

# Star-QAM Signaling Constellations for Spatial Modulation

Ping Yang, Yue Xiao, Bo Zhang, Shaoqian Li, *Senior Member, IEEE*,  
Mohammed El-Hajjar, *Member, IEEE*, and Lajos Hanzo, *Fellow, IEEE*

**Abstract**—The performance of spatial modulation (SM)-assisted multiple-input–multiple-output (MIMO) communication systems is highly dependent on the specific amplitude/phase modulation (APM) signal constellation adopted. In this paper, we conceive new star-quadrature amplitude modulation (star-QAM)-aided SM schemes. Our goal is to minimize the system’s average bit error probability (ABEP). More specifically, a new class of star-QAM constellations is introduced for SM, which is capable of flexibly adapting ring ratios of the amplitude levels. Then, under a specific MIMO configuration and a predetermined transmission rate, a simple and efficient ring-ratio optimization algorithm is proposed to minimize the ABEP. Moreover, to improve further the performance of our star-QAM-aided SM scheme, a diagonal precoding technique is proposed, and a low-complexity minimum-distance-based approach is conceived for extracting the precoding parameters. Our numerical results show that the proposed star-QAM-aided SM arrangement provides beneficial system performance improvements compared with the identical-throughput maximum–minimum distance (MMD) QAM and phase-shift keying (PSK) benchmarks. Moreover, our precoding scheme is capable of further improving the attainable system performance at a modest feedback requirement.

**Index Terms**—Constellation optimization, multiple-input–multiple-output (MIMO), spatial modulation (SM), star-quadrature amplitude modulation (star-QAM).

## I. INTRODUCTION

**S**patial Modulation (SM), which maps the information bits to two information-carrying entities, namely the antenna indexes and the combined amplitude/phase modulation (APM) constellation, constitutes a promising low-complexity multiple-input–multiple-output (MIMO) transmission technique [1]–[8]. In a conventional single-input–single-output (SISO) system, the Gray-coded maximum–minimum distance

(MMD) quadrature amplitude modulation (QAM) constellation minimizes the bit error rate (BER) [9], [10]. However, the advantage of MMD-QAM may be eroded in SM-MIMO systems [11]. This is due to the fact that the BER performance of SM-MIMO systems is jointly determined by the spatial signal (i.e., antenna indexes), by the classic APM constellation, and by their interaction [11]–[18].

Recently, the effects of APM schemes on the performance of SM have been investigated in [11], [14], and [18]. More specifically, in [11], the performance of SM systems relying both on conventional QAM and PSK modulation was studied, demonstrating that, in some MIMO setups, the PSK-modulated SM scheme may outperform the identical-throughput MMD-QAM-aided SM scheme. In [18], the dispersion matrices and the signal constellations were jointly optimized for a near-capacity irregular precoded space–time shift keying (STSK) system, which includes SM as a special case and strikes a flexible rate–diversity tradeoff. It was also shown in [14] that the star-QAM-aided STSK scheme outperforms its MMD-based square-QAM-aided counterpart. This observation may be also valid for SM systems [11]. The aforementioned results indicated that the performance of SM is highly dependent on the specific APM adopted; hence, a suitable APM scheme has to be designed for this hybrid modulation scheme.

On the other hand, star-QAM constitutes a special case of circular amplitude- and phase-shift keying, which is capable of outperforming the classic square-QAM constellation in peak-power-limited systems [19]. Hence, it has been adopted in most of the recent satellite communication standards, such as in the Digital Video Broadcast System (DVB) S2, DVB-SH, and the Internet Protocol over Satellite and Advanced Broadcasting System via Satellite [19]. The star-QAM constellation is composed of multiple concentric circles, and it was shown to be beneficial in the context of STSK systems. Hence, star-QAM may be an attractive APM candidate for SM-MIMO. However, the constellations’ optimization has not been carried out for star-QAM-aided SM.

Moreover, to increase the robustness of the SM-MIMO system, limited-feedback-aided link adaptation schemes have been proposed in [20]–[26]. For example, in [20], an opportunistic power-allocation (PA) scheme was conceived for achieving a beneficial transmit diversity gain in SM-MIMO systems. In [21], a beamforming codebook was designed for optimizing the coding gain of SM-MIMO based on the knowledge of the channel envelope’s spatial correlation. Recently, an adaptive closed-loop-aided method was invoked for providing both diversity and coding gains in the context of space-shift keying (SSK)[22],

Manuscript received July 27, 2013; revised December 26, 2013; accepted February 8, 2014. This work was supported in part by the European Research Council under an Advanced Fellow Grant, by the National Science Foundation of China under Grant 61101101, by the Foundation Project of the National Key Laboratory of Science and Technology on Communications under Grant 9140C020404120C0201, and by the Key Laboratory of Universal Wireless Communications, Beijing University of Posts and Telecommunications, Chinese Ministry of Education, under Grant KFKT-2012102. The review of this paper was coordinated by Dr. G. Bauch.

P. Yang and Y. Xiao are with the National Key Laboratory of Science and Technology on Communications, University of Electronic Science and Technology of China, Chengdu 611731, China (e-mail: yplxw@163.com).

B. Zhang, S. Li, M. El-Hajjar, and L. Hanzo are with the School of Electronics and Computer Science, University of Southampton, Southampton SO17 1BJ, U.K. (e-mail: bz2g10@ecs.soton.ac.uk; lsq@uestc.edu.cn; meh@ecs.soton.ac.uk; lh@ecs.soton.ac.uk).

Color versions of one or more of the figures in this paper are available online at <http://ieeexplore.ieee.org>.

Digital Object Identifier 10.1109/TVT.2014.2306986

which is a special case of SM. However, the scheme proposed for SSK may not be directly applicable to the conventional SM scheme. Moreover, ASM-MIMO architectures relying on different combinations of modulation schemes were proposed in [24], which aimed for maximizing the channel capacity at a predefined target BER, rather than for minimizing the BER. In contrast, in [25] and [26], a transmit precoding (TPC) technique was used for improving the modulated signal design for SM. However, this technique may only be suitable for a new class of SM relying on a single-receiver antenna. For the conventional SM, we proposed a near-instantaneously adaptive-modulation-aided scheme for minimizing the BER [7], which was termed adaptive SM (ASM). Then, we further generalized this paper in [12] and [15], where the implementation complexity of ASM was considerably reduced. However, ASM typically transmits a different number of bits in the different-quality time slots, which may be inconvenient in fixed-rate applications and potentially leads to error propagation in the case of ASM-mode signaling errors.

Against this background, the novel contributions of this paper are threefold.

- We introduced the class of star-QAM constellations [27], which is capable of flexibly adapting the ring ratios, hence subsuming classic PSK as a special case. Alternatively, if the ring ratio is appropriately selected, the proposed star-QAM is capable of achieving almost the same Euclidean distance (ED) as the MMD-based QAM.
- Given a specific MIMO configuration and a predetermined transmission rate, a low-complexity yet efficient optimization algorithm is proposed to minimize the average bit error probability (ABEP) of SM-MIMO systems, where the effects of both the antenna index, as well as of the APM signal and their interaction, are jointly considered. Only the optimal ring ratios of star-QAM constellation have to be found by the optimization algorithm.
- We introduce a new TPC scheme for star-QAM-aided SM-MIMO systems, which further improves the performance. To retain the benefits of SM, such as its low-complexity single-stream detector and its single RF chain, we design its TPC matrix  $\mathbf{P}$  to be diagonal. We demonstrate that this precoded scheme and the ASM schemes of [12] and [15] are capable of exploiting the same degrees of freedom as that offered by the classic SM-MIMO for maximizing the free distance (FD). However, our TPC scheme assigns the same number of bits to each time slot; hence, it is capable of avoiding the potential error propagation effects of ASM encountered in the case of ASM-mode signaling errors. Our simulation results show that the proposed TPC scheme considerably improves the system's performance compared with the conventional star-QAM-aided SM, the PA-aided SM, and ASM arrangements.

The remainder of this paper is organized as follows. In Section II, we conceive a signaling constellation optimization method for star-QAM-aided SM and elaborate both on the choice of our optimization criterion and on the corresponding optimization algorithm. In Section III, we propose a new TPC scheme for enhancing the performance of the star-QAM-aided

SM. Our numerical analysis is carried out in Section IV. Finally, our conclusions are presented in Section V.

## II. SIGNALING CONSTELLATION OPTIMIZATION

### A. Performance Metric and Star-QAM Constellation

Consider a flat-fading MIMO channel associated with  $N_t$  transmit antennas (TAs) and  $N_r$  receive antennas. The  $(N_t \times 1)$ -element transmit symbol vector  $\mathbf{x}$  is assumed to satisfy  $E[\mathbf{x}\mathbf{x}^H] = \mathbf{I}_{N_t}$ , where  $\mathbf{I}_{N_t}$  denotes an  $(N_t \times N_t)$ -element identity matrix. Then, the transmitted SM symbol  $\mathbf{x} \in \mathbb{C}^{N_t \times 1}$  is given as  $\mathbf{x} = s_l^n \mathbf{e}_n$  [21], where  $s_l^n$  is the complex-valued symbol of the APM scheme employed at the  $n$ th TA. For example,  $L$ -PSK/QAM is associated with  $m_{\text{APM}} = \log_2(L)$  input bits, whereas  $\mathbf{e}_n (1 \leq n \leq N_t)$  is selected from the  $N_t$ -dimensional standard basis vectors (i.e.,  $\mathbf{e}_1 = [1, 0, \dots, 0]^T$ ), according to  $\log_2(N_t)$  input bits. The corresponding received signal is given by

$$\mathbf{y} = \mathbf{H}\mathbf{x} + \mathbf{n} = \mathbf{h}_n s_l^n + \mathbf{n} \quad (1)$$

where  $\mathbf{H}$  is an  $(N_r \times N_t)$ -element channel matrix,  $\mathbf{h}_n$  is the  $n$ th column of  $\mathbf{H}$ , and the elements of the  $N_r$ -dimensional noise vector  $\mathbf{n}$  are Gaussian random variables obeying  $\mathcal{CN}(0, N_0)$ .

In [11], an improved union bound partitions the ABEP expression of SM-MIMO systems into three terms: the  $P_{\text{spatial}}$  term related to the TA index, the  $P_{\text{signal}}$  term related to the APM signals, and the joint term  $P_{\text{joint}}$ , which depends on both the TA index and on the APM signals. This bound is formulated as

$$P_{\text{SM}}(\rho) \leq P_{\text{spatial}}(\rho) + P_{\text{signal}}(\rho) + P_{\text{joint}}(\rho). \quad (2)$$

This improved union bound is more accurate than the conventional union-bound-based methods, hence facilitating a deeper understanding of the joint impact of spatial and APM signals, as illustrated in [11]. We focus our attention on the system's performance for transmission over i.i.d. Rayleigh fading channels, which may be readily extended to the Nakagami- $m$  fading model of [11]. Let us assume that  $\rho$  is the average SNR, whereas  $x_l$  and  $x_i$  represent two different APM constellation points, with their modulus values being given as  $\beta_l$  and  $\beta_i$ , respectively. Then, we have

$$P_{\text{signal}}(\rho) = \frac{\log_2(L)}{\log_2(N_t \cdot L)} P_{\text{APM}}(\rho) \quad (3)$$

$$P_{\text{spatial}}(\rho) = \frac{\log_2(N_t) N_t}{2L \log_2(N_t \cdot L)} \sum_{l=1}^L \mathcal{F}(\rho \beta_l^2) \quad (4)$$

$$P_{\text{joint}}(\rho) = A \sum_{l=1}^L \sum_{i \neq l=1}^L \left[ B + C D_H(x_l \rightarrow x_i) \right] \times \mathcal{F}\left(\frac{\rho}{2} (\beta_l^2 + \beta_i^2)\right). \quad (5)$$

Here,  $P_{\text{APM}}(\rho)$  represents the error probability of conventional  $L$ -APM, which depends on the ED of the constellation points of APM, whereas  $D_H(x_l \rightarrow x_i)$  is the Hamming distance between signals  $x_l$  and  $x_i$ . Here,  $A = 1/L \log(N_t \cdot L)$ ,  $B = N_t \log(N_t)/2$ , and  $C = (N_t - 1)$  are constants for a fixed

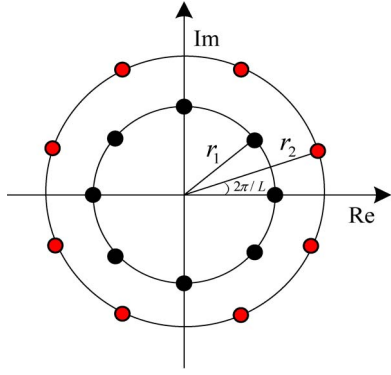


Fig. 1. Complex signal constellation of 16-star-QAM. The symbols are evenly distributed on two rings and the phase differences between the neighboring symbols on the same ring are equal.

MIMO setup. Moreover, the function  $\mathcal{F}(\varepsilon)$  in (4) and (5) is the pairwise error probability function [11], which is given by

$$\mathcal{F}(\varepsilon) = \gamma(\varepsilon)^{N_r} \sum_{n=0}^{N_r-1} \binom{N_r-1+n}{n} [1 - \gamma(\varepsilon)]^n \quad (6)$$

where we have  $\gamma(\varepsilon) \triangleq (1/2)(1 - \sqrt{(\varepsilon/2 + \varepsilon)})$ . Note that the ABEP bound of (2) was proposed for the general family of APM schemes, which contains not only the conventional PSK but also the generic rectangular nonsquare-QAM schemes and the square-QAM schemes. Moreover, since  $P_{\text{signal}}$  is available in closed form for conventional APM modulation schemes, the bound of (2) is more accurate than the conventional results of [21].

As indicated in (3)–(5),  $P_{\text{signal}}$  mainly depends on the minimum ED  $d_{\min}$  of the APM constellation points, whereas  $P_{\text{joint}}$  and  $P_{\text{spatial}}$  mainly depend on the modulus values  $\beta_l$  ( $l = 1, \dots, L$ ) of the APM constellation points.

Note that the modulus values  $\beta_l$  are represented by the Frobenius norms of the APM constellation points. These results suggested that, for jointly minimizing  $P_{\text{signal}}$ ,  $P_{\text{joint}}$ , and  $P_{\text{spatial}}$ , we can focus our attention on the design of  $d_{\min}$  and on the  $\beta_l$  parameters of APM.

To make the choice of the APM parameters  $d_{\min}$  and  $\beta_l$  as flexible as possible, we consider a class of star-QAM constellations, which subsumes the classic PSK as a special case but may also be configured for maximizing the minimum ED of the constellation by appropriately adjusting the ring ratios of the amplitude levels. For simplicity, we consider the example of a twin-ring 16-star-QAM constellation having a ring ratio of  $\alpha = r_2/r_1$ , as shown in Fig. 1. The symbols are evenly distributed on the two rings, and the phase differences between the neighboring symbols on the same ring are equal. Unlike the conventional twin-ring star-QAM constellation [19], [28], the constellation points on the outer circle of our proposed star-QAM constellation are rotated by  $2\pi/L$  degrees compared with the corresponding constellation points on the inner circle [27]. Hence, again, the conventional PSK constitutes an integral part of our star-QAM scheme, which is associated with  $\alpha = 1$ . Table I summarizes the minimum EDs  $d_{\min}$  between the constellation points for different APM schemes. It is found that this star-QAM scheme is capable of achieving almost the same

TABLE I  
MINIMUM ED BETWEEN THE CONSTELLATION  
POINTS FOR DIFFERENT APM SCHEMES

Modulation order	2	4 (MMD)	8 ([9])	16 (MMD)	32 ([9])
PSK	2	$\sqrt{2}$	0.7654	0.3902	0.1960
QAM	-	$\sqrt{2}$	0.8165	0.6325	0.4082
Proposed star-QAM	2	$\sqrt{2}$	0.9134	0.5737	0.3952

minimum ED as the MMD-based QAM. Note that, although this twin-ring star-QAM constellation has been indeed applied for noncoherent detection [27], it has not been considered whether this constellation can be directly applied to SM for achieving performance improvements.

