transferring03)
  grd3 : x0  $\mapsto$  x1  $\notin$  ResendingProcess
  grd4 : x1  $\leq$  MaxResend
  grd5 : Error = FALSE
  grd6 : x0  $\mapsto$  x1-1  $\in$  Sending03  $\Rightarrow$  time  $\geq$  Sending03T(x0  $\mapsto$  x1-1) + ResendingDL
  grd7 : x0  $\mapsto$  x1-1  $\in$  ResendingProcess  $\Rightarrow$  time  $\geq$  ResendingProcessT(x0  $\mapsto$  x1-1) + ResendingDL
THEN
  act1 : ResendingProcess := ResendingProcess  $\cup$  {x0  $\mapsto$  x1}
  act2 : ResendingProcessT(x0  $\mapsto$  x1) := time
END

Transferring03  $\triangleq$ 
  STATUS
  ordinary
REFINES
  Transferring
ANY
  m
  x0
  x1
  y
WHERE
  grd1 : m  $\in$  Send_Message
  grd2 : m = x0  $\mapsto$  y
  grd3 : x0  $\notin$  dom(Transferring03)
  grd4 : x0  $\mapsto$  x1  $\in$  Sending03  $\cup$  ResendingProcess
  grd5 : Error = FALSE
WITH
  x : x=x0
THEN
  act1 : Transferring03 := Transferring03  $\cup$  {x0  $\mapsto$  x1}
  act2 : transfered := transfered  $\cup$  {m}
```

Message Passing Case-study (Time Added Manually)

```
act3 : Transferring03T( $x_0 \mapsto x_1$ ) := time
END

Error  $\triangleq$ 
  STATUS
  ordinary
REFINES
  Error
ANY
  x
  y
WHERE
  grd1 :  $x \mapsto y \in \text{ResendingProcess}$ 
  grd2 :  $x \notin \text{dom}(\text{Transferring03})$ 
  grd3 :  $y = \text{MaxResend}$ 
  grd4 :  $\text{Error} = \text{FALSE}$ 
  grd5 :  $\text{time} \geq \text{ResendingProcessT}(x \mapsto y) + \text{ResendingDL}$ 
THEN
  act1 :  $\text{Error} := \text{TRUE}$ 
END

Tick_Tock  $\triangleq$ 
  STATUS
  ordinary
REFINES
  Tick_Tock
ANY
  tick
WHERE
  grd1 :  $\text{tick} \in \mathbb{N}$ 
  grd2 :  $\text{tick} > 0$ 
  grd3 :  $\forall x \cdot x \mapsto 0 \in \text{Sending03} \wedge x \mapsto 0 \notin \text{Transferring03} \wedge x \mapsto 1 \notin \text{ResendingProcess}$   

 $\Rightarrow \text{time} + \text{tick} \leq \text{Sending03T}(x \mapsto 0) + \text{ResendingDL}$ 
  grd4 :  $\forall x_0, x_1 \cdot x_1 < \text{MaxResend} \wedge x_0 \mapsto x_1 \in \text{ResendingProcess} \wedge x_0 \mapsto x_1 \notin \text{Transferring03} \wedge x_0 \mapsto x_1 + 1 \notin \text{Resending}$   

 $\text{Process}$   

 $\Rightarrow \text{time} + \text{tick} \leq \text{ResendingProcessT}(x_0 \mapsto x_1) + \text{ResendingDL}$ 
  grd5 :  $\forall x_0 \cdot x_0 \mapsto \text{MaxResend} \in \text{ResendingProcess} \wedge x_0 \mapsto \text{MaxResend} \notin \text{Transferring03} \wedge \text{Error} = \text{FALSE}$   

 $\Rightarrow \text{time} + \text{tick} \leq \text{ResendingProcessT}(x_0 \mapsto \text{MaxResend}) + \text{ResendingDL}$ 
  grd6 :  $\forall x_0, x_1 \cdot x_0 < \text{last} \wedge x_0 \mapsto x_1 \in \text{Transferring03} \wedge x_0 + 1 \mapsto 0 \notin \text{Sending03} \wedge \text{Error} = \text{FALSE}$   

 $\Rightarrow \text{time} + \text{tick} \leq \text{Transferring03T}(x_0 \mapsto x_1) + 0$ 
THEN
  act1 :  $\text{time} := \text{time} + \text{tick}$ 
END

END
```

Machine m05

MACHINE

```

// @grd3 Deadline(Start_Transferring, {Sending03(0 ↦ 0)}, 0)
// @grd4  $\forall x \cdot x \leq \text{last} \mid \text{Deadline}(\text{Sending03}(x \mapsto 0), \{\text{Transferred03}(x \mapsto 0), \text{ResendingProcess}(x \mapsto 1)\}, \text{ResendingDL})$ 
m0 // @grd5  $\forall x0, x1 \cdot x1 < \text{MaxResend} \mid \text{Deadline}(\text{ResendingProcess}(x0 \mapsto x1), \{\text{Transferred03}(x0 \mapsto x1), \text{ResendingProcess}(x0 \mapsto x1 + 1)\}, \text{ResendingDL})$ 
5 // @grd6  $\forall x0 \cdot x0 \leq \text{last} \mid \text{Deadline}(\text{ResendingProcess}(x0 \mapsto \text{MaxResend}), \{\text{Transferred03}(x0 \mapsto \text{MaxResend}), \text{Error}\}, \text{ResendingDL})$ 
// @grd7  $\forall x0, x1 \cdot x0 < \text{last} \mid \text{Deadline}(\text{Transferred03}(x0 \mapsto x1), \{\text{Sending03}(x0 + 1 \mapsto 0), \text{Error}\}, 0)$ 

```

REFINES

m04

SEES

c02

VARIABLES

```

Sending03      // Flag
Error          // Flag
Transferring03 // Flag
transferred
sent2          // sent packets
time
Sending03T
Transferring03T // time
ResendingProcess // Flag
ResendingProcessT // time
DataLost       // Flag
ACKLost        // Flag

```

INVARIANTS

```

inv1 : DataLost  $\subseteq$  Sending03  $\cup$  ResendingProcess
inv2 : ACKLost  $\subseteq$  Sending03  $\cup$  ResendingProcess

```

EVENTS

INITIALISATION $\triangleq$

extended

STATUS

ordinary

BEGIN

```

act1 : Sending03 :=  $\emptyset$ 
act2 : Error := FALSE
act3 : Transferring03 :=  $\emptyset$ 
act4 : transferred :=  $\emptyset$ 
act5 : sent2 :=  $\emptyset$ 
act6 : time := 0
act7 : Sending03T :=  $\emptyset$ 
act8 : Transferring03T :=  $\emptyset$ 
act9 : ResendingProcess :=  $\emptyset$ 
act10 : ResendingProcessT :=  $\emptyset$ 
act13 : DataLost :=  $\emptyset$ 
act14 : ACKLost :=  $\emptyset$ 

```

END

Sending03 $\triangleq$

extended

STATUS

ordinary

REFINES

Sending03

ANY

m
x
y

WHERE

```

grd1 :  $m \in \text{Send\_Message}$ 
grd2 :  $m = x \mapsto y$ 
grd3 :  $x \mapsto 0 \notin \text{Sending03}$ 

```

Message Passing Case-study (Time Added Manually)

```

    grd4 :  $x = 0 \Rightarrow \text{Transferring03} = \emptyset$ 
    grd5 :  $x > 0 \Rightarrow x-1 \in \text{dom}(\text{Transferring03})$ 
    grd6 :  $\text{Error} = \text{FALSE}$ 
THEN
    act1 :  $\text{Sending03} := \text{Sending03} \cup \{x \mapsto 0\}$ 
    act2 :  $\text{sent2} := \text{sent2} \cup \{m\}$ 
    act3 :  $\text{Sending03T}(x \mapsto 0) := \text{time}$ 
END

DataLost  $\triangleq$ 
    STATUS
    ordinary
ANY
    x0
    x1
WHERE
    grd1 :  $x0 \mapsto x1 \in \text{Sending03} \cup \text{ResendingProcess}$ 
    grd2 :  $x0 \mapsto x1 \notin \text{Transferring03}$ 
    grd3 :  $x0 \mapsto x1 \notin \text{DataLost}$ 
    grd4 :  $x0 \mapsto x1 \notin \text{ACKLost}$ 
THEN
    act1 :  $\text{DataLost} := \text{DataLost} \cup \{x0 \mapsto x1\}$ 
END

ACKLost  $\triangleq$ 
    STATUS
    ordinary
ANY
    x0
    x1
WHERE
    grd1 :  $x0 \mapsto x1 \in \text{Sending03} \cup \text{ResendingProcess}$ 
    grd2 :  $x0 \mapsto x1 \notin \text{Transferring03}$ 
    grd3 :  $x0 \mapsto x1 \notin \text{DataLost}$ 
    grd4 :  $x0 \mapsto x1 \notin \text{ACKLost}$ 
THEN
    act1 :  $\text{ACKLost} := \text{ACKLost} \cup \{x0 \mapsto x1\}$ 
END

ResendingProcess  $\triangleq$ 
    extended
    STATUS
    ordinary
REFINES
    ResendingProcess
ANY
    x0
    x1
WHERE
    grd1 :  $x0 \mapsto x1-1 \in \text{Sending03} \cup \text{ResendingProcess}$ 
    grd2 :  $x0 \notin \text{dom}(\text{Transferring03})$ 
    grd3 :  $x0 \mapsto x1 \notin \text{ResendingProcess}$ 
    grd4 :  $x1 \leq \text{MaxResend}$ 
    grd5 :  $\text{Error} = \text{FALSE}$ 
    grd6 :  $x0 \mapsto x1-1 \in \text{Sending03} \Rightarrow \text{time} \geq \text{Sending03T}(x0 \mapsto x1-1) + \text{ResendingDL}$ 
    grd7 :  $x0 \mapsto x1-1 \in \text{ResendingProcess} \Rightarrow \text{time} \geq \text{ResendingProcessT}(x0 \mapsto x1-1) + \text{ResendingDL}$ 
THEN
    act1 :  $\text{ResendingProcess} := \text{ResendingProcess} \cup \{x0 \mapsto x1\}$ 
    act2 :  $\text{ResendingProcessT}(x0 \mapsto x1) := \text{time}$ 
END

Error  $\triangleq$ 
    extended
    STATUS
    ordinary
REFINES
    Error
ANY

```

Message Passing Case-study (Time Added Manually)

```

x
y
WHERE
  grd1 :  $x \mapsto y \in \text{ResendingProcess}$ 
  grd2 :  $x \notin \text{dom}(\text{Transferring03})$ 
  grd3 :  $y = \text{MaxResend}$ 
  grd4 :  $\text{Error} = \text{FALSE}$ 
  grd5 :  $\text{time} \geq \text{ResendingProcessT}(x \mapsto y) + \text{ResendingDL}$ 
THEN
  act1 :  $\text{Error} := \text{TRUE}$ 
END

