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Determination of Dynamic Flexure Model Parameters for Ship Angular Deformation Measurement

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Outline

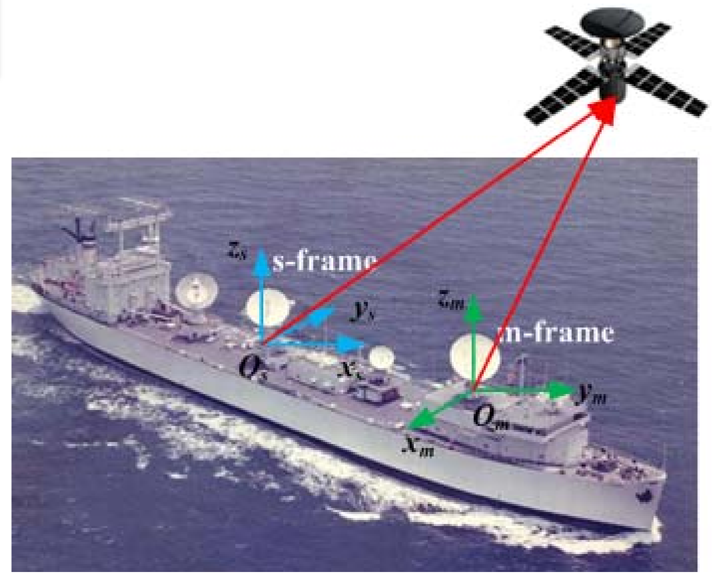
1. **Background**
2. **Parameters Estimation Approach**
3. **Simulation System**
4. **Results and Analysis**
5. **Conclusions**

Background

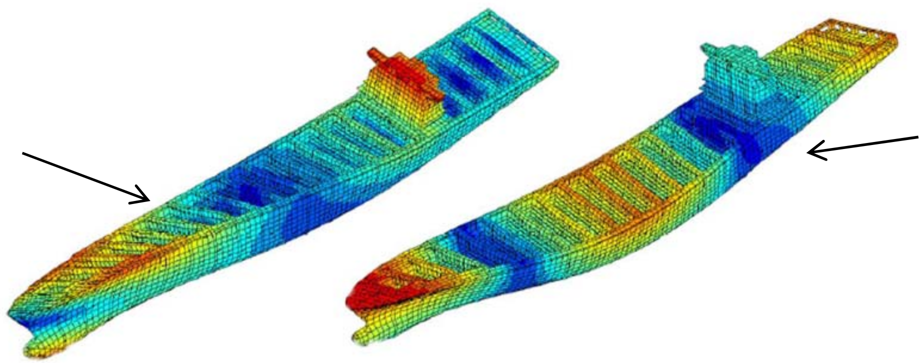
● Ship Angular Deformation

Ship angular deformation refers to the two frames angle displacement

Pitching: cross *x*-axis
Rolling: cross *y*-axis
Yawing: cross *z*-axis



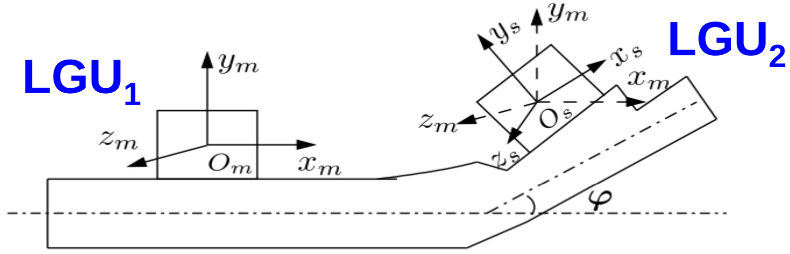
rolling deformation



pitching deformation

Background

● Measurement Approach



Measurement system

Ship deformation:

