

Transmit Antenna Selection for Multiple-Input Multiple-Output Spatial Modulation Systems

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Abstract—The benefits of transmit antenna selection (TAS) invoked for spatial modulation (SM) aided multiple-input multiple-output (MIMO) systems are investigated. Specifically, we commence with a brief review of the existing TAS algorithms and focus on the recently proposed Euclidean distance-based TAS (ED-TAS) schemes due to their high diversity gain. Then, a pair of novel ED-TAS algorithms, termed as the improved QR decomposition (QRD)-based TAS (QRD-TAS) and the error-vector magnitude-based TAS (EVM-TAS) are proposed, which exhibit an attractive system performance at low complexity. Moreover, the proposed ED-TAS algorithms are amalgamated with the low-complexity yet efficient power allocation (PA) technique, termed as TAS-PA, for the sake of further improving the system's performance. Our simulation results show that the proposed TAS-PA algorithms achieve signal-to-noise ratio (SNR) gains of up to 9 dB over the conventional TAS algorithms and up to 6 dB over the TAS-PA algorithm designed for spatial multiplexing systems.

Index Terms—Antenna selection, MIMO, power allocation, spatial modulation, link adaptation.

I. INTRODUCTION

SPATIAL modulation (SM) and its variants constitute a class of promising low-complexity and low-cost multiple-input multiple-output (MIMO) transmission techniques [1]–[5]. However, the conventional SM schemes only achieve receiver-diversity, but no transmit diversity [6]. To circumvent this impediment, recently some SM solutions have been proposed [7]–[11] on how to glean a beneficial transmit-diversity gain both with the aid of open-loop as well as closed-loop transmit-symbol design techniques.

As an attractive closed-loop regime, transmit antenna selection (TAS) constitutes a promising technique of providing a

high diversity potential as offered by the classic MIMO architectures. TAS has been lavishly researched in the context of spatial multiplexing systems [12]. As a new MIMO technique, SM can also be beneficially combined with TAS. Recently, several TAS algorithms have been conceived for the class of SM-MIMO systems with the goal of enhancing either its bit error rate (BER) or its capacity [13]–[20]. In [13], a norm-based TAS algorithm was proposed for providing diversity gain. In [14], a closed-form expression of the SM scheme's outage probability was derived for norm-based TAS. In [16], a two-stage TAS-based SM scheme was proposed for overcoming the specific constraint of SM, namely that the number of transmit antennas has to be a power of two. In [17], a novel TAS criterion was proposed for circumventing the detrimental effects of antenna correlation. In [18], the joint design of TAS and constellation breakdown was investigated and a graph-based search algorithm was proposed for reducing the search complexity imposed. In [19], a low-complexity TAS algorithm based on circle packing was proposed for a transmitter-optimized spatial modulation (TOSM) system, which trades off the spatial constellation size against the amplitude and phase modulation (APM) constellation size for improving the system's average bit error probability (ABEP). The adaptive TAS algorithm conceived for TOSM was further developed in [20], where a low-complexity two-stage optimization was proposed for selecting the best transmission mode.

More recently, the research of TAS-aided SM has been focused on the optimization of the Euclidean Distance (ED) of the received constellation points, since they achieve a high diversity gain at a moderate complexity compared to other TAS criteria [21]–[24]. Specifically, in [21] and [22] the ED-based TAS algorithm (ED-TAS) was compared to the signal-to-noise ratio (SNR)-optimized and capacity-optimized algorithms, and a low-complexity realization of ED-TAS, termed as the QR decomposition-based TAS (QRD-TAS) was proposed. The QRD-TAS algorithm constructs an ED-element matrix and exploits the QRD of the resultant matrix for reducing the imposed complexity. Moreover, in [24], the authors exploited the rotational symmetry of the APM adopted for the sake of reducing the complexity of QRD-TAS. Compared to directly optimizing the ED, in [23], Ntontin *et al.* proposed a low-complexity singular value decomposition-based TAS (SVD-TAS) algorithm for maximizing the lower bound of the ED. In [25], the complexity of SVD-TAS was reduced through an alternative computation of the singular value. In [26], the transmit diversity order of ED-TAS was quantified. In [27], the authors proposed several low-complexity TAS schemes relying

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84 on exploiting the channel's amplitude, the antenna correla-
 85 tion, the ED between transmit vectors and their combinations
 86 for selecting the optimal TA subset for the sake of improv-
 87 ing the system's reliability. However, as shown in [21]–[27],
 88 the QRD-TAS achieves an attractive BER performance at the
 89 cost of adopting high-complexity QRD operations, while the
 90 low-complexity SVD-TAS may suffer some performance loss.

91 On the other hand, power allocation (PA) is another promis-
 92 ing link adaptation technique for MIMO systems. Recently, PA
 93 has been extended to SM systems [28]–[31]. For example, in
 94 [28], an adaptive PA algorithm based on maximizing the min-
 95 imum ED was proposed, which is capable of improving the
 96 system's BER performance, while retaining all the single-RF
 97 benefits of SM. Subsequently, this attractive PA algorithm was
 98 further simplified in [29]. However, to the best of our knowl-
 99 edge, the potential benefits of TAS intrinsically amalgamated
 100 with PA have not been investigated in SM-MIMO systems.

101 Against this background, the contributions of this paper are:

- 102 1) We investigate the benefits of ED-TAS and propose a pair
 103 of novel ED-TAS schemes for SM-MIMO systems. In
 104 these schemes, we first classify the legitimate EDs into
 105 three specific subsets and then invoke a carefully designed
 106 upper bound as well as a set-reduction method for the
 107 most dominant set imposing a high complexity.
- 108 2) Specifically, we propose an improved QRD-TAS, where
 109 a tighter QRD-based lower bound of the ED is derived to
 110 replace the SVD-based bound of [23]. A low-complexity
 111 method is proposed for directly calculating the bound
 112 parameters, in order to avoid the high-complexity QRD
 113 or SVD operations of [21]–[24]. More importantly, com-
 114 pared to the conventional SVD-TAS of [25], the achieved
 115 QRD-based tighter bound can achieve a better BER
 116 performance.
- 117 3) Moreover, for striking a flexible tradeoff in terms of the
 118 BER attained and the complexity imposed, we propose
 119 an error-vector magnitude based TAS (EVM-TAS), which
 120 exploits the error vector selection probability to shrink
 121 the search space. The relevant optimization metrics of
 122 EVM-TAS are also derived for different PSK and QAM
 123 schemes.
- 124 4) Finally, we intrinsically amalgamate the proposed ED-
 125 TAS with the recently conceived PA technique of [29] for
 126 fully exploiting the MIMO channel's resources. A pair of
 127 different joint TAS-PA algorithms are conceived, which
 128 provide beneficial gains over both the conventional TAS
 129 algorithms and over the TAS-PA techniques designed for
 130 spatial multiplexing systems [32].

131 The organization of the paper is as follows. Section II intro-
 132 duces the system model of TAS-based SM, while Section III
 133 reviews the family of existing TAS algorithms designed for
 134 SM. In Section IV, we introduce the proposed QRD-TAS and
 135 EVM-TAS algorithms. In Section V, the joint design of the ED-
 136 TAS and PA algorithms is proposed. Then, we carry out their
 137 complexity analysis. Our simulation results and performance
 138 comparisons are presented in Section VI. Finally, Section VII
 139 concludes the paper.

140 *Notation:* $(\cdot)^*$, $(\cdot)^T$ and $(\cdot)^H$ denote conjugate, transpose, and
 141 Hermitian transpose, respectively. Furthermore, $\|\cdot\|_F$ stands

142 for the Frobenius norm. \mathbf{I}_b denotes a $(b \times b)$ -element iden-
 143 tity matrix and the operator $\text{diag}\{\cdot\}$ is the diagonal operator.
 144 $\Re\{\mathbf{x}\}$ and $\Im\{\mathbf{x}\}$ represent the real and imaginary parts of \mathbf{x} ,
 145 respectively.

146 II. SYSTEM MODEL

147 Consider a SM system having N_t transmit and N_r
 148 receive antennas, as depicted in Fig. 1. The frequency-
 149 flat quasi-static fading MIMO channel is represented
 150 by $\mathbf{H} = [\mathbf{h}(1), \mathbf{h}(2), \dots, \mathbf{h}(N_t)] \sim \mathcal{CN}(0, \mathbf{I}_{N_r \times N_t})$, where
 151 $\mathbf{h}(1), \mathbf{h}(2), \dots, \mathbf{h}(N_t)$ are the column vectors corresponding
 152 to each transmit antenna (TA) in \mathbf{H} . The receiver first selects
 153 L TAs according to a specific selection criterion. Then, the
 154 receiver sends this information to the transmitter via a feedback
 155 link. As shown in [23], let U_u denote the u th legitimate TA
 156 subset, where we have

$$\begin{aligned} U_1 &= \{1, 2, \dots, L\}, \\ U_2 &= \{1, 2, \dots, L-1, L+1\}, \\ &\vdots \\ U_{N_U} &= \{N_t - L + 1, \dots, N_t\}. \end{aligned} \quad (1)$$

157 In Eq. (1), there are $N_U = \binom{N_t}{L}$ possible TA subsets, each of
 158 which corresponds to an $(N_r \times L)$ -element MIMO channel. As
 159 shown in Fig. 1, $\mathbf{b} = [b_1, \dots, b_L]$ is the transmit bit vector in
 160 each time slot, which contains $m = \log_2(LM)$ bits, where M is
 161 the size of the APM constellation. In SM, the input vector \mathbf{b} is
 162 partitioned into two sub-vectors of $\log_2(L)$ and $\log_2(M)$ bits,
 163 denoted as \mathbf{b}_1 and \mathbf{b}_2 , respectively. The bits in \mathbf{b}_1 are used for
 164 selecting a unique TA index q for activation, while the bits of
 165 \mathbf{b}_2 are mapped to a Gray-coded APM symbol $s_l^q \in \mathcal{S}$. Then, the
 166 SM symbol $\mathbf{x} \in \mathbb{C}^{L \times 1}$ is formulated as

$$\mathbf{x} = s_l^q \mathbf{e}_q = [0, \dots, s_l^q, \dots, 0]^T, \quad (2)$$

167 where $\mathbf{e}_q (1 \leq q \leq L)$ is selected from the L -dimensional basis
 168 vectors (as exemplified by $\mathbf{e}_1 = [1, 0, \dots, 0]^T$). In the sce-
 169 nario that U_u is selected, the signal observed at the N_r receive
 170 antennas is given by

$$\mathbf{y} = \mathbf{H}_u \mathbf{x} + \mathbf{n}, \quad (3)$$

171 where \mathbf{H}_u is the $(N_r \times L)$ -element TAS matrix correspond-
 172 ing to the selected TA set U_u , and \mathbf{n} is the $(N_r \times 1)$ -element
 173 noise vector. The elements of the noise vector \mathbf{n} are complex
 174 Gaussian random variables obeying $\mathcal{CN}(0, N_0)$.

175 The receiver performs maximum-likelihood (ML) detection
 176 over all legitimate SM symbols $\mathbf{x} \in \mathbb{C}^{L \times 1}$ to obtain

$$\hat{\mathbf{x}} = \arg \min_{\mathbf{x} \in \mathbb{X}} \|\mathbf{y} - \mathbf{H}_u \mathbf{x}\|_F^2 = \arg \min_{\mathbf{x} \in \mathbb{X}} \|\mathbf{y} - \mathbf{h}_u(q) s_l^q\|_F^2, \quad (4)$$

177 where \mathbb{X} is the set of all legitimate transmit symbols and $\mathbf{h}_u(q)$
 178 is the q th column of the equivalent channel matrix \mathbf{H}_u . The
 179 complexity of the single-stream ML detection of Eq. (4) is low,
 180 since a single TA is activated during any time slot [34], [35].

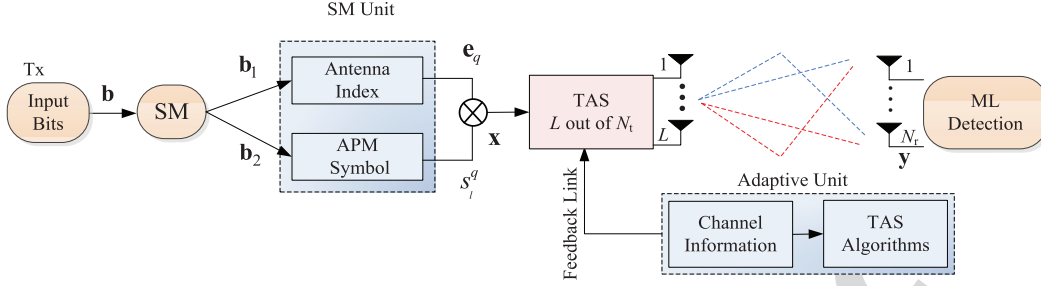


Fig. 1. The system model of the TAS-based SM system.

III. CONVENTIONAL TAS ALGORITHMS

This section offers a brief state-of-the-art review of the existing TAS algorithms proposed for SM systems.

A. The Maximum-Capacity and The Maximum-Norm Based TAS Algorithms

The capacity C_u of the SM-aided MIMO system depends on the classic transmitted signal s_i^q and the TA index signal \mathbf{e}_q . As shown in [21], [33], the capacity C_s relying on the signal s_i^q and the channel \mathbf{H}_u is lower bounded by

$$\alpha = \frac{1}{L} \sum_{i=1}^L \log_2(1 + \rho \|\mathbf{h}_u(i)\|_F^2) \leq C_s, \quad (5)$$

where $\mathbf{h}_u(i)$ is the i th column of \mathbf{H}_u and ρ is the average SNR at the receiver. Moreover, the capacity C_{TA} relying on the signal \mathbf{e}_q is bounded by $C_{TA} \leq \log_2(L)$ [33]. It is proved in [33] that the total capacity $C_u = C_{TA} + C_s$ is bounded by

$$\alpha \leq C_u \leq \alpha + \log_2(L), \quad (6)$$

Based on the bound of Eq. (6), a maximum-capacity based TAS algorithm was formulated in [21] as

$$\mathbf{H}_{\hat{u}} = \arg \max_{u \in \{1, \dots, N_U\}} \alpha. \quad (7)$$

Based on Eq. (5), the optimization objective α of Eq. (7) is maximized by selecting the L TASs associated with the largest channel norms out of the N_t TASs, which is equivalent to the maximum-norm based TAS [13] given by

$$\mathbf{H}_{\hat{u}} = \arg \max_{u \in \{1, \dots, N_U\}} \|\mathbf{H}_u\|_F^2. \quad (8)$$

B. The Exhaustive Max- d_{\min} Based ED-TAS

In order to improve the BER performance of SM, the free distance (FD) d_{\min} was optimized in [21]. For a given channel \mathbf{H}_u , its FD can be formulated as

$$\begin{aligned} d_{\min}(\mathbf{H}_u) &= \min_{\substack{\mathbf{x}_i, \mathbf{x}_j \in \mathbb{X} \\ \mathbf{x}_i \neq \mathbf{x}_j}} \|\mathbf{H}_u(\mathbf{x}_i - \mathbf{x}_j)\|_F^2 \\ &= \min_{\mathbf{e}_{ij} \in \mathbb{E}} \|\mathbf{H}_u \mathbf{e}_{ij}\|_F^2 = \min_{\mathbf{e}_{ij} \in \mathbb{E}} \mathbf{e}_{ij}^H \mathbf{H}_u^H \mathbf{H}_u \mathbf{e}_{ij}, \end{aligned} \quad (9)$$

where we have the error vector $\mathbf{e}_{ij} = \mathbf{x}_i - \mathbf{x}_j$, $\mathbf{x}_i, \mathbf{x}_j \in \mathbb{X}$. In [21], the max- d_{\min} aided ED-TAS algorithm is defined as

$$\mathbf{H}_{\hat{u}} = \arg \max_{u \in \{1, \dots, N_U\}} d_{\min}(\mathbf{H}_u). \quad (10)$$

The optimum solution obeying the objective function of Eq. (10) can be found by an exhaustive search over all possible $\binom{N_t}{L}$ candidate channel matrices and all the different error vectors, which imposes a complexity order of $\mathcal{O}(N_t^2 M^2)$. This results in an excessive complexity, when high data rates are required.

C. The Conventional QRD-Based ED-TAS

In order to reduce the complexity of the exhaustive ED-TAS of Eq. (10), in [21] an ED-TAS based on an equivalent decision metric $\mathbf{D}(u)$ was formulated as:

$$\mathbf{H}_{\hat{u}} = \arg \max_{u \in \{1, \dots, N_U\}} \{\min[\mathbf{D}(u)]\}, \quad (11)$$

where $\mathbf{D}(u)$ is an $(L \times L)$ -element sub-matrix of an upper triangular $(N_t \times N_t)$ -element matrix \mathbf{D} obtained by deleting the specific rows and columns that are absent in u , while $\min[\mathbf{D}(u)]$ is the minimum non-zero value of $\mathbf{D}(u)$. Here, the (i, j) -th element of \mathbf{D} can be expressed as

$$\begin{aligned} \mathbf{D}_{ij} &= \min_{s_1, s_2 \in \mathbb{S}} \|\mathbf{H}(s_1 \mathbf{e}_i - s_2 \mathbf{e}_j)\|_F^2 \\ &= \min_{s_1, s_2 \in \mathbb{S}} \|\mathbf{h}(i)s_1 - \mathbf{h}(j)s_2\|_F^2, \end{aligned} \quad (12)$$

where s_1 and s_2 are M -ary APM constellation points, while $\mathbf{h}(i)$ and $\mathbf{h}(j)$ are the i th and j th columns of \mathbf{H} . Provided that we have $i = j$ in Eq. (12), the corresponding element becomes $\mathbf{D}_{ii} = \min_{s_1, s_2 \in \mathbb{S}} (\|\mathbf{h}(i)\|_F^2 |s_1 - s_2|^2) =$

$d_{\min}^{\text{APM}} \|\mathbf{h}(i)\|_F^2$, where d_{\min}^{APM} is the minimum distance of the APM constellation. For the case of $i \neq j$, \mathbf{D}_{ij} is re-formulated in the real-valued representation of the QRD as

$$\mathbf{D}_{ij} = \min_{\substack{s_{1I}, s_{2I} \in \mathcal{R}\{\mathbb{S}\}, \\ s_{1Q}, s_{2Q} \in \mathcal{I}\{\mathbb{S}\}}} \|\mathbf{R}[s_{1I}, s_{1Q}, -s_{2I}, -s_{2Q}]\|_F^2, \quad (13)$$

where we have $s_{nI} = \mathcal{R}\{s_n\}$ and $s_{nQ} = \mathcal{I}\{s_n\}$ for $n = 1, 2$, while \mathbf{R} is a (4×4) -element upper triangular matrix created by the QRD of the resultant channel matrix [21]. As shown in [21], the complexity order of this QRD-TAS is $\mathcal{O}(N_t^2 M)$, which

increases only linearly with the modulation order M . In [22] and [24], both the modulus and the symbol set symmetry of the APM constellations were exploited for further reducing the complexity of this algorithm.

