

Energy & Environmental Science

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Cite this: DOI: 10.1039/xxxxxxxxxx

Can slow-moving ions explain hysteresis in the current-voltage curves of perovskite solar cells?

Giles Richardson,^a Simon E. J. O'Kane,^b Ralf G. Niemann^c, Timo A. Peltola^b, Jamie M. Foster^d, Petra J. Cameron^c and Alison B. Walker^e

Received Date

Accepted Date

DOI: 10.1039/xxxxxxxxxx

www.rsc.org/journalname

The hypothesis that ion motion is responsible for anomalous hysteresis in the current-voltage curves of perovskite solar cells is investigated through a combination of electrical transport modelling and experimental measurements. In a combined computational and experimental study, good agreement is obtained between experiment and the results of a charge transport model covering mixed ionic-electronic conduction. Our model couples electrons, holes and defect mediated ion motion suggesting that slow moving ions are indeed the origin of the hysteresis. The magnitude of the ion diffusion coefficient required to match experiment and theory, $\sim 10^{-12}$ cm² s⁻¹, depends on the cell, but is similar to that predicted by microscopic theory of vacancy mediated diffusion. The investigation is extended to preconditioning procedures which are known to substantially influence the hysteresis. The method developed for solving the stiff equations in the drift diffusion model is widely applicable to other double layer problems occurring in electrochemical applications such as the evolution of transmembrane potentials in living cells.

1 Introduction

Since the first use of organolead halide perovskites as a sensitizer in a solar cell in 2009¹, the power conversion efficiency, PCE, of perovskite solar cells has risen from 3%^{2,3} to around 20% within five years. Recent reviews of perovskite solar cells are given by Stranks and Snaith⁴, Niu *et al.*⁵, Miyasaka⁶, and Park⁷.

Planar perovskite cells are produced by sandwiching a layer of perovskite, such as the compound MAPbI₃ (where MA is short for methylammonium, CH₃NH₃) between electron transporting and hole transporting contacts. The most common combination is titania (TiO₂) for the former and spiro, namely spiro-MeOTAD,2,2',7,7'-tetrakis-(N,N-di-p-methoxyphenyl amine)-9,9'-spirobifluorene as the latter.

A major weakness that undermines the credibility of measurements of perovskite solar cell PCEs is the choice of a voltage scanning protocol that takes advantage of hysteresis in the current density-voltage, *J-V*, curves to obtain apparent efficiencies that are in excess of the real efficiency of the cell. Indeed it was not until 2014, in the work of Snaith *et al.*⁸, and others⁹⁻¹², that this

source of inaccuracy was openly discussed in the literature. An understanding of the underlying working principles of perovskite cells is crucial to their future improvement¹⁰, not just the PCEs but also to achieve rapid energy payback time and sustainability¹³. Ion motion within the perovskite could lead to degradation of the perovskite material as it becomes depleted in I⁻, and will inevitably lower the PCE of the cell by reducing the built-in electric field in the perovskite. Furthermore, ion motion is not an effect that can be averted by encapsulation^{14,15}.

Snaith *et al.*⁸ suggested three origins for hysteresis from the perovskite layer, either solely or in combination: (a) a large defect density close to interfaces with adjacent layers; (b) slow polarization of the material due to bias dependent motion or changes in configuration of the ferroelectric domains¹⁶; (c) vacancy aided migration of ions through the film. Mechanism (a) is unlikely since electronic transport to the layer takes \sim ns due to the high electronic mobility (though we note that charges could detrapp on a timescale comparable to that associated with the hysteresis) and mechanism (b) is ruled out by electrical measurements¹⁷. Belstein-Edmands *et al.*¹⁷ provide strong evidence for mechanism (c) estimating that motion of up to 3.7 % of I⁻ contributes to the hysteresis. With a measured stored charge density of 2.5 mC/cm² at 2 V, an ionic capacitance of 0.28 mF is inferred, similar to the low frequency capacitance reported elsewhere⁹. Recent work¹⁸ has shown that hysteresis can be reduced by replacing the TiO₂ layer by PCBM and that this is associated with a reduction in the

^a Mathematical Sciences, University of Southampton, UK.

^b Department of Physics, University of Bath, UK.

^c Department of Chemistry, University of Bath, UK.

^d Department of Mathematics and Statistics, McMaster University, Hamilton, Canada.

^e Department of Physics, University of Bath, UK. E-mail: a.b.walker@bath.ac.uk

† Electronic Supplementary Information (ESI) available. See DOI: 10.1039/b000000x/



low frequency capacitance of the cell. Apparent PCEs of 11 % and 13 % have been measured from the J - V scans of meso-structured cells without a TiO₂ blocking layer but the cells have nevertheless been shown to have nearly zero stabilized power output¹⁹. Li *et al.*¹⁵ have shown that by preconditioning similar cells that apparent PCEs increased from less than 1% to over 8% and that this can be attributed to ion motion. O'Regan *et al.*²⁰ found that that the apparent efficiency of a cell aged for 100 days varied between 0.1% and 9% depending on the time for which the cell was held at forward bias. In addition they were able to identify two distinct contributions to the transient response of the cell one of which (on a microsecond timescale) they ascribe to detrapping of electrons and the other (on the scale of 10s of seconds) they ascribe to ion motion or dipole realignment. In terms of their capacitances the slow timescale response is much more significant than the fast timescale one.

Yang *et al.*²¹ support the hypothesis that hysteresis arises from the motion of I⁻ ions in the perovskite, inferring an ionic diffusion coefficient of $2.4 \times 10^{-8} \text{ cm}^2 \text{ s}^{-1}$. Atomistic calculations by Eames *et al.*²² using Density Functional Theory, DFT, methods employing an ab initio code showed the fastest ion motion is vacancy assisted I⁻ diffusion. Here the positively charged I⁻ vacancies are the mobile species rather than the I⁻ ions, with an activation energy E_A of 0.58 eV from which a diffusion coefficient $D_+ \sim 10^{-12} \text{ cm}^2 \text{ s}^{-1}$ was deduced at a temperature of 320 K for an assumed attempt frequency of 10^{12} Hz . They *postulated* that this vacancy migration could help to explain hysteresis. Other ion species that could also explain hysteresis include negatively charged I⁻ interstitials, which could also explain the results of Yang *et al.*²¹ and negatively charged MA⁺ and Pb²⁺ vacancies. Eames *et al.*²² calculated E_A to be 0.84 eV and 2.31 eV respectively, leading to $D_+ \sim 10^{-16} \text{ cm}^2 \text{ s}^{-1}$ and effectively zero respectively. On the other hand, DFT calculations by Azpiroz *et al.*²³ yielded E_A to be $\sim 0.16 \text{ eV}$, 0.5 eV and 0.8 eV respectively for I⁻, MA⁺ and Pb²⁺ vacancies. They suggested that I⁻ vacancies and interstitials move too quickly to be responsible for the hysteresis and therefore MA⁺ vacancies are a possible cause. A $D_+ \sim 10^{-4} \text{ cm}^2 \text{ s}^{-1}$ for I⁻ vacancies that can be deduced from E_A of 0.16 eV is large enough for the electric field across the device to be fully compensated before the MA⁺ vacancies could move. MA⁺ and Pb²⁺ vacancy motion is also inconsistent with the results of Yang *et al.*²¹.