Tick_Tock  $\triangleq$ 
  extended
    STATUS
  ordinary
REFINES
  Tick_Tock
ANY
  tick
WHERE
  grd1 :  $\text{tick} \in \mathbb{N}$ 
  grd2 :  $\text{tick} > 0$ 
  grd3 :  $\forall x \cdot x \mapsto 0 \in \text{Sending03} \wedge x \mapsto 0 \notin \text{Transferring03} \wedge x \mapsto 1 \notin \text{ResendingProcess}$ 
     $\Rightarrow \text{time} + \text{tick} \leq \text{Sending03T}(x \mapsto 0) + \text{ResendingDL}$ 
  grd4 :  $\forall x0, x1 \cdot x1 < \text{MaxResend} \wedge x0 \mapsto x1 \in \text{ResendingProcess} \wedge x0 \mapsto x1 \notin \text{Transferring03} \wedge x0 \mapsto x1 + 1 \notin \text{Resending}$ 
     $\text{Process}$ 
     $\Rightarrow \text{time} + \text{tick} \leq \text{ResendingProcessT}(x0 \mapsto x1) + \text{ResendingDL}$ 
  grd5 :  $\forall x0 \cdot x0 \mapsto \text{MaxResend} \in \text{ResendingProcess} \wedge x0 \mapsto \text{MaxResend} \notin \text{Transferring03} \wedge \text{Error} = \text{FALSE}$ 
     $\Rightarrow \text{time} + \text{tick} \leq \text{ResendingProcessT}(x0 \mapsto \text{MaxResend}) + \text{ResendingDL}$ 
  grd6 :  $\forall x0, x1 \cdot x0 < \text{last} \wedge x0 \mapsto x1 \in \text{Transferring03} \wedge x0 + 1 \mapsto 0 \notin \text{Sending03} \wedge \text{Error} = \text{FALSE}$ 
     $\Rightarrow \text{time} + \text{tick} \leq \text{Transferring03T}(x0 \mapsto x1) + 0$ 
THEN
  act1 :  $\text{time} := \text{time} + \text{tick}$ 
END

Transferring03  $\triangleq$ 
  extended
    STATUS
  ordinary
REFINES
  Transferring03
ANY
  m
  x0
  x1
  y
WHERE
  grd1 :  $m \in \text{Send\_Message}$ 
  grd2 :  $m = x0 \mapsto y$ 
  grd3 :  $x0 \notin \text{dom}(\text{Transferring03})$ 
  grd4 :  $x0 \mapsto x1 \in \text{Sending03} \cup \text{ResendingProcess}$ 
  grd5 :  $\text{Error} = \text{FALSE}$ 
THEN
  act1 :  $\text{Transferring03} := \text{Transferring03} \cup \{x0 \mapsto x1\}$ 
  act2 :  $\text{transferred} := \text{transferred} \cup \{m\}$ 
  act3 :  $\text{Transferring03T}(x0 \mapsto x1) := \text{time}$ 
END
END

```

Machine m06

MACHINE

```

// Deadline(Start_Transferring, Sending03(0 ↦ 0), 0)
//  $\forall x \cdot x \leq \text{last} \mid \text{Deadline}(\text{Sending03}(x \mapsto 0), \text{Transferred03}(x \mapsto 0) \vee \text{ResendingProcess}(x \mapsto 1), \text{ResendingDL})$ 
//  $\forall x0, x1 \cdot x1 < \text{MaxResend} \mid \text{Deadline}(\text{ResendingProcess}(x0 \mapsto x1), \text{Transferred03}(x0 \mapsto x1) \vee \text{ResendingProcess}(x0 \mapsto x1 + 1), \text{ResendingDL})$ 
//  $\forall x0 \cdot x \leq \text{last} \mid \text{Deadline}(\text{ResendingProcess}(x0 \mapsto \text{MaxResend}), \text{Transferred03}(x0 \mapsto \text{MaxResend}) \vee \text{Error}, \text{ResendingDL})$ 
m0 //  $\forall x0, x1 \cdot x0 < \text{last} \mid \text{Deadline}(\text{Transferred03}(x0 \mapsto x1), \text{Sending03}(x0 + 1 \mapsto 0) \vee \text{Error}, 0)$ 
6 //  $\forall x \cdot x \leq \text{last} \wedge y \leq \text{MaxResend} \mid \text{Deadline}(\text{Sending03}(x \mapsto 0), \text{Receiving}(x \mapsto 0) \vee \text{DataLost}(x \mapsto 0), \text{ChannelDL})$ 
//  $\forall x, y \cdot x \leq \text{last} \wedge y \leq \text{MaxResend} \mid \text{Deadline}(\text{Resending}(x \mapsto y), \text{Receiving}(x \mapsto y) \vee \text{Rereceiving}(x \mapsto y) \vee \text{DataLost}(x \mapsto y), \text{ChannelDL})$ 
//  $\forall x, y \cdot x \leq \text{last} \wedge y \leq \text{MaxResend} \mid \text{Deadline}(\text{Receiving}(x \mapsto y), \text{ReceivingACK}(x \mapsto y) \vee \text{ACKLost}(x \mapsto y), \text{ChannelIDL})$ 
//  $\forall x, y \cdot x \leq \text{last} \wedge y \leq \text{MaxResend} \mid \text{Deadline}(\text{Rereceiving}(x \mapsto y), \text{ReceivingACK}(x \mapsto y) \vee \text{ACKLost}(x \mapsto y), \text{ChannelIDL})$ 

```

REFINES

m05

SEES

c03

VARIABLES

```

Sending03      // Flag
Error          // Flag
ReceivingACK    // Flag
transferred
sent2          // sent packets
time
Sending03T
ReceivingACKT   // time
Resending       // Flag
ResendingT      // time
DataLost        // Flag
ACKLost         // Flag
Receiving       // Flag
ReceivingT      // time
received        // Keep track of the received packetes in the receiver
Rereceiving     // Flag
RereceivingT    // time
Receiver_Error  // Flag

```

INVARIANTS

```

inv1 : Transferring03 = ReceivingACK      // Gluing
inv2 : Transferring03T = ReceivingACKT    // Gluing
inv3 : Receiving ∈ dom(Sending03) ⇒ 0 · MaxResend // Type
inv4 : ReceivingT ∈ Receiving → ℕ        // Type
inv5 : received ⊆ sent2                  // Type
inv6 : ResendingProcess = Resending
inv7 : ResendingProcessT = ResendingT
inv8 : Rereceiving ⊆ Resending           // Type
inv9 : RereceivingT ∈ Rereceiving → ℕ    // Type
inv10 : Receiving ⊆ Sending03 ∪ Resending
inv11 : ACKLost ⊆ Receiving ∪ Rereceiving
inv12 :  $\forall x \cdot x \in \text{Receiving} \cup \text{Rereceiving} \Rightarrow x \notin \text{DataLost}$ 
inv13 : ReceivingACK ⊆ Receiving ∪ Rereceiving
inv14 : Receiver_Error ∈ BOOL           // Type
inv15 :  $\forall x \cdot x \mapsto 0 \in \text{Sending03} \wedge x \mapsto 1 \in \text{Resending} \Rightarrow \text{ResendingT}(x \mapsto 1) \geq \text{Sending03T}(x \mapsto 0) + \text{ResendingDL}$ 
inv16 :  $\forall x, y \cdot x \mapsto y - 1 \in \text{Resending} \wedge x \mapsto y \in \text{Resending} \Rightarrow \text{ResendingT}(x \mapsto y) \geq \text{ResendingT}(x \mapsto y - 1) + \text{ResendingDL}$ 

```

EVENTS

INITIALISATION ≜

STATUS

ordinary

BEGIN

act1 : Sending03 := ∅

Message Passing Case-study (Time Added Manually)

```
act2 : Error := FALSE
act3 : ReceivingACK := ∅
act4 : transfered := ∅
act5 : sent2 := ∅
act6 : time := 0
act7 : Sending03T := ∅
act8 : ReceivingACKT := ∅
act9 : Resending := ∅
act10 : ResendingT := ∅
act11 : DataLost := ∅
act12 : ACKLost := ∅
act13 : Receiving := ∅
act14 : ReceivingT := ∅
act15 : received := ∅
act16 : Rereceiving := ∅
act17 : RereceivingT := ∅
act18 : Receiver_Error := FALSE

END

Sending03 ≜
  STATUS
  ordinary
REFINES
  Sending03
ANY
  m
  x
  y
WHERE
  grd1 : m ∈ Send_Message
  grd2 : m = x ↦ y
  grd3 : x ↦ 0 ∉ Sending03
  grd4 : x = 0 ⇒ ReceivingACK = ∅
  grd5 : x > 0 ⇒ x-1 ∈ dom(ReceivingACK)
  grd6 : Error = FALSE
THEN
  act1 : Sending03 := Sending03 ∪ {x ↦ 0}
  act2 : sent2 := sent2 ∪ {m}
  act3 : Sending03T(x ↦ 0) := time
END

DataLost ≜
  STATUS
  ordinary
REFINES
  DataLost
ANY
  x0
  x1
WHERE
  grd1 : x0 ↦ x1 ∈ Sending03 ∪ Resending
  grd2 : x0 ↦ x1 ∉ Receiving ∪ Rereceiving
  grd3 : x0 ↦ x1 ∉ DataLost
THEN
  act1 : DataLost := DataLost ∪ {x0 ↦ x1}
END

Receiving ≜
  STATUS
  ordinary
ANY
  m
  x0
  x1
  y
WHERE
  grd1 : m ∈ Send_Message
  grd2 : m = x0 ↦ y
```

Message Passing Case-study (Time Added Manually)

```
    grd3 :  $x_0 \mapsto x_1 \in \text{Resending} \cup \text{Sending03}$ 
    grd4 :  $x_0 \notin \text{dom}(\text{Receiving})$ 
    grd5 :  $x_0 \mapsto x_1 \notin \text{DataLost}$ 
THEN
    act1 :  $\text{Receiving} := \text{Receiving} \cup \{x_0 \mapsto x_1\}$ 
    act2 :  $\text{received} := \text{received} \cup \{m\}$ 
    act3 :  $\text{ReceivingT}(x_0 \mapsto x_1) := \text{time}$ 
END