The aforementioned twin-ring philosophy of Fig. 1 may be readily extended to multiple-ring star-QAM. The reasons for considering twin-ring star-QAM in our paper are the following.

- It is an attractive APM modulation candidate for SM, exhibiting a high performance at low detection complexity compared with conventional QAM schemes, as detailed in [13]–[15].
- It can be flexibly designed for different  $d_{\min}$  and  $\beta_l$  ( $l = 1, \dots, L$ ) combinations, which is achieved by simply adjusting a single parameter  $\alpha$ , whereas  $\beta_l$  can assume two values because only two rings are considered.
- The ABEP of star-QAM, which is related to the  $P_{\text{spatial}}$  term of (3), has been documented in [28] and [29].

## B. Optimization Criteria and Optimization Algorithm

Observe in Fig. 1 that there are numerous options for the parameter  $\alpha$  of the star-QAM constellation, for a given MIMO setup, specified by the total number of bits per symbol  $m_{\text{all}}$ , the  $(N_r \times N_t)$  configuration of transceiver, and the number of modulation level  $L$ . The goal of star-QAM-aided signaling constellation optimization is to find the specific ring ratio  $\alpha$ , which minimizes the ABEP of the SM-MIMO of (2). Note that, although the term  $P_{\text{SM}}(\rho)$  in (2) cannot be directly represented by parameter  $\alpha$ , it varies as a function of  $\alpha$ , which may be formulated as  $P_{\text{SM}}(\rho, \alpha)$ . Following the aforementioned approach, we formulated this optimization problem as

$$\begin{cases} \alpha^* = \min_{\alpha} P_{\text{SM}}(\rho, \alpha) \\ \text{s.t. } \alpha \geq 1 \end{cases} \quad (7)$$

which may be a convex one for a fixed SNR value  $\rho$ , as indicated in Fig. 4. However, deriving the closed-form solution of (7) remains an open challenge since the expression of  $P_{\text{SM}}(\rho, \alpha)$  depends both on the specific APM constellation and on the particular MIMO setup [19], and since the expressions of  $P_{\text{signal}}$ ,  $P_{\text{joint}}$  and  $P_{\text{spatial}}$  in (3)–(5) are complex. Hence, a numerical search is adopted.

Our optimization algorithm conceived for finding the ring ratio is summarized as follows.

Step 1: Initialize the values of  $N_r$ ,  $N_t$ ,  $m_{\text{all}}$ ,  $L$ , and the SNR value  $\rho$ . Set the iteration step size to  $\Delta\alpha = 0.1$  and the number of iterations to  $n = 1$ . The choice of  $\Delta\alpha$  is flexible, and a lower value of  $\Delta\alpha$  may lead to a better performance. We then set the search area of  $\alpha$  to  $1 \leq \alpha \leq U_\alpha$  and the performance metric to  $P_{\text{iter}}(n) = 0$ .



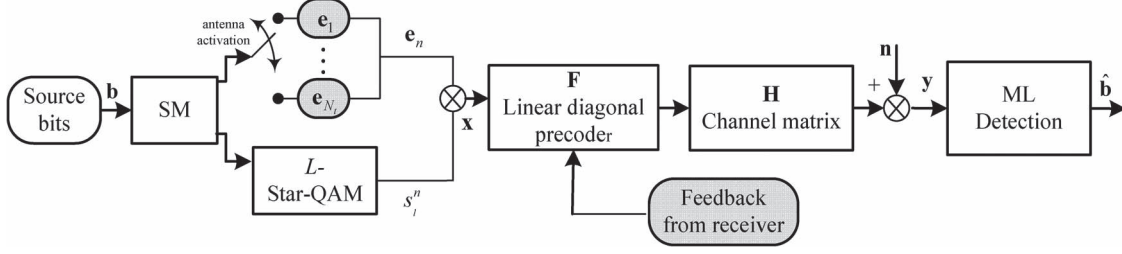


Fig. 2. System model of the diagonal-precoding-assisted star-QAM-aided SM scheme.

Step 2: While  $\alpha \leq U_\alpha$ , let  $\Delta\hat{\alpha} = \min\{\Delta\hat{\alpha}, U_\alpha - \alpha\}$ , and calculate the probabilities of  $P_{\text{signal}}$ ,  $P_{\text{joint}}$ , and  $P_{\text{spatial}}$  by using (3)–(5) associated with  $\alpha$ . Then, let  $P_{\text{iter}}(n) = P_{\text{SM}}(\rho)$  using (2), and set  $\alpha = \alpha + \Delta\hat{\alpha}$  and  $n = n + 1$ .  
 Step 3: Find the index  $n^* = \min_n\{P_{\text{iter}}(n)\}$  to achieve the optimal ring ratio of  $\alpha^* = 1 + (n^* - 1)\Delta\hat{\alpha}$ .

In the aforementioned optimization algorithm, we have to choose an appropriate  $U_\alpha$  to promptly find the optimal  $\alpha^*$ . More explicitly, an excessively low value of  $U_\alpha$  may lead to missing the optimal solution, whereas an excessively high value of  $U_\alpha$  imposes excessive computational complexity on the optimization process. Hence, we will show in Section III that  $U_\alpha = 3$  is a beneficial choice for promptly approaching the optimal results. Moreover, the optimum ring ratio  $\alpha^*$  is a function of the SNR. However, we will show that the optimum ratio approaches its asymptotic optimum as the SNR increases.

### III. PROPOSED DIAGONAL PRECODING FOR

#### STAR-QUADRATURE AMPLITUDE MODULATION-AIDED SPATIAL MODULATION

Since the performance of the optimum maximum-likelihood (ML) receiver depends on the FD of the received signal constellation [30], we propose a new TPC based on maximizing the FD for the family of star-QAM-aided SM-MIMO systems, when limited channel state information is available at the transmitter. Since the FD is increased by the TPC algorithm, the proposed scheme is expected to provide a beneficial system performance improvement. To retain all the single-RF-related benefits of SM, we design the TPC matrix  $\mathbf{P}$  to be diagonal. The system model of the diagonal-TPC-assisted star-QAM-aided SM scheme is shown in Fig. 2. To identify the specific TPC parameters, which are capable of maximizing the FD, we propose a low-complexity TPC design algorithm. We will demonstrate that as few as two elements of the diagonal TPC matrix have to be fed back to the transmitter, regardless of  $N_t$ .

##### A. TPC Design Criterion

To construct a TPC for star-QAM-aided SM-MIMO systems, we can rewrite the system model of (1) as

$$\mathbf{y} = \mathbf{H}\mathbf{P}\mathbf{x} + \mathbf{n} \quad (8)$$

where  $\mathbf{P}$  denotes the diagonal TPC matrix, which can be represented as

$$\mathbf{P} = \text{diag}\{p_1, \dots, p_n, \dots, p_{N_t}\} \quad (9)$$

where  $p_n$  controls the channel gain associated with  $x_n$ . Here, we let  $\sum_{n=1}^{N_t} |p_n|^2 = N_t$  for normalizing the transmit power. Note that the introduction of TPC in SM does not affect the advantages of SM, such as the avoidance of the interantenna interference and the reliance on a single RF chain, because the precoded transmit vector  $\mathbf{P}\mathbf{x}$  includes only a single nonzero component; hence, only a single TA is activated in each time slot, as indicated in (8).

Numerous techniques may be invoked for constructing the TPC  $\mathbf{P}$  [21], [25]. In this paper, similar to the precoding methods conceived for the orthogonalized spatial multiplexing of [31], we decompose  $\mathbf{P}$  as

$$\mathbf{P} = \bar{\mathbf{P}}\mathbf{\Theta} = \text{diag}\{\bar{p}_1 e^{j\theta_1}, \dots, \bar{p}_n e^{j\theta_n}, \dots, \bar{p}_{N_t} e^{j\theta_{N_t}}\} \quad (10)$$

where  $\bar{\mathbf{P}} = \text{diag}\{\bar{p}_1, \dots, \bar{p}_n, \dots, \bar{p}_{N_t}\}$  represents the PA matrix, whereas  $\mathbf{\Theta} = \text{diag}\{e^{j\theta_1}, \dots, e^{j\theta_n}, \dots, e^{j\theta_{N_t}}\}$  is the phase rotation matrix. The FD between the constellation points at the receiver is defined as

$$\begin{aligned} d_{\min}(\mathbf{H}, \mathbf{P}) &= \min_{\substack{\mathbf{x}_i, \mathbf{x}_j \in \mathbb{X}, \\ \mathbf{x}_i \neq \mathbf{x}_j}} \|\mathbf{H}\mathbf{P}(\mathbf{x}_i - \mathbf{x}_j)\|_F \\ &= \min_{\mathbf{e}_{ij} \in \mathbb{E}} \|\mathbf{H}\bar{\mathbf{P}}\mathbf{\Theta}\mathbf{e}_{ij}\|_F \end{aligned} \quad (11)$$

where  $\mathbb{X}$  is the set of all legitimate transmit symbols,  $\mathbf{e}_{ij} = \mathbf{x}_i - \mathbf{x}_j$ ,  $i \neq j$  denotes the error vector, and  $\mathbb{E}$  is a set of error vectors. Then, we design the TPC  $\mathbf{P}$  by maximizing the FD with the aid of the following criterion:

$$\begin{cases} \mathbf{P}_{\text{opt}} = \arg \max_{\mathbf{P}} d_{\min}(\mathbf{H}, \mathbf{P}) \\ \text{s.t.} \quad \sum_{n=1}^{N_t} |p_n|^2 = N_t; \quad p_n \in C; \\ \quad \theta_n \in (0, 2\pi]; \quad n = 1, \dots, N_t. \end{cases} \quad (12)$$

Note that, since the attainable performance of the optimum single-stream ML receiver depends on the FD of the received signal constellation [30], the maximization of the FD directly reduces the probability of error.<sup>1</sup> Let  $\mathbf{x}_i = s_l^i \mathbf{e}_i$  and  $\mathbf{x}_j = s_k^j \mathbf{e}_j$  denote two different transmit symbols, whereas  $s_l^i$  and  $s_k^j$  denote the constellation points  $l$  and  $k$  represented by the  $i$ th and  $j$ th antennas, respectively. Then, the FD of (11) can be represented as (13), where  $\phi = \angle((s_l^i)^* s_k^j) = -\angle(s_l^i (s_k^j)^*)$ . In

<sup>1</sup>Because the conventional PSK-and-QAM-aided SM scheme's performance is worse than that of the proposed star-QAM-aided SM, we only invoked the TPC algorithm for the star-QAM-aided SM for the sake of achieving further performance improvements. However, it is worth noting that the proposed TPC algorithm is also suitable for SM in conjunction with both conventional PSK and QAM schemes.

331 the ASM scheme of [7], only the APM modulation orders to  
 332 be used by the transmitter are adapted, i.e., only the elements  
 333  $|s_l^i|$ ,  $|s_k^j|$ , and  $\phi$  of (13), shown at the bottom of the page, are  
 334 dynamically adapted to the channel conditions, and the legit-  
 335 imate values of these elements are selected from the discrete  
 336 set depending on the modulation order set utilized. By contrast,  
 337 our proposed scheme adjusts all the TPC elements  $|p_i|$ ,  $|p_j|$ ,  
 338  $\theta_i$ , and  $\theta_j$  of (13) for maximizing the FD  $d_{\min}(\mathbf{H}, \mathbf{P})$ , whose  
 339 legitimate values are drawn from the real-valued number field.  
 340 Based on these observations and on (13), the proposed scheme  
 341 and the ASM scheme may exploit the same degrees of freedom  
 342 as that offered by the SM-MIMO in terms of maximizing the  
 343 FD. However, unlike the ASM scheme of [7] and [15], our  
 344 proposed scheme assigns the same number of bits to each time  
 345 slot; hence, the potential error propagation effects experienced  
 346 in ASM are avoided.

### 347 B. Low-Complexity TPC Design Algorithm

348 To identify the specific TPC matrix  $\mathbf{P}$ , which is capable of  
 349 maximizing the FD, we have to determine all the  $N_t$  parameters  
 350  $p_n (n = 1, \dots, N_t)$ . Since it may become excessively complex  
 351 to jointly optimize these  $N_t$  parameters in the complex-valued  
 352 field, we propose a low-complexity precoder design algorithm.  
 353 Similar to the one-bit reallocation algorithm designed for ASM  
 354 in [15], only the specific TA pair associated with the FD is con-  
 355 sidered, and the TPC parameters are selected for appropriately  
 356 weighting the SM symbols because the FD of this particular  
 357 TA pair predominantly determines the achievable performance.  
 358 The calculation of the TPC matrix is summarized in Fig. 3.

359 To be specific, given the channel matrix  $\mathbf{H}$ , the indexes of  
 360 the TA pair  $(g, k)$  associated with the FD  $d_{\min}(\mathbf{H})$  can be  
 361 found with the aid of the flowchart shown in Fig. 3. To offer  
 362 an increased FD, the precoding parameters of this TA pair can  
 363 be dynamically adapted. Note that, if the value of  $g$  is the same  
 364 as  $k$ , it is plausible that the TA  $g$  has the smallest channel gain.  
 365 In this case, the phase rotation elements of (10) do not have to  
 366 be considered because this would not increase the FD of (13).  
 367 To increase the FD, we only consider the PA matrix of (10)  
 368 and may deduct some power from the TA  $u$  having the highest  
 369 channel gain, which may hence be reassigned it to the TA  $g$ .  
 370 As a result,  $p_u$  and  $p_g$  have to be optimized. On the other hand,  
 371 if the value of  $g$  and  $k$  is not the same, parameters  $p_g$  and  $p_k$   
 372 have to be calculated. Overall, there are only two parameters,  
 373 namely,  $p_g$  and  $p_k$ , ( $p_u$  for  $g = k$ ) that have to be searched  
 374 for. Finding the optimal values of  $p_g$  and  $p_k$  as a function of

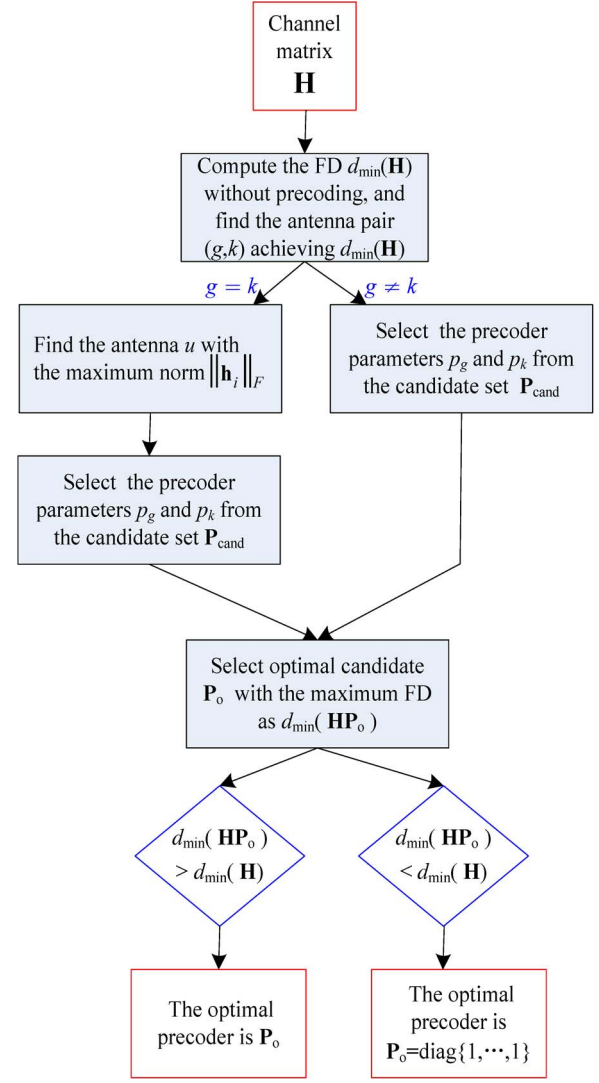


Fig. 3. Calculation of the diagonal precoding matrix for star-QAM-aided SM-MIMO.