The large number of results described above that lack a coherent explanation demonstrate that much perovskite research is based on a 'shake and bake' approach, uninformed by an understanding of the underlying mechanisms. Given the complexity of the proposed hysteresis mechanisms, a device model is essential and is one of 10 critical challenges posed in a recent review²⁴. Atomistic models show considerable discrepancies for parameters governing ion motion as shown in the previous paragraph. Furthermore, the use of such models on the length scales required to study charge transport in solar cells is not feasible because of the huge computational cost involved; the appropriate tool for such studies (especially for planar devices) is the drift diffusion, DD, method²⁵. DD models of coupled ion-electron conduction allow us to understand the effect of mobile ions on the opera-

tional mechanism of the device^{8–12,19,22,23} and pave the way for the development of cells with improved and reproducible performance. The model reported here is a development of the DD model by Foster *et al.*²⁶. This model has guided developments in cell longevity via an equivalent circuit model that quantified the loss in charge arising from shunting where the metal electrode and the perovskite absorber layer make contact²⁷.

Within our DD picture, a built-in voltage V_{bi} , determined by the difference in the Fermi levels in the TiO₂ and the spiro layers, gives rise to an electric field V_{bi}/b in the perovskite layer. This field drives positive charges towards the spiro layer and negative charges towards the TiO₂. At short circuit, free electron-hole pairs are separated by this field to create a current in which electrons are extracted through the TiO₂ layer and holes are extracted through the spiro layer. A positive applied bias, V , produces an electric field that opposes the built-in field. In the absence of charge build up within the perovskite there is a net electric field $(V_{bi} - V)/b$ from left to right. When $V < V_{bi}$, this field drives the positively charged iodide vacancies into the region of the perovskite adjacent to its interface with the spiro, where they create a narrow positively charged layer of total areal charge density Q_+ . To maintain overall charge neutrality, there is also a negatively charged layer, created by depletion of the iodide vacancies of total areal charge density Q_- , in the region of the perovskite adjacent to its interface with the TiO₂. Fig. 1 illustrates the resulting electric potential and conduction band profile.

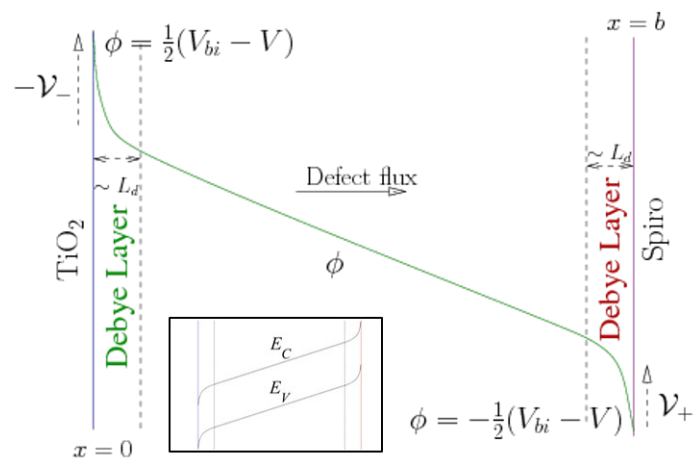


Fig. 1 Schematic of the electric potential ϕ in the perovskite. ϕ is linear across most of the perovskite film but varies rapidly across narrow Debye layers at its edges, jumping by an amount V_- across the left-hand layer and V_+ across the right-hand layer. We assume the applied bias V is zero at short circuit and is positive at the right hand contact relative to the left hand contact. The inset shows the equivalent band energy diagram in the perovskite. E_C and E_V depend upon ϕ via $E_C = -E_{ea} - q\phi$ and $E_V = -E_{ea} - E_g - q\phi$ where E_{ea} and E_g are the electron affinity and energy gap, respectively.

The charge accumulation layers, termed Debye layers, are examples of a diffuse double layer, such as seen in electrolytes^{28,29}. The width of the layers can (as for electrolytes) be estimated from the Debye length L_D , which is proportional to the reciprocal of the square root of the density of the mobile charged species. Ab initio theory³⁰, predicts an equilibrium I⁻ vacancy density of 1.6×10^{19}



cm^{-3} and a corresponding Debye length $L_D \approx 1.5$ nm that is much smaller than the perovskite layer width ≈ 300 nm. Our approach explicitly accounts for ion motion and *predicts* charge accumulation in these layers on the time scales associated with mobile defect motion in the perovskite that are consistent with experimental measurements and theoretical estimates of D_+ . Using the vacancy diffusion coefficient $10^{-12} \text{ cm}^2 \text{ s}^{-1}$ calculated by Eames *et al.*²² leads to an estimate of the timescale for vacancy diffusion across a distance $5L_D$ of around 0.5 s which is consistent with experimental observations of hysteresis at scan rates of $\sim 1 \text{ V s}^{-1}$ from open circuit to short circuit and back.

There are very few published DD models of perovskite cells^{31–34}. Of these, only Van Reenen *et al.*³⁴ (published while this work was in review) addresses ion migration. In that work a finite difference based numerical scheme is employed. The constant grid spacing of 4 nm is far too coarse to resolve the Debye layers. Their assumed value of D_+ is 10^6 times greater than that of Eames *et al.*²² and voltage scan rates around 10^6 times greater than the experimental scan rates at which hysteresis is observed, ruling out a quantitative comparison with experiment.

Our approach is more sophisticated and involves solving explicitly for the potential and ion distributions in the narrow (and problematic) Debye layers. By comparing our results to experiment, we can deduce the value of D_+ , finding it to be close to the value of $10^{-12} \text{ cm}^2 \text{ s}^{-1}$ predicted by Eames *et al.*²². With additional experimental J - V curves for different device structures and scan rates, our model would help resolve the question whether other mobile species, such as MA^+ and Pb^{2+} vacancies contribute to hysteresis. With a little additional work our model can also be used to address empirical observations showing that cells with fullerene (C60) derivative PCBM, [6,6]-phenyl-C61-butyric acid methyl ester, as an electron transport layer have reduced hysteresis¹⁸. This reduction is especially marked in inverted structures such as ITO/PEDOT:PSS/MAPbI₃/PCBM/C60/BCP/Al. Here ITO is Indium Tin Oxide, PEDOT:PSS is poly(3,4-ethylenedioxythiophene) polystyrene sulfonate and BCP is bathocuproine^{18,35}. The reduction in hysteresis in these devices is also predicted by our model and is the subject of a current study, but is outside the scope of this paper which focuses on the conventional TiO₂ and spiro based devices.