D. The Conventional SVD-Based ED-TAS

Although the QRD-based ED-TAS of Eq. (13) is capable of finding the optimal solution, its complexity imposed is a function of the modulation order M . Moreover, the high-complexity QRD has to be applied to the $(2N_r \times 4)$ -element channel matrices [21], [22], [24]. Hence, the complexity of this TAS remains high. This problem was circumvented in [23], where the ED was classified into three categories as follows

$$d_{\min}(\mathbf{H}_u) = \min \left\{ d_{\min}^{\text{signal}}, d_{\min}^{\text{spatial}}, d_{\min}^{\text{joint}} \right\}, \quad (14)$$

where we have

$$\begin{aligned} d_{\min}^{\text{signal}} &= \min_{i=1, \dots, L} \|\mathbf{h}_u(i)\|_F^2 \min_{s_a \neq s_b \in \mathbb{S}} |s_a - s_b|^2 \\ &= d_{\min}^{\text{APM}} \min_{i=1, \dots, L} \|\mathbf{h}_u(i)\|_F^2, \end{aligned} \quad (15)$$

$$\begin{aligned} d_{\min}^{\text{spatial}} &= \min_{\substack{i, j=1, \dots, L \\ i \neq j}} \|\mathbf{h}_u(i) - \mathbf{h}_u(j)\|_F^2 \min_{s_l \in \mathbb{S}} |s_l|^2 \\ &= d_{\min}^{\text{Modulus}} \min_{\substack{i, j=1, \dots, L \\ i \neq j}} \|\mathbf{h}_u(i) - \mathbf{h}_u(j)\|_F^2, \end{aligned} \quad (16)$$

$$d_{\min}^{\text{joint}} = \min_{\substack{i, j=1, \dots, L, i \neq j \\ s_a, s_b \in \mathbb{S}, a \neq b}} \|\mathbf{h}_u(i)s_a - \mathbf{h}_u(j)s_b\|_F^2. \quad (17)$$

In Eq. (16), the term $d_{\min}^{\text{Modulus}} = \min_{s_l \in \mathbb{S}} |s_l|^2$ is the minimum squared modulus value of the APM constellation. Since the calculations of d_{\min}^{signal} and $d_{\min}^{\text{spatial}}$ in Eqs. (15) and (16) do not depend on the size of APM constellation and the corresponding complexity is low, the complexity of computing the FD of Eq. (14) is dominated by the computation of d_{\min}^{joint} in Eq. (17). To reduce this complexity, in [23] the Rayleigh-Ritz theorem was utilized for driving a lower bound of d_{\min}^{joint} as

$$\begin{aligned} d_{\min}^{\text{joint}} &= \min_{\substack{i, j=1, \dots, L, i \neq j \\ s_a, s_b \in \mathbb{S}, a \neq b}} \left\| [\mathbf{h}_u(i), -\mathbf{h}_u(j)] [s_a, s_b]^T \right\|_F^2 \\ &\geq d_{\min}^{\text{SVD-bound}} \\ &= \min_{i, j=1, \dots, L, i \neq j} \lambda_{\min}^2(\mathbf{H}_{u,ij}) \min_{s_a, s_b \in \mathbb{S}} \left\| [s_a, s_b]^T \right\|_F^2 \\ &= \min_{i, j=1, \dots, L, i \neq j} \lambda_{\min}^2(\mathbf{H}_{u,ij}) d_{\min}^{\text{all}} \end{aligned} \quad (18)$$

where we have $d_{\min}^{\text{all}} = \min_{s_a, s_b \in \mathbb{S}} \left\| [s_a, s_b]^T \right\|_F^2$ and $\mathbf{H}_{u,ij} = [\mathbf{h}_u(i), -\mathbf{h}_u(j)]$ is an $(N_r \times 2)$ -element matrix. Here, $\lambda_{\min}^2(\mathbf{H}_{u,ij})$ is the minimum squared singular value of the submatrix $\mathbf{H}_{u,ij}$. Upon exploiting Eq. (18), the distance $d_{\min}(\mathbf{H}_u)$ of Eq. (14) is bounded by

$$d_{\min}^{\text{SVD}}(\mathbf{H}_u) = \min \{ d_{\min}^{\text{signal}}, d_{\min}^{\text{spatial}}, d_{\min}^{\text{SVD-bound}} \}. \quad (19)$$

Based on Eq. (19), the SVD-TAS algorithm is given by

$$\mathbf{H}_{\hat{u}} = \arg \max_{u \in \{1, \dots, N_U\}} d_{\min}^{\text{SVD}}(\mathbf{H}_u). \quad (20)$$

Compared to the conventional QRD-based TAS, this bound-aided algorithm has the following advantages:

- Using the SVD-based bound of Eq. (18), the calculation of the distance d_{\min}^{joint} is independent of the APM modulation order;
- Moreover, the SVD operation of Eq. (18) is performed on the smaller channel matrices of size $(N_r \times 2)$ compared to the QRD-based ED-TAS, which is performed on $(2N_r \times 4)$ -element matrices. In [25], the complexity of SVD-TAS [23] was further reduced through an alternative computation of the singular value.

IV. THE PROPOSED LOW-COMPLEXITY ED-TAS

As shown in subsection III, the conventional QRD-based ED-TAS is capable of achieving the optimal BER, but it imposes high complexity. In contrast, the SVD-based ED-TAS imposes a lower complexity at the cost of a BER performance degradation, because the derived bound may be loose and the corresponding TAS results may be suboptimal.

To circumvent this problem, in this section, a pair of ED-TAS algorithms are proposed. Specifically, an improved QRD-TAS is proposed, where a tighter QRD-based lower bound of the ED is found for replacing the SVD-based bound of [23], while the sparse nature¹ of the error vectors of SM is exploited to avoid the full-dimensional QRD operation. Then, for striking a further flexible BER vs complexity tradeoff, we propose an EVM-based ED-TAS algorithm, which exploits the error vector selection probability to shrink the search space.

A. The Proposed QRD-Based ED-TAS

1) *The QRD-Based Bounds:* To evaluate the value of d_{\min}^{joint} more accurately, in this paper, we apply the QRD-based bound to replace the SVD-bound of Eq. (18). Specifically, the submatrix $\mathbf{H}_{u,ij}$ of Eq. (18) is first subjected to the QRD [38], yielding $\mathbf{H}_{u,ij} = \tilde{\mathbf{Q}}\tilde{\mathbf{R}}$, where $\tilde{\mathbf{Q}}$ is an $(N_r \times 2)$ column-wise orthonormal matrix and $\tilde{\mathbf{R}}$ is a (2×2) upper triangular matrix with positive real-valued diagonal entries formulated as

$$\tilde{\mathbf{R}} = \begin{bmatrix} \tilde{R}_{1,1} & \tilde{R}_{1,2} \\ 0 & \tilde{R}_{2,2} \end{bmatrix}. \quad (21)$$

Let $[\tilde{\mathbf{R}}]_k = \tilde{R}_{k,k}$ denote the k th diagonal entry of $\tilde{\mathbf{R}}$. Based on this decomposition, another lower bound of the distance d_{\min}^{joint} in Eq. (18) can be formulated as

$$\begin{aligned} d_{\min}^{\text{joint}} &\geq d_{\min}^{\text{QRD-bound}} \\ &= \min_{i, j=1, \dots, L, i \neq j} \{ [\tilde{\mathbf{R}}]_{\min}^2 \} \min_{s_a \neq s_b \in \mathbb{S}} \left\| [s_a, s_b]^T \right\|_F^2, \\ &= \min_{i, j=1, \dots, L, i \neq j} \{ [\tilde{\mathbf{R}}]_{\min}^2 \} d_{\min}^{\text{all}} \end{aligned} \quad (22)$$

¹In SM, the transmit vector \mathbf{x} only has a single non-zero element, hence the number of non-zero elements of the error vectors \mathbf{e}_{ij} of SM is no more than 2.

297 where $[\tilde{\mathbf{R}}]_{\min}^2$ is the minimum squared nonzero diagonal entry
 298 of the upper matrix $\tilde{\mathbf{R}}$, given by

$$[\tilde{\mathbf{R}}]_{\min} = \min\{\tilde{R}_{1,1}, \tilde{R}_{2,2}\}. \quad (23)$$

299 *Lemma 1:* For an $(N_r \times 2)$ -element full column-rank matrix
 300 $\mathbf{H}_{u,ij}$ associated with its minimum squared singular non-zero
 301 value $\lambda_{\min}^2(\mathbf{H}_{u,ij})$ for SVD and its minimum squared diago-
 302 onal non-zero entry $[\tilde{\mathbf{R}}]_{\min}^2$ of $\tilde{\mathbf{R}}$ for QRD, respectively, the
 303 inequality $[\tilde{\mathbf{R}}]_{\min}^2 \geq \lambda_{\min}^2(\mathbf{H}_{u,ij})$ is satisfied.

304 According to the analysis process in Section III of [38], the
 305 formulation of Lemma 1 is straightforward. As a result, the
 306 lower bound of Eq. (22) achieved by the QRD is tighter than
 307 that of the SVD algorithm in Eq. (18).

308 To derive an even tighter upper QRD bound than that of
 309 Eq. (22), the permutation matrix $\mathbf{\Pi}_m$ can be invoked for
 310 calculating d_{\min}^{joint} of Eq. (22) as

$$d_{\min}^{\text{joint}} = \min_{\substack{i,j=1,\dots,L, \\ i \neq j, s_a, s_b \in \mathcal{S}}} \left\| [\mathbf{h}_u(i), -\mathbf{h}_u(j)] \mathbf{\Pi}_m \mathbf{\Pi}_m^{-1} [s_a, s_b]^T \right\|_F^2, \quad (24)$$

311 where $\mathbf{\Pi}_m$ is an orthogonal matrix satisfying $\mathbf{\Pi}_m^{-1} = \mathbf{\Pi}_m^T$.
 312 Since the size of the channel matrix $\mathbf{H}_{u,ij} = [\mathbf{h}_u(i), -\mathbf{h}_u(j)]$
 313 is $N_r \times 2$, we only have two legitimate permutation matrices
 314 $\mathbf{\Pi}_m \in \mathbb{C}^{2 \times 2}$, $m = 1, 2$, namely

$$\mathbf{\Pi}_1 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \text{ and } \mathbf{\Pi}_2 = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}. \quad (25)$$

315 For each matrix $\mathbf{\Pi}_m$, similar to Eq. (22), the corresponding
 316 QRD-based bound is

$$\begin{aligned} d_{\min}^{\text{joint}} &\geq \min_{i,j=1,\dots,L, i \neq j} \left\{ [\tilde{\mathbf{R}}_m]_{\min}^2 \right\} \min_{s_a, s_b \in \mathcal{S}} \left\| \mathbf{\Pi}_m^T [s_a, s_b]^T \right\|_F^2 \\ &= [\tilde{\mathbf{R}}_m]_{\min}^2 d_{\min}^{\text{all}}, \end{aligned} \quad (26)$$

317 where $\tilde{\mathbf{R}}_m$ is the upper triangular part of the QRD of
 318 the equivalent matrix $\mathbf{H}_{u,ij} \mathbf{\Pi}_m$. Note in Eq. (26) that
 319 the permutation matrix does not change the distance
 320 of $\left\| \mathbf{\Pi}_m^T [s_a, s_b]^T \right\|_F^2$ and we have $\min_{s_a, s_b \in \mathcal{S}} \left\| \mathbf{\Pi}_m^T [s_a, s_b]^T \right\|_F^2 =$

321 $\min_{s_a, s_b \in \mathcal{S}} \left\| [s_a, s_b]^T \right\|_F^2 = d_{\min}^{\text{all}}$. For the permutation matrices given
 322 in Eq. (25), we can obtain two different values $[\tilde{\mathbf{R}}_m]_{\min}$,
 323 ($m = 1, 2$), which are given by $[\tilde{\mathbf{R}}_1]_{\min} = \min\{\tilde{R}_{1,1}(\mathbf{\Pi}_1),$
 324 $\tilde{R}_{2,2}(\mathbf{\Pi}_1)\}$ and $[\tilde{\mathbf{R}}_2]_{\min} = \min\{\tilde{R}_{1,1}(\mathbf{\Pi}_2), \tilde{R}_{2,2}(\mathbf{\Pi}_2)\}$. Here,
 325 $\tilde{R}_{1,1}(\mathbf{\Pi}_m)$ and $\tilde{R}_{2,2}(\mathbf{\Pi}_m)$, $m = 1, 2$ are the diagonal elements
 326 of $\tilde{\mathbf{R}}_m$.

327 *Remark:* The bound of Eq. (22) constitutes a special case of
 328 the bound of Eq. (26), which can be obtained by setting $m = 1$.

329 Based on Eq. (26), an improved QRD-based upper bound of
 330 the distance d_{\min}^{joint} is given by

$$\begin{aligned} d_{\min}^{\text{joint}} &\geq d_{\min}^{\text{QRD-bound}_P} \\ &= \min_{i,j=1,\dots,L, i \neq j} \{ [\tilde{\mathbf{R}}_{\text{QRQ-P}}]_{\min}^2 \} d_{\min}^{\text{all}}. \end{aligned} \quad (27)$$

where we have $[\tilde{\mathbf{R}}_{\text{QRQ-P}}]_{\min}^2 = \max\{[\tilde{\mathbf{R}}_1]_{\min}^2, [\tilde{\mathbf{R}}_2]_{\min}^2\}$. 331

Lemma 2: For an $(N_r \times 2)$ -element full column-rank 332
 matrix $\mathbf{H}_{u,ij}$ having a minimum squared diagonal non-zero 333
 entry $[\tilde{\mathbf{R}}]_{\min}^2$ for its QRD and a value of $[\tilde{\mathbf{R}}_{\text{QRQ-P}}]_{\min}^2 =$ 334
 $\max\{[\tilde{\mathbf{R}}_1]_{\min}^2, [\tilde{\mathbf{R}}_2]_{\min}^2\}$ based on the pair of legitimate permuta- 335
 tion matrices $\mathbf{\Pi}_m \in \mathbb{C}^{2 \times 2}$, $m = 1, 2$, respectively, the inequal- 336
 ity $[\tilde{\mathbf{R}}_{\text{QRQ-P}}]_{\min}^2 \geq [\tilde{\mathbf{R}}]_{\min}^2$ is satisfied. 337

Since we have $[\tilde{\mathbf{R}}]_{\min}^2 = [\tilde{\mathbf{R}}_1]_{\min}^2$, Lemma 2 can be obtained. 338

2) *The Proposed QRD-Based ED-TAS:* According to 339
 Lemma 2, the QRD bound of Eq. (27) is tighter than that 340
 of Eq. (22). Hence, we use this tighter bound to derive the 341
 proposed QRD-based ED-TAS as 342

$$\hat{\mathbf{H}}_u = \arg \max_{u \in \{1, \dots, N_U\}} \left\{ d_{\min}^{\text{signal}}, d_{\min}^{\text{spatial}}, d_{\min}^{\text{QRD-bound}_P} \right\}. \quad (28)$$

Note that the complexity of the QRD-based TAS is domi- 343
 nated by the computation of $[\tilde{\mathbf{R}}_m]_{\min}$. In general, the full QRD 344
 can be adopted in Eq. (26) for solving Eq. (27). However, this 345
 may impose a high complexity. In order to reduce this com- 346
 plexity, for a fixed channel $\mathbf{H}_{u,ij}$, we found that the value of 347
 $[\tilde{\mathbf{R}}_m]_{\min}$ only depends on the diagonal entries of $\tilde{\mathbf{R}}_m$, namely 348
 $\tilde{R}_{k,k}(\mathbf{\Pi}_m)$ ($k = 1, 2$), which can be directly calculated as [38] 349

$$[\tilde{\mathbf{R}}_m]_k = \tilde{R}_{k,k}(\mathbf{\Pi}_m) = \sqrt{\frac{\det[(\mathbf{G}(1:k))^H \mathbf{G}(1:k)]}{\det[(\mathbf{G}(1:k-1))^H \mathbf{G}(1:k-1)]}}, \quad (29)$$

where $\mathbf{G}(1:k)$ denotes a matrix consisting of the first k 350
 columns of $\mathbf{H}_{u,ij} \mathbf{\Pi}_m$. In the classic V-BLAST systems, the cal- 351
 culation of Eq. (29) suffers from the problem of having a high 352
 complexity [38]. In SM, the number of non-zero elements of 353
 the error vectors of SM is up to 2. This sparse character leads 354
 to the simple sub-matrix $\mathbf{H}_{u,ij} = [\mathbf{h}_u(i), -\mathbf{h}_u(j)] \in \mathbb{C}^{N_r \times 2}$ and 355
 hence the values of $\tilde{R}_{k,k}(\mathbf{\Pi}_m)$ ($m = 1, 2, k = 1, 2$) are given by 356

$$\tilde{R}_{1,1}(\mathbf{\Pi}_1) = \sqrt{\|\mathbf{h}_u(i)\|_F^2}, \quad (30)$$

$$\tilde{R}_{2,2}(\mathbf{\Pi}_1) = \sqrt{\frac{\|\mathbf{h}_u(i)\|_F^2 + \|\mathbf{h}_u(j)\|_F^2 - 2\Re\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\}}{\|\mathbf{h}_u(i)\|_F^2}} \quad (31)$$

$$\tilde{R}_{1,1}(\mathbf{\Pi}_2) = \sqrt{\|\mathbf{h}_u(j)\|_F^2} \quad (32)$$

and 357

$$\tilde{R}_{2,2}(\mathbf{\Pi}_2) = \sqrt{\frac{\|\mathbf{h}_u(i)\|_F^2 + \|\mathbf{h}_u(j)\|_F^2 - 2\Re\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\}}{\|\mathbf{h}_u(j)\|_F^2}} \quad (33)$$

The complexity of our proposed QRD-TAS of Eq. (28) 358
 is dominated by the computation of $\tilde{R}_{k,k}(\mathbf{\Pi}_m)$, $m = 1, 2$. In 359
 SM, these values only depend on the values of $\|\mathbf{h}_u(i)\|_F^2$, 360
 $\|\mathbf{h}_u(j)\|_F^2$ and $\mathbf{h}_u(i)^H \mathbf{h}_u(j)$, which are elements of the matrix 361
 $\mathbf{H}^H \mathbf{H}$, as shown in Eqs. (30)-(33). Based on this observa- 362
 tion, we can calculate the values of $\tilde{R}_{k,k}(\mathbf{\Pi}_m)$, $m = 1, 2$ by 363
 reusing these elements for the different TAS candidates \mathbf{H}_u , 364

TABLE I
COMPLEXITY COMPARISON OF DIFFERENT TAS ALGORITHMS FOR SM SYSTEMS

TAS algorithm	ED Optimality	Computational complexity
Exhaustive ED-TAS [13]	optimal	$\frac{N_t(N_t-1)}{2}(5N_r-1)M^2$
Maximum-norm based TAS of [21]	sub-optimal	$2N_tN_r - N_t$
Minimum-correlation based TAS of [15]	sub-optimal	$2N_t^2N_r - N_t^2 + \frac{3}{2}N_t(N_t-1)$
Conventional QRD-based ED-TAS of [24]	optimal	$2N_tN_r - N_t + 32N_t(N_t-1)(N_r - \frac{2}{3})\frac{M}{N_{APM}}$ ($N_{APM}=M$ for PSK, $N_{APM}=4$ for QAM)
Conventional SVD-based ED-TAS of [23]	sub-optimal	$2N_tN_r - N_t + \frac{19}{2}N_t(N_t-1)(N_r - \frac{1}{3})$
Simplified SVD-TAS [25]	sub-optimal	$\frac{N_t(N_t-1)}{2}(2N_r+1) + N_t(2N_r-1)$
Proposed QRD-based ED-TAS	sub-optimal	$2N_t^2N_r + \frac{3}{2}N_t(N_t-1)$
Proposed EVM-based ED-TAS	M -PSK: optimal	$2N_t^2N_r - N_t^2 + \frac{1}{2}N_t(N_t-1)(M+7)$
	M -QAM: sub-optimal, $K < v$ optimal, $K = v$	$2N_t^2N_r - N_t^2 + \frac{15}{2}GN_t(N_t-1)$
Exhaustive TAS&PA	—	$\binom{N_t}{L}C_{PA}$
Low-complexity TAS&PA	—	$C_{TAS} + C_{PA} = \begin{cases} C_{PQRD} + C_{PA} \\ C_{EVM} + C_{PA} \end{cases}$

365 hence the resultant complexity is considerably reduced compared to the conventional QRD-based ED-TAS, as will show in
366 Table I.
367

368 To confirm the benefits of the QRD-based bound derived in
369 Eq. (27), Fig. 2 shows the BER performance of the proposed
370 QRD-based ED-TAS algorithm in contrast to the existing SVD-
371 based ED-TAS of [23]. Moreover, we add the performance
372 of the norm-based TAS of [13] and of the exhaustive-search
373 based optimal ED-TAS of [21] as benchmarks. In Fig. 2, the
374 number of TAs is set to $N_t = 4$, where $L = 2$ out of $N_t =$
375 4 TAs were selected in these TAS algorithms. As expected,
376 since the proposed QRD-based ED-TAS has a tighter bound,
377 in Fig. 2 it performs better than the SVD-based ED-TAS.
378 Quantitatively, observe in Fig. 2 that this scheme provides an
379 SNR gain of about 1.2 dB over the SVD-based ED-TAS at
380 the BER of 10^{-5} . In Fig. 2, we also observe that the QRD-
381 based ED-TAS achieves a near-optimum performance, where
382 the performance gap between the proposed QRD-based ED-
383 TAS and the exhaustive-search-based optimal ED-TAS is only
384 about 0.2 dB. We will provide more detailed comparisons about
385 the BER and the complexity issues in Section VI.

386 B. The Proposed EVM-Based ED-TAS

387 In this section, for striking a further flexible tradeoff in terms
388 of the BER attained and the complexity imposed, we propose
389 an EVM-based ED-TAS algorithm. The proposed EVM-TAS
390 directly calculates the value of $d_{\min}(\mathbf{H}_u)$ for the specific TAS
391 candidate \mathbf{H}_u , rather than exploiting the equivalent decision
392 metric of Eq. (13) or the estimated bound of (18). Specifically,
393 we will derive simple optimization metrics for both PSK and
394 QAM constellations, where the error-vector selection probabil-
395 ity is exploited for reducing the search space.

