

## RESEARCH ARTICLE

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## Key Points:

- Nodal variations were estimated and compared with equilibrium tidal theory
- Nodal cycle was found in  $S_2$
- Significant trends were found in semidiurnal tides

## Supporting Information:

- Readme
- Auxiliary Material Revised

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## Nodal variations and long-term changes in the main tides on the coasts of China

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**Abstract** The long-term changes in the main tidal constituents ( $O_1$ ,  $K_1$ ,  $M_2$ ,  $N_2$ , and  $S_2$ ) along the coasts of China and in adjacent seas are investigated based on 17 tide-gauge records covering the period 1954–2012. The observed 18.61 year nodal modulations of the diurnal constituents  $O_1$  and  $K_1$  are in agreement with the equilibrium tidal theory, except in the South China Sea. The observed modulations of the  $M_2$  and  $N_2$  amplitudes are smaller than theoretically predicted at the northern stations and larger at the southern stations. The discrepancies between the theoretically predicted nodal variations and the observations are discussed. The 8.85 year perigean cycle is identifiable in the  $N_2$  parameters at most stations, except those in the South China Sea. The radiational component of  $S_2$  contributes on average 16% of the observed  $S_2$  except in the Gulf of Tonkin, on the south coast, where it accounts for up to 65%. We confirmed the existence of nodal modulation in  $S_2$ , which is stronger on the north coast. The semidiurnal tidal parameters show significant secular trends in the Bohai and Yellow Seas, on the north coast, and in the Taiwan Strait. The largest increase is found for  $M_2$  for which the amplitude increases by 4–7 mm/yr in the Yellow Sea. The potential causes for the linear trends in tidal constants are discussed.

## 1. Introduction

The nodal cycle is the main long-term modulation of lunar tidal parameters. It is caused by the precession of the lunar ascending node that has a period of 18.61 years. The late 19th century saw the development of the harmonic analysis of tidal observations [Darwin and Adams, 1883], in which the nodal cycle was initially referred to as “reduction,” representing the apparent variations in amplitude and phase of the main tidal components because of the impossibility of including in annual analyses all the satellites that are in the tidal potential. Doodson [1928] refined the method of calculating “nodal factors” which determine the nodal variations of amplitude and phase of each tidal component. Pugh and Woodworth [2014] include a description of nodal variations in the equilibrium tide, while Haigh *et al.* [2011] have mapped the worldwide distribution of nodal variations for the major tidal components using a numerical tidal model.

Deviations from the equilibrium theory have been identified in several regions around the world. The observed nodal modulation of  $M_2$  amplitude has been found to be less than that predicted by the equilibrium theory along the British Isles coasts [Amin, 1983, 1985; Woodworth *et al.*, 1991; Woodworth, 2010], the western coast of Australia [Amin, 1993; Woodworth, 2010], and the Bay of Fundy and Gulf of Maine [Ku *et al.*, 1985; Ray, 2006; Müller, 2011]. The differences have been suggested to be caused by the effect of bottom friction on the tidal signal [Ku *et al.*, 1985; Pingree and Griffiths, 1987]. By contrast, along the coasts of the Mediterranean and the Caribbean Seas, the nodal modulations of the main lunar constituents were found to follow the equilibrium tidal theory [Shaw and Tsimplis, 2010; Torres and Tsimplis, 2011]. The differences in these results correspond to the size of the tidal signal, with the latter studies referring to regions with small tides. A study based on altimetry data suggests that in the Pacific and western Atlantic Oceans the observed nodal amplitudes for main tidal constituents are in general close to the theoretical equilibrium values, but tend to exceed theory where the nodal amplitudes are small [Cherniawsky *et al.*, 2010].

The  $S_2$  tide is primarily generated by the solar gravitational potential. Thus, its amplitude and phase are, in principle, not expected to be affected by the lunar nodal cycle. However, variations of 1–2% in  $S_2$  amplitude at the nodal frequency were found from interannual analyses on UK coasts and the Gulf of Maine, as well as

on western Australian coasts [Amin, 1983, 1993; Woodworth, 2010; Müller, 2011]. The nonlinear interaction with  $M_2$  has been suggested to be the cause of such long-term variation [Woodworth, 2010]. In addition to the gravitational forcing of  $S_2$ , oscillations in barometric pressure, changes in ocean temperature, and onshore-offshore wind have also been argued as contributing to the sea surface variations at the  $S_2$  frequency [Chapman and Lindzen, 1970; Zetler, 1971; Pugh and Woodworth, 2014]. The nongravitational component of  $S_2$  is called the radiational tide and its amplitude has been estimated to be 10–18% of the gravitational amplitude, depending on geographical region and the physical parameters concerned (e.g., pressure, wind stress, and/or thermal forcing) [Cartwright, 1968; Zetler, 1971; Amin, 1982; Arbic, 2005].

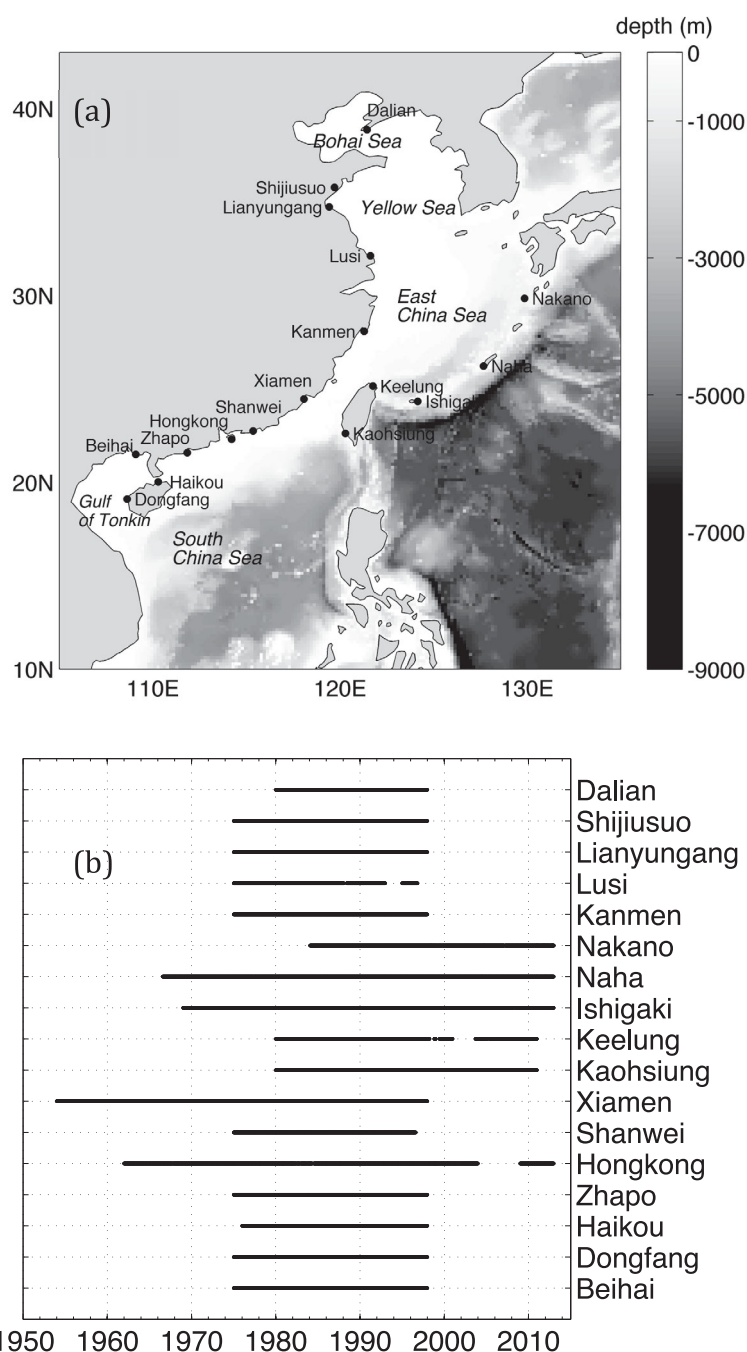
Linear trends in the amplitude and phase of tidal constituents have been identified around the British Isles [Amin, 1983], southern North Sea [Hollebrandse, 2005], Gulf of Maine [Ray, 2006], Northwest America [Jay, 2009], North Atlantic [Müller, 2011], Caribbean Sea [Torres and Tsimplis, 2011], and East China Sea [Feng and Tsimplis, 2014]. The largest rate reported is  $\sim 7$  mm/yr for the  $M_2$  amplitude occurring at Lianyungang on the west coast of the Yellow Sea [Feng and Tsimplis, 2014]. Woodworth [2010] and Müller *et al.* [2011] analyzed the spatial distribution of the observed trends in the major tidal constituents and found that the linear changes are commonplace for the North American coasts.  $S_2$  was found to be the component that usually shows the largest linear changes among the main tidal constituents [Müller *et al.*, 2011].

Why tidal components change linearly with time is not well understood. Changes in mean sea level have been argued as being able to distort the propagation of tidal waves [Amin, 1983], and the resulting changes in the tide have been estimated on the basis of numerical models [Amin, 1983; Green, 2010; Pickering *et al.*, 2012]. In general, the model estimates are small and unable to explain fully the observed tidal changes on the American and European coasts [Jay, 2009; Müller *et al.*, 2011]. Changes in the coastal morphology and bathymetry due to natural processes and anthropogenic works have also been argued as being the cause of changes in the tide in the Bohai Sea [Pelling *et al.*, 2013]. Ray [2009] argued that the decrease in the  $S_2$  amplitude on the east coast of North America could be due to changes in the radiational forcing. Woodworth [2010], Müller *et al.* [2011], and Müller [2011, 2012] discussed additional potential causes, for example, changes in the tidal potential, atmospheric dynamics, ocean circulation, stratification conditions, and thermocline depths. However, the causes for most of observed changes remain unclear.