It is possible that illumination levels may also influence vacancy concentration. Hoke *et al.*³⁶, for example, speculate that photoexcitation may cause halide segregation in mixed halide perovskites resulting in photoinduced trap formation that could influence hysteresis. However, since no clear experimental evidence exists for such effects, we omit them from our model.

To validate our model, we compare its predictions with experimental measurements on two cells *chosen* to demonstrate high levels of hysteresis. Features seen in the measured J - V curves at varying scan rates, such as a shallow peak on scans from 1.2 V to short circuit, can be explained in terms of a time varying internal electric field across the perovskite layer. These measurements, and their interpretation, are extended to include discussion of the influence of preconditioning. By reporting on the two cells, we show how much J - V characteristics vary for cells fabricated

in the same way but with different preconditioning. Validation of our methodology through this comparison opens the way to study other solar cells containing mixed ionic electronic conductor materials, such as CuInSe₂ in which Cu⁺ can migrate¹⁴.

2 Methods

Choice of Model Parameters

Table 1 shows parameter definitions and values adopted in our model. All values are for room temperature, set as 300 K. Values for n_0 and p_0 were calculated from the effective density of states \hat{g}_c , \hat{g}_v , the conduction and valence band edges E_C and E_V and the Fermi levels in the TiO₂ and spiro E_{Ft} , E_{Fs} . Parameters fit to ex-

Table 1 Parameters used in the drift-diffusion simulations fixed a priori

Symbol	Description	Value
N_0	I ⁻ vacancy equilibrium density	$1.0 \times 10^{17} \text{ cm}^{-3}$ Figs. 3, 4 $1.6 \times 10^{19} \text{ cm}^{-3}$ Figs. 5–8 ³⁰
n_0	Density of free electrons at TiO ₂	$6.9 \times 10^{13} \text{ cm}^{-3}$ Refs. ^{37,38}
p_0	Density of free holes at spiro	$1.0 \times 10^{12} \text{ cm}^{-3}$ Refs. ^{37,38}
\hat{g}_c	Conduction band density of states	$8.1 \times 10^{18} \text{ cm}^{-3}$ Ref. ³⁸
\hat{g}_v	Valence band density of states	$5.8 \times 10^{18} \text{ cm}^{-3}$ Ref. ³⁸
\hat{D}_n	Electron diffusion coefficient	$1.7 \text{ cm}^2 \text{ s}^{-1}$ Ref. ³⁹
\hat{D}_p	Hole diffusion coefficient	$1.7 \text{ cm}^2 \text{ s}^{-1}$ Ref. ³⁹
E_C	Conduction band minimum	-3.7 eV Ref. ³⁷
E_V	Valence band maximum	-5.4 eV Ref. ³⁷
E_{Ft}	TiO ₂ Fermi level	-4.0 eV Ref. ³⁷
E_{Fs}	Spiro Fermi level	-5.0 eV Ref. ³⁷
L_d	Debye length = $(\epsilon_p V_T / (q N_0))^{1/2}$	1.5 nm
b	Perovskite layer width	$6 \times 10^{-5} \text{ cm}$ Ref. ³⁹
ϵ_0	Vacuum permittivity	$8.85187 \times 10^{-12} \text{ Fm}^{-1}$
ϵ_p	Static dielectric constant	$24.1 \epsilon_0$ Ref. ³⁸
q	Electron charge magnitude	$1.602 \times 10^{-19} \text{ C}$
V_T	Thermal voltage	0.0257 V
V_{bi}	Built-in voltage	1V
v_{scan}	scan rate	see figure caption
α	absorption coefficient	$1.3 \times 10^5 \text{ cm}^{-1}$ Ref. ⁴⁰

periment are shown in Table 2. Our treatment of light absorption via the Beer-Lambert law with a single value for the absorption coefficient is approximate so we have used a value of F_{ph} that gives short circuit current densities in the range 5–15 mA cm^{-2} , reproducing measurements by Sanchez *et al.*⁹ and the measurements reported in the Results section. Tress *et al.*¹¹ find that hysteresis is independent of illumination, motivating our assumption that D_+ is similarly independent of illumination despite its soft structure. The perovskite film nanoscale morphology, in the form of its grain boundary structure, influences D_+ and accounts differences between cells fabricated in the same way. Fitting predicted J - V characteristics for varying scan rates to experiment gives an estimate of D_+ that differs by a factor of three between the two cells. Our estimates for D_{1+} and D_{2+} are both within a factor of 10 of that calculated by Eames *et al.*²² but are further away from that determined by Yang *et al.*²¹.

The differences in the values of τ_n and τ_p between the cells can be accounted for by the strong influence of perovskite morphology on recombination. These values were chosen to give an open circuit voltage of 1 V, which approximately matches the experimentally measured values on the scan from 0 V to 1.2 V. The predicted J - V curves for this scan are sensitive to τ_p/τ_n (ESI Note 2).



Table 2 Parameter values derived from fitting the drift-diffusion simulations to experiment.

Symbol	Description	Value
F_{ph}	Intensity at $x = 0$	$9.45 \times 10^{16} \text{ cm}^{-2} \text{ s}^{-1}$
D_{1+}	Cell 1 I^- vacancy diffusion coefficient	$1.0 \times 10^{-11} \text{ cm}^2 \text{ s}^{-1}$
τ_{n1}	Cell 1 Electron pseudo-lifetime	0.38 ns
τ_{p1}	Cell 1 Hole pseudo-lifetime	3.8 ps
D_{2+}	Cell 2 I^- vacancy diffusion coefficient	$3.7 \times 10^{-12} \text{ cm}^2 \text{ s}^{-1}$
τ_{n2}	Cell 2 Electron pseudo-lifetime	0.30 ns
τ_{p2}	Cell 2 Hole pseudo-lifetime	3.0 ps