both  $\mathbf{H}$  and of the optimal transmit parameters involves an  
 exhaustive search over the vast design space of  $\bar{p}_g$ ,  $\bar{p}_k$ ,  $\theta_g$ , and  
 $\theta_k$  of (10), which is overly complex. To reduce the complexity,  
 according to (12), the power of the TA pair  $(g, k)$  satisfies the  
 constraint  $\bar{p}_k^2 + \bar{p}_g^2 = 2$ ; hence, only the element  $\bar{p}_k$  has to be  
 searched for in the power matrix  $\bar{\mathbf{P}}$  of (10). Moreover, since  
 the phase rotation of the symbol is only carried by two TAs  
 and their phase difference is correlated, we can simplify the  
 computations by fixing  $\theta_k = 1$  and then finding the optimal

$$\begin{aligned}
 d_{\min}(\mathbf{H}, \mathbf{P}) &= \min_{s_l^i, s_k^j \in S} \left\| \mathbf{H} \mathbf{P} \left( s_l^i \mathbf{e}_i - s_k^j \mathbf{e}_j \right) \right\|_F \\
 &= \min_{s_l^i, s_k^j \in S} \left\| \left( \mathbf{h}_i p_i s_l^i - \mathbf{h}_j p_j s_k^j \right) \right\|_F \\
 &= \min_{s_l^i, s_k^j \in S} \sqrt{|s_l^i|^2 |p_i|^2 \mathbf{h}_i^H \mathbf{h}_i + |s_k^j|^2 |p_j|^2 \mathbf{h}_j^H \mathbf{h}_j - 2 |p_i| |p_j| |s_l^i| |s_k^j| \operatorname{Re} \{ \mathbf{h}_i^H \mathbf{h}_j e^{j(\phi - \theta_i + \theta_j)} \}}
 \end{aligned} \tag{13}$$

384  $\theta_g$ . This implies that only the phase parameter  $\theta_g$  has to be  
 385 optimized for the phase matrix  $\Theta$ . In Fig. 3, a numerical search  
 386 is used for varying  $\bar{p}_g$  and  $\theta_g$  in small steps. Note that we  
 387 have  $0 \leq \bar{p}_g \leq \sqrt{2}$  and  $0 \leq \theta_g \leq 2\pi$  according to (12). For our  
 388 numerical search, we have assumed

$$\begin{cases} \bar{p}_g = \sqrt{2}/V_1 * v_1, & v_1 = 0, \dots, V_1 \\ \theta_g = 2\pi/V_2 * v_2, & v_2 = 0, \dots, V_2 \end{cases} \quad (14)$$

389 where  $V_1$  and  $V_2$  represent the number of quantization steps and  
 390 can be flexibly selected according to the prevalent performance  
 391 requirements. As a result, the corresponding diagonal TPC  
 392 matrix candidates are

$$\mathbf{P}_{\text{cand}} = \text{diag} \left\{ \underset{\uparrow g\text{th}}{1, \dots, \bar{p}_g e^{j\theta_g}}, \dots, \underset{\uparrow k\text{th.}}{\sqrt{2 - \bar{p}_g^2}, \dots, 1} \right\} \quad (15)$$

393 Upon denoting the quantized TPC matrix  $\mathbf{P}$  as  $\mathbf{P}_{\text{cand}}$ , the  
 394 optimization problem of (12) is reformulated as

$$\mathbf{P}_{\text{opt}} = \arg \max_{\{\mathbf{P} \in \mathbf{P}_{\text{cand}}, \mathbf{P}_I\}} d_{\min}(\mathbf{H}, \mathbf{P}). \quad (16)$$

395 where we have  $\mathbf{P}_I = \mathbf{I}_{N_t}$ . In (16), the FD of the TPC matrices  
 396  $\mathbf{P}_{\text{cand}}$  generated will be compared with that of the conventional  
 397 scheme associated with  $\mathbf{P}_I$ , and then we select the one having  
 398 the largest FD as our final result. The receiver determines the  
 399 optimal diagonal TPC matrix based on (16) and feeds back the  
 400 TA indexes and their TPC parameters to the transmitter. Since  
 401 only the specific TA pair, which predominantly determines  
 402 the achievable performance, is considered, the proposed low-  
 403 complexity algorithm can be readily extended to a high number  
 404 of TAs.

#### 405 IV. SIMULATION RESULTS

406 Here, we characterize the performance of both the proposed  
 407 star-QAM-aided SM scheme and of the corresponding TPC  
 408 scheme, and compare it with that of the conventional QAM-  
 409 modulated SM schemes, with the PSK-modulated SM schemes  
 410 and with the ASM schemes [15] for transmission over inde-  
 411 pendent Rayleigh block-flat MIMO channels. It is assumed that  
 412 the receiver is capable of perfect phase and gain tracking, i.e.,  
 413 of perfect channel estimation. In practice, pilot symbols are  
 414 used for estimating the MIMO channel; hence, the estimated  
 415 channel matrix will inevitably be imperfect. To alleviate the  
 416 effects of channel estimation errors, the joint channel estimation  
 417 and data detection algorithm of [32] may be considered in the  
 418 proposed schemes, where the channel estimator and the data  
 419 detector iteratively exchange their information. We consider  
 420 two practical MIMO systems here, namely,  $(2 \times 2)$  and  $(4 \times$   
 421  $4)$  MIMO systems. Moreover, in the TPC design algorithm, we  
 422 select  $V_1 = V_2 = 5$  for simplicity.<sup>2</sup>

423 Fig. 4 shows the optimal ring ratios of star-QAM-aided  
 424 SM relying on  $(4 \times 4)$  elements for a different number of  
 425 modulation levels  $L$ , where the optimal ring ratio  $\alpha^*$  is seen  
 426 to be a function of the SNR. The bound of (2) is well suited

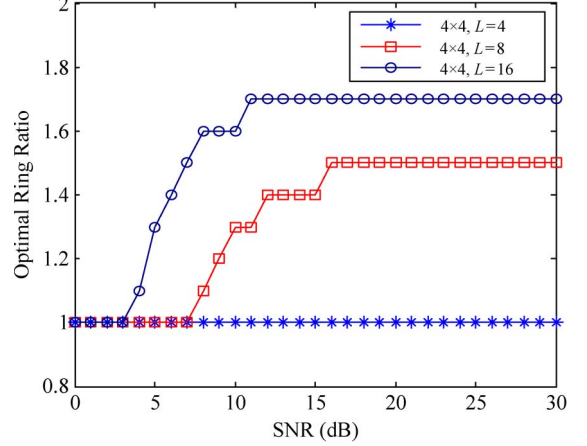


Fig. 4. Optimal ring ratios of star-QAM-aided SM with  $(4 \times 4)$  MIMO for different numbers of modulation levels  $L$ .

for numerically optimizing the ring ratio, particularly in the  
 427 high-SNR region. Observe in Fig. 4 that the optimal ratios  
 428 approach their asymptotic values, as the SNR increases. This  
 429 is expected since the bound of (2) is also asymptotically tight  
 430 and the probability of an error event in slow fading associated  
 431 with ML detection is dominated by the minimum-distance error  
 432 event at high values of the SNR. Moreover, the optimal ring  
 433 ratios are different for different MIMO parameters. 434

Since the transmitter operates at a fixed ring ratio, we have  
 435 opted for the asymptotic ring-ratio value for the evaluation  
 436 of the BER. For example, we have chosen the optimal ring  
 437 ratio  $\alpha^* = 1.7$  for the 16-star-QAM-aided  $(4 \times 4)$  SM-MIMO,  
 438 according to the results in Fig. 4. This result may be readily  
 439 extended to other star-QAM-aided SM scenarios, such as the  $(4$   
 440  $\times 4)$ -element star-QAM-aided SM schemes using  $L = 4, 8$  in  
 441 Fig. 4. 442

In Figs. 5 and 6, we compare various SM-MIMO systems  
 443 relying on diverse MIMO parameters and modulation orders. 444  
 445 First, in Figs. 5 and 6, we depict the BER performance  
 446 of the conventional QAM-modulated SM schemes, of the  
 447 PSK-modulated SM arrangements, and of the proposed star-  
 448 QAM-aided SM scheme. Note that the optimized star-QAM  
 449 constellation is designed offline for different SM-MIMO sys-  
 450 tems. Hence, the resultant system does not need any feedback. 450  
 451 To be specific, we may create a parameter lookup table for  
 452 the star-QAM SM schemes associated with the MIMO setups  
 453 considered; hence, the complexity of the optimal ring-ratio  
 454 search process detailed in Section II is negligible. For com-  
 455 pleteness, we also included the theoretical upper bound [30]  
 456 for the family of conventional SM schemes. We found that  
 457 the conventional QAM-modulated SM scheme outperforms its  
 458 identical-throughput PSK counterpart for a  $(4 \times 4)$ -element  
 459 MIMO channel in Fig. 5, whereas the PSK scheme is preferred  
 460 for a  $(2 \times 2)$ -element MIMO channel in Fig. 6. This indicates  
 461 that the best choice of the APM scheme depends on the specific  
 462 SM parameters, such as the MIMO setup and throughput. 462  
 463 Moreover, as shown in Fig. 5, the optimized star-QAM-aided  
 464 SM scheme provides an SNR gain of about 3 dB at  $\text{BER} =$   
 465  $10^{-5}$  over the conventional 16-PSK-modulated SM scheme and  
 466 an SNR gain of about 1.1 dB over the identical-throughput

<sup>2</sup>Note that the values of  $V_1$  and  $V_2$  can be different. Moreover, the selection of  $V_1$  and  $V_2$  is flexible, and higher values of  $V_1$  and  $V_2$  may lead to better performance at the cost of a higher TPC design complexity.



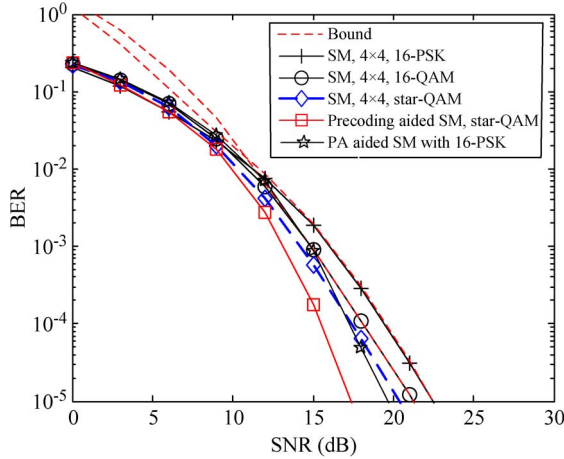


Fig. 5. BER performance of various SM-MIMO schemes operating in a  $(4 \times 4)$  MIMO channel at a total throughput of 6 b/s. Since the transmitter operates with a fixed ring ratio, we have chosen the asymptotic ring-ratio value for the evaluation of star-QAM-aided schemes. Here,  $\alpha$  is chosen as  $\alpha = 1.7$ .

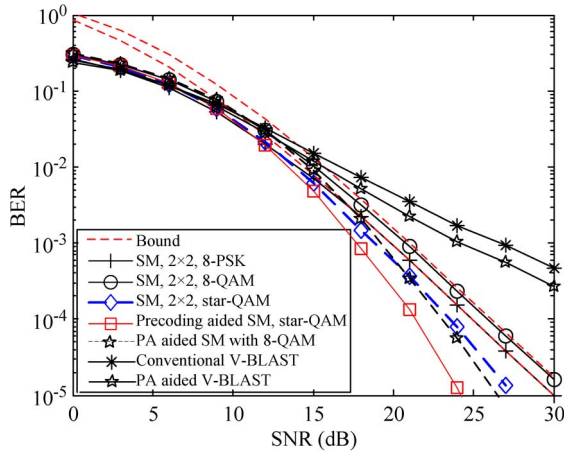


Fig. 6. BER performance of various SM schemes operating in a  $(2 \times 2)$  MIMO channel at a total throughput of 4 b/s. Here,  $\alpha$  is chosen as  $\alpha = 1.5$ .

Gray-coded MMD 16-QAM SM scheme. This advantage of the optimized star-QAM scheme recorded for SM-MIMO is also visible in Fig. 6.

Moreover, in Figs. 5 and 6, we also compare the achievable BER performance of the limited-feedback-aided ASM schemes. To be specific, two diagonal-precoding-aided schemes, namely, the precoding-assisted star-QAM-based SM schemes and the PA-aided SM schemes of [33] are compared. For simplicity, the PA algorithm is only applied to the non-ASM schemes exhibiting an inferior performance in Figs. 5 and 6, namely, to the conventional  $(4 \times 4)$ -element SM using 16-PSK and  $(2 \times 2)$ -element SM employing 8-QAM. Note that the  $(4 \times 4)$ -element SM associated with 16-QAM and  $(2 \times 2)$ -element SM employing 8-PSK can also use the PA regime to attain a BER improvement. Due to space limitations, these results are not presented here. As shown in Figs. 5 and 6, the proposed TPC schemes provide a gain of 2.5–3 dB at the BER of  $10^{-5}$  over the PA-aided SM schemes. This is because PA-aided SM may be viewed as a special case of the proposed precoding-aided SM created by only considering the PA matrix in (10). To be specific, compared with the PA-aided SM of

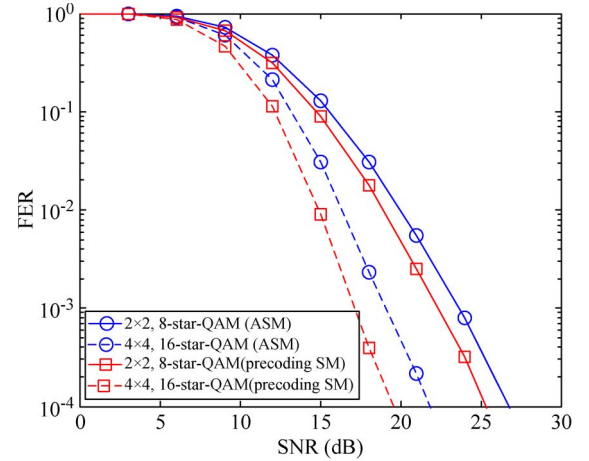


Fig. 7. FER performance of the proposed precoding star-QAM-aided SM and the ASM schemes at total throughputs of 4 and 6 b/s.

[33], our precoding-based SM regime jointly adapts the power and the phases of the transmit signals and hence improves the achievable BER performance.

Furthermore, in Fig. 6, we compare the QPSK-modulated V-BLAST scheme and its PA-aided counterpart associated with a zero-forcing-based successive interference cancellation (ZF-SIC) detector [18] as the benchmarks because their detection complexity is similar to that of the single-stream ML-based SM schemes. Observe in Fig. 6 for  $m_{\text{all}} = 4$  b/s that our TPC-aided SM scheme outperforms the PA-aided VBLAST arrangement relying on a ZF-SIC detector. Indeed, if a powerful ML detector is employed for the VBLAST system, we can achieve a better BER performance. However, designing PA algorithms for ML-based VBLAST systems is a challenge, and their detection complexity is high, as indicated in [34].

