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# A large geometric distortion in the first photointermediate of rhodopsin, determined by double-quantum solid-state NMR

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Abstract Double-quantum magic-angle-spinning NMR experiments were performed on  $11,12^{-13}C_2$ -retinylidenerhodopsin under illumination at low temperature, in order to characterize torsional angle changes at the C11-C12 photoisomerization site. The sample was illuminated in the NMR rotor at low temperature (~ 120 K) in order to trap the primary photointermediate, bathorhodopsin. The NMR data are consistent with a strong torsional twist of the HCCH moiety at the isomerization site. Although the HCCH torsional twist was determined to be at least 40°, it was not possible to quantify it more closely. The presence of a strong twist is in agreement with previous Raman observations. The energetic implications of this geometric distortion are discussed.

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#### Introduction

Rhodopsin is the protein component of the light receptor in the retinal rod cells of the vertebrate eye and is responsible for vision under dim light. It is a 41 kDa membrane protein which consists of a single polypeptide, called opsin, and a 11-Z-retinylidene chromophore, derived by oxidation of vitamin A. Rhodopsin, a prototypical G-protein coupled receptor (GPCR) for signal transduction, passes through a series of photointermediates after light absorption, until the isomerized ligand splits from the opsin protein (Palczewski 2006; Wald 1968). Light sensitivity is provided by the 11-Z-retinylidene chromophore covalently bound to the Lys-296 residue of the protein by a protonated Schiff base (PSB) linkage (Fig. 1a). The signal transduction process is initiated by light absorption that leads to an ultrafast (200 fs) and highly selective isomerization of the chromophore from the initial 11-Z configuration to a distorted all-E configuration (Fig. 1a). The first stable photostate, bathorhodopsin, can be trapped at temperatures below 125 K (Palczewski 2006) which allows its structure and properties to be studied by low-temperature illumination of rhodopsin. Bathorhodopsin is an energetic molecule that stores about 2/3 of the absorbed photon energy (Palczewski 2006; Wald 1968). The mechanism for storing this large amount of energy, which corresponds to about  $134 \pm 12$  kJ mol<sup>-1</sup> (32  $\pm$  3 kcal/mol), is not yet completely known. Three different mechanisms have been proposed and widely discussed (Honig et al. 1979; Kukura et al. 2005; Yan et al. 2004; Birge et al. 1998; Nishimura et al. 1997a, b; Kandori and Maeda 1995; Ganter et al. 1988; Rath et al. 1998; Gascon et al. 2006; Schreiber et al. 2006; Rohrig et al. 2004; Schreiber and Buss 2003): electrostatic energy storage by charge separation between the protonated Schiff base and a counterion (most likely

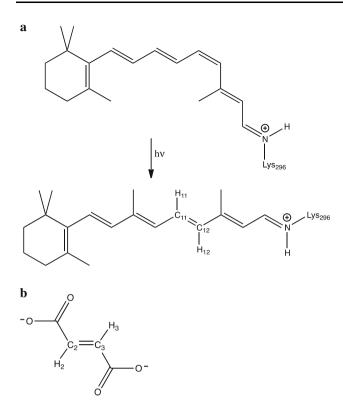


Fig. 1 a The retinylidene chromophore of rhodopsin and its photoinduced cis-trans isomerization. This work used samples labeled with <sup>13</sup>C at positions C11 and C12. b Molecular structure of the anion in  $2,3-^{13}C_2$ -diammonium-fumarate (DAF)

Glu113 or a more extended complex of ions); mechanical energy storage in the form of steric strain energy; and van der Waals interactions between the chromophore and the protein. The first model proposed in 1979 by Honig et al. (1979) considered the charge separation between the negatively charged counterion and the positively charged PSB as the main mechanism. Later Raman studies, however, suggested that intramolecular strain also gives a major contribution to the energy storage (Kukura et al. 2005; Yan et al. 2004). According to calculations by Birge et al. (Birge et al. 1998) about the 60 % of the stored energy can be attributed to strain and the rest of it to electrostatic effects. FT-IR spectroscopy studies (Nishimura et al. 1997a, b; Kandori and Maeda 1995; Ganter et al. 1988; Rath et al. 1998) seem to indicate that a rearrangement of the water network takes place after phoisomerization and this influences the electrostatic forces between the PSB and the counterion. A series of calculations using quantum mechanics/molecular mechanics (QM/MM) (Gascon et al. 2006; Schreiber et al. 2006), molecular dynamics (MD) (Rohrig et al. 2004), and density functional theory (DFT) (Schreiber and Buss 2003) have also been used to assess the relative importance of the three proposed contributions to the energy storage mechanism.