396 1) *The Calculation of $d_{\min}(\mathbf{H}_u)$ in EVM-Based ED-TAS:*
397 Specifically, the M -PSK constellation can be expressed as
398 $\mathcal{S}_{PSK} = \{e^{j\frac{2m\pi}{M}}, m = 0, \dots, M-1\}$, and the symbols of the
399 rectangular $M = 4^k$ QAM constellation belong to the set
400 of [36]

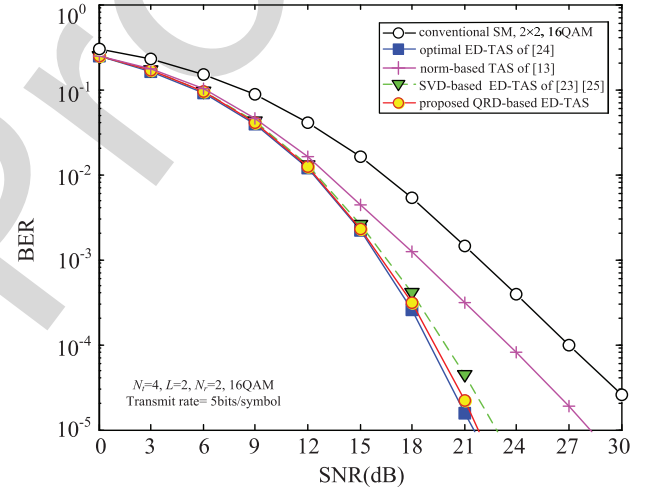


Fig. 2. BER performance comparison of the existing TAS algorithms and the proposed QRD-based ED-TAS algorithm. The setup of the simulation is based on $N_t = 4$, $N_r = 2$, $L = 2$ and 16-QAM. The transmit rate is 5 bits/symbol.

$$\mathcal{S}_{QAM} = \frac{1}{\sqrt{\beta_k}}\{a + bj, a - bj, -a + bj, -a - bj\}, \quad (34)$$

where we have $\beta_k = \frac{2}{3}(4^k - 1)$ and $a, b \in \{1, 3, \dots, 2^k - 1\}$.
401 Similar to Eq. (14), the calculation of $d_{\min}(\mathbf{H}_u)$ is parti-
402 tioned into three cases: d_{\min}^{signal} , $d_{\min}^{\text{spatial}}$ and d_{\min}^{joint} . As shown in
403 Eqs. (15)-(16), d_{\min}^{signal} depends the minimum distance of the
404 APM d_{\min}^{APM} as [39]
405

$$d_{\min}^{\text{APM}} = \begin{cases} 4 \sin^2(\pi/M) & \text{for } M - \text{PSK} \\ \frac{4}{\beta_k} & \text{for } M - \text{QAM} \end{cases}, \quad (35)$$

while $d_{\min}^{\text{spatial}}$ relies on the minimum squared modulus value
406 $d_{\min}^{\text{Modulus}}$ of the APM constellation as
407

$$d_{\min}^{\text{Modulus}} = \begin{cases} 1 & \text{for } M - \text{PSK} \\ \frac{2}{\beta_k} & \text{for } M - \text{QAM} \end{cases}. \quad (36)$$

408 Based on Eqs. (35) and (36), the complexity of computing the
 409 values of d_{\min}^{signal} and $d_{\min}^{\text{spatial}}$ in Eqs. (15)-(16) may be deemed
 410 negligible. Hence, we only have to reduce the complexity of
 411 computing d_{\min}^{joint} , which can be achieved as follows:

$$\begin{aligned} d_{\min}^{\text{joint-EVM}} &= \min_{\substack{i,j=1,\dots,L,i\neq j \\ s_a, s_b \in \mathbb{S}}} \|\mathbf{h}_u(i)s_a - \mathbf{h}_u(j)s_b\|_F^2 \\ &= \min_{\substack{i,j=1,\dots,L, \\ i\neq j, s_a, s_b \in \mathbb{S}}} |s_a|^2 \|\mathbf{h}_u(i)\|_F^2 + |s_b|^2 \|\mathbf{h}_u(j)\|_F^2 - 2m_{\text{APM}}, \end{aligned} \quad (37)$$

412 where we have $m_{\text{APM}} = \mathcal{R}\{s_a^H s_b \mathbf{h}_u(i)^H \mathbf{h}_u(j)\}$, which relies on
 413 the specific APM scheme adopted. Next, we will derive the sim-
 414 plified metrics $d_{\min}^{\text{joint-EVM}}$ for the general family of M -PSK and
 415 M -QAM modulated SM systems.

416 2) *Simplification for M-PSK Schemes:* For a pair of
 417 M -PSK symbols $s_a = e^{j\frac{2a\pi}{M}}$ and $s_b = e^{j\frac{2b\pi}{M}}$, the possible values
 418 of $s_a^H s_b$ obey $e^{j\frac{2(b-a)\pi}{M}}$, $(b-a) \in \{-(M-1), \dots, (M-1)\}$.
 419 As a result, m_{APM} of the general M -PSK scheme obeys:

$$m_{\text{APM}} \in \{\mathcal{R}\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\} \cos \theta_n - \mathcal{J}\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\} \sin \theta_n\}, \quad (38)$$

420 where $\theta_n = \frac{2n\pi}{M}$, $n = -(M-1), \dots, (M-1)$. Since the mini-
 421 mum ED is considered in Eq (37), only the maximum value
 422 of m_{APM} needs to be considered, which is given by Eq. (39),
 423 shown at the bottom of the page. As shown in Eq. (39), the num-
 424 ber of possible θ_n values is reduced from $2M-1$ to $\frac{M}{4}+1$.
 425 According to Eq. (39), $|s_a|^2 = 1$ and $|s_b|^2 = 1$, the distance
 426 $d_{\min}^{\text{joint-EVM}}$ of Eq. (37) is simplified for M -PSK as follows:

$$d_{\min}^{\text{joint-EVM}} = \min_{\substack{i,j=1,\dots,L, \\ i\neq j}} \|\mathbf{h}_u(i)\|_F^2 + \|\mathbf{h}_u(j)\|_F^2 - 2m_{M\text{-PSK}}(\mathbf{H}_u). \quad (40)$$

427 *Example:* The constellation points s_a and s_b of
 428 BPSK and QPSK modulation schemes belong to the
 429 set $\mathbb{S}_{\text{BPSK}} = \{\pm 1\}$ and $\mathbb{S}_{\text{QPSK}} = \{\pm 1, \pm j\}$, respec-
 430 tively. Based on Eq. (39), the corresponding optimized
 431 metrics $m_{M\text{-PSK}}(\mathbf{H}_u) = \max m_{\text{APM}}$ are simplified to
 432 $m_{2\text{-PSK}}(\mathbf{H}_u) = |\mathcal{R}\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\}|$ and $m_{4\text{-PSK}}(\mathbf{H}_u) =$
 433 $\max\{|\mathcal{R}\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\}|, |\mathcal{J}\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\}|\}$, respectively.

434 As shown in Eqs. (37)-(40), since we have $|s_a|^2 = 1$, $|s_b|^2 =$
 435 1 and a reduced set $s_a^H s_b$ for M -PSK constellation, the com-
 436 plexity of calculating $d_{\min}^{\text{joint-EVM}}$ is low, as it will be shown in
 437 Table I.

438 3) *Simplification for M-QAM Schemes:* When M -QAM
 439 constellations are considered, the calculation of $d_{\min}^{\text{joint-EVM}}$ in
 440 Eq. (37) becomes substantially complicated, because there are
 441 many combinations of the values of $|s_a|^2$, $|s_b|^2$ and $s_a^H s_b$ in
 442 Eq. (37), which lead to different received SM-symbol distances.
 443 To derive a simplified optimized metrics for M -QAM, we first
 444 introduce the following Lemma.

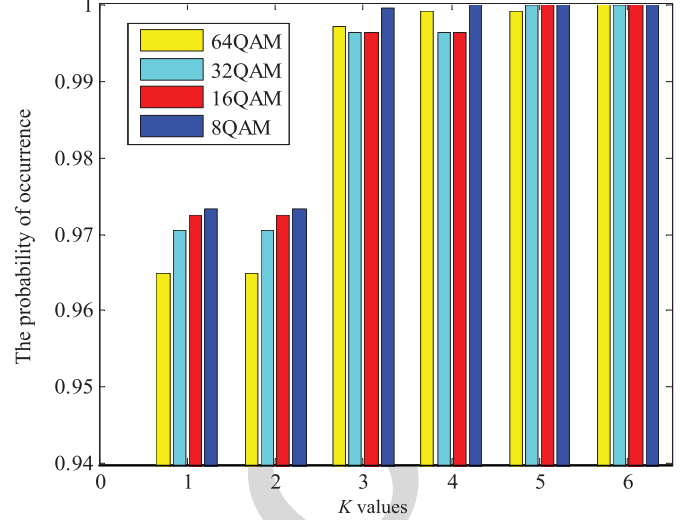


Fig. 3. The statistical probability of the norm error vectors relying on K minimum moduli, yielding the optimal ED-TAS solution, where the system setup is $N_t = 4$, $N_r = 2$ and $L = 2$.

445 *Lemma 3:* It is highly likely that an error vector associated
 446 with a small norm value yields the FD value of Eq. (9). Thus,
 447 the search space to be evaluated for finding the FD can be
 448 reduced to a few dominant error vectors having small norm
 449 values.

450 *Proof:* Based on the Rayleigh-Ritz theorem of [37], for
 451 a fixed channel matrix $\mathbf{H}_{u,ij}$ and a given error vector \mathbf{e}_{ij} ,
 452 the distance amongst the received symbols is bounded by
 453 $\lambda_{\max}^2(\mathbf{H}_{u,ij}) \|\mathbf{e}_{ij}\|^2 \geq \|\mathbf{H}_u \mathbf{e}_{ij}\|^2 \geq \lambda_{\min}^2(\mathbf{H}_{u,ij}) \|\mathbf{e}_{ij}\|^2$, where
 454 $\lambda_{\max}^2(\mathbf{H}_{u,ij})$ is the maximum squared singular value of the sub-
 455 matrix $\mathbf{H}_{u,ij} = [\mathbf{h}_u(i), -\mathbf{h}_u(j)]$. It may be readily shown that
 456 the values of $\lambda_{\max}^2(\mathbf{H}_{u,ij})$ and $\lambda_{\min}^2(\mathbf{H}_{u,ij})$ are constants for
 457 a fixed channel realization $\mathbf{H}_{u,ij}$, while the value of $\|\mathbf{e}_{ij}\|^2$
 458 depends on the specific APM constellation points. Based on the
 459 bound above, it is highly likely that an \mathbf{e}_{ij} with a small norm
 460 yields low upper bound and lower bound. Hence it has a high
 461 probability of generating the FD value, as it will be exemplified
 462 in Fig. 3. ■

463 Based on Lemma 3, for the sake of striking a beneficial
 464 trade-off between the BER performance and complexity for
 465 M -QAM, the search space is limited to the error vectors hav-
 466 ing small modulus values and only these vectors are utilized to
 467 compute the FD metric. Specifically, we first evaluate all possi-
 468 ble modulus values $T_1, T_2, T_3, \dots, T_v$ of all the legitimate error
 469 vectors \mathbf{e}_{ij} , then we find the K smallest T_K from the full set
 470 of $\{T_1, T_2, T_3, \dots, T_v\}$ and only consider the set of \mathbf{e}_{ij} having
 471 moduli lower than T_K to compute $d_{\min}(\mathbf{H}_u)$. In this process,
 472 the error vectors can be divided into the pair of sub-sets \mathbb{D}_1 and
 473 \mathbb{D}_2 based on their sparsity, where \mathbb{D}_1 contains the error vectors,
 474 which have only a single non-zero element, while \mathbb{D}_2 contains

$$\begin{aligned} m_{M\text{-PSK}}(\mathbf{H}_u) &= \max_n m_{\text{APM}} = \max_{n \in \{-(M-1), \dots, M-1\}} \{\mathcal{R}\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\} \cos \theta_n - \mathcal{J}\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\} \sin \theta_n\} \\ &= \max_{n \in \{0, \dots, M/4\}} \{|\mathcal{R}\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\} \cos \theta_n - \mathcal{J}\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\} \sin \theta_n|\} \end{aligned} \quad (39)$$

the error vectors, which have two non-zero elements. As will be shown in our simulation results, $K = 3$ is a good choice for diverse configurations, hence we only provide the simplified expressions of $d_{\min}^{\text{joint-EVM}}$ for $K \leq 3$ as follows.

For $K = 1$, according to the M -QAM constellation of Eq. (34), only error vectors having $T_1 = \sqrt{\frac{4}{\beta_k}}$ are considered and the associated sets \mathbb{D}_1 and \mathbb{D}_2 are given by $\mathbb{D}_1 = \frac{1}{\sqrt{\beta_k}}\{\pm 2\mathbf{e}_i, \pm 2j\mathbf{e}_i\}, i = 1, \dots, L$ and $\mathbb{D}_2 = \frac{1}{\sqrt{\beta_k}}\{(\pm 1 \pm 1j)\mathbf{e}_i - (\pm 1 \pm 1j)\mathbf{e}_j, i, j = 1, \dots, L, i \neq j\}$, respectively, where \mathbf{e}_i and \mathbf{e}_j are the active TA selection vectors in Eq. (2). Since only the minimum ED is considered, the set \mathbb{D}_1 can be reduced to $\mathbb{D}_1 = \frac{1}{\sqrt{\beta_k}}\{2\mathbf{e}_i, i = 1, \dots, L\}$. Moreover, based on the set \mathbb{D}_2 , it is found that the elements s_a and s_b belong to the reduced set $\frac{1}{\sqrt{\beta_k}}\{\pm 1 \pm 1j\}$ and we have $|s_a|^2 = \frac{2}{\beta_k}, |s_b|^2 = \frac{2}{\beta_k}$ and $s_a^H s_b \in \frac{1}{\beta_k}\{\pm 1, \pm 1j\}$. Substituting these values into Eq. (37), we get the simplified optimized metric for $K = 1$ as

$$d_{\min, K=1}^{\text{joint-EVM}} = \min_{\substack{i, j=1, \dots, L, \\ i \neq j}} \frac{2}{\beta_k} \|\mathbf{h}_u(i)\|_F^2 + \frac{2}{\beta_k} \|\mathbf{h}_u(j)\|_F^2 - 2m_{M-QAM}^{K=1}, \quad (41)$$

where we have

$$m_{M-QAM}^{K=1} = \max m_{\text{APM}} = \max \left\{ \frac{2}{\beta_k} |\Re\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\}|, \frac{2}{\beta_k} |\Im\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\}| \right\}. \quad (42)$$

For the case of $K = 2$, all the error vectors \mathbf{e}_{ij} having moduli lower than T_2 are used for FD calculation. Compared to $K = 1$, we have to consider the added error vectors $\frac{1}{\sqrt{\beta_k}}\{\pm 2 \pm 2j\mathbf{e}_i\} (i = 1, \dots, L)$ having $T_2 = \sqrt{\frac{8}{\beta_k}}$, which belong to \mathbb{D}_1 and do not change the set \mathbb{D}_2 . After eliminating all collinear elements, the set \mathbb{D}_1 of $K = 2$ is reduced to $\frac{1}{\sqrt{\beta_k}}\{2\mathbf{e}_i, \pm 2 \pm 2j\mathbf{e}_i, i = 1, \dots, L\}$. Moreover, since only the minimum distance is investigated, the set is further reduced to $\mathbb{D}_1 = \frac{1}{\sqrt{\beta_k}}\{2\mathbf{e}_i, i = 1, \dots, L\}$, which is the same as that of $K = 1$. Therefore, the setups of $K = 1$ and $K = 2$ will provide the same FD $d_{\min}(\mathbf{H}_u)$.

Moreover, for the case of $K = 3$, besides the error vectors \mathbf{e}_{ij} for $K = 2$, the error vectors having $T_3 = \sqrt{\frac{10}{\beta_k}}$ should be considered, which are given by $\frac{1}{\sqrt{\beta_k}}\{(\pm 3 \pm 1j)\mathbf{e}_i - (\pm 1 \pm 1j)\mathbf{e}_j, (\pm 1 \pm 3j)\mathbf{e}_i - (\pm 1 \pm 1j)\mathbf{e}_j\}, i, j = 1, \dots, L, i \neq j$. For these added error vectors, we have $s_a^H s_b \in \frac{1}{\beta_k}\{\pm 2 \pm 4j, \pm 4 \pm 2j\}$ and two legitimate combinations of the values of $|s_a|^2$ and $|s_b|^2$ as: (1) $|s_a|^2 = \frac{2}{\beta_k}, |s_b|^2 = \frac{10}{\beta_k}$

and (2) $|s_a|^2 = \frac{10}{\beta_k}, |s_b|^2 = \frac{2}{\beta_k}$. For each combination, similar to the process of Eqs. (41)-(42), we can substitute the values of $|s_a|^2, |s_b|^2$ and $s_a^H s_b$ into Eq. (37) and get the simplified optimized metric for $K = 3$ as

$$d_{\min, K=3}^{\text{joint-EVM}} = \min\{d_{\min, K=1}^{\text{joint-EVM}}, d_{\min, (1)}^{\text{joint-EVM}}, d_{\min, (2)}^{\text{joint-EVM}}\} \quad (43)$$

where $d_{\min, (1)}^{\text{joint-EVM}}$ and $d_{\min, (2)}^{\text{joint-EVM}}$ are the simplified ED for the above-mentioned two combinations, given by Eq. (44), shown at the bottom of the page.

4) *The Proposed EVM-Based ED-TAS*: Based on the simplified versions of $d_{\min}^{\text{joint-EVM}}$ for M -PSK and M -QAM schemes derived in Eqs. (41) and (43), the solution of our EVM-based ED-TAS algorithm is given by

$$\mathbf{H}_{\hat{u}} = \arg \max_{u \in \{1, \dots, N_U\}} \left\{ d_{\min}^{\text{signal}}, d_{\min}^{\text{spatial}}, d_{\min}^{\text{joint-EVM}} \right\}. \quad (45)$$

Note that similar to the proposed QRD-TAS, the terms $\|\mathbf{h}_u(i)\|_F^2, \|\mathbf{h}_u(j)\|_F^2$ and $\mathbf{h}_u(i)^H \mathbf{h}_u(j)$ in Eqs. (40)-(44) are elements of the matrix $\mathbf{H}^H \mathbf{H}$. Then, we can find the solution of Eq. (45) by reusing these elements for different TAS candidates \mathbf{H}_u .

Fig. 3 shows the probability that the error vectors having the minimum norm do result in finding the optimal ED-TAS solution as a function of K . For example, we have a probability of 97% for 16-QAM modulated SM for $K = 1$ using $N_t = 4, L = 2$ and $N_r = 2$. Moreover, it is observed from Fig. 3 that this probability is also high for other QAM schemes; hence the EVM-based ED-TAS can be readily used in diverse scenarios. In general, for striking a flexible BER vs complexity tradeoff, we can adjust the parameter K to reduce the search space to a subset of the error vectors that may yield the optimal ED-TAS solution with a high probability.

Note that in [17] a PEP-based TAS (PEP-TAS) algorithm was proposed, which was based on a different search set reduction. The main differences of the proposed EVM-TAS and the PEP-TAS of [17] are:

- The PEP-TAS is based on the assumption that a smaller APM symbol amplitude leads to a smaller distance d_{\min}^{joint} , whereas based on our analysis it is highly likely that an error vector with a small norm yields the distance d_{\min}^{joint} .
- Moreover, in EVM-TAS, we propose to use the parameter K for striking a flexible tradeoff between the conflicting factors of the computational complexity imposed and the attainable BER.

