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Whispering Gallery Mode Resonances from Ge Micro-Disks on Suspended Beams

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2 ABSTRACT

Ge is considered to be one of the most promising materials for realizing full monolithic integration of a light source on a silicon (Si) photonic chip. Tensile-strain is required to convert Ge into an optical gain material and to reduce the pumping required for population inversion. Several methods of strain application to Ge are proposed in literature, of which the use of free-standing beams fabricated by micro-electro-mechanical systems (MEMS) processes are capable of delivering very high strain values. However, it is challenging to make an optical cavity within free-standing Ge beams, and here, we demonstrate the fabrication of a simple cavity while imposing tensile strain by suspension using Ge-On-Insulator (GOI) wafers. Ge micro-disks are made on top of suspended SiO₂ beams by partially removing the supporting Si substrate. According to Raman spectroscopy, a slight tensile strain was applied to the Ge disks through the bending of the SiO₂ beams. Whispering-Gallery-Mode (WGM) resonances were observed from a disk with a diameter of 3 μm, consistent with the finite-domain time-difference simulations. The quality (Q) factor was 192, and upon increasing the pumping power, the Q-factor was degraded due to the red-shift of Ge direct-gap absorption edge caused by heating.

17 **Keywords:** Germanium, Photonics, Photoluminescence, Strain, Micro-cavity, Whispering-Gallery-Mode

1 INTRODUCTION

18 Transmitting uncharged photons, rather than electrons, has an advantage of reducing signal delays by
19 eliminating capacitive coupling, reducing heating effects and therefore total power consumption (Miller,
20 2009; Saito et al., 2014). The use of optical signals is responsible for a rapid growth in long-distance

21 optical data communication technology (Brinkman et al., 2000). The demand for bandwidth is also incre-
22 asing for short distance communications, and Si photonics is providing a novel solution to revolutionize
23 the integration capability by introducing photonic circuitries within the state-of-the-art Complementary
24 Metal-Oxide-Semiconductor (CMOS) foundries (Miller, 2009; Saito et al., 2014). Novel monolithic laser
25 diodes will further accelerate the innovation in terms of cost and yield (Goodman et al., 1984; Saito et al.,
26 2011, 2014). Germanium (Ge) is considered as a promising candidate (Menéndez and Kouvetakis, 2004;
27 Liu et al., 2007, 2009, 2012a; Liu, 2014; Kurdi et al., 2010b; Liang and Bowers, 2010; Michel et al.,
28 2010; Boucaud et al., 2013; Saito et al., 2014), being a group IV material that can acquire a positive opti-
29 cal gain by reducing its pseudo-direct band-gap using tensile-strain and filling the L valleys using heavy
30 n -type doping (Menéndez and Kouvetakis, 2004; Liu et al., 2007, 2009, 2012a; Liu, 2014; Kurdi et al.,
31 2010b; Liang and Bowers, 2010; Michel et al., 2010; Boucaud et al., 2013; Saito et al., 2014). In fact,
32 the positive optical gain (Liu et al., 2009) and lasing by optical pumping (Liu et al., 2010) and electrical
33 pumping (Camacho-Aguilera et al., 2012) were reported in Fabry-Perot (FP) structures. More recently,
34 lasing from a GeSn FP cavity by optical pumping at low temperature was also achieved (Wirths et al.,
35 2015).

36

37 Light emissions from other novel cavities, including micro-rings (Lim et al., 2008), micro-disks
38 (Shambat et al., 2010; Cheng et al., 2011; Ghrib et al., 2013, 2014, 2015), photonic crystals (Ngo
39 et al., 2008; Kurdi et al., 2008; Boztug et al., 2013), and distributed brag reflectors (Saito et al., 2011),
40 have also been investigated. Among them, Ge micro-disks are increasingly gaining attention due to their
41 compact sizes which have advantages for high-density integration, high Quality (Q) factors, enhanced
42 spontaneous emission rate by the Purcell effect (Purcell, 1946), and efficient coupling to waveguides.
43 Direct-gap resonances including FP (Ghrib et al., 2013, 2014, 2015) and Whispering-Gallery Modes
44 (WGM) (Lim et al., 2008; Shambat et al., 2010; Cheng et al., 2011; Ghrib et al., 2013, 2014, 2015)
45 were observed from Ge micro-disks by optical (Ghrib et al., 2013) and electrical (Cheng et al., 2011)
46 carriers injection. WGMs, which have higher Q -factors compared to FP modes, existed for certain disk
47 diameters ranging between $2\ \mu\text{m}$ and $4\ \mu\text{m}$ from intrinsic (Lim et al., 2008; Shambat et al., 2010; Cheng
48 et al., 2011) and doped (Ghrib et al., 2013, 2014, 2015; Xu et al., 2014) Ge. A Q -factor of 620 is reported
49 by (Lim et al., 2008) from optically-pumped intrinsic Ge micro-ring resonators, while Q -factors of doped
50 Ge-on-GaAs micro-disks with reduced interface-defect density was 1350 (Ghrib et al., 2013). The degrada-
51 tion of Q -factor with higher pumping levels is observed, either by optical or electrical carriers injection
52 (Shambat et al., 2010; Cheng et al., 2011). This degradation of Q -factor with pumping prevents lasing,
53 and has to be overcome by further improvements on Ge micro-disk structures, for example, by improving
54 crystalline qualities (Saito et al., 2011, 2014), reducing surface roughness at the edges (Liu et al., 2012b),
55 reducing defect density at the Ge-substrate interface (Nam et al., 2014), optimizing n -doping (Xu et al.,
56 2014), and increasing tensile strain (Liu et al., 2012a; Liu, 2014; Süess et al., 2013).

57

58 In particular, applying tensile strain has a significant impact on transforming Ge into an optical gain
59 medium (Liu et al., 2007; Kurdi et al., 2010b; Suwa and Saito, 2011; Virgilio et al., 2013b,a). The ten-
60 sile strain minimizes the energy difference between direct (Γ) and indirect (L) conduction band minima
61 (de Walle, 1989; Fischetti and Laux, 1996; Wada et al., 2006), which increases the probability of elec-
62 trons' dwelling in the Γ valley (Camacho-Aguilera et al., 2012; Süess et al., 2013; Nam et al., 2013).
63 A tensile strain of 0.2% is inherent in Ge epitaxially grown on a Si substrate due to difference in thermal
64 expansion coefficients (Ishikawa et al., 2003, 2005; Liu et al., 2005; Cannon et al., 2004). In order
65 to enhance the strain further, the use of buffer layers such as $\text{Ge}_x\text{Si}_{1-x}$ (People and Bean, 1986) and
66 $\text{In}_x\text{Ga}_{1-x}\text{As}$ (Bai et al., 2008; Huo et al., 2011) were reported. It is also possible to employ external
67 stressors, such as Si_3N_4 (Ghrib et al., 2012), which is a tempting approach due to its tuneability and
68 compatibility with standard CMOS processes, however, non-uniformity of strain in this case must be
69 addressed (Ghrib et al., 2012, 2013, 2014; Ortolland et al., 2009; Saito et al., 2014). Moreover, suspen-
70 sion or micro-mechanical buckling may be used to impose even higher tensile strain (Jain et al., 2012;
71 Nam et al., 2013; Süess et al., 2013; Sukhdeo et al., 2014). This technique involves the relaxation of a
72 stressed layer upon releasing by under-etching. Uni-axially stressed beams are capable of delivering high

73 strain values, up to 3.1% as reported by (Süess et al., 2013). The transition from the in-direct to the direct
74 band gap structures occurs at 4.7% uni-axial tensile strain (Süess et al., 2013), and the highest uni-axial
75 strain of 5.7% was achieved (Sukhdeo et al., 2014). The use of freestanding beams is a promising approach
76 to apply higher strain (Jain et al., 2012; Nam et al., 2013; Süess et al., 2013; Sukhdeo et al., 2014),
77 however, it is not trivial to make an optical cavity on a fragile beam.