Rereceiving  $\triangleq$ 
  STATUS
  ordinary
ANY
  x0
  x1
WHERE
  grd1 :  $x_0 \mapsto x_1 \in \text{Resending}$ 
  grd2 :  $x_0 \mapsto x_1 \notin \text{DataLost}$ 
  grd3 :  $x_0 \mapsto x_1 \notin \text{Rereceiving}$ 
  grd4 :  $x_0 \mapsto x_1 \notin \text{Receiving}$ 
  grd5 :  $x_0 \in \text{dom}(\text{Receiving})$ 
THEN
  act1 :  $\text{Rereceiving} := \text{Rereceiving} \cup \{x_0 \mapsto x_1\}$ 
  act2 :  $\text{RereceivingT}(x_0 \mapsto x_1) := \text{time}$ 
END

ACKLost  $\triangleq$ 
  STATUS
  ordinary
REFINES
  ACKLost
ANY
  x0
  x1
WHERE
  grd1 :  $x_0 \mapsto x_1 \in \text{Receiving} \cup \text{Rereceiving}$ 
  grd2 :  $x_0 \mapsto x_1 \notin \text{ReceivingACK}$ 
  grd3 :  $x_0 \mapsto x_1 \notin \text{ACKLost}$ 
THEN
  act1 :  $\text{ACKLost} := \text{ACKLost} \cup \{x_0 \mapsto x_1\}$ 
END

Resending  $\triangleq$ 
  STATUS
  ordinary
REFINES
  ResendingProcess
ANY
  x0
  x1
WHERE
  grd1 :  $x_0 \mapsto x_1 - 1 \in \text{Sending03} \cup \text{Resending}$ 
  grd2 :  $x_0 \notin \text{dom}(\text{ReceivingACK})$ 
  grd3 :  $x_0 \mapsto x_1 \notin \text{Resending}$ 
  grd4 :  $x_1 \leq \text{MaxResend}$ 
  grd5 :  $\text{Error} = \text{FALSE}$ 
  grd6 :  $x_0 \mapsto x_1 - 1 \in \text{Sending03} \Rightarrow \text{time} \geq \text{Sending03T}(x_0 \mapsto x_1 - 1) + \text{ResendingDL}$ 
  grd7 :  $x_0 \mapsto x_1 - 1 \in \text{Resending} \Rightarrow \text{time} \geq \text{ResendingT}(x_0 \mapsto x_1 - 1) + \text{ResendingDL}$ 
THEN
  act1 :  $\text{Resending} := \text{Resending} \cup \{x_0 \mapsto x_1\}$ 
  act2 :  $\text{ResendingT}(x_0 \mapsto x_1) := \text{time}$ 
END

ReceivingACK  $\triangleq$ 
  STATUS
  ordinary
REFINES
  Transferring03
```

Message Passing Case-study (Time Added Manually)

```
ANY
  m
  x0
  x1
  y
WHERE
  grd1 : m ∈ Send_Message
  grd2 : m = x0 ↦ y
  grd3 : x0 ∉ dom(ReceivingACK)
  grd4 : x0 ↦ x1 ∈ Receiving ∪ Rereceiving
  grd5 : x0 ↦ x1 ∉ ACKLost
  grd6 : Error = FALSE
THEN
  act1 : ReceivingACK := ReceivingACK ∪ {x0 ↦ x1}
  act2 : transfered := transfered ∪ {m}
  act3 : ReceivingACKT(x0 ↦ x1) := time
END
```

Error $\triangleq$
STATUS

ordinary

REFINES

Error

ANY

x

y

WHERE

```
grd1 : x ↦ y ∈ Resending
grd2 : x ∉ dom(ReceivingACK)
grd3 : y = MaxResend
grd4 : Error = FALSE
grd5 : time ≥ ResendingT(x ↦ y) + ResendingDL
```

THEN

```
act1 : Error := TRUE
```

END

Receiver_Error $\triangleq$
STATUS

ordinary

ANY

x

y

WHERE

```
grd1 : Receiver_Error = FALSE
grd2 : Receiving ≠ ∅
grd3 : last ∉ dom(Receiving)
grd4 : x ↦ y ∈ Receiving
grd5 : x < last
grd6 : x+1 ↦ y ∉ Receiving
grd7 : time ≥ ReceivingT(x ↦ y) + MaxResend * ResendingDL
```

THEN

```
act1 : Receiver_Error := TRUE
```

END

Tick_Tock $\triangleq$
STATUS

ordinary

REFINES

Tick_Tock

ANY

tick

WHERE

```
grd1 : tick ∈ ℕ
grd2 : tick > 0
grd3 : ∀ x · x ↦ 0 ∈ Sending03 ∧ x ↦ 0 ∉ ReceivingACK ∧ x ↦ 1 ∉ Resending
      ⇒ time + tick ≤ Sending03T(x ↦ 0) + ResendingDL
grd4 : ∀ x0, x1 · x1 < MaxResend ∧ x0 ↦ x1 ∈ Resending ∧ x0 ↦ x1+1 ∉ ReceivingACK ∧ x0 ↦ x1+1 ∉ Resending
      ⇒ time + tick ≤ ResendingT(x0 ↦ x1) + ResendingDL
```

Message Passing Case-study (Time Added Manually)

```

grd5 :  $\forall x_0 \cdot x_0 \mapsto \text{MaxResend} \in \text{Resending} \wedge x_0 \mapsto \text{MaxResend} \notin \text{ReceivingACK} \wedge \text{Error} = \text{FALSE}$ 
       $\Rightarrow \text{time} + \text{tick} \leq \text{ResendingT}(x_0 \mapsto \text{MaxResend}) + \text{ResendingDL}$ 
grd6 :  $\forall x_0, x_1 \cdot x_0 < \text{last} \wedge x_0 \mapsto x_1 \in \text{ReceivingACK} \wedge x_0 + 1 \mapsto 0 \notin \text{Sending03} \wedge \text{Error} = \text{FALSE}$ 
       $\Rightarrow \text{time} + \text{tick} \leq \text{ReceivingACKT}(x_0 \mapsto x_1) + 0$ 
grd7 :  $\forall x \cdot x \mapsto 0 \in \text{Sending03} \wedge x \mapsto 0 \notin \text{Receiving} \wedge x \mapsto 0 \notin \text{DataLost} \Rightarrow \text{time} + \text{tick} \leq \text{Sending03T}(x$  // Chan
       $\mapsto 0) + \text{ChannelDL}$  // nel
grd8 :  $\forall x, y \cdot x \mapsto y \in \text{Resending} \wedge x \mapsto y \notin \text{Receiving} \wedge x \mapsto y \notin \text{Rereceiving} \wedge x \mapsto y \notin \text{DataLost} \Rightarrow \text{time} +$  // Cha
       $\text{tick} \leq \text{ResendingT}(x \mapsto y) + \text{ChannelDL}$  // nnel
grd9 :  $\forall x, y \cdot x \mapsto y \in \text{Receiving} \wedge x \mapsto y \notin \text{ReceivingACK} \wedge x \mapsto y \notin \text{ACKLost} \Rightarrow \text{time} + \text{tick} \leq \text{Receiv}$  // Chan
       $\text{gT}(x \mapsto y) + \text{ChannelDL}$  // nel
grd10 :  $\forall x, y \cdot x \mapsto y \in \text{Rereceiving} \wedge x \mapsto y \notin \text{ReceivingACK} \wedge x \mapsto y \notin \text{ACKLost} \Rightarrow \text{time} + \text{tick} \leq \text{Rerecei}$  // Chan
       $\text{vingT}(x \mapsto y) + \text{ChannelDL}$  // nel
grd11 :  $\forall x_0, x_1, x_2 \cdot x_0 < \text{last} \wedge x_0 \mapsto x_1 \in \text{Receiving} \wedge x_0 + 1 \mapsto x_2 \notin \text{Receiving} \wedge x_0 \mapsto x_1 + 1 \notin \text{Rereceivi}$  // Rece
       $\text{ng} \wedge \text{Receiver\_Error} = \text{FALSE}$  // iver
       $\Rightarrow \text{time} + \text{tick} \leq \text{ReceivingT}(x_0 \mapsto x_1) + \text{ReceiverDL}$ 
grd12 :  $\forall x_0, x_1, x_2 \cdot x_0 < \text{last} \wedge x_0 \mapsto x_1 \in \text{Rereceiving} \wedge x_0 + 1 \mapsto x_2 \notin \text{Receiving} \wedge x_0 \mapsto x_1 + 1 \notin \text{Rereceiv}$  // Rece
       $\text{ing} \wedge \text{Receiver\_Error} = \text{FALSE}$  // iver
       $\Rightarrow \text{time} + \text{tick} \leq \text{RereceivingT}(x_0 \mapsto x_1) + \text{ReceiverDL}$ 

THEN
act1 :  $\text{time} := \text{time} + \text{tick}$ 

END

END

```

Machine m07

MACHINE

m07 // Added the created order between drop and resend based on delay

REFINES

m06

SEES

c03

VARIABLES

Sending03 // Flag
 Error // Flag
 ReceivingACK // Flag
 transfered
 sent2 // sent packets
 time
 Sending03T
 ReceivingACKT // time
 Resending // Flag
 ResendingT // time
 DataLost // Flag
 ACKLost // Flag
 Receiving // Flag
 ReceivingT // time
 received // Keep track of the received packetes in the receiver
 Rereceiving // Flag
 RereceivingT // time
 Receiver_Error // Flag

INVARIANTS

inv1 : $\forall x \cdot x \mapsto 0 \in \text{Sending03} \wedge x \mapsto 0 \notin \text{Receiving} \wedge x \mapsto 0 \notin \text{DataLost} \Rightarrow \text{time} \leq \text{Sending03T}(x \mapsto 0) + \text{ChannelDL}$ // ChannelDL
inv2 $\forall x, y \cdot x \mapsto y \in \text{Resending} \wedge x \mapsto y \notin \text{Receiving} \wedge x \mapsto y \notin \text{Rereceiving} \wedge x \mapsto y \notin \text{DataLost} \Rightarrow \text{time} \leq \text{ResendingT}(x \mapsto y) + \text{ChannelDL}$ // ChannelDL
inv3 : $\forall x, y \cdot x \mapsto y \in \text{Receiving} \wedge x \mapsto y \notin \text{ReceivingACK} \wedge x \mapsto y \notin \text{ACKLost} \Rightarrow \text{time} \leq \text{ReceivingT}(x \mapsto y) + \text{ChannelDL}$ // ChannelDL
inv4 : $\forall x, y \cdot x \mapsto y \in \text{Rereceiving} \wedge x \mapsto y \notin \text{ReceivingACK} \wedge x \mapsto y \notin \text{ACKLost} \Rightarrow \text{time} \leq \text{RereceivingT}(x \mapsto y) + \text{ChannelDL}$ // ChannelDL
inv5 : $\forall x \cdot x \mapsto 0 \in \text{Sending03} \wedge x \mapsto 0 \in \text{Receiving} \Rightarrow \text{ReceivingT}(x \mapsto 0) \leq \text{Sending03T}(x \mapsto 0) + \text{ChannelDL}$
inv6 : $\forall x, y \cdot x \mapsto y \in \text{Resending} \wedge x \mapsto y \in \text{Receiving} \Rightarrow \text{ReceivingT}(x \mapsto y) \leq \text{ResendingT}(x \mapsto y) + \text{ChannelDL}$
inv7 : $\forall x, y \cdot x \mapsto y \in \text{Rereceiving} \Rightarrow x \in \text{dom}(\text{Receiving})$
inv8 : $\forall x, y \cdot x \mapsto y \in \text{Resending} \wedge x \mapsto y \in \text{Rereceiving} \Rightarrow \text{RereceivingT}(x \mapsto y) \leq \text{ResendingT}(x \mapsto y) + \text{ChannelDL}$
inv9 : $\forall x, y \cdot x \mapsto y \in \text{Rereceiving} \Rightarrow x \mapsto y \in \text{Resending}$
inv17 : $\forall x, y \cdot x \mapsto y \in \text{Resending} \Rightarrow (x \mapsto y-1 \in \text{Receiving} \cup \text{Rereceiving} \wedge x \mapsto y-1 \in \text{ACKLost}) \vee (x \mapsto y-1 \in \text{DataLost})$

EVENTS

INITIALISATION $\triangleq$

extended

STATUS

ordinary

BEGIN

act1 : $\text{Sending03} := \emptyset$
act2 : $\text{Error} := \text{FALSE}$
act3 : $\text{ReceivingACK} := \emptyset$
act4 : $\text{transfered} := \emptyset$
act5 : $\text{sent2} := \emptyset$
act6 : $\text{time} := 0$
act7 : $\text{Sending03T} := \emptyset$
act8 : $\text{ReceivingACKT} := \emptyset$
act9 : $\text{Resending} := \emptyset$
act10 : $\text{ResendingT} := \emptyset$
act11 : $\text{DataLost} := \emptyset$
act12 : $\text{ACKLost} := \emptyset$
act13 : $\text{Receiving} := \emptyset$
act14 : $\text{ReceivingT} := \emptyset$
act15 : $\text{received} := \emptyset$
act16 : $\text{Rereceiving} := \emptyset$

Message Passing Case-study (Time Added Manually)

