

1 **Hydrodynamic Behaviour of Compacted Granite Sawdust**  
2 **from the Dimension Stone Industry of Pontevedra (Spain):**

3 **Experimental and Modelling**

4 by

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1 **Abstract**

2 Two large-scale column experiments have been performed to test the hydrodynamic  
3 behaviour of unsaturated, compacted granite sawdust - a material produced during  
4 the dressing of dimension stone in Pontevedra (Spain). One of the columns was  
5 equipped with psychrometers and capacity probes while, in the other, a radial array  
6 of 80 electrodes made possible a time-dependent 3D electrical resistivity survey. All  
7 these devices allowed investigating and modelling the progressive saturation of the  
8 material. The study includes a straightforward methodology developed to calibrate  
9 the resistivity signals based on standard Proctor-compacted specimens. The  
10 progressive saturation of the granite sawdust reveals different stages: initially, an  
11 uneven advance of the saturation front (fingering) occurs; later on, this feature  
12 vanishes and is replaced by a more regular advance of the saturation front.  
13 Numerical analysis of the results shows that the yield capacity of the granite sawdust  
14 is  $\sim 0.39 \text{ m}^3 \text{ m}^{-3}$  and a saturated hydraulic conductivity  $\sim 2 \cdot 10^{-6} \text{ m s}^{-1}$ . The last value,  
15 which corresponds to the specific standard Proctor compaction, is not sufficient to  
16 support the use of granite sawdust for compacted-single-layer capping structures.  
17 Nonetheless, increased compaction efforts or improved design criteria (multilayer  
18 systems or capillary barriers) can keep bearing when considering granite sawdust for  
19 this purpose.

20

21 **Key words:**

22 Sustainable waste management, sanitary landfills, unsaturated soil behaviour,  
23 hydraulic conductivity, yield capacity, water fingering.

## 1 **1 Introduction**

2       The modern mining industry faces a significant environmental challenge related  
3 with the sustainable management and safe disposal of their processing wastes.

4 Dimension stone industry is widespread worldwide and major producers concentrate  
5 rock extraction and processing in relatively reduced areas. This is the case in  
6 Pontevedra, Galicia (NW Spain) where only the granite industry generates  $\sim 2.2 \times 10^5$   
7 tons of rock dust (granite sawdust) on a yearly basis (Barrientos et al., 2010).

8       The use of waste and by-products from mining and industrial activities (e.g. fly  
9 ash, dewatered sludge, quarry fines, mine tailings, etc.) in geotechnical engineering  
10 projects constitute a sustainable waste management approach (e.g. Borghetti et al.  
11 2009; Carro et al. 2008; Falcon 2011; Fraser and McBride 2000; ICAR 2000;  
12 Navarro et al. 2008). However, this requires suitable studies of the material  
13 properties so that the considered by-product can be appropriately applied to solve  
14 engineering problems. In the case of sealing barriers specific restrictions apply  
15 according to Directive 1999/31/EC, where it is ruled that the sealing and capping  
16 layers in a landfills must comprise a mineral layer with combined properties of  
17 hydraulic conductivity and thickness that ensure the protection of soil, surface water  
18 and groundwater. To this respect, the requirement for the lining varies depending on  
19 the type of waste to be stored.

20       Based on different preliminary works (Vázquez 2005; Vázquez et al. 2007;  
21 Navarro et al. 2008; Carro et al. 2008; Barrientos et al. 2010; Falcon-Suarez 2011)  
22 the inert nature and small grain size of granite sawdust make it amenable of use in  
23 compacted sealing barriers provided that sufficient performance is attained. This  
24 performance is typically assessed in most engineering practice codes based on  
25 compacted thickness, hydraulic conductivity, geotechnical properties (plasticity and

1 fines content) and waste compatibility issues (eg. Daniel and Koerner, 1993). Granite  
2 sawdust is made of fine grained, low plasticity natural inert minerals consisting of  
3 silty and clay size grains of granite particles with additional mineral components  
4 derived from the abrasive materials used in the workshops. Hence, the key point for  
5 its application as liner would be its hydrodynamic behavior.

6       The assessment of hydraulic conductivity in compacted clay materials is an  
7 standard practice in geotechnical laboratories (eg. ASTM D5856-15). However, it is  
8 well known that laboratory results often differ from in-situ behavior. For instance,  
9 Shackelford and Javed (1991) have pointed that the in-situ permeability of  
10 compacted clay soils can be as much as two to three orders of magnitude higher  
11 than the permeability values predicted by laboratory tests so that they suggest the  
12 convenience of performing big size (or large scale) permeability determinations in  
13 order to get more realistic estimates of this critical parameter. Keeping that in mind,  
14 in the present study we have performed a detailed assessment of the hydrodynamic  
15 behaviour of compacted, unsaturated granite sawdust specimens emplaced within  
16 PVC columns as they were progressively saturated and monitored with a variety of  
17 sensors to record the evolution of the corresponding moisture content. The  
18 monitoring survey has been also employed to model the unsaturated/saturated  
19 behaviour of the tested material.