In the marginal seas adjacent to China, spatial features of the main tidal signals have been identified from numerical models [Kang *et al.*, 1998; Fang *et al.*, 1999; Lefèvre *et al.*, 2000; Fang *et al.*, 2004], tide gauges [Fang, 1986, 1994], and satellite observations [Hu *et al.*, 2001], in which the nodal variations are assumed to follow the equilibrium tidal theory. However, in this shallow-water region (usually less than 100 m, see Figure 1a) the bottom friction effect on tides has been well recognized [Kang *et al.*, 1998; Lefèvre *et al.*, 2000; He *et al.*, 2004], and this effect in other regions has been found to be capable of altering the nodal behavior of tides from that expected, such as those mentioned above. Thus, it is worthwhile to investigate the observed nodal variations of tides in the China seas, and to compare them with the equilibrium tidal theory.

The Chinese coasts are being heavily modified due to sediment deposition at river mouths [Chu *et al.*, 2006; Pelling *et al.*, 2013], coastal erosion because of the impact of frequent tropical cyclones [Qi *et al.*, 2010; Feng *et al.*, 2012; Feng and Tsimplis, 2014], and extensive tidal flat reclamation that has taken place over the past few decades [Li *et al.*, 2004; Wang *et al.*, 2011; Li *et al.*, 2013; Wang *et al.*, 2014]. To our knowledge, there are no published papers describing the long-term trends in tides in this region, despite their importance for coastal planning.

In this paper, the 18.61 year nodal modulations of the main tidal constituents for the Chinese coasts are estimated from observations and compared with the equilibrium theory. Trends in tidal constituents are also mapped. The paper is organized in five sections. The data processing of sea level records and the methodology used for empirically fitting the nodal modulations are described in section 2. In section 3, the observed nodal modulations and linear trends of the main tidal constituents ( $O_1$ ,  $K_1$ ,  $M_2$ ,  $N_2$ , and  $S_2$ ) are presented and the ability of the equilibrium tidal theory to explain the observed changes is discussed. Section 4 discusses the possible causes for the differences between the observed nodal modulations and the equilibrium theory. Furthermore, it discusses the observed linear trends in the tidal components. Finally, our conclusions are presented in section 5.



**Figure 1.** (a) Locations of tide-gauge stations along the seas adjacent to China and (b) corresponding periods of valid data. The bathymetry in the studied areas is also shown in Figure 1a, which is based on the GEBCO\_08 Grid data set from the British Oceanographic Data Centre.

## 2. Data and Methodology

### 2.1. Sea Level Data

Hourly sea level data from 16 tide gauges on the Chinese coasts and 3 Japanese stations in the East China Sea are used (Figure 1a). The data were obtained from the University of Hawaii Sea Level Center (UHSLC). The sea level data span the period 1954–2012. From the 19 records available, 16 are longer than 23 years (Figure 1b). Two pairs of records were combined leaving 17 records covering at least 18 years for the analysis.

The nearby Dalian and Laohutan stations have data for the periods 1975–1990 and 1991–1997, respectively. However, at Dalian the tide gauge was relocated twice, once at the end of 1976, and once in 1979. After 1979, it shared the same position as Laohutan. Thus, the data for the periods 1980–1990 at Dalian and 1991–1997 at Laohutan were combined.

At Hongkong, the tide gauge was located at North Point for the period 1962–1986, and then moved half a kilometer away to Quarry Bay for the period 1987–2012. The same datum applies to both locations with an offset of 1.02 cm [Ding *et al.*, 2001]. Thus, the two Hongkong records were merged into a 51 year record, the longest in the study.

The tidal constituents were estimated annually by using the sea level processing package SLPR2 version 3.0 provided by UHSLC, after the mean value of sea level over the whole period of observations was removed from the record. The tidal analysis program is described in detail in Foreman [1977]. A maximum of 68 constituents is allowed in the analysis of 1 year of hourly records. It was required that the difference in tidal frequency between two resolvable tidal constituents is at least one cycle per year. Thus, the Rayleigh criterion was given a value of 1. The tidal amplitude and phase lag for each constituent are expressed as cosine and sine functions, which are estimated in observations by a least squares regression method. When the regression is finished, the difference between the sum of the observation squares and the sum of the predicted tidal curve squares is calculated. This difference is divided by the degrees of freedom providing the squares residual, where the “degrees of freedom” is the difference between the number of hourly observations and the number of functions fit in the analysis. The square root of the squares residual is then used to determine the errors for the tidal parameters. Through this method, the errors in the tidal parameters in each year have approximately the same magnitude.

Note that during the process the equilibrium nodal correction in the program was not applied to any lunar constituent. The annual and semiannual components were not included either, as these are not primarily astronomical in character. The tidal constants for each year, with their estimated errors (standard deviations) as their uncertainty, were then used to estimate the nodal variations and the linear trends for the tidal constituents.

The quality control performed included visual checks of the time series of the hourly measurements and the tidal residuals. Checks were also performed on the estimated annual tidal constants at each station. Values with spurious jumps, datum shifts, and time shifts from the values in other years were excluded. Using this quality control, data in the years 1993 and 1994 at Lusi and 1997 at Shanwei were removed. The periods with valid observations are shown in Figure 1b.

## 2.2. Lunar Constituent Modulation Model

All lunar constituents are modulated by the 18.61 year nodal cycle, and some of them are also affected by the 8.85 year perigean cycle, e.g.,  $L_2$  and  $N_2$ . The harmonic parameters of the 18.61 year and the 8.85 year cycles as well as the long-term trends were estimated by a least squares estimation model. The expression of the joint estimation is described as:

$$H_m(t) = \beta_1 + \beta_2 t + \beta_3 \cos(R_t) + \beta_4 \sin(R_t) \quad (1)$$

where  $H_m(t)$  is the estimated value of amplitude or phase lag for tidal constituent  $m$ ,  $\beta_1$  is the constant value,  $\beta_2$  is the linear trend, and  $t$  the time in units of year.  $\beta_3$  and  $\beta_4$  are the amplitudes of the cosine and sine functions of either nodal cycle or perigean cycle, and  $R_t$  is the argument of the cosine and sine functions and equal to either the negative of the longitude of the Moon's ascending node ( $N'$ ) (i.e.,  $N' = -N$ ) or the longitude of the perigean cycle  $P$  [Doodson and Warburg, 1941]:

$$\begin{aligned} N' &= 100.8432^\circ + 1934.142^\circ * T - 0.0021^\circ * T^2 \\ P &= 334.3853^\circ + 4069.034^\circ * T - 0.0103^\circ * T^2 \end{aligned} \quad (2)$$

where  $T$  is the time  $t$  in units of Julian century starting from zero hours at the Greenwich meridian on the first of January 1900.

After fitting equation (1), the estimated mean value of amplitude (or phase lag) ( $\bar{B}$ ), and estimated amplitude ( $\alpha_{N' \text{ or } P}$ ) and phase lag ( $\varphi_{N' \text{ or } P}$ ) of the nodal cycle or perigean cycle can be derived as:

**Table 1.** Nodal Factor ( $f$ ) and Nodal Angle ( $u$ ) for Long-Term Modulations of Major Lunar Constituents Derived From the Equilibrium Tidal Theory<sup>a</sup>

	$f$	$u$
$O_1$	$1.009 + 0.187 \cos(N)$	$10.8^\circ \sin(N)$
$K_1$	$1.006 + 0.115 \cos(N)$	$-8.9^\circ \sin(N)$
$M_2, N_2$	$1.000 - 0.037 \cos(N)$	$-2.1^\circ \sin(N)$

<sup>a</sup>Note that  $N$  is the longitude of lunar ascending node.  $N = 0$  in March 1969, November 1987, June 2006, etc., and  $N = 180^\circ$  in July 1978, March 1997, October 2015, etc.

$$\begin{aligned} \bar{B} &= \beta_1 + \beta_2 \bar{t} \\ \alpha_{N' \text{ or } P} &= \sqrt{\beta_3^2 + \beta_4^2} \\ \varphi_{N' \text{ or } P} &= \tan^{-1} \left( \frac{\beta_4}{\beta_3} \right) \end{aligned} \quad (3)$$

where  $\bar{t}$  is the time at the middle of record.

The ratio of estimated nodal amplitude over the mean value of tidal amplitude ( $\alpha_{N'}/\bar{B}$ ) expressed as a percentage is also calculated and compared with the theoretical ratio (nodal factor  $f$  in Table

1) from the equilibrium tidal theory [Pugh and Woodworth, 2014]. Similarly, the estimated nodal amplitude for tidal phase lag is also calculated and compared with that from the theoretical estimate (nodal angle  $u$  in Table 1).

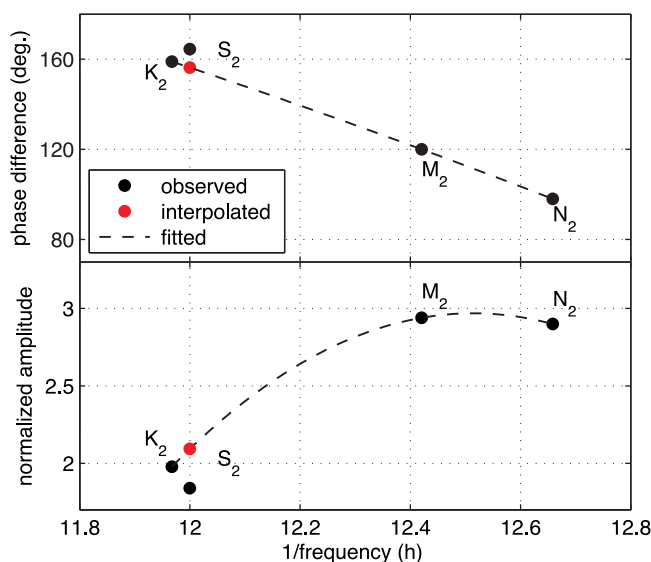
The perigean modulation is a third-order term in the tidal potential. The perigean factors are weakly dependent on the latitude ( $\theta$ ) of each station. Based on Doodson's classic expansion method [Godin, 1972], the perigean amplitude ratio (the ratio between the perigean change and mean amplitude) ( $\alpha_p/\bar{B}$ ) and the phase factor ( $\varphi_p$ ) are expressed as:

$$\begin{aligned} \alpha_p/\bar{B} &= 0.085 * \sin(\theta) \\ \varphi_p &\approx \alpha_p/\bar{B} \end{aligned} \quad (4)$$

The value of phase factor ( $\varphi_p$ ) in radians is approximately equal to the amplitude ratio ( $\alpha_p/\bar{B}$ ) because of the amplitude ratio  $\ll 1$ . At stations studied here, the perigean modulation predicted from the equilibrium tidal theory is 2.8–5.3% for the  $N_2$  amplitude and 1.6–3.1° for the phase lag. We also checked the perigean factors based on the tables of Cartwright and Tayler [1971] and Cartwright and Edden [1973], and found that the difference between the different treatments is very small, less than 0.1% for  $\alpha_p/\bar{B}$  and 0.1° for  $\varphi_p$ .