Solid-state NMR can contribute significantly to this debate by providing additional experimental data on the charge distribution and the geometry of the bathorhodopsin chromophore. For example, the chemical shifts of nuclear sites within the chromophore are sensitive to the charge distribution in the unsaturated retinylidene chain. In a previous paper (Concistrè et al. 2008), we used low-temperature (<120 K) in situ illumination of rhodopsin to isolate and trap bathorhodopsin, and performed doublequantum magic-angle-spinning NMR to isolate the <sup>13</sup>C NMR chromophore signals, allowing the <sup>13</sup>C chemical shifts in bathorhodopsin to be estimated unambiguously, for the first time. The chemical shift evidence suggests that the electrostatic interaction between the chromophore and the counterion is strongly involved in the energy storage mechanism of bathorhodopsin (Gansmüller et al. 2009). This conclusion was supported by the consistent downfield shifts of the odd-numbered carbon sites in the retinylidene chain, which correlate well with the red shift in the bathorhodopsin optical absorption maximum (Gansmüller et al. 2009). However, the same study showed an unusually large (9.4 ppm) downfield shift for the C10 resonance which is difficult to explain by charge delocalization effects (see Fig. 1a for the retinylidene carbon numbering scheme). This chemical shift anomaly suggests the simultaneous presence of a geometric distortion in the vicinity of the isomerization site (Gansmüller et al. 2009).

The solid-state NMR technique known as doublequantum heteronuclear local-field spectroscopy can provide direct estimation of the torsional angle in a H–C–C–H moiety (Feng et al. 1996). This paper reports the results of such an investigation on the H-C11-C12-H moiety in bathorhodopsin. These are the double bonded carbons where photo-isomerization takes place and where a distortion from planarity is most expected if a high degree of steric strain contributes to the storage of light energy. For this purpose rhodopsin was <sup>13</sup>C-labeled at positions C11 and C12 of the retinylidene chain.

The interpretation of the resulting NMR data is quite complicated due to a high degree of spectral overlap between the C11 and C12 resonances of bathorhodopsin and those of the rhodopsin molecules that failed to isomerize. Nevertheless, we were able to use a deconvolution technique to extract information on the H-C11-C12-H torsional angle, establishing a deviation from planarity of at least 40° in bathorhodopsin. These findings agree with previous Raman observations (Kukura et al. 2005; Yan et al. 2004). This strong geometric distortion implies that a significant part of the light energy, used to drive the subsequent protein conformational changes that activate rhodopsin, is stored as steric strain in the bathorhodopsin retinylidene chain.

### Materials and methods

# Samples

# Diammonium 2,3-<sup>13</sup> $C_2$ -fumarate

Diammonium  $2,3^{-13}C_2$ -fumarate (DAF, see Fig. 1b) was used to validate the double-quantum heteronuclear local field experiment and to provide a benchmark for comparison of the bathorhodopsin data. The HCCH torsional angle in this compound is known to be exactly  $180^{\circ}$  from the crystal structure (Hosomi et al. 1998). The sample of diammonium  $2,3^{-13}C_2$ -fumarate was purchased from Cambridge Isotopes (Andover, MA, US) and used without modification.

# $[11, 12^{-13}C_2]$ -retinylidene-rhodopsin

[11,12-<sup>13</sup>C2]-11-Z-retinal was prepared by enantioselective organic synthesis (Groesbeek and Lugtenburg 1992; Lai et al. 2006; McLean et al. 2011). The labeled 11-Z-retinal was incorporated into bovine opsin, isolated from fresh cattle eyes (de Grip et al. 1980). The sample was stored at -80 °C and handled under dim red light. The rhodopsin was reconstituted with natural membrane lipids, frozen with liquid nitrogen, ground into small particles, mixed with ~100 µm diameter glass beads to maximize the light penetration, and packed into a thin-wall zirconia magic-angle-spinning NMR rotor (4 mm outer-diameter). The characterization of the retinal and rhodopsin samples is described elsewhere (Concistrè et al. 2008).

# $[11, 12^{-13}C_2]$ -retinylidene-bathorhodopsin

About 30 % of the rhodopsin was converted into bathorhodopsin by illuminating the NMR rotor for 12 h with filtered light of wavelength 420 nm at a temperature below 120 K. The NMR probe and illumination conditions are described below.

Apparatus

### NMR probe

A custom-built 4 mm MAS NMR probe, designed to allow in situ magic-angle-spinning NMR experiments on an illuminated cold sample, was used. The gas lines were designed to minimize the temperature gradient between the cooling, spinning and bearing gases. Dry nitrogen gas was used for the journal bearings, turbine drive, and sample temperature control.

#### Illumination

Light was generated using two 250 W quartz lamps, filtered through cooled  $420 \pm 5$  nm interference filters, and conveyed into the sample region using 14 optical fibres (Concistrè et al. 2008, 2009). As described in Ref. (Concistrè et al. 2009), the use of the glass beads and the choice of illumination wavelength optimizes the yield of bathorhodopsin while minimizing the generation of the undesired isorhodopsin (9-Z) ground state.

The experimental apparatus and the procedures used for sample characterization, temperature control, temperature calibration, and illumination, are described in detail elsewhere (Concistrè et al. 2008).

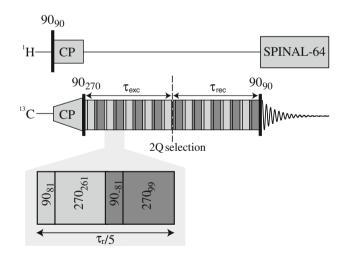
# Experimental procedures

#### NMR experiments

All NMR experiments were performed at a magnetic field of 9.4 T on a Varian Infinity + solid-state NMR spectrometer, using a spinning frequency of  $\omega_r/2\pi = 7,000$  Hz in the rhodopsin case and  $\omega_r/2\pi = 5,600$  Hz for the DAF. The spinning frequency stability was  $\pm$  50 Hz.