Fig. 7 shows the frame error rate (FER) of both the proposed precoded star-QAM-aided SM scheme and of the ASM scheme [15]. The transmission frame size is  $L_F = 60$  b.<sup>3</sup> Note that, although the proposed scheme and the ASM scheme exploit the same degrees of freedom offered by the SM-MIMO for improving the performance, our proposed scheme is capable of avoiding the error propagation effects often experienced in ASM, owing to ASM-mode signaling errors. Moreover, the selection of TPC parameters is more flexible than that of ASM because the modulation orders of ASM are selected from a discrete set, whereas the TPC parameters are chosen from the complex-valued field. As expected, the performance gain of the proposed scheme over ASM is seen to be about 2 dB at  $\text{FER} = 10^{-3}$  in Fig. 7.

## V. CONCLUSION

In this paper, we have investigated the problem of designing APM constellations that minimize the SM system's ABEP. We considered a class of star-QAM constellations, which is

<sup>3</sup>Here, we assume that the channel matrix remains constant within each transmit frame and consider the FER performance of these schemes. Note that the ASM schemes often suffer from error-propagation effects, as indicated in Section I. Hence, using the FER comparison of the ASM and TPC-aided SM schemes may be more suitable than the BER metric.

capable of flexibly adapting the ring ratios. We formulated the constellation design problem as an optimization problem and conceived an efficient iterative constellation-optimization method. Moreover, a diagonal TPC technique was proposed for the optimized star-QAM-aided SM to attain an improved performance. The simulation results confirm that our proposed optimized star-QAM-aided SM scheme outperforms the conventional PSK/QAM schemes. Moreover, our TPC method also exhibits an attractive BER/FER performance. For achieving an improved performance for a high number of bits per symbol, our further work will be focused on the integration of GSM and channel coding into the proposed TPC schemes.

## REFERENCES

- [1] R. Mesleh, H. Haas, S. Sinanovi, C. W. Ahn, and S. Yun, "Spatial modulation," *IEEE Trans. Veh. Technol.*, vol. 57, no. 4, pp. 2228–2241, Jul. 2008.
- [2] Y. Yang and B. Jiao, "Information-guided channel-hopping for high data rate wireless communication," *IEEE Commun. Lett.*, vol. 12, no. 4, pp. 225–227, Apr. 2008.
- [3] J. Jeganathan, A. Ghrayeb, L. Szczecinski, and A. Ceron, "Space shift keying modulation for MIMO channels," *IEEE Trans. Wireless Commun.*, vol. 8, no. 7, pp. 3692–3703, Jul. 2009.
- [4] M. Di Renzo, H. Haas, A. Ghrayeb, S. Sugiura, and L. Hanzo, "Spatial modulation for generalized MIMO: challenges, opportunities and implementation," *Proc. IEEE*, vol. 102, no. 1, pp. 56–103, Jan. 2014. [Online]. Available: <http://eprints.soton.ac.uk/354175/>
- [5] J. Wang, S. Jia, and J. Song, "Generalised spatial modulation system with multiple active transmit antennas and low complexity detection scheme," *IEEE Trans. Wireless Commun.*, vol. 11, no. 4, pp. 1605–1615, Apr. 2012.
- [6] E. Başar, Ü. Aygözü, E. Panayircı, and H. V. Poor, "Space-time block coded spatial modulation," *IEEE Trans. Commun.*, vol. 59, no. 3, pp. 823–832, Mar. 2011.
- [7] P. Yang, Y. Xiao, Y. Yu, and S. Q. Li, "Adaptive spatial modulation for wireless MIMO transmission systems," *IEEE Commun. Lett.*, vol. 15, no. 6, pp. 602–605, Jun. 2011.
- [8] M. Di Renzo, H. Haas, and P. M. Grant, "Spatial modulation for multiple-antenna wireless systems: A survey," *IEEE Commun. Mag.*, vol. 49, no. 12, pp. 182–191, Dec. 2011.
- [9] L. Hanzo, S. X. Ng, T. Keller, and W. Webb, *Quadrature Amplitude Modulation: From Basics to Adaptive Trellis-Coded, Turbo-Equalised and Space-Time Coded OFDM, CDMA and MC-CDMA Systems*. Hoboken, NJ, USA: Wiley, 2004.
- [10] L. Hanzo, O. Alamri, M. El-Hajjar, and N. Wu, *Near-Capacity Multi-Functional MIMO Systems: Sphere-Packing, Iterative Detection and Cooperation*. Hoboken, NJ, USA: Wiley, 2009.
- [11] M. Di Renzo and H. Haas, "Bit error probability of spatial modulation (SM-) MIMO over generalized fading channels," *IEEE Trans. Veh. Technol.*, vol. 61, no. 3, pp. 1124–1144, Mar. 2012.
- [12] P. Yang, Y. Xiao, L. Li, Q. Tang, Y. Yi, and S. Q. Li, "Link adaptation for spatial modulation with limited feedback," *IEEE Trans. Veh. Technol.*, vol. 61, no. 8, pp. 3808–3813, Oct. 2012.
- [13] J. Jeganathan, A. Ghrayeb, and L. Szczecinski, "Spatial modulation: optimal detection and performance analysis," *IEEE Commun. Lett.*, vol. 12, no. 8, pp. 545–547, Aug. 2008.
- [14] S. Sugiura, C. Xu, S. X. Ng, and L. Hanzo, "Reduced-complexity coherent versus non-coherent QAM-aided space-time shift keying," *IEEE Trans. Commun.*, vol. 59, no. 11, pp. 3090–3101, Nov. 2011.
- [15] P. Yang, Y. Xiao, Y. Yi, L. Li, Q. Tang, and S. Q. Li, "Simplified adaptive spatial modulation for limited-feedback MIMO," *IEEE Trans. Veh. Technol.*, vol. 62, no. 6, pp. 2656–2666, Jul. 2013.
- [16] R. Y. Chang, S. J. Lin, and W. H. Chung, "Energy efficient transmission over space shift keying modulated MIMO channels," *IEEE Trans. Commun.*, vol. 60, no. 12, pp. 2950–2959, Oct. 2012.
- [17] S. S. Ikki and R. Mesleh, "A general framework for performance analysis of space shift keying (SSK) modulation in the presence of Gaussian imperfect estimations," *IEEE Commun. Lett.*, vol. 16, no. 2, pp. 228–230, Feb. 2012.
- [18] S. Sugiura and L. Hanzo, "On the joint optimization of dispersion matrices and constellations for near-capacity irregular precoded space-time shift keying," *IEEE Trans. Wireless Commun.*, vol. 12, no. 1, pp. 380–387, Jan. 2013.
- [19] K. Ishibashi, W. Shin, H. Ochiai, and V. Tarokh, "A peak power efficient cooperative diversity using star-QAM with coherent/noncoherent detection," *IEEE Trans. Wireless Commun.*, vol. 12, no. 5, pp. 2137–2147, May 2013.
- [20] M. Di Renzo and H. Haas, "Improving the performance of space shift keying (SSK) modulation via opportunistic power allocation," *IEEE Commun. Lett.*, vol. 14, no. 6, pp. 500–502, Jun. 2010.
- [21] T. Handte, A. Muller, and J. Speidel, "BER analysis and optimization of generalized spatial modulation in correlated fading channels," in *Proc. IEEE Veh. Technol. Conf. Fall*, Sep. 2009, pp. 1–5.
- [22] K. Ntontin, M. Di Renzo, A. Perez-Neira, and C. Verikoukis, "Adaptive generalized space shift keying modulation," *EURASIP J. Wireless Commun. Netw.*, pp. 1–10, Feb. 2013.
- [23] M. Maleki, H. Bahrami, S. Beygi, M. Kafashan, and N. H. Tran, "Space modulation with CSI: constellation design and performance evaluation," *IEEE Trans. Veh. Technol.*, vol. 62, no. 4, pp. 1623–1634, May 2013.
- [24] B. M. Mthethwa and H. Xu, "Adaptive M-ary quadrature amplitude spatial modulation," *IET Commun.*, vol. 6, no. 18, pp. 3098–3108, Dec. 2012.
- [25] L. L. Yang, "Transmitter preprocessing aided spatial modulation for multiple-input multiple-output systems," in *Proc. IEEE 73th Veh. Technol. Conf.-Spring*, Budapest, Hungary, May. 2011, pp. 15–18.
- [26] A. Stavridis, S. Sinanovic, M. Di Renzo, and H. Haas, "Transmit precoding for receive spatial modulation using imperfect channel knowledge," in *Proc. IEEE Veh. Technol. Conf. - Spring*, Yokohama, Japan, May 6–9, 2012, pp. 1–5.
- [27] L. Lampe, "Noncoherent coded modulation," Ph.D. dissertation, Dept. Elect. Eng., Univ. Erlangen, Erlangen, Germany, 2002.
- [28] X. Dong, N. C. Beaulieu, and P. H. Wittke, "Error probabilities of two-dimensional M-ary signaling in fading," *IEEE Trans. Commun.*, vol. 47, no. 3, pp. 352–355, Mar. 1999.
- [29] L. Szczecinski, H. Xu, X. Gao, and R. Bettancourt, "Efficient evaluation of BER for arbitrary modulation and signaling in fading channels," *IEEE Trans. Commun.*, vol. 55, no. 11, pp. 2061–2064, Nov. 2007.
- [30] A. Goldsmith, *Wireless Communication*. New York, NY, USA: Cambridge Univ. Press, 2005, ch. 5.
- [31] Y. T. Kim, H. Lee, S. Park, and I. Lee, "Optimal precoding for orthogonalized spatial multiplexing in closed-loop MIMO systems," *IEEE J. Sel. Areas Commun.*, vol. 26, no. 8, pp. 1556–1567, Oct. 2008.
- [32] S. Chen, S. Sugiura, and L. Hanzo, "Semi-blind joint channel estimation and data detection for space-time shift keying systems," *IEEE Signal Process. Lett.*, vol. 17, no. 12, pp. 993–996, Dec. 2010.
- [33] Y. Xiao, Q. Tang, L. Gong, P. Yang, and Z. Yang, "Power scaling for spatial modulation with limited feedback." [Online]. Available: <http://downloads.hindawi.com/journals/ijap/aip/718482.pdf>
- [34] S. H. Nam, O. S. Shin, and K. B. Lee, "Transmit power allocation for a modified V-BLAST system," *IEEE Trans. Commun.*, vol. 52, no. 7, pp. 1074–1080, 2008.



**Ping Yang** received the B.E. and M.E. degrees from the University of Electronic Science and Technology of China, Chengdu, China, in 2006 and 2009, respectively, where he is currently working toward the Ph.D. degree.

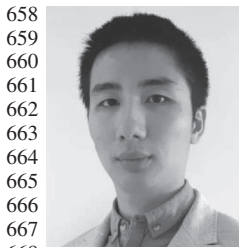
His research interests include multiple-input-multiple-output systems, space-time coding, and communication signal processing.



**Yue Xiao** received the Ph.D. degree in communication and information systems from the University of Electronic Science and Technology of China, Chengdu, China, in 2007.

He is currently an Associate Professor with the University of Electronic Science and Technology of China. He is the author of more than 30 international journal articles and has been involved in several 654 projects in the Chinese Beyond 3G Communication R&D Program. His research interests include wireless and mobile communications.





**Bo Zhang** received the B.S. degree in information engineering from the National University of Defense Technology, Changsha, China, in 2010. He is currently working toward the Ph.D. degree with the Communications, Signal Processing, and Control Group, School of Electronics and Computer Science, University of Southampton, Southampton, U.K.

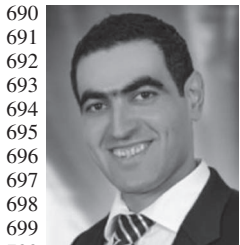
His research interests include wireless communications, particularly the design and analysis of cooperative communications and network-coded networks.



**Shaoqian Li** (SM'12) received the B.Eng. degree in electrical engineering from the American University of Beirut, Beirut, Lebanon, in 2004 and the M.Sc. degree in radio-frequency communication systems and the Ph.D. degree in wireless communications from the University of Southampton, Southampton, U.K., in 2005 and 2008, respectively.

After his doctoral years, he joined Imagination Technologies as a Research Engineer, where he worked on designing and developing the bit-interleaved coded modulation peripherals in Imagination's multistandard communications platform, which resulted in several patent applications. Since January 2012, he has been a Lecturer with the Communications, Signal Processing, and Control Group, School of Electronics and Computer Science, University of Southampton. He is the author of a Wiley-IEEE book and has written more than 40 journal and international conference papers. His research interests include machine-to-machine communications, millimeter-wave communications, large-scale multiple-input-multiple-output systems, cooperative communications, and radio over fiber systems.

Dr. Li has received several academic awards.



**Mohammed El-Hajjar** (M'08) received the B.Eng. degree in electrical engineering from the American University of Beirut, Beirut, Lebanon, in 2004 and the M.Sc. degree in radio-frequency communication systems and the Ph.D. degree in wireless communications from the University of Southampton, Southampton, U.K., in 2005 and 2008, respectively.

After his doctoral years, he joined Imagination Technologies as a Research Engineer, where he worked on designing and developing the bit-interleaved coded modulation peripherals in Imagination's multistandard communications platform, which resulted in several patent applications. Since January 2012, he has been a Lecturer with the Communications, Signal Processing, and Control Group, School of Electronics and Computer Science, University of Southampton. He is the author of a Wiley-IEEE book and has written more than 40 journal and international conference papers. His main research interests include the development of intelligent communications systems for the Internet of Things, including energy-efficient transceiver design, cross-layer optimization for large-scale networks, massive multiple-input-multiple-output systems for millimeter-wave communications, cooperative communications, and radio-over-fiber systems.

Dr. El-Hajjar has received several academic awards.



**Lajos Hanzo** (F'08) received the Master's degree in electronics, the Ph.D. degree, and the Doctor Honoris Causa degree from the Technical University of Budapest, Budapest, Hungary, in 1976, 1983, and 2009, respectively.

During his 35-year career in telecommunications, he has held various research and academic posts in Hungary, Germany, and the U.K. From 2008 to 2012, he was a Chaired Professor with Tsinghua University, Beijing, China. Since 1986, he has been with the School of Electronics and Computer Science,

University of Southampton, Southampton, U.K., where he is currently the Chair in telecommunications. He has successfully supervised 80 Ph.D. students. He is the author or coauthor of 20 John Wiley/IEEE Press books on mobile radio communications, totalling in excess of 10 000 pages, and more than 1300 research entries on IEEE Xplore. He has more than 16 000 citations. He is currently directing a 100-strong academic research team, working on a range of research projects in the field of wireless multimedia communications sponsored by industry, the Engineering and Physical Sciences Research Council, U.K., the European Information Society Technology Programme, and the Mobile Virtual Centre of Excellence, U.K. He is an enthusiastic supporter of industrial and academic liaison, and he offers a range of industrial courses. His research is funded by the European Research Council's Senior Research Fellow Grant. For further information on research in progress and associated publications please refer to <http://www-mobile.ecs.soton.ac.uk>.

Dr. Hanzo is a Fellow of the Royal Academy of Engineering, the Institution of Engineering and Technology, and the European Association for Signal Processing. He is also a Governor of the IEEE Vehicular Technology Society. He has been a Technical Program Committee Chair and a General Chair of IEEE conferences, has presented keynote lectures, and has been awarded a number of distinctions. From 2008 to 2012, he was the Editor-in-Chief for the IEEE Press.

## AUTHOR QUERIES

AUTHOR PLEASE ANSWER ALL QUERIES

AQ1 = There were discrepancies with the current affiliations of S. Li in the first footnote and that in the biography. Please check if the following changes are appropriate. If not, kindly provide the necessary corrections.

AQ2 = The sentence was modified for clarity. Please check if the following changes are appropriate. If not, kindly provide the necessary corrections.