20       In addition to material performance assessment, our study is also aimed at  
21 providing fundamental knowledge on the processes governing water transfer through  
22 a compacted fines barrier, to better understand the engineering limits of the studied  
23 material and to point towards acceptable technical solutions for the use of granite  
24 sawdust as liner.

25

## 1 **2 Materials and Methods**

### 2 2.1 Granite fines

3 Granite sawdust or granite fines (hereafter also called GF) is a granular  
4 material dominated by a silt-size fraction (10-15% clay; 70-75% silt; 10-15% fine  
5 sand), with low plasticity (class ML of the USCS classification scheme) and relatively  
6 small specific surface area (i.e., BET, 6 to 10 m<sup>2</sup> g<sup>-1</sup>). The material includes quartz,  
7 feldspars (microcline, plagioclase) and phyllosilicates (biotite, muscovite, chlorite,  
8 etc.) among its mineralogical constituents, plus minor amounts of other minerals  
9 associated with the manufacturing processes in the workshops (mainly calcite and  
10 steel grit; 3 and 16 wt.%, respectively). Neglecting the origin, because of its small  
11 grain size and the type of infiltration tests used in this study, GF will be also referred  
12 to as soil within the text.

13

### 14 2.2 Experimental columns: assembly and initial test conditions

15 The experiments were conducted in two plastic columns (nominal capacity  
16 ~0.05 m<sup>3</sup> each), specifically designed to monitor the water flow through the soil  
17 during controlled flooding tests. The two columns were set up with different sensor  
18 configurations: column 1 (COL-1) used invasive sensors (capacitance probes and  
19 psychrometers); column 2 (COL-2) used non-invasive remote sensing of electrical  
20 conductivity (ring electrodes) to monitor changes in soil moisture content.

21 COL-1 was a 2 cm wall thickness acrylic column (0.5 m length; 0.35 m ID)  
22 closed at the bottom with two drains, and fitted with lateral ports to insert up to 12  
23 sensors at different heights (Fig. 2a and Fig. 2b). The column was instrumented with  
24 four soil moisture sensors (ECHO EC-5) and eight psychrometers (PCT-55-15-SF  
25 Wescor Inc.) for measuring humidity variations along the column. Sensors were

1 approximately located along the same axial plane. The bottom of the column was  
2 designed with a 2 cm high spacer-annulus (ID 27 cm, OD 31 cm) able to separate  
3 central leachates from those generated by preferential pathways at the interface  
4 between the column wall and the soil specimen. The column was filled with gravel up  
5 to the spacer height (2 cm) to prevent the occlusion of the pipework caused by fines  
6 migration and deposition. Above the gravel, eight layers of granite fines were  
7 stepwise poured and compacted with the aid of a modified Proctor hammer (ASTM-  
8 D1557 2009), on the basis of 75 hits per layer. Once compacted, each layer was  
9 sampled to obtain the initial properties shown in Table 1: water content was  
10 determined from oven-drying, while porosity and the remaining derived parameters  
11 were computed knowing the volume of a given layer (according to the layer height  
12 and the column diameter), using the density of solid particles reported by Barrientos  
13 et al. (2010). An extended formulation of the calculated parameters can be found in  
14 Falcon (2011).

15 COL-2 was a PVC tube (1.5 cm wall thickness; 0.75 m length; 0.3 m ID)  
16 perforated to insert 2 cm length electrodes distributed in five rings holding 16 units  
17 each (22.5° separation; Fig. 3a). The electrodes were connected to a SIPLab  
18 (Spectral Induced Polarization, Radic Research, Berlin) - a tool designed to measure  
19 resistivity in sediments and rocks. Likewise in COL-1, the bottom of the COL-2  
20 column was also equipped with a spacer-annulus and filled with gravel up to the  
21 spacer height. A 35 cm thick layer of coarse sand was then used to fill the space  
22 between rings one and two. Sand was chosen to replace the GF in this region to  
23 avoid interpolation of moisture measurements that would be unrepresentative of the  
24 soil behaviour. Consequently, the study focused on the upper 25 cm of the column,  
25 where four rings of electrodes were located. Above the sand layer, four GF beds

1 were poured above the sand, each compacted and sampled as described above for  
2 COL-1 (see initial conditions in Table 1).

3         The interpretation of resistivity measurements with SIPLab was based on the  
4 software BERT (Günther and Rucker 2013) which has been optimized for  
5 multielectrode array measurements either in the complex frequency domain or for  
6 direct-current. In our experiments, a direct current configuration (dipole-dipole; Seidel  
7 and Lange 2007) was adopted. That made possible the execution of up to 320  
8 sequential measurements. One single cycle of measurement and processing lasted  
9 approximately 1 hour, which turns out to have a significant importance in terms of  
10 data interpretation. This is because the data from COL-2 is unable to fully describe  
11 the flow evolution, since each cycle represents resistivity values at different times.  
12 The electrical resistivity survey results in a 3D mesh of 8505 tetrahedral elements  
13 (Fig. 3b) which has been post processed with the aid of the software ParaView 3.8.0-  
14 RC1.