Remark: Compared to the EVM-TAS, the PEP-TAS considers only the error vectors generated by M -QAM symbols having the minimum amplitude. It can be shown that the non-linear error vectors of the PEP-TAS are the same as those of the

$$\left\{ \begin{array}{l} d_{\min, (1)}^{\text{joint-EVM}} = \min_{\substack{i, j=1, \dots, L \\ i \neq j}} \frac{2}{\beta_k} \|\mathbf{h}_u(i)\|_F^2 + \frac{10}{\beta_k} \|\mathbf{h}_u(j)\|_F^2 - 2m_{M-QAM}^{K=3} \\ d_{\min, (2)}^{\text{joint-EVM}} = \min_{\substack{i, j=1, \dots, L \\ i \neq j}} \frac{10}{\beta_k} \|\mathbf{h}_u(i)\|_F^2 + \frac{2}{\beta_k} \|\mathbf{h}_u(j)\|_F^2 - 2m_{M-QAM}^{K=3} \\ m_{M-QAM}^{K=3} = \max \frac{1}{\beta_k} \left\{ |2\Re\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\}| + |4\Im\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\}|, |4\Re\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\}| + |2\Im\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\}| \right\} \end{array} \right. \quad (44)$$

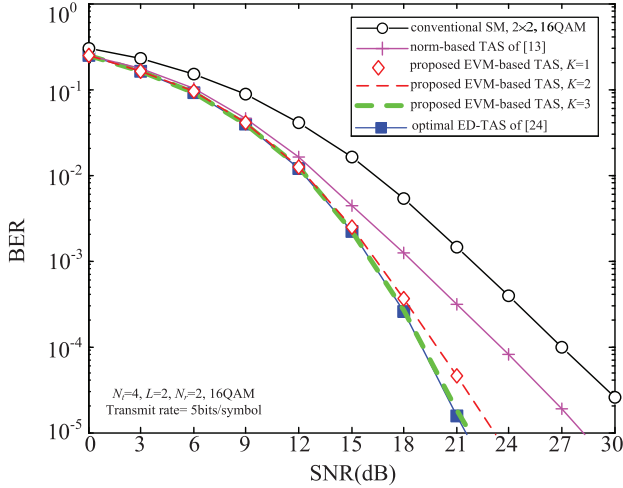


Fig. 4. BER performance comparison of the existing TAS algorithms and the proposed EVM-based TAS algorithm for $N_t = 4$, $N_r = 2$, 16QAM and $L = 2$. The transmit rate is 5 bits/symbol.

554 EVM-TAS associated with $K = 1$. Therefore, it can be viewed
 555 as a special case of EVM-TAS by setting $K = 1$.

556 Fig. 4 shows our BER comparison for the existing TAS
 557 algorithms and the proposed EVM-TAS algorithm. The simu-
 558 lation parameters are the same as those of Fig. 2. Firstly,
 559 as proved in Section IV-B and observed in Fig. 3, the proba-
 560 bility that the error vectors do indeed result in the optimal
 561 ED-TAS solution is the same for the cases of $K = 1$ and $K = 2$.
 562 Hence, they provide the same BER performance, as shown in
 563 Fig. 4. Furthermore, we observe in Fig. 3 that this probabili-
 564 ty is increased from 0.975 to 0.998 upon increasing K from 1
 565 to 3. As a result, in Fig. 4 the performance of the EVM-based
 566 ED-TAS associated with $K = 3$ is improved compared to that
 567 scheme with $K = 1$. Moreover, compared the results in Figs. 2
 568 and 4, the EVM-based ED-TAS outperforms the SVD-based
 569 ED-TAS for $K = 3$.

570 V. JOINT TAS AND PA ALGORITHMS FOR SM

571 Similar to the TAS technique, PA is another attractive link
 572 adaptation technique conceived for SM, which has been advo-
 573 cated in [7], [11], [28], [29]. The process of PA can be modeled
 574 by the PA matrix \mathbf{P} , which is given by

$$\mathbf{P} = \text{diag}\{p_1, \dots, p_q, \dots, p_L\}, \quad (46)$$

575 where p_q controls the channel gain of the q th TA. Here, we let
 576 $\sum_{q=1}^L p_q^2 = 1$ for normalizing the transmit power. Based on our
 577 TAS algorithms, we propose a pair of combined algorithms for
 578 jointly considering the PA and TAS as follows:

579 1) **TAS&PA**

- 580 • *Step 1:* Each $(N_r \times N_t)$ channel matrix \mathbf{H} has $N_U =$
 581 $\binom{N_t}{L}$ possible subchannel matrices \mathbf{H}_u , each of
 582 which corresponds to a specifically selected $(N_r \times$
 583 $L)$ MIMO channel. For each \mathbf{H}_u , we calculate the
 584 corresponding PA matrix \mathbf{P}_u and its FD with the aid
 585 of the algorithm of [29].
- 586 • *Step 2:* The particular combinations of $\mathbf{H}_u \mathbf{P}_u (u =$
 587 $1, \dots, N_U)$ constitute the legitimate TAS&PA

candidates. Let us interpret the matrices $\mathbf{H}_u \mathbf{P}_u$ 588
 ($u = 1, \dots, N_U$) as being the equivalent channel 589
 matrices of Section IV and select the specific can- 590
 didate with the maximum free distance as the final 591
 solution. 592

Since for each channel realization \mathbf{H} , there are N_U pos- 593
 sible PA matrices $\mathbf{P}_u (u = 1, \dots, N_U)$, we have a high 594
 computational complexity if N_U is high. Next, we intro- 595
 duce a lower-complexity solution for this joint TAS and 596
 PA algorithm. 597

2) **Low-complexity TAS&PA** 598

- 599 • *Step 1:* Assume $\mathbf{P}_u = \mathbf{I}_L (u = 1, \dots, N_U)$ and use
 600 the proposed low-complexity QRD-based ED-TAS
 601 or the EVM-based ED-TAS algorithm to select a
 602 particular subset of TAs from the set of options,
 603 which corresponds to $\mathbf{H}_{\hat{u}}$.
- 604 • *Step 2:* Calculate the power weights for the selected
 605 TAs, which can be represented by the PA matrix $\hat{\mathbf{P}}_{\hat{u}}$.
 606 During this step, the low-complexity PA algorithm
 607 of [29] can be invoked. In the simple TAS&PA, the
 608 PA matrix only has to be calculated once, hence the
 609 associated complexity is low.

610 VI. SIMULATION RESULTS

In this section, we provide simulation results for further char- 611
 acterizing the proposed QRD-based ED-TAS, EVM-based ED- 612
 TAS and TAS&PA schemes for transmission over frequency- 613
 flat fading MIMO channels. For comparison, these performance 614
 results are compared to various existing TAS-SM schemes of 615
 [13], [21], [23], [25], to the classic TAS/maximal-ratio combin- 616
 ing (TAS/MRC) schemes of [40], as well as to the TAS&PA 617
 aided V-BLAST of [32]. In our simulations, the single-stream 618
 ML detector of [34], [35] is utilized. 619

620 A. BER Comparisons of Different TAS Algorithms for SM

In Fig. 5, we compare the BER performance of various TAS- 621
 SM schemes for 4 bits/symbol associated with $N_t = 8$, $L = 4$, 622
 $N_r = 4$ and QPSK. We also considered the conventional single- 623
 RF based TAS/MRC arrangement of [40] as benchmarker. As 624
 seen from Fig. 5, the proposed QRD-based ED-TAS outper- 625
 forms the conventional SVD-based ED-TAS of [23], as also 626
 formally shown in Fig. 2. Moreover, as expected, in Fig. 5 627
 the EVM-based TAS is capable of achieving the same per- 628
 formance as the optimal ED-TAS of [21]. We also confirm 629
 that our proposed EVM-based ED-TAS schemes outperform 630
 the norm-based TAS of [13] and the QRD-based ED-TAS pro- 631
 posed for PSK modulation. These results are consistent with the 632
 analysis results in Section IV, where the EVM-based TAS has 633
 considered all legitimate error vectors for simplifying d_{\min}^{joint} in 634
 Eq. (40), while the QRD-based ED-TAS may achieve uncorrect 635
 estimation of d_{\min}^{joint} due to the employment of lower bound of 636
 Eq. (27). 637

Fig. 5 also shows that our new TAS-SM schemes outper- 638
 form the TAS/MRC scheme of [40]. The main reason behind 639
 the poorer performance of TAS/MRC is the employment of 640
 a higher modulation order required for achieving the same 641

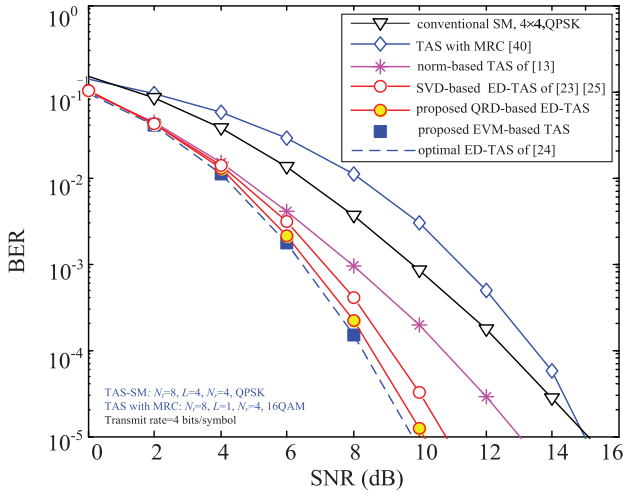


Fig. 5. BER comparison at $m = 4$ bits/symbol for the proposed TAS-SM schemes, the existing TAS-SM schemes and the classic TAS/MRC scheme having $N_t = 8$ and $L = 4$.

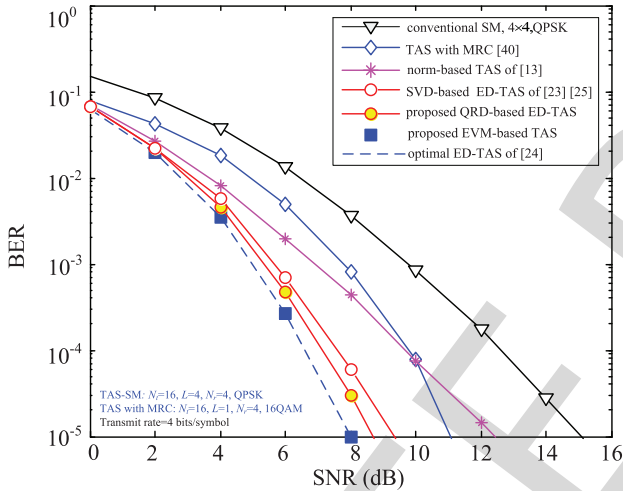


Fig. 6. BER comparison at $m = 4$ bits/symbol for the proposed TAS-SM schemes, the existing TAS-SM schemes and the classic TAS/MRC scheme having $N_t = 16$ and $L = 4$.

throughput as our SM-based schemes. Note that this benefit depends on the particular MIMO setups. To be specific, as noted in [23], the TAS-SM and the TAS/MRC schemes exhibit different BER advantages for different system setups. However, similar to the results achieved in [23], our new TAS-SM schemes strike an attractive tradeoff between the complexity and the BER attained. The above-mentioned trends of these proposed TAS-SM schemes are also confirmed in Fig. 6, where the number N_t of TAs increases from 8 to 16.

In Fig. 7, a spatially correlated MIMO channel model characterized by $\mathbf{H}^{corr} = \mathbf{R}_r^{1/2} \mathbf{H} \mathbf{R}_t^{1/2}$ [24], [41] is considered for the proposed QRD-based ED-TAS and EVM-based TAS ($K = 3$) schemes, where $\mathbf{R}_t = [r_{ij}]_{N_t \times N_t}$ and $\mathbf{R}_r = [r_{ij}]_{N_r \times N_r}$ are the positive definite Hermitian matrices that specify the transmit and receive correlations, respectively. In Fig. 7, the components of \mathbf{R}_t and \mathbf{R}_r are calculated as $r_{ij} = r_{ji}^* = r^{j-i}$ for $i \leq j$, where r is the correlation coefficient ($0 \leq r \leq 1$). Here, the simulation parameters are the same as those of Figs. 2 and 4

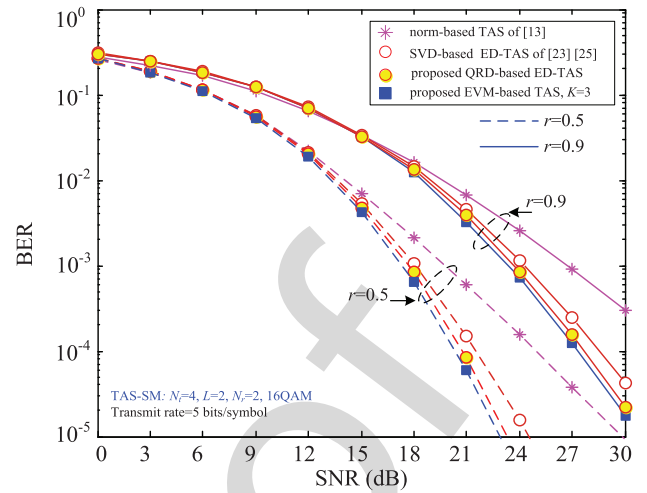


Fig. 7. BER comparison of different TAS algorithms for SM systems in correlated Rayleigh fading channels.

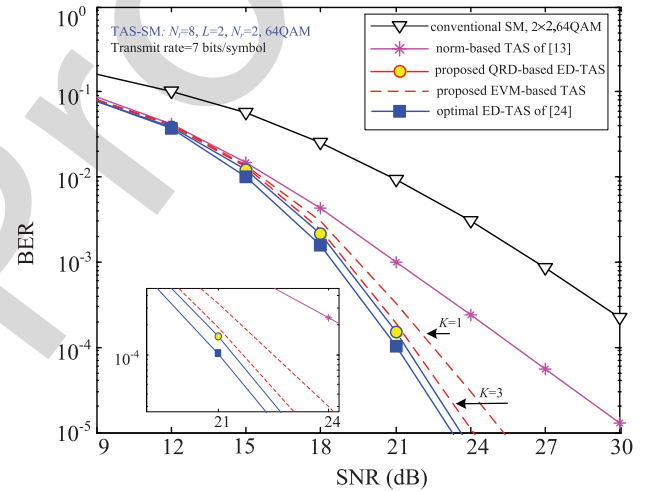


Fig. 8. BER comparison at $m = 7$ bits/symbol for the proposed QRD-based ED-TAS and EVM-based ED-TAS with 64-QAM.

for 5 bits/symbol transmissions. We found that the BER curves of the EVM-based TAS schemes and of the optimal ED-TAS are almost overlapped (similar to the results seen in Fig. 4), hence for clarity in Fig. 7 we simply provide the BER curves for the EVM-based TAS schemes only. Compared to the BER curves in Figs. 2 and 4 for the correlation coefficient $r = 0$, we observe in Fig. 7 that the BER performance of all schemes is substantially degraded by these correlations. However, the proposed schemes remain capable of operating efficiently for the correlated channels.

In Fig. 8, we further compare the proposed QRD-based ED-TAS scheme and the proposed EVM-based TAS schemes for a higher modulation order, where the 64-QAM scheme is employed. Observe in Fig. 8 that the proposed QRD-based ED-TAS scheme outperforms the EVM-based TAS scheme in conjunction with $K = 1$ and the corresponding performance gain is seen to be about 1 dB. Similar to the results in Figs. 2 and 4, the EVM-based TAS associated with $K = 3$ provide an improved BER compared to that scheme with $K = 1$. At

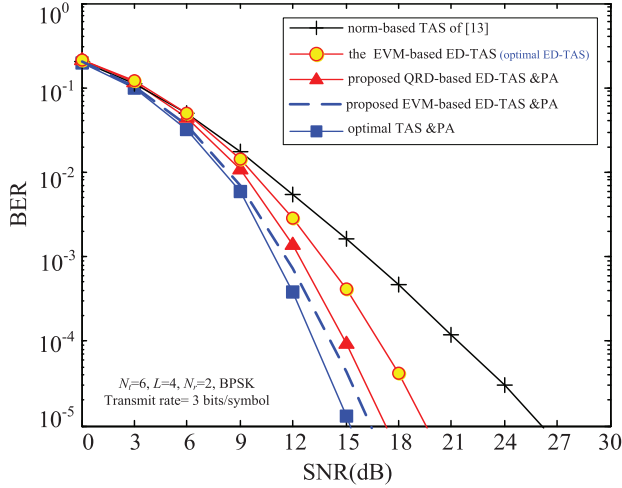


Fig. 9. BER performance comparison of the TAS algorithms and of the proposed TAS &PA algorithms in SM systems, having the transmit rate of 3 bits/symbol.

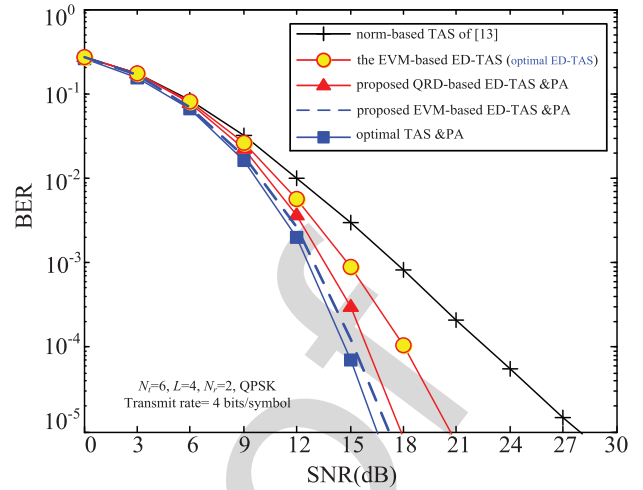


Fig. 10. BER performance comparison of the TAS algorithms and of the proposed TAS &PA algorithms in SM systems, having the transmit rate of 4 bits/symbol.

679 BER= 10^{-5} , the performance gap between the proposed EVM-
 680 based TAS with $K = 3$ and the proposed QRD-based ED-TAS
 681 becomes negligible.

682 The main conclusions observed from Figs. 2, 4 and 5–8 are:
 683 (1) the proposed EVM-based TAS and QRD-based ED-TAS
 684 schemes exhibit different BER advantages for different system
 685 setups; (2) the proposed QRD-based ED-TAS is preferred
 686 to the QAM-modulated SM schemes, since its complexity is
 687 independent of the modulation order; (3) The proposed EVM-
 688 based TAS is preferred to the PSK-modulated SM schemes,
 689 since it can achieve the performance of optimal ED-TAS at
 690 the reduced error vector set. (4) For the QAM-modulated SM
 691 schemes, the parameter K of the proposed EVM-based TAS
 692 can be flexibly selected for striking a beneficial trade-off between
 693 the complexity imposed and the BER attained.

694 *B. BER Comparisons of TAS Algorithms and TAS &PA*
 695 *Algorithms for SM*

696 In this subsection, we focus our attention on studying the
 697 BER performance of our TAS&PA algorithms. Here, for the
 698 low-complexity TAS&PA, the proposed QRD-based ED-TAS
 699 as well as the EVM-based ED-TAS algorithms are utilized and
 700 the corresponding algorithms are termed as the QRD-based
 701 ED-TAS &PA and the EVM-based ED-TAS &PA, respec-
 702 tively. Note that the EVM-based ED-TAS achieves the same
 703 performance as the optimal ED-TAS for the PSK-modulated
 704 SM schemes. The BER performances of other TAS algorithms
 705 are similar to the results seen in Figs. 2, 4 and 5–8. Hence,
 706 for clarity, when only pure TAS is considered, we simply
 707 provide the corresponding BER curves of the proposed EVM-
 708 based ED-TAS and of the conventional norm-based TAS as
 709 benchmarks.