```
act17 : RereceivingT := ∅
act18 : Receiver_Error := FALSE
END

Sending03 ≜
  extended
    STATUS
    ordinary
REFINES
  Sending03
ANY
  m
  x
  y
WHERE
  grd1 : m ∈ Send_Message
  grd2 : m = x ↦ y
  grd3 : x ↦ 0 ∉ Sending03
  grd4 : x = 0 ⇒ ReceivingACK = ∅
  grd5 : x > 0 ⇒ x-1 ∈ dom(ReceivingACK)
  grd6 : Error = FALSE
THEN
  act1 : Sending03 := Sending03 ∪ {x ↦ 0}
  act2 : sent2 := sent2 ∪ {m}
  act3 : Sending03T(x ↦ 0) := time
END

DataLost ≜
  extended
    STATUS
    ordinary
REFINES
  DataLost
ANY
  x0
  x1
WHERE
  grd1 : x0 ↦ x1 ∈ Sending03 ∪ Resending
  grd2 : x0 ↦ x1 ∉ Receiving ∪ Rereceiving
  grd3 : x0 ↦ x1 ∉ DataLost
THEN
  act1 : DataLost := DataLost ∪ {x0 ↦ x1}
END

Receiving ≜
  extended
    STATUS
    ordinary
REFINES
  Receiving
ANY
  m
  x0
  x1
  y
WHERE
  grd1 : m ∈ Send_Message
  grd2 : m = x0 ↦ y
  grd3 : x0 ↦ x1 ∈ Resending ∪ Sending03
  grd4 : x0 ∉ dom(Receiving)
  grd5 : x0 ↦ x1 ∉ DataLost
THEN
  act1 : Receiving := Receiving ∪ {x0 ↦ x1}
  act2 : received := received ∪ {m}
  act3 : ReceivingT(x0 ↦ x1) := time
END

Rereceiving ≜
  extended
```

Message Passing Case-study (Time Added Manually)

```

    STATUS
    ordinary
REFINES
  Rereceiving
ANY
  x0
  x1
WHERE
  grd1 :  $x0 \mapsto x1 \in \text{Resending}$ 
  grd2 :  $x0 \mapsto x1 \notin \text{DataLost}$ 
  grd3 :  $x0 \mapsto x1 \notin \text{Rereceiving}$ 
  grd4 :  $x0 \mapsto x1 \notin \text{Receiving}$ 
  grd5 :  $x0 \in \text{dom}(\text{Receiving})$ 
THEN
  act1 :  $\text{Rereceiving} := \text{Rereceiving} \cup \{x0 \mapsto x1\}$ 
  act2 :  $\text{RereceivingT}(x0 \mapsto x1) := \text{time}$ 
END

ACKLost  $\triangleq$ 
  extended
  STATUS
  ordinary
REFINES
  ACKLost
ANY
  x0
  x1
WHERE
  grd1 :  $x0 \mapsto x1 \in \text{Receiving} \cup \text{Rereceiving}$ 
  grd2 :  $x0 \mapsto x1 \notin \text{ReceivingACK}$ 
  grd3 :  $x0 \mapsto x1 \notin \text{ACKLost}$ 
THEN
  act1 :  $\text{ACKLost} := \text{ACKLost} \cup \{x0 \mapsto x1\}$ 
END

Resending  $\triangleq$ 
  extended
  STATUS
  ordinary
REFINES
  Resending
ANY
  x0
  x1
WHERE
  grd1 :  $x0 \mapsto x1 - 1 \in \text{Sending03} \cup \text{Resending}$ 
  grd2 :  $x0 \notin \text{dom}(\text{ReceivingACK})$ 
  grd3 :  $x0 \mapsto x1 \notin \text{Resending}$ 
  grd4 :  $x1 \leq \text{MaxResend}$ 
  grd5 :  $\text{Error} = \text{FALSE}$ 
  grd6 :  $x0 \mapsto x1 - 1 \in \text{Sending03} \Rightarrow \text{time} \geq \text{Sending03T}(x0 \mapsto x1 - 1) + \text{ResendingDL}$ 
  grd7 :  $x0 \mapsto x1 - 1 \in \text{Resending} \Rightarrow \text{time} \geq \text{ResendingT}(x0 \mapsto x1 - 1) + \text{ResendingDL}$ 
THEN
  act1 :  $\text{Resending} := \text{Resending} \cup \{x0 \mapsto x1\}$ 
  act2 :  $\text{ResendingT}(x0 \mapsto x1) := \text{time}$ 
END

ReceivingACK  $\triangleq$ 
  extended
  STATUS
  ordinary
REFINES
  ReceivingACK
ANY
  m
  x0
  x1
  y
WHERE
```

Message Passing Case-study (Time Added Manually)

```

    grd1 :  $m \in \text{Send\_Message}$ 
    grd2 :  $m = x0 \mapsto y$ 
    grd3 :  $x0 \notin \text{dom}(\text{ReceivingACK})$ 
    grd4 :  $x0 \mapsto x1 \in \text{Receiving} \cup \text{Rereceiving}$ 
    grd5 :  $x0 \mapsto x1 \notin \text{ACKLost}$ 
    grd6 :  $\text{Error} = \text{FALSE}$ 
THEN
    act1 :  $\text{ReceivingACK} := \text{ReceivingACK} \cup \{x0 \mapsto x1\}$ 
    act2 :  $\text{transferred} := \text{transferred} \cup \{m\}$ 
    act3 :  $\text{ReceivingACKT}(x0 \mapsto x1) := \text{time}$ 
END

Error  $\triangleq$ 
    extended
        STATUS
    ordinary
REFINES
    Error
ANY
    x
    y
WHERE
    grd1 :  $x \mapsto y \in \text{Resending}$ 
    grd2 :  $x \notin \text{dom}(\text{ReceivingACK})$ 
    grd3 :  $y = \text{MaxResend}$ 
    grd4 :  $\text{Error} = \text{FALSE}$ 
    grd5 :  $\text{time} \geq \text{ResendingT}(x \mapsto y) + \text{ResendingDL}$ 
THEN
    act1 :  $\text{Error} := \text{TRUE}$ 
END

Receiver_Error  $\triangleq$ 
    extended
        STATUS
    ordinary
REFINES
    Receiver_Error
ANY
    x
    y
WHERE
    grd1 :  $\text{Receiver\_Error} = \text{FALSE}$ 
    grd2 :  $\text{Receiving} \neq \emptyset$ 
    grd3 :  $\text{last} \notin \text{dom}(\text{Receiving})$ 
    grd4 :  $x \mapsto y \in \text{Receiving}$ 
    grd5 :  $x < \text{last}$ 
    grd6 :  $x+1 \mapsto y \notin \text{Receiving}$ 
    grd7 :  $\text{time} \geq \text{ReceivingT}(x \mapsto y) + \text{MaxResend} * \text{ResendingDL}$ 
THEN
    act1 :  $\text{Receiver\_Error} := \text{TRUE}$ 
END

Tick_Tock  $\triangleq$ 
    extended
        STATUS
    ordinary
REFINES
    Tick_Tock
ANY
    tick
WHERE
    grd1 :  $\text{tick} \in \mathbb{N}$ 
    grd2 :  $\text{tick} > 0$ 
    grd3 :  $\forall x \cdot x \mapsto 0 \in \text{Sending03} \wedge x \mapsto 0 \notin \text{ReceivingACK} \wedge x \mapsto 1 \notin \text{Resending}$ 
         $\Rightarrow \text{time} + \text{tick} \leq \text{Sending03T}(x \mapsto 0) + \text{ResendingDL}$ 
    grd4 :  $\forall x0, x1 \cdot x1 < \text{MaxResend} \wedge x0 \mapsto x1 \in \text{Resending} \wedge x0 \mapsto x1 \notin \text{ReceivingACK} \wedge x0 \mapsto x1 + 1 \notin \text{Resending}$ 
         $\Rightarrow \text{time} + \text{tick} \leq \text{ResendingT}(x0 \mapsto x1) + \text{ResendingDL}$ 
    grd5 :  $\forall x0 \cdot x0 \mapsto \text{MaxResend} \in \text{Resending} \wedge x0 \mapsto \text{MaxResend} \notin \text{ReceivingACK} \wedge \text{Error} = \text{FALSE}$ 

```

Message Passing Case-study (Time Added Manually)