$$\varphi(t)=\phi_0+\theta(t)$$

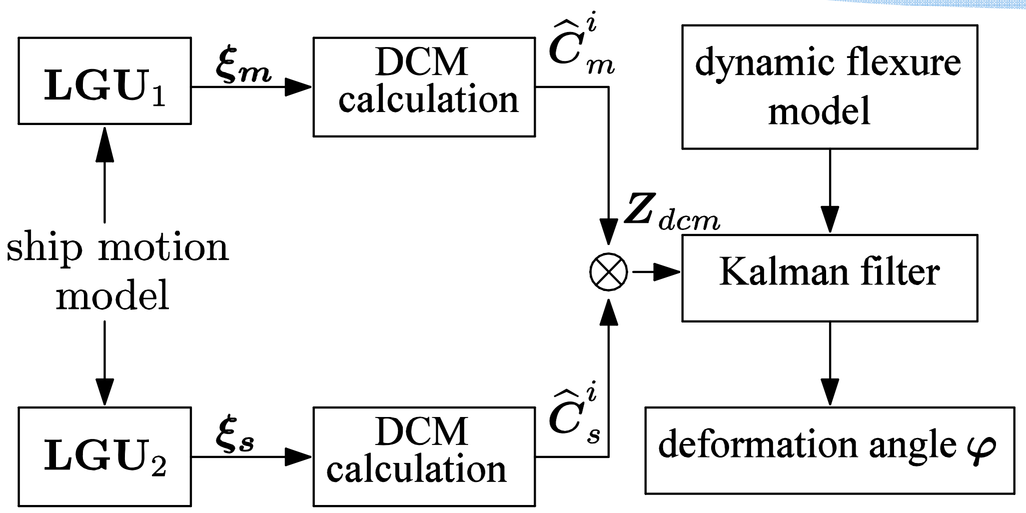
where ϕ_0 is time-invariant component,

$\theta(t)$ is dynamic component, which is usually modeled as a second-order Gauss-Markov process, the correlation function is

$$R_{\theta_i}(\tau)=\sigma_i^{\,2}\exp\left(-\alpha_i\left|\tau\right|\right)\left(\cos\beta_i\tau+\frac{\alpha_i}{\beta_i}\sin\beta_i\left|\tau\right|\right),i=x,y,z$$

in which σ^2 is the variance, α is the damping factor, β is the circular frequency.

Background



Schematic diagram of ship deformation measurement system

Kalman Filter

Measurement function: $Z_{dcm} = B\theta - A\phi_0 + B\left(\hat{C}_i^m \psi_m - \hat{C}_i^s \psi_s\right)$

State function: $\dot{X} = FX + w$

State vector: $X = [\phi_0^T \ \theta^T \ \dot{\theta}^T \ \psi_m^T \ \psi_s^T \ \tilde{\varepsilon}_m^T \ \tilde{\varepsilon}_s^T]^T$

Background

Specifically, the measurement vector is given by

$$\boldsymbol{Z}_{dcm} = \begin{bmatrix} C_{13}C'_{12} + C_{23}C'_{22} + C_{33}C'_{32} \\ C_{13}C'_{11} + C_{23}C'_{21} + C_{33}C'_{31} \\ C_{11}C'_{12} + C_{21}C'_{22} + C_{31}C'_{32} \end{bmatrix},$$

and the matrices A and B are given by

$$\boldsymbol{A} = \begin{bmatrix} C_{33}C'_{22} - C_{23}C'_{32} & C_{13}C'_{32} - C_{33}C'_{12} & C_{23}C'_{12} - C_{13}C'_{22} \\ C_{33}C'_{21} - C_{23}C'_{31} & C_{13}C'_{31} - C_{33}C'_{11} & C_{23}C'_{11} - C_{13}C'_{21} \\ C_{31}C'_{22} - C_{21}C'_{32} & C_{11}C'_{32} - C_{31}C'_{12} & C_{21}C'_{12} - C_{11}C'_{22} \end{bmatrix} \text{ and } \boldsymbol{B} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{bmatrix},$$

where C_{ij} and C'_{ij} are the components of DCMs of LGU_1 and LGU_2, respectively.