In the first step of fitting the joint model of equation (1), the linear trend ( $\beta_2$ ) and the parameters ( $\beta_3$  and  $\beta_4$ ) of the nodal cycle (and the perigean cycle for  $N_2$ ) were estimated. In next step, if the linear trend ( $\beta_2$ ) is not significantly different from zero at the 95% confidence level, the model of equation (1) was reprocessed by omitting the linear trend, while the model was reduced to the linear trend fitting only if the nodal cycle ( $\beta_3$

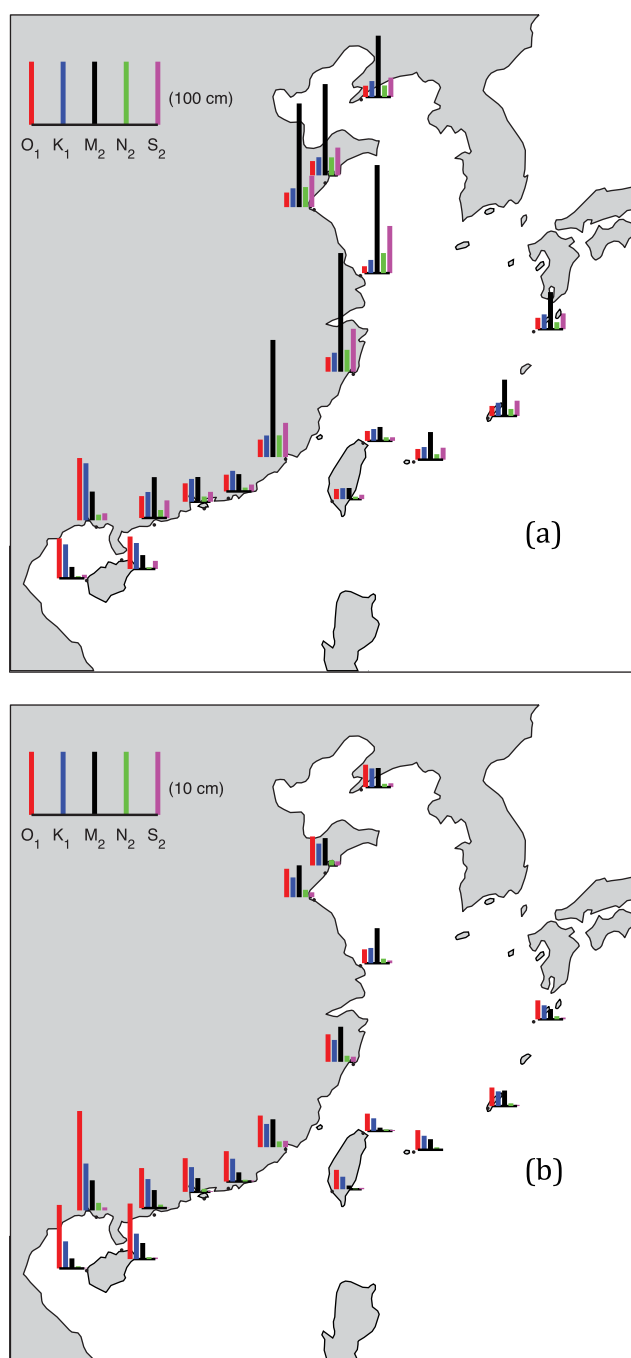
and  $\beta_4$ ) (and the perigean cycle for  $N_2$ ) is not statistically significant. The uncertainty in the trend assessment due to errors in the tidal parameters each year was also considered. The linear trend is treated as valid only when the change is still significant when the errors of the series of estimated parameters are taken into account.



**Figure 2.** Phase differences and normalized amplitudes relative to the equilibrium tide for  $K_2$ ,  $S_2$ ,  $M_2$ , and  $N_2$  at Xiamen in 1990. Black dots present the observed values, while the dashed line is the best fit function connecting values of  $K_2$ ,  $M_2$ , and  $N_2$ . The red dot is the interpolated value of gravitational  $S_2$  on the fitted line.

### 2.3. Radiational Component of $S_2$

For  $S_2$ , we separate the response of sea level to radiational forcing from the response to gravitational forcing using the empirical method suggested by Zetler [1971]. The method was devised based on the “credo of smoothness” [Munk and Cartwright, 1966] which leads to the admittances of tidal constituents within a narrow frequency band being regarded as similar. As a demonstration, Figure 2 shows the phase differences and the ratios



**Figure 3.** (a) Maps of the mean amplitudes and (b) amplitudes of 18.61 year variations for major tidal constituents  $O_1$ ,  $K_1$ ,  $M_2$ ,  $N_2$ , and  $S_2$ . The corresponding uncertainty in each value is provided in the supporting information Tables S1–S5.

The mean values ( $\bar{B}$ ), nodal modulation amplitudes ( $\alpha_{N'}$ ), and linear trends ( $\beta_2$ ) in the tidal constants as estimated by equation (1) are mapped in Figures 3 and 4. The estimation parameters of equation (1) along with their error bars are provided in the supporting information Tables S1–S5.

### 3.1. The $O_1$ and $K_1$ Components and Their Changes

The mean amplitude ( $\bar{B}$ ) of the main diurnal constituents  $O_1$  and  $K_1$  is in the range 11–98 cm and 16–90 cm, respectively (Figure 3a). The largest values found in the Gulf of Tonkin (Haikou, Dongfang, and Beihai) have

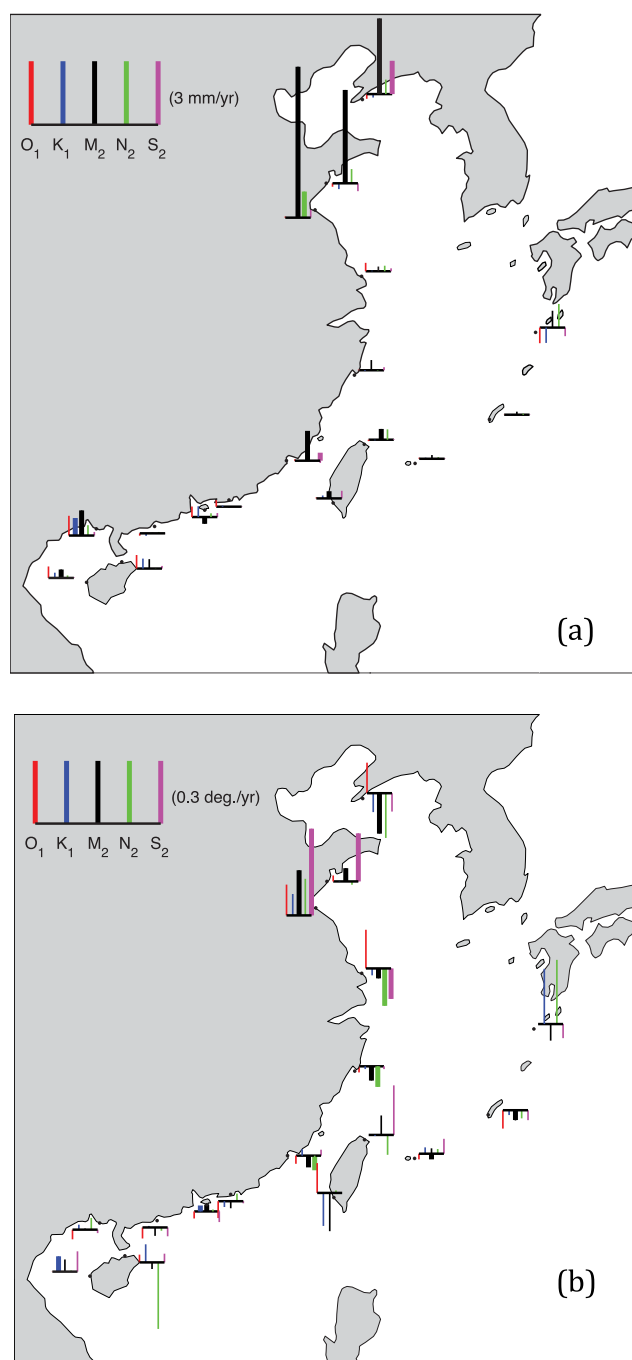
between the observed and the equilibrium amplitudes (normalized amplitudes) at Xiamen in 1990. The phase difference of  $N_2$ ,  $M_2$ ,  $S_2$ , and  $K_2$  can be plotted versus a function of frequency by the equilibrium tidal theory. Then, a smooth function of frequency, empirically fitted to the phase differences of  $N_2$ ,  $M_2$ , and  $K_2$ , is employed to interpolate to the phase of the gravitational component of  $S_2$  (Figure 2, top). Similarly, another function is used to fit the ratios of the observed amplitude over the equilibrium amplitude for  $N_2$ ,  $M_2$ , and  $K_2$  (Figure 2, bottom). The interpolated ratio at the frequency of  $S_2$  and the equilibrium amplitude of  $S_2$  then gives the amplitude of the gravitational component  $S_2$ . Subtracting the gravitational component of  $S_2$  vectorially from the observed  $S_2$  furnishes the radiational component of  $S_2$ . This calculation is performed separately for every year of data.

In the above process, the observed parameters of  $N_2$ ,  $M_2$ , and  $K_2$  are treated as the purely gravitational components because the radiational forcing has no influence on the first two constituents and is negligible in the latter [Chapman and Lindzen, 1970; Zetler, 1971]. Note also that the 18.61 year cycle is removed from the four involved constituents before the calculation is made to avoid the nodal cycle of the lunar constituents influencing the interpolated gravitational  $S_2$ .

### 3. Results

Five major tidal constituents ( $O_1$ ,  $K_1$ ,  $M_2$ ,  $N_2$ , and  $S_2$ ) are analyzed.