Modelling charge transport in the perovskite layer by Drift Diffusion, DD

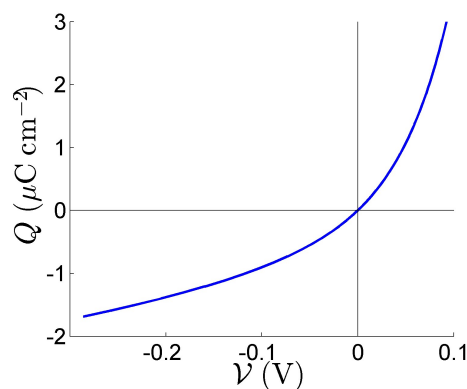
Vacancy mediated ion transport is modelled in a single layer of perovskite sandwiched between highly doped spiro and TiO_2 buffer layers. It is assumed that the doping levels in the buffer layers are sufficiently high to force them to be at the same electric potential as their respective contacts. The potentials at the perovskite-buffer layer interfaces are thus approximately equal to the potentials at their respective contacts. This allows the problem to be simplified to one in the perovskite layer only. In line with Eames *et al.*²² who estimate the diffusion coefficient of the I^- vacancies to be four orders of magnitude greater than that of the other ionic constituents (Pb^{2+} and MA^+) we assume that the only mobile charged species in the perovskite, other than holes and electrons, are the I^- vacancies. Furthermore we assume that these vacancies do not migrate into the blocking layers. Whilst in some cells there is evidence that the I^- ions pass through pinholes in the spiro to the metal contact⁴¹, our overall conclusions still hold, and we are currently looking to how to extend our model to this case.

The narrowness of the Debye layers that ensue from the high ion density, and the very strong variations of ion concentration and potential within them, render direct numerical solution of a drift-diffusion (DD) model extremely challenging, see for example²⁹. Even with a highly tailored numerical approach, such as the one adopted here, it is not possible on a practical timescale to compute an accurate representation of the solution. Here, in order to circumvent these difficulties an approximate approach is adopted based on asymptotic expansions.

The validity of this approach is demonstrated by comparing the potentials and ion densities obtained from a numerical solution to the DD model (ESI note 1) with the asymptotic approximation (briefly described below) to the same model, albeit for unrealistically low iodide vacancy concentrations. A brief description of the asymptotic method follows. Matched asymptotic expansions (cf. Foster *et al.*²⁶) can be used to derive a capacitance relation between the charge Q per unit area in a Debye layers and the potential drop V across it; for a single mobile positively charged species (*i.e.* an I^- vacancy)

$$Q(V) = \frac{\varepsilon V_T}{L_d} \text{sign}(V) \left[2 \left(e^{V/V_T} - 1 - \frac{V}{V_T} \right) \right]^{1/2}, \quad (1)$$

and is plotted in Fig. 2 (a similar capacitance relation has been derived, in a different context, by Richardson⁴²). Equation (1) is valid for diffuse layers in which the density of vacancy sites

**Fig. 2** The relation between the charge Q in the Debye layer and the potential drop V across the layer.

does not limit vacancy density (*i.e.* volume exclusion effects are insignificant) and is thus analogous to the capacitance relation calculated from Gouy-Chapman theory for a 1:1 electrolyte. The fact that only one ion species is mobile is reflected in the asymmetry of the capacitance curve in Fig. 2, which contrasts to the symmetric capacitance curve predicted for a 1:1 electrolyte by Gouy-Chapman theory. The diffuse layer approximation holds well for $N_0 = 1.0 \times 10^{17} \text{ cm}^{-3}$ used in Figs. 3 & 4 but can start to break down for the higher equilibrium vacancy density, $N_0 = 1.6 \times 10^{19} \text{ cm}^{-3}$ predicted by Walsh *et al.*³⁰. This breakdown occurs if Q_+ , the charge per unit area in the vacancy accumulation layer (the right-hand layers in Figs 3 & 4), becomes sufficiently large to result in vacancy densities comparable to the density of vacancy sites (*i.e.* volume exclusion effects become significant). Nevertheless this effect is not strong enough, with $N_0 = 1.6 \times 10^{19} \text{ cm}^{-3}$, to alter the results qualitatively.

In practice it is easier to solve directly for surface charge densities stored in the left- and right-hand Debye layers (Q_- and Q_+ , respectively) rather than for the potential drops across these layers, V_- and V_+ (illustrated in Fig 1). In order to do this it is necessary to invert the capacitance relation (1) to obtain expressions for V_- and V_+ in terms of Q_- and Q_+ of the form

$$V_- = V(Q_-), \quad V_+ = V(Q_+) \quad \text{where} \quad V(\cdot) = Q^{-1}(\cdot). \quad (2)$$

The density of generated electron-hole pairs is insufficient to screen the electric field in the perovskite between the Debye layers so that the potential profile is linear, as shown in Fig. 1, and the electric field $E_{bulk}(t)$ is spatially uniform; $E_{bulk}(t)$ can therefore be evaluated from the potential difference between points just inside the two Debye layers and is thus given by

$$E_{bulk}(t) = \frac{V_{bi} - V(t) - V_+ + V_-}{b}. \quad (3)$$

as can be seen from Fig. 1. Furthermore since the mobile ion concentration is uniform (and equal to N_0) within the perovskite bulk, the corresponding ion current density is well-approximated by $j_{ion} = \sigma E_{bulk}(t)$, where $\sigma = qD_+N_0/V_T$ is the ionic conductivity. It follows, from the assumption that ions cannot migrate into the blocking layers, that the rates of change of Q_- and Q_+ are given



by the ion currents flowing from the perovskite into the Debye layers

$$\frac{dQ_-}{dt} = -j_{ion}(t), \quad \frac{dQ_+}{dt} = j_{ion}(t). \quad (4)$$

Given initial charge neutrality these equations imply the charge conservation relation

$$Q_- = -Q_+. \quad (5)$$

It therefore suffices to solve only for Q_+ from the equation obtained by substituting for j_{ion} in (4), namely

$$\frac{dQ_+}{dt} = \frac{qD_+N_0}{V_T} E_{bulk}(t) \quad (6)$$

Here $E_{bulk}(t)$, V_- and V_+ are obtained, in terms of Q_+ , from (2), (3) and (5) and are used as input to a 1-d DD model for electron and hole densities (n and p) within the perovskite. Multiple ion species can be introduced by providing a contribution for each species on the right hand side of equation (6).

The equations for the drift diffusion model are well known and so are provided in ESI Note 2 rather than the main paper. Equations (1) and (2) of ESI Note 2 are the continuity equations for electrons and holes combined with the equations for the current densities in terms of their diffusion and drift components. The generation rate used in this DD model is the Beer-Lambert law while charge recombination is assumed to be predominantly trap assisted and to obey Shockley-Read-Hall theory. Its numerical solution is determined by using the package Chebfun⁴³ and yields electron and hole current densities (j_n and j_p , respectively) which are used to obtain an expression for the total current density across the cell $J(t)$. Plots of $J(t)$ versus the applied voltage $V(t)$ yield the predicted hysteresis curves which are compared to measurements from 2 cells. The latter are made using the same process which is described in the cell fabrication and characterization section below.