#### Pulse sequences

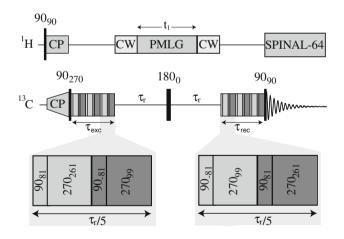
*Double-quantum*  ${}^{13}C$  spectroscopy The double-quantumfiltered dipolar recoupling pulse sequence used for the selective observation of  ${}^{13}C$  NMR signals from  ${}^{13}C_2$  pairs is shown in Fig. 2. Cross-polarization of  ${}^{1}H$  magnetization



**Fig. 2** Pulse sequence used for the double quantum filtered dipolar recoupling experiment.  $\tau_r$  is the rotor period,  $\tau_{exc}$  and  $\tau_{rec}$  are the double-quantum excitation and reconversion intervals, respectively. CP indicates a Cross-Polarization step while SPINAL-64 (Fung et al. 2000) is the decoupling scheme used during signal acquisition. The pulse flip angles and phases (in degrees), and the indicated timing, correspond to the symmetry R20<sup>9</sup><sub>2</sub>

to <sup>13</sup>C is followed by excitation of double-quantum <sup>13</sup>C coherences by a symmetry-based R20<sup>9</sup><sub>2</sub> recoupling sequence (Levitt 2002). The phases of the radiofrequency pulses are shown explicitly in Fig. 2. The double-quantum excitation and reconversion intervals ( $\tau_{exc}$  and  $\tau_{rec}$ , respectively) were both set equal to 380 µs to maximize the double-quantum efficiency. No radiofrequency field was applied on the <sup>1</sup>H channel during the R20<sup>9</sup><sub>2</sub> recoupling sequence since the high-power <sup>13</sup>C rf field (70 kHz in the present case) achieved sufficient heteronuclear decoupling (Marin-Montesinos et al. 2005). A SPINAL-64 (Fung et al. 2000) decoupling sequence was applied on the <sup>1</sup>H channel during detection of the <sup>13</sup>C free induction decay. Double-quantum filtering was achieved using a 16-step phase cycle (Levitt 2008).

2*Q*-HLF experiments The 2Q-HLF experiment for estimating the HCCH torsional angle is discussed in Ref. (Feng et al. 1996) and (Brinkmann 2001). The pulse sequence is shown in Fig. 3. The experiment involves the following steps: (i) a double-quantum state involving the two <sup>13</sup>C sites is prepared using cross-polarization followed by a double-quantum (2Q) homonuclear dipolar recoupling sequence of symmetry R20<sup>9</sup><sub>2</sub> (Levitt 2002); (ii) the 2Q <sup>13</sup>C<sub>2</sub> coherence evolves for one rotor period  $\tau_r = |2\pi/\omega_r|$ , where  $\omega_r/2\pi$  is the spinning frequency in Hz, followed by a  $\pi$ -pulse for refocusing the <sup>13</sup>C chemical shift evolution, and



**Fig. 3** The 2Q-HLF pulse sequence used for torsional angle measurements.  $\tau_r$  is the rotor period;  $\tau_{exc}$  and  $\tau_{rec}$  are the double-quantum excitation and reconversion intervals, respectively. A Phase-Modulated Lee-Goldburg (PMLG) scheme (Vinogradov et al. 1999, 2002) is used for homonuclear decoupling during  $t_1$  while continuous decoupling (CW) was used during the interval  $\tau_r - t_1$ . CP indicates Cross-Polarization and SPINAL-64 (Fung et al. 2000) is the decoupling scheme used during signal acquisition. The pulse flip angles and phases (in degrees), and indicated timing, correspond to the symmetries R20<sup>9</sup><sub>2</sub> (for double-quantum excitation) and R20<sup>-9</sup><sub>2</sub> (for double-quantum reconversion)

a second rotor period  $\tau_r$ . A proton homonuclear decoupling sequence of variable duration  $t_1$  is simultaneously applied during this interval (see below); (iii) the 2Q coherence is converted back into observable signal by a second recoupling sequence, with symmetry  $R20_2^{-9}$ . The change in sign of the winding number for the second recoupling sequence takes into account the phase inversion induced by the central  $\pi$  pulse. The  $\tau_{exc}$  and  $\tau_{rec}$  recoupling intervals were both set to 380 µs to maximize the double-quantum efficiency.

A Phase-Modulated-Lee-Goldburg (PMLG) homonuclear decoupling scheme (Vinogradov et al. 1999, 2002) was applied to remove proton-proton dipolar couplings during the variable evolution interval, which consists of two equal intervals  $t_1/2$ , one before and one after the <sup>13</sup>C  $\pi$ pulse. The duration of each the  $t_1/2$  half-intervals was incremented stepwise from 0 to a full rotor period. In practice we used a PMLG-5 pulse scheme that comprises ten radiofrequency pulses of flip angle  $\pi/2$  and equal duration  $\tau_p$  (Paul et al. 2009). For the DAF experiments, 8 increments were fitted into a single rotor period  $\tau_r = 178.6 \ \mu s$  (spinning speed 5,600 Hz) using the PMLG-5 pulse duration  $\tau_p = 2.55 \ \mu s$ . For the bathorhodopsin experiments, 7 increments were fitted into a rotor period  $\tau_r = 142.8 \ \mu s$  (spinning speed 7,000 Hz) using a PMLG-5 pulse duration of  $\tau_p = 2.38 \ \mu s$ . Unmodulated ("continuous-wave", CW) decoupling was applied on the proton channel during the two intervals  $\tau_{\rm r} - t_1/2$  in order to decouple the heteronuclear <sup>13</sup>C-<sup>1</sup>H and homonuclear <sup>1</sup>H–<sup>1</sup>H interactions.