```

 $\Rightarrow \text{time} + \text{tick} \leq \text{ResendingT}(x0 \mapsto \text{MaxResend}) + \text{ResendingDL}$ 
grd6 :  $\forall x0, x1 \cdot x0 < \text{last} \wedge x0 \mapsto x1 \in \text{ReceivingACK} \wedge x0 + 1 \mapsto 0 \notin \text{Sending03} \wedge \text{Error} = \text{FALSE}$ 
 $\Rightarrow \text{time} + \text{tick} \leq \text{ReceivingACKT}(x0 \mapsto x1) + 0$ 
grd7 :  $\forall x \cdot x \mapsto 0 \in \text{Sending03} \wedge x \mapsto 0 \notin \text{Receiving} \wedge x \mapsto 0 \notin \text{DataLost} \Rightarrow \text{time} + \text{tick} \leq \text{Sending03T}(x \mapsto 0) + \text{ChannelDL}$  // Channel
grd8 :  $\forall x, y \cdot x \mapsto y \in \text{Resending} \wedge x \mapsto y \notin \text{Receiving} \wedge x \mapsto y \notin \text{Rereceiving} \wedge x \mapsto y \notin \text{DataLost} \Rightarrow \text{time} + \text{tick} \leq \text{ResendingT}(x \mapsto y) + \text{ChannelDL}$  // Channel
grd9 :  $\forall x, y \cdot x \mapsto y \in \text{Receiving} \wedge x \mapsto y \notin \text{ReceivingACK} \wedge x \mapsto y \notin \text{ACKLost} \Rightarrow \text{time} + \text{tick} \leq \text{ReceivingT}(x \mapsto y) + \text{ChannelDL}$  // Channel
grd10 :  $\forall x, y \cdot x \mapsto y \in \text{Rereceiving} \wedge x \mapsto y \notin \text{ReceivingACK} \wedge x \mapsto y \notin \text{ACKLost} \Rightarrow \text{time} + \text{tick} \leq \text{RereceivingT}(x \mapsto y) + \text{ChannelDL}$  // Channel
grd11 :  $\forall x0, x1, x2 \cdot x0 < \text{last} \wedge x0 \mapsto x1 \in \text{Receiving} \wedge x0 + 1 \mapsto x2 \notin \text{Receiving} \wedge x0 \mapsto x1 + 1 \notin \text{Rereceiving} \wedge \text{Receiver\_Error} = \text{FALSE}$  // Receiver
 $\Rightarrow \text{time} + \text{tick} \leq \text{ReceivingT}(x0 \mapsto x1) + \text{ReceiverDL}$ 
grd12 :  $\forall x0, x1, x2 \cdot x0 < \text{last} \wedge x0 \mapsto x1 \in \text{Rereceiving} \wedge x0 + 1 \mapsto x2 \notin \text{Receiving} \wedge x0 \mapsto x1 + 1 \notin \text{Rereceiving} \wedge \text{Receiver\_Error} = \text{FALSE}$  // Receiver
 $\Rightarrow \text{time} + \text{tick} \leq \text{RereceivingT}(x0 \mapsto x1) + \text{ReceiverDL}$ 

THEN
act1 :  $\text{time} := \text{time} + \text{tick}$ 

END

END

```

Machine m08

MACHINE

m08 // Duplicate variables to decompose

REFINES

m07

SEES

c03

VARIABLES

Sending03 // Flag
 Error // Flag
 ReceivingACK // Flag
 transfered
 sent2 // sent packets
 time
 Sending03T
 ReceivingACKT // time
 Resending // Flag
 ResendingT // time
 DataLost // Flag
 ACKLost // Flag
 Receiving // Flag
 ReceivingT // time
 received // Keep track of the received packetes in the receiver
 Rereceiving // Flag
 RereceivingT // time
 Receiver_Error // Type
 Sending03_Channel // duplicate
 Receiving_Channel // duplicate
 Sending03T_Channel // duplicate
 Resending_Channel // duplicate
 Rereceiving_Channel // duplicate
 ReceivingACK_Channel // duplicate
 ReceivingT_Channel // duplicate
 RereceivingT_Channel // duplicate
 ResendingT_Channel // duplicate
 ReceivingACKT_Channel // duplicate
 time_channel // duplicate
 time_receiver // duplicate

INVARIANTS

inv1 : Sending03_Channel = Sending03
 inv2 : Receiving_Channel = Receiving
 inv3 : Sending03T_Channel = Sending03T
 inv4 : Resending_Channel = Resending
 inv5 : Rereceiving_Channel = Rereceiving
 inv6 : ReceivingACK_Channel = ReceivingACK
 inv7 : ReceivingT_Channel = ReceivingT
 inv8 : RereceivingT_Channel = RereceivingT
 inv9 : ResendingT_Channel = ResendingT
 inv10 : ReceivingACKT_Channel = ReceivingACKT
 inv11 : time_channel = time
 inv12 : time_receiver = time

EVENTS

INITIALISATION $\triangle$

extended

STATUS

ordinary

BEGIN

act1 : Sending03 := $\emptyset$
 act2 : Error := FALSE
 act3 : ReceivingACK := $\emptyset$
 act4 : transfered := $\emptyset$
 act5 : sent2 := $\emptyset$
 act6 : time := 0
 act7 : Sending03T := $\emptyset$
 act8 : ReceivingACKT := $\emptyset$
 act9 : Resending := $\emptyset$

Message Passing Case-study (Time Added Manually)

```

act10 : ResendingT := ∅
act11 : DataLost := ∅
act12 : ACKLost := ∅
act13 : Receiving := ∅
act14 : ReceivingT := ∅
act15 : received := ∅
act16 : Rereceiving := ∅
act17 : RereceivingT := ∅
act18 : Receiver_Error := FALSE
act19 : Sending03_Channel := ∅
act20 : Receiving_Channel := ∅
act21 : Sending03T_Channel := ∅
act22 : Resending_Channel := ∅
act23 : Rereceiving_Channel := ∅
act24 : ReceivingACK_Channel := ∅
act25 : ReceivingT_Channel := ∅
act26 : RereceivingT_Channel := ∅
act27 : ResendingT_Channel := ∅
act28 : ReceivingACKT_Channel := ∅
act29 : time_receiver := 0
act30 : time_channel := 0

END

Sending03 ≜
  extended
    STATUS
    ordinary
REFINES
  Sending03
ANY
  m
  x
  y
WHERE
  grd1 : m ∈ Send_Message
  grd2 : m = x ↦ y
  grd3 : x ↦ 0 ∉ Sending03
  grd4 : x = 0 ⇒ ReceivingACK = ∅
  grd5 : x > 0 ⇒ x-1 ∈ dom(ReceivingACK)
  grd6 : Error = FALSE
THEN
  act1 : Sending03 := Sending03 ∪ {x ↦ 0}
  act2 : sent2 := sent2 ∪ {m}
  act3 : Sending03T(x ↦ 0) := time
  act4 : Sending03_Channel := Sending03_Channel ∪ {x ↦ 0}
  act5 : Sending03T_Channel(x ↦ 0) := time_channel
END

Resending ≜
  extended
    STATUS
    ordinary
REFINES
  Resending
ANY
  x0
  x1
WHERE
  grd1 : x0 ↦ x1-1 ∈ Sending03 ∪ Resending
  grd2 : x0 ∉ dom(ReceivingACK)
  grd3 : x0 ↦ x1 ∉ Resending
  grd4 : x1 ≤ MaxResend
  grd5 : Error = FALSE
  grd6 : x0 ↦ x1-1 ∈ Sending03 ⇒ time ≥ Sending03T(x0 ↦ x1-1) + ResendingDL
  grd7 : x0 ↦ x1-1 ∈ Resending ⇒ time ≥ ResendingT(x0 ↦ x1-1) + ResendingDL
THEN
  act1 : Resending := Resending ∪ {x0 ↦ x1}
  act2 : ResendingT(x0 ↦ x1) := time

```

Message Passing Case-study (Time Added Manually)

```
act3 : Resending_Channel := Resending_Channel  $\cup$  {x0  $\mapsto$  x1}
act4 : ResendingT_Channel(x0  $\mapsto$  x1) := time_channel
END

ReceivingACK  $\triangleq$ 
  STATUS
  ordinary
REFINES
  ReceivingACK
ANY
  m
  x0
  x1
  y
WHERE
  grd1 : m  $\in$  Send_Message
  grd2 : m = x0  $\mapsto$  y
  grd3 : x0  $\notin$  dom(ReceivingACK)
  grd4 : x0  $\mapsto$  x1  $\in$  Receiving_Channel  $\cup$  Rereceiving_Channel
  grd5 : x0  $\mapsto$  x1  $\notin$  ACKLost
  grd6 : Error = FALSE
THEN
  act1 : ReceivingACK := ReceivingACK  $\cup$  {x0  $\mapsto$  x1}
  act2 : transfered := transfered  $\cup$  {m}
  act3 : ReceivingACKT(x0  $\mapsto$  x1) := time
  act4 : ReceivingACK_Channel := ReceivingACK_Channel  $\cup$  {x0  $\mapsto$  x1}
  act5 : ReceivingACKT_Channel(x0  $\mapsto$  x1) := time_channel
END

Error  $\triangleq$ 
  STATUS
  ordinary
REFINES
  Error
ANY
  x
  y
WHERE
  grd1 : x  $\mapsto$  y  $\in$  Resending
  grd2 : x  $\notin$  dom(ReceivingACK)
  grd3 : y = MaxResend
  grd4 : Error = FALSE
  grd5 : time  $\geq$  ResendingT(x  $\mapsto$  y) + ResendingDL
THEN
  act1 : Error := TRUE
END

DataLost  $\triangleq$ 
  STATUS
  ordinary
REFINES
  DataLost
ANY
  x0
  x1
WHERE
  grd1 : x0 $\mapsto$ x1  $\in$  Sending03_Channel  $\cup$  Resending_Channel
  grd2 : x0 $\mapsto$ x1  $\notin$  Receiving_Channel  $\cup$  Rereceiving_Channel
  grd3 : x0 $\mapsto$ x1  $\notin$  DataLost
THEN
  act1 : DataLost := DataLost  $\cup$  {x0  $\mapsto$  x1}
END

ACKLost  $\triangleq$ 
  STATUS
  ordinary
REFINES
  ACKLost
ANY
```

Message Passing Case-study (Time Added Manually)

```
x0
x1
WHERE
  grd1 :  $x0 \mapsto x1 \in \text{Receiving\_Channel} \cup \text{Rereceiving\_Channel}$ 
  grd2 :  $x0 \mapsto x1 \notin \text{ReceivingACK\_Channel}$ 
  grd3 :  $x0 \mapsto x1 \notin \text{ACKLost}$ 
THEN
  act1 :  $\text{ACKLost} := \text{ACKLost} \cup \{x0 \mapsto x1\}$ 
END