710 Fig. 9 compares the BER performance of the proposed
 711 TAS&PA arrangement to that of other SM-based schemes. In
 712 Fig. 9, the parameter setup is $N_t = 6$, $L = 4$, $N_r = 2$ and
 713 $M = 2$. It becomes clear from Fig. 9 that the TAS&PA algo-
 714 rithms advocated outperform both the EVM-based ED-TAS and

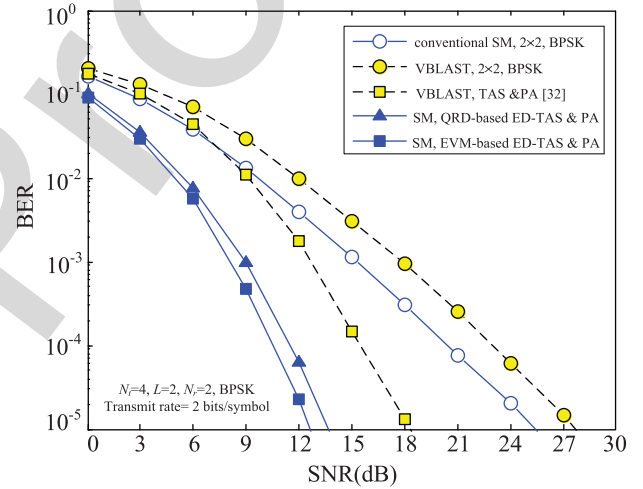


Fig. 11. BER performance comparison of the proposed TAS &PA algorithms in SM systems and the conventional identical-throughput TAS&TA algorithm in V-BLAST systems, where the throughput is 2 bits/symbol ($N_t = 4$, $N_r = 2$, $L = 2$).

the norm-based ED-TAS. At a BER of 10^{-5} , the exhaustive- 715
 search based optimal TAS&PA provides 9.5 dB and 4 dB SNR 716
 gains over the norm-based ED-TAS and over the EVM-based 717
 ED-TAS, respectively. Moreover, the low-complexity QRD- 718
 based ED-TAS &PA provides about 4 dB SNR gain over the 719
 EVM-based TAS operating without PA. 720

Fig. 9 also shows that the EVM-based ED-TAS &PA outper- 721
 forms the QRD-based ED-TAS&PA and is capable of achieving 722
 almost the same BER performance as the optimal TAS&PA. 723
 The performance advantages of our schemes are attained as 724
 a result of exploiting all the benefits of MIMO channels. The 725
 above-mentioned trends of these TAS&PA algorithms recorded 726
 for SM are also visible in Fig. 10, where a SM system using 727
 $N_t = 6$, $L = 4$, $N_r = 2$ and QPSK modulation is considered. 728

In Fig. 11, the BPSK-modulated V-BLAST scheme and its 729
 TAS&PA-aided counterpart [32] associated with zero-forcing 730
 successive interference cancellation (ZF-SIC) are compared to 731

TABLE II
COMPLEXITY COMPARISON OF DIFFERENT TAS-SM ALGORITHMS IN DIVERSE CONFIGURATIONS

TAS algorithm	Configuration 1 ($N_t = 4, N_r = 2$ $L = 2, 16\text{QAM}$)	Configuration 2 ($N_t = 8, N_r = 4$ $L = 4, \text{QPSK}$)	Configuration 3 ($N_t = 8, N_r = 2$ $L = 2, 64\text{-QAM}$)
Exhaustive ED-TAS [13]	13824	8512	1032192
Maximum-norm based TAS [21]	12	56	24
Conventional QRD-based ED-TAS [24]	2060	6029	38253
SVD-based ED-TAS [25]	102	588	444
Proposed QRD-based ED-TAS	82	596	340
Proposed EVM-based ED-TAS	$\begin{cases} 84, K = 1 \\ 180, K = 3 \end{cases}$	756	$\begin{cases} 360, K = 1 \\ 808, K = 3 \end{cases}$
Exhaustive TAS&PA	4626	46340	256788
Proposed QRD-based ED-TAS&PA	853	1004	9511
Proposed EVM-based ED-TAS&PA	$\begin{cases} 855, K = 1 \\ 951, K = 3 \end{cases}$	1164	$\begin{cases} 9531, K = 1 \\ 9979, K = 3 \end{cases}$

our TAS&PA based schemes. For maintaining an identical-throughput, in Fig. 11 we let $N_t = 4, N_r = 2, L = 2$ and use BPSK for all schemes. Observe in Fig. 11 that our TAS&PA based SM schemes outperform the TAS&PA aided V-BLAST schemes by about 5-6 dB SNR at the BER of 10^{-5} .

C. Complexity Comparison

Table I shows the complexity comparison of various TAS algorithms conceived for SM, where the total number of floating point operations is considered. The Appendix provides the details of our computational complexity evaluations for the proposed TAS algorithms list in Table I. The complexity estimation of the existing TAS algorithms can be found in [15], [23] and [24]. Moreover, our complexity analysis is similar to that of [23] and [24].

Explicitly, in Table II, the quantified complexity of different TAS algorithms for some specific configurations are provided. As shown in Table I, the proposed QRD-based ED-TAS has a similar complexity order to that of the low-complexity SVD-based ED-TAS of [23], while exhibiting a lower complexity compared to the conventional QRD-based ED-TAS of [24]. For example, the proposed QRD-based ED-TAS imposes an approximately 168 times and 25 times lower complexity than the exhaustive ED-TAS and the conventional QRD-based ED-TAS for configuration 1. This is due to the fact that it is capable of avoiding the high-complexity QRD operation by directly computing the bound parameters of Eq. (27). Moreover, as shown in Tables I-II and Figs. 4-8, the EVM-based ED-TAS advocated is capable of striking a flexible BER vs complexity trade-off by employing the parameter K for diverse M -QAM schemes. Furthermore, the proposed low-complexity TAS&PA schemes impose a lower complexity than the exhaustive-search based TAS&PA and only impose a slightly increased complexity compared to the proposed EVM-based TAS and QRD-based TAS schemes. By considering the BER vs complexity results of Tables I-II and Figs. 9-11, the proposed low-complexity TAS&PA is seen to provide an improved BER performance at a modest complexity cost.

VII. CONCLUSIONS

In this paper, we have investigated TAS algorithms conceived for SM systems. Firstly, a pair of low-complexity

ED-TAS algorithms, namely the QRD-based ED-TAS and the EVM-based ED-TAS, were proposed. The theoretical analysis and simulation results indicated that the QRD-based ED-TAS exhibits a better BER performance compared with the conventional SVD-based ED-TAS, while the EVM-based ED-TAS is capable of striking a flexible BER vs complexity trade-off. To further improve the attainable performance, the proposed TAS algorithms were amalgamated with PA. A pair of beneficial joint TAS-PA algorithms were proposed and our simulation results demonstrated that they outperform both the pure TAS algorithms and the TAS&PA algorithm designed for spatial multiplexing systems.

APPENDIX

Computational complexity of the proposed TAS algorithms designed for SM systems.

A. The Proposed QRD-Based ED-TAS

As detailed in Section IV-A, the calculation of the QRD-based bound of Eq. (27) only depends on the elements of the matrix $\mathbf{H}^H \mathbf{H}$, which incurs a complexity in the order of $\text{comp}(\mathbf{H}^H \mathbf{H}) = 2N_t^2 N_r - N_t^2$. Then, we can calculate the values of $\tilde{R}_{k,k}(\mathbf{\Pi}_m)$, ($m = 1, 2, k = 1, 2$) in Eqs. (30)-(33) by reusing these elements for the different TAS candidates \mathbf{H}_u . Specifically, the calculation of $\sqrt{\|\mathbf{h}_u(j)\|_F^2}$, $j = 1, \dots, N_t$ for estimating $\tilde{R}_{1,1}(\mathbf{\Pi}_m)$, $m = 1, 2$ in Eqs. (30) and (32) requires N_t flops. Moreover, to calculate the values of $\tilde{R}_{2,2}(\mathbf{\Pi}_m)$, $m = 1, 2$ in Eqs. (31) and (33), we have to consider $\binom{N_t}{2}$ possible combinations (i, j) for computing the value of $\sqrt{\frac{\|\mathbf{h}_u(i)\|_F^2 + \|\mathbf{h}_u(j)\|_F^2 - 2\Re\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\}}{\|\mathbf{h}_u(j)\|_F^2}}$. For each combination, the complexity imposed is 5 flops. Hence, the complexity of computing $\tilde{R}_{2,2}(\mathbf{\Pi}_m)$, $m = 1, 2$ is $5\binom{N_t}{2}$ flops. The overall complexity of the proposed QRD-based ED-TAS is

$$\begin{aligned} C_{\text{PQRD}} &= 2N_t^2 N_r - N_t^2 + N_t + 5\binom{N_t}{2} \\ &= 2N_t^2 N_r + \frac{3}{2}N_t(N_t - 1). \end{aligned} \quad (47)$$

Note that based on Eq. (28), $d_{\min}^{\text{Modulus}}$, d_{\min}^{APM} and d_{\min}^{all} are constants for a specific APM scheme and the calculation of d_{\min}^{signal} and $d_{\min}^{\text{spatial}}$ can also exploit the common elements, such as $\|\mathbf{h}_u(i)\|_F^2 + \|\mathbf{h}_u(j)\|_F^2 - 2\Re\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\}$, $\|\mathbf{h}_u(i)\|_F^2$, in the

807 calculation of the bound of d_{\min}^{joint} , as shown in Eqs. (15) and
 808 (16). Hence, the complexity imposed can be deemed negligible.

809 *B. The Proposed EVM-Based ED-TAS*

810 Similar to the proposed QRD-based ED-TAS, the com-
 811 putational complexity of EVM-based ED-TAS is also domi-
 812 nated by computing d_{\min}^{joint} . Specifically, we also first have to
 813 evaluate the elements $\|\mathbf{h}_u(i)\|_F^2$, $\|\mathbf{h}_u(j)\|_F^2$ and $\mathbf{h}_u(i)^H \mathbf{h}_u(j)$,
 814 which incurs a complexity of $2N_t^2 N_r - N_t^2$ flops. Then,
 815 for M -PSK, the simplified version of d_{\min}^{joint} is given in
 816 Eq. (40), which has to consider $\binom{N_t}{2}$ legitimate TA com-
 817 bination (i, j) . For each combination (i, j) , the computa-
 818 tion of the term $m_{M\text{-PSK}}(\mathbf{H}_u)$ of Eq. (39) has to consider
 819 $(\frac{M}{4} + 1)$ possible θ_n values. For each θ_n , the complexity of
 820 evaluating $|\Re\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\} \cos \theta_n - \Im\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\} \sin \theta_n|$ is
 821 4 flops. Moreover, for a specific $m_{M\text{-PSK}}(\mathbf{H}_u)$ and a fixed
 822 combination (i, j) , the computation of $\|\mathbf{h}_u(i)\|_F^2 + \|\mathbf{h}_u(j)\|_F^2 -$
 823 $2m_{M\text{-PSK}}(\mathbf{H}_u)$ in Eq. (40) requires 3 flops. Hence, the overall
 824 complexity of the M -PSK modulated EVM-based ED-TAS is

$$\begin{aligned} C_{\text{EVM}} &= 2N_t^2 N_r - N_t^2 + \binom{N_t}{2} \{4(\frac{M}{4} + 1) + 3\} \\ &= 2N_t^2 N_r - N_t^2 + \frac{1}{2} N_t (N_t - 1) (M + 7). \end{aligned} \quad (48)$$

825 For the M -QAM scheme, this complexity depends on the
 826 parameter K . Specifically, the simplified versions of d_{\min}^{joint} are
 827 different for different values of K . In general, for a given K ,
 828 we first characterize all possible combinations of $|s_a|^2$ and $|s_b|^2$
 829 by using the method of Section IV-B. Let us assume that the
 830 number of these combinations is G . For each combination, we
 831 can simplify Eq. (37) similar to the process of Eqs. (43)-(44),
 832 which corresponds to G simplified equations and each requires
 833 15 flops, as shown in Eq. (37). Since $\binom{N_t}{2}$ legitimate TA com-
 834 binations (i, j) should be considered in Eq. (37), we arrive at a
 835 complexity of $15G \binom{N_t}{2}$ for all possible combinations. Overall,
 836 the complexity of the EVM-based TAS for M -QAM modulated
 837 SM is

$$C_{\text{EVM}} = 2N_t^2 N_r - N_t^2 + 15G \binom{N_t}{2}. \quad (49)$$

838 Note that the complexity of Eq. (49) is an approximate result,
 839 which can be further refined based on the specific simplified
 840 version of d_{\min}^{joint} . For example, based on Eqs. (41) and (43)
 841 derived for $K = 1$ and $K = 3$, similar to the complexity anal-
 842 ysis of M -PSK, the computational complexity orders of the
 843 EVM-based TAS for $K = 1$ and $K = 3$ are

$$C_{\text{EVM-TAS}} = 2N_t^2 N_r - N_t^2 + 6 \binom{N_t}{2}, \quad (50)$$

844 and

$$C_{\text{EVM-TAS}} = 2N_t^2 N_r - N_t^2 + 22 \binom{N_t}{2}. \quad (51)$$

845 *C. The Proposed PA & TAS*

846 The exhaustive-search based TAS&PA algorithm has to cal-
 847 culate all legitimate PA matrix candidates. According to Section

V, there are $N_U = \binom{N_t}{L}$ legitimate PA matrix candidates $\mathbf{P}_u (u =$ 848
 849 $1, \dots, N_U)$, which can be obtained by using the method pro-
 850 posed in [29]. The complexity of computing each PA matrix is
 851 C_{PA} (Eq. (22) in [29]) flops. Hence, the associated complexity
 852 of the exhaustive-search based TAS&PA algorithm is $N_U C_{\text{PA}}$
 853 flops. By contrast, the low-complexity TAS&PA algorithm first
 854 selects the optimal TA subset and then calculates the PA matrix
 855 for the selected set. Hence, the associated complexity order of
 856 the low-complexity TAS&PA algorithm is $C_{\text{TAS}} + C_{\text{PA}}$ flops,
 857 where C_{TAS} is the complexity of the TAS algorithm employed,
 858 i. e. C_{EVM} or C_{PQRD} .

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IEEE PROOF

Transmit Antenna Selection for Multiple-Input Multiple-Output Spatial Modulation Systems

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Abstract—The benefits of transmit antenna selection (TAS) invoked for spatial modulation (SM) aided multiple-input multiple-output (MIMO) systems are investigated. Specifically, we commence with a brief review of the existing TAS algorithms and focus on the recently proposed Euclidean distance-based TAS (ED-TAS) schemes due to their high diversity gain. Then, a pair of novel ED-TAS algorithms, termed as the improved QR decomposition (QRD)-based TAS (QRD-TAS) and the error-vector magnitude-based TAS (EVM-TAS) are proposed, which exhibit an attractive system performance at low complexity. Moreover, the proposed ED-TAS algorithms are amalgamated with the low-complexity yet efficient power allocation (PA) technique, termed as TAS-PA, for the sake of further improving the system's performance. Our simulation results show that the proposed TAS-PA algorithms achieve signal-to-noise ratio (SNR) gains of up to 9 dB over the conventional TAS algorithms and up to 6 dB over the TAS-PA algorithm designed for spatial multiplexing systems.

Index Terms—Antenna selection, MIMO, power allocation, spatial modulation, link adaptation.

I. INTRODUCTION

SPATIAL modulation (SM) and its variants constitute a class of promising low-complexity and low-cost multiple-input multiple-output (MIMO) transmission techniques [1]–[5]. However, the conventional SM schemes only achieve receiver-diversity, but no transmit diversity [6]. To circumvent this impediment, recently some SM solutions have been proposed [7]–[11] on how to glean a beneficial transmit-diversity gain both with the aid of open-loop as well as closed-loop transmit-symbol design techniques.

As an attractive closed-loop regime, transmit antenna selection (TAS) constitutes a promising technique of providing a

high diversity potential as offered by the classic MIMO architectures. TAS has been lavishly researched in the context of spatial multiplexing systems [12]. As a new MIMO technique, SM can also be beneficially combined with TAS. Recently, several TAS algorithms have been conceived for the class of SM-MIMO systems with the goal of enhancing either its bit error rate (BER) or its capacity [13]–[20]. In [13], a norm-based TAS algorithm was proposed for providing diversity gain. In [14], a closed-form expression of the SM scheme's outage probability was derived for norm-based TAS. In [16], a two-stage TAS-based SM scheme was proposed for overcoming the specific constraint of SM, namely that the number of transmit antennas has to be a power of two. In [17], a novel TAS criterion was proposed for circumventing the detrimental effects of antenna correlation. In [18], the joint design of TAS and constellation breakdown was investigated and a graph-based search algorithm was proposed for reducing the search complexity imposed. In [19], a low-complexity TAS algorithm based on circle packing was proposed for a transmitter-optimized spatial modulation (TOSM) system, which trades off the spatial constellation size against the amplitude and phase modulation (APM) constellation size for improving the system's average bit error probability (ABEP). The adaptive TAS algorithm conceived for TOSM was further developed in [20], where a low-complexity two-stage optimization was proposed for selecting the best transmission mode.

More recently, the research of TAS-aided SM has been focused on the optimization of the Euclidean Distance (ED) of the received constellation points, since they achieve a high diversity gain at a moderate complexity compared to other TAS criteria [21]–[24]. Specifically, in [21] and [22] the ED-based TAS algorithm (ED-TAS) was compared to the signal-to-noise ratio (SNR)-optimized and capacity-optimized algorithms, and a low-complexity realization of ED-TAS, termed as the QR decomposition-based TAS (QRD-TAS) was proposed. The QRD-TAS algorithm constructs an ED-element matrix and exploits the QRD of the resultant matrix for reducing the imposed complexity. Moreover, in [24], the authors exploited the rotational symmetry of the APM adopted for the sake of reducing the complexity of QRD-TAS. Compared to directly optimizing the ED, in [23], Ntontin *et al.* proposed a low-complexity singular value decomposition-based TAS (SVD-TAS) algorithm for maximizing the lower bound of the ED. In [25], the complexity of SVD-TAS was reduced through an alternative computation of the singular value. In [26], the transmit diversity order of ED-TAS was quantified. In [27], the authors proposed several low-complexity TAS schemes relying

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84 on exploiting the channel's amplitude, the antenna correla-
 85 tion, the ED between transmit vectors and their combinations
 86 for selecting the optimal TA subset for the sake of improv-
 87 ing the system's reliability. However, as shown in [21]–[27],
 88 the QRD-TAS achieves an attractive BER performance at the
 89 cost of adopting high-complexity QRD operations, while the
 90 low-complexity SVD-TAS may suffer some performance loss.

91 On the other hand, power allocation (PA) is another promis-
 92 ing link adaptation technique for MIMO systems. Recently, PA
 93 has been extended to SM systems [28]–[31]. For example, in
 94 [28], an adaptive PA algorithm based on maximizing the min-
 95 imum ED was proposed, which is capable of improving the
 96 system's BER performance, while retaining all the single-RF
 97 benefits of SM. Subsequently, this attractive PA algorithm was
 98 further simplified in [29]. However, to the best of our knowl-
 99 edge, the potential benefits of TAS intrinsically amalgamated
 100 with PA have not been investigated in SM-MIMO systems.

101 Against this background, the contributions of this paper are:

- 102 1) We investigate the benefits of ED-TAS and propose a pair
 103 of novel ED-TAS schemes for SM-MIMO systems. In
 104 these schemes, we first classify the legitimate EDs into
 105 three specific subsets and then invoke a carefully designed
 106 upper bound as well as a set-reduction method for the
 107 most dominant set imposing a high complexity.
- 108 2) Specifically, we propose an improved QRD-TAS, where
 109 a tighter QRD-based lower bound of the ED is derived to
 110 replace the SVD-based bound of [23]. A low-complexity
 111 method is proposed for directly calculating the bound
 112 parameters, in order to avoid the high-complexity QRD
 113 or SVD operations of [21]–[24]. More importantly, com-
 114 pared to the conventional SVD-TAS of [25], the achieved
 115 QRD-based tighter bound can achieve a better BER
 116 performance.
- 117 3) Moreover, for striking a flexible tradeoff in terms of the
 118 BER attained and the complexity imposed, we propose
 119 an error-vector magnitude based TAS (EVM-TAS), which
 120 exploits the error vector selection probability to shrink
 121 the search space. The relevant optimization metrics of
 122 EVM-TAS are also derived for different PSK and QAM
 123 schemes.
- 124 4) Finally, we intrinsically amalgamate the proposed ED-
 125 TAS with the recently conceived PA technique of [29] for
 126 fully exploiting the MIMO channel's resources. A pair of
 127 different joint TAS-PA algorithms are conceived, which
 128 provide beneficial gains over both the conventional TAS
 129 algorithms and over the TAS-PA techniques designed for
 130 spatial multiplexing systems [32].

131 The organization of the paper is as follows. Section II intro-
 132 duces the system model of TAS-based SM, while Section III
 133 reviews the family of existing TAS algorithms designed for
 134 SM. In Section IV, we introduce the proposed QRD-TAS and
 135 EVM-TAS algorithms. In Section V, the joint design of the ED-
 136 TAS and PA algorithms is proposed. Then, we carry out their
 137 complexity analysis. Our simulation results and performance
 138 comparisons are presented in Section VI. Finally, Section VII
 139 concludes the paper.

140 *Notation:* $(\cdot)^*$, $(\cdot)^T$ and $(\cdot)^H$ denote conjugate, transpose, and
 141 Hermitian transpose, respectively. Furthermore, $\|\cdot\|_F$ stands

142 for the Frobenius norm. \mathbf{I}_b denotes a $(b \times b)$ -element iden-
 143 tity matrix and the operator $\text{diag}\{\cdot\}$ is the diagonal operator.
 144 $\Re\{\mathbf{x}\}$ and $\Im\{\mathbf{x}\}$ represent the real and imaginary parts of \mathbf{x} ,
 145 respectively.