78

79 The purpose of this work is to demonstrate that it is possible to confine the optical mode in a micro-disk
80 optical cavity, compatible with the tensile strain application in a free-standing structure. This is achieved
81 by using Germanium-on-Insulator (GOI) wafers to fabricate Ge micro-disks on top of the buried oxide
82 (BOX). Then SiO₂ beams were suspended by locally removing the supporting Si substrate by alkali wet
83 etching.

84

2 DEVICE STRUCTURE AND FABRICATION

85 The device structure is shown in Fig. ?? in which a Ge micro-disk is dry-etched on an SiO₂ beam with
86 curved edges, which is suspended in order to release the built-in compressive stress by etching the bulk
87 Si. Thermally-grown SiO₂ has a residual compressive stress due to high growth temperatures and the
88 difference in thermal expansion coefficient between Si and SiO₂ (Wilmsen et al., 1972). Consequently,
89 thermally-stressed SiO₂ films are capable of delivering tensile-strain upon suspension because of
90 their tendency to deflect (Fang and Wickert, 1994; Senturia, 2001). Manipulating beam dimensions and
91 suspension area can be implemented to control this strain (Jain et al., 2012; Nam et al., 2013; Süess et al.,
92 2013). In order to realize this configuration, we have used commercially available intrinsic GOI wafers
93 with the Ge/BOX thickness of 100–nm/145–nm. The thin Ge layer was preferable to obtain higher
94 strain values without fracturing (Boztug et al., 2013). Moreover, thinner micro-disks support lowest order
95 modes and provide a reduced modal volume, so that they are preferable for single mode operation in the
96 future (Gaponenko, 2010; Boztug et al., 2013).

97

98 GOI wafers were cleaned by diluted hydrofluoric (HF) and hydrochloric (HCl) acids. Then, Ge micro-
99 disks were patterned using electron beam lithography with diameters ranging from 1 μm to 10 μm, and
100 dry-etched using reactive-ion etching (RIE). To define the SiO₂ beams such that they hold the Ge micro-
101 disks on top, circular holes were dry-etched into the BOX layer on both sides of the micro-disk, as shown
102 on the top right corner of Fig. ?. Circular-hole openings allow manipulation of suspended beam dimen-
103 sions, and thus tuning the strain, such that the diameter of the holes defines the beam length (l) and the
104 minimum separation between them defines the beam width (w). Beam design parameters, l and w , were
105 set to 36 μm and 12 μm respectively. After dry etching, the surface was passivated by 100–nm SiO₂
106 deposited by plasma-enhanced chemical-vapor deposition (PECVD) at 350 °C. To suspend the beams,
107 we used the 22% Tetramethylammonium hydroxide (TMAH) solution, to etch 10 μm of a supporting Si
108 substrate.

109

110 For the SiO₂ beams to be suspended, the beams have to be aligned with $\langle 010 \rangle$ directions (Süess et al.,
111 2013) of the Si substrate, as shown in the optical microscopy image in Fig. 2 (A). Remarkably, aniso-
112 tropy of TMAH etching through circular-hole openings on Si is pronounced along two directions: $\langle 110 \rangle$
113 at 45° degrees relative to the beam direction $\langle 010 \rangle$, and $\langle 210 \rangle$ directions at 63.4° relative to beam direction
114 $\langle 010 \rangle$, as shown in Fig. 2 (A). After TMAH etching, beams were suspended and deflected either upwards
115 or downwards. Direction of bending was not perfectly controlled, however the majority of the devices
116 were bent upward. We expect that upward bending will impose tensile strain on the top Ge micro-disks
117 due to the longer length of the beam (Senturia, 2001).

118

119 Laser microscopy imaging was used to create precise three-dimensional height maps of the devices in
120 order to examine the bending behavior of the beams and Ge disks, which is related to the tensile-strain.
121 As shown by laser microscopy image (Fig. 3), the SiO₂ beam is bent upward with a maximum deflection
122 of approximately 0.8 μm. Height variations across the area of the Ge micro-disk was approximately 0.2
123 μm as seen in Fig. 3. The bending of the disk edges may contribute to strain inhomogeneity across its
124 height (Ghrib et al., 2013, 2014, 2015).
125

3 RESULTS AND DISCUSSION

3.1 STRAIN CHARACTERIZATION USING RAMAN SPECTROSCOPY

126 In this section we discuss the impact of beam suspension on Ge micro-disks by Raman spectroscopy. Ten-
127 sile strain causes shrinkage of Ge band-gap (Peng et al., 2009; Süess et al., 2013; Sukhdeo et al., 2014),
128 with a deformation rate that depends on its orientation, being either uni-axial or bi-axial (de Walle, 1989;
129 Kurdi et al., 2010b). This tensile strain can be determined by Raman spectroscopy measurements, as ten-
130 sile strain has the effect of red-shifting the Raman peak of bulk Ge (301 cm⁻¹) according to the relation
131 $\Delta\omega = S\epsilon$, where $\Delta\omega$ is the shift in wavenumbers, ϵ is the strain, and S is a proportionality coefficient. For
132 bi-axial strain, S was reported as 390 cm⁻¹ (Capellini et al., 2013, 2014). For $\langle 001 \rangle$ uni-axial strain, S
133 was reported as 152 cm⁻¹ (Peng et al., 2009; Sukhdeo et al., 2014; Süess et al., 2013).
134

135 We measured the strain using a laser with 532 nm wavelength and 2 μm spot size. Signals were collected
136 through 3000 lines/mm grating with the exposure time of 10 s and 50 repetitions to enhance signal-to-
137 noise ratio. The experimental data points were fitted by a Lorentzian to estimate peak positions. First, we
138 examined excitation power dependence to identify the impacts of heating on the additional red-shift in
139 the Raman peak position for suspended structures. The Raman shift was found to be linear against the
140 excitation power, the rate was -6.3×10^{-4} cm⁻¹/μW for a suspended 3-μm-diameter Ge disk, while the
141 rate was -0.18×10^{-4} cm⁻¹/μW for the un-patterned GOI wafer without suspension. In order to subtract
142 the impact of heating, we linearly extrapolated the power dependence curves to find the interception of
143 the Raman peak position.
144

145 The GOI wafer before patterning was slightly tensile-strained with a Raman shift of approximately -0.8
146 cm⁻¹. This shift can be attributed to bi-axial tensile-strain due to Ge on Si growth process, and the tensile
147 strain value can then be calculated as $\epsilon_{biaxial} \approx 0.2\%$. Figure 4 shows the relative Raman shifts for Ge
148 micro-disks with different diameters after suspension. We expected to apply uni-axial strain to the Ge disk
149 by making a narrow bended beam, however, it is not straightforward to identify whether uni-axial strain
150 overcame the original bi-axial strain. Assuming a bi-axial tensile strain is still dominant on the disks, a
151 bi-axial tensile strain of 0.29%, 0.28%, and 0.35% is estimated for disks with a diameter of 1 μm, 3 μm,
152 and 10 μm, respectively. On the other hand, if the uni-axial strain is dominant, the proportionality factor
153 S is smaller, so that the corresponding strain values are estimated to be larger, 0.78%, 0.73%, and 0.92%,
154 respectively. In reality, both uni-axial and bi-axial components should exist, and the actual strain values
155 should be somewhere in between the above estimations.
156