Since device history affects the measured J - V curves it is important to capture its effects accurately. After light soaking at open circuit, both cells were preconditioned at 1.2 V for 5 s, then swept from 1.2 V to 0 V and back again three times (these measurements are described below and the full results shown in ESI Fig 1). The scan rate, v_{scan} , was assigned values 1 V/s, 500 mV/s, 250 mV/s and 100 mV/s. Further J - V curves, reported in ESI Fig 2(b), were measured from cell 2, which was subsequently preconditioned for 5 s at 0 V immediately after the initial set of measurements were performed.

Two different protocols were used to model: (I) the J - V curve obtained from the third scan after the effects of the preconditioning have worn off and (II) the J - V curve obtained from the first scan immediately after the preconditioning step. Since simulating all three scans is computationally intensive we choose in case (I) to start the simulation by letting the cell equilibrate at $V = 1$ V (i.e. V_{bi}) so that the Debye layers are initially uncharged (i.e. the sweep begins at $t = 0$ with $Q_+ = 0$) and then scan the voltage down from 1 V down to 0 V by setting $V(t) = 1 \text{ V} - v_{scan}t$ between $t = 0$ to $t = (1 \text{ V})/v_{scan}$ and then scan back again at the same

rate. Although this procedure may appear *ad-hoc* we can justify it by noting that after two cycles the preconditioning effects have worn off so that the Debye layers will be close to being uncharged ($Q_+ = Q_- \approx 0$) at $V = V_{bi}$. In case (II) the pre-conditioning step is explicitly accounted for by starting the simulation at $t = -5$ s with $Q_+ = 0$ and then immediately increasing V to 1.2 V where it remains for 5 s until $t = 0$, after which the downward scan is commenced with $V(t) = 1.2 \text{ V} - v_{scan}t$ from $t = 0$ to $t = (1.2 \text{ V})/v_{scan}$; when V reaches 0 at $t = (1.2 \text{ V})/v_{scan}$ the direction of the scan is reversed by choosing $V(t) = v_{scan}t - 1.2 \text{ V}$ between $t = (1.2 \text{ V})/v_{scan}$ and $t = (2.4 \text{ V})/v_{scan}$. ESI Fig. 2(a),(c),(d) shows predictions from our model where we follow a similar procedure to case (II), but here the preconditioning is at 0 V for 5 s before scanning to 1.2 V and back.

Cell fabrication and characterization

Methylammonium iodide was synthesized by drop-wise addition of 10 mL of HI (57 wt% in water, *Sigma-Aldrich*) to a cooled solution of 24 mL methylamine (33 wt% in EtOH, *Sigma-Aldrich*) in 100 mL ethanol under steady stirring. The solvent was removed in a rotary evaporator and then the salt was recrystallized from ethanol. Upon slowly cooling the ethanol solution, white crystals formed. Washing with diethylether and drying at 70 °C for 6 hours gave a pure product. For the compact layer of TiO₂ a solution with 35 μL of 2 M HCl in 2.5 mL IPA was drop-wise added to a solution with 369 μL titanium isopropoxide (97%, *Sigma-Aldrich*) in 2.5 mL of IPA under heavy stirring. The solution for the hole transporting layer was mixed by dissolving 72.3 mg of spiro-MeOTAD (99%), *Borun chemicals*) in 1 mL chlorobenzene at ~ 60 °C for 30 min and then adding 8.75 μL 4-tert-butyl pyridine (tBP) and 18.75 μL Li-TFSA solution (170 mg/mL in acetonitrile).

For device fabrication, substrates of FTO/glass (TEC7, 7 Ω/cm², *Pilkington*) were partially etched with Zn and 2 M HCl and cut into device sizes. Cleaning was done with Hellmanex solution (2 wt % in water), deionized water, acetone and oxygen plasma treatment for 30 min. A compact layer of TiO₂ was spin-coated from the TTIP solution for 60 s at 2000 rpm (2000 rpm/s ramp rate) then annealed at 500 °C for 30 min.

The perovskite layer was deposited via vapour assisted solution processing, VASP⁴⁴. First, a hot solution of PbI₂ (99 %, *Sigma-Aldrich*) in DMSO (1 M, 70 °C) was spin-coated onto the heated FTO/glass substrate (70 °C) for 60 s at 2000 rpm. The PbI₂ film was then annealed at 100 °C for 10 min. Conversion into perovskite films was done by vapor deposition of MAI. Therefore the MAI powder was put onto a hotplate together with the substrates and sealed with a desiccator lid. A temperature of 120 °C and low-vacuum were applied. Sublimation of the MAI converted the PbI₂ into MAPbI₃ within 30 min. The perovskite films were rinsed with IPA and blow-dried with nitrogen. For the hole-transporting layer the spiro solution was spread on the sample and left for 10 s before spin-coating at 4000 rpm for 45 s. Finally, a gold cathode was deposited via thermal evaporation with a shadow mask, resulting in a active area of 0.1 cm².

A *TS Space Systems* solar simulator was used with a 200 W metal halide lamp and an internal AM1.5 filter, which is cali-



brated against a *Fraunhofer* reference cell (ISE, RS-OD-4). The solar simulator is classified according IEC 60904-9 Edition2 and ASTM E927-10 standards as class A. *Keithley* 2600A SourceMeter was used for the *J-V* measurements.

Two cells were prepared using the above methods, each containing ten pixels. Both cells were measured with the following protocol. The cells were connected to the solar simulator and held at open circuit, V_{oc} , in the dark for several minutes. Then the cells were then held at V_{oc} for 30 s under illumination to allow a steady photovoltage to be achieved. In a preconditioning stage, the cells were held at 1.2 V for 5 s. Following this stage, the cells were swept from 1.2 V to 0 V and back to 1.2 V three times. The scan rate was then reduced and the scans repeated. In ESI Fig. 2(b), cell 2 *J-V* characteristics were measured in the same way except that the preconditioning voltage was 0 V. These cell 2 measurements followed immediately after the measurements for preconditioning at 1.2 V.

3 Results

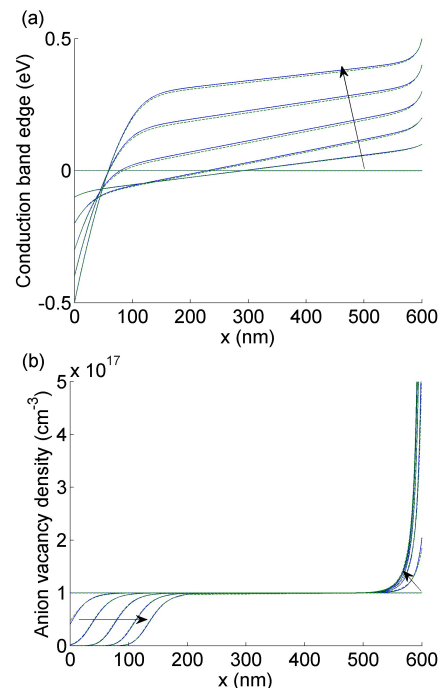


Fig. 3 Comparison between the numerical (solid blue) and the asymptotic (dashed green) solutions to $E_C(x)$ (panel a) and $P(x)$ (panel b) as the applied voltage $V(t)$ is scanned from 1 V to 0 V taking values in V of 0.8, 0.6, 0.4, 0.2, 0. At time $t=0$, $E_C(x)=0$ for all x . The arrow indicates the direction of increasing time. For this Figure and Fig. 4, $N_0 = 10^{17} \text{ cm}^{-3}$.