15         The GF used in both tests came directly from selected workshops located in  
16 Pontevedra, Spain and they had an initial water content of ~38 wt.%. To reduce the  
17 original moisture content, the material was primarily dehydrated (oven-drying, COL-  
18 1; lyophilisation, COL-2), and then partially rehydrated in a controlled manner. Since  
19 either inter- or intra-layer capillary effects might occur, particularly in the interfaces  
20 gravel-GF and sand-GF, the procedure adopted during specimen assembly was  
21 aimed at ensuring hydrodynamic equilibrium between layers, according to the  
22 following procedure. Firstly, both the gravel and sand were slightly hydrated (~0.3 of  
23 GF wt.%); secondly, the first layer of GF was compacted and covered with plastic  
24 sheeting (i.e., to minimize evaporation) for one day; thirdly, the layer of GF was  
25 sampled to gravimetrically determine its water content; finally, the remaining layers

1 were hydrated according to the water/soil ratio determined for the first GF layer.  
2 Likewise, after being compacted, each subsequent layer was covered with plastic  
3 sheeting and sampled after about eight hours. Table 1 shows the results of the  
4 sampling, which represent the initial conditions of the tests.

5

### 6 2.3 Sensors calibration

7 Moisture influences the electrical response of a porous medium. When  
8 considering soils or rocks, the influence varies from one medium to another because  
9 the transmission of electrical current depends on the nature of the porous network  
10 (i.e., a combined effect of porosity, tortuosity and cementation of grains). Hence,  
11 determining the moisture of a soil through the electrical response requires  
12 calibration.

13 Separate calibrations were performed for the EC-5 soil moisture sensors and  
14 the electrode sensor arrays, since the way they detect the electrical response is  
15 different: while capacitance probes are based on induced polarization electrodes use  
16 direct current. Therefore, in COL-1, EC-5 sensors measure volumetric water content  
17 through the dielectric constant of the soil using capacitance technology (Campbell et  
18 al. 2005; Kelleners et al. 2004a; Kelleners et al. 2004b), which derives moisture  
19 content from changes in the permittivity of the porous medium; in COL-2, electrodes  
20 reciprocally act as transmitters of direct current and receptors of the electrical signal  
21 attenuated after travelling through the soil.

22 Calibration required soil specimens of well-known properties. Therefore, in the  
23 present study were performed standard Proctor tests (ASTM-D698, 2007) varying  
24 the water to soil ratio to cover the whole range of soil saturation: 34 and 28 Standard  
25 Proctor tests were used to calibrate capacitance sensors and electrodes,



1 respectively. For each specimen, bulk density was calculated from the volume of the  
2 standard Proctor cell, while water content was gravimetrically determined; porosity  
3 and derived parameters were computed afterwards as referred earlier.

4 Soil moisture data from EC-5 were obtained by inserting the sensor in the soil  
5 specimen. For the measurement of the electrical response, the adopted protocol was  
6 as follow: first, the compacted Proctor specimen was transferred to an acrylic  
7 chamber of Proctor size (Fig. 4), and closed at both ends with wooden end-caps;  
8 second, four electrodes were inserted along the axis of the specimen through holes  
9 drilled in the acrylic cylinder; third, the electrodes were connected to SIPLab (at  
10 conditions of  $\pm 10V$  and  $\pm 10mA$ ) to determine the bulk electrical resistivity of the  
11 sample, using a Wenner configuration (Seidel and Lange 2007).

12 Experimental data from the capacitance sensors were fitted with a third-order  
13 polynomial (Fig. 5) following the observations of Topp et al. (1980). Direct current  
14 measurements were corrected using the well-known Archie's relationship (Archie,  
15 1942) which equates the porous medium bulk electrical conductivity ( $\sigma_b$ ) with  
16 porosity ( $\phi$ ), degree of saturation ( $S_w$ ), and the electrical conductivity of the pore fluid  
17 ( $\sigma_w$ ):

$$18 \quad \sigma_b = \frac{\phi^m S_w^n \sigma_w}{a} \quad (1)$$

19 In the previous Eq. 1, m and n are cementation and saturation exponents,  
20 respectively, and a is the tortuosity factor. To determine  $\sigma_w$ , pore water was  
21 extracted from the Proctor specimens of highest water content using soil moisture  
22 pore water samplers (SMS) Rhizon (Falcon-Suarez et al. 2014; Seeberg-Elverfeldt et  
23 al. 2005). The electrical conductivity of extracted water ( $\sigma_w$ ) was determined with

1 standard benchtop conductivity meter, obtaining a mean value  $\sim 0.28 \text{ S m}^{-1}$ . Then,  
2 the experimental parameters were adjusted by  $n=2.18$ ,  $m=1.17$ , and  $a=0.92$  (Fig. 6).

3 Thermocouple psychrometers measure air pressure, which is related to the  
4 relative humidity according to the Kelvin's equation (Vázquez, 2005; Falcon-Suarez,  
5 2011). The psychrometers used in COL-1 were limited to the suction range of 8 to  
6 0.05 MPa ( $\pm 0.03$  MPa) according to the technical specifications reported by the  
7 manufacturer (Wescor Inc.), who also provided calibration certificates. Therefore, no  
8 further calibrations were undertaken.