Background

The state transition matrix is given by

$$\boldsymbol{F} = \begin{bmatrix} \boldsymbol{O}_{3\times3} & & \\ & \boldsymbol{F}^1_{6\times6} & \\ & & \boldsymbol{F}^2_{12\times12} \end{bmatrix}$$

in which

$$\boldsymbol{F}^1_{6\times6} = \begin{bmatrix} & \boldsymbol{O}_{3\times3} & & & \boldsymbol{I}_3 & \\ -b_x^2 & 0 & 0 & -2\mu_x & 0 & 0 \\ 0 & -b_y^2 & 0 & 0 & -2\mu_y & 0 \\ 0 & 0 & -b_z^2 & 0 & 0 & -2\mu_z \end{bmatrix}$$

and

$$\boldsymbol{F}^2_{12\times12} = \begin{bmatrix} \boldsymbol{O}_{3\times6} & -\widehat{\boldsymbol{C}}^i_m & \boldsymbol{O}_{3\times3} \\ \boldsymbol{O}_{3\times6} & \boldsymbol{O}_{3\times3} & -\widehat{\boldsymbol{C}}^i_s \\ & \boldsymbol{O}_{6\times12} & \end{bmatrix},$$

The state noise covariance is

$$E\left[\boldsymbol{w}\boldsymbol{w}^{\mathrm{T}}\right] = \mathrm{diag}\Big\{\boldsymbol{O}_{1\times3}, 4b_x^2\sigma_x^2\alpha_x, 4b_y^2\sigma_y^2\alpha_y, 4b_z^2\sigma_z^2\alpha_z, \boldsymbol{O}_{1\times9}, \left(\boldsymbol{\sigma}^2_{mr}\right)^{\mathrm{T}}, \left(\boldsymbol{\sigma}^2_{sr}\right)^{\mathrm{T}}\Big\},$$

Background

Determine the Dynamic Flexure Model Parameters

- **Empirical method**

  The parameters are determined according to experience

- **Statistical method**

  The parameters are obtained from previously recorded measurement data

In actual condition, the parameters depend on sea condition, ship velocity and ship structure, etc. It requires to estimate the parameters on-line.

Background

Our Novelty

The dynamic flexure information is existing in attitude difference measured by LGU_1 and LGU_2.

$$Z_{dcm} = B\theta - A\phi_0 + B\left(\hat{C}_i^m \psi_m - \hat{C}_i^s \psi_s\right)$$

Assume the dynamic flexure can be depicted as a second-order Gauss-Markov process, we developed an on-line dynamic flexure parameters estimation method by utilising the attitude difference measured by two LGUs, and Tufts-Kumaresan (T-K) method was applied to obtain a robust and accuracy estimates.

Parameters Estimation Approach

The attitude matching function can be written as

$$Z_{dcm} = B\theta + (B - A)\phi_0 + B\left(\hat{C}_i^m \psi_m - \hat{C}_i^s \psi_s\right)$$

$$\tilde{Z}_{dcm} \approx B\theta$$

Remove the second term $(B - A)\phi_0$ **: for** $(B\text{-}A)$ **is a small, and** ϕ_0 **can be compensated to several** ***mrads*** **using the course estimate results, so the multiply results are small and can be removed.**

Remove the third term $B\left(\hat{C}_i^m \psi_m - \hat{C}_i^s \psi_s\right)$**: for the frequency of attitude error caused by gyro bias and random walk noise is far less than** θ**, this term can be removed through a high-pass filter.**

Parameters Estimation Approach

The correlation function of $\tilde{Z}_{dcm}$ is given by

$$R_Z(\tau) = \left\langle \tilde{Z}_{dcm}(t), \tilde{Z}_{dcm}(t+\tau) \right\rangle = \left\langle \theta(t), \theta(t+\tau) \right\rangle$$

Recall that the correlation function of dynamic flexure $\theta(t)$, based on the second-order Gauss-Markov process assumption is

$$R_\theta(\tau) = \sigma^2 \exp\left(-\alpha|\tau|\right)\left(\cos\beta\tau + \frac{\alpha}{\beta}\sin\beta|\tau|\right)$$

Therefore, the parameters σ^2, α and β can be obtained from $R_Z(\tau)$.