157 Uniformity of tensile strain is also vital for Ge direct-gap emission, the fact that variations in strain
158 correspond to variations in band-gap energies (de Walle, 1989; Kurdi et al., 2010b), since electrons have
159 a higher probability of dwelling regions with higher tensile strain, consequently this leads to converting
160 less strained regions into lossy mediums, and reduces the total overlap between gain regions and reso-
161 nant modes (Ghrib et al., 2013, 2014, 2015). In order to examine uniformity of strain distribution in our
162 device, we scanned a two-dimensional Raman spectra of a 3 μm suspended Ge disk, with a step of 200

163 nm. The intensity distribution of Raman peaks of the Ge disk is shown in Fig. 5(A), while Fig. 5(B) shows
 164 the actual Raman-shift distribution across the top surface of the disk. The black dotted contour lines spe-
 165 cify the regions with highest Raman intensity. It can be concluded from this mapping that a Raman shift
 166 of -1.11 cm^{-1} (0.28% bi-axial or 0.73% uniaxial tensile strain) exists over the majority of the Ge disk
 167 area. The stress seems to be relaxed at the circumference, which may be related to deformation of the disk
 168 at the edges.
 169

3.2 PHOTOLUMINESCENCE AND DIRECT-GAP RESONANCES

170 We performed finite-domain time-difference (FDTD) simulations using Lumerical FDTD software, to
 171 estimate direct-gap resonances that exist in a $3 \mu\text{m}$ disk suspended on SiO_2 beam, as shown in the inset
 172 of Fig. 6. We chose the diameter to be $3 \mu\text{m}$ because WGM resonances were observed only in $3 \mu\text{m}$ disks
 173 as will be shown below. Thicknesses of Ge and SiO_2 films are 100 and 145 nm, and refractive indexes
 174 were set to 4.2 and 1.45 respectively. We used an in-plane electric field source ($\vec{\mathcal{E}}_{x,y}$) assuming that only
 175 transverse-electric (TE) modes can be guided in 100 nm Ge (McCall et al., 1992; Boztug et al., 2013).
 176 The source pulse was chosen to have a Gaussian distribution centered around $1.7 \mu\text{m}$ to excite the modes
 177 within the direct-gap of Ge under slight tensile strain conditions. Simulation time was long enough to
 178 ensure clear visualization of resonant modes. The spectrum of the suspended $3 \mu\text{m}$ disk is shown in Fig.
 179 6, with resonant peaks identified as WGMs at 1.508, 1.561, 1.626, 1.708, and $1.811 \mu\text{m}$. Surface plots of
 180 magnetic field component perpendicular to the plane of the disk ($\vec{\mathcal{H}}_z$) of these resonances are shown on
 181 top of Fig. 6. From these surface plots we can label the $\text{TE}_{m,n}$ WGMs as $\text{TE}_{13,1}$, $\text{TE}_{12,1}$, $\text{TE}_{11,1}$, $\text{TE}_{10,1}$,
 182 and $\text{TE}_{9,1}$, respectively. Where m is the azimuthal number (number of full wavelengths across the inner
 183 circumference of the disk) and n is the radial number (number of field maxima along the radius).
 184

185 Photo-Luminescence (PL) measurements were conducted at room temperature using a continuous-wave
 186 laser with a wavelength of 730 nm and $2 \mu\text{m}$ spot size. Suspended Ge disks with diameters ranging from
 187 $1 \mu\text{m}$ to $10 \mu\text{m}$ were excited from top with $400 \mu\text{W}$ laser power. PL spectra for different disk sizes are
 188 shown in Fig. 7(A), which corresponds to Ge direct-gap recombinations (Saito et al., 2011, 2014; Sun
 189 et al., 2009; Liu et al., 2012b; Kurdi et al., 2010a). Accumulation of slight tensile strain within the Ge
 190 disks, as proved by Raman measurements, causes a corresponding red-shift in PL spectra (de Walle, 1989;
 191 Süess et al., 2013; Sukhdeo et al., 2014). Sharp-peak resonances were obtained for $3 \mu\text{m}$ disks only, and
 192 these peaks are attributed to WGMs occurring at 1591.5 nm, 1704.4 nm, and 1809.9 nm as shown in
 193 Fig. 7(B). Corresponding quality factors of 67, 182, and 191.8, respectively, were determined by fitting
 194 the resonant peaks with a Lorentzian. According to FDTD simulations, we identified these peaks to be
 195 $\text{TE}_{11,1}$, $\text{TE}_{10,1}$, and $\text{TE}_{9,1}$ WGMs, respectively. On contrary, smaller disks with $1 \mu\text{m}$ and $2 \mu\text{m}$ diame-
 196 ters, suffered from extreme broadening in emission spectrum and no modulation by cavity resonances
 197 was observed. This broadening can be explained by severe heating effects, due to the small disk diameters
 198 which were comparable to the spot-size of the excitation laser. On the other hand, larger disks of $6 \mu\text{m}$,
 199 $8 \mu\text{m}$, and $10 \mu\text{m}$ diameter had broad-peak resonances. As the disk size increases, number of broad-peak
 200 resonances increases, and free spectral range (FSR) between them decreases. The exact identification of
 201 these peaks is not straightforward, however, these resonances have broader peaks compared to WGMs
 202 observed in $3 \mu\text{m}$ disks, and consequently less important for monolithic operation.
 203

204 Figure 7(B) shows PL spectra of the suspended $3 \mu\text{m}$ disk for different excitation-power conditions.
 205 As the excitation power increases, the direct-gap emission intensity of the Ge disk increases. $\text{TE}_{11,1}$
 206 mode is barely visible on a log-scale figure because of its low intensity and Q -factor; presumably it is
 207 highly-affected by absorption from Ge due to its lower wavelength (Ishikawa et al., 2005; Wang et al.,
 208 2013). So, we will concentrate our discussions on $\text{TE}_{10,1}$, and $\text{TE}_{9,1}$. It was found that the intensities of
 209 $\text{TE}_{10,1}$ and $\text{TE}_{9,1}$ modes were proportional to $P^{2.28}$ and $P^{1.98}$, respectively, where P is the excitation

210 power, as shown in Fig. 8. This indicates that the tensile-strain was not high enough to observe direct-
 211 gap characteristics. This agrees with our previous results (Al-Attili et al., 2014) in which we discussed
 212 the quadratic ($\propto P^2$) power dependence of emission intensities for intrinsic Ge, compared to a linear
 213 dependence ($\propto P^1$) for n -doped Ge. This difference was explained by the initial consumption of injected
 214 carriers in filling the L valleys in the case of intrinsic Ge due to its inherent in-direct band gap character,
 215 which causes a modest increase in emission intensity with power.
 216