# Simulations

Numerical simulations of the double-quantum signal as a function of the evolution interval  $t_1$  were performed using SIMPSON (Bak et al. 2000), assuming a regular geometry for the HCCH fragment [ $r_{CC} = 1.34$  Å (Feng et al. 1996);  $r_{CH} = 1.1$  Å;  $\theta_{CCH} = 120^{\circ}$ ]. The simulations involved the local system of two protons and two <sup>13</sup>C nuclei, including all dipolar couplings within the fourspin-1/2 system. The simulation parameters for the case of a HCCH torsional angle of  $\phi = 180^{\circ}$  are reported in Table 1 (for DAF) and Table 2 (for bathorhodopsin). The SIMPSON simulations did not include relaxation. Damping due to relaxation was added afterwards in a simplified way as explained below.

Simulations were repeated for a set of torsional angles  $\phi$  varying between 0 and 180° in 10° steps. The spin system parameters for torsional angles other than 180° were generated by varying  $\phi$  while keeping the molecular bond lengths and angles fixed, and deriving new sets of nuclear coordinates, from which the dipolar coupling tensors were calculated. All chemical shift tensors were kept fixed with

Chemical shift	$\delta^{\imath\sigma o}$ (ppm)	$\delta^{\mathrm{an}\imath\sigma o}$ (ppm)	η	$\substack{(\alpha_{PM}^{CS},\beta_{PM}^{CS},\gamma_{PM}^{CS})\\(^{\circ})}$
C2	0*	94 <sup>a</sup>	0.59 <sup>a</sup>	(-65, 102, 9) <sup>a</sup>
C3	0*	94 <sup>a</sup>	0.59 <sup>a</sup>	$(-65, -102, 9)^{a}$
H3	0*	0*	0*	$(0, 0, 0)^*$
H4	0*	0*	0*	$(0, 0, 0)^*$
Coupling	J (Hz)	b/(2πkH)	$(\alpha_{PM}^{DD}, \beta_{P}^{L})$	$(\gamma_{PM}^{DD}, \gamma_{PM}^{DD})$ (°)
C2–C3	68 <sup>a</sup>	$-3.350^{a}$	(0, 0, 0)	a
C2-H3	0*	$-3.293^{b}$	(-180,	27.1, -180) <sup>b</sup>
C2-H2	0*	$-22.698^{b}$	(-180,	120, 0) <sup>b</sup>
C3-H3	0*	$-22.698^{b}$	(-180,	60, -180) <sup>b</sup>
C3-H2	0*	$-3.293^{b}$	(-180,	153.9, 0) <sup>b</sup>
H2–H3	0*	-4.130 <sup>b</sup>	(-180,	141.7, 0) <sup>b</sup>
Other param	neters			
B <sub>0</sub> (T)		9.39		
$\omega_{\rm r}/(2\pi)$ (kHz)		5.6		
$\omega_{nut}^H/(2\pi)$ (kHz)		76.5		
$\omega_{nut}^c/(2\pi)$ (kHz)		71.2		
Crystal File		REP256		
$\gamma$ angles		20		

 Table 1
 Chemical shift, coupling and other parameters used in the SIMPSON simulations of DAF

 $\delta^{i\sigma o}$  is the isotropic chemical shift,  $\delta^{ani\sigma o}$ , the chemical shift anisotropy,  $\eta$  is the chemical shift biaxiality parameter and  $(\alpha_{PM}^{CS}, \beta_{PM}^{CS}, \gamma_{PM}^{CS})$  are the Euler angles that relate the principal axes of the chemical shift tensor to the molecular frame chose with is *z*-axis along the C2–C3 bond and its *y*-axis perpendicular to the HCCH plane. The isotropic chemical shifts are specified relative to the experimental carrier frequency. J is the indirect spin–spin coupling constant, b is the dipolar coupling constant (in rad s<sup>-1</sup>) and  $(\alpha_{PM}^{DD}, \beta_{PM}^{DD}, \gamma_{PM}^{DD})$  are the Euler angles that relate the principal axes of the dipolar coupling tensor to the molecular frame. B<sub>0</sub> is the strength of the magnetic field,  $\omega_r$  is the spinning frequency,  $\omega_{nut}^H$  is the nutation frequency on the proton channel and  $\omega_{nut}^{Cu}$  is the nutation frequency on the carbon-13 channel.\* Assumed. <sup>a</sup>Ref. (Carravetta et al. 2001). <sup>b</sup>values calculated for  $r_{CC} = 1.34$  Å (Feng et al. 1996),  $r_{CH} = 1.1$  Å and  $\theta_{CCH} = 120^{\circ}$ 

respect to the local molecular groups. A *Mathematica* program (Wolfram Research Inc 2010) was used to generate the nuclear coordinates as a function of  $\phi$  and to derive the Euler angle sets describing the tensor orientations.