**Figure 4.** (a) Maps of linear trends of tidal amplitude and (b) phase lag for major tidal constituents  $O_1$ ,  $K_1$ ,  $M_2$ ,  $N_2$ , and  $S_2$ . The thin bars indicate the trends that do not pass the significance test as described in section 2.2. The corresponding uncertainty in each value is provided in the supporting information Tables S1–S5.

tively) falls into the confidence limits of the observed values ( $\alpha_N$ ) at all stations, except at Shanwei where the observed  $O_1$  modulation is slightly higher than the predicted by  $0.4^\circ$ .

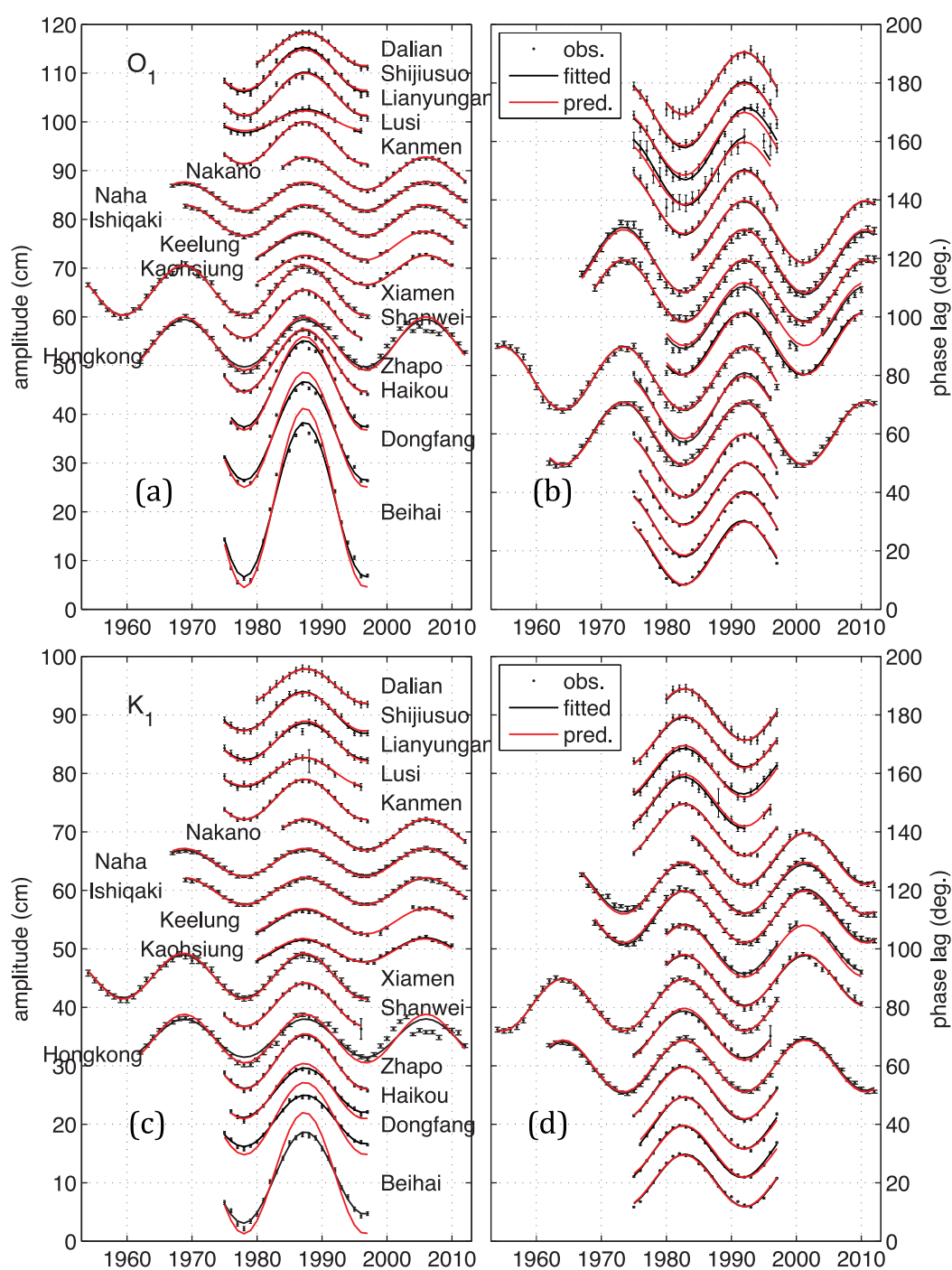
There is no significant trend found in either the amplitude or phase lag of  $O_1$  (Figure 4). The  $K_1$  amplitude has a significant trend of  $0.8 \pm 0.3$  mm/yr at Beihai, and the phase lag shows a significant trend at Hongkong and Dongfang, with a small magnitude of  $0.03 \pm 0.01^\circ/\text{yr}$  and  $0.07 \pm 0.05^\circ/\text{yr}$ , respectively.

been indicated to be caused by resonance [Zu *et al.*, 2008; Green, 2010]. The nodal modulation ( $\alpha_N$ ) is 2.2–15.9 cm for  $O_1$  and 2.0–7.4 cm for  $K_1$  (Figure 3b). In the Gulf of Tonkin, the nodal modulation of  $O_1$  is the strongest signal among the nodal parts of all tidal constituents.

The estimation model accounts for more than 90% of the variance of the  $O_1$  and  $K_1$  amplitudes at all the stations, except at Hongkong for  $K_1$  (82%) (Figures 5a and 5c). There is no phase difference between the theoretical estimate and the estimation model within the range of uncertainty.

The ratio of the observed nodal amplitude over the mean tidal amplitude ( $\alpha_N/\bar{B}$ ) is in agreement with the ratio predicted by the equilibrium theory (18.7% and 11.5% for  $O_1$  and  $K_1$ , respectively) at most stations. However, at Hongkong, Dongfang, and Beihai the observed ratio is significantly lower than the theoretically predicted, with values of  $16.7 \pm 1.9\%$ ,  $16 \pm 2\%$ , and  $16 \pm 2\%$  for  $O_1$  and  $9 \pm 1\%$ ,  $8.3 \pm 0.6\%$ , and  $8.2 \pm 0.5\%$  for  $K_1$ , respectively. At Beihai, the difference between the predicted and the observed amplitudes is up to 1 cm for  $O_1$  and 3 cm for  $K_1$ .

The estimation model accounts for at least 95% of the variance of the phase lag at all stations (Figures 5b and 5d). The predicted amplitude of the nodal cycle of the phase lag ( $10.8^\circ$  and  $8.9^\circ$  for  $O_1$  and  $K_1$ , respec-

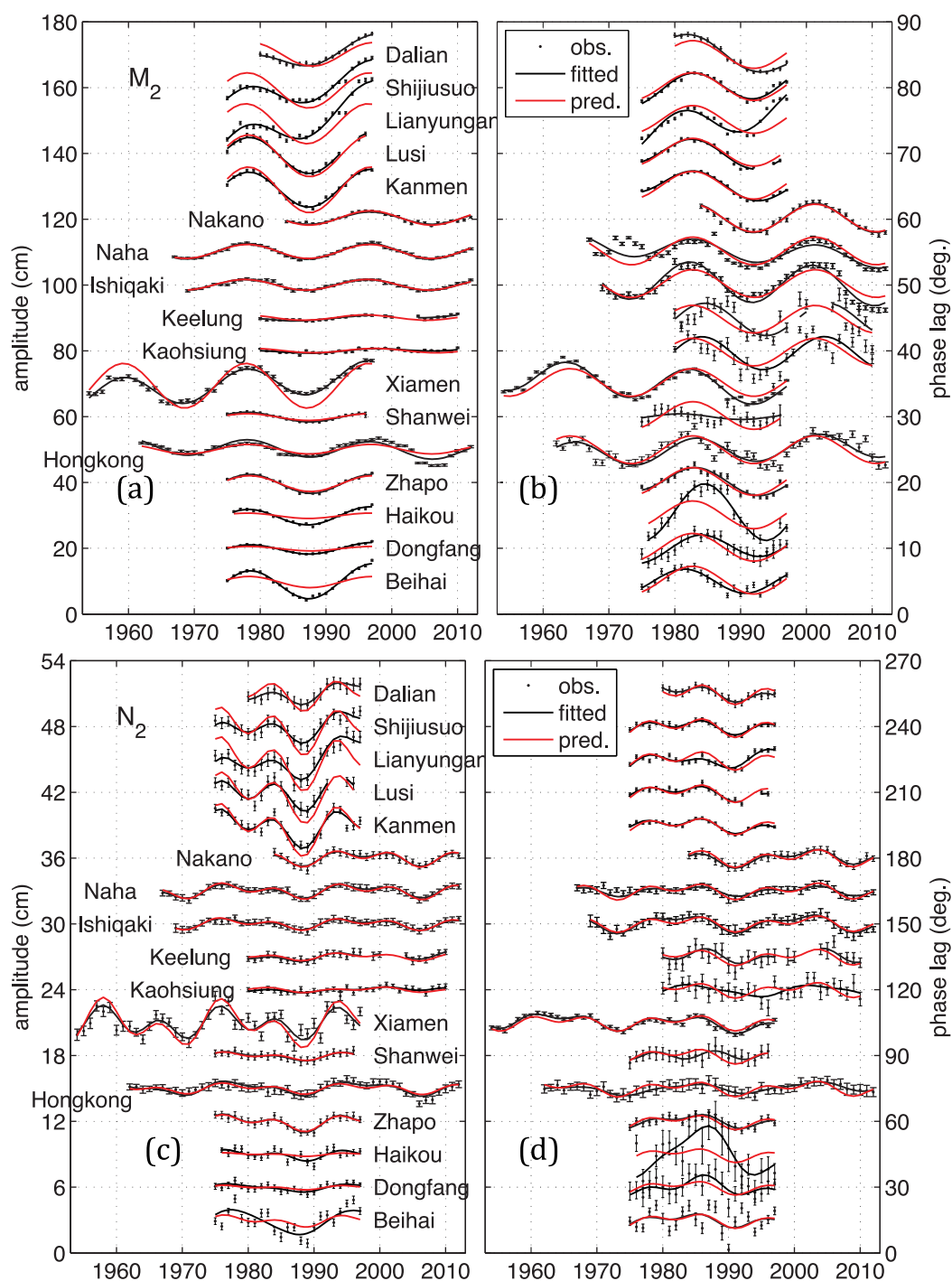


**Figure 5.** (left) Time series of tidal amplitude and (right) phase lag for major lunar constituents (a and b)  $O_1$  and (c and d)  $K_1$ . Black dots present annual values with error bars at 95% confidence level obtained from the harmonic analysis of each 1 year of hourly data. Black and red solid lines are the best fitted curve and theoretical nodal modulation, respectively. Note that the series have been offset for display. Parameters of the best estimations (black solid lines) are presented in the supporting information Tables S1 and S2.