Receiving  $\triangleq$ 
  STATUS
  ordinary
REFINES
  Receiving
ANY
  m
  x0
  x1
  y
WHERE
  grd1 :  $m \in \text{Send\_Message}$ 
  grd2 :  $m = x0 \mapsto y$ 
  grd3 :  $x0 \mapsto x1 \in \text{Resending\_Channel} \cup \text{Sending03\_Channel}$ 
  grd4 :  $x0 \notin \text{dom}(\text{Receiving})$ 
  grd5 :  $x0 \mapsto x1 \notin \text{DataLost}$ 
THEN
  act1 :  $\text{Receiving} := \text{Receiving} \cup \{x0 \mapsto x1\}$ 
  act2 :  $\text{received} := \text{received} \cup \{m\}$ 
  act3 :  $\text{ReceivingT}(x0 \mapsto x1) := \text{time\_receiver}$ 
  act4 :  $\text{Receiving\_Channel} := \text{Receiving\_Channel} \cup \{x0 \mapsto x1\}$ 
  act5 :  $\text{ReceivingT\_Channel}(x0 \mapsto x1) := \text{time\_channel}$ 
END

Rereceiving  $\triangleq$ 
  STATUS
  ordinary
REFINES
  Rereceiving
ANY
  x0
  x1
WHERE
  grd1 :  $x0 \mapsto x1 \in \text{Resending\_Channel}$ 
  grd2 :  $x0 \mapsto x1 \notin \text{DataLost}$ 
  grd3 :  $x0 \mapsto x1 \notin \text{Rereceiving}$ 
  grd4 :  $x0 \mapsto x1 \notin \text{Receiving}$ 
  grd5 :  $x0 \in \text{dom}(\text{Receiving})$ 
THEN
  act1 :  $\text{Rereceiving} := \text{Rereceiving} \cup \{x0 \mapsto x1\}$ 
  act2 :  $\text{RereceivingT}(x0 \mapsto x1) := \text{time\_receiver}$ 
  act3 :  $\text{Rereceiving\_Channel} := \text{Rereceiving\_Channel} \cup \{x0 \mapsto x1\}$ 
  act4 :  $\text{RereceivingT\_Channel}(x0 \mapsto x1) := \text{time\_channel}$ 
END

Receiver_Error  $\triangleq$ 
  STATUS
  ordinary
REFINES
  Receiver_Error
ANY
  x
  y
WHERE
  grd1 :  $\text{Receiver\_Error} = \text{FALSE}$ 
  grd2 :  $\text{Receiving} \neq \emptyset$ 
  grd3 :  $\text{last} \notin \text{dom}(\text{Receiving})$ 
  grd4 :  $x \mapsto y \in \text{Receiving}$ 
  grd5 :  $x < \text{last}$ 
```

Message Passing Case-study (Time Added Manually)

```

    grd6 :  $x+1 \mapsto y \notin \text{Receiving}$ 
    grd7 :  $\text{time\_receiver} \geq \text{ReceivingT}(x \mapsto y) + \text{MaxResend} * \text{ResendingDL}$ 
THEN
    act1 :  $\text{Receiver\_Error} := \text{TRUE}$ 
END