146 II. SYSTEM MODEL

147 Consider a SM system having N_t transmit and N_r
 148 receive antennas, as depicted in Fig. 1. The frequency-
 149 flat quasi-static fading MIMO channel is represented
 150 by $\mathbf{H} = [\mathbf{h}(1), \mathbf{h}(2), \dots, \mathbf{h}(N_t)] \sim \mathcal{CN}(0, \mathbf{I}_{N_r \times N_t})$, where
 151 $\mathbf{h}(1), \mathbf{h}(2), \dots, \mathbf{h}(N_t)$ are the column vectors corresponding
 152 to each transmit antenna (TA) in \mathbf{H} . The receiver first selects
 153 L TAs according to a specific selection criterion. Then, the
 154 receiver sends this information to the transmitter via a feedback
 155 link. As shown in [23], let U_u denote the u th legitimate TA
 156 subset, where we have

$$\begin{aligned} U_1 &= \{1, 2, \dots, L\}, \\ U_2 &= \{1, 2, \dots, L-1, L+1\}, \\ &\vdots \\ U_{N_U} &= \{N_t - L + 1, \dots, N_t\}. \end{aligned} \quad (1)$$

157 In Eq. (1), there are $N_U = \binom{N_t}{L}$ possible TA subsets, each of
 158 which corresponds to an $(N_r \times L)$ -element MIMO channel. As
 159 shown in Fig. 1, $\mathbf{b} = [b_1, \dots, b_L]$ is the transmit bit vector in
 160 each time slot, which contains $m = \log_2(LM)$ bits, where M is
 161 the size of the APM constellation. In SM, the input vector \mathbf{b} is
 162 partitioned into two sub-vectors of $\log_2(L)$ and $\log_2(M)$ bits,
 163 denoted as \mathbf{b}_1 and \mathbf{b}_2 , respectively. The bits in \mathbf{b}_1 are used for
 164 selecting a unique TA index q for activation, while the bits of
 165 \mathbf{b}_2 are mapped to a Gray-coded APM symbol $s_l^q \in \mathcal{S}$. Then, the
 166 SM symbol $\mathbf{x} \in \mathbb{C}^{L \times 1}$ is formulated as

$$\mathbf{x} = s_l^q \mathbf{e}_q = [0, \dots, s_l^q, \dots, 0]^T, \quad (2)$$

167 where $\mathbf{e}_q (1 \leq q \leq L)$ is selected from the L -dimensional basis
 168 vectors (as exemplified by $\mathbf{e}_1 = [1, 0, \dots, 0]^T$). In the sce-
 169 nario that U_u is selected, the signal observed at the N_r receive
 170 antennas is given by

$$\mathbf{y} = \mathbf{H}_u \mathbf{x} + \mathbf{n}, \quad (3)$$

171 where \mathbf{H}_u is the $(N_r \times L)$ -element TAS matrix correspond-
 172 ing to the selected TA set U_u , and \mathbf{n} is the $(N_r \times 1)$ -element
 173 noise vector. The elements of the noise vector \mathbf{n} are complex
 174 Gaussian random variables obeying $\mathcal{CN}(0, N_0)$.

175 The receiver performs maximum-likelihood (ML) detection
 176 over all legitimate SM symbols $\mathbf{x} \in \mathbb{C}^{L \times 1}$ to obtain

$$\hat{\mathbf{x}} = \arg \min_{\mathbf{x} \in \mathbb{X}} \|\mathbf{y} - \mathbf{H}_u \mathbf{x}\|_F^2 = \arg \min_{\mathbf{x} \in \mathbb{X}} \|\mathbf{y} - \mathbf{h}_u(q) s_l^q\|_F^2, \quad (4)$$

177 where \mathbb{X} is the set of all legitimate transmit symbols and $\mathbf{h}_u(q)$
 178 is the q th column of the equivalent channel matrix \mathbf{H}_u . The
 179 complexity of the single-stream ML detection of Eq. (4) is low,
 180 since a single TA is activated during any time slot [34], [35].

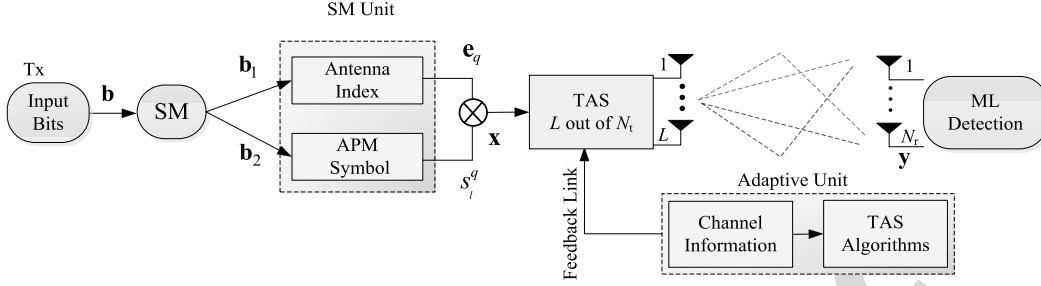


Fig. 1. The system model of the TAS-based SM system.

III. CONVENTIONAL TAS ALGORITHMS

This section offers a brief state-of-the-art review of the existing TAS algorithms proposed for SM systems.

A. The Maximum-Capacity and The Maximum-Norm Based TAS Algorithms

The capacity C_u of the SM-aided MIMO system depends on the classic transmitted signal s_i^q and the TA index signal \mathbf{e}_q . As shown in [21], [33], the capacity C_s relying on the signal s_i^q and the channel \mathbf{H}_u is lower bounded by

$$\alpha = \frac{1}{L} \sum_{i=1}^L \log_2(1 + \rho \|\mathbf{h}_u(i)\|_F^2) \leq C_s, \quad (5)$$

where $\mathbf{h}_u(i)$ is the i th column of \mathbf{H}_u and ρ is the average SNR at the receiver. Moreover, the capacity C_{TA} relying on the signal \mathbf{e}_q is bounded by $C_{TA} \leq \log_2(L)$ [33]. It is proved in [33] that the total capacity $C_u = C_{TA} + C_s$ is bounded by

$$\alpha \leq C_u \leq \alpha + \log_2(L), \quad (6)$$

Based on the bound of Eq. (6), a maximum-capacity based TAS algorithm was formulated in [21] as

$$\mathbf{H}_{\hat{u}} = \arg \max_{u \in \{1, \dots, N_U\}} \alpha. \quad (7)$$

Based on Eq. (5), the optimization objective α of Eq. (7) is maximized by selecting the L TAs associated with the largest channel norms out of the N_t TAs, which is equivalent to the maximum-norm based TAS [13] given by

$$\mathbf{H}_{\hat{u}} = \arg \max_{u \in \{1, \dots, N_U\}} \|\mathbf{H}_u\|_F^2. \quad (8)$$

B. The Exhaustive Max- d_{\min} Based ED-TAS

In order to improve the BER performance of SM, the free distance (FD) d_{\min} was optimized in [21]. For a given channel \mathbf{H}_u , its FD can be formulated as

$$\begin{aligned} d_{\min}(\mathbf{H}_u) &= \min_{\substack{\mathbf{x}_i, \mathbf{x}_j \in \mathbb{X} \\ \mathbf{x}_i \neq \mathbf{x}_j}} \|\mathbf{H}_u(\mathbf{x}_i - \mathbf{x}_j)\|_F^2 \\ &= \min_{\mathbf{e}_{ij} \in \mathbb{E}} \|\mathbf{H}_u \mathbf{e}_{ij}\|_F^2 = \min_{\mathbf{e}_{ij} \in \mathbb{E}} \mathbf{e}_{ij}^H \mathbf{H}_u^H \mathbf{H}_u \mathbf{e}_{ij}, \end{aligned} \quad (9)$$

where we have the error vector $\mathbf{e}_{ij} = \mathbf{x}_i - \mathbf{x}_j$, $\mathbf{x}_i, \mathbf{x}_j \in \mathbb{X}$. In [21], the max- d_{\min} aided ED-TAS algorithm is defined as

$$\mathbf{H}_{\hat{u}} = \arg \max_{u \in \{1, \dots, N_U\}} d_{\min}(\mathbf{H}_u). \quad (10)$$

The optimum solution obeying the objective function of Eq. (10) can be found by an exhaustive search over all possible $\binom{N_t}{L}$ candidate channel matrices and all the different error vectors, which imposes a complexity order of $\mathcal{O}(N_t^2 M^2)$. This results in an excessive complexity, when high data rates are required.

C. The Conventional QRD-Based ED-TAS

In order to reduce the complexity of the exhaustive ED-TAS of Eq. (10), in [21] an ED-TAS based on an equivalent decision metric $\mathbf{D}(u)$ was formulated as:

$$\mathbf{H}_{\hat{u}} = \arg \max_{u \in \{1, \dots, N_U\}} \{\min[\mathbf{D}(u)]\}, \quad (11)$$

where $\mathbf{D}(u)$ is an $(L \times L)$ -element sub-matrix of an upper triangular $(N_t \times N_t)$ -element matrix \mathbf{D} obtained by deleting the specific rows and columns that are absent in u , while $\min[\mathbf{D}(u)]$ is the minimum non-zero value of $\mathbf{D}(u)$. Here, the (i, j) -th element of \mathbf{D} can be expressed as

$$\begin{aligned} \mathbf{D}_{ij} &= \min_{s_1, s_2 \in \mathbb{S}} \|\mathbf{H}(s_1 \mathbf{e}_i - s_2 \mathbf{e}_j)\|_F^2 \\ &= \min_{s_1, s_2 \in \mathbb{S}} \|\mathbf{h}(i)s_1 - \mathbf{h}(j)s_2\|_F^2, \end{aligned} \quad (12)$$

where s_1 and s_2 are M -ary APM constellation points, while $\mathbf{h}(i)$ and $\mathbf{h}(j)$ are the i th and j th columns of \mathbf{H} . Provided that we have $i = j$ in Eq. (12), the corresponding element becomes $\mathbf{D}_{ii} = \min_{s_1, s_2 \in \mathbb{S}} (\|\mathbf{h}(i)\|_F^2 |s_1 - s_2|^2) =$

$d_{\min}^{\text{APM}} \|\mathbf{h}(i)\|_F^2$, where d_{\min}^{APM} is the minimum distance of the APM constellation. For the case of $i \neq j$, \mathbf{D}_{ij} is re-formulated in the real-valued representation of the QRD as

$$\mathbf{D}_{ij} = \min_{\substack{s_{1I}, s_{2I} \in \mathcal{R}\{\mathbb{S}\}, \\ s_{1Q}, s_{2Q} \in \mathcal{I}\{\mathbb{S}\}}} \|\mathbf{R}[s_{1I}, s_{1Q}, -s_{2I}, -s_{2Q}]\|_F^2, \quad (13)$$

where we have $s_{nI} = \mathcal{R}\{s_n\}$ and $s_{nQ} = \mathcal{I}\{s_n\}$ for $n = 1, 2$, while \mathbf{R} is a (4×4) -element upper triangular matrix created by the QRD of the resultant channel matrix [21]. As shown in [21], the complexity order of this QRD-TAS is $\mathcal{O}(N_t^2 M)$, which

increases only linearly with the modulation order M . In [22] and [24], both the modulus and the symbol set symmetry of the APM constellations were exploited for further reducing the complexity of this algorithm.

D. The Conventional SVD-Based ED-TAS

Although the QRD-based ED-TAS of Eq. (13) is capable of finding the optimal solution, its complexity imposed is a function of the modulation order M . Moreover, the high-complexity QRD has to be applied to the $(2N_r \times 4)$ -element channel matrices [21], [22], [24]. Hence, the complexity of this TAS remains high. This problem was circumvented in [23], where the ED was classified into three categories as follows

$$d_{\min}(\mathbf{H}_u) = \min \left\{ d_{\min}^{\text{signal}}, d_{\min}^{\text{spatial}}, d_{\min}^{\text{joint}} \right\}, \quad (14)$$

where we have

$$\begin{aligned} d_{\min}^{\text{signal}} &= \min_{i=1, \dots, L} \|\mathbf{h}_u(i)\|_F^2 \min_{s_a \neq s_b \in \mathbb{S}} |s_a - s_b|^2 \\ &= d_{\min}^{\text{APM}} \min_{i=1, \dots, L} \|\mathbf{h}_u(i)\|_F^2, \end{aligned} \quad (15)$$

$$\begin{aligned} d_{\min}^{\text{spatial}} &= \min_{\substack{i, j=1, \dots, L \\ i \neq j}} \|\mathbf{h}_u(i) - \mathbf{h}_u(j)\|_F^2 \min_{s_l \in \mathbb{S}} |s_l|^2 \\ &= d_{\min}^{\text{Modulus}} \min_{\substack{i, j=1, \dots, L \\ i \neq j}} \|\mathbf{h}_u(i) - \mathbf{h}_u(j)\|_F^2, \end{aligned} \quad (16)$$

$$d_{\min}^{\text{joint}} = \min_{\substack{i, j=1, \dots, L, i \neq j \\ s_a, s_b \in \mathbb{S}, a \neq b}} \|\mathbf{h}_u(i)s_a - \mathbf{h}_u(j)s_b\|_F^2. \quad (17)$$

In Eq. (16), the term $d_{\min}^{\text{Modulus}} = \min_{s_l \in \mathbb{S}} |s_l|^2$ is the minimum squared modulus value of the APM constellation. Since the calculations of d_{\min}^{signal} and $d_{\min}^{\text{spatial}}$ in Eqs. (15) and (16) do not depend on the size of APM constellation and the corresponding complexity is low, the complexity of computing the FD of Eq. (14) is dominated by the computation of d_{\min}^{joint} in Eq. (17). To reduce this complexity, in [23] the Rayleigh-Ritz theorem was utilized for driving a lower bound of d_{\min}^{joint} as

$$\begin{aligned} d_{\min}^{\text{joint}} &= \min_{\substack{i, j=1, \dots, L, i \neq j \\ s_a, s_b \in \mathbb{S}, a \neq b}} \left\| [\mathbf{h}_u(i), -\mathbf{h}_u(j)] [s_a, s_b]^T \right\|_F^2 \\ &\geq d_{\min}^{\text{SVD-bound}} \\ &= \min_{i, j=1, \dots, L, i \neq j} \lambda_{\min}^2(\mathbf{H}_{u,ij}) \min_{s_a, s_b \in \mathbb{S}} \left\| [s_a, s_b]^T \right\|_F^2 \\ &= \min_{i, j=1, \dots, L, i \neq j} \lambda_{\min}^2(\mathbf{H}_{u,ij}) d_{\min}^{\text{all}} \end{aligned} \quad (18)$$

where we have $d_{\min}^{\text{all}} = \min_{s_a, s_b \in \mathbb{S}} \left\| [s_a, s_b]^T \right\|_F^2$ and $\mathbf{H}_{u,ij} = [\mathbf{h}_u(i), -\mathbf{h}_u(j)]$ is an $(N_r \times 2)$ -element matrix. Here, $\lambda_{\min}^2(\mathbf{H}_{u,ij})$ is the minimum squared singular value of the submatrix $\mathbf{H}_{u,ij}$. Upon exploiting Eq. (18), the distance $d_{\min}(\mathbf{H}_u)$ of Eq. (14) is bounded by

$$d_{\min}^{\text{SVD}}(\mathbf{H}_u) = \min \{ d_{\min}^{\text{signal}}, d_{\min}^{\text{spatial}}, d_{\min}^{\text{SVD-bound}} \}. \quad (19)$$

Based on Eq. (19), the SVD-TAS algorithm is given by

$$\mathbf{H}_{\hat{u}} = \arg \max_{u \in \{1, \dots, N_U\}} d_{\min}^{\text{SVD}}(\mathbf{H}_u). \quad (20)$$

Compared to the conventional QRD-based TAS, this bound-aided algorithm has the following advantages:

- Using the SVD-based bound of Eq. (18), the calculation of the distance d_{\min}^{joint} is independent of the APM modulation order;
- Moreover, the SVD operation of Eq. (18) is performed on the smaller channel matrices of size $(N_r \times 2)$ compared to the QRD-based ED-TAS, which is performed on $(2N_r \times 4)$ -element matrices. In [25], the complexity of SVD-TAS [23] was further reduced through an alternative computation of the singular value.

IV. THE PROPOSED LOW-COMPLEXITY ED-TAS

As shown in subsection III, the conventional QRD-based ED-TAS is capable of achieving the optimal BER, but it imposes high complexity. In contrast, the SVD-based ED-TAS imposes a lower complexity at the cost of a BER performance degradation, because the derived bound may be loose and the corresponding TAS results may be suboptimal.

To circumvent this problem, in this section, a pair of ED-TAS algorithms are proposed. Specifically, an improved QRD-TAS is proposed, where a tighter QRD-based lower bound of the ED is found for replacing the SVD-based bound of [23], while the sparse nature¹ of the error vectors of SM is exploited to avoid the full-dimensional QRD operation. Then, for striking a further flexible BER vs complexity tradeoff, we propose an EVM-based ED-TAS algorithm, which exploits the error vector selection probability to shrink the search space.

A. The Proposed QRD-Based ED-TAS

1) *The QRD-Based Bounds:* To evaluate the value of d_{\min}^{joint} more accurately, in this paper, we apply the QRD-based bound to replace the SVD-bound of Eq. (18). Specifically, the submatrix $\mathbf{H}_{u,ij}$ of Eq. (18) is first subjected to the QRD [38], yielding $\mathbf{H}_{u,ij} = \tilde{\mathbf{Q}}\tilde{\mathbf{R}}$, where $\tilde{\mathbf{Q}}$ is an $(N_r \times 2)$ column-wise orthonormal matrix and $\tilde{\mathbf{R}}$ is a (2×2) upper triangular matrix with positive real-valued diagonal entries formulated as

$$\tilde{\mathbf{R}} = \begin{bmatrix} \tilde{R}_{1,1} & \tilde{R}_{1,2} \\ 0 & \tilde{R}_{2,2} \end{bmatrix}. \quad (21)$$

Let $[\tilde{\mathbf{R}}]_k = \tilde{R}_{k,k}$ denote the k th diagonal entry of $\tilde{\mathbf{R}}$. Based on this decomposition, another lower bound of the distance d_{\min}^{joint} in Eq. (18) can be formulated as

$$\begin{aligned} d_{\min}^{\text{joint}} &\geq d_{\min}^{\text{QRD-bound}} \\ &= \min_{i, j=1, \dots, L, i \neq j} \{ [\tilde{\mathbf{R}}]_{\min}^2 \} \min_{s_a \neq s_b \in \mathbb{S}} \left\| [s_a, s_b]^T \right\|_F^2, \\ &= \min_{i, j=1, \dots, L, i \neq j} \{ [\tilde{\mathbf{R}}]_{\min}^2 \} d_{\min}^{\text{all}} \end{aligned} \quad (22)$$

¹In SM, the transmit vector \mathbf{x} only has a single non-zero element, hence the number of non-zero elements of the error vectors \mathbf{e}_{ij} of SM is no more than 2.

297 where $[\tilde{\mathbf{R}}]_{\min}^2$ is the minimum squared nonzero diagonal entry
 298 of the upper matrix $\tilde{\mathbf{R}}$, given by

$$[\tilde{\mathbf{R}}]_{\min} = \min\{\tilde{R}_{1,1}, \tilde{R}_{2,2}\}. \quad (23)$$

299 *Lemma 1:* For an $(N_r \times 2)$ -element full column-rank matrix
 300 $\mathbf{H}_{u,ij}$ associated with its minimum squared singular non-zero
 301 value $\lambda_{\min}^2(\mathbf{H}_{u,ij})$ for SVD and its minimum squared diago-
 302 nal non-zero entry $[\tilde{\mathbf{R}}]_{\min}^2$ of $\tilde{\mathbf{R}}$ for QRD, respectively, the
 303 inequality $[\tilde{\mathbf{R}}]_{\min}^2 \geq \lambda_{\min}^2(\mathbf{H}_{u,ij})$ is satisfied.

304 According to the analysis process in Section III of [38], the
 305 formulation of Lemma 1 is straightforward. As a result, the
 306 lower bound of Eq. (22) achieved by the QRD is tighter than
 307 that of the SVD algorithm in Eq. (18).