Parameters Estimation Approach

● T-K Method

The T-K methods is widely applied in estimation of parameters for closely spaced sinusoidal signals in noise

$$y(n) = \sum_{l=1}^{M} a_l \exp\left[\left(-\alpha_l + j\beta_l\right)n\right] + q(n), n = 1, 2, \cdots, N$$

where M is the number of sinusoidal signals, N is the sample length, a_l is the amplitude, α_l is the damping factor and β_l is circular frequency.

The parameters α_l and β_l can be resolved by using T-K method. Then, substitute the estimate results α_l and β_l to above equation, and the magnitude a_l can be resolved by using the least square methods.

Parameters Estimation Approach

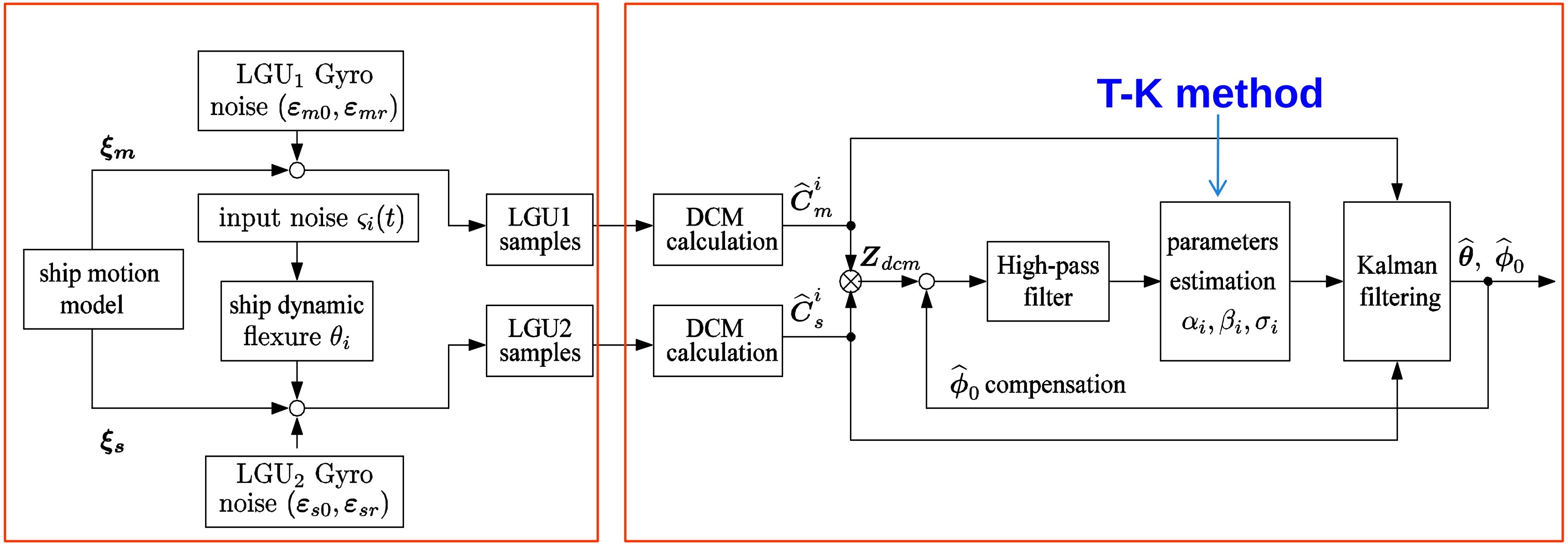
Parameters Estimation Procedure

- **Initialization**
  - **Calculate the DCMs of $\hat{C}_m^i$ and $\hat{C}_s^i$, derive Z_{dcm}**
  - **Compensate the $\hat{\phi}_0$ using course estimation results**
  - **Remove gyro errors through high-pass filter**
- **T-K Based Parameters Estimation**
  - **Calculate the correlation function $R_Z(\tau)$ of Z_{dcm}**
  - **Construct the T-K prediction function and evaluate the frequency $\beta/2\pi$ and damping factor α**
  - **Calculate the variance σ^2 using the least square algorithm**
- **KF Based Angular Deformation Measurement**