The evolution of E_{bulk} is illustrated in Figs. 3(a) and 4(a) and the I^- vacancy concentration profile $P(x,t)$ in Figs. 3(b) and 4(b). These figures show a series of snapshots of the solution at evenly spaced time intervals in the scans down from $V = 1 \text{ V}$ to $V = 0 \text{ V}$ and back from $V = 0 \text{ V}$ to $V = 1 \text{ V}$, respectively. Comparison between the uniformly valid asymptotic solution and the numerical solution to the ion transport problem (green dashed and blue solid curves, respectively) is made in these figures (the agreement is extremely good).

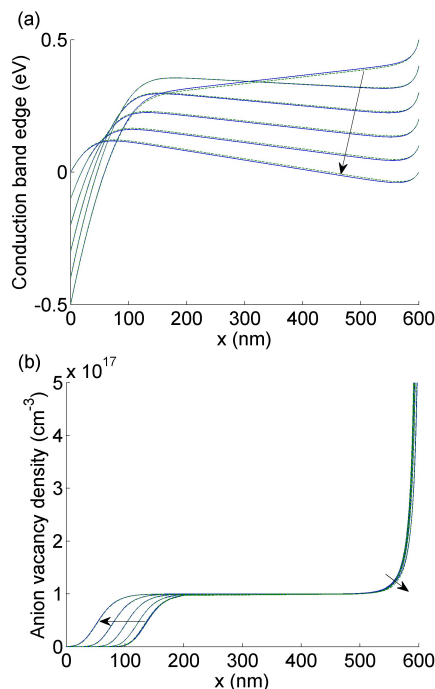


Fig. 4 As for Fig. 3 but here $V(t)$ is scanned from 0 V to 1 V and plotted at values in V 0, 0.2, 0.4, 0.6, 0.8, 1.0.

The bulk electric field $E_{bulk}(t)$ is equal to the gradient of $E_C(x,t)/q$ within the central portion of the perovskite layer and is positive as $V(t)$ is decreased from 1 V to 0 V (Fig. 3(a)), driving holes to the spiro layer and electrons to the TiO_2 layer. Sharp changes in $E_C(x)$ (of magnitude qV_- , qV_+) are seen across the left-hand and right-hand Debye layers, respectively. Positively charged I^- vacancies flow into the right-hand Debye layer, increasing Q_+ , and away from the left-hand Debye layer. The latter layer acquires its negative charge through vacancy depletion. Its width L_- is determined by the need to maintain charge neutrality, so that

$$Q_+(t) = |Q_-(t)| = q \int_0^{L_-} P(x,t) dx = q \int_{b-L_+}^b P(x,t) dx, \quad (7)$$

where L_+ is the width of the right-hand Debye layer. Since $0 < P(x,t) < N_0$ in the left hand layer while $P(x,t) \gg N_0$ in the right-hand layer, the extent of the left-hand layer L_- is greater than that of the right-hand one L_+ in order to fit the same amount of charge into both. As Q_+ and $|Q_-|$ increase, L_- also increases significantly, see Fig. 3. The greater extent of the left-hand layer in comparison to that of the right-hand one gives a greater magnitude of potential drop $|V_-|$ across it compared to that across the right-hand one V_+ .

Note that $E_{bulk}(t)$ becomes negative as $V(t)$ returns from 0 V to 1 V (Fig. 4(a)). This change in the sign of E_{bulk} can be used, in part, to explain the difference between the measured current in the 1.2 V to 0 V scan from that in the 0 V to 1.2 V scan. When $E_{bulk} < 0$, the field drives the free charge carriers away from the contacts where they are extracted, into the bulk of the device, leading to large carrier concentrations and increased recombination. The charge density accumulations from the mobile vacan-



cies Q_- and Q_+ influence the free charge carrier densities at the boundaries, causing diffusion currents towards or away from the contacts. These diffusion currents can exceed the drift component. In spite of this diffusion contribution, the current is typically smaller on the 0 V to 1.2 V scan than it is on the 0 V to 1.2 V scan.

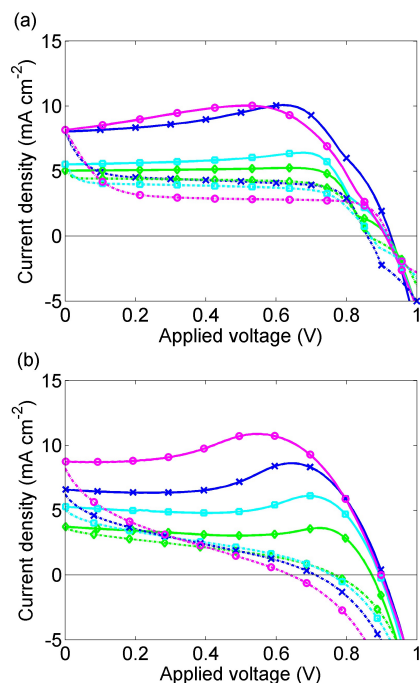


Fig. 5 a) Calculated J - V curves for cell 1 without allowing for preconditioning; (b) measured J - V curves for cell 1 after an initial preconditioning at 1.2 V and two scan cycles. Solid lines show the 1.2 V to 0 V scan; broken lines show the 0 V to 1.2 V scan. Scan rates are 1 V/s (magenta, circles), 500 mV/s (blue, crosses), 250 mV/s (cyan, filled squares), 100 mV/s (green, diamonds). As discussed in the text the third scans are shown as the effect of the 1.2 V preconditioning is removed.

Experimental J - V data from 3 complete scan cycles of cell 1 which has been preconditioned for 5 s at 1.2 V are shown in ESI Fig. 1(a)-(c). Fig. 5(b) plots experimental J - V data from the third scan cycle performed on cell 1. The agreement between these results and the model solutions, computed as described above, case (I) in the Methods section, and plotted in Fig. 5(a), is very good.