308 To derive an even tighter upper QRD bound than that of
 309 Eq. (22), the permutation matrix $\mathbf{\Pi}_m$ can be invoked for
 310 calculating d_{\min}^{joint} of Eq. (22) as

$$d_{\min}^{\text{joint}} = \min_{\substack{i,j=1,\dots,L, \\ i \neq j, s_a, s_b \in \mathcal{S}}} \left\| [\mathbf{h}_u(i), -\mathbf{h}_u(j)] \mathbf{\Pi}_m \mathbf{\Pi}_m^{-1} [s_a, s_b]^T \right\|_F^2, \quad (24)$$

311 where $\mathbf{\Pi}_m$ is an orthogonal matrix satisfying $\mathbf{\Pi}_m^{-1} = \mathbf{\Pi}_m^T$.
 312 Since the size of the channel matrix $\mathbf{H}_{u,ij} = [\mathbf{h}_u(i), -\mathbf{h}_u(j)]$
 313 is $N_r \times 2$, we only have two legitimate permutation matrices
 314 $\mathbf{\Pi}_m \in \mathbb{C}^{2 \times 2}$, $m = 1, 2$, namely

$$\mathbf{\Pi}_1 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \text{ and } \mathbf{\Pi}_2 = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}. \quad (25)$$

315 For each matrix $\mathbf{\Pi}_m$, similar to Eq. (22), the corresponding
 316 QRD-based bound is

$$\begin{aligned} d_{\min}^{\text{joint}} &\geq \min_{i,j=1,\dots,L, i \neq j} \left\{ [\tilde{\mathbf{R}}_m]_{\min}^2 \right\} \min_{s_a, s_b \in \mathcal{S}} \left\| \mathbf{\Pi}_m^T [s_a, s_b]^T \right\|_F^2 \\ &= [\tilde{\mathbf{R}}_m]_{\min}^2 d_{\min}^{\text{all}}, \end{aligned} \quad (26)$$

317 where $\tilde{\mathbf{R}}_m$ is the upper triangular part of the QRD of
 318 the equivalent matrix $\mathbf{H}_{u,ij} \mathbf{\Pi}_m$. Note in Eq. (26) that
 319 the permutation matrix does not change the distance
 320 of $\left\| \mathbf{\Pi}_m^T [s_a, s_b]^T \right\|_F^2$ and we have $\min_{s_a, s_b \in \mathcal{S}} \left\| \mathbf{\Pi}_m^T [s_a, s_b]^T \right\|_F^2 =$

321 $\min_{s_a, s_b \in \mathcal{S}} \left\| [s_a, s_b]^T \right\|_F^2 = d_{\min}^{\text{all}}$. For the permutation matrices given
 322 in Eq. (25), we can obtain two different values $[\tilde{\mathbf{R}}_m]_{\min}$,
 323 ($m = 1, 2$), which are given by $[\tilde{\mathbf{R}}_1]_{\min} = \min\{\tilde{R}_{1,1}(\mathbf{\Pi}_1),$
 324 $\tilde{R}_{2,2}(\mathbf{\Pi}_1)\}$ and $[\tilde{\mathbf{R}}_2]_{\min} = \min\{\tilde{R}_{1,1}(\mathbf{\Pi}_2), \tilde{R}_{2,2}(\mathbf{\Pi}_2)\}$. Here,
 325 $\tilde{R}_{1,1}(\mathbf{\Pi}_m)$ and $\tilde{R}_{2,2}(\mathbf{\Pi}_m)$, $m = 1, 2$ are the diagonal elements
 326 of $\tilde{\mathbf{R}}_m$.

327 *Remark:* The bound of Eq. (22) constitutes a special case of
 328 the bound of Eq. (26), which can be obtained by setting $m = 1$.

329 Based on Eq. (26), an improved QRD-based upper bound of
 330 the distance d_{\min}^{joint} is given by

$$\begin{aligned} d_{\min}^{\text{joint}} &\geq d_{\min}^{\text{QRD-bound}_P} \\ &= \min_{i,j=1,\dots,L, i \neq j} \{ [\tilde{\mathbf{R}}_{\text{QRQ-P}}]_{\min}^2 \} d_{\min}^{\text{all}}. \end{aligned} \quad (27)$$

where we have $[\tilde{\mathbf{R}}_{\text{QRQ-P}}]_{\min}^2 = \max\{[\tilde{\mathbf{R}}_1]_{\min}^2, [\tilde{\mathbf{R}}_2]_{\min}^2\}$. 331

Lemma 2: For an $(N_r \times 2)$ -element full column-rank 332
 matrix $\mathbf{H}_{u,ij}$ having a minimum squared diagonal non-zero 333
 entry $[\tilde{\mathbf{R}}]_{\min}^2$ for its QRD and a value of $[\tilde{\mathbf{R}}_{\text{QRQ-P}}]_{\min}^2 =$ 334
 $\max\{[\tilde{\mathbf{R}}_1]_{\min}^2, [\tilde{\mathbf{R}}_2]_{\min}^2\}$ based on the pair of legitimate permuta- 335
 tion matrices $\mathbf{\Pi}_m \in \mathbb{C}^{2 \times 2}$, $m = 1, 2$, respectively, the inequal- 336
 ity $[\tilde{\mathbf{R}}_{\text{QRQ-P}}]_{\min}^2 \geq [\tilde{\mathbf{R}}]_{\min}^2$ is satisfied. 337

Since we have $[\tilde{\mathbf{R}}]_{\min}^2 = [\tilde{\mathbf{R}}_1]_{\min}^2$, Lemma 2 can be obtained. 338

2) *The Proposed QRD-Based ED-TAS:* According to 339
 Lemma 2, the QRD bound of Eq. (27) is tighter than that 340
 of Eq. (22). Hence, we use this tighter bound to derive the 341
 proposed QRD-based ED-TAS as 342

$$\hat{\mathbf{H}}_u = \arg \max_{u \in \{1, \dots, N_U\}} \left\{ d_{\min}^{\text{signal}}, d_{\min}^{\text{spatial}}, d_{\min}^{\text{QRD-bound}_P} \right\}. \quad (28)$$

Note that the complexity of the QRD-based TAS is domi- 343
 nated by the computation of $[\tilde{\mathbf{R}}_m]_{\min}$. In general, the full QRD 344
 can be adopted in Eq. (26) for solving Eq. (27). However, this 345
 may impose a high complexity. In order to reduce this com- 346
 plexity, for a fixed channel $\mathbf{H}_{u,ij}$, we found that the value of 347
 $[\tilde{\mathbf{R}}_m]_{\min}$ only depends on the diagonal entries of $\tilde{\mathbf{R}}_m$, namely 348
 $\tilde{R}_{k,k}(\mathbf{\Pi}_m)$ ($k = 1, 2$), which can be directly calculated as [38] 349

$$[\tilde{\mathbf{R}}_m]_k = \tilde{R}_{k,k}(\mathbf{\Pi}_m) = \sqrt{\frac{\det[(\mathbf{G}(1:k))^H \mathbf{G}(1:k)]}{\det[(\mathbf{G}(1:k-1))^H \mathbf{G}(1:k-1)]}}, \quad (29)$$

where $\mathbf{G}(1:k)$ denotes a matrix consisting of the first k 350
 columns of $\mathbf{H}_{u,ij} \mathbf{\Pi}_m$. In the classic V-BLAST systems, the cal- 351
 culation of Eq. (29) suffers from the problem of having a high 352
 complexity [38]. In SM, the number of non-zero elements of 353
 the error vectors of SM is up to 2. This sparse character leads 354
 to the simple sub-matrix $\mathbf{H}_{u,ij} = [\mathbf{h}_u(i), -\mathbf{h}_u(j)] \in \mathbb{C}^{N_r \times 2}$ and 355
 hence the values of $\tilde{R}_{k,k}(\mathbf{\Pi}_m)$ ($m = 1, 2, k = 1, 2$) are given by 356

$$\tilde{R}_{1,1}(\mathbf{\Pi}_1) = \sqrt{\|\mathbf{h}_u(i)\|_F^2}, \quad (30)$$

$$\tilde{R}_{2,2}(\mathbf{\Pi}_1) = \sqrt{\frac{\|\mathbf{h}_u(i)\|_F^2 + \|\mathbf{h}_u(j)\|_F^2 - 2\Re\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\}}{\|\mathbf{h}_u(i)\|_F^2}} \quad (31)$$

$$\tilde{R}_{1,1}(\mathbf{\Pi}_2) = \sqrt{\|\mathbf{h}_u(j)\|_F^2} \quad (32)$$

and 357

$$\tilde{R}_{2,2}(\mathbf{\Pi}_2) = \sqrt{\frac{\|\mathbf{h}_u(i)\|_F^2 + \|\mathbf{h}_u(j)\|_F^2 - 2\Re\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\}}{\|\mathbf{h}_u(j)\|_F^2}} \quad (33)$$

The complexity of our proposed QRD-TAS of Eq. (28) 358
 is dominated by the computation of $\tilde{R}_{k,k}(\mathbf{\Pi}_m)$, $m = 1, 2$. In 359
 SM, these values only depend on the values of $\|\mathbf{h}_u(i)\|_F^2$, 360
 $\|\mathbf{h}_u(j)\|_F^2$ and $\mathbf{h}_u(i)^H \mathbf{h}_u(j)$, which are elements of the matrix 361
 $\mathbf{H}^H \mathbf{H}$, as shown in Eqs. (30)-(33). Based on this observa- 362
 tion, we can calculate the values of $\tilde{R}_{k,k}(\mathbf{\Pi}_m)$, $m = 1, 2$ by 363
 reusing these elements for the different TAS candidates \mathbf{H}_u , 364

TABLE I
COMPLEXITY COMPARISON OF DIFFERENT TAS ALGORITHMS FOR SM SYSTEMS

TAS algorithm	ED Optimality	Computational complexity
Exhaustive ED-TAS [13]	optimal	$\frac{N_t(N_t-1)}{2}(5N_r-1)M^2$
Maximum-norm based TAS of [21]	sub-optimal	$2N_tN_r - N_t$
Minimum-correlation based TAS of [15]	sub-optimal	$2N_t^2N_r - N_t^2 + \frac{3}{2}N_t(N_t-1)$
Conventional QRD-based ED-TAS of [24]	optimal	$2N_tN_r - N_t + 32N_t(N_t-1)(N_r - \frac{2}{3})\frac{M}{N_{APM}}$ ($N_{APM}=M$ for PSK, $N_{APM}=4$ for QAM)
Conventional SVD-based ED-TAS of [23]	sub-optimal	$2N_tN_r - N_t + \frac{19}{2}N_t(N_t-1)(N_r - \frac{1}{3})$
Simplified SVD-TAS [25]	sub-optimal	$\frac{N_t(N_t-1)}{2}(2N_r+11) + N_t(2N_r-1)$
Proposed QRD-based ED-TAS	sub-optimal	$2N_t^2N_r + \frac{3}{2}N_t(N_t-1)$
Proposed EVM-based ED-TAS	M -PSK: optimal	$2N_t^2N_r - N_t^2 + \frac{1}{2}N_t(N_t-1)(M+7)$
	M -QAM: sub-optimal, $K < v$ optimal, $K = v$	$2N_t^2N_r - N_t^2 + \frac{15}{2}GN_t(N_t-1)$
Exhaustive TAS&PA	—	$\binom{N_t}{L}C_{PA}$
Low-complexity TAS&PA	—	$C_{TAS} + C_{PA} = \begin{cases} C_{PQRD} + C_{PA} \\ C_{EVM} + C_{PA} \end{cases}$

365 hence the resultant complexity is considerably reduced compared to the conventional QRD-based ED-TAS, as will show in
366 Table I.
367

368 To confirm the benefits of the QRD-based bound derived in
369 Eq. (27), Fig. 2 shows the BER performance of the proposed
370 QRD-based ED-TAS algorithm in contrast to the existing SVD-
371 based ED-TAS of [23]. Moreover, we add the performance
372 of the norm-based TAS of [13] and of the exhaustive-search
373 based optimal ED-TAS of [21] as benchmarks. In Fig. 2, the
374 number of TAs is set to $N_t = 4$, where $L = 2$ out of $N_t =$
375 4 TAs were selected in these TAS algorithms. As expected,
376 since the proposed QRD-based ED-TAS has a tighter bound,
377 in Fig. 2 it performs better than the SVD-based ED-TAS.
378 Quantitatively, observe in Fig. 2 that this scheme provides an
379 SNR gain of about 1.2 dB over the SVD-based ED-TAS at
380 the BER of 10^{-5} . In Fig. 2, we also observe that the QRD-
381 based ED-TAS achieves a near-optimum performance, where
382 the performance gap between the proposed QRD-based ED-
383 TAS and the exhaustive-search-based optimal ED-TAS is only
384 about 0.2 dB. We will provide more detailed comparisons about
385 the BER and the complexity issues in Section VI.

386 B. The Proposed EVM-Based ED-TAS

387 In this section, for striking a further flexible tradeoff in terms
388 of the BER attained and the complexity imposed, we propose
389 an EVM-based ED-TAS algorithm. The proposed EVM-TAS
390 directly calculates the value of $d_{\min}(\mathbf{H}_u)$ for the specific TAS
391 candidate \mathbf{H}_u , rather than exploiting the equivalent decision
392 metric of Eq. (13) or the estimated bound of (18). Specifically,
393 we will derive simple optimization metrics for both PSK and
394 QAM constellations, where the error-vector selection probabil-
395 ity is exploited for reducing the search space.

396 1) *The Calculation of $d_{\min}(\mathbf{H}_u)$ in EVM-Based ED-TAS:*
397 Specifically, the M -PSK constellation can be expressed as
398 $\mathcal{S}_{PSK} = \{e^{j\frac{2m\pi}{M}}, m = 0, \dots, M-1\}$, and the symbols of the
399 rectangular $M = 4^k$ QAM constellation belong to the set
400 of [36]

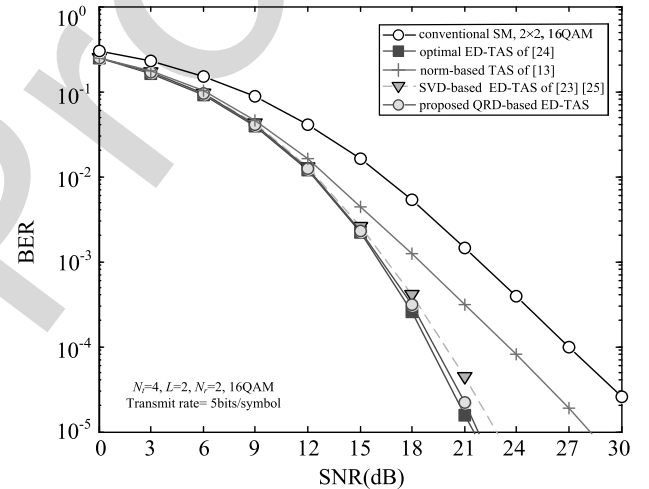


Fig. 2. BER performance comparison of the existing TAS algorithms and the proposed QRD-based ED-TAS algorithm. The setup of the simulation is based on $N_t = 4$, $N_r = 2$, $L = 2$ and 16-QAM. The transmit rate is 5 bits/symbol.

$$\mathcal{S}_{QAM} = \frac{1}{\sqrt{\beta_k}}\{a + bj, a - bj, -a + bj, -a - bj\}, \quad (34)$$

where we have $\beta_k = \frac{2}{3}(4^k - 1)$ and $a, b \in \{1, 3, \dots, 2^k - 1\}$.
401 Similar to Eq. (14), the calculation of $d_{\min}(\mathbf{H}_u)$ is parti-
402 tioned into three cases: d_{\min}^{signal} , $d_{\min}^{\text{spatial}}$ and d_{\min}^{joint} . As shown in
403 Eqs. (15)-(16), d_{\min}^{signal} depends the minimum distance of the
404 APM d_{\min}^{APM} as [39]
405

$$d_{\min}^{\text{APM}} = \begin{cases} 4 \sin^2(\pi/M) & \text{for } M - \text{PSK} \\ \frac{4}{\beta_k} & \text{for } M - \text{QAM} \end{cases}, \quad (35)$$

while $d_{\min}^{\text{spatial}}$ relies on the minimum squared modulus value
406 $d_{\min}^{\text{Modulus}}$ of the APM constellation as
407

$$d_{\min}^{\text{Modulus}} = \begin{cases} 1 & \text{for } M - \text{PSK} \\ \frac{2}{\beta_k} & \text{for } M - \text{QAM} \end{cases}. \quad (36)$$

408 Based on Eqs. (35) and (36), the complexity of computing the
 409 values of d_{\min}^{signal} and $d_{\min}^{\text{spatial}}$ in Eqs. (15)-(16) may be deemed
 410 negligible. Hence, we only have to reduce the complexity of
 411 computing d_{\min}^{joint} , which can be achieved as follows:

$$\begin{aligned} d_{\min}^{\text{joint-EVM}} &= \min_{\substack{i,j=1,\dots,L,i\neq j \\ s_a, s_b \in \mathbb{S}}} \|\mathbf{h}_u(i)s_a - \mathbf{h}_u(j)s_b\|_F^2 \\ &= \min_{\substack{i,j=1,\dots,L, \\ i\neq j, s_a, s_b \in \mathbb{S}}} |s_a|^2 \|\mathbf{h}_u(i)\|_F^2 + |s_b|^2 \|\mathbf{h}_u(j)\|_F^2 - 2m_{\text{APM}}, \end{aligned} \quad (37)$$

412 where we have $m_{\text{APM}} = \mathcal{R}\{s_a^H s_b \mathbf{h}_u(i)^H \mathbf{h}_u(j)\}$, which relies on
 413 the specific APM scheme adopted. Next, we will derive the sim-
 414 plified metrics $d_{\min}^{\text{joint-EVM}}$ for the general family of M -PSK and
 415 M -QAM modulated SM systems.

416 2) *Simplification for M-PSK Schemes:* For a pair of
 417 M -PSK symbols $s_a = e^{j\frac{2a\pi}{M}}$ and $s_b = e^{j\frac{2b\pi}{M}}$, the possible values
 418 of $s_a^H s_b$ obey $e^{j\frac{2(b-a)\pi}{M}}$, $(b-a) \in \{-(M-1), \dots, (M-1)\}$.
 419 As a result, m_{APM} of the general M -PSK scheme obeys:

$$m_{\text{APM}} \in \{\mathcal{R}\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\} \cos \theta_n - \mathcal{J}\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\} \sin \theta_n\}, \quad (38)$$

420 where $\theta_n = \frac{2n\pi}{M}$, $n = -(M-1), \dots, (M-1)$. Since the mini-
 421 mum ED is considered in Eq (37), only the maximum value
 422 of m_{APM} needs to be considered, which is given by Eq. (39),
 423 shown at the bottom of the page. As shown in Eq. (39), the num-
 424 ber of possible θ_n values is reduced from $2M-1$ to $\frac{M}{4}+1$.
 425 According to Eq. (39), $|s_a|^2 = 1$ and $|s_b|^2 = 1$, the distance
 426 $d_{\min}^{\text{joint-EVM}}$ of Eq. (37) is simplified for M -PSK as follows:

$$d_{\min}^{\text{joint-EVM}} = \min_{\substack{i,j=1,\dots,L, \\ i\neq j}} \|\mathbf{h}_u(i)\|_F^2 + \|\mathbf{h}_u(j)\|_F^2 - 2m_{M\text{-PSK}}(\mathbf{H}_u). \quad (40)$$

427 *Example:* The constellation points s_a and s_b of
 428 BPSK and QPSK modulation schemes belong to the
 429 set $\mathbb{S}_{\text{BPSK}} = \{\pm 1\}$ and $\mathbb{S}_{\text{QPSK}} = \{\pm 1, \pm j\}$, respec-
 430 tively. Based on Eq. (39), the corresponding optimized
 431 metrics $m_{M\text{-PSK}}(\mathbf{H}_u) = \max m_{\text{APM}}$ are simplified to
 432 $m_{2\text{-PSK}}(\mathbf{H}_u) = |\mathcal{R}\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\}|$ and $m_{4\text{-PSK}}(\mathbf{H}_u) =$
 433 $\max\{|\mathcal{R}\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\}|, |\mathcal{J}\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\}|\}$, respectively.

434 As shown in Eqs. (37)-(40), since we have $|s_a|^2 = 1$, $|s_b|^2 =$
 435 1 and a reduced set $s_a^H s_b$ for M -PSK constellation, the com-
 436 plexity of calculating $d_{\min}^{\text{joint-EVM}}$ is low, as it will be shown in
 437 Table I.

438 3) *Simplification for M-QAM Schemes:* When M -QAM
 439 constellations are considered, the calculation of $d_{\min}^{\text{joint-EVM}}$ in
 440 Eq. (37) becomes substantially complicated, because there are
 441 many combinations of the values of $|s_a|^2$, $|s_b|^2$ and $s_a^H s_b$ in
 442 Eq. (37), which lead to different received SM-symbol distances.
 443 To derive a simplified optimized metrics for M -QAM, we first
 444 introduce the following Lemma.

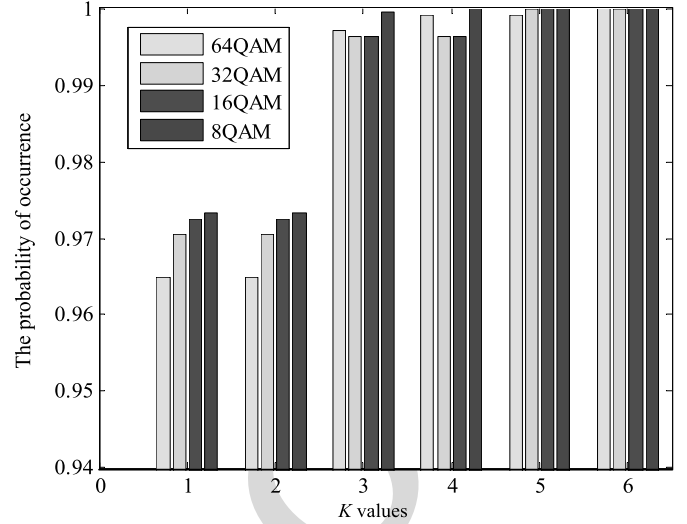


Fig. 3. The statistical probability of the norm error vectors relying on K minimum moduli, yielding the optimal ED-TAS solution, where the system setup is $N_t = 4$, $N_r = 2$ and $L = 2$.