217 Figure 9 shows the behavior of $TE_{9,1}$ and $TE_{10,1}$ Q -factors and resonant-peak positions as we increase
 218 the excitation power. A general trend of Q -factor degradation and red-shifting of resonant peaks with
 219 increased carriers' injection is evident, this agrees with the work of other groups under optical (Shambat
 220 et al., 2010; Ghrib et al., 2013, 2014, 2015) and electrical (Cheng et al., 2011) pumping. Degradation
 221 of Q -factors with pumping has two main reasons: (I) Heating which effectively shrinks Ge band-gap causing
 222 a red-shift in the direct-gap absorption edge (Ishikawa et al., 2003, 2005; Cannon et al., 2004; Liu
 223 et al., 2005; Wang et al., 2013), and consequently increasing the absorption coefficient at lower wave-
 224 lengths. This loss mechanism affects high-energy (short wavelength) modes (Ishikawa et al., 2005; Lim
 225 et al., 2008; Wang et al., 2013). In addition to (II) the increase in free-carrier absorption (FCA) losses
 226 due to additional photo-induced carriers (Liu et al., 2007, 2012b; Kurdi et al., 2010b; Shambat et al.,
 227 2010). This loss mechanism is pronounced for lower energy (higher wavelength) resonances which suffer
 228 higher FCA (Liu et al., 2007; Kurdi et al., 2010b; Ghrib et al., 2013). Due to the association of both
 229 factors with injected carriers' density, Q -factors of WGMs in Ge micro-disks are consequently affected
 230 by pumping levels. These excitation-related loss mechanisms cause broadening of resonant peaks until
 231 they become undetectable at high pumping powers, as shown in Fig. 7(B).
 232

233 Moreover, examining the different behavior of Q -factor degradation for different resonances according
 234 to Fig. 9. It is obvious that up to $300 \mu\text{W}$ the resonant peaks at 1704.4 nm ($TE_{10,1}$) and 1809.9 nm ($TE_{9,1}$)
 235 are broadened in a similar manner. However, as we keep increasing the excitation power above $300 \mu\text{W}$,
 236 the lower-wavelength mode ($TE_{10,1}$) undergoes a higher degradation rate, while the higher-wavelength
 237 mode ($TE_{9,1}$) remains broadening at the same degradation rate. This can be explained as follows, at pump
 238 powers lower than $300 \mu\text{W}$ both modes are affected by FCA, while the red-shift in the Ge direct-gap
 239 absorption edge is not enough to approach $TE_{10,1}$ yet. As we keep increasing the pump power, Ge direct-
 240 gap continues to red-shift due to heating until the direct-gap absorption totally overshadows the resonant
 241 peak of $TE_{10,1}$ and we can no longer observe this peak at $600 \mu\text{W}$, as shown in Fig. 7. At this stage,
 242 the higher-wavelength mode is still suffering from increasing FCA but it remains unaffected by the Ge
 243 direct-gap absorption, and we still observe this peak even at $800 \mu\text{W}$. This indicates that absorption due
 244 to heating is more significant than the FCA in preventing lasing. In order to avoid high injection levels,
 245 and reduce absorption due to heating, higher tensile strain levels in addition to high n -type doping levels
 246 are required. n -type doping (Xu et al., 2014) also reduces FCA losses by allowing inversion with reduced
 247 levels of injected holes, which have a higher contribution to the total FCA compared to electrons (Liu
 248 et al., 2012b).
 249

4 CONCLUSION AND FUTURE WORK

250 In this paper, we have proposed a configuration to apply tensile-strain on Ge micro-disks by suspension
 251 of the underlying SiO_2 layer, for Ge monolithic emission purposes. We have shown that it is possible to
 252 accumulate tensile strain by using this structure. Further optimization has to be made in order to obtain
 253 higher strain values. Uniformity of the applied strain was examined by performing a Raman scan and a
 254 slight variations of strain at the disk edges were observed. PL spectra of suspended Ge disks with diffe-
 255 rent diameters were discussed, and we identified sharp-peak WGMs only for the disk with the diameter
 256 of $3 \mu\text{m}$, while broad-peak resonances existed in larger disks. We found that the achieved tensile-stress

257 was not enough to observe direct-gap characteristics, and heating effects were predominant for disk dia-
258 meters smaller than $3\ \mu\text{m}$. Q -factors of WGMs were degraded with higher pump powers and this was
259 related to the red-shift of the Ge direct-gap absorption edge and FCA. We also confirmed a quadratic
260 power dependence of the emission intensity of intrinsic slightly-strained Ge, which agrees with our pre-
261 vious results. We believe that Ge micro-disks hold great potential for future integration of low threshold
262 CMOS-compatible laser sources and building a mature photonic circuitry on-chip.
263

DISCLOSURE/CONFLICT-OF-INTEREST STATEMENT

264 The authors declare that the research was conducted in the absence of any commercial or financial
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REFERENCES

- 275 Bai, Y., Lee, K. E., Cheng, C., Lee, M. L., and Fitzgerald, E. A. (2008), Growth of highly tensile-strained
276 Ge on relaxed $\text{In}_x\text{Ga}_{1-x}\text{As}$ by metal-organic chemical vapor deposition, *J. Appl. Phys.*, 104, 084518,
277 doi:10.1063/1.3005886
- 278 Boucaud, P., Kurdi, M. E., Ghrib, A., Prost, M., de Kersauson, M., Sauvage, S., et al. (2013), Recent
279 advances in germanium emission, *Photon. Res.*, 1, 3, 102–109, doi:10.1364/PRJ.1.000102
- 280 Boztug, C., Sánchez-Pérez, J. R., Yin, J., Lagally, M. G., and Paiella, R. (2013), Gating-coupled mid-
281 infrared light emission from tensilely strained germanium nanomembranes, *Appl. Phys. Lett.*, 103,
282 201114, doi:10.1063/1.4830377
- 283 Brinkman, W. F., Koch, T. L., Lang, D. V., and Wilt, D. P. (2000), The lasers behind the communications
284 revolution, *Bell Labs Tech. J.*, 5, 1, 150–167, doi:10.1002/bltj.2212
- 285 Camacho-Aguilera, R. E., Cai, Y., Patel, N., Bessette, J. T., Romagnoli, M., Kimerling, L. C., et al.
286 (2012), An electrically pumped germanium laser, *Opt. Express*, 20, 10, 11316–11320, doi:10.1364/OE.
287 20.011316
- 288 Cannon, D. D., Liu, J., Ishikawa, Y., Wada, K., Danielson, D. T., Jongthammanurak, S., et al.
289 (2004), Tensile strained epitaxial Ge film on Si(100) substrate with potential application to L-band
290 telecommunications, *Appl. Phys. Lett.*, 84, 6, 906, doi:10.1063/1.1645677
- 291 Capellini, G., Kozłowski, G., Yamamoto, Y., Lisker, M., Wenger, C., Niu, G., et al. (2013), Strain analy-
292 sis in Si/Ge microstructures obtained via Si -complementary metal oxide semiconductor compatible
293 approach, *J. Appl. Phys.*, 113, 013513, doi:10.1063/1.4772781