The validity of the numerical simulations is limited by the uncertainties in some of the assumed parameters, such as the bond lengths, bond angles, and chemical shift tensors, and the effects of magnetic nuclei outside the local 4-spin system. Simulations show that the pulse sequences are robust with respect to reasonable deviations in the chemical shift tensors, so this source of uncertainty may be discounted. The influence of geometrical uncertainties is more significant and is discussed further below.

**Table 2** Chemical shift, coupling and other parameters used in SIMPSON simulations in the case of bathorhodospin, assuming perfect all-trans geometry ( $\phi = 180^{\circ}$ )

$(S, \gamma_{PM}^{CS})$ a a * *		
a * *		
*		
*		
o)		
$(\alpha_{PM}^{DD},\beta_{PM}^{DD},\gamma_{PM}^{DD})~(^{\circ})$		
$(0, 0, 0)^{a}$		
$(-180, 120, 0)^{b}$		
$(-180, 26.7, -180)^{b}$		
(-180, 153.3, 0) <sup>b</sup>		
) <sup>b</sup>		
)) <sup>b</sup>		
REP2000		

 $\delta^{i\sigma o}$  is the isotropic chemical shift,  $\delta^{ani\sigma o}$ , the chemical shift anisotropy,  $\eta$  is the chemical shift biaxiality and  $(\alpha_{PM}^{CS}, \beta_{PM}^{CS}, \gamma_{PM}^{CS})$  are the Euler angles that relate the principal axes of the chemical shift tensor to the molecular frame chose with is z-axis along the C11-C12 bond and its y-axis perpendicular to the HCCH plane. The isotropic chemical shifts are specified relative to the experimental carrier frequency. J is the indirect spin-spin coupling value (here neglected). b is the dipolar coupling constant (in units of rad  $s^{-1}$ ) and  $(\alpha_{PM}^{DD}, \beta_{PM}^{DD}, \gamma_{PM}^{DD})$  are the Euler angles that relate the principal axes of the dipolar coupling tensor to the molecular frame.  $B_0$  is the strength of the magnetic field,  $\omega_r$  is the spinning frequency,  $\omega_{nut}^H$  is the nutation frequency on the proton channel and  $\omega_{nut}^c$  is the nutation frequency on the carbon channel. <sup>+</sup>Ref. (Concistrè et al. 2008) \*Assumed. <sup>a</sup>Assumed equal to the rhodopsin case in Ref. (Carravetta et al. 2001). <sup>b</sup>values calculated assuming  $r_{CC} = 1.34$  Å (Feng et al. 1996),  $r_{CH} = 1.1$  Å and  $\theta_{CCH} = 120^{\circ}$ 

#### Peak amplitude estimation

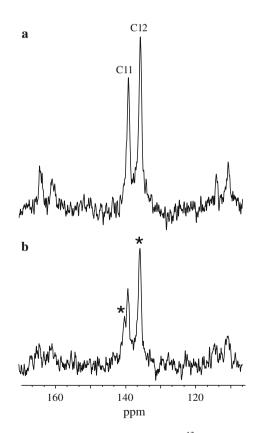
# Diammonium $2,3-{}^{13}C_2$ -fumarate

The determination of torsional angle requires the estimation of the double-quantum-filtered peak amplitudes for a series of evolution intervals  $t_1$ , and comparison with numerical simulations. In the case of DAF, the good signalto-noise ratio and the presence of a single resonance peak in the spectrum, allow the integrated spectral amplitudes  $I(t_1)$  to be used directly.

# $[11, 12^{-13}C_2]$ -retinylidene-bathorhodopsin

The estimation of the bathorhodopsin spectral amplitudes is considerably more challenging, since the signal-to-noise ratio is limited, even after considerable signal averaging, and there is a great deal of overlap between the C11 peaks of bathorhodopsin and non-isomerized rhodopsin. In the case of C12 the situation is even worse, with the peaks of the two species overlapping completely (see Fig. 4).

The following procedure was used to estimate the bathorhodopsin spectral amplitude as a function of  $t_1$ , and its confidence limits, in the presence of strong overlap with the rhodopsin peaks. Two different spectral masking functions were constructed, one for bathorhodopsin and one for rhodopsin, denoted  $S_B^M(\omega)$  and  $S_R^M(\omega)$  respectively. The masking functions for the species  $X \in (R, B)$  are defined to have unit integral, and consist of sums of Lorentzian peaks, with peak frequencies  $\omega_X^j$ , relative peak amplitudes  $a_X^j$  and peak halfwidths-at-half-height  $\lambda_X$  matching the observed <sup>13</sup>C peaks of the corresponding species in the  $t_1 = 0$  spectrum (including both the C11 and C12 centrebands)