### 3.2. The $M_2$ Component and Its Changes

$M_2$  is the largest tidal constituent along the northern coasts, from Dalian to Xiamen, with the highest amplitude ( $\bar{B}$ ) of 188 cm at Kanmen (Figure 3a) and small values at the southern stations and the islands. The  $M_2$  amplitude at Xianmen (184 cm) is significantly higher than that at the neighboring stations, probably due to wave reflection of the southward propagating tidal wave due to the deep trench in the southern Taiwan





**Figure 6.** Same as Figure 5, but for (a and b)  $M_2$  and (c and d)  $N_2$ . Note that for  $N_2$ , the 8.85 year perigean cycle is also involved. Parameters of the best estimations (black solid lines) are listed in the supporting information Tables S3 and S4.

Strait [Jan *et al.*, 2004]. The nodal cycle values ( $\alpha_N$ ) are in range 0.5–5.6 cm, with the highest and lowest values at Kanmen and the Taiwan Island, respectively.

The estimation model accounts for more than 91% of the variance in the  $M_2$  amplitude at all stations, except at Keelung, Kaohsiung, and Hongkong (Figure 6a) where the variance accounted for is 87%, 57%, and 76%, respectively. The low values of  $M_2$  amplitude at the first two stations and the reduction of the  $M_2$  amplitude between 2003 and 2007 at Hongkong (which appear suspect) are associated with the reduced amount of the variance accounted for.

The nodal amplitude ratio of the  $M_2$  amplitude ( $\alpha_N/\bar{B}$ ) is smaller by 0.1–1% (the absolute difference between two percentage values) than that estimated from the equilibrium theory (3.7%) at eight stations in the north of the region (Figure 6a). At the six southernmost stations and Naha, the observed ratios are higher than the expected ratio by 0.4–8.6%. The biggest underestimation by the theory occurs at Haikou,  $\sim 3$  cm in amplitude. Thus, the equilibrium theory generally overestimates the nodal modulation of the  $M_2$  amplitude in the north but underestimates it in the south.

The percentage of variance accounted for by the estimation model for phase lag is 95% at the stations of the northern mainland coast and 74% at the other stations where low amplitude values are found (Figure 6b). The observed values of the nodal amplitude of the  $M_2$  phase lag ( $\alpha_N$ ) are consistent with the theoretically estimated value of  $2.1^\circ$  at 11 of the 17 stations. However, values 0.1– $1.1^\circ$  lower are found at Kanmen, Naha, and Shanwei, and values 0.1– $1.7^\circ$  higher at Ishiqaki, Xiamen, and Haikou.

The agreement between the estimated and predicted time dependence for the nodal variations of the semidiurnal constituents is worse than that for the diurnal constituents, probably because the nodal signal for modulations of the semidiurnal tides is weaker and the linear trends are larger.

The  $M_2$  amplitude has significant trends at nine stations (Figure 4a). These trends are mostly positive. They are higher at Dalian, Shijiusuo, and Lianyungang with values of  $3.6 \pm 0.8$  mm/yr,  $4.4 \pm 0.5$  mm/yr, and  $7.1 \pm 0.9$  mm/yr, respectively, lower at Xiamen and Beihai with values of  $1.4 \pm 0.2$  mm/yr and  $1.2 \pm 0.3$  mm/yr, respectively, small at Keelung, Kaohsiung, and Dongfang with 0.3–0.5 mm/yr, and negative at Hongkong with  $-0.3 \pm 0.2$  mm/yr.

Most tide gauges on the mainland coast have observations for the period 1975–1997. During that period, the trend at Hongkong is  $0.5 \pm 0.2$  mm/yr. No significant difference in the trends between the common period 1975 and 1997 and the extended period are found at Keelung and Kaohsiung. Thus, the negative trends at Hongkong are due to changes before 1975. We conclude that the  $M_2$  amplitude has been increasing along the Chinese coasts between 1975 and 1997, with high rates in the Bohai and Yellow Seas.

There are nine stations with significant trends in the  $M_2$  phase lag, three stations showing positive trends, and six stations showing negative trends (Figure 4b). Five of the nine stations also indicate significant trends in the  $M_2$  amplitude: Dalian, Shijiusuo, Lianyungang, Xiamen, and Hongkong. The higher trends in the  $M_2$  amplitude (over 1.0 mm/yr) coincide with significant changes in the  $M_2$  phase lag.

### 3.3. The $N_2$ Component and Its Changes

The mean  $N_2$  amplitude ( $\bar{B}$ ) is 15.5 cm on average, with higher values between 18.4 and 34.8 cm along the northern mainland coast, from Dalian to Xiamen, and smaller values between 2.6 and 12.8 cm in the off-shore islands and the South China Sea (Figure 3a). The average nodal and perigean modulation amplitudes ( $\alpha_N$  and  $\alpha_P$ ) are 0.56 and 0.45 cm, respectively, much smaller than the nodal modulations in the other main lunar constituents (Figure 3b). At Dongfang and Beihai, the perigean cycle of  $N_2$  is statistically insignificant.

The estimation model accounts on average for 76% of the  $N_2$  amplitude variance (Figure 6c). The estimation performance is worse in the south where the signal is weaker. The nodal cycle explains on average 17% more variance in the  $N_2$  amplitude than the perigean cycle does at most stations, except at Lusi, Kanmen, and Xiamen where the perigean modulation explains more.

The observed ratio of nodal modulation amplitude ( $\alpha_N/\bar{B}$ ) agrees with the expected value of 3.7% at 11 stations, but is significantly lower at Lusi, Kanmen, and Xiamen by 0.1–0.7% and higher at Hongkong, Dongfang, and Beihai by 1–2.5%. The discrepancy from the theoretical expectation presents a similar spatial pattern as for  $M_2$  with slight underestimations in the north but with significant overestimations in the South China Sea. The observed ratio of the perigean cycle ( $\alpha_P/\bar{B}$ ) is around 3.4% at all stations, except at Naha and Ishiqaki. The observed perigean ratio is lower than the predicted ratio from equation (4) in the north, from Dalian to Ishiqaki by 0.2–1.7%, but consistent with the predicted ratio in the south.

The nodal cycle in the  $N_2$  phase lag is significant at 16 stations except at Beihai, while the perigean cycle is significant at 13 stations except at Kaohsiung, Haikou, Dongfang, and Beihai. The joint estimation model accounts for 67.5% of the variance on average. The nodal cycle explains on average 14.8% more of the variance than the perigean cycle does.

**Table 2.** Gravitational and Radiational Components of  $S_2$ <sup>a</sup>

Station	Amplitude (cm)				Phase (°)			
	Total $S_2$	Gravitational Component $S_2$	Radiational Component $S_2$	Ratio of Radiational Over Gravitational	Total $S_2$	Gravitational Component $S_2$	Radiational Component $S_2$	Difference
Dalian	30.8 ± 0.4	33.6 ± 1.3	4.3 ± 1.1	0.13 ± 0.04	100.2 ± 0.8	94.9 ± 2.3	231.5 ± 16.2	136.7 ± 18.6
Shijiusuo	43.9 ± 0.5	50.1 ± 1.2	8.4 ± 1.1	0.17 ± 0.03	324.6 ± 0.6	318.0 ± 1.6	100.1 ± 8.3	142.1 ± 9.9
Lianyungang	49.7 ± 0.5	56.4 ± 1.4	9.0 ± 1.3	0.16 ± 0.03	343.6 ± 0.5	337.6 ± 1.6	120.9 ± 8.7	143.3 ± 10.4
Lusi	74.8 ± 0.5	81.6 ± 1.4	14.7 ± 1.3	0.18 ± 0.02	156.5 ± 0.4	147.2 ± 1.0	269.0 ± 4.9	121.9 ± 5.9
Kanmen	68.0 ± 0.4	73.1 ± 0.9	8.9 ± 0.9	0.12 ± 0.01	54.7 ± 0.3	48.8 ± 0.8	176.9 ± 5.7	128.1 ± 6.6
Nakano	25.3 ± 0.3	26.8 ± 0.8	3.5 ± 0.7	0.13 ± 0.03	321.3 ± 0.7	314.6 ± 1.7	73.6 ± 12.5	119.0 ± 14.2
Naha	24.1 ± 0.3	25.5 ± 0.7	3.1 ± 0.6	0.12 ± 0.03	327.5 ± 0.6	321.4 ± 1.6	82.8 ± 12.1	121.5 ± 13.7
Ishiqaki	19.0 ± 0.3	19.9 ± 0.8	2.4 ± 0.7	0.12 ± 0.04	329.2 ± 0.9	322.9 ± 2.2	78.0 ± 18.7	115.1 ± 20.9
Keelung	5.5 ± 0.3	5.5 ± 0.7	1.1 ± 0.5	0.19 ± 0.10	40.6 ± 3.2	36.3 ± 8.0	152.6 ± 78.1	116.4 ± 86.1
Kaohsiung	6.9 ± 0.2	7.0 ± 0.6	5.5 ± 2.0	0.78 ± 0.31	351.6 ± 1.5	208.7 ± 97.1	187.6 ± 101.0	339.0 ± 198.0
Xiamen	53.7 ± 0.4	60.8 ± 1.2	9.9 ± 1.1	0.16 ± 0.02	163.8 ± 0.4	157.2 ± 1.3	297.9 ± 6.6	140.7 ± 7.9
Shanwei	11.0 ± 0.3	12.0 ± 0.8	1.4 ± 0.6	0.12 ± 0.06	35.9 ± 1.8	34.6 ± 4.0	200.0 ± 49.0	165.4 ± 53.0
Hongkong	15.6 ± 0.3	17.3 ± 0.8	2.0 ± 0.6	0.12 ± 0.04	26.9 ± 1.2	24.4 ± 2.5	182.6 ± 25.1	158.2 ± 27.7
Zhapo	27.9 ± 0.3	33.3 ± 0.9	9.9 ± 0.8	0.30 ± 0.03	92.8 ± 0.5	77.3 ± 1.7	207.7 ± 4.8	130.5 ± 6.5
Haikou	13.0 ± 0.2	28.2 ± 0.8	16.0 ± 0.7	0.57 ± 0.07	81.4 ± 1.0	66.9 ± 1.6	235.0 ± 2.4	168.2 ± 4.0
Dongfang	5.6 ± 0.3	10.3 ± 0.7	6.7 ± 0.6	0.65 ± 0.17	237.8 ± 2.7	201.0 ± 3.9	330.5 ± 70.6	129.5 ± 74.5
Beihai	11.1 ± 0.3	29.5 ± 0.8	18.8 ± 0.7	0.64 ± 0.10	341.7 ± 1.4	10.2 ± 1.6	197.7 ± 2.2	187.5 ± 3.8

<sup>a</sup>Note that the nodal cycle of the tidal constituents involved in the estimation has been removed.