9

#### 10 2.4 Test execution and data processing

11 The tests were developed simulating prescribed conditions of hydration from  
12 the top of the columns. Furthermore, evaporation ( $E$ ) was also considered to  
13 calculate the water balance ( $BH$ ).  $E$  was measured in an evaporation tank located in  
14 the laboratory, in the case of COL-1; for COL-2,  $E$  was assessed from the change in  
15 weight observed in a smaller column, similar to those used by Redwan and  
16 Rammlmair (2010) and Falcon-Suarez et al. (2014). This auxiliary column was filled  
17 with GF under similar moisture content and compaction conditions to those of COL-  
18 2, and also subjected to the same hydration process. Knowing the water poured  
19 ( $WP$ ) and the volume of leachates ( $L$ ) at the bottom, the water balance was  
20 determined by the expression  $BH=WP-E-L$ . This allowed the average saturation  
21 state of the porous media to be calculated based on the variation from its initial  
22 moisture content.

23 Watering was executed with the aid of nebulizers in order to minimize any  
24 erosive effect related to water impacting on the soil. During the test carried out in  
25 COL-1, the water infiltration was monitored by the EC-5 probes and psychrometers

1 at frequencies of 0.033 and 0.017 Hz, respectively. In the case of the EC-5 sensors,  
2 the raw data were processed to correct the values according to the calibration  
3 function defined for granite fines (Fig. 5). Additionally, once leachates were  
4 observed, a last hydration step was purposely undertaken to flood the column. The  
5 aim was twofold: to observe the evolution of sensor reading under the highest  
6 moisture conditions, and to compute the mean hydraulic conductivity ( $K_0$ ) by the  
7 constant head method.

8 In COL-2, the recorded resistivity data were inverted to obtain the bulk  
9 electrical conductivity of the soil ( $\sigma_b$ ), and then transformed into degree of saturation  
10 by Archie's law using the experimental parameters for GF previously estimated and  
11 the electrical conductivity of the pore water ( $\sigma_w$ ). To determine  $\sigma_w$ , at the end of the  
12 test pore water was extracted by inserting SMS Rhizon sensors using the 5 cm  
13 depth spaced electrode ports. A linear correlation with depth was determined  
14 ( $r^2=0.99$ ) for electrical conductivity and this relationship was later used to compute  
15  $S_w$ ; the average value of  $\sigma_w$  along the column was  $\sim 0.18 \text{ S m}^{-1}$ .

16

## 17 2.5 Infiltration flow modelling

18 The COMPASS code (COde for Modelling PARTly Saturated Soil, Thomas et  
19 al. 2012; Thomas and He 1997; Thomas and He 1998) was used to model the  
20 results of the experiment. COMPASS is a finite element code that allows simulation  
21 of soil behaviours using coupled multiphysical processes (i.e., unsaturated flow, heat  
22 and solute transport, and different mechanical phenomena). The software GID is a  
23 graphic interface coupled with COMPASS for pre- and post-processing data and  
24 visualization. It allowed the definition of the geometry of the problem (2D model);  
25 implementing the characteristics of the different layers, boundary conditions, the

1 algorithms applied (Table 2) and temporal hydration curves; building the finite  
2 elements grid; calculating from COMPASS; and visualizing and editing results.

3 Only COL-1 was considered for modelling. A 2D grid of 5600 quadratic  
4 elements (5751 nodes) was used to simulate the central section of the column (0.35  
5 m diameter; 0.38 m height). Initial conditions and geometry were defined according  
6 to the information provided in Table 1; relevant water-soil behaviour equations and  
7 associated parameters are listed in Table 2. Boundary conditions included  
8 impervious side walls and free drainage condition at the bottom, whilst variable  
9 vertical flow was imposed at the top of the column – a flow-time curve reproducing  
10 the hydration sequence developed during the test.

11

## 12 **3 Results**

### 13 3.1 Invasive sensors column (COL-1)

14 Fig. 7 and Fig. 8 illustrate data corresponding to the COL-1 capacitance and  
15 psychrometer sensors, respectively. Pore pressure shows the original  
16 psychrometers data record, while EC-5 data have been corrected using the  
17 calibration function for granite fines (see Fig. 5). Volumetric water content ( $\theta$ ) was  
18 then transformed into degree of saturation ( $S_w$ ) based on the mean porosity of the  
19 bed where the sensor was emplaced. The figures also illustrate the best fit obtained  
20 from the numerical modelling of water saturation (Fig. 7) and pore pressure (Fig. 8),  
21 at sensor heights. Above the sensor curves, both figures display the water balance  
22 of the column. Water contribution steps ( $WP$ ) are labelled by the theoretical degree  
23 of saturation ( $S_{Tw}$ ) achieved, in terms of mean  $S_w$  of the whole column. As previously  
24 mentioned, the last hydration step flooded the column and, at this point, the hydraulic  
25 conductivity was  $\sim 4 \cdot 10^{-6} \text{ m s}^{-1}$ .