**Fig. 4** Double quantum spectrum of  $[11,12^{-13}C_2]$ -retinilydene-rhodopsin **a** before and **b** after continuous illumination for 12 h at 420 nm and 120 Kelvin. The spectra are the sum of 6144 signal transients using a MAS frequency of 7.00  $\pm$  0.05 kHz. Both spectra were acquired at a sample temperature of 120 Kelvin. The positions of the bathorhodopsin peaks are indicated by *asterisks* 

$$S_X^M(\omega) = \sum_j \frac{a_X^j}{\lambda_X - i(\omega - \omega_X^j)}$$

where  $\sum_{i} a_x^j = 1$ 

The overlap matrix between the masking functions for bathorhodopsin and rhodopsin is calculated as follows:

$$\mathbf{L} = \begin{pmatrix} L_{BB} & L_{BR} \\ L_{RB} & L_{RR} \end{pmatrix}$$

where by definition

$$L_{BB} = L_{RR} = 1$$

and the overlap integrals are defined as follows:

$$L_{BR} = L_{RB}^* = \int_{-\infty}^{+\infty} S_B^M(\omega)^* S_R^M(\omega) d\omega$$

In the experiments described here, the overlap integrals were determined numerically to be  $L_{BR} = L_{RB}^* = 0.26$ .

Suppose that experimental spectra  $S^{\exp}(\omega, t_1)$  are obtained for each evolution interval  $t_1$ . A rough estimate of the spectral intensities for the two species is given by integrating the products of the spectral masking functions for the two species by the experimental spectra:

$$c_X(t_1) = \int_{-\infty}^{+\infty} S_X^M(\omega)^* S^{\exp}(\omega, t_1) d\omega$$

where  $X \in (R, B)$ . These rough intensity estimates may be assembled into a 2-component vector:

$$c(t_1) = \begin{pmatrix} c_B(t_1) \\ c_R(t_1) \end{pmatrix}$$

The true intensities of the B and R signals at time point  $t_1$  are estimated by applying the inverse of the overlap matrix to the vector  $\mathbf{c}(t_1)$ :

$$\mathbf{I}(t_1) = \begin{pmatrix} a_B(t_1) \\ a_R(t_1) \end{pmatrix} = L^{-1}c(t_1)$$

The elements  $I_B$  ( $t_1$ ) of the intensity vector provide estimates of the signal intensities, corrected for peak overlap, and with optimal use of the available signal. These signal intensity estimates are used in the analysis of the bathorhodopsin torsional angle.

Note that for complete peak overlap, the overlap matrix is singular and cannot be inverted. The confidence limits on  $I_B(t_1)$  were estimated by shifting the masking function  $S_B^M(\omega)$  to a signal-free region of the spectrum, obtaining an amplitude estimate, and repeating 50 times using a different signal-free spectral region each time. The confidence limits were set equal to the standard deviation  $\sigma$  of the 50 samples.

#### Torsional Angle Estimation

To obtain an estimate of the H–C–C–H torsional angle  $\phi$ , and its confidence limits, the experimental signal amplitudes  $I(t_1)$ were compared to numerical simulations as a function of torsional angle  $\phi$  obtained using the parameters given in Table 1 (for DAF) and Table 2 (for bathorhodopsin).

For each torsional angle value, the simulated amplitudes  $I^{sim}(\phi, t_1)$  were multiplied by a vertical scale factor and an exponential damping function in order to include the effects of enhanced spin dephasing occurring during the PMLG sequences:

$$I^{sim}(\phi, t_1)' = k_{fit}(\phi) \exp\{-\lambda_{fit}(\phi)t_1\} \times I^{sim}(\phi, t_1)$$

The parameters  $k_{fir}(\phi)$  and  $\lambda_{fir}(\phi)$  were optimized numerically at each torsional angle to minimize the mean-square deviation between the experimental set of points  $I(t_1)$  and the simulated best-fit points  $I^{sim}(\phi, t_1)'$ .

The  $\chi^2$  statistic was calculated for each torsional angle  $\phi$  by summing the mean-square-deviations between experiment and simulation for each  $t_1$  point, and dividing by the squared confidence limits  $\sigma_i^2$  on the signal intensities for each point:

$$\chi^{2} = \sum_{i} \frac{\left\{ I_{i}(t_{1}) - I^{sim}(\phi, t_{1})' \right\}^{2}}{\sigma^{2}}$$

A plot of  $\chi^2(\phi)$  against  $\phi$  displays a minimum value  $\chi^2_{\min}$ . The confidence limits on the torsional angle determination may be estimated from the region of torsional angles for which  $\chi^2(\phi)$  is less than or equal to  $\chi^2_{\min} + 1$  (Numerical Recipes in C. The art of scientific computing, 2nd Edn 1992).

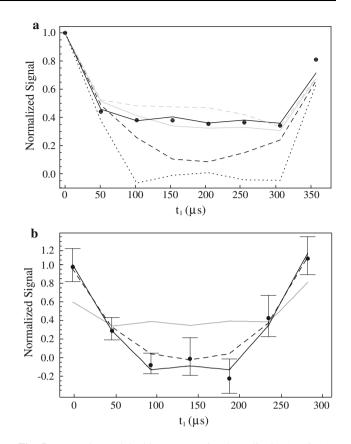
#### Results

Diammonium 2,3-<sup>13</sup>C<sub>2</sub>-fumarate

Figure 5a shows the signal intensities  $I(t_1)$  obtained for a sample of DAF using the pulse sequence in Fig. 3. Eight points were collected by equal increments of  $t_1$  from 0 to  $2\tau_r$ . Each point is the sum of 64 transients. The experimental points are well-fitted by numerical simulations using the parameters in Table 1 with  $\phi = 170^\circ$  or  $\phi = 175^\circ$  for the torsional angle HCCH.