AQ3 = Refs. [4] and [13] were the same and so was deleted from the list. Citations were renumbered accordingly. Please check.

END OF ALL QUERIES

# Star-QAM Signaling Constellations for Spatial Modulation

Ping Yang, Yue Xiao, Bo Zhang, Shaoqian Li, *Senior Member, IEEE*,  
Mohammed El-Hajjar, *Member, IEEE*, and Lajos Hanzo, *Fellow, IEEE*

**Abstract**—The performance of spatial modulation (SM)-assisted multiple-input–multiple-output (MIMO) communication systems is highly dependent on the specific amplitude/phase modulation (APM) signal constellation adopted. In this paper, we conceive new star-quadrature amplitude modulation (star-QAM)-aided SM schemes. Our goal is to minimize the system’s average bit error probability (ABEP). More specifically, a new class of star-QAM constellations is introduced for SM, which is capable of flexibly adapting ring ratios of the amplitude levels. Then, under a specific MIMO configuration and a predetermined transmission rate, a simple and efficient ring-ratio optimization algorithm is proposed to minimize the ABEP. Moreover, to improve further the performance of our star-QAM-aided SM scheme, a diagonal precoding technique is proposed, and a low-complexity minimum-distance-based approach is conceived for extracting the precoding parameters. Our numerical results show that the proposed star-QAM-aided SM arrangement provides beneficial system performance improvements compared with the identical-throughput maximum–minimum distance (MMD) QAM and phase-shift keying (PSK) benchmarks. Moreover, our precoding scheme is capable of further improving the attainable system performance at a modest feedback requirement.

**Index Terms**—Constellation optimization, multiple-input–multiple-output (MIMO), spatial modulation (SM), star-quadrature amplitude modulation (star-QAM).

## I. INTRODUCTION

**S**patial Modulation (SM), which maps the information bits to two information-carrying entities, namely the antenna indexes and the combined amplitude/phase modulation (APM) constellation, constitutes a promising low-complexity multiple-input–multiple-output (MIMO) transmission technique [1]–[8]. In a conventional single-input–single-output (SISO) system, the Gray-coded maximum–minimum distance

(MMD) quadrature amplitude modulation (QAM) constellation minimizes the bit error rate (BER) [9], [10]. However, the advantage of MMD-QAM may be eroded in SM-MIMO systems [11]. This is due to the fact that the BER performance of SM-MIMO systems is jointly determined by the spatial signal (i.e., antenna indexes), by the classic APM constellation, and by their interaction [11]–[18].

Recently, the effects of APM schemes on the performance of SM have been investigated in [11], [14], and [18]. More specifically, in [11], the performance of SM systems relying both on conventional QAM and PSK modulation was studied, demonstrating that, in some MIMO setups, the PSK-modulated SM scheme may outperform the identical-throughput MMD-QAM-aided SM scheme. In [18], the dispersion matrices and the signal constellations were jointly optimized for a near-capacity irregular precoded space–time shift keying (STSK) system, which includes SM as a special case and strikes a flexible rate–diversity tradeoff. It was also shown in [14] that the star-QAM-aided STSK scheme outperforms its MMD-based square-QAM-aided counterpart. This observation may be also valid for SM systems [11]. The aforementioned results indicated that the performance of SM is highly dependent on the specific APM adopted; hence, a suitable APM scheme has to be designed for this hybrid modulation scheme.

On the other hand, star-QAM constitutes a special case of circular amplitude- and phase-shift keying, which is capable of outperforming the classic square-QAM constellation in peak-power-limited systems [19]. Hence, it has been adopted in most of the recent satellite communication standards, such as in the Digital Video Broadcast System (DVB) S2, DVB-SH, and the Internet Protocol over Satellite and Advanced Broadcasting System via Satellite [19]. The star-QAM constellation is composed of multiple concentric circles, and it was shown to be beneficial in the context of STSK systems. Hence, star-QAM may be an attractive APM candidate for SM-MIMO. However, the constellations’ optimization has not been carried out for star-QAM-aided SM.

Moreover, to increase the robustness of the SM-MIMO system, limited-feedback-aided link adaptation schemes have been proposed in [20]–[26]. For example, in [20], an opportunistic power-allocation (PA) scheme was conceived for achieving a beneficial transmit diversity gain in SM-MIMO systems. In [21], a beamforming codebook was designed for optimizing the coding gain of SM-MIMO based on the knowledge of the channel envelope’s spatial correlation. Recently, an adaptive closed-loop-aided method was invoked for providing both diversity and coding gains in the context of space-shift keying (SSK)[22],

Manuscript received July 27, 2013; revised December 26, 2013; accepted February 8, 2014. This work was supported in part by the European Research Council under an Advanced Fellow Grant, by the National Science Foundation of China under Grant 61101101, by the Foundation Project of the National Key Laboratory of Science and Technology on Communications under Grant 9140C020404120C0201, and by the Key Laboratory of Universal Wireless Communications, Beijing University of Posts and Telecommunications, Chinese Ministry of Education, under Grant KFKT-2012102. The review of this paper was coordinated by Dr. G. Bauch.

P. Yang and Y. Xiao are with the National Key Laboratory of Science and Technology on Communications, University of Electronic Science and Technology of China, Chengdu 611731, China (e-mail: yplxw@163.com).

B. Zhang, S. Li, M. El-Hajjar, and L. Hanzo are with the School of Electronics and Computer Science, University of Southampton, Southampton SO17 1BJ, U.K. (e-mail: bz2g10@ecs.soton.ac.uk; lsq@uestc.edu.cn; meh@ecs.soton.ac.uk; lh@ecs.soton.ac.uk).

Color versions of one or more of the figures in this paper are available online at <http://ieeexplore.ieee.org>.

Digital Object Identifier 10.1109/TVT.2014.2306986



which is a special case of SM. However, the scheme proposed for SSK may not be directly applicable to the conventional SM scheme. Moreover, ASM-MIMO architectures relying on different combinations of modulation schemes were proposed in [24], which aimed for maximizing the channel capacity at a predefined target BER, rather than for minimizing the BER. In contrast, in [25] and [26], a transmit precoding (TPC) technique was used for improving the modulated signal design for SM. However, this technique may only be suitable for a new class of SM relying on a single-receiver antenna. For the conventional SM, we proposed a near-instantaneously adaptive-modulation-aided scheme for minimizing the BER [7], which was termed adaptive SM (ASM). Then, we further generalized this paper in [12] and [15], where the implementation complexity of ASM was considerably reduced. However, ASM typically transmits a different number of bits in the different-quality time slots, which may be inconvenient in fixed-rate applications and potentially leads to error propagation in the case of ASM-mode signaling errors.

Against this background, the novel contributions of this paper are threefold.

- We introduced the class of star-QAM constellations [27], which is capable of flexibly adapting the ring ratios, hence subsuming classic PSK as a special case. Alternatively, if the ring ratio is appropriately selected, the proposed star-QAM is capable of achieving almost the same Euclidean distance (ED) as the MMD-based QAM.
- Given a specific MIMO configuration and a predetermined transmission rate, a low-complexity yet efficient optimization algorithm is proposed to minimize the average bit error probability (ABEP) of SM-MIMO systems, where the effects of both the antenna index, as well as of the APM signal and their interaction, are jointly considered. Only the optimal ring ratios of star-QAM constellation have to be found by the optimization algorithm.
- We introduce a new TPC scheme for star-QAM-aided SM-MIMO systems, which further improves the performance. To retain the benefits of SM, such as its low-complexity single-stream detector and its single RF chain, we design its TPC matrix  $\mathbf{P}$  to be diagonal. We demonstrate that this precoded scheme and the ASM schemes of [12] and [15] are capable of exploiting the same degrees of freedom as that offered by the classic SM-MIMO for maximizing the free distance (FD). However, our TPC scheme assigns the same number of bits to each time slot; hence, it is capable of avoiding the potential error propagation effects of ASM encountered in the case of ASM-mode signaling errors. Our simulation results show that the proposed TPC scheme considerably improves the system's performance compared with the conventional star-QAM-aided SM, the PA-aided SM, and ASM arrangements.

The remainder of this paper is organized as follows. In Section II, we conceive a signaling constellation optimization method for star-QAM-aided SM and elaborate both on the choice of our optimization criterion and on the corresponding optimization algorithm. In Section III, we propose a new TPC scheme for enhancing the performance of the star-QAM-aided

SM. Our numerical analysis is carried out in Section IV. Finally, our conclusions are presented in Section V.

## II. SIGNALING CONSTELLATION OPTIMIZATION

### A. Performance Metric and Star-QAM Constellation

Consider a flat-fading MIMO channel associated with  $N_t$  transmit antennas (TAs) and  $N_r$  receive antennas. The  $(N_t \times 1)$ -element transmit symbol vector  $\mathbf{x}$  is assumed to satisfy  $E[\mathbf{x}\mathbf{x}^H] = \mathbf{I}_{N_t}$ , where  $\mathbf{I}_{N_t}$  denotes an  $(N_t \times N_t)$ -element identity matrix. Then, the transmitted SM symbol  $\mathbf{x} \in \mathbb{C}^{N_t \times 1}$  is given as  $\mathbf{x} = s_l^n \mathbf{e}_n$  [21], where  $s_l^n$  is the complex-valued symbol of the APM scheme employed at the  $n$ th TA. For example,  $L$ -PSK/QAM is associated with  $m_{\text{APM}} = \log_2(L)$  input bits, whereas  $\mathbf{e}_n (1 \leq n \leq N_t)$  is selected from the  $N_t$ -dimensional standard basis vectors (i.e.,  $\mathbf{e}_1 = [1, 0, \dots, 0]^T$ ), according to  $\log_2(N_t)$  input bits. The corresponding received signal is given by

$$\mathbf{y} = \mathbf{H}\mathbf{x} + \mathbf{n} = \mathbf{h}_n s_l^n + \mathbf{n} \quad (1)$$

where  $\mathbf{H}$  is an  $(N_r \times N_t)$ -element channel matrix,  $\mathbf{h}_n$  is the  $n$ th column of  $\mathbf{H}$ , and the elements of the  $N_r$ -dimensional noise vector  $\mathbf{n}$  are Gaussian random variables obeying  $\mathcal{CN}(0, N_0)$ .

In [11], an improved union bound partitions the ABEP expression of SM-MIMO systems into three terms: the  $P_{\text{spatial}}$  term related to the TA index, the  $P_{\text{signal}}$  term related to the APM signals, and the joint term  $P_{\text{joint}}$ , which depends on both the TA index and on the APM signals. This bound is formulated as

$$P_{\text{SM}}(\rho) \leq P_{\text{spatial}}(\rho) + P_{\text{signal}}(\rho) + P_{\text{joint}}(\rho). \quad (2)$$

This improved union bound is more accurate than the conventional union-bound-based methods, hence facilitating a deeper understanding of the joint impact of spatial and APM signals, as illustrated in [11]. We focus our attention on the system's performance for transmission over i.i.d. Rayleigh fading channels, which may be readily extended to the Nakagami- $m$  fading model of [11]. Let us assume that  $\rho$  is the average SNR, whereas  $x_l$  and  $x_i$  represent two different APM constellation points, with their modulus values being given as  $\beta_l$  and  $\beta_i$ , respectively. Then, we have

$$P_{\text{signal}}(\rho) = \frac{\log_2(L)}{\log_2(N_t \cdot L)} P_{\text{APM}}(\rho) \quad (3)$$

$$P_{\text{spatial}}(\rho) = \frac{\log_2(N_t) N_t}{2L \log_2(N_t \cdot L)} \sum_{l=1}^L \mathcal{F}(\rho \beta_l^2) \quad (4)$$

$$P_{\text{joint}}(\rho) = A \sum_{l=1}^L \sum_{i \neq l=1}^L \left[ B + C D_H(x_l \rightarrow x_i) \right] \times \mathcal{F}\left(\frac{\rho}{2} (\beta_l^2 + \beta_i^2)\right). \quad (5)$$

Here,  $P_{\text{APM}}(\rho)$  represents the error probability of conventional  $L$ -APM, which depends on the ED of the constellation points of APM, whereas  $D_H(x_l \rightarrow x_i)$  is the Hamming distance between signals  $x_l$  and  $x_i$ . Here,  $A = 1/L \log(N_t \cdot L)$ ,  $B = N_t \log(N_t)/2$ , and  $C = (N_t - 1)$  are constants for a fixed

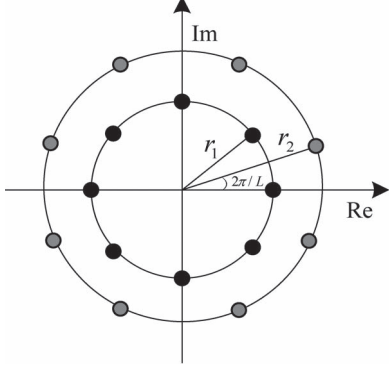


Fig. 1. Complex signal constellation of 16-star-QAM. The symbols are evenly distributed on two rings and the phase differences between the neighboring symbols on the same ring are equal.

MIMO setup. Moreover, the function  $\mathcal{F}(\varepsilon)$  in (4) and (5) is the pairwise error probability function [11], which is given by

$$\mathcal{F}(\varepsilon) = \gamma(\varepsilon)^{N_r} \sum_{n=0}^{N_r-1} \binom{N_r-1+n}{n} [1 - \gamma(\varepsilon)]^n \quad (6)$$

where we have  $\gamma(\varepsilon) \triangleq (1/2)(1 - \sqrt{(\varepsilon/2 + \varepsilon)})$ . Note that the ABEP bound of (2) was proposed for the general family of APM schemes, which contains not only the conventional PSK but also the generic rectangular nonsquare-QAM schemes and the square-QAM schemes. Moreover, since  $P_{\text{signal}}$  is available in closed form for conventional APM modulation schemes, the bound of (2) is more accurate than the conventional results of [21].

As indicated in (3)–(5),  $P_{\text{signal}}$  mainly depends on the minimum ED  $d_{\min}$  of the APM constellation points, whereas  $P_{\text{joint}}$  and  $P_{\text{spatial}}$  mainly depend on the modulus values  $\beta_l$  ( $l = 1, \dots, L$ ) of the APM constellation points.

Note that the modulus values  $\beta_l$  are represented by the Frobenius norms of the APM constellation points. These results suggested that, for jointly minimizing  $P_{\text{signal}}$ ,  $P_{\text{joint}}$ , and  $P_{\text{spatial}}$ , we can focus our attention on the design of  $d_{\min}$  and on the  $\beta_l$  parameters of APM.

To make the choice of the APM parameters  $d_{\min}$  and  $\beta_l$  as flexible as possible, we consider a class of star-QAM constellations, which subsumes the classic PSK as a special case but may also be configured for maximizing the minimum ED of the constellation by appropriately adjusting the ring ratios of the amplitude levels. For simplicity, we consider the example of a twin-ring 16-star-QAM constellation having a ring ratio of  $\alpha = r_2/r_1$ , as shown in Fig. 1. The symbols are evenly distributed on the two rings, and the phase differences between the neighboring symbols on the same ring are equal. Unlike the conventional twin-ring star-QAM constellation [19], [28], the constellation points on the outer circle of our proposed star-QAM constellation are rotated by  $2\pi/L$  degrees compared with the corresponding constellation points on the inner circle [27]. Hence, again, the conventional PSK constitutes an integral part of our star-QAM scheme, which is associated with  $\alpha = 1$ . Table I summarizes the minimum EDs  $d_{\min}$  between the constellation points for different APM schemes. It is found that this star-QAM scheme is capable of achieving almost the same

TABLE I  
MINIMUM ED BETWEEN THE CONSTELLATION  
POINTS FOR DIFFERENT APM SCHEMES

Modulation order	2	4 (MMD)	8 ([9])	16 (MMD)	32 ([9])
PSK	2	$\sqrt{2}$	0.7654	0.3902	0.1960
QAM	-	$\sqrt{2}$	0.8165	0.6325	0.4082
Proposed star-QAM	2	$\sqrt{2}$	0.9134	0.5737	0.3952

minimum ED as the MMD-based QAM. Note that, although this twin-ring star-QAM constellation has been indeed applied for noncoherent detection [27], it has not been considered whether this constellation can be directly applied to SM for achieving performance improvements.