1           The capacitance sensors data are highly dependent on the sensor depth, the  
2 time lags from hydration events and the degree of saturation of the column. The  
3 shallowest sensor (11 cm depth) peaks sharply as a result of hydration up to the  
4 fourth step. Onwards, despite more water was being poured into the column,  $S_w$   
5 remained constant at a value of  $\sim 0.62$ . At deeper positions, EC-5 sensors show  
6 peaks associated with the hydration events, although the peaks are smoother  
7 because water progressively spreads into the adjacent pore volume. Likewise, at  
8 either position, EC-5 sensors remain approximately constant when  $S_w$  is around  
9 0.62, i.e.,  $\theta > 0.35$ .

10           The maximum water content recorded is still significantly below the full  
11 saturation value. This indicates that, in COL-1, the field capacity of GF, which highly  
12 depends on the compaction, is nearly the same throughout the entire column. Thus,  
13 capacitance sensors located at 11 and 17.5 cm display a steadily increasing trend up  
14 to a moisture limit of  $\theta \sim 0.35$ , while deeper sensors show a transient evolution that  
15 overcomes this value before steadiness is attained. Such an effect is also observed  
16 in the sensor at 24.5 cm depth after the fifth watering episode and later on in the  
17 deepest one. This can be interpreted as a buffering effect related to capillary  
18 phenomena along the interface of drainage GF-gravel.

19           Psychrometer also present sharp variations in the shallower positions (up to  
20 13.5 cm depth), while deeper ones respond to watering with a progressive reduction  
21 of pore pressure. However, after the first hydration step, only the sensors located at  
22 27 and 32 cm depth have recorded pore pressure variations; psychrometers at 17.5  
23 and 34.5 cm depth remained unresponsive during the test.

24           The interpretation of psychrometers data at medium-high soil moisture is  
25 inaccurate. Note that, according to the water retention curve for GF reported by

1 Barrientos et al. (2010), suction lays below 0.05 MPa at  $\theta > 0.25$ . In as much as this  
2 value fits into the lower edge of the sensor response, the recorded values may only  
3 be considered representative of the soil moisture only during the first two hydration  
4 episodes. That means that we only can take them as qualitative indicators of the  
5 transition from a low to a medium moisture domain.

6

### 7 3.2 Numerical modelling

8 Because of the uncertainty in the data reported by the psychrometers at  
9 medium-high moisture contents, only the results obtained by capacitance sensors  
10 were considered for numerical modelling. That was conducted to determine the  
11 hydraulic conductivity  $K_0$  and the associated moisture conditions,  $\theta_s$ . The numerical  
12 model was addressed using an optimization approach to the measured data,  
13 applying equations and controlling the parameters shown in Table 2.

14 The evolution of the degree of saturation was analysed at 67 discrete times  
15 ( $N$ ), and the relative mean error ( $M_P$ ) determined from the theoretical ( $R_t$ ) and the  
16 experimental ( $R_e$ ) observation using the following expression:

$$17 \quad M_P = \frac{1}{N} \sum_{i=1}^N \frac{(R_t^i - R_e^i)^2}{(R_e^i)^2} \quad (2)$$

18 Applying Eq. 2 to each one of the four capacity probes, a best fit was obtained  
19 using a  $K_0$  value of  $2 \cdot 10^{-6} \text{ m s}^{-1}$ . That corresponds with a maximum soil moisture of  
20 0.39. For these conditions,  $M_P$  was 0.03, 0.04, 0.004 and 0.006, for the capacitance  
21 sensors located at 11, 17.5, 24.5 and 32 cm depth, respectively (Fig. 7 and 8).

22 Further uncertainties associated with the accuracy of instrumentation and other  
23 random errors were considered in an exploratory sensitivity analysis carried out with  
24 respect to  $K_0$ ,  $\theta_s$ , and the water retention curve parameters  $\alpha$  and  $m$ . This analysis

1 showed that the determination of parameter  $m$  and also the estimation of  $\theta_s$  must be  
2 carefully addressed because changes of ~5% in any of them might affect the result  
3 of the simulation up to 15-20%. The sensitivity analysis is fully presented as  
4 supplementary material.

5

### 6 3.3 Non-invasive sensors column (COL-2)

7 Fig. 9 shows the water balance distribution resulting from COL-2 test.

8 Although the test extended over two weeks, the results presented here focus on the  
9 last five days as they better highlight the most relevant features.

10 Fig. 10 shows the distribution of the water in the column at six different  
11 hydration states labelled with the mean degree of saturation ( $S_{Tw}$ ) estimated from the  
12 water balance. The 3D plots illustrate the degree of saturation ( $S_w$ ) through 160°  
13 open-slices on the upper column, where GF were emplaced; the lower part, which  
14 was filled with sand, is not represented. In addition, the figure also shows 2D  
15 saturation sections at 0.1 (AA'), 0.15 (BB') and 0.2 (CC') m depth. The first stage  
16 ( $S_{Tw}=0.45$ ) is the initial condition of the column, while those following correspond to  
17 the  $S_w$  distribution at some later time, once watering has occurred.