Excluding stations where the nodal cycle is not statistically significant, the observed nodal amplitude of the  $N_2$  phase lag is in agreement with the theoretically predicted  $2.1^\circ$  at most stations (12 stations), except at Ishiqaki, Xiamen, and Haikou where the theoretical estimate underestimates the phase lag variations by  $0.1$ – $4.3^\circ$  and at Naha where it overestimates the phase lag variations by  $0.1^\circ$  (Figure 6d and see supporting information Table S4b for more details). The significant perigean modulations of the phase lag are all around  $1.7^\circ$  except at Hongkong, and are lower than the perigean modulation suggested by the equilibrium theory.

The only significant trend in the  $N_2$  amplitude is found at Lianyungang, with an increase of  $1.2 \pm 0.4$  mm/yr (Figure 4a). Linear trends in the  $N_2$  phase lag are found at Lusi, Kanmen, and Xiamen, with rates of  $-0.2 \pm 0.1^\circ/\text{yr}$ ,  $-0.09 \pm 0.05^\circ/\text{yr}$ , and  $-0.07 \pm 0.03^\circ/\text{yr}$ , respectively (Figure 4b). Note that where the  $N_2$  constants linearly change the  $M_2$  parameters also change.

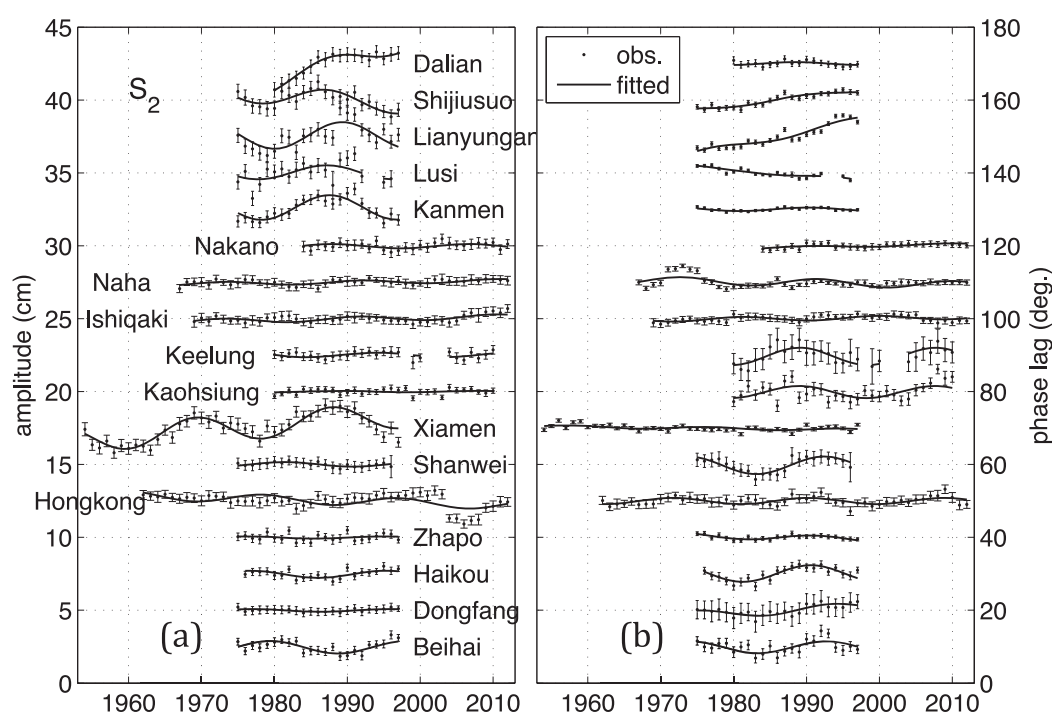
### 3.4. The $S_2$ Component and Its Changes

$S_2$  shows a spatial pattern similar to  $M_2$ . The mean amplitude ( $\bar{B}$ ) has higher values of 30.8–74.8 cm along the northern mainland coast, and lower values of 5.5–27.8 cm on the south coast and at the offshore islands (Figure 3a). The highest and lowest values of  $\bar{B}$  occur at Lusi and Keelung, respectively.

The radiational part of the  $S_2$  amplitude is 7.4 cm on average, with the highest values of  $14.7 \pm 1.3$  cm,  $16.0 \pm 0.7$  cm, and  $18.8 \pm 0.7$  cm found at Lusi, Haikou, and Beihai, respectively (Table 2). From Dalian to Zhapo except at Kaohsiung, the ratio of the radiational amplitude over the gravitational amplitude ranges 0.12–0.30 with an average of 0.16, and the phase differences between the two components are between  $115^\circ$  and  $165^\circ$  with an average of  $134^\circ$ . These results for amplitude and phase are consistent with estimates for the UK and US coasts [Zetler, 1971; Amin, 1982]. However, in the Gulf of Tonkin (at Haikou, Dongfang, and Beihai) and at Kaohsiung, the amplitude ratio goes up to 0.57–0.78, and the phase difference is nearly  $180^\circ$ .

In Zetler's method, the accuracy of the estimated values of the  $S_2$  radiational component depends highly on the uncertainties in the measured values of  $K_2$ ,  $M_2$ ,  $S_2$ , and  $N_2$ . When the tidal estimation errors of these constituents are taken into account, however, the ratios of the radiational amplitude over the gravitational amplitude of  $S_2$  in the Gulf of Tonkin (at Haikou, Dongfang, and Beihai) still remain much larger than the values in other regions (Table 2). Thus, we conclude that the radiational forcing is strong in this area of small semidiurnal tides.

Interannual changes in the  $S_2$  amplitude are significantly correlated with the 18.61 year nodal cycle at 12 stations, except at Nakano, Naha, Kaohsiung, Zhapo, and Dongfang (Figure 7a). The nodal amplitude ( $\alpha_N$ ) is about 0.5 cm on average, with values higher than 0.5 cm on the northern mainland coast from Dalian to



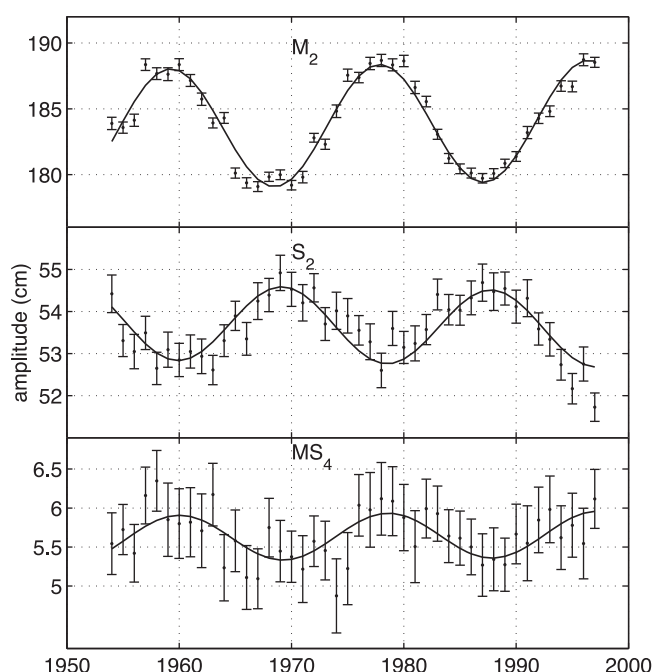
**Figure 7.** Same as Figure 5, but for  $S_2$ . Parameters of the best estimations (black solid lines) are presented in the supporting information Table S5.

Xiamen. The largest changes occur at Xiamen and Lianyungang with values of  $0.9 \pm 0.2$  cm and  $0.9 \pm 0.4$  cm, respectively. The ratios of the nodal amplitude over the  $S_2$  amplitude ( $\alpha_N/\bar{B}$ ) are 1.8% on average. The changes in the  $S_2$  phase lag also show variation with the 18.61 year cycle at 13 stations, except at Dalian, Shijiusuo, Nakano, and Xiamen (Figure 7b). The nodal cycle of the  $S_2$  phase lag is  $1.3^\circ$  on average, with a maximum value of  $2.4^\circ$  at Shanwei. The estimation model can overall account for 57% of the variance both in the  $S_2$  amplitude and phase lag.

Nodal modulation of the  $S_2$  constituent has also been found at the UK coasts [Amin, 1983], the Gulf of Maine [Müller, 2011], and other coastlines with primarily semidiurnal tides [Woodworth, 2010], and has been attributed to shallow-water nonlinear interactions between  $S_2$  and  $M_2$ . The nonlinear interactions between the two tidal constituents take place via their currents and the effect will also be larger when the elevations are larger in their nodal cycle. The currents will dissipate most when  $S_2$  and  $M_2$  are in phase [Parker, 2007] due to bottom friction that is approximately proportional to the square of the combined current speed [see Pugh and Woodworth, 2014, section 6.2.1]. The interactions result in a shallow-water tidal constituent  $MS_4$  [Pugh and Woodworth, 2014, Table 4.4] that will remove energy from both  $M_2$  and  $S_2$ . Consequently, at nodal maximum the  $M_2$  amplitude will tend to be slightly reduced compared to equilibrium expectations, while the  $S_2$  amplitude will also be reduced compared to its average.  $S_2$  amplitude will, therefore, appear in 1 year analyses such as those performed here to have a nodal variation out-of-phase with  $M_2$ , as demonstrated by observations at Xiamen (Figure 8). In addition, at  $M_2$  nodal maximum we expect the  $MS_4$  term to also be largest.