- 294 Capellini, G., Reich, C., Guha, S., Yamamoto, Y., Lisker, M., Virgilio, M., et al. (2014), Tensile ge
295 microstructures for lasing fabricated by means of a silicon complementary metal-oxide-semiconductor
296 process, *Opt. Express*, 22, 1, 399–410, doi:10.1364/OE.22.000399
- 297 Cheng, S. L., Shambat, G., Lu, J., Yu, H. Y., Saraswat, K., Kamins, T. I., et al. (2011), Cavity-enhanced
298 direct band electroluminescence near 1550 nm from germanium microdisk resonator diode on silicon,
299 *Appl. Phys. Lett.*, 98, 211101, doi:10.1063/1.3592837
- 300 de Walle, C. G. V. (1989), Band lineups and deformation potentials in the model-solid theory, *Phys. Rev.*
301 *B*, 39, 3, 1871, doi:10.1103/PhysRevB.39.1871
- 302 Fang, W. and Wickert, J. A. (1994), Post buckling of micromachined beams, *J. micromech. microeng.*, 4,
303 3, 116, doi:10.1088/0960-1317/4/3/004
- 304 Fischetti, M. V. and Laux, S. E. (1996), Band structure, deformation potentials, and carrier mobility in
305 strained Si, Ge, and SiGe alloys, *J. Appl. Phys.*, 80, 4, 2234, doi:10.1063/1.363052
- 306 Gaponenko, S. V. (2010), Introduction to nanophotonics (Cambridge University Press, New York)
- 307 Ghrib, A., de Kersauson, M., Kurdi, M. E., Jakomin, R., Beaudoin, G., Sauvage, S., et al. (2012), Control
308 of tensile strain in germanium waveguides through silicon nitride layers, *Appl. Phys. Lett.*, 100, 201104,
309 doi:10.1063/1.4718525
- 310 Ghrib, A., Kurdi, M. E., de Kersauson, M., Prost, M., Sauvage, S., Checoury, X., et al. (2013), Tensile-
311 strained germanium microdisks, *Appl. Phys. Lett.*, 102, 221112, doi:10.1063/1.4809832
- 312 Ghrib, A., Kurdi, M. E., Prost, M., de Kersauson, M., Largeau, L., Mauguin, O., et al. (2014), Strain
313 engineering in germanium microdisks, *Proc. SPIE*, 8990, doi:10.1117/12.2037307
- 314 Ghrib, A., Kurdi, M. E., Prost, M., Sauvage, S., Checoury, X., Beaudoin, G., et al. (2015), All-around SiN
315 stressor for high and homogeneous tensile strain in germanium microdisk cavities, *Adv. Optical Mater.*,
316 3, 3, 353–358, doi:10.1002/adom.201400369
- 317 Goodman, J. W., Leonberger, F. J., Kung, S. Y., and Athale, R. A. (1984), Optical interconnections for
318 VLSI systems, *Proceedings of the IEEE*, 72, 7, 850–866, doi:10.1109/PROC.1984.12943
- 319 Huo, Y., Lin, H., Chen, R., Makarova, M., Rong, Y., Li, M., et al. (2011), Strong enhancement of direct
320 transition photoluminescence with highly tensile-strained Ge grown by molecular beam epitaxy, *Appl.*
321 *Phys. Lett.*, 98, 1, 011111, doi:10.1063/1.3534785
- 322 Ishikawa, Y., Wada, K., Cannon, D. D., Liu, J., Luan, H. C., and Kimerling, L. C. (2003), Strain-induced
323 band gap shrinkage in Ge grown on Si substrate, *Appl. Phys. Lett.*, 82, 13, 2044, doi:10.1063/1.1564868
- 324 Ishikawa, Y., Wada, K., Liu, J., Cannon, D. D., Luan, H. C., Michel, J., et al. (2005), Strain-induced
325 enhancement of near-infrared absorption in Ge epitaxial layers grown on Si substrate, *J. Appl. Phys.*,
326 98, 013501, doi:10.1063/1.1943507
- 327 Jain, J. R., Hryciw, A., Baer, T. M., Miller, D. A. B., Brongersma, M. L., and Howe, R. T. (2012),
328 A micromachining-based technology for enhancing germanium light-emission via tensile strain, *Nat.*
329 *Photonics*, 6, 6, 398–405, doi:10.1038/NPHOTON.2012.111
- 330 Kurdi, M. E., Bertin, H., Martincic, E., de Kersauson, M., Fishman, G., Sauvage, S., et al. (2010a),
331 Control of direct band gap emission of bulk germanium by mechanical tensile strain, *Appl. Phys. Lett.*,
332 96, 041909, doi:10.1063/1.3297883
- 333 Kurdi, M. E., David, S., Checoury, X., Fishman, G., Boucaud, P., Kermarrec, O., et al. (2008), Two-
334 dimensional photonic crystals with pure germanium-on-insulator, *Opt. Commun.*, 281, 4, 846–850,
335 doi:10.1016/j.optcom.2007.10.008
- 336 Kurdi, M. E., Fishman, G., Sauvage, S., and Boucaud, P. (2010b), Band structure and optical gain of
337 tensile-strained germanium based on a 30 band k.p formalism, *J. Appl. Phys.*, 107, 013710, doi:10.
338 1063/1.3279307
- 339 Liang, D. and Bowers, J. E. (2010), Recent progress in lasers on silicon, *Nat. Photonics*, 4, 8, 511–517,
340 doi:10.1038/nphoton.2010.167
- 341 Lim, P. H., Kobayashi, Y., Takita, S., Ishikawa, Y., and Wada, K. (2008), Enhanced photoluminescence
342 from germanium-based ring resonators, *Appl. Phys. Lett.*, 93, 041103, doi:10.1063/1.2950087
- 343 Liu, J. (2014), Monolithically integrated Ge-on-Si active photonics, *Photonics*, 1, 3, 162–197, doi:10.
344 3390/photonics1030162
- 345 Liu, J., Camacho-Aguilera, R., Bessette, J. T., Sun, X., Wang, X., Cai, Y., et al. (2012a), Ge-on-Si
346 optoelectronics, *Thin Solid Films*, 520, 8, 3354–3360, doi:10.1016/j.tsf.2011.10.121