The aforementioned twin-ring philosophy of Fig. 1 may be readily extended to multiple-ring star-QAM. The reasons for considering twin-ring star-QAM in our paper are the following.

- It is an attractive APM modulation candidate for SM, exhibiting a high performance at low detection complexity compared with conventional QAM schemes, as detailed in [13]–[15].
- It can be flexibly designed for different  $d_{\min}$  and  $\beta_l$  ( $l = 1, \dots, L$ ) combinations, which is achieved by simply adjusting a single parameter  $\alpha$ , whereas  $\beta_l$  can assume two values because only two rings are considered.
- The ABEP of star-QAM, which is related to the  $P_{\text{spatial}}$  term of (3), has been documented in [28] and [29].

## B. Optimization Criteria and Optimization Algorithm

Observe in Fig. 1 that there are numerous options for the parameter  $\alpha$  of the star-QAM constellation, for a given MIMO setup, specified by the total number of bits per symbol  $m_{\text{all}}$ , the  $(N_r \times N_t)$  configuration of transceiver, and the number of modulation level  $L$ . The goal of star-QAM-aided signaling constellation optimization is to find the specific ring ratio  $\alpha$ , which minimizes the ABEP of the SM-MIMO of (2). Note that, although the term  $P_{\text{SM}}(\rho)$  in (2) cannot be directly represented by parameter  $\alpha$ , it varies as a function of  $\alpha$ , which may be formulated as  $P_{\text{SM}}(\rho, \alpha)$ . Following the aforementioned approach, we formulated this optimization problem as

$$\begin{cases} \alpha^* = \min_{\alpha} P_{\text{SM}}(\rho, \alpha) \\ \text{s.t. } \alpha \geq 1 \end{cases} \quad (7)$$

which may be a convex one for a fixed SNR value  $\rho$ , as indicated in Fig. 4. However, deriving the closed-form solution of (7) remains an open challenge since the expression of  $P_{\text{SM}}(\rho, \alpha)$  depends both on the specific APM constellation and on the particular MIMO setup [19], and since the expressions of  $P_{\text{signal}}$ ,  $P_{\text{joint}}$  and  $P_{\text{spatial}}$  in (3)–(5) are complex. Hence, a numerical search is adopted.

Our optimization algorithm conceived for finding the ring ratio is summarized as follows.

Step 1: Initialize the values of  $N_r$ ,  $N_t$ ,  $m_{\text{all}}$ ,  $L$ , and the SNR value  $\rho$ . Set the iteration step size to  $\Delta\alpha = 0.1$  and the number of iterations to  $n = 1$ . The choice of  $\Delta\alpha$  is flexible, and a lower value of  $\Delta\alpha$  may lead to a better performance. We then set the search area of  $\alpha$  to  $1 \leq \alpha \leq U_\alpha$  and the performance metric to  $P_{\text{iter}}(n) = 0$ .

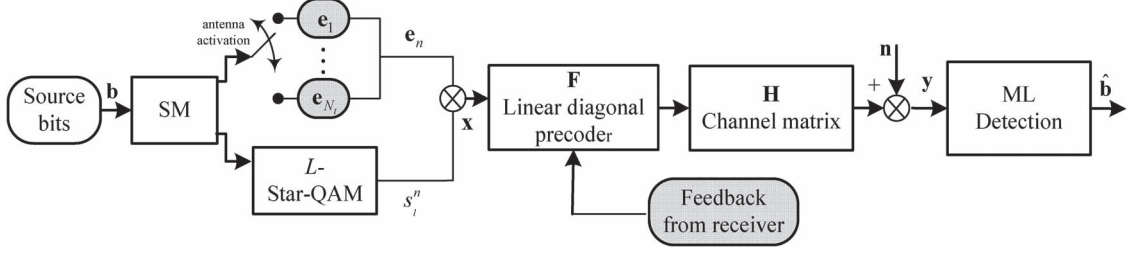


Fig. 2. System model of the diagonal-precoding-assisted star-QAM-aided SM scheme.

Step 2: While  $\alpha \leq U_\alpha$ , let  $\Delta\hat{\alpha} = \min\{\Delta\hat{\alpha}, U_\alpha - \alpha\}$ , and calculate the probabilities of  $P_{\text{signal}}$ ,  $P_{\text{joint}}$ , and  $P_{\text{spatial}}$  by using (3)–(5) associated with  $\alpha$ . Then, let  $P_{\text{iter}}(n) = P_{\text{SM}}(\rho)$  using (2), and set  $\alpha = \alpha + \Delta\hat{\alpha}$  and  $n = n + 1$ .  
 Step 3 : Find the index  $n^* = \min_n\{P_{\text{iter}}(n)\}$  to achieve the optimal ring ratio of  $\alpha^* = 1 + (n^* - 1)\Delta\hat{\alpha}$ .

In the aforementioned optimization algorithm, we have to choose an appropriate  $U_\alpha$  to promptly find the optimal  $\alpha^*$ . More explicitly, an excessively low value of  $U_\alpha$  may lead to missing the optimal solution, whereas an excessively high value of  $U_\alpha$  imposes excessive computational complexity on the optimization process. Hence, we will show in Section III that  $U_\alpha = 3$  is a beneficial choice for promptly approaching the optimal results. Moreover, the optimum ring ratio  $\alpha^*$  is a function of the SNR. However, we will show that the optimum ratio approaches its asymptotic optimum as the SNR increases.

### III. PROPOSED DIAGONAL PRECODING FOR

#### STAR-QUADRATURE AMPLITUDE MODULATION-AIDED SPATIAL MODULATION

Since the performance of the optimum maximum-likelihood (ML) receiver depends on the FD of the received signal constellation [30], we propose a new TPC based on maximizing the FD for the family of star-QAM-aided SM-MIMO systems, when limited channel state information is available at the transmitter. Since the FD is increased by the TPC algorithm, the proposed scheme is expected to provide a beneficial system performance improvement. To retain all the single-RF-related benefits of SM, we design the TPC matrix  $\mathbf{P}$  to be diagonal. The system model of the diagonal-TPC-assisted star-QAM-aided SM scheme is shown in Fig. 2. To identify the specific TPC parameters, which are capable of maximizing the FD, we propose a low-complexity TPC design algorithm. We will demonstrate that as few as two elements of the diagonal TPC matrix have to be fed back to the transmitter, regardless of  $N_t$ .

##### A. TPC Design Criterion

To construct a TPC for star-QAM-aided SM-MIMO systems, we can rewrite the system model of (1) as

$$\mathbf{y} = \mathbf{H}\mathbf{P}\mathbf{x} + \mathbf{n} \quad (8)$$

where  $\mathbf{P}$  denotes the diagonal TPC matrix, which can be represented as

$$\mathbf{P} = \text{diag}\{p_1, \dots, p_n, \dots, p_{N_t}\} \quad (9)$$

where  $p_n$  controls the channel gain associated with  $x_n$ . Here, we let  $\sum_{n=1}^{N_t} |p_n|^2 = N_t$  for normalizing the transmit power. Note that the introduction of TPC in SM does not affect the advantages of SM, such as the avoidance of the interantenna interference and the reliance on a single RF chain, because the precoded transmit vector  $\mathbf{P}\mathbf{x}$  includes only a single nonzero component; hence, only a single TA is activated in each time slot, as indicated in (8).

Numerous techniques may be invoked for constructing the TPC  $\mathbf{P}$  [21], [25]. In this paper, similar to the precoding methods conceived for the orthogonalized spatial multiplexing of [31], we decompose  $\mathbf{P}$  as

$$\mathbf{P} = \bar{\mathbf{P}}\mathbf{\Theta} = \text{diag}\{\bar{p}_1 e^{j\theta_1}, \dots, \bar{p}_n e^{j\theta_n}, \dots, \bar{p}_{N_t} e^{j\theta_{N_t}}\} \quad (10)$$

where  $\bar{\mathbf{P}} = \text{diag}\{\bar{p}_1, \dots, \bar{p}_n, \dots, \bar{p}_{N_t}\}$  represents the PA matrix, whereas  $\mathbf{\Theta} = \text{diag}\{e^{j\theta_1}, \dots, e^{j\theta_n}, \dots, e^{j\theta_{N_t}}\}$  is the phase rotation matrix. The FD between the constellation points at the receiver is defined as

$$\begin{aligned} d_{\min}(\mathbf{H}, \mathbf{P}) &= \min_{\substack{\mathbf{x}_i, \mathbf{x}_j \in \mathbb{X}, \\ \mathbf{x}_i \neq \mathbf{x}_j}} \|\mathbf{H}\mathbf{P}(\mathbf{x}_i - \mathbf{x}_j)\|_F \\ &= \min_{\mathbf{e}_{ij} \in \mathbb{E}} \|\mathbf{H}\bar{\mathbf{P}}\mathbf{\Theta}\mathbf{e}_{ij}\|_F \end{aligned} \quad (11)$$

where  $\mathbb{X}$  is the set of all legitimate transmit symbols,  $\mathbf{e}_{ij} = \mathbf{x}_i - \mathbf{x}_j$ ,  $i \neq j$  denotes the error vector, and  $\mathbb{E}$  is a set of error vectors. Then, we design the TPC  $\mathbf{P}$  by maximizing the FD with the aid of the following criterion:

$$\begin{cases} \mathbf{P}_{\text{opt}} = \arg \max_{\mathbf{P}} d_{\min}(\mathbf{H}, \mathbf{P}) \\ \text{s.t.} \quad \sum_{n=1}^{N_t} |p_n|^2 = N_t; \quad p_n \in C; \\ \quad \theta_n \in (0, 2\pi]; \quad n = 1, \dots, N_t. \end{cases} \quad (12)$$

Note that, since the attainable performance of the optimum single-stream ML receiver depends on the FD of the received signal constellation [30], the maximization of the FD directly reduces the probability of error.<sup>1</sup> Let  $\mathbf{x}_i = s_l^i \mathbf{e}_i$  and  $\mathbf{x}_j = s_k^j \mathbf{e}_j$  denote two different transmit symbols, whereas  $s_l^i$  and  $s_k^j$  denote the constellation points  $l$  and  $k$  represented by the  $i$ th and  $j$ th antennas, respectively. Then, the FD of (11) can be represented as (13), where  $\phi = \angle((s_l^i)^* s_k^j) = -\angle(s_l^i (s_k^j)^*)$ . In

<sup>1</sup>Because the conventional PSK-and-QAM-aided SM scheme's performance is worse than that of the proposed star-QAM-aided SM, we only invoked the TPC algorithm for the star-QAM-aided SM for the sake of achieving further performance improvements. However, it is worth noting that the proposed TPC algorithm is also suitable for SM in conjunction with both conventional PSK and QAM schemes.



331 the ASM scheme of [7], only the APM modulation orders to  
 332 be used by the transmitter are adapted, i.e., only the elements  
 333  $|s_l^i|$ ,  $|s_k^j|$ , and  $\phi$  of (13), shown at the bottom of the page, are  
 334 dynamically adapted to the channel conditions, and the legit-  
 335 imate values of these elements are selected from the discrete  
 336 set depending on the modulation order set utilized. By contrast,  
 337 our proposed scheme adjusts all the TPC elements  $|p_i|$ ,  $|p_j|$ ,  
 338  $\theta_i$ , and  $\theta_j$  of (13) for maximizing the FD  $d_{\min}(\mathbf{H}, \mathbf{P})$ , whose  
 339 legitimate values are drawn from the real-valued number field.  
 340 Based on these observations and on (13), the proposed scheme  
 341 and the ASM scheme may exploit the same degrees of freedom  
 342 as that offered by the SM-MIMO in terms of maximizing the  
 343 FD. However, unlike the ASM scheme of [7] and [15], our  
 344 proposed scheme assigns the same number of bits to each time  
 345 slot; hence, the potential error propagation effects experienced  
 346 in ASM are avoided.

### 347 B. Low-Complexity TPC Design Algorithm

348 To identify the specific TPC matrix  $\mathbf{P}$ , which is capable of  
 349 maximizing the FD, we have to determine all the  $N_t$  parameters  
 350  $p_n (n = 1, \dots, N_t)$ . Since it may become excessively complex  
 351 to jointly optimize these  $N_t$  parameters in the complex-valued  
 352 field, we propose a low-complexity precoder design algorithm.  
 353 Similar to the one-bit reallocation algorithm designed for ASM  
 354 in [15], only the specific TA pair associated with the FD is con-  
 355 sidered, and the TPC parameters are selected for appropriately  
 356 weighting the SM symbols because the FD of this particular  
 357 TA pair predominantly determines the achievable performance.  
 358 The calculation of the TPC matrix is summarized in Fig. 3.

359 To be specific, given the channel matrix  $\mathbf{H}$ , the indexes of  
 360 the TA pair  $(g, k)$  associated with the FD  $d_{\min}(\mathbf{H})$  can be  
 361 found with the aid of the flowchart shown in Fig. 3. To offer  
 362 an increased FD, the precoding parameters of this TA pair can  
 363 be dynamically adapted. Note that, if the value of  $g$  is the same  
 364 as  $k$ , it is plausible that the TA  $g$  has the smallest channel gain.  
 365 In this case, the phase rotation elements of (10) do not have to  
 366 be considered because this would not increase the FD of (13).  
 367 To increase the FD, we only consider the PA matrix of (10)  
 368 and may deduct some power from the TA  $u$  having the highest  
 369 channel gain, which may hence be reassigned it to the TA  $g$ .  
 370 As a result,  $p_u$  and  $p_g$  have to be optimized. On the other hand,  
 371 if the value of  $g$  and  $k$  is not the same, parameters  $p_g$  and  $p_k$   
 372 have to be calculated. Overall, there are only two parameters,  
 373 namely,  $p_g$  and  $p_k$ , ( $p_u$  for  $g = k$ ) that have to be searched  
 374 for. Finding the optimal values of  $p_g$  and  $p_k$  as a function of

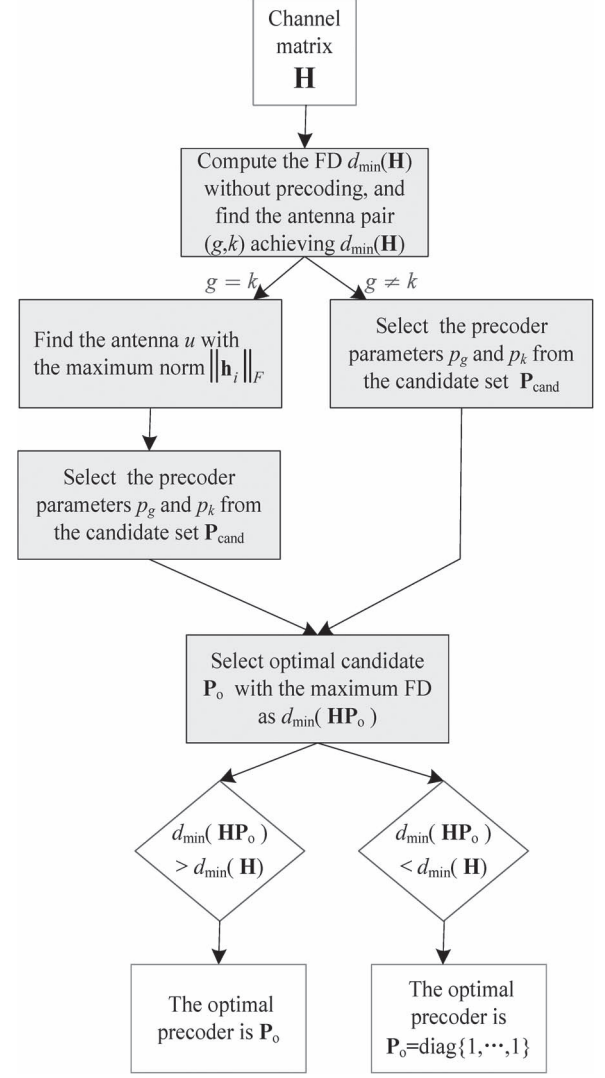


Fig. 3. Calculation of the diagonal precoding matrix for star-QAM-aided SM-MIMO.