Simulation System

Gyro samples generation

Parameters estimation and KF based deformation measurement



Schematic diagram of gyro samples generation and dynamic flexure parameters estimation

Simulation System

The ship attitude can also be modeled as a second-order Gauss-Markov process, whose correlation function takes the form

$$R_{\xi_i}(\tau) = \sigma_{\xi_i}^2 e\,\mathrm{xp}\left(-\alpha_{\xi_i}|\tau|\right)\left(\cos\beta_{\xi_i}\tau + \frac{\alpha_{\xi_i}}{\beta_{\xi_i}}\sin\beta_{\xi_i}|\tau|\right)$$

Ship attitude parameters

	Magnitude σ_{ξ_i} (deg)	Frequency $\beta_{\xi_i}/2\pi$ (Hz)	Damping factor α_{ξ_i} (s^{-1})
Pitch	2.2	0.18	0.10
Roll	3.4	0.07	0.06
Yaw	0.8	0.05	0.12

Set according to experience (Magnitude)

Identified from experiment data (Frequency and Damping factor)

Simulation System

True dynamic flexure parameters

	Magnitude σ_i (mrad)	Frequency $\beta_i / 2\pi$ (Hz)	Damping factor α_i (s^{-1})
Pitch	0.40	0.19	0.13
Roll	0.68	0.17	0.11
Yaw	0.50	0.18	0.10

Set according to experience (Magnitude)

Identified from experiment data (Frequency, Damping factor)

In order to reflect actual measurement environment, we add Gaussian white noise with variance $\sigma_{\varsigma_i}^2$ in dynamic flexure signal. The SNR is defined by