In our data set, we find that  $MS_4$  has an amplitude of 2.3 cm on average along the coast, with higher values in the north where the nodal changes of the  $S_2$  amplitude are larger. At Xiamen and Lianyungang, where the average  $MS_4$  amplitude is 5.6 cm (Figure 8) and 7.9 cm, respectively, this constituent is seen to have a nodal cycle that is in phase with that of  $M_2$ , consistent with equilibrium expectations [Pugh and Woodworth, 2014, Table 4.4].

Where the nodal cycle in  $S_2$  is statistically significant, this signal is removed from the linear trend assessment. The  $S_2$  trends are significant at Dalian and Xiamen with  $1.6 \pm 0.3$  mm/yr and  $0.4 \pm 0.1$  mm/yr, respectively (Figure 4a). At these two stations, when the gravitational and radiational components of  $S_2$  are separated for every year of the observed  $S_2$  values, the gravitational component of  $S_2$  has significant trends



**Figure 8.** Amplitudes for  $M_2$  and  $S_2$  constituents along with the shallow-water constituent  $MS_4$  at Xiamen. Note that the tidal amplitudes are the values after the linear trend has been removed.

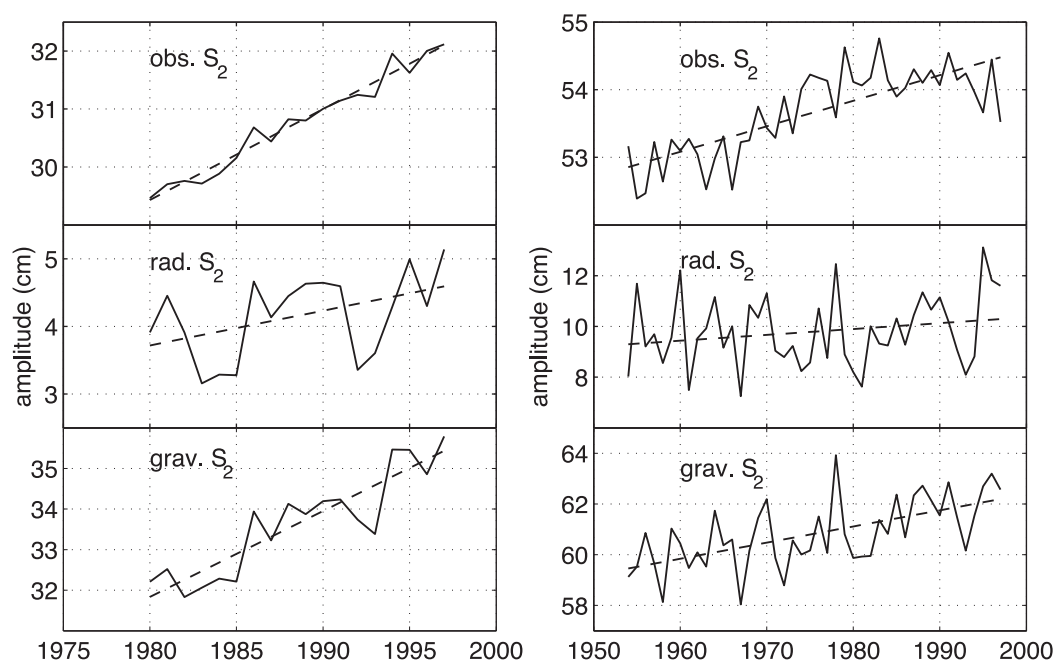
of  $2.1 \pm 0.6$  mm/yr and  $0.6 \pm 0.3$  mm/yr, respectively, whilst no significant trend was found for the radiational component at 95% confidence level (Figure 9). Significant trends in the  $S_2$  phase lag are found at Shijiusuo, Lianyungang, and Lusi, with values of  $0.23 \pm 0.05^\circ/\text{yr}$ ,  $0.42 \pm 0.08^\circ/\text{yr}$ , and  $-0.15 \pm 0.05^\circ/\text{yr}$ , respectively (Figure 4b). The trends in the  $S_2$  phase lag are found to be consistent with trends in the gravitational component as well. Therefore, we conclude that the observed linear trends in the  $S_2$  parameters are due to the changes in the gravitational component.

## 4. Discussion

### 4.1. Possible Causes of Discrepancies in the Nodal Modulations

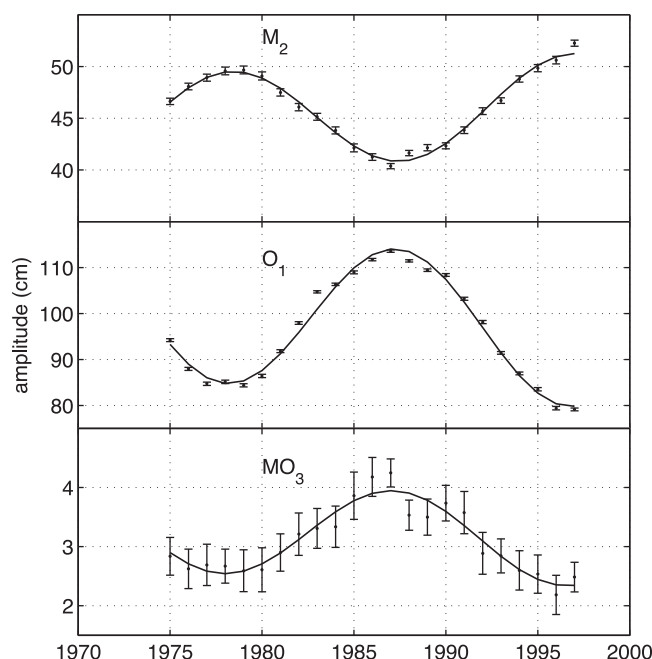
We found that the equilibrium theory tends to over-predict the

nodal modulations of the semidiurnal tidal amplitudes of  $M_2$  and  $N_2$  in the Bohai, Yellow, and East China Seas. Over-prediction of the nodal modulations of  $M_2$  by the equilibrium theory has been observed in the British Isles [Amin, 1983, 1985; Woodworth *et al.*, 1991], the Bay of Fundy and Gulf of Maine [Ku *et al.*, 1985; Ray, 2006; Müller, 2011] and western Australian coasts [Amin, 1993; Woodworth, 2010]. As mentioned above, modeling studies suggest that tidal friction with the seabed is the main cause of the reduction of the nodal modulation at semidiurnal frequencies across the North-West European Continental Shelf including the



**Figure 9.** Amplitudes of the total (observed), radiational and gravitational  $S_2$  at (left) Dalian and (right) Xiamen, along with their linear trends (dashed line). Note that the observed  $S_2$  values are the values after the estimated nodal cycle has been subtracted.





**Figure 10.** Amplitudes for  $M_2$  and  $O_1$  constituents along with the shallow-water constituent  $MO_3$  at Beihai. Note that the tidal amplitudes are the values after the linear trend has been removed.

North Sea [Pingree and Griffiths, 1987], and in the Bay of Fundy and Gulf of Maine particularly under tidal resonance [Ku *et al.*, 1985]. The Bohai, Yellow, and East China Seas have water depths less than 100 m and a continental shelf with widths of several hundred kilometers (Figure 1a). Thus, bottom friction effects may also be responsible for the mismatch between observed and theoretically predicted nodal variations in this area too.

The nodal modulation of  $M_2$  and  $N_2$  amplitudes is underestimated by the equilibrium theory in the South China Sea. Pingree and Griffiths [1987] suggested that the difference in the location of the tidal amphidromes of the nodal and the main  $M_2$  components and the associated differences in the bottom friction may be the reason for the amplified nodal modulations observed in the western Irish Sea. However, because

there is no amphidrome for the semidiurnal constituents in the region of the South China Sea under study here [Fang *et al.*, 1999; Hu *et al.*, 2001], similar mechanisms are not likely to be relevant in the present case.

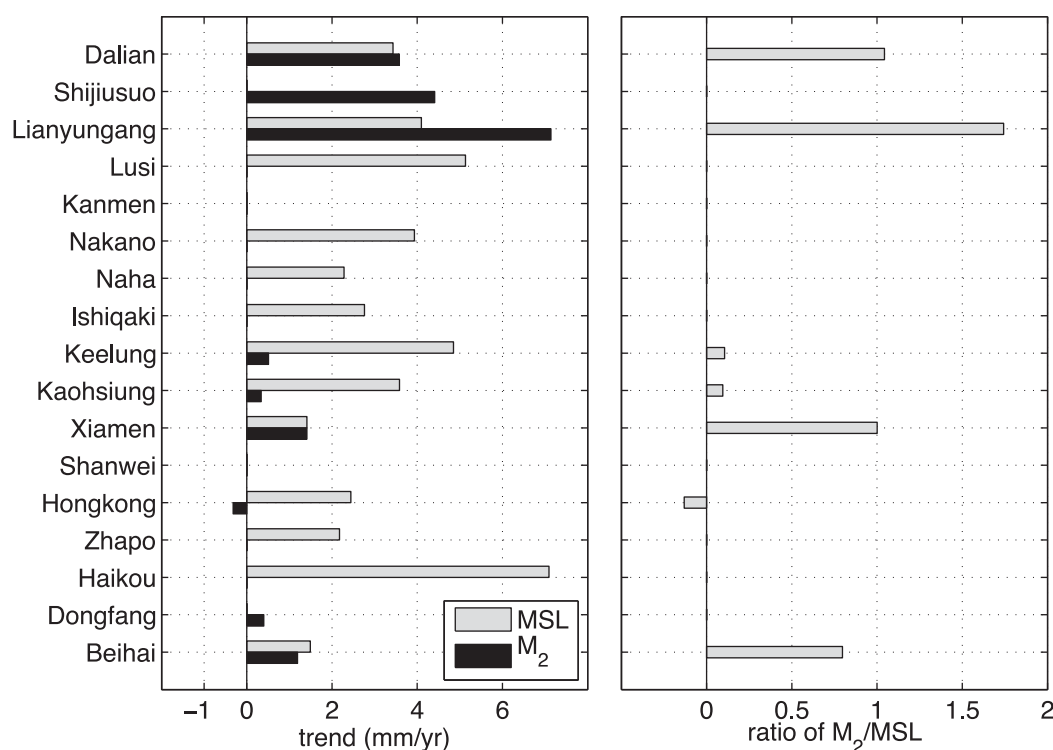
We suggest that shallow-water interactions between the semidiurnal and diurnal constituents can be responsible for the observed discrepancies between the predicted and observed nodal modulations of the semidiurnal tides in the south. In the South China Sea, especially in the Gulf of Tonkin, the diurnal constituents of  $O_1$  and  $K_1$  are the dominating tidal signals, and the amplitudes of both constituents in the equilibrium tide have nodal variations that are out-of-phase with those in  $M_2$ . This can be seen clearly in the data from Beihai, for example (Figure 10). If we invoke a similar interaction mechanism as above for  $M_2$  and  $S_2$  in a semidiurnal area, the interactions in this diurnal area will result in shallow-water constituents  $MO_3$  and  $MK_3$ . In the case of  $O_1$  interacting with  $M_2$ , at  $O_1$  nodal maximum, in addition to an increased  $MO_3$  amplitude (Figure 10, bottom), there will be a slightly reduced  $O_1$  amplitude compared to equilibrium expectations and also reduced  $M_2$  amplitude. Similarly, at  $O_1$  nodal minimum there will be a slightly larger  $M_2$  amplitude. Because the nodal variations of  $O_1$  and  $M_2$  are out-of-phase, the interactions serve to amplify  $M_2$ 's own nodal variation.