18 There is a general agreement between the progressive increase of moisture  
19 based on the electrical measurements and those obtained through water balance  
20 computation. The moisture distribution is more homogeneous in the upper part of the  
21 column (where the degree of saturation is lower), after every single hydration event.  
22 This becomes less significant when moisture content increases ( $S_{Tw}=0.72$  and  $0.75$ ),  
23 which may be interpreted as resulting from: i) gravity-driven fast flows towards  
24 deeper levels; ii) evaporation ( $\sim 1.74 \text{ mm d}^{-1}$ ); or iii) a combination of both effects.  
25 The last watering step coincided with the first appearance of outflowing of leachates

1 at the bottom of the column. At that moment, the degree of saturation reached a  
2 value of  $\sim 0.7$ , which is equivalent to a volumetric water content of  $\sim 0.39$ .

3 Fig. 10 illustrates preferential pathways located at the sides of the column  
4 during the early stages of hydration. In the following watering episodes preferential  
5 flow gains importance but, after some time, this effect declines and moisture  
6 distribution tends to homogenize in the column. The preferential pathways display an  
7 annular distribution that could be related to perturbations induced while assembling  
8 the column or during its compaction. Among the possible causes explaining  
9 preferential pathways, it is worth highlighting the following: i) grain arching upon  
10 compaction; ii) fissuring associated with minor moisture anisotropies; iii) local over  
11 compaction resulting from the insertion of electrodes. Regardless of the cause,  
12 preferential flow has triggered the formation of gravity-driven high saturation fingers  
13 during the earliest watering stages (Glass and Yarrington 1996), an effect that was  
14 later progressively attenuated as a result of the advance of the saturation front.

15

#### 16 **4 Discussion**

17 The experimental results indicate that the field capacity of GF ranges from  
18 0.35 to 0.39, in terms of water content. This range is sensitive to compaction, since  
19 the highest value is observed in COL-2, which presented lower porosity than COL-1.  
20 However, according to the numerical modelling, the best fit is obtained for a field  
21 capacity  $\sim 0.39$ . This difference leads us to conjecture that experimental data from  
22 COL-1 might be limited by the resolution of the capacitance sensors at high  
23 moistures contents rather than by compaction itself.

24 Simulated and measured degree of saturation match both qualitatively and  
25 quantitatively throughout the studied domain. By contrast, soil suction evolved



1 differently due to uncertainty in the measurements from psychrometers at high  
2 moisture contents. Those parameters under unsaturated conditions and relations  
3 used for modelling yield reasonable results, exhibiting a realistic retardation of the  
4 wetting front moving through the column. In addition, the hydraulic conductivity  
5 shown by GF at the yield capacity in COL-1 was  $4 \cdot 10^{-6} \text{ m s}^{-1}$ , which is consistent with  
6 the results of numerical modelling ( $2 \cdot 10^{-6} \text{ m s}^{-1}$ ). This differs by several orders of  
7 magnitude from the values reported in Barrientos (2007), which were mainly derived  
8 from oedometer tests ( $K_s < 10^{-8} \text{ m s}^{-1}$  or  $K_s \sim 6 \cdot 10^{-7} \text{ m s}^{-1}$  in the worst case scenario).  
9 However, the same author reports an in-situ hydraulic conductivity  $\sim 4 \cdot 10^{-6} \text{ m s}^{-1}$   
10 resulting from a Lefranc-type test conducted in a self-compacted GF landfill which is  
11 readily comparable with our assessment, which we consider representative of field  
12 service conditions.

13 In so far as the modelling neglects irregularities in the column, the agreement  
14 indicates that the hydrodynamics of the system is not very much affected by the  
15 formation of preferential pathways; however, data obtained from COL-2 suggests the  
16 contrary, where the generation of gravity fingers related to early stages of hydration  
17 is apparent. The origin of gravity fingers is commonly associated with local  
18 heterogeneities in the soil matrix. Without considering the role of grain arching in  
19 COL-2, driving electrodes into the soil column during assembly might have also  
20 contributed to develop local heterogeneity features. On the other hand, electrical  
21 data and processed images allow the identification of 3D structures that could be of  
22 great interest for larger scale contexts.

23 The use of capacitance sensors in COL-1 at a larger scale would render a  
24 rapid respond to changes in the soil moisture, which contrasts with the fact that  
25 capacitance probes are only informative of the small volume of porous media

1 adjacent to the sensor. Moreover, the study also reveals that the use of  
2 psychrometers might not be adequate to accurately monitor watering processes in  
3 granular, fine grained materials. Even if psychrometers are neglected, a combination  
4 of electrical mapping and point moisture determinations based on capacitance  
5 probes has a great informative potential when considering larger scale tests.

6         Whatever the tool used for monitoring moisture changes, a calibration from  
7 one soil to another is always required. The methodology used to calibrate the  
8 electrical response of granite sawdust has provided valuable information for the  
9 interpretation of the experimental data. The standard Proctor test is a fast, cheap  
10 and simple way to obtain reasonably homogenous samples for the determination of  
11 different physical properties. Therefore, it constitutes a complementary analysis  
12 technique when electrical properties are required.