$$SNR_i = 10\log_{10}\frac{\sigma_i^2}{\sigma_{\varsigma_i}^2}$$

Results and Analysis

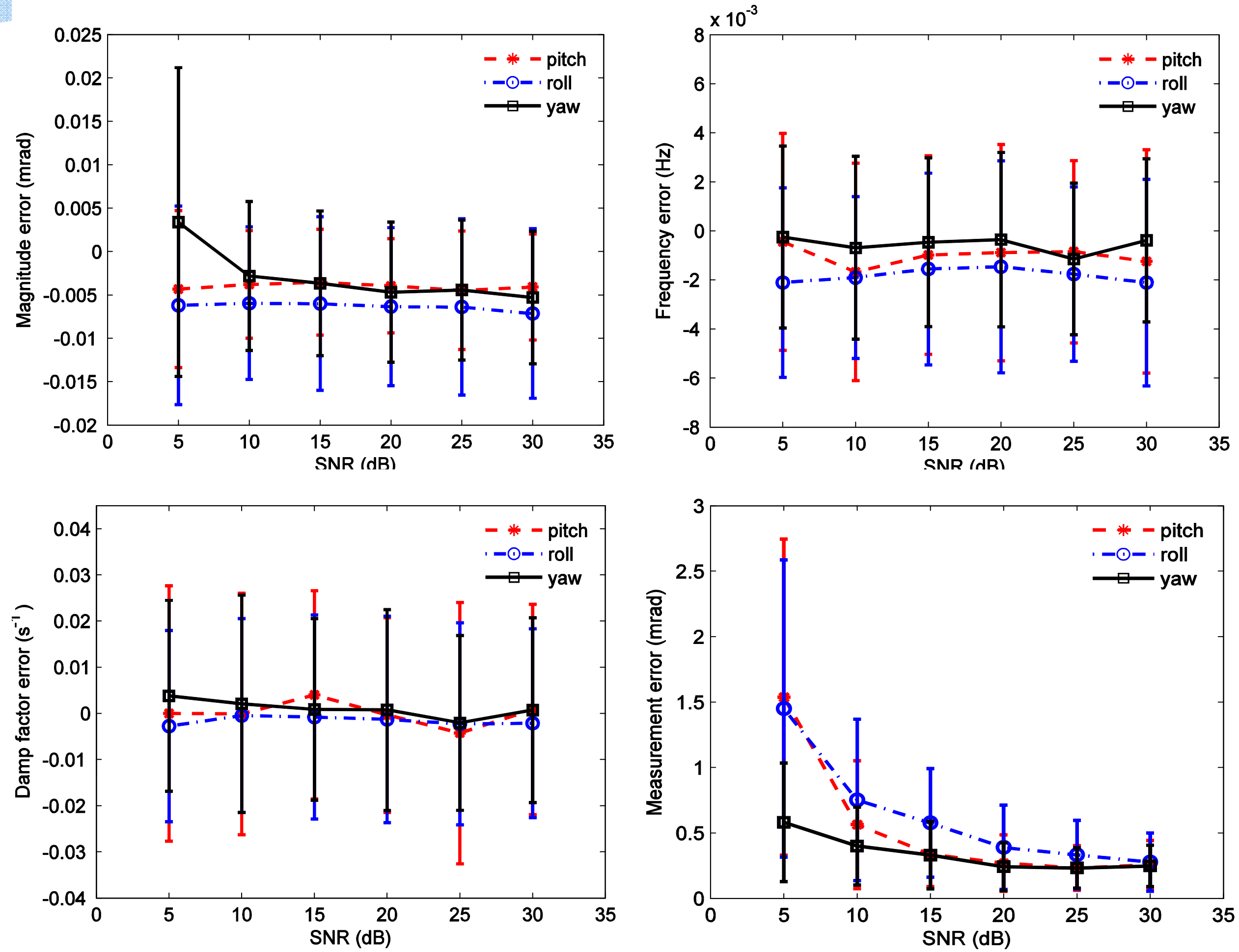
MEANS AND STANDARD DEVIATIONS OF THE ESTIMATED DYNAMIC FLEXURE PARAMETERS OBTAINED UNDER THE CONDITION OF $\sigma^2_{\varsigma_i} = 0$, GIVEN $T = 600$ s, $N = 20$ s, $L = 6$ s AND $M = 2$.

	Magnitude σ_i (mrad)	Frequency $\beta_i/2\pi$ (Hz)	Damping factor α_i (s^{-1})
Pitch	0.3950 (0.0064)	0.1892 (0.0041)	0.1272 (0.0252)
Roll	0.6722 (0.0089)	0.1685 (0.0039)	0.1054 (0.0188)
Yaw	0.4961 (0.0075)	0.1798 (0.0034)	0.1013 (0.0183)

PERFORMANCE OF THE KALMAN FILTER BASED SHIP ANGULAR DEFORMATION MEASUREMENT OBTAINED BASED ON THE DYNAMIC FLEXURE MODEL IDENTIFIED UNDER THE CONDITION OF $\sigma^2_{\varsigma_i} = 0$.

	Mean and standard deviation of true deformation angle (mrad)	Mean and standard deviation of KF estimated deformation angle (mrad)	Mean and standard deviation of KF based measurement error (mrad)
Pitch	3.4981 (0.4267)	3.5179 (0.5525)	0.2626 (0.2005)
Roll	3.4792 (0.7209)	3.5131 (0.7776)	0.3259 (0.2369)
Yaw	3.5027 (0.4840)	3.5483 (0.5626)	0.1944 (0.1382)

Results and Analysis



Mean estimate errors for dynamic flexure parameters magnitude σ^2, frequency $\beta/2\pi$ and damping factor α as well as measurement error with different SNR

Conclusions

- **we have developed an on-line dynamic flexure parameters estimation approach based on T-K method for KF based ship angular deformation measurement**

- **Compared with previous methods, the proposed method offers:**

  - **on-line estimation (not require *a priori* knowledge)**
  - **accurate estimation**
  - **robust to noise and work conditions**

Thank You For Your Attention