- 347 Liu, J., Cannon, D. D., Wada, K., Ishikawa, Y., Jongthammanurak, S., Danielson, D. T., et al. (2005),
348 Tensile strained Ge *p-i-n* photodetectors on Si platform for C and L band telecommunications, *Appl.*
349 *Phys. Lett.*, 87, 011110, doi:10.1063/1.1993749
- 350 Liu, J., Kimerling, L. C., and Michel, J. (2012b), Monolithic Ge-on-Si lasers for large-scale electronic-
351 photonic integration, *Semicond. Sci. Technol.*, 27, 094006, doi:10.1088/0268-1242/27/9/094006
- 352 Liu, J., Sun, X., Camacho-Aguilera, R., Kimerling, L. C., and Michel, J. (2010), Ge-on-Si laser operating
353 at room temperature, *Optics Lett.*, 35, 5, 679–681, doi:10.1364/OL.35.000679
- 354 Liu, J., Sun, X., Kimerling, L. C., and Michel, J. (2009), Direct-gap optical gain of ge on si at room
355 temperature, *Opt. Lett.*, 34, 11, 1738–1740, doi:10.1364/OL.34.001738
- 356 Liu, J., Sun, X., Pan, D., Wang, X., Kimerling, L. C., Koch, T. L., et al. (2007), Tensile-strained, n-
357 type Ge as a gain medium for monolithic laser integration on Si, *Opt. Express*, 15, 18, 11272–11277,
358 doi:10.1364/OE.15.011272
- 359 McCall, S. L., Levi, A. F. J., Slusher, R. E., Pearnton, S. J., and Logan, R. A. (1992), Whispering gallery
360 mode microdisk lasers, *Appl. Phys. Lett.*, 60, 3, 289–291, doi:10.1063/1.106688
- 361 Menéndez, J. and Kouvetakis, J. (2004), Type-I Ge/Ge_{1-x-y}Si_xSn_y strained-layer heterostructure with a
362 direct Ge bandgap, *Appl. Phys. Lett.*, 85, 7, 1175, doi:10.1063/1.1784032
- 363 Michel, J., Liu, J., and Kimerling, L. C. (2010), High-performance Ge-on-Si photodetectors, *Nat.*
364 *Photonics*, 4, 8, 527–534, doi:10.1038/nphoton.2010.157
- 365 Miller, D. A. B. (2009), Device requirements for optical interconnections to silicon chips, *Proceedings of*
366 *the IEEE*, 97, 7, 1166–1185, doi:10.1109/JPROC.2009.2014298
- 367 Nam, D., Kang, J. H., Brongersma, M. L., and Saraswat, K. C. (2014), Observation of improved minority
368 carrier lifetimes in high-quality Ge-on-insulator using time-resolved photoluminescence, *Opt. Lett.*, 39,
369 21, 6205–6208, doi:10.1364/OL.39.006205
- 370 Nam, D., Sukhdeo, D. S., Kang, J. H., Petykiewicz, J., Lee, J. H., Jung, W. S., et al. (2013), Strain-induced
371 pseudoheterostructure nanowires confining carriers at room temperature with nanoscale-tunable band
372 profiles, *Nano Lett.*, 13, 7, 3118–3123, doi:10.1021/nl401042n
- 373 Ngo, T. P., Kurdi, M. E., Checoury, X., Boucaud, P., Damlencourt, J. F., Kermarrec, O., et al. (2008),
374 Two-dimensional photonic crystals with germanium on insulator obtained by a condensation method,
375 *Appl. Phys. Lett.*, 93, 241112, doi:10.1063/1.3054332
- 376 Ortolland, C., Okuno, Y., Verheyen, P., Kerner, C., Stapelmann, C., Aoulaiche, M., et al. (2009), Stress
377 memorization technique—fundamental understanding and low-cost integration for advanced CMOS
378 technology using a nonselective process, *Electron Devices, IEEE Transactions on*, 56, 8, 1690–1697,
379 doi:10.1109/TED.2009.2024021
- 380 Peng, C. Y., Huang, C. F., Fu, Y. C., Yang, Y. H., Lai, C. Y., Chang, S. T., et al. (2009), Comprehensive
381 study of the raman shifts of strained silicon and germanium, *J. of Appl. Phys.*, 105, 083537, doi:10.
382 1063/1.3110184
- 383 People, R. and Bean, J. C. (1986), Band alignments of coherently strained Ge_xSi_{1-x}/Si heterostructures on
384 $\langle 001 \rangle$ Ge_ySi_{1-y} substrates, *Appl. Phys. Lett.*, 48, 8, 538, doi:10.1063/1.96499
- 385 Purcell, E. M. (1946), Spontaneous emission probabilities at radio frequencies, *Phys. Rev.*, 69, 681,
386 doi:10.1103/PhysRev.69.674.2
- 387 Saito, S., Gardes, F. Y., Al-Attili, A. Z., Tani, K., Oda, K., Suwa, Y., et al. (2014), Group iv light sources
388 to enable the convergence of photonics and electronics, *Front. Mater.*, 1, 15, doi:10.3389/fmats.2014.
389 00015
- 390 Saito, S., Oda, K., Takahama, T., Tani, K., and Mine, T. (2011), Germanium fin light-emitting diode,
391 *Appl. Phys. Lett.*, 99, 241105, doi:10.1063/1.3670053
- 392 Senturia, S. D. (2001), *Microsystem Design* (Kluwer academic publishers, Boston)
- 393 Shambat, G., Cheng, S. L., Lu, J., Nishi, Y., and Vuckovic, J. (2010), Direct band Ge photoluminescence
394 near 1.6 μm coupled to Ge-on-Si microdisk resonators, *Appl. Phys. Lett.*, 97, 241102, doi:10.1063/1.
395 3526732
- 396 Süess, M. J., Geiger, R., Minamisawa, R. A., Schiefler, G., Frigerio, J., Chrastina, D., et al. (2013),
397 Analysis of enhanced light emission from highly strained germanium microbridges, *Nat. Photonics*, 7,
398 6, 466–472, doi:10.1038/nphoton.2013.67

- 399 Sukhdeo, D. S., Nam, D., Kang, J. H., Brongersma, M. L., and Saraswat, K. C. (2014), Direct bandgap
400 germanium-on-silicon inferred from 5.7% $\langle 100 \rangle$ uniaxial tensile strain, *Photon. Res.*, 2, 3, A8–A13,
401 doi:10.1364/PRJ.2.0000A8
- 402 Sun, X., Liu, J., Kimerling, L. C., and Michel, J. (2009), Direct gap photoluminescence of n -type tensile-
403 strained Ge-on-Si, *Appl. Phys. Lett.*, 95, 011911, doi:10.1063/1.3170870
- 404 Suwa, Y. and Saito, S. (2011), First-principles study of light emission from silicon and germanium due to
405 direct transitions, in IEEE 8th Int. Conf. Group IV Photonics, 222–224, doi:10.1109/GROUP4.2011.
406 6053770
- 407 Virgilio, M., Manganelli, C. L., Grosso, G., Pizzi, G., and Capellini, G. (2013a), Radiative recombination
408 and optical gain spectra in biaxially strained n -type germanium, *Phys. Rev. B*, 87, 235313, doi:10.1103/
409 PhysRevB.87.235313
- 410 Virgilio, M., Manganelli, C. L., Grosso, G., Schroeder, T., and Capellini, G. (2013b), Photoluminescence,
411 recombination rate, and gain spectra in optically excited n -type and tensile strained germanium layers,
412 *J. Appl. Phys.*, 114, 243102, doi:10.1063/1.4849855
- 413 Wada, K., Liu, J., Jongthammanurak, S., Cannon, D. D., Danielson, D. T., Ahn, D., et al. (2006), Si
414 Microphotonics for Optical Interconnection (Springer Verlag, Berlin)
- 415 Wang, X., Li, H., Camacho-Aguilera, R., Cai, Y., Kimerling, L. C., Michel, J., et al. (2013), Infrared
416 absorption of n -type tensile-strained Ge-on-Si, *Opt. Lett.*, 38, 5, 652–654, doi:10.1364/OL.38.000652
- 417 Wilmsen, C. W., Thompson, E. G., and Meissner, G. H. (1972), Buckling of thermally-grown SiO₂
418 thin-films, *IEEE Trans. Electron Devices*, 19, 1, 122, doi:10.1109/t-ed.1972.17381
- 419 Wirths, S., Geiger, R., von den Driesch, N., Mussler, G., Stoica, T., Mantl, S., et al. (2015), Lasing in
420 direct-bandgap GeSn alloy grown on Si, *Nat. Photonics*, 9, 2, 88–92, doi:10.1038/nphoton.2014.321
- 421 Xu, X., Nishida, K., Sawano, K., Maruizumi, T., and Shiraki, Y. (2014), Resonant photoluminescence
422 from Ge microdisks on Ge-on-insulator, in 7th International Silicon-Germanium Technology and
423 Device Meeting (ISTDM), 135–136, doi:10.1109/ISTDM.2014.6874670

FIGURES

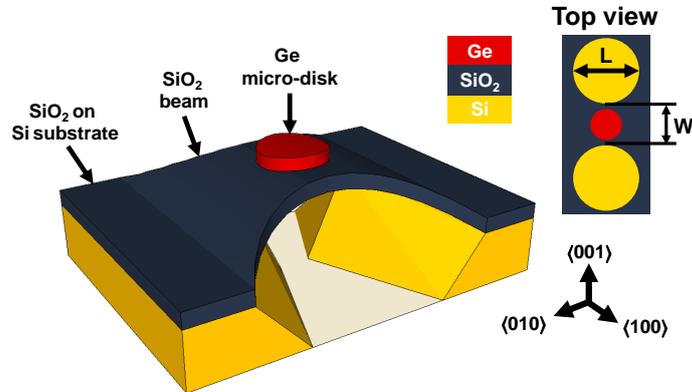


Figure 1. Three-dimensional sketch showing a Ge micro-disk on a suspended SiO₂ beam with curved edges and supported by SiO₂ on Si substrate. Fabrication design parameters, beam width w and beam length l , are shown from a top-view in the top right corner. Axes orientation apply for the 3D sketch only.