Tick_Tock  $\triangleq$ 
    STATUS
    ordinary
REFINES
    Tick_Tock
ANY
    tick
WHERE
    grd1 :  $\text{tick} \in \mathbb{N}$ 
    grd2 :  $\text{tick} > 0$ 
    grd3 :  $\forall x \cdot x \mapsto 0 \in \text{Sending03} \wedge x \mapsto 0 \notin \text{ReceivingACK} \wedge x \mapsto 1 \notin \text{Resending}$ 
             $\Rightarrow \text{time} + \text{tick} \leq \text{Sending03T}(x \mapsto 0) + \text{ResendingDL}$ 
    grd4 :  $\forall x0, x1 \cdot x1 < \text{MaxResend} \wedge x0 \mapsto x1 \in \text{Resending} \wedge x0 \mapsto x1 \notin \text{ReceivingACK} \wedge x0 \mapsto x1+1 \notin \text{Resending}$ 
             $\Rightarrow \text{time} + \text{tick} \leq \text{ResendingT}(x0 \mapsto x1) + \text{ResendingDL}$ 
    grd5 :  $\forall x0 \cdot x0 \mapsto \text{MaxResend} \in \text{Resending} \wedge x0 \mapsto \text{MaxResend} \notin \text{ReceivingACK} \wedge \text{Error} = \text{FALSE}$ 
             $\Rightarrow \text{time} + \text{tick} \leq \text{ResendingT}(x0 \mapsto \text{MaxResend}) + \text{ResendingDL}$ 
    grd6 :  $\forall x0, x1 \cdot x0 < \text{last} \wedge x0 \mapsto x1 \in \text{ReceivingACK} \wedge x0+1 \mapsto 0 \notin \text{Sending03} \wedge \text{Error} = \text{FALSE}$ 
             $\Rightarrow \text{time} + \text{tick} \leq \text{ReceivingACKT}(x0 \mapsto x1) + 0$ 
    grd7 :  $\forall x \cdot x \mapsto 0 \in \text{Sending03\_Channel} \wedge x \mapsto 0 \notin \text{Receiving\_Channel} \wedge x \mapsto 0 \notin \text{DataLost} \Rightarrow \text{time\_channel} + \text{tick} \leq \text{Sending03T\_Channel}(x \mapsto 0) + \text{ChannelDL}$ 
    grd8 :  $\forall x, y \cdot x \mapsto y \in \text{Resending\_Channel} \wedge x \mapsto y \notin \text{Receiving\_Channel} \wedge x \mapsto y \notin \text{Rereceiving\_Channel} \wedge x \mapsto y \notin \text{DataLost}$ 
             $\Rightarrow \text{time\_channel} + \text{tick} \leq \text{ResendingT\_Channel}(x \mapsto y) + \text{ChannelDL}$ 
    grd9 :  $\forall x, y \cdot x \mapsto y \in \text{Receiving\_Channel} \wedge x \mapsto y \notin \text{ReceivingACK\_Channel} \wedge x \mapsto y \notin \text{ACKLost} \Rightarrow \text{time\_channel} + \text{tick}$ 
             $\leq \text{ReceivingT\_Channel}(x \mapsto y) + \text{ChannelDL}$ 
    grd10 :  $\forall x, y \cdot x \mapsto y \in \text{Rereceiving\_Channel} \wedge x \mapsto y \notin \text{ReceivingACK\_Channel} \wedge x \mapsto y \notin \text{ACKLost} \Rightarrow \text{time\_channel} + \text{tick}$ 
             $\leq \text{RereceivingT\_Channel}(x \mapsto y) + \text{ChannelDL}$ 
    grd11 :  $\forall x0, x1, x2 \cdot x0 < \text{last} \wedge x0 \mapsto x1 \in \text{Receiving} \wedge x0+1 \mapsto x2 \notin \text{Receiving} \wedge x0 \mapsto x1+1 \notin \text{Rereceiving} \wedge \text{Receiver\_Error} = \text{FALSE}$ 
             $\Rightarrow \text{time\_receiver} + \text{tick} \leq \text{ReceivingT}(x0 \mapsto x1) + \text{ReceiverDL}$ 
    grd12 :  $\forall x0, x1, x2 \cdot x0 < \text{last} \wedge x0 \mapsto x1 \in \text{Rereceiving} \wedge x0+1 \mapsto x2 \notin \text{Receiving} \wedge x0 \mapsto x1+1 \notin \text{Rereceiving} \wedge \text{Receiver\_Error} = \text{FALSE}$ 
             $\Rightarrow \text{time\_receiver} + \text{tick} \leq \text{RereceivingT}(x0 \mapsto x1) + \text{ReceiverDL}$ 
THEN
    act1 :  $\text{time} := \text{time} + \text{tick}$ 
    act2 :  $\text{time\_channel} := \text{time\_channel} + \text{tick}$ 
    act3 :  $\text{time\_receiver} := \text{time\_receiver} + \text{tick}$ 
END
END

```

Decomposed Machine Sender

MACHINE

Sender

SEES

c03

VARIABLES

Sending03
Error
ReceivingACK
transferred
sent2
time
Sending03T
ReceivingACKT
Resending
ResendingT

INVARIANTS

typing_ReceivingACK : $\text{ReceivingACK} \in \mathbb{P}(\mathbb{Z} \times \mathbb{Z})$
typing_Resending : $\text{Resending} \in \mathbb{P}(\mathbb{Z} \times \mathbb{Z})$
typing_time : $\text{time} \in \mathbb{Z}$
typing_Sending03 : $\text{Sending03} \in \mathbb{P}(\mathbb{Z} \times \mathbb{Z})$
typing_ResendingT : $\text{ResendingT} \in \mathbb{P}(\mathbb{Z} \times \mathbb{Z} \times \mathbb{Z})$
typing_transferred : $\text{transferred} \in \mathbb{P}(\mathbb{Z} \times \text{NET_MESSAGE})$
typing_sent2 : $\text{sent2} \in \mathbb{P}(\mathbb{Z} \times \text{NET_MESSAGE})$
typing_ReceivingACKT : $\text{ReceivingACKT} \in \mathbb{P}(\mathbb{Z} \times \mathbb{Z} \times \mathbb{Z})$
typing_Sending03T : $\text{Sending03T} \in \mathbb{P}(\mathbb{Z} \times \mathbb{Z} \times \mathbb{Z})$
typing_Error : $\text{Error} \in \text{BOOL}$
m00_inv5 : $\text{time} \in \mathbb{N}$
m00_inv7 : $\text{dom}(\text{Send_Message}) = 0 \cdot \dots \text{last}$
m00_inv8 : $\text{last} \geq 0$
m01_inv1 : $\text{transferred} \subseteq \text{Send_Message}$
m01_inv17 : $\forall x, y \cdot x \in \mathbb{N} \rightarrow \text{NET_MESSAGE} \wedge y \subseteq x \wedge \text{dom}(x) = \text{dom}(y) \Rightarrow x = y$
m03_inv3 : $\text{sent2} \subseteq \text{Send_Message}$
m04_inv4 : $\text{Sending03T} \in \text{Sending03} \rightarrow \mathbb{N}$
m06_inv15 : $\forall x \cdot x \mapsto 0 \in \text{Sending03} \wedge x \mapsto 1 \in \text{Resending} \Rightarrow \text{ResendingT}(x \mapsto 1) \geq \text{Sending03T}(x \mapsto 0) + \text{ResendingDL}$
m06_inv16 : $\forall x, y \cdot x \mapsto y - 1 \in \text{Resending} \wedge x \mapsto y \in \text{Resending} \Rightarrow \text{ResendingT}(x \mapsto y) \geq \text{ResendingT}(x \mapsto y - 1) + \text{ResendingDL}$
:

EVENTS

INITIALISATION $\triangleq$

STATUS

ordinary

BEGIN

act1 : $\text{Sending03} := \emptyset$
act2 : $\text{Error} := \text{FALSE}$
act3 : $\text{ReceivingACK} := \emptyset$
act4 : $\text{transferred} := \emptyset$
act5 : $\text{sent2} := \emptyset$
act6 : $\text{time} := 0$
act7 : $\text{Sending03T} := \emptyset$
act8 : $\text{ReceivingACKT} := \emptyset$
act9 : $\text{Resending} := \emptyset$
act10 : $\text{ResendingT} := \emptyset$

END

Sending03 $\triangleq$

STATUS

ordinary

Message Passing Case-study (Time Added Manually)

ANY

m
x
y

WHERE

typing_m : $m \in \mathbb{Z} \times \text{NET_MESSAGE}$
typing_y : $y \in \text{NET_MESSAGE}$
typing_x : $x \in \mathbb{Z}$
grd1 : $m \in \text{Send_Message}$
grd2 : $m = x \mapsto y$
grd3 : $x \mapsto 0 \notin \text{Sending03}$
grd4 : $x = 0 \Rightarrow \text{ReceivingACK} = \emptyset$
grd5 : $x > 0 \Rightarrow x-1 \in \text{dom}(\text{ReceivingACK})$
grd6 : $\text{Error} = \text{FALSE}$

THEN

act1 : $\text{Sending03} := \text{Sending03} \cup \{x \mapsto 0\}$
act2 : $\text{sent2} := \text{sent2} \cup \{m\}$
act3 : $\text{Sending03T}(x \mapsto 0) := \text{time}$

END

Resending $\triangleq$

STATUS

ordinary

ANY

x0
x1

WHERE

typing_x0 : $x0 \in \mathbb{Z}$
typing_x1 : $x1 \in \mathbb{Z}$
grd1 : $x0 \mapsto x1-1 \in \text{Sending03} \cup \text{Resending}$
grd2 : $x0 \notin \text{dom}(\text{ReceivingACK})$
grd3 : $x0 \mapsto x1 \notin \text{Resending}$
grd4 : $x1 \leq \text{MaxResend}$
grd5 : $\text{Error} = \text{FALSE}$
grd6 : $x0 \mapsto x1-1 \in \text{Sending03} \Rightarrow \text{time} \geq \text{Sending03T}(x0 \mapsto x1-1) + \text{ResendingDL}$
grd7 : $x0 \mapsto x1-1 \in \text{Resending} \Rightarrow \text{time} \geq \text{ResendingT}(x0 \mapsto x1-1) + \text{ResendingDL}$

THEN

act1 : $\text{Resending} := \text{Resending} \cup \{x0 \mapsto x1\}$
act2 : $\text{ResendingT}(x0 \mapsto x1) := \text{time}$

END

ReceivingACK $\triangleq$

STATUS

ordinary

ANY

m
x0
x1
y

WHERE

typing_m : $m \in \mathbb{Z} \times \text{NET_MESSAGE}$
typing_y : $y \in \text{NET_MESSAGE}$
typing_x0 : $x0 \in \mathbb{Z}$
typing_x1 : $x1 \in \mathbb{Z}$
grd1 : $m \in \text{Send_Message}$
grd2 : $m = x0 \mapsto y$
grd3 : $x0 \notin \text{dom}(\text{ReceivingACK})$
grd6 : $\text{Error} = \text{FALSE}$

THEN

act1 : $\text{ReceivingACK} := \text{ReceivingACK} \cup \{x0 \mapsto x1\}$
act2 : $\text{transferred} := \text{transferred} \cup \{m\}$
act3 : $\text{ReceivingACKT}(x0 \mapsto x1) := \text{time}$

Message Passing Case-study (Time Added Manually)

END

Error $\triangleq$

STATUS

ordinary

ANY

x

y

WHERE

typing_y : $y \in \mathbb{Z}$

typing_x : $x \in \mathbb{Z}$

grd1 : $x \mapsto y \in \text{Resending}$

grd2 : $x \notin \text{dom}(\text{ReceivingACK})$

grd3 : $y = \text{MaxResend}$

grd4 : $\text{Error} = \text{FALSE}$

grd5 : $\text{time} \geq \text{ResendingT}(x \mapsto y) + \text{ResendingDL}$

THEN

act1 : $\text{Error} := \text{TRUE}$

END

Tick_Tock $\triangleq$

STATUS

ordinary

ANY

tick

WHERE

typing_tick : $\text{tick} \in \mathbb{Z}$

grd1 : $\text{tick} \in \mathbb{N}$

grd2 : $\text{tick} > 0$

grd3 : $\forall x \cdot x \mapsto 0 \in \text{Sending03} \wedge x \mapsto 0 \notin \text{ReceivingACK} \wedge x \mapsto 1 \notin \text{Resending}$
 $\Rightarrow \text{time} + \text{tick} \leq \text{Sending03T}(x \mapsto 0) + \text{ResendingDL}$

grd4 : $\forall x_0, x_1 \cdot x_1 < \text{MaxResend} \wedge x_0 \mapsto x_1 \in \text{Resending} \wedge x_0 \mapsto x_1 \notin \text{ReceivingACK} \wedge x_0 \mapsto x_1 + 1 \notin \text{Resending}$
 $\Rightarrow \text{time} + \text{tick} \leq \text{ResendingT}(x_0 \mapsto x_1) + \text{ResendingDL}$

grd5 : $\forall x_0 \cdot x_0 \mapsto \text{MaxResend} \in \text{Resending} \wedge x_0 \mapsto \text{MaxResend} \notin \text{ReceivingACK} \wedge \text{Error} = \text{FALSE}$
 $\Rightarrow \text{time} + \text{tick} \leq \text{ResendingT}(x_0 \mapsto \text{MaxResend}) + \text{ResendingDL}$

grd6 : $\forall x_0, x_1 \cdot x_0 < \text{last} \wedge x_0 \mapsto x_1 \in \text{ReceivingACK} \wedge x_0 + 1 \mapsto 0 \notin \text{Sending03} \wedge \text{Error} = \text{FALSE}$
 $\Rightarrow \text{time} + \text{tick} \leq \text{ReceivingACKT}(x_0 \mapsto x_1) + 0$

THEN

act1 : $\text{time} := \text{time} + \text{tick}$

END

END

Decomposed Machine Receiver

MACHINE

Receiver

SEES

c03

VARIABLES

Receiving
ReceivingT
received
Rereceiving
RereceivingT
Receiver_Error
time_receiver

INVARIANTS

typing_Receiving : $\text{Receiving} \in \mathbb{P}(\mathbb{Z} \times \mathbb{Z})$
typing_ReceivingT : $\text{ReceivingT} \in \mathbb{P}(\mathbb{Z} \times \mathbb{Z} \times \mathbb{Z})$
typing_time_receiver : $\text{time_receiver} \in \mathbb{Z}$
typing_received : $\text{received} \in \mathbb{P}(\mathbb{Z} \times \text{NET_MESSAGE})$
typing_Receiver_Error : $\text{Receiver_Error} \in \text{BOOL}$
typing_RereceivingT : $\text{RereceivingT} \in \mathbb{P}(\mathbb{Z} \times \mathbb{Z} \times \mathbb{Z})$
typing_Rereceiving : $\text{Rereceiving} \in \mathbb{P}(\mathbb{Z} \times \mathbb{Z})$
m00_inv7 : $\text{dom}(\text{Send_Message}) = 0 \cdot \text{last}$
m00_inv8 : $\text{last} \geq 0$
m01_inv17 : $\forall x, y \cdot x \in \mathbb{N} \rightarrow \text{NET_MESSAGE} \wedge y \subseteq x \wedge \text{dom}(x) = \text{dom}(y) \Rightarrow x = y$
m06_inv4 : $\text{ReceivingT} \in \text{Receiving} \rightarrow \mathbb{N}$
m06_inv9 : $\text{RereceivingT} \in \text{Rereceiving} \rightarrow \mathbb{N}$
m07_inv7 : $\forall x, y \cdot x \mapsto y \in \text{Rereceiving} \Rightarrow x \in \text{dom}(\text{Receiving})$

EVENTS

INITIALISATION $\triangleq$

STATUS

ordinary

BEGIN

act13 : $\text{Receiving} := \emptyset$
act14 : $\text{ReceivingT} := \emptyset$
act15 : $\text{received} := \emptyset$
act16 : $\text{Rereceiving} := \emptyset$
act17 : $\text{RereceivingT} := \emptyset$
act18 : $\text{Receiver_Error} := \text{FALSE}$
act29 : $\text{time_receiver} := 0$

END

Receiving $\triangleq$

STATUS

ordinary

ANY

m
x0
x1
y

WHERE

typing_m : $m \in \mathbb{Z} \times \text{NET_MESSAGE}$
typing_y : $y \in \text{NET_MESSAGE}$
typing_x0 : $x0 \in \mathbb{Z}$
typing_x1 : $x1 \in \mathbb{Z}$
grd1 : $m \in \text{Send_Message}$
grd2 : $m = x0 \mapsto y$
grd4 : $x0 \notin \text{dom}(\text{Receiving})$

THEN

act1 : $\text{Receiving} := \text{Receiving} \cup \{x0 \mapsto x1\}$
act2 : $\text{received} := \text{received} \cup \{m\}$

Message Passing Case-study (Time Added Manually)

act3 : ReceivingT($x0 \mapsto x1$) := time_receiver
END

Rereceiving $\triangleq$
STATUS

ordinary

ANY

x0
x1

WHERE

typing_x0 : $x0 \in \mathbb{Z}$
typing_x1 : $x1 \in \mathbb{Z}$
grd3 : $x0 \mapsto x1 \notin \text{Rereceiving}$
grd4 : $x0 \mapsto x1 \notin \text{Receiving}$
grd5 : $x0 \in \text{dom}(\text{Receiving})$

THEN

act1 : $\text{Rereceiving} := \text{Rereceiving} \cup \{x0 \mapsto x1\}$
act2 : $\text{RereceivingT}(x0 \mapsto x1) := \text{time_receiver}$

END

Receiver_Error $\triangleq$
STATUS

ordinary

ANY

x
y

WHERE

typing_y : $y \in \mathbb{Z}$
typing_x : $x \in \mathbb{Z}$
grd1 : $\text{Receiver_Error} = \text{FALSE}$
grd2 : $\text{Receiving} \neq \emptyset$
grd3 : $\text{last} \notin \text{dom}(\text{Receiving})$
grd4 : $x \mapsto y \in \text{Receiving}$
grd5 : $x < \text{last}$
grd6 : $x+1 \mapsto y \notin \text{Receiving}$
grd7 : $\text{time_receiver} \geq \text{ReceivingT}(x \mapsto y) + \text{MaxResend} * \text{ResendingDL}$

THEN

act1 : $\text{Receiver_Error} := \text{TRUE}$

END

Tick_Tock $\triangleq$
STATUS

ordinary

ANY

tick

WHERE

typing_tick : $\text{tick} \in \mathbb{Z}$
grd1 : $\text{tick} \in \mathbb{N}$
grd2 : $\text{tick} > 0$
grd11 : $\forall x0, x1, x2 \cdot x0 < \text{last} \wedge x0 \mapsto x1 \in \text{Receiving} \wedge x0+1 \mapsto x2 \notin \text{Receiving} \wedge x0 \mapsto x1+1 \notin \text{Rereceiving}$
: $\wedge \text{Receiver_Error} = \text{FALSE}$
: $\Rightarrow \text{time_receiver} + \text{tick} \leq \text{ReceivingT}(x0 \mapsto x1) + \text{ReceiverDL}$
grd12 : $\forall x0, x1, x2 \cdot x0 < \text{last} \wedge x0 \mapsto x1 \in \text{Rereceiving} \wedge x0+1 \mapsto x2 \notin \text{Receiving} \wedge x0 \mapsto x1+1 \notin \text{Rereceiving}$
: $\wedge \text{Receiver_Error} = \text{FALSE}$
: $\Rightarrow \text{time_receiver} + \text{tick} \leq \text{RereceivingT}(x0 \mapsto x1) + \text{ReceiverDL}$

THEN

act3 : $\text{time_receiver} := \text{time_receiver} + \text{tick}$

END

END

Decomposed Machine Channel

MACHINE

Channel

SEES

c03

VARIABLES

DataLost
ACKLost
time_channel
Sending03_Channel
Receiving_Channel
Sending03T_Channel
Resending_Channel
Rereceiving_Channel
ReceivingACK_Channel
ReceivingT_Channel
RereceivingT_Channel
ResendingT_Channel
ReceivingACKT_Channel

INVARIANTS

typing_Resending_Channel : Resending_Channel $\in \mathbb{P}(\mathbb{Z} \times \mathbb{Z})$
typing_ACKLost : ACKLost $\in \mathbb{P}(\mathbb{Z} \times \mathbb{Z})$
typing_DataLost : DataLost $\in \mathbb{P}(\mathbb{Z} \times \mathbb{Z})$
typing_Sending03T_Channel : Sending03T_Channel $\in \mathbb{P}(\mathbb{Z} \times \mathbb{Z} \times \mathbb{Z})$
typing_RereceivingT_Channel : RereceivingT_Channel $\in \mathbb{P}(\mathbb{Z} \times \mathbb{Z} \times \mathbb{Z})$
typing_Sending03_Channel : Sending03_Channel $\in \mathbb{P}(\mathbb{Z} \times \mathbb{Z})$
typing_Rereceiving_Channel : Rereceiving_Channel $\in \mathbb{P}(\mathbb{Z} \times \mathbb{Z})$
typing_time_channel : time_channel $\in \mathbb{Z}$
typing_ReceivingACK_Channel : ReceivingACK_Channel $\in \mathbb{P}(\mathbb{Z} \times \mathbb{Z})$
typing_Receiving_Channel : Receiving_Channel $\in \mathbb{P}(\mathbb{Z} \times \mathbb{Z})$
typing_ReceivingACKT_Channel : ReceivingACKT_Channel $\in \mathbb{P}(\mathbb{Z} \times \mathbb{Z} \times \mathbb{Z})$
typing_ReceivingT_Channel : ReceivingT_Channel $\in \mathbb{P}(\mathbb{Z} \times \mathbb{Z} \times \mathbb{Z})$
typing_ResendingT_Channel : ResendingT_Channel $\in \mathbb{P}(\mathbb{Z} \times \mathbb{Z} \times \mathbb{Z})$
m00_inv7 : dom(Send_Message) = 0 · last
m00_inv8 : last ≥ 0
m01_inv17 : $\forall x, y \cdot x \in \mathbb{N} \rightarrow \text{NET_MESSAGE} \wedge y \subseteq x \wedge \text{dom}(x) = \text{dom}(y) \Rightarrow x = y$

EVENTS

INITIALISATION $\triangleq$

STATUS

ordinary

BEGIN

act11 : DataLost := $\emptyset$
act12 : ACKLost := $\emptyset$
act19 : Sending03_Channel := $\emptyset$
act20 : Receiving_Channel := $\emptyset$
act21 : Sending03T_Channel := $\emptyset$
act22 : Resending_Channel := $\emptyset$
act23 : Rereceiving_Channel := $\emptyset$
act24 : ReceivingACK_Channel := $\emptyset$
act25 : ReceivingT_Channel := $\emptyset$
act26 : RereceivingT_Channel := $\emptyset$
act27 : ResendingT_Channel := $\emptyset$
act28 : ReceivingACKT_Channel := $\emptyset$
act30 : time_channel := 0

END

Sending03 $\triangleq$

Message Passing Case-study (Time Added Manually)