Fig. 6 depicts the evolution of the bulk electric field E_{bulk} and the Debye layer surface charge density Q_+ arising from the vacancy motion predicted by the model used to simulate the J - V curves in Fig. 5(a). As noted previously where $E_{bulk}(t) > 0$, positively charged I^- vacancies flow into the right-hand Debye layer, increasing Q_+ . For large positive Q_+ , the potential drop across the left-hand Debye layer, $-V_-$, is large and positive and screens out the field from the potential across the contacts. In the subsequent 0 V to 1 V scan the screening, which lags behind the scan, typically leads to negative E_{bulk} , putting the cell into effective forward bias and leading to high recombination rates.

The model is able to predict the maximum in the current density on the 1 V to 0 V scan, seen in measurements reported here and elsewhere^{9,11}. This is closely associated with a maximum in E_{bulk} the field that drives the charge carriers apart. This re-

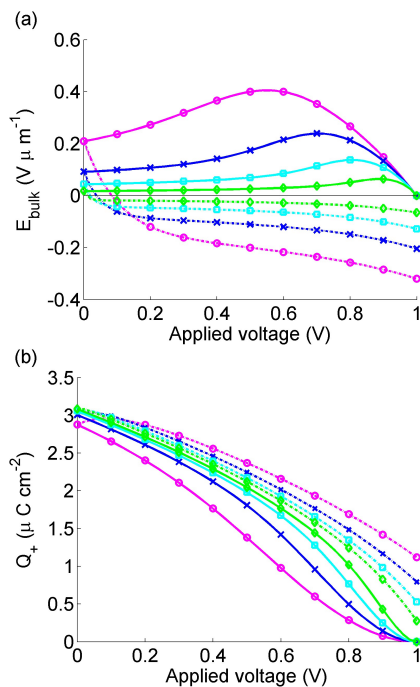


Fig. 6 Electric field between the Debye layers E_{bulk} (panel a) and charge per unit area in the Debye layer next to the spiro Q_+ (panel b) used to find calculated J - V curves for cell 1 shown in Fig. 5. Scan rates and solid and dashed lines as for Fig. 5.

sult strengthens the hypothesis that large positive values of E_{bulk} suppress recombination, increasing current output.

The vacancy mediated ion motion hypothesis provides a clear explanation for the influence of scan rate on J - V curves. For slower scan rates, the vacancies have more time to respond to the change in applied voltage than for faster scans. Hence, the vacancy charge screens the bulk electric field more effectively on slower scans than on fast ones, so $|E_{bulk}|$ remains relatively small on such slow scans, resulting in limited hysteresis. For intermediate scan rates, hysteresis is strongest. At the other extreme, if the scan is sufficiently fast, the ions do not have a chance to build up in the Debye layers so that there is very limited screening and consequently little hysteresis (and increased short circuit current). This effect is not addressed here but is reported elsewhere^{10,11}.

Snaith *et al.*⁸ also report an increase in hysteresis with reduction in scan rate even at scan rates as low as 11 mVs⁻¹. This observation contrasts with our data which suggests that hysteresis is reduced by a decrease in scan rates below about 1 Vs⁻¹. The 1.4 V to 0 V scans in ref.⁸ vary little with scan rate, which could be a result of the strong preconditioning (60 s at 1.4 V) used. It may be the case that this strong preconditioning makes E_{bulk} high enough to yield a large current for the whole of 1.4 V to 0 V and 0 V to 1.4 V scans, unless the scan rate is very slow. Only when Snaith *et al.*⁸ decreased the scan rate to 11 mVs⁻¹ did the current maximum reappear.

Deviations between the experimental and theoretical results occur for the fastest scan rate, 1 V/s, and when the applied voltage is increasing from 0 V to 1 V. For the calculated 0 V to 1 V scans, J



is nearly independent of V except for sharp changes in J close to open circuit. In contrast, the measured 0 V to 1.2 V scans have a continuously varying slope. Evidence from an analytic solution to the DD carrier equations that we have derived when $\tau_p = 0$ suggests that decreasing τ_p further could help correct this discrepancy between experiment and theory. However for $\tau_p < \tau_n/100$, the DD equations for the free charge carriers become so stiff that numerical solutions become very difficult to find.

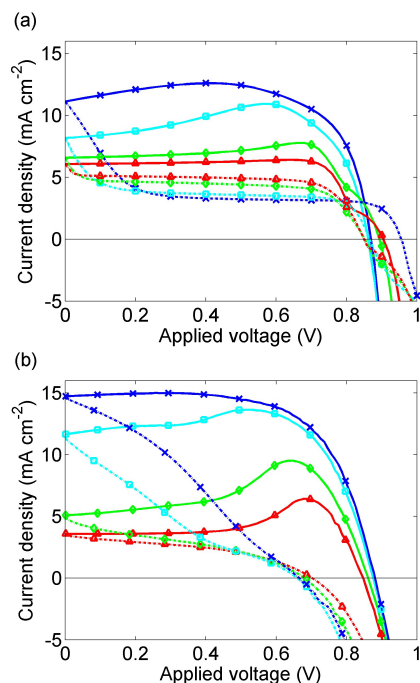


Fig. 7 (a) Calculated J - V curves for cell 2 allowing for 5 s preconditioning at 1.2 V. (b) Measured J - V curves for cell 2 on the 1st scan cycle immediately after preconditioning for 5 s at 1.2 V. Solid lines show the 1.2 V to 0 V scan; broken lines show the 0 V to 1.2 V scan. Scan rates are as for Fig. 5 with the addition of a scan rate of 50 mV/s (red, triangles). In the fastest scans the shapes of the J - V curves are improved by the preconditioning.

Experimental J - V data from 3 complete scan cycles of cell 2, which like cell 1 has been preconditioned for 5 s at 1.2 V, are shown in ESI Fig. 1(d)-(f). These plots show how the effects of the preconditioning step diminish over successive scan cycles. In Fig. 7(b), this data is shown for the first scan cycle. Preconditioning plays a significant role in the subsequent evolution of the J - V curve in contrast to the data presented in Fig. 5(b) for the third scan cycle.

The simulated J - V curve for cell 2, computed using case (II) in the Methods section, is plotted in Fig. 7(a) while the solution for E_{bulk} and Q_+ are plotted in Fig. 8. Comparison to experimental data, though still good, is not as good as in Fig. 5. This discrepancy may arise because the preconditioning step occurs at 1.2 V, outside the range $V \leq 1V$ in which the effect of electrons and holes on the potential can be neglected. The model therefore overpredicts the charge accumulation (negative Q_+) in the preconditioning step. The sensitivity to preconditioning seen in Figs. 7(a) and (b) was also observed by O'Regan *et al.*²⁰.