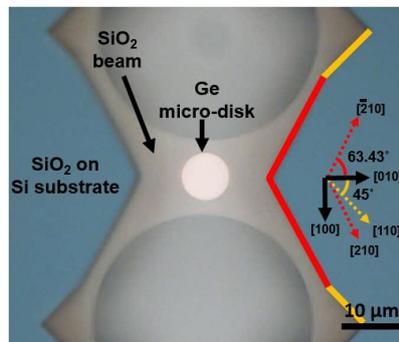


Figure 2. Optical microscopy image showing a Ge micro-disk on a suspended SiO₂ beam, along with the crystal orientations of the Si substrate. Anisotropy of TMAH wet-etching of Si through circular hole openings is determined by $\langle 110 \rangle$ and $\langle 210 \rangle$ Si lattice orientations.

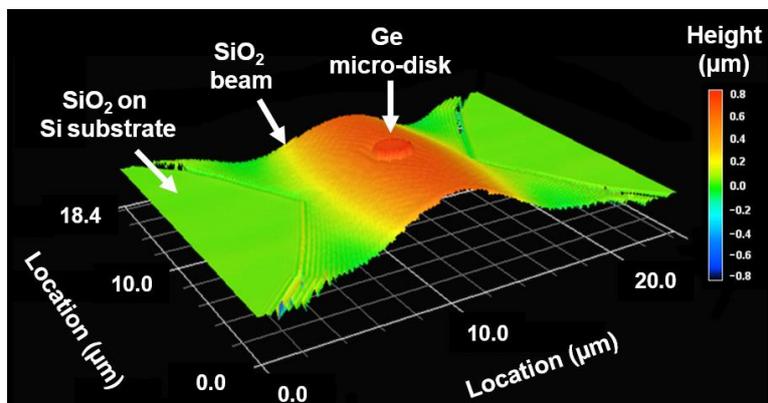


Figure 3. Laser microscopy image showing a three-dimensional height map of a Ge micro-disk on a suspended SiO₂ beam.

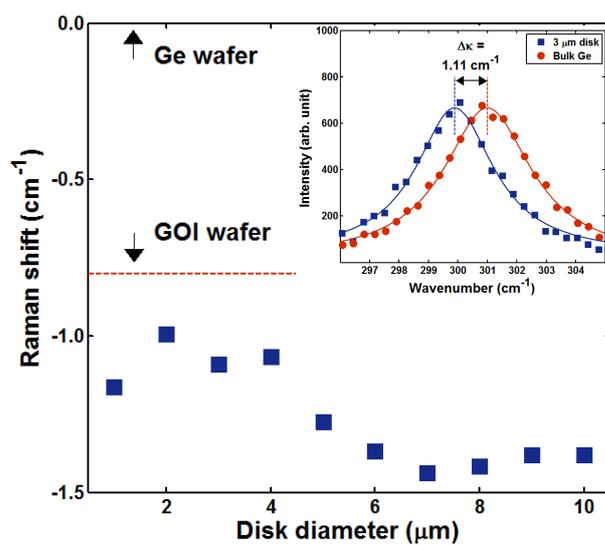


Figure 4. Raman shift (from bulk Ge) in cm⁻¹ for suspended Ge micro-disks with different diameters. Top inset shows the actual Raman spectra for bulk Ge and 3 μm disk.

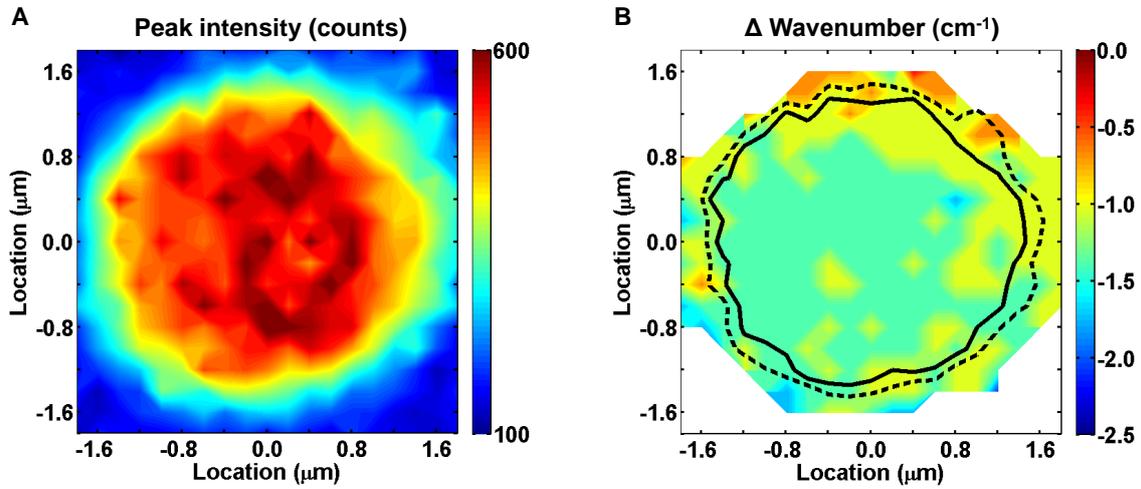


Figure 5. Two-dimensional Raman spectroscopy map of a suspended $3 \mu\text{m}$ Ge disk showing: (A) Raman intensity distribution, and (B) actual Raman shift across the Ge surface.

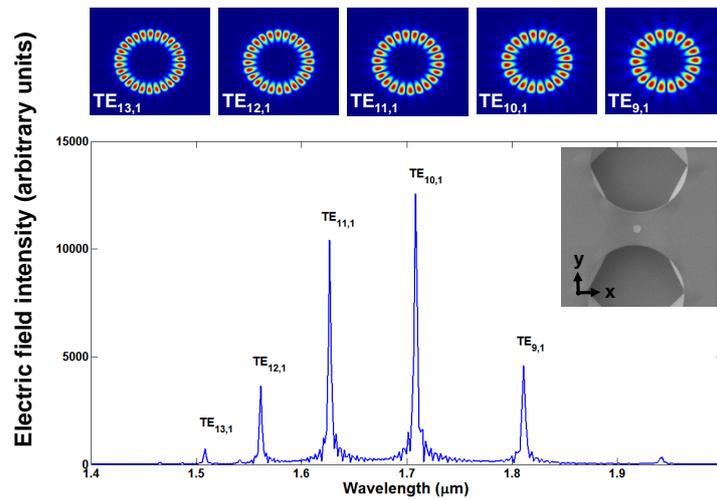


Figure 6. Spectrum of electric field ($\mathcal{E}_{x,y}^{\vec{}}$) resonances in-plane of a $3 \mu\text{m}$ disk on a suspended SiO_2 beam (shown in the SEM image inset). Confined modes with sharp peaks are whispering gallery modes as confirmed by the surface plots (top) of the vertical magnetic field component ($\vec{\mathcal{H}}_z$).