13         The techniques used in this study have provided useful information regarding  
14 the behaviour of GF which were progressively saturated with water starting from low  
15 moisture content. The real-time monitoring of the soil response as a result of the  
16 hydration-front advance and the test scale, has allowed the recognition of  
17 phenomena and structures that single permeability tests would have neglected.  
18 Furthermore, the study partially fulfils a knowledge gap regarding the non-saturated  
19 hydrodynamics of GF. Since real atmospheric conditions combine wet and dry  
20 periods, the information reported in this study is valuable for understanding and  
21 predict the hydration of layers of granite fines exposed to long dry periods.

22         The potential use of granite sawdust as compacted liner or cover layer in  
23 landfills widely rests on its hydrodynamic properties and also because it represents a  
24 suitable and elegant strategy of sustainable waste management. According to RD  
25 1481/2001 dealing with the landfill of waste (which transposes the 1999/31/EC

1 Directive to the Spanish law) the landfill base and sides shall consist of a mineral  
2 layer which satisfies permeability ( $K_s$ ) and thickness (T) requirements with a  
3 combined effect in terms of protection of soil, groundwater and surface water at least  
4 equivalent to the one resulting from the following requirements: i) for hazardous  
5 waste  $K_s \leq 10^{-9} \text{ m s}^{-1}$  and  $T \geq 5 \text{ m}$ ; ii) for non-hazardous waste  $K_s \leq 10^{-9} \text{ m s}^{-1}$  and  $T$   
6  $> 1 \text{ m}$ ; iii) for inert waste,  $K_s \leq 10^{-7} \text{ m s}^{-1}$ ,  $T \geq 1 \text{ m}$ . Therefore, according with our  
7 results, the direct application of GF for such a purpose is not directly granted unless  
8 greater compaction energy (in excess to the relatively gentle  $600 \text{ kN}\cdot\text{m}/\text{m}^3$  of the  
9 standard Proctor conditions used in our study) is applied, as it is expected for this  
10 type of engineering elements. Furthermore, our results do not preclude the use of  
11 standard Proctor-compacted GF in capillary barrier configurations (e.g., Khire et al.  
12 2000), which would represent a suitable alternative as suggested in Falcon-Suarez  
13 (2011).

14

## 15 **5 Conclusions**

16 Two large-scale column infiltration tests have been performed to characterize  
17 the hydrodynamic properties of standard Proctor-compacted unsaturated granite  
18 sawdust. The two columns have been widely instrumented and they have provided  
19 useful data to monitor the progressive saturation of GF (and corresponding moisture  
20 evolution) and to model the time-dependent behaviour of the overall system. Worth  
21 mentioning among the results are the identification of features and structures that  
22 occur at the early stages of hydration (e.g., fingering) that, if neglected, could lead to  
23 incomplete interpretations. Furthermore, the calibration of the resistivity electrodes  
24 based on standard Proctor-compacted specimens provides with a straightforward,

1 technique that can be routinely applied to reconstituted soils of different  
2 compositions when performing electrical resistivity surveys.

3 The hydrodynamic study illustrates that GF have a yield capacity  $\sim 0.39$  while  
4 the corresponding saturated hydraulic conductivity is  $\sim 2 \cdot 10^{-6} \text{ m s}^{-1}$ . Both parameters  
5 are of the utmost importance when considering water storage and the hydraulic  
6 performance of GF either compacted in a single layer or in multilayer systems or  
7 capillary barriers. To this respect, based on the present results and mandatory limits  
8 of the European and Spanish waste landfill regulation standard Proctor-compacted  
9 GF would not be a suitable material for single-layer capping structures. However,  
10 enhanced compaction (using, for instance sheepsfoot-type rollers in the field or  
11 modified-effort Proctor test, ASTM (2009), in the laboratory) makes possible the  
12 attainment of higher material densities and concomitantly lower permeability values.  
13 Moreover, improved design considerations using, for instance, multilayer systems or  
14 capillary barriers can render GF a useful and cost-effective alternative to the more  
15 expensive geomembrane-based solutions.

16

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**Table 1** Initial conditions of column tests

	Top (cm)	Bottom (cm)	$\rho_d$ (g cm <sup>-3</sup> )	$\phi$ (cm <sup>3</sup> cm <sup>-3</sup> )	$\theta$ (cm <sup>3</sup> cm <sup>-3</sup> )	$S_w$	Sensors
<i>COL-1</i>							
	38.5		1.26	0.61	0.18	0.29	
	34		1.27	0.6	0.17	0.29	<i>Psy</i>
	29		1.23	0.61	0.13	0.21	<i>Psy</i> <i>EC</i>
	25		1.25	0.61	0.19	0.3	<i>Psy</i> <i>EC</i>
	20		1.16	0.64	0.17	0.27	<i>Psy</i> <i>EC</i>
	15.5		1.21	0.62	0.17	0.28	<i>Psy</i> <i>EC</i>
	10.5		1.2	0.62	0.17	0.28	<i>Psy</i> <i>EC</i>
	4		1.11	0.65	0.17	0.25	<i>Psy</i> <i>EC</i>
<i>COL-2</i>							
	46		1.37	0.57	0.26	0.46	
	32		1.37	0.57	0.27	0.47	
	22		1.3	0.59	0.26	0.44	
	8		1.44	0.55	0.28	0.51	

Top and bottom position of each layer from the top of the column;  $\rho_d$ , dry density;  $\phi$ , porosity;  $\theta$ , moisture;  $S_w$ , degree of saturation; *Psy* and *EC* are psychrometers (PCT-55-15-SF) and EC-5 soil moisture sensors, at their respective locations.