On commencing preconditioning, $Q_+ = 0$. Since the preconditioning occurs at 1.2 V which exceeds V_{bi} , the net field in the bulk

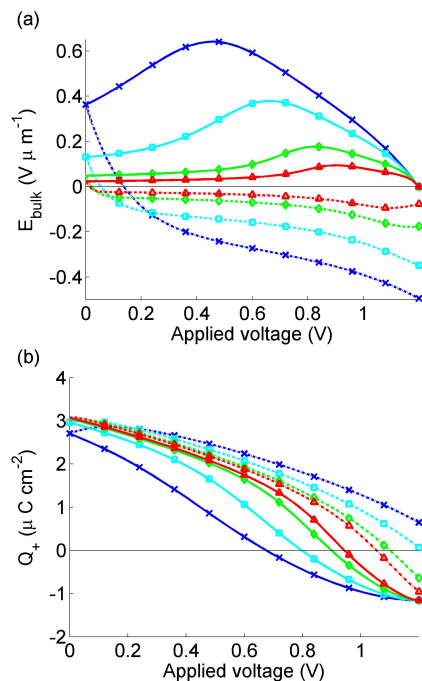


Fig. 8 As for Fig. 6, but for calculated J - V curves for cell 2 shown in Fig. 7 where we model effects of 5 s preconditioning at $FB = 1.2$ V.

of the perovskite layer E_{bulk} is negative. As a consequence, the I^- vacancies drift towards the TiO_2 layer. A net negative charge is left next to the spiro layer, causing Q_+ to become progressively more negative. This negative Q_+ gives a negative V_+ and a positive V_- which is opposite to the signs depicted in Fig. 1. By the end of the relatively short preconditioning period, the net voltage drop of -1.2 V is nearly all accounted for by V_+ and V_- so that $E_{bulk} \approx 0$.

Once the scan begins, $V(t)$ begins to drop. However it takes time for the vacancies to move away from their accumulation layer and for Q_+ to increase from its negative value, so the reduction in E_{bulk} from V_+ and V_- is less than it would have been without the preconditioning. This result aids extraction of electrons from the TiO_2 and holes from the spiro and explains the widely reported observation that preconditioning at a voltage exceeding V_{bi} improves the apparent solar cell performance.

4 Conclusions

In conclusion, a time-dependent drift-diffusion model has been developed to explore the effects of defect mediated ion motion on the J - V curves of planar perovskite solar cells. We have shown that an accurate representation of the ionic charge buildup in narrow Debye layers close to the blocking layers is crucial to understanding the experimental J - V curves reported here.

Our model predicts hysteresis that compares well to the experimental data reported here and which is similar to that reported in the literature. The hypothesis that mobile ions in the perovskite are responsible for hysteresis is confirmed, although other explanations, such as large-scale trapping of electrons⁴⁵, are not ruled out. We have also shown why apparently high efficiencies, obtained from measurements at fast scan rates, are not be a use-



ful indicator of device performance, even over several voltage cycles. Our approach can be generalized to explore recombination schemes other than the one considered here, to accommodate multiple ion species with different mobilities and to study why hysteresis effects increase as the temperature decreases, even in low hysteresis cells^{46,47}.

The markedly lower hysteresis observed in perovskite solar cells employing a 60-PCBM hole blocking layer has been attributed by Shao *et al.*³⁵ to passivation of perovskite grain boundaries by the PCBM. This explanation has been questioned by Tao *et al.*⁴⁸ who note that the PCBM layer is so thin (~ 40 nm) in comparison to the perovskite layer ($b \approx 300 - 600$ nm) that the amount of PCBM leakage required for effective passivation is enough to cause degradation of the PCBM layer and reduce device performance. The moving ion hypothesis, however, points to an alternative explanation for the lower hysteresis in these cells. Under normal operating conditions (*i.e.* $V < V_{bi}$), vacancies drift towards the spiro (PEDOT:PSS for inverted structures) and away from the PCBM, *i.e.* I^- ions move towards the PCBM. Since PCBM is made up of small molecules of functionalized C_{60} it is quite possible that I^- ions could drift across the interface entering gaps between the PCBM molecules. This cannot happen in titania, which is crystalline. It is also possible that positively charged ions, *e.g.* Li^+ from the spiro, protons or MA^+ , could enter the PCBM, compensating the negative charge of the iodide ions and causing the hysteric effect to be further reduced.

Acknowledgements

The authors wish to acknowledge helpful discussions with Laurie Peter, Saiful Islam and Aron Walsh. The research leading to these results has received funding from the European Union Seventh Framework Programme FP7/2007-2013 under grant agreement 316494 and the UK Engineering and Physical Sciences Research Council grants EP/J017361/1 & EP/I01702X/1.

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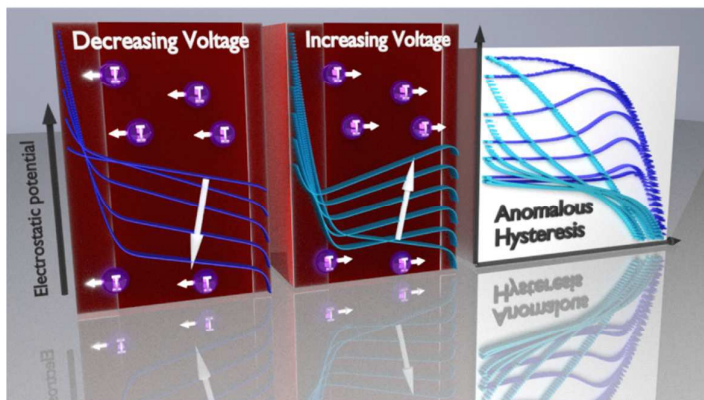
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We have developed a charge transport model that explicitly accounts for ion migration. This model has been used to interpret measured current-voltage characteristics that show hysteresis.



Broader Context

A perovskite solar cell is so-called because it includes a perovskite structured compound, most commonly a hybrid organic-inorganic lead or tin halide-based material, as the light-harvesting active layer. These cells were mentioned as an exciting development in the climate change conference in Paris in December 2015. The record certified power conversion efficiency for these cells is 21.0%. A well-known problem is hysteresis in which the cell current-voltage characteristics are strongly dependent on the voltage scan rate, direction and pre-conditioning treatments. Despite evidence from cell measurements identifying the likely cause of hysteresis as ion migration, there is no theoretical model capable of interpreting measured current-voltage characteristics that show hysteresis. Here, we report a combined theoretical-experimental investigation of hysteresis where we have identified the physical origin of the features seen in the measurements. Our model takes an approach to solving the charge transport equations that is widely applicable to other double layer problems occurring in electrochemical applications such as the evolution of transmembrane potentials in living cells. The model allows us to understand the effect of mobile defects on the operational mechanisms of the devices and paves the way for the development of cells with improved and reproducible performance.