```

    STATUS
ordinary
ANY
    m
    x
    y
WHERE
    typing_m : m ∈ ℤ × NET_MESSAGE
    typing_y : y ∈ NET_MESSAGE
    typing_x : x ∈ ℤ
    grd1 : m ∈ Send_Message
    grd2 : m = x ↦ y
THEN
    act4 : Sending03_Channel := Sending03_Channel ∪ {x ↦ 0}
    act5 : Sending03T_Channel(x ↦ 0) := time_channel
END

Resending ≜
    STATUS
ordinary
ANY
    x0
    x1
WHERE
    typing_x0 : x0 ∈ ℤ
    typing_x1 : x1 ∈ ℤ
    grd4 : x1 ≤ MaxResend
THEN
    act3 : Resending_Channel := Resending_Channel ∪ {x0 ↦ x1}
    act4 : ResendingT_Channel(x0 ↦ x1) := time_channel
END

ReceivingACK ≜
    STATUS
ordinary
ANY
    m
    x0
    x1
    y
WHERE
    typing_m : m ∈ ℤ × NET_MESSAGE
    typing_y : y ∈ NET_MESSAGE
    typing_x0 : x0 ∈ ℤ
    typing_x1 : x1 ∈ ℤ
    grd1 : m ∈ Send_Message
    grd2 : m = x0 ↦ y
    grd4 : x0 ↦ x1 ∈ Receiving_Channel ∪ Rereceiving_Channel
    grd5 : x0 ↦ x1 ∉ ACKLost
THEN
    act4 : ReceivingACK_Channel := ReceivingACK_Channel ∪ {x0 ↦ x1}
    act5 : ReceivingACKT_Channel(x0 ↦ x1) := time_channel
END

DataLost ≜
    STATUS
ordinary
ANY
    x0
    x1
WHERE
    typing_x0 : x0 ∈ ℤ
```

Message Passing Case-study (Time Added Manually)

```
typing_x1 : x1 ∈ ℤ
grd1 : x0↦x1 ∈ Sending03_Channel ∪ Resending_Channel
grd2 : x0↦x1 ∉ Receiving_Channel ∪ Rereceiving_Channel
grd3 : x0↦x1 ∉ DataLost
THEN
  act1 : DataLost := DataLost ∪ {x0 ↦ x1}
END

ACKLost ≜
  STATUS
  ordinary
ANY
  x0
  x1
WHERE
  typing_x0 : x0 ∈ ℤ
  typing_x1 : x1 ∈ ℤ
  grd1 : x0↦x1 ∈ Receiving_Channel ∪ Rereceiving_Channel
  grd2 : x0↦x1 ∉ ReceivingACK_Channel
  grd3 : x0↦x1 ∉ ACKLost
THEN
  act1 : ACKLost := ACKLost ∪ {x0 ↦ x1}
END

Receiving ≜
  STATUS
  ordinary
ANY
  m
  x0
  x1
  y
WHERE
  typing_m : m ∈ ℤ × NET_MESSAGE
  typing_y : y ∈ NET_MESSAGE
  typing_x0 : x0 ∈ ℤ
  typing_x1 : x1 ∈ ℤ
  grd1 : m ∈ Send_Message
  grd2 : m = x0 ↦ y
  grd3 : x0↦x1 ∈ Resending_Channel ∪ Sending03_Channel
  grd5 : x0↦x1 ∉ DataLost
THEN
  act4 : Receiving_Channel := Receiving_Channel ∪ {x0↦x1}
  act5 : ReceivingT_Channel(x0↦x1) := time_channel
END

Rereceiving ≜
  STATUS
  ordinary
ANY
  x0
  x1
WHERE
  typing_x0 : x0 ∈ ℤ
  typing_x1 : x1 ∈ ℤ
  grd1 : x0↦x1 ∈ Resending_Channel
  grd2 : x0↦x1 ∉ DataLost
THEN
  act3 : Rereceiving_Channel := Rereceiving_Channel ∪ {x0↦x1}
  act4 : RereceivingT_Channel(x0↦x1) := time_channel
END
```

Message Passing Case-study (Time Added Manually)

```
Tick_Tock  $\triangleq$ 
  STATUS
  ordinary
ANY
  tick
WHERE
  typing_tick : tick  $\in \mathbb{Z}$ 
  grd1 : tick  $\in \mathbb{N}$ 
  grd2 : tick  $> 0$ 
  grd7  $\forall x \cdot x \mapsto 0 \in \text{Sending03\_Channel} \wedge x \mapsto 0 \notin \text{Receiving\_Channel} \wedge x \mapsto 0 \notin \text{DataLost} \Rightarrow \text{time\_channel} +$ 
    : tick  $\leq \text{Sending03T\_Channel}(x \mapsto 0) + \text{ChannelDL}$ 
  grd8  $\forall x, y \cdot x \mapsto y \in \text{Resending\_Channel} \wedge x \mapsto y \notin \text{Receiving\_Channel} \wedge x \mapsto y \notin \text{Rereceiving\_Channel} \wedge x$ 
    :  $\mapsto y \notin \text{DataLost} \Rightarrow \text{time\_channel} + \text{tick} \leq \text{ResendingT\_Channel}(x \mapsto y) + \text{ChannelDL}$ 
  grd9  $\forall x, y \cdot x \mapsto y \in \text{Receiving\_Channel} \wedge x \mapsto y \notin \text{ReceivingACK\_Channel} \wedge x \mapsto y \notin \text{ACKLost} \Rightarrow \text{time\_ch}$ 
    : annel + tick  $\leq \text{ReceivingT\_Channel}(x \mapsto y) + \text{ChannelDL}$ 
  grd10  $\forall x, y \cdot x \mapsto y \in \text{Rereceiving\_Channel} \wedge x \mapsto y \notin \text{ReceivingACK\_Channel} \wedge x \mapsto y \notin \text{ACKLost} \Rightarrow \text{time\_}$ 
    : channel + tick  $\leq \text{RereceivingT\_Channel}(x \mapsto y) + \text{ChannelDL}$ 
THEN
  act2 : time_channel := time_channel + tick
END
END
```