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**Table 2** Hydraulic model parameters and equations

Parameters	Expression*	Value	Unit	Reference
Specific degree of saturation ( $S_e$ )	$S_e = \frac{\theta_i - \theta_r}{\theta_s - \theta_r}$	--	--	Experimental
Suction ( $\psi_i$ )	$\psi_i = \frac{(S_e^m - 1)^{1/n}}{-\alpha}$	--	kPa	Van Genuchten (1980)
Hydraulic conductivity ( $k_i$ )	$k(\psi_i) = K_0 S_e^{0.5} \left(1 - (1 - S_e^{1/m})^m\right)^2$	--	$\text{m s}^{-1}$	(Mualem, 1976)
Granite fines parameters (water retention curve)	$\alpha$	0.193	$\text{kPa}^{-1}$	Barrientos et al. (2010)
	$m$	0.291	--	Barrientos et al. (2010)
	$n$	1.41	--	Barrientos et al. (2010)
	$\theta_r$	0.09	$\text{m}^3 \text{m}^{-3}$	Barrientos et al. (2010)

\*Subscript i, initial conditions from experimental data;  $\theta$ , volumetric water content (r, residual; s, saturated);  $\phi$ , porosity;  $K_0$ , hydraulic conductivity at maximum saturation conditions

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1           **Fig. 1** Dimension stone activities in Pontevedra (Spain): **a**, panoramic view of  
2 the quarries; **b**, primary block; **c**, workshops; **d**, granite saw dust.

3           **Fig. 2** Experimental column COL-1: **a**, global view of the column; **b**, column  
4 schematic where elements are numbered with [1] acrylic column, [2] granite fines  
5 layers, [3] psychrometers, [4] EC-5 soil moisture sensors, [5] gravel layer, [6] spacer-  
6 annulus, [7, 8] lateral and central drainage.

7           **Fig. 3** Experimental column, COL-2. **a**, global view of the column: [1] SIPLab  
8 connectors, [2] PVC column, [3] Electrodes, [4] electrodes to SIPLab-connectors  
9 cables, [5] drainage system. **b**, transversal (top) and longitudinal (bottom) drawing of  
10 the electrode distribution and the mesh generated by software BERT.

11           **Fig. 4** Experimental setup to measure the bulk electrical conductivity of Standard  
12 Proctor samples: [1] electrodes; [2] acrylic mould where the sample is emplaced; [3]  
13 SIPLab equipment.

14           **Fig. 5** Calibration of the moisture signal recorded by EC-5 sensors on granite fines  
15 using Standard Proctor samples.  $\theta_P$  and  $\theta_E$  are moistures determined from Proctor  
16 properties and measured by EC-5 sensors, respectively.

17           **Fig. 6** Calibration of the bulk electrical conductivity on GF using Standard Proctor  
18 samples at different degrees of saturation. The inner graph compares the bulk  
19 electrical conductivity measured ( $\sigma_{b,Proctor}$ ) and calculated according to the Archie's  
20 adjustment for GF ( $\sigma_{b,Archie}$ ).

21           **Fig. 7** COL-1 test. Evolution of water content ( $\theta$ ) and degree of saturation ( $S_w$ ).  
22 Results of the numerical modelling are also displayed, in terms of  $S_w$  at sensors  
23 depths. The water balance (WB) indicates water coming in and out the column  
24 ( $\pm\Delta w$ ): L-L and L-C, lateral and central leachates; E, evaporation; WP, water  
25 contributions;  $S_{Tw}$ , mean degree of saturation calculated at WP instants.

1 **Fig. 8** COL-1 test. Evolution of pore pressure ( $\psi$ , suction). Results of the numerical  
2 modelling are also displayed, in terms of  $\psi$  at sensors depths. The water balance  
3 (WB) indicates water coming in and out the column ( $\pm\Delta w$ ): L-L and L-C, lateral and  
4 central leachates; E, evaporation; WP, water contributions;  $S_{Tw}$ , mean degree of  
5 saturation calculated at WP instants.

6 **Fig. 9** Water balance (WB) of COL-2 test:  $\Delta w$ , water coming in (+) and out (-) the  
7 column; L-L and L-C, lateral and central leachates; E, evaporation. Dark area  
8 involves the steps shown in Figure 11.

9 **Fig. 10** COL-2 test. Evolution of the degree of saturation ( $S_w$ ) in 3D (top) and 2D  
10 sections at 10 (AA'), 15 (BB') and 20 (CC') cm depth.  $S_{Tw}$ , mean degree of  
11 saturation of the column obtained from the water balance.

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