The  $\chi^2$  analysis of DAF is reported in Fig. 6a. Only a narrow range of torsional angles  $\phi$  between 170° and 175° fall within one standard deviation from the minimum.

In practice the fumarate dianion is exactly planar ( $\phi = 180^{\circ}$ ), so there is a small discrepancy of about 5° between the determined torsional angle and the correct result. The same discrepancy has been noted before



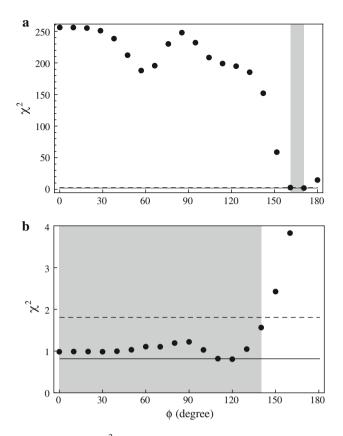
**Fig. 5** a Experimental double quantum signal amplitudes (*circles*) as a function of  $t_1$  obtained for DAF using the pulse sequence in Fig. 3. Lines represent numerical simulations with  $\phi$  equal to 0° (*dotted black*), 160° (*dashed black*), 170° (*solid grey*), 175° (*solid black*) and 180° (*dashed grey*). *Error bars* fall within the point size. **b** Experimental signal intensities (*circles*) and *error bars* as a function of  $t_1$  in the case of bathorhodopsin and compared with numerical simulations (*lines*) for  $\phi = 0^\circ$  (*solid black*),  $\phi = 140^\circ$  (*dashed black*) and  $\phi = 180^\circ$  (*solid grey*)

(Brinkmann 2001). Since the modulation curves are extremely sensitive in this range of  $\phi$ , the small discrepancy could be due to numerous factors, for example the presence of *rf* inhomogeneity, non-uniform cross-polarization, or the influence of remote spins outside the local H–C–C–H moiety (Brinkmann 2001). The influence of such factors, in any possible combination, is also visible in the incomplete refocusing observed at  $t_1 = 2 \tau_r$  (see Fig. 5). A precise explanation is not yet available.

#### Bathorhodopsin

#### Double-Quantum filtered experiment

Figure 4 shows DQ-filtered <sup>13</sup>C spectra of 11,12-<sup>13</sup>C<sub>2</sub>-retinylidene rhodopsin, acquired using the pulse sequence in Fig. 3, before (a) and after (b) illumination. Both spectra are the averages of 6144 signal transients. The leftmost peak on the top spectrum belongs to the C11 site of



**Fig. 6** Chi-square  $(\chi^2)$  values (calculated from Eq. 1) plotted versus the torsional angle  $\phi$  in the case of DAF (**a**) and bathorhodopsin (**b**). The *solid* and *dashed line* indicates the value of and +1, respectively Rough 68 % confidence limits on the parameter  $\phi$  may be estimated from the bounds of the region (The angles falling in that regions are *shaded in light grey*)

rhodopsin, whose chemical shift was determined to be  $\delta_{iso} = 141.4$  ppm (Creemers et al. 2002). The rightmost peak, at  $\delta_{iso} = 131.8$  ppm, is attributed to the C12 site (Creemers et al. 2002). The double-quantum-filtering efficiency was about 35 %.

After illumination, a new peak appears at 144.4 ppm. The evident decrease in intensity of the 141.4 ppm retinylidene-C11 peak in the spectrum acquired after sample illumination indicates that this new peak belongs to the retinylidene-C11 site of bathorhodopsin. The C12 peaks of rhodopsin and bathorhodopsin are not spectrally resolved since they have very close <sup>13</sup>C chemical shift (less than 1 ppm difference). The bathorhodopsin chemical shifts are consistent with previous experiments on different <sup>13</sup>C<sub>2</sub>-isotopomers (Concistrè et al. 2008).

# Double-Quantum Heteronuclear Local Field experiment

The pulse sequence in Fig. 3 was applied to the illuminated sample. Seven experimental points were acquired obtained by equal increments of  $t_1$  from 0 to  $2_r$ . Each point is the sum of 5632 transients.

Figure 5b shows the overlap-corrected experimental peak intensities for bathorhodopsin  $I_B(t_1)$  (filled circles) as a function of the evolution interval  $t_1$ . The error bars on the points indicate the confidence limits  $\sigma_i$ , which take into account the relatively poor signal-to-noise ratio as well as the strong overlap with the rhodopsin peaks.

The plotted lines join points  $I^{sim}$  ( $\phi$ ,  $t_1$ )' obtained by best-fit numerical simulations using values of 0° (solid black), 140° (dotted) and 180° (solid grey) for the H-C11-C12-H torsional angle. The experimental points are reasonably well fitted for a wide range of  $\phi$  values spanning from 0° to 140°, but the exact trans geometry ( $\phi = 180^\circ$ ) is clearly a poor fit.