The shallow-water constituents  $MO_3$  and  $MK_3$  are significant throughout the South China Sea, with average values of 1.6 cm and 1.8 cm, respectively, supporting our suggestion of the importance of shallow-water interactions in modifying the nodal behavior of  $M_2$  amplitude in this area dominated by diurnal tides.

The equilibrium nodal theory works well for  $O_1$  and  $K_1$  at most stations on the Chinese coast. This is consistent with what has been found in other regions [Jay, 2009; Shaw and Tsimplis, 2010; Woodworth, 2010; Torres and Tsimplis, 2011]. However, at some stations in the South China Sea, the nodal modulations are significantly overestimated by the theory. By contrast, altimetry data indicate that the observed nodal cycles in the open areas of the South China Sea are consistent with the equilibrium predictions [Cherniawsky *et al.*, 2010, see their Table 2]. The agreement between the theoretical estimates and the altimetry analysis at the open sea [Cherniawsky *et al.*, 2010] is consistent with the view that the deviation of the equilibrium theory from tide-gauge observations occurs primarily near the coasts, and is mainly due to interactions between the various tidal constituents.

The nodal amplitudes of the shallow-water constituents  $M_4$ ,  $MS_4$ ,  $MK_3$ , and  $MO_3$  are less than 1 cm for all stations, except for  $M_4$  at Lianyungang ( $1.5 \pm 0.1$  cm) and for  $MK_3$  and  $MO_3$  at Haikou ( $1.2 \pm 0.1$  cm and





**Figure 11.** (left) Comparisons of significant linear trends in mean sea level (MSL) with those in the  $M_2$  amplitude, (right) and the ratio between the two trends. Nonexistence of values at some stations indicates that the linear trends in either MSL or  $M_2$  amplitude do not pass the significance test with 95% confidence level.

$1.0 \pm 0.2$  cm, respectively). For these three exceptions, the ratio of nodal modulation to the mean value is  $12.7 \pm 1.5\%$ ,  $53.7 \pm 14.8\%$ , and  $56.6 \pm 22.0\%$ , respectively, which exceeds what is expected from the equilibrium theory [Pugh and Woodworth, 2014, see their Table 4.4].

#### 4.2. Possible Causes of the Linear Trends

The observed trends in the  $M_2$  constituent are problematic. Trends in tidal constituents have been identified in modeling studies under the assumption of large mean sea level (MSL) rise of the order of meters [Amin, 1983; Green, 2010; Pickering *et al.*, 2012]. For the Asian coasts, the tidal changes due to MSL rise have been estimated by a numerical model in which the maximum increase of  $M_2$  amplitude was found to be  $\sim 30$  cm on the coasts of China when MSL is raised by 2 m, i.e., 15% of the MSL increase [Pickering, 2014, see his Figures 3.9, 3.10 and Table 3.5]. However, in observations, we find that the changes in the  $M_2$  amplitude do not always correspond to the MSL rise (Figure 11), and the observed trends at some stations are much larger than 15% of those in MSL. In addition, the interannual variability of the  $M_2$  amplitude was found to be uncorrelated with the interannual variability of MSL, both sets detrended (not shown here). Thus, the rates of tidal change due to the MSL rise suggested by numerical models are too small to explain the observed changes.

The rapid evolution of bathymetry in the area of study may provide another explanation for the linear trends in the tidal signal. Numerical experiments indicate that changes in coastline and bathymetry in the Bohai and Yellow Seas can significantly alter the  $M_2$  amplitude [Pelling *et al.*, 2013; Song *et al.*, 2013]. Since the 1950s, significant reclamation of tidal flats has created new land areas of thousands of square km, which have changed the coastline significantly [Li *et al.*, 2004; Wang *et al.*, 2011; Li *et al.*, 2013; Wang *et al.*, 2014]. Three large river estuaries, i.e., the Yellow River, Yangtze River, and Pearl River, bring to the Bohai, East China, and South China Seas, respectively, very large amounts of sediment, which also cause significant changes in the bathymetry [Zhang *et al.*, 2008; Yang *et al.*, 2011; Yu *et al.*, 2011]. In addition, the coastline is exposed to typhoons [Feng *et al.*, 2012; Feng and Tsimplis, 2014] that are able to erode the shoreline and change the bathymetry [Qi *et al.*, 2010; Milliman *et al.*, 2007]. These changes could alter the propagation of

the tidal signal, and thus cause changes in the observed tides, including displacement of the amphidromes. However, the resolution of this issue requires numerical studies that are beyond the scope of this paper.

Finally, as suggested by one reviewer, changes in stratification could present another mechanism. In this region, a strong seasonal cycle of the tides is apparent [Kang *et al.*, 2002; Müller *et al.*, 2014], and could possibly be explained by the changes in stratification and thereby tidal transports. The same effect can also cause long-term changes in the tides if the stratification changes over long timescales due to climate change.

## 5. Conclusions

The spatiotemporal changes of the five main tidal constituents ( $O_1$ ,  $K_1$ ,  $M_2$ ,  $N_2$ , and  $S_2$ ) along the coasts of the China seas and in adjacent seas have been investigated using 17 tide-gauge records spanning the period 1954–2012. The semidiurnal tide  $M_2$  dominates the north coast, whilst the coastline of the South China Sea is dominated by the diurnal tides. The mainland coast has higher tides than the offshore islands.

The 18.61 year nodal modulations of the main lunar constituents were identified in observations and compared with the theoretical predictions based on the tidal potential. The equilibrium theory estimates compare well with the observed nodal changes in the  $O_1$  and  $K_1$  parameters at most stations. However, the equilibrium theory overestimates the nodal modulations of the diurnal tidal amplitudes for the South China Sea. The discrepancy amounts up to 1–3 cm in amplitude.

The equilibrium tidal theory over-predicts the nodal modulations of the  $M_2$  and  $N_2$  amplitudes in the north and under-predicts them in the south. The maximum discrepancy of 3 cm was found in the Gulf of Tonkin. It has been suggested that shallow-water interactions between tidal constituents may be the cause of the discrepancies in the south. We believe this to be a plausible explanation, although it is not a proof and only more extensive measurements and modeling can provide more insight.

The nodal cycle in the  $N_2$  amplitude and phase lag in general accounts for 17% and 15% more variance, respectively, than the perigean cycle does. The impact of perigean cycle is small in the South China Sea.

The interannual changes in the  $S_2$  constituent are correlated significantly with the 18.61 year nodal cycle at most places. Shallow-water nonlinear interactions with  $M_2$  are the suggested explanation.

For  $S_2$ , the contribution from radiational forcing has been separated from that of the gravitational forcing. The ratio of the radiational over the gravitational component is about 0.16 and the phase difference is  $134^\circ$ . These results are in agreement with results in other regions. In areas like the Gulf of Tonkin, where the semidiurnal constituents are small, the ratios obtained reach up to 0.57–0.65.

Linear changes in the amplitude and phase of the various tidal components were also examined. The records at several stations are not very long and, therefore, the linear changes found may not reflect the real long-term trends.  $O_1$  and  $K_1$  were found to be generally stable over the observed period, except at two stations in the South China Sea where small but significant trends were obtained. The main semidiurnal constituents show significant changes. The  $M_2$  amplitude, in particular, increases at 9 of the 17 stations, and the  $N_2$  and  $S_2$  amplitudes increase also at a few stations. The highest changes for  $M_2$ , with rates between 3 and 7 mm/yr, were found in the Bohai and Yellow Seas. Rates of 0.3–1.4 mm/yr were found in the Taiwan Strait. The phase lags of the semidiurnal constituents were found to be changing in time as well, getting smaller at Bohai and East China Seas, but progressively larger in the Yellow Sea.

We found no convincing evidence supporting a link between the linear tidal changes and MSL rise. We suspect changes in tidal wave propagation, due to the rapid evolution of the coastal bathymetry caused by natural and anthropogenic processes, as the main cause for these changes.

Land reclamation along the Chinese coasts has been intensive for the last few decades, and is expected to continue in the future, with even higher intensity. Around 6000 km<sup>2</sup> of land, in terms of coastal reclamations and artificial offshore islands, is planned to be built in the next 10 years [Joss and Molella, 2013; Wang *et al.*, 2014, and references therein]. The significant expansion of land raises serious concerns for potential changes in the tidal environment. Flood risks, which depend on MSL rise and the combination of typhoons and tides [Feng and Tsimplis, 2014], are likely to become more uncertain.

## Acknowledgments

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## Erratum

In the originally published version of this article, there were minor typos in the headings of Table 2 and on top of Figure 10. The figure and the table have since been corrected, and this version may be considered the authoritative version of record.