both  $\mathbf{H}$  and of the optimal transmit parameters involves an  
 exhaustive search over the vast design space of  $\bar{p}_g$ ,  $\bar{p}_k$ ,  $\theta_g$ , and  
 $\theta_k$  of (10), which is overly complex. To reduce the complexity,  
 according to (12), the power of the TA pair  $(g, k)$  satisfies the  
 constraint  $\bar{p}_k^2 + \bar{p}_g^2 = 2$ ; hence, only the element  $\bar{p}_k$  has to be  
 searched for in the power matrix  $\bar{\mathbf{P}}$  of (10). Moreover, since  
 the phase rotation of the symbol is only carried by two TAs  
 and their phase difference is correlated, we can simplify the  
 computations by fixing  $\theta_k = 1$  and then finding the optimal

$$\begin{aligned}
 d_{\min}(\mathbf{H}, \mathbf{P}) &= \min_{s_l^i, s_k^j \in S} \left\| \mathbf{H} \mathbf{P} \begin{pmatrix} s_l^i \mathbf{e}_i - s_k^j \mathbf{e}_j \end{pmatrix} \right\|_F \\
 &= \min_{s_l^i, s_k^j \in S} \left\| \begin{pmatrix} \mathbf{h}_i p_i s_l^i - \mathbf{h}_j p_j s_k^j \end{pmatrix} \right\|_F \\
 &= \min_{s_l^i, s_k^j \in S} \sqrt{|s_l^i|^2 |p_i|^2 \mathbf{h}_i^H \mathbf{h}_i + |s_k^j|^2 |p_j|^2 \mathbf{h}_j^H \mathbf{h}_j - 2 |p_i| |p_j| |s_l^i| |s_k^j| \operatorname{Re} \{ \mathbf{h}_i^H \mathbf{h}_j e^{j(\phi - \theta_i + \theta_j)} \}}
 \end{aligned} \tag{13}$$

384  $\theta_g$ . This implies that only the phase parameter  $\theta_g$  has to be  
 385 optimized for the phase matrix  $\Theta$ . In Fig. 3, a numerical search  
 386 is used for varying  $\bar{p}_g$  and  $\theta_g$  in small steps. Note that we  
 387 have  $0 \leq \bar{p}_g \leq \sqrt{2}$  and  $0 \leq \theta_g \leq 2\pi$  according to (12). For our  
 388 numerical search, we have assumed

$$\begin{cases} \bar{p}_g = \sqrt{2}/V_1 * v_1, & v_1 = 0, \dots, V_1 \\ \theta_g = 2\pi/V_2 * v_2, & v_2 = 0, \dots, V_2 \end{cases} \quad (14)$$

389 where  $V_1$  and  $V_2$  represent the number of quantization steps and  
 390 can be flexibly selected according to the prevalent performance  
 391 requirements. As a result, the corresponding diagonal TPC  
 392 matrix candidates are

$$\mathbf{P}_{\text{cand}} = \text{diag} \left\{ \underset{\uparrow g\text{th}}{1, \dots, \bar{p}_g e^{j\theta_g}}, \dots, \underset{\uparrow k\text{th.}}{\sqrt{2 - \bar{p}_g^2}}, \dots, 1 \right\} \quad (15)$$

393 Upon denoting the quantized TPC matrix  $\mathbf{P}$  as  $\mathbf{P}_{\text{cand}}$ , the  
 394 optimization problem of (12) is reformulated as

$$\mathbf{P}_{\text{opt}} = \arg \max_{\{\mathbf{P} \in \mathbf{P}_{\text{cand}}, \mathbf{P}_I\}} d_{\min}(\mathbf{H}, \mathbf{P}). \quad (16)$$

395 where we have  $\mathbf{P}_I = \mathbf{I}_{N_t}$ . In (16), the FD of the TPC matrices  
 396  $\mathbf{P}_{\text{cand}}$  generated will be compared with that of the conventional  
 397 scheme associated with  $\mathbf{P}_I$ , and then we select the one having  
 398 the largest FD as our final result. The receiver determines the  
 399 optimal diagonal TPC matrix based on (16) and feeds back the  
 400 TA indexes and their TPC parameters to the transmitter. Since  
 401 only the specific TA pair, which predominantly determines  
 402 the achievable performance, is considered, the proposed low-  
 403 complexity algorithm can be readily extended to a high number  
 404 of TAs.

#### 405 IV. SIMULATION RESULTS

406 Here, we characterize the performance of both the proposed  
 407 star-QAM-aided SM scheme and of the corresponding TPC  
 408 scheme, and compare it with that of the conventional QAM-  
 409 modulated SM schemes, with the PSK-modulated SM schemes  
 410 and with the ASM schemes [15] for transmission over inde-  
 411 pendent Rayleigh block-flat MIMO channels. It is assumed that  
 412 the receiver is capable of perfect phase and gain tracking, i.e.,  
 413 of perfect channel estimation. In practice, pilot symbols are  
 414 used for estimating the MIMO channel; hence, the estimated  
 415 channel matrix will inevitably be imperfect. To alleviate the  
 416 effects of channel estimation errors, the joint channel estimation  
 417 and data detection algorithm of [32] may be considered in the  
 418 proposed schemes, where the channel estimator and the data  
 419 detector iteratively exchange their information. We consider  
 420 two practical MIMO systems here, namely,  $(2 \times 2)$  and  $(4 \times$   
 421  $4)$  MIMO systems. Moreover, in the TPC design algorithm, we  
 422 select  $V_1 = V_2 = 5$  for simplicity.<sup>2</sup>

423 Fig. 4 shows the optimal ring ratios of star-QAM-aided  
 424 SM relying on  $(4 \times 4)$  elements for a different number of  
 425 modulation levels  $L$ , where the optimal ring ratio  $\alpha^*$  is seen  
 426 to be a function of the SNR. The bound of (2) is well suited

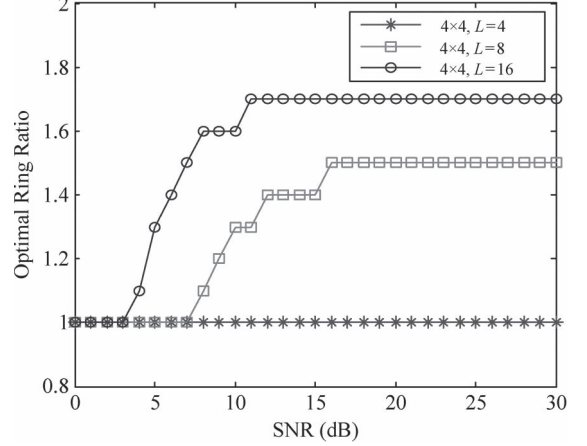


Fig. 4. Optimal ring ratios of star-QAM-aided SM with  $(4 \times 4)$  MIMO for different numbers of modulation levels  $L$ .

for numerically optimizing the ring ratio, particularly in the  
 427 high-SNR region. Observe in Fig. 4 that the optimal ratios  
 428 approach their asymptotic values, as the SNR increases. This  
 429 is expected since the bound of (2) is also asymptotically tight  
 430 and the probability of an error event in slow fading associated  
 431 with ML detection is dominated by the minimum-distance error  
 432 event at high values of the SNR. Moreover, the optimal ring  
 433 ratios are different for different MIMO parameters. 434

Since the transmitter operates at a fixed ring ratio, we have  
 435 opted for the asymptotic ring-ratio value for the evaluation  
 436 of the BER. For example, we have chosen the optimal ring  
 437 ratio  $\alpha^* = 1.7$  for the 16-star-QAM-aided  $(4 \times 4)$  SM-MIMO,  
 438 according to the results in Fig. 4. This result may be readily  
 439 extended to other star-QAM-aided SM scenarios, such as the  $(4$   
 440  $\times 4)$ -element star-QAM-aided SM schemes using  $L = 4, 8$  in  
 441 Fig. 4. 442

In Figs. 5 and 6, we compare various SM-MIMO systems  
 443 relying on diverse MIMO parameters and modulation orders. 444  
 445 First, in Figs. 5 and 6, we depict the BER performance  
 446 of the conventional QAM-modulated SM schemes, of the  
 447 PSK-modulated SM arrangements, and of the proposed star-  
 448 QAM-aided SM scheme. Note that the optimized star-QAM  
 449 constellation is designed offline for different SM-MIMO sys-  
 450 tems. Hence, the resultant system does not need any feedback. 450  
 451 To be specific, we may create a parameter lookup table for  
 452 the star-QAM SM schemes associated with the MIMO setups  
 453 considered; hence, the complexity of the optimal ring-ratio  
 454 search process detailed in Section II is negligible. For com-  
 455 pleteness, we also included the theoretical upper bound [30]  
 456 for the family of conventional SM schemes. We found that  
 457 the conventional QAM-modulated SM scheme outperforms its  
 458 identical-throughput PSK counterpart for a  $(4 \times 4)$ -element  
 459 MIMO channel in Fig. 5, whereas the PSK scheme is preferred  
 460 for a  $(2 \times 2)$ -element MIMO channel in Fig. 6. This indicates  
 461 that the best choice of the APM scheme depends on the specific  
 462 SM parameters, such as the MIMO setup and throughput. 462  
 463 Moreover, as shown in Fig. 5, the optimized star-QAM-aided  
 464 SM scheme provides an SNR gain of about 3 dB at  $\text{BER} =$   
 465  $10^{-5}$  over the conventional 16-PSK-modulated SM scheme and  
 466 an SNR gain of about 1.1 dB over the identical-throughput

<sup>2</sup>Note that the values of  $V_1$  and  $V_2$  can be different. Moreover, the selection of  $V_1$  and  $V_2$  is flexible, and higher values of  $V_1$  and  $V_2$  may lead to better performance at the cost of a higher TPC design complexity.

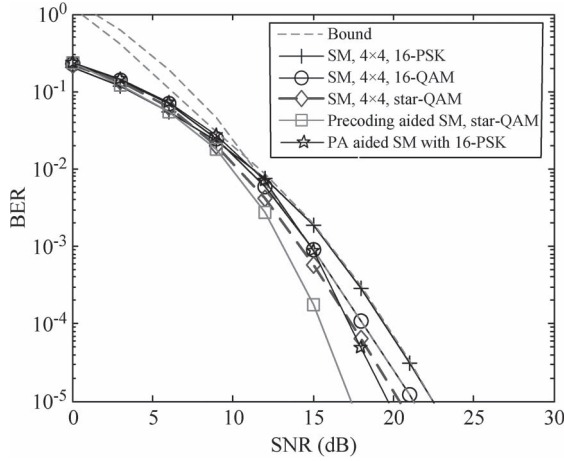


Fig. 5. BER performance of various SM-MIMO schemes operating in a  $(4 \times 4)$  MIMO channel at a total throughput of 6 b/s. Since the transmitter operates with a fixed ring ratio, we have chosen the asymptotic ring-ratio value for the evaluation of star-QAM-aided schemes. Here,  $\alpha$  is chosen as  $\alpha = 1.7$ .

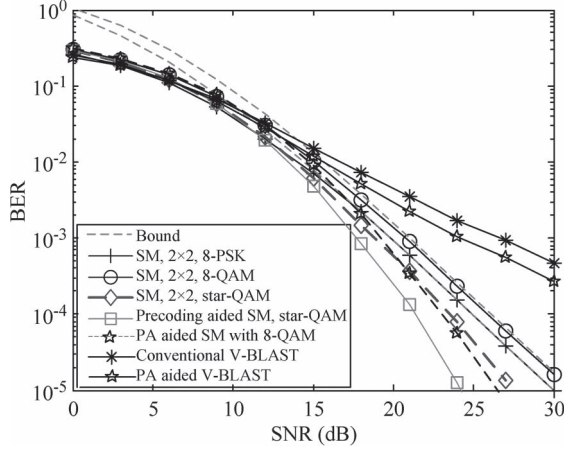


Fig. 6. BER performance of various SM schemes operating in a  $(2 \times 2)$  MIMO channel at a total throughput of 4 b/s. Here,  $\alpha$  is chosen as  $\alpha = 1.5$ .

Gray-coded MMD 16-QAM SM scheme. This advantage of the optimized star-QAM scheme recorded for SM-MIMO is also visible in Fig. 6.

Moreover, in Figs. 5 and 6, we also compare the achievable BER performance of the limited-feedback-aided ASM schemes. To be specific, two diagonal-precoding-aided schemes, namely, the precoding-assisted star-QAM-based SM schemes and the PA-aided SM schemes of [33] are compared. For simplicity, the PA algorithm is only applied to the non-ASM schemes exhibiting an inferior performance in Figs. 5 and 6, namely, to the conventional  $(4 \times 4)$ -element SM using 16-PSK and  $(2 \times 2)$ -element SM employing 8-QAM. Note that the  $(4 \times 4)$ -element SM associated with 16-QAM and  $(2 \times 2)$ -element SM employing 8-PSK can also use the PA regime to attain a BER improvement. Due to space limitations, these results are not presented here. As shown in Figs. 5 and 6, the proposed TPC schemes provide a gain of 2.5–3 dB at the BER of  $10^{-5}$  over the PA-aided SM schemes. This is because PA-aided SM may be viewed as a special case of the proposed precoding-aided SM created by only considering the PA matrix in (10). To be specific, compared with the PA-aided SM of

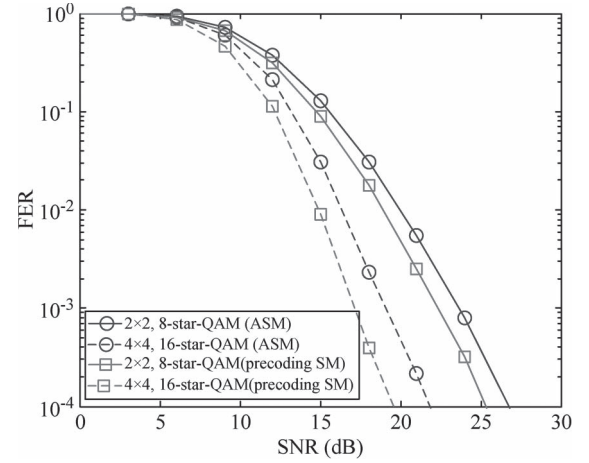


Fig. 7. FER performance of the proposed precoding star-QAM-aided SM and the ASM schemes at total throughputs of 4 and 6 b/s.

[33], our precoding-based SM regime jointly adapts the power and the phases of the transmit signals and hence improves the achievable BER performance.

Furthermore, in Fig. 6, we compare the QPSK-modulated V-BLAST scheme and its PA-aided counterpart associated with a zero-forcing-based successive interference cancellation (ZF-SIC) detector [18] as the benchmarks because their detection complexity is similar to that of the single-stream ML-based SM schemes. Observe in Fig. 6 for  $m_{\text{all}} = 4$  b/s that our TPC-aided SM scheme outperforms the PA-aided VBLAST arrangement relying on a ZF-SIC detector. Indeed, if a powerful ML detector is employed for the VBLAST system, we can achieve a better BER performance. However, designing PA algorithms for ML-based VBLAST systems is a challenge, and their detection complexity is high, as indicated in [34].