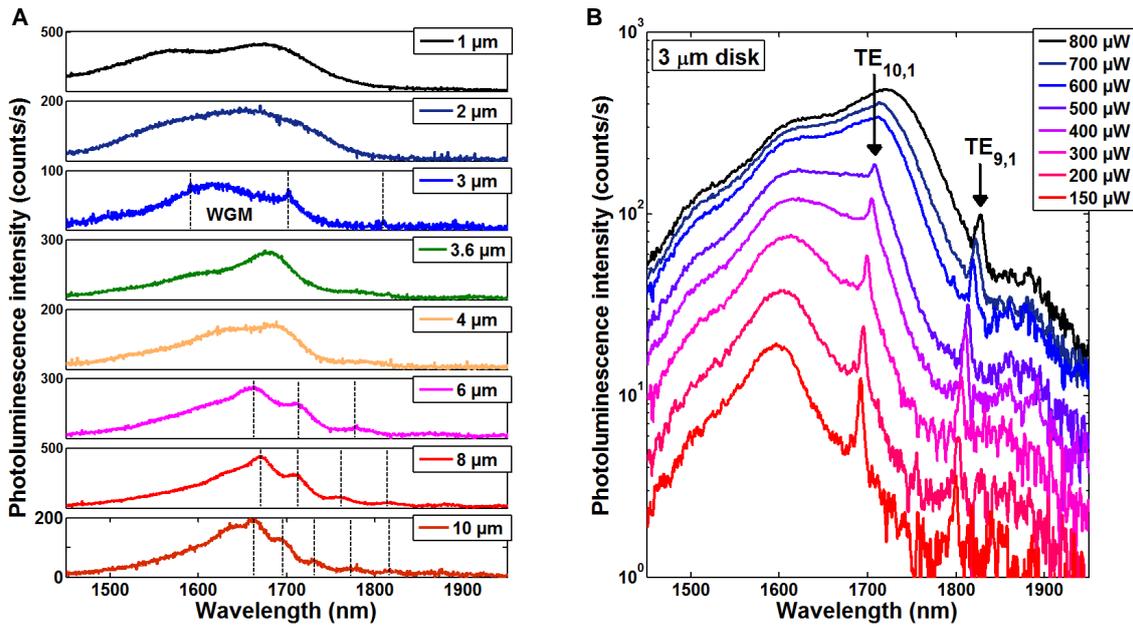


Figure 7. (A) Photoluminescence spectra of Ge micro-disks on suspended SiO₂ beams with different diameters ranging from 1 μm to 10 μm using 400 μW excitation power, WGM are observed in the 3 μm disk spectrum, while broad-peak resonances are observed for 6 μm, 8 μm, and 10 μm disks. (B) Photoluminescence power-dependence of the suspended 3 μm Ge disk. The resonant WGMs are labelled as TE_{10,1} and TE_{9,1} according to FDTD simulations. At 800 μW pumping level TE_{10,1} peak is invisible, while we can still observe TE_{9,1}.

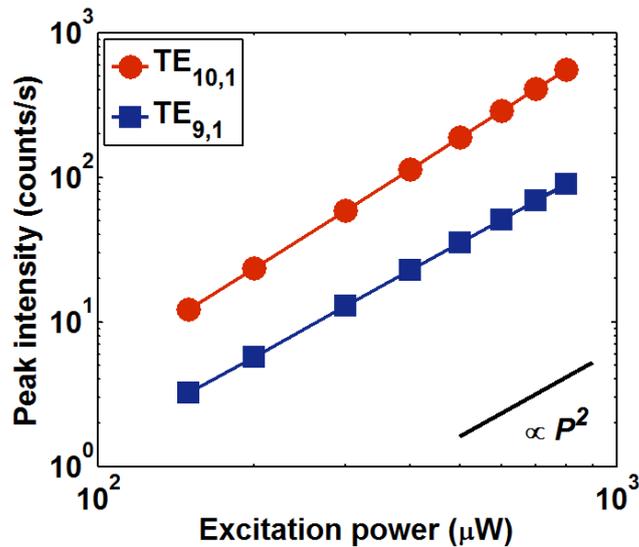


Figure 8. Excitation power dependence of the emission intensities for resonant whispering gallery modes at 1704.4 nm (TE_{10,1}) and 1809.9 nm (TE_{9,1}), observed in the 3 μm Ge disks.

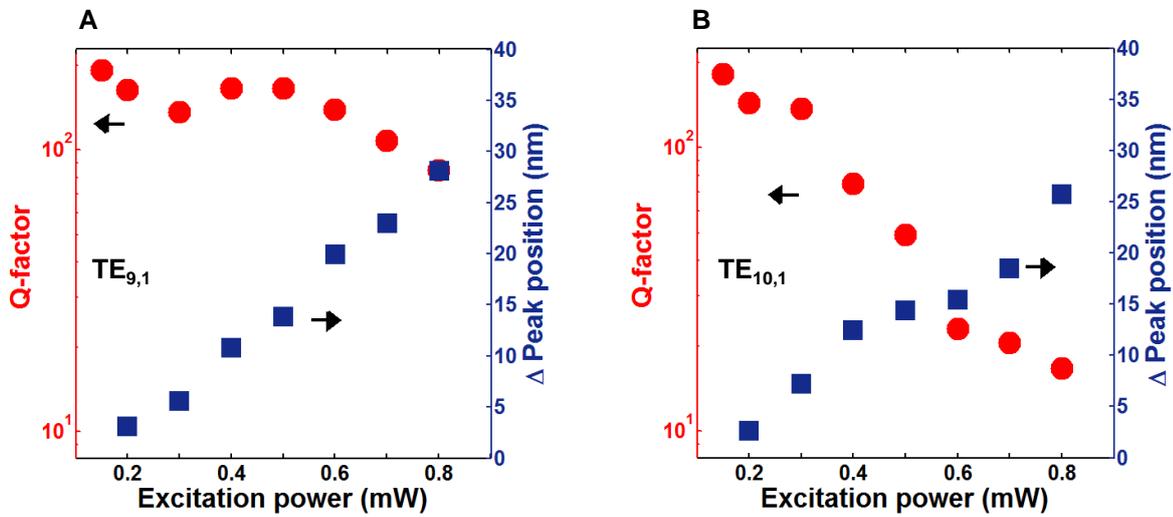


Figure 9. The effect of excitation power on Q -factor and peak position of (A) $TE_{9,1}$ and (B) $TE_{10,1}$. Increasing the power contributes to degradation in Q -factor and a red-shift in peak position. $TE_{10,1}$ suffers higher degradation rate with excitation power, presumably due to the redshift of direct-gap absorption edge of Ge with increasing excitation power due to heating, in addition to FCA losses. While $TE_{9,1}$ being less affected by the Ge direct-gap absorption, undergoes increasing FCA losses with higher pumping levels.