The  $\chi^2$  plot shown in Fig. 6b makes the same point with more rigour. Although any torsional angle between 0° to 140° is consistent with the experimental data (as shown by the grey region), this result in principle implies a deviation from planarity of at least 40° around the C11 = C12 double bond in bathorhodopsin.

One word of caution must be sounded: The analysis, as formulated above, only considered structural models in which the H-C-C-H retains canonical bond angles and lengths as the torsional angle is changed. In addition, the H-C11-C12-H torsional angle may not always be directly related to the structurally more informative C10-C11-C12-C13 torsional angle. In practice, modulation curves corresponding to a 40° deviation from H–C–C–H planarity might also be consistent with a variety of other geometric distortions, including a strong change in bond angles, an asymmetry in the two H-C bond lengths, and so on. In addition, our analysis ignores vibrations and other molecular dynamic modes that could influence the data. A rigorous conclusion is that the H-C11-C12-H moiety in bathorhodopsin displays a strong deviation from the canonical geometry of a planar all-trans H-C-C-H group such as that found in fumarate. However the exact nature of the geometrical distortion cannot be determined from the NMR data alone.

### Discussion

The evidence of a strong geometric distortion at the C11-C12 site in bathorhodopsin strengthens the hypothesis that geometric strain contributes to the storage of a significant fraction of the absorbed photon energy. How much energy is stored this way?

An estimate of the amount of energy stored through geometric strain might be achieved by quantum-mechanical techniques. Although such a calculation is beyond the scope of this work, some brief comments may be appropriate. A crude potential energy surface calculation run on the isolated retinal chromophore showed that about 67 kJ mol<sup>-1</sup> (16 kcal/mol) are stored in a 40° twist about the C11-C12 bond. These calculations were run using Gaussian09 (Gaussian et al. 2009), optimizing the geometry of the all-trans-conformation using DFT theory (B3LYP functional, 6-31G\* basis set) and then changing the torsional angle to a new value (without re-optimization of the geometry) and calculating the energy for this new conformation. These calculations are clearly only indicative since the whole protein has been neglected. Nevertheless. more sophisticated quantum mechanical calculations do agree with cis-trans isomerization of the protein-bound chromophore leading to a highly strained all-trans-conformer in bathorhodopsin (Gascon et al. 2006; Bifone et al. 1997; Frutos et al. 2007; Polli et al. 2010; Schapiro et al. 2011; Andruniów et al. 2004) in general agreement with the results of this work and previous Raman studies (Kukura et al. 2005; Yan et al. 2004). In addition, two earlier reports (Gascon et al. 2006; Bifone et al. 1997) predict a torsional twist in the H–C11=C12–H moiety of approximately 20°, but subsequent ones (Frutos et al. 2007; Polli et al. 2010; Schapiro et al. 2011; Andruniów et al. 2004) all converge upon a twist of 35°-40°. On the other hand, they strongly disagree about the overall twist in the C10-C11=C12-C13 fragment. The estimated energy stored in the twisted H-C11=C12-H bond varies between ca. 11 kcal/mol to about 26 kcal/mol in these publications, in the same range as our calculations.

To summarize, our results do not provide sufficient information to estimate the amount of stored energy through geometrical distortion, except very roughly. The solid-state NMR data is consistent with H–C11–C12–H torsional angles ranging from 0° (the original *cis* conformation of rhodopsin, which corresponds to zero torsional strain) to a conformation twisted by 40° away from *trans*, which corresponds to a geometrical strain energy of around  $80 \pm 12 \text{ kJ mol}^{-1}$  (19 ± 3 kcal/mol). This upper limit represents 59 ± 13 % of the stored photon energy, which is  $32 \pm 3$  kcal/mol. More detailed computations are required to assess the strain energy more accurately.

# Conclusion

A solid state NMR 2Q-HLF experiment was calibrated on a simple model compound (DAF), which shows that in favorable cases the method is able to correctly yield torsional angles within  $\pm 5^{\circ}$  (Figs. 5a, 6a). This approach was subsequently applied to a complicated physiological system, thermally trapped bathorhodopsin, the first and very energetic photoproduct of the rod visual pigment rhodopsin, characterized by a poor S/N ratio and strongly overlapping resonances of rhodopsin and bathorhodopsin (Fig. 4). In such a case the method is less accurate, and we

had to apply a comprehensive extraction and simulation procedure to obtain tangible results. We could deduce that our data indicate for the central H-C11=C1-2H element of the retinylidene chromophore in bathorhodopsin a deviation of planarity of at least 40°. This result is in very good agreement with previous Raman observations (Kukura et al. 2005; Yan et al. 2004) and is supported by recent quantum-chemical calculations (Frutos et al. 2007; Polli et al. 2010; Schapiro et al. 2011; Andruniów et al. 2004). Such a torsional twist may be responsible for the storage of at least 16 kcal/mol out of the 32  $\pm$  3 kcal/mol of the total photon energy stored in this first photointermediate. Although an anomaly in the chemical shift value of C10 was at the source of this investigation, the data presented here cannot pin down the origin of the anomaly. However these data can be used as input for a new set of QM calculations that may resolve the issue. The technique here described is quite general and it could be applied to other photo-inducible systems, like, for example, the other intermediates of the rhodopsin photocycle, providing that they may be trapped thermally at temperatures compatible with magic-angle-spinning NMR.

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