Fig. 7 shows the frame error rate (FER) of both the proposed precoded star-QAM-aided SM scheme and of the ASM scheme [15]. The transmission frame size is  $L_F = 60$  b.<sup>3</sup> Note that, although the proposed scheme and the ASM scheme exploit the same degrees of freedom offered by the SM-MIMO for improving the performance, our proposed scheme is capable of avoiding the error propagation effects often experienced in ASM, owing to ASM-mode signaling errors. Moreover, the selection of TPC parameters is more flexible than that of ASM because the modulation orders of ASM are selected from a discrete set, whereas the TPC parameters are chosen from the complex-valued field. As expected, the performance gain of the proposed scheme over ASM is seen to be about 2 dB at  $\text{FER} = 10^{-3}$  in Fig. 7.

## V. CONCLUSION

In this paper, we have investigated the problem of designing APM constellations that minimize the SM system's ABEP. We considered a class of star-QAM constellations, which is

<sup>3</sup>Here, we assume that the channel matrix remains constant within each transmit frame and consider the FER performance of these schemes. Note that the ASM schemes often suffer from error-propagation effects, as indicated in Section I. Hence, using the FER comparison of the ASM and TPC-aided SM schemes may be more suitable than the BER metric.



capable of flexibly adapting the ring ratios. We formulated the constellation design problem as an optimization problem and conceived an efficient iterative constellation-optimization method. Moreover, a diagonal TPC technique was proposed for the optimized star-QAM-aided SM to attain an improved performance. The simulation results confirm that our proposed optimized star-QAM-aided SM scheme outperforms the conventional PSK/QAM schemes. Moreover, our TPC method also exhibits an attractive BER/FER performance. For achieving an improved performance for a high number of bits per symbol, our further work will be focused on the integration of GSM and channel coding into the proposed TPC schemes.

## REFERENCES

- [1] R. Mesleh, H. Haas, S. Sinanovi, C. W. Ahn, and S. Yun, "Spatial modulation," *IEEE Trans. Veh. Technol.*, vol. 57, no. 4, pp. 2228–2241, Jul. 2008.
- [2] Y. Yang and B. Jiao, "Information-guided channel-hopping for high data rate wireless communication," *IEEE Commun. Lett.*, vol. 12, no. 4, pp. 225–227, Apr. 2008.
- [3] J. Jeganathan, A. Ghrayeb, L. Szczecinski, and A. Ceron, "Space shift keying modulation for MIMO channels," *IEEE Trans. Wireless Commun.*, vol. 8, no. 7, pp. 3692–3703, Jul. 2009.
- [4] M. Di Renzo, H. Haas, A. Ghrayeb, S. Sugiura, and L. Hanzo, "Spatial modulation for generalized MIMO: challenges, opportunities and implementation," *Proc. IEEE*, vol. 102, no. 1, pp. 56–103, Jan. 2014. [Online]. Available: <http://eprints.soton.ac.uk/354175/>
- [5] J. Wang, S. Jia, and J. Song, "Generalised spatial modulation system with multiple active transmit antennas and low complexity detection scheme," *IEEE Trans. Wireless Commun.*, vol. 11, no. 4, pp. 1605–1615, Apr. 2012.
- [6] E. Başar, Ü. Aygözü, E. Panayircı, and H. V. Poor, "Space-time block coded spatial modulation," *IEEE Trans. Commun.*, vol. 59, no. 3, pp. 823–832, Mar. 2011.
- [7] P. Yang, Y. Xiao, Y. Yu, and S. Q. Li, "Adaptive spatial modulation for wireless MIMO transmission systems," *IEEE Commun. Lett.*, vol. 15, no. 6, pp. 602–605, Jun. 2011.
- [8] M. Di Renzo, H. Haas, and P. M. Grant, "Spatial modulation for multiple-antenna wireless systems: A survey," *IEEE Commun. Mag.*, vol. 49, no. 12, pp. 182–191, Dec. 2011.
- [9] L. Hanzo, S. X. Ng, T. Keller, and W. Webb, *Quadrature Amplitude Modulation: From Basics to Adaptive Trellis-Coded, Turbo-Equalised and Space-Time Coded OFDM, CDMA and MC-CDMA Systems*. Hoboken, NJ, USA: Wiley, 2004.
- [10] L. Hanzo, O. Alamri, M. El-Hajjar, and N. Wu, *Near-Capacity Multi-Functional MIMO Systems: Sphere-Packing, Iterative Detection and Cooperation*. Hoboken, NJ, USA: Wiley, 2009.
- [11] M. Di Renzo and H. Haas, "Bit error probability of spatial modulation (SM-) MIMO over generalized fading channels," *IEEE Trans. Veh. Technol.*, vol. 61, no. 3, pp. 1124–1144, Mar. 2012.
- [12] P. Yang, Y. Xiao, L. Li, Q. Tang, Y. Yi, and S. Q. Li, "Link adaptation for spatial modulation with limited feedback," *IEEE Trans. Veh. Technol.*, vol. 61, no. 8, pp. 3808–3813, Oct. 2012.
- [13] J. Jeganathan, A. Ghrayeb, and L. Szczecinski, "Spatial modulation: optimal detection and performance analysis," *IEEE Commun. Lett.*, vol. 12, no. 8, pp. 545–547, Aug. 2008.
- [14] S. Sugiura, C. Xu, S. X. Ng, and L. Hanzo, "Reduced-complexity coherent versus non-coherent QAM-aided space-time shift keying," *IEEE Trans. Commun.*, vol. 59, no. 11, pp. 3090–3101, Nov. 2011.
- [15] P. Yang, Y. Xiao, Y. Yi, L. Li, Q. Tang, and S. Q. Li, "Simplified adaptive spatial modulation for limited-feedback MIMO," *IEEE Trans. Veh. Technol.*, vol. 62, no. 6, pp. 2656–2666, Jul. 2013.
- [16] R. Y. Chang, S. J. Lin, and W. H. Chung, "Energy efficient transmission over space shift keying modulated MIMO channels," *IEEE Trans. Commun.*, vol. 60, no. 12, pp. 2950–2959, Oct. 2012.
- [17] S. S. Ikkı and R. Mesleh, "A general framework for performance analysis of space shift keying (SSK) modulation in the presence of Gaussian imperfect estimations," *IEEE Commun. Lett.*, vol. 16, no. 2, pp. 228–230, Feb. 2012.
- [18] S. Sugiura and L. Hanzo, "On the joint optimization of dispersion matrices and constellations for near-capacity irregular precoded space-time shift keying," *IEEE Trans. Wireless Commun.*, vol. 12, no. 1, pp. 380–387, Jan. 2013.
- [19] K. Ishibashi, W. Shin, H. Ochiai, and V. Tarokh, "A peak power efficient cooperative diversity using star-QAM with coherent/noncoherent detection," *IEEE Trans. Wireless Commun.*, vol. 12, no. 5, pp. 2137–2147, May 2013.
- [20] M. Di Renzo and H. Haas, "Improving the performance of space shift keying (SSK) modulation via opportunistic power allocation," *IEEE Commun. Lett.*, vol. 14, no. 6, pp. 500–502, Jun. 2010.
- [21] T. Handte, A. Muller, and J. Speidel, "BER analysis and optimization of generalized spatial modulation in correlated fading channels," in *Proc. IEEE Veh. Technol. Conf. Fall*, Sep. 2009, pp. 1–5.
- [22] K. Ntontin, M. Di Renzo, A. Perez-Neira, and C. Verikoukis, "Adaptive generalized space shift keying modulation," *EURASIP J. Wireless Commun. Netw.*, pp. 1–10, Feb. 2013.
- [23] M. Maleki, H. Bahrami, S. Beygi, M. Kafashan, and N. H. Tran, "Space modulation with CSI: constellation design and performance evaluation," *IEEE Trans. Veh. Technol.*, vol. 62, no. 4, pp. 1623–1634, May 2013.
- [24] B. M. Mthethwa and H. Xu, "Adaptive M-ary quadrature amplitude spatial modulation," *IET Commun.*, vol. 6, no. 18, pp. 3098–3108, Dec. 2012.
- [25] L. L. Yang, "Transmitter preprocessing aided spatial modulation for multiple-input multiple-output systems," in *Proc. IEEE 73th Veh. Technol. Conf.-Spring*, Budapest, Hungary, May. 2011, pp. 15–18.
- [26] A. Stavridis, S. Sinanovic, M. Di Renzo, and H. Haas, "Transmit precoding for receive spatial modulation using imperfect channel knowledge," in *Proc. IEEE Veh. Technol. Conf. - Spring*, Yokohama, Japan, May 6–9, 2012, pp. 1–5.
- [27] L. Lampe, "Noncoherent coded modulation," Ph.D. dissertation, Dept. Elect. Eng., Univ. Erlangen, Erlangen, Germany, 2002.
- [28] X. Dong, N. C. Beaulieu, and P. H. Wittke, "Error probabilities of two-dimensional M-ary signaling in fading," *IEEE Trans. Commun.*, vol. 47, no. 3, pp. 352–355, Mar. 1999.
- [29] L. Szczecinski, H. Xu, X. Gao, and R. Bettancourt, "Efficient evaluation of BER for arbitrary modulation and signaling in fading channels," *IEEE Trans. Commun.*, vol. 55, no. 11, pp. 2061–2064, Nov. 2007.
- [30] A. Goldsmith, *Wireless Communication*. New York, NY, USA: Cambridge Univ. Press, 2005, ch. 5.
- [31] Y. T. Kim, H. Lee, S. Park, and I. Lee, "Optimal precoding for orthogonalized spatial multiplexing in closed-loop MIMO systems," *IEEE J. Sel. Areas Commun.*, vol. 26, no. 8, pp. 1556–1567, Oct. 2008.
- [32] S. Chen, S. Sugiura, and L. Hanzo, "Semi-blind joint channel estimation and data detection for space-time shift keying systems," *IEEE Signal Process. Lett.*, vol. 17, no. 12, pp. 993–996, Dec. 2010.
- [33] Y. Xiao, Q. Tang, L. Gong, P. Yang, and Z. Yang, "Power scaling for spatial modulation with limited feedback." [Online]. Available: <http://downloads.hindawi.com/journals/ijap/aip/718482.pdf>
- [34] S. H. Nam, O. S. Shin, and K. B. Lee, "Transmit power allocation for a modified V-BLAST system," *IEEE Trans. Commun.*, vol. 52, no. 7, pp. 1074–1080, 2008.



**Ping Yang** received the B.E. and M.E. degrees from the University of Electronic Science and Technology of China, Chengdu, China, in 2006 and 2009, respectively, where he is currently working toward the Ph.D. degree.

His research interests include multiple-input-multiple-output systems, space-time coding, and communication signal processing.



**Yue Xiao** received the Ph.D. degree in communication and information systems from the University of Electronic Science and Technology of China, Chengdu, China, in 2007.

He is currently an Associate Professor with the University of Electronic Science and Technology of China. He is the author of more than 30 international journal articles and has been involved in several 654 projects in the Chinese Beyond 3G Communication R&D Program. His research interests include wireless and mobile communications.



**Bo Zhang** received the B.S. degree in information engineering from the National University of Defense Technology, Changsha, China, in 2010. He is currently working toward the Ph.D. degree with the Communications, Signal Processing, and Control Group, School of Electronics and Computer Science, University of Southampton, Southampton, U.K.

His research interests include wireless communications, particularly the design and analysis of cooperative communications and network-coded networks.



**Shaoqian Li** (SM'12) received the B.Eng. degree in electrical engineering from the American University of Beirut, Beirut, Lebanon, in 2004 and the M.Sc. degree in radio-frequency communication systems and the Ph.D. degree in wireless communications from the University of Southampton, Southampton, U.K., in 2005 and 2008, respectively.

After his doctoral years, he joined Imagination Technologies as a Research Engineer, where he worked on designing and developing the bit-interleaved coded modulation peripherals in Imagination's multistandard communications platform, which resulted in several patent applications. Since January 2012, he has been a Lecturer with the Communications, Signal Processing, and Control Group, School of Electronics and Computer Science, University of Southampton. He is the author of a Wiley-IEEE book and has written more than 40 journal and international conference papers. His research interests include machine-to-machine communications, millimeter-wave communications, large-scale multiple-input-multiple-output systems, cooperative communications, and radio over fiber systems.

Dr. Li has received several academic awards.



**Mohammed El-Hajjar** (M'08) received the B.Eng. degree in electrical engineering from the American University of Beirut, Beirut, Lebanon, in 2004 and the M.Sc. degree in radio-frequency communication systems and the Ph.D. degree in wireless communications from the University of Southampton, Southampton, U.K., in 2005 and 2008, respectively.

After his doctoral years, he joined Imagination Technologies as a Research Engineer, where he worked on designing and developing the bit-interleaved coded modulation peripherals in Imagination's multistandard communications platform, which resulted in several patent applications. Since January 2012, he has been a Lecturer with the Communications, Signal Processing, and Control Group, School of Electronics and Computer Science, University of Southampton. He is the author of a Wiley-IEEE book and has written more than 40 journal and international conference papers. His main research interests include the development of intelligent communications systems for the Internet of Things, including energy-efficient transceiver design, cross-layer optimization for large-scale networks, massive multiple-input-multiple-output systems for millimeter-wave communications, cooperative communications, and radio-over-fiber systems.

Dr. El-Hajjar has received several academic awards.



**Lajos Hanzo** (F'08) received the Master's degree in electronics, the Ph.D. degree, and the Doctor Honoris Causa degree from the Technical University of Budapest, Budapest, Hungary, in 1976, 1983, and 2009, respectively.

During his 35-year career in telecommunications, he has held various research and academic posts in Hungary, Germany, and the U.K. From 2008 to 2012, he was a Chaired Professor with Tsinghua University, Beijing, China. Since 1986, he has been with the School of Electronics and Computer Science,

University of Southampton, Southampton, U.K., where he is currently the Chair in telecommunications. He has successfully supervised 80 Ph.D. students. He is the author or coauthor of 20 John Wiley/IEEE Press books on mobile radio communications, totalling in excess of 10 000 pages, and more than 1300 research entries on IEEE Xplore. He has more than 16 000 citations. He is currently directing a 100-strong academic research team, working on a range of research projects in the field of wireless multimedia communications sponsored by industry, the Engineering and Physical Sciences Research Council, U.K., the European Information Society Technology Programme, and the Mobile Virtual Centre of Excellence, U.K. He is an enthusiastic supporter of industrial and academic liaison, and he offers a range of industrial courses. His research is funded by the European Research Council's Senior Research Fellow Grant. For further information on research in progress and associated publications please refer to <http://www-mobile.ecs.soton.ac.uk>.

Dr. Hanzo is a Fellow of the Royal Academy of Engineering, the Institution of Engineering and Technology, and the European Association for Signal Processing. He is also a Governor of the IEEE Vehicular Technology Society. He has been a Technical Program Committee Chair and a General Chair of IEEE conferences, has presented keynote lectures, and has been awarded a number of distinctions. From 2008 to 2012, he was the Editor-in-Chief for the IEEE Press.

## AUTHOR QUERIES

AUTHOR PLEASE ANSWER ALL QUERIES

AQ1 = There were discrepancies with the current affiliations of S. Li in the first footnote and that in the biography. Please check if the following changes are appropriate. If not, kindly provide the necessary corrections.

AQ2 = The sentence was modified for clarity. Please check if the following changes are appropriate. If not, kindly provide the necessary corrections.

AQ3 = Refs. [4] and [13] were the same and so was deleted from the list. Citations were renumbered accordingly. Please check.

END OF ALL QUERIES