445 *Lemma 3:* It is highly likely that an error vector associated
 446 with a small norm value yields the FD value of Eq. (9). Thus,
 447 the search space to be evaluated for finding the FD can be
 448 reduced to a few dominant error vectors having small norm
 449 values.

450 *Proof:* Based on the Rayleigh-Ritz theorem of [37], for
 451 a fixed channel matrix $\mathbf{H}_{u,ij}$ and a given error vector \mathbf{e}_{ij} ,
 452 the distance amongst the received symbols is bounded by
 453 $\lambda_{\max}^2(\mathbf{H}_{u,ij}) \|\mathbf{e}_{ij}\|^2 \geq \|\mathbf{H}_u \mathbf{e}_{ij}\|^2 \geq \lambda_{\min}^2(\mathbf{H}_{u,ij}) \|\mathbf{e}_{ij}\|^2$, where
 454 $\lambda_{\max}^2(\mathbf{H}_{u,ij})$ is the maximum squared singular value of the sub-
 455 matrix $\mathbf{H}_{u,ij} = [\mathbf{h}_u(i), -\mathbf{h}_u(j)]$. It may be readily shown that
 456 the values of $\lambda_{\max}^2(\mathbf{H}_{u,ij})$ and $\lambda_{\min}^2(\mathbf{H}_{u,ij})$ are constants for
 457 a fixed channel realization $\mathbf{H}_{u,ij}$, while the value of $\|\mathbf{e}_{ij}\|^2$
 458 depends on the specific APM constellation points. Based on the
 459 bound above, it is highly likely that an \mathbf{e}_{ij} with a small norm
 460 yields low upper bound and lower bound. Hence it has a high
 461 probability of generating the FD value, as it will be exemplified
 462 in Fig. 3. ■

463 Based on Lemma 3, for the sake of striking a beneficial
 464 trade-off between the BER performance and complexity for
 465 M -QAM, the search space is limited to the error vectors hav-
 466 ing small modulus values and only these vectors are utilized to
 467 compute the FD metric. Specifically, we first evaluate all possi-
 468 ble modulus values $T_1, T_2, T_3, \dots, T_v$ of all the legitimate error
 469 vectors \mathbf{e}_{ij} , then we find the K smallest T_K from the full set
 470 of $\{T_1, T_2, T_3, \dots, T_v\}$ and only consider the set of \mathbf{e}_{ij} having
 471 moduli lower than T_K to compute $d_{\min}(\mathbf{H}_u)$. In this process,
 472 the error vectors can be divided into the pair of sub-sets \mathbb{D}_1 and
 473 \mathbb{D}_2 based on their sparsity, where \mathbb{D}_1 contains the error vectors,
 474 which have only a single non-zero element, while \mathbb{D}_2 contains

$$\begin{aligned} m_{M\text{-PSK}}(\mathbf{H}_u) &= \max_n m_{\text{APM}} = \max_{n \in \{-(M-1), \dots, M-1\}} \{\mathcal{R}\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\} \cos \theta_n - \mathcal{J}\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\} \sin \theta_n\} \\ &= \max_{n \in \{0, \dots, M/4\}} \{|\mathcal{R}\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\} \cos \theta_n - \mathcal{J}\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\} \sin \theta_n|\} \end{aligned} \quad (39)$$

the error vectors, which have two non-zero elements. As will be shown in our simulation results, $K = 3$ is a good choice for diverse configurations, hence we only provide the simplified expressions of $d_{\min}^{\text{joint-EVM}}$ for $K \leq 3$ as follows.

For $K = 1$, according to the M -QAM constellation of Eq. (34), only error vectors having $T_1 = \sqrt{\frac{4}{\beta_k}}$ are considered and the associated sets \mathbb{D}_1 and \mathbb{D}_2 are given by $\mathbb{D}_1 = \frac{1}{\sqrt{\beta_k}}\{\pm 2\mathbf{e}_i, \pm 2j\mathbf{e}_i\}, i = 1, \dots, L$ and $\mathbb{D}_2 = \frac{1}{\sqrt{\beta_k}}\{(\pm 1 \pm 1j)\mathbf{e}_i - (\pm 1 \pm 1j)\mathbf{e}_j, i, j = 1, \dots, L, i \neq j\}$, respectively, where \mathbf{e}_i and \mathbf{e}_j are the active TA selection vectors in Eq. (2). Since only the minimum ED is considered, the set \mathbb{D}_1 can be reduced to $\mathbb{D}_1 = \frac{1}{\sqrt{\beta_k}}\{2\mathbf{e}_i, i = 1, \dots, L\}$. Moreover, based on the set \mathbb{D}_2 , it is found that the elements s_a and s_b belong to the reduced set $\frac{1}{\sqrt{\beta_k}}\{\pm 1 \pm 1j\}$ and we have $|s_a|^2 = \frac{2}{\beta_k}, |s_b|^2 = \frac{2}{\beta_k}$ and $s_a^H s_b \in \frac{2}{\beta_k}\{\pm 1, \pm 1j\}$. Substituting these values into Eq. (37), we get the simplified optimized metric for $K = 1$ as

$$d_{\min, K=1}^{\text{joint-EVM}} = \min_{\substack{i, j=1, \dots, L, \\ i \neq j}} \frac{2}{\beta_k} \|\mathbf{h}_u(i)\|_F^2 + \frac{2}{\beta_k} \|\mathbf{h}_u(j)\|_F^2 - 2m_{M-QAM}^{K=1}, \quad (41)$$

where we have

$$m_{M-QAM}^{K=1} = \max m_{\text{APM}} = \max \left\{ \frac{2}{\beta_k} |\Re\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\}|, \frac{2}{\beta_k} |\Im\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\}| \right\}. \quad (42)$$

For the case of $K = 2$, all the error vectors \mathbf{e}_{ij} having moduli lower than T_2 are used for FD calculation. Compared to $K = 1$, we have to consider the added error vectors $\frac{1}{\sqrt{\beta_k}}\{\pm 2 \pm 2j\mathbf{e}_i\} (i = 1, \dots, L)$ having $T_2 = \sqrt{\frac{8}{\beta_k}}$, which belong to \mathbb{D}_1 and do not change the set \mathbb{D}_2 . After eliminating all collinear elements, the set \mathbb{D}_1 of $K = 2$ is reduced to $\frac{1}{\sqrt{\beta_k}}\{2\mathbf{e}_i, \pm 2 \pm 2j\mathbf{e}_i, i = 1, \dots, L\}$. Moreover, since only the minimum distance is investigated, the set is further reduced to $\mathbb{D}_1 = \frac{1}{\sqrt{\beta_k}}\{2\mathbf{e}_i, i = 1, \dots, L\}$, which is the same as that of $K = 1$. Therefore, the setups of $K = 1$ and $K = 2$ will provide the same FD $d_{\min}(\mathbf{H}_u)$.

Moreover, for the case of $K = 3$, besides the error vectors \mathbf{e}_{ij} for $K = 2$, the error vectors having $T_3 = \sqrt{\frac{10}{\beta_k}}$ should be considered, which are given by $\frac{1}{\sqrt{\beta_k}}\{(\pm 3 \pm 1j)\mathbf{e}_i - (\pm 1 \pm 1j)\mathbf{e}_j, (\pm 1 \pm 3j)\mathbf{e}_i - (\pm 1 \pm 1j)\mathbf{e}_j\}, i, j = 1, \dots, L, i \neq j$. For these added error vectors, we have $s_a^H s_b \in \frac{1}{\beta_k}\{\pm 2 \pm 4j, \pm 4 \pm 2j\}$ and two legitimate combinations of the values of $|s_a|^2$ and $|s_b|^2$ as: (1) $|s_a|^2 = \frac{2}{\beta_k}, |s_b|^2 = \frac{10}{\beta_k}$

and (2) $|s_a|^2 = \frac{10}{\beta_k}, |s_b|^2 = \frac{2}{\beta_k}$. For each combination, similar to the process of Eqs. (41)-(42), we can substitute the values of $|s_a|^2, |s_b|^2$ and $s_a^H s_b$ into Eq. (37) and get the simplified optimized metric for $K = 3$ as

$$d_{\min, K=3}^{\text{joint-EVM}} = \min\{d_{\min, K=1}^{\text{joint-EVM}}, d_{\min, (1)}^{\text{joint-EVM}}, d_{\min, (2)}^{\text{joint-EVM}}\} \quad (43)$$

where $d_{\min, (1)}^{\text{joint-EVM}}$ and $d_{\min, (2)}^{\text{joint-EVM}}$ are the simplified ED for the above-mentioned two combinations, given by Eq. (44), shown at the bottom of the page.

4) *The Proposed EVM-Based ED-TAS*: Based on the simplified versions of $d_{\min}^{\text{joint-EVM}}$ for M -PSK and M -QAM schemes derived in Eqs. (41) and (43), the solution of our EVM-based ED-TAS algorithm is given by

$$\mathbf{H}_{\hat{u}} = \arg \max_{u \in \{1, \dots, N_U\}} \left\{ d_{\min}^{\text{signal}}, d_{\min}^{\text{spatial}}, d_{\min}^{\text{joint-EVM}} \right\}. \quad (45)$$

Note that similar to the proposed QRD-TAS, the terms $\|\mathbf{h}_u(i)\|_F^2, \|\mathbf{h}_u(j)\|_F^2$ and $\mathbf{h}_u(i)^H \mathbf{h}_u(j)$ in Eqs. (40)-(44) are elements of the matrix $\mathbf{H}^H \mathbf{H}$. Then, we can find the solution of Eq. (45) by reusing these elements for different TAS candidates \mathbf{H}_u .

Fig. 3 shows the probability that the error vectors having the minimum norm do result in finding the optimal ED-TAS solution as a function of K . For example, we have a probability of 97% for 16-QAM modulated SM for $K = 1$ using $N_t = 4, L = 2$ and $N_r = 2$. Moreover, it is observed from Fig. 3 that this probability is also high for other QAM schemes; hence the EVM-based ED-TAS can be readily used in diverse scenarios. In general, for striking a flexible BER vs complexity tradeoff, we can adjust the parameter K to reduce the search space to a subset of the error vectors that may yield the optimal ED-TAS solution with a high probability.

Note that in [17] a PEP-based TAS (PEP-TAS) algorithm was proposed, which was based on a different search set reduction. The main differences of the proposed EVM-TAS and the PEP-TAS of [17] are:

- The PEP-TAS is based on the assumption that a smaller APM symbol amplitude leads to a smaller distance d_{\min}^{joint} , whereas based on our analysis it is highly likely that an error vector with a small norm yields the distance d_{\min}^{joint} .
- Moreover, in EVM-TAS, we propose to use the parameter K for striking a flexible tradeoff between the conflicting factors of the computational complexity imposed and the attainable BER.

Remark: Compared to the EVM-TAS, the PEP-TAS considers only the error vectors generated by M -QAM symbols having the minimum amplitude. It can be shown that the non-linear error vectors of the PEP-TAS are the same as those of the

$$\left\{ \begin{array}{l} d_{\min, (1)}^{\text{joint-EVM}} = \min_{\substack{i, j=1, \dots, L \\ i \neq j}} \frac{2}{\beta_k} \|\mathbf{h}_u(i)\|_F^2 + \frac{10}{\beta_k} \|\mathbf{h}_u(j)\|_F^2 - 2m_{M-QAM}^{K=3} \\ d_{\min, (2)}^{\text{joint-EVM}} = \min_{\substack{i, j=1, \dots, L \\ i \neq j}} \frac{10}{\beta_k} \|\mathbf{h}_u(i)\|_F^2 + \frac{2}{\beta_k} \|\mathbf{h}_u(j)\|_F^2 - 2m_{M-QAM}^{K=3} \\ m_{M-QAM}^{K=3} = \max \frac{1}{\beta_k} \left\{ |2\Re\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\}| + |4\Im\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\}|, |4\Re\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\}| + |2\Im\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\}| \right\} \end{array} \right. \quad (44)$$

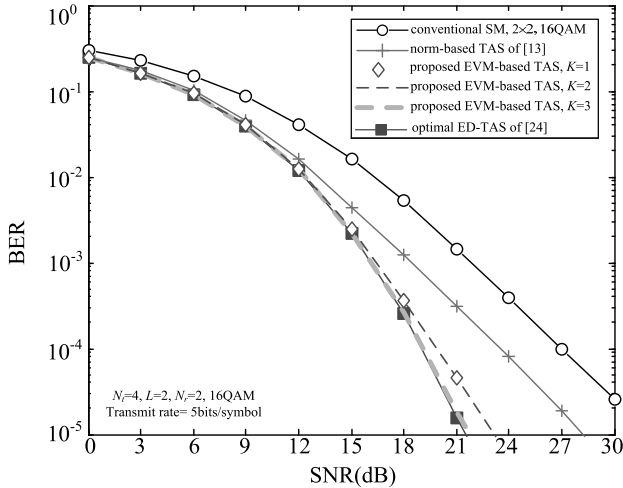


Fig. 4. BER performance comparison of the existing TAS algorithms and the proposed EVM-based TAS algorithm for $N_t = 4$, $N_r = 2$, 16QAM and $L = 2$. The transmit rate is 5 bits/symbol.

554 EVM-TAS associated with $K = 1$. Therefore, it can be viewed
 555 as a special case of EVM-TAS by setting $K = 1$.

556 Fig. 4 shows our BER comparison for the existing TAS
 557 algorithms and the proposed EVM-TAS algorithm. The simu-
 558 lation parameters are the same as those of Fig. 2. Firstly,
 559 as proved in Section IV-B and observed in Fig. 3, the proba-
 560 bility that the error vectors do indeed result in the optimal
 561 ED-TAS solution is the same for the cases of $K = 1$ and $K = 2$.
 562 Hence, they provide the same BER performance, as shown in
 563 Fig. 4. Furthermore, we observe in Fig. 3 that this probabili-
 564 ty is increased from 0.975 to 0.998 upon increasing K from 1
 565 to 3. As a result, in Fig. 4 the performance of the EVM-based
 566 ED-TAS associated with $K = 3$ is improved compared to that
 567 scheme with $K = 1$. Moreover, compared the results in Figs. 2
 568 and 4, the EVM-based ED-TAS outperforms the SVD-based
 569 ED-TAS for $K = 3$.

570 V. JOINT TAS AND PA ALGORITHMS FOR SM

571 Similar to the TAS technique, PA is another attractive link
 572 adaptation technique conceived for SM, which has been advo-
 573 cated in [7], [11], [28], [29]. The process of PA can be modeled
 574 by the PA matrix \mathbf{P} , which is given by

$$\mathbf{P} = \text{diag}\{p_1, \dots, p_q, \dots, p_L\}, \quad (46)$$

575 where p_q controls the channel gain of the q th TA. Here, we let
 576 $\sum_{q=1}^L p_q^2 = 1$ for normalizing the transmit power. Based on our
 577 TAS algorithms, we propose a pair of combined algorithms for
 578 jointly considering the PA and TAS as follows:

579 1) TAS&PA

- 580 • *Step 1:* Each $(N_r \times N_r)$ channel matrix \mathbf{H} has $N_U =$
 581 $\binom{N_t}{L}$ possible subchannel matrices \mathbf{H}_u , each of
 582 which corresponds to a specifically selected $(N_r \times$
 583 $L)$ MIMO channel. For each \mathbf{H}_u , we calculate the
 584 corresponding PA matrix \mathbf{P}_u and its FD with the aid
 585 of the algorithm of [29].
- 586 • *Step 2:* The particular combinations of $\mathbf{H}_u \mathbf{P}_u (u =$
 587 $1, \dots, N_U)$ constitute the legitimate TAS&PA

candidates. Let us interpret the matrices $\mathbf{H}_u \mathbf{P}_u$ 588
 ($u = 1, \dots, N_U$) as being the equivalent channel 589
 matrices of Section IV and select the specific can- 590
 didate with the maximum free distance as the final 591
 solution. 592

Since for each channel realization \mathbf{H} , there are N_U pos- 593
 sible PA matrices $\mathbf{P}_u (u = 1, \dots, N_U)$, we have a high 594
 computational complexity if N_U is high. Next, we intro- 595
 duce a lower-complexity solution for this joint TAS and 596
 PA algorithm. 597

2) Low-complexity TAS&PA 598

- 599 • *Step 1:* Assume $\mathbf{P}_u = \mathbf{I}_L (u = 1, \dots, N_U)$ and use
 600 the proposed low-complexity QRD-based ED-TAS
 601 or the EVM-based ED-TAS algorithm to select a
 602 particular subset of TAs from the set of options,
 603 which corresponds to $\mathbf{H}_{\hat{u}}$.
- 604 • *Step 2:* Calculate the power weights for the selected
 605 TAs, which can be represented by the PA matrix $\hat{\mathbf{P}}_{\hat{u}}$.
 606 During this step, the low-complexity PA algorithm
 607 of [29] can be invoked. In the simple TAS&PA, the
 608 PA matrix only has to be calculated once, hence the
 609 associated complexity is low.

610 VI. SIMULATION RESULTS

In this section, we provide simulation results for further char- 611
 acterizing the proposed QRD-based ED-TAS, EVM-based ED- 612
 TAS and TAS&PA schemes for transmission over frequency- 613
 flat fading MIMO channels. For comparison, these performance 614
 results are compared to various existing TAS-SM schemes of 615
 [13], [21], [23], [25], to the classic TAS/maximal-ratio combin- 616
 ing (TAS/MRC) schemes of [40], as well as to the TAS&PA 617
 aided V-BLAST of [32]. In our simulations, the single-stream 618
 ML detector of [34], [35] is utilized. 619

620 A. BER Comparisons of Different TAS Algorithms for SM

In Fig. 5, we compare the BER performance of various TAS- 621
 SM schemes for 4 bits/symbol associated with $N_t = 8$, $L = 4$, 622
 $N_r = 4$ and QPSK. We also considered the conventional single- 623
 RF based TAS/MRC arrangement of [40] as benchmarker. As 624
 seen from Fig. 5, the proposed QRD-based ED-TAS outper- 625
 forms the conventional SVD-based ED-TAS of [23], as also 626
 formally shown in Fig. 2. Moreover, as expected, in Fig. 5 627
 the EVM-based TAS is capable of achieving the same per- 628
 formance as the optimal ED-TAS of [21]. We also confirm 629
 that our proposed EVM-based ED-TAS schemes outperform 630
 the norm-based TAS of [13] and the QRD-based ED-TAS pro- 631
 posed for PSK modulation. These results are consistent with the 632
 analysis results in Section IV, where the EVM-based TAS has 633
 considered all legitimate error vectors for simplifying d_{\min}^{joint} in 634
 Eq. (40), while the QRD-based ED-TAS may achieve uncorrect 635
 estimation of d_{\min}^{joint} due to the employment of lower bound of 636
 Eq. (27). 637

Fig. 5 also shows that our new TAS-SM schemes outper- 638
 form the TAS/MRC scheme of [40]. The main reason behind 639
 the poorer performance of TAS/MRC is the employment of 640
 a higher modulation order required for achieving the same 641

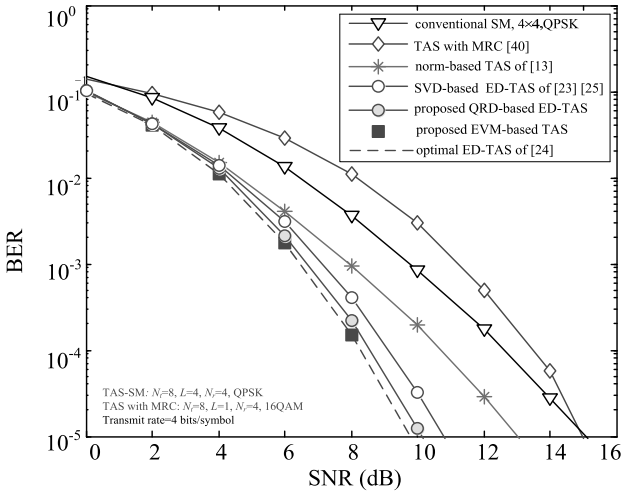


Fig. 5. BER comparison at $m = 4$ bits/symbol for the proposed TAS-SM schemes, the existing TAS-SM schemes and the classic TAS/MRC scheme having $N_t = 8$ and $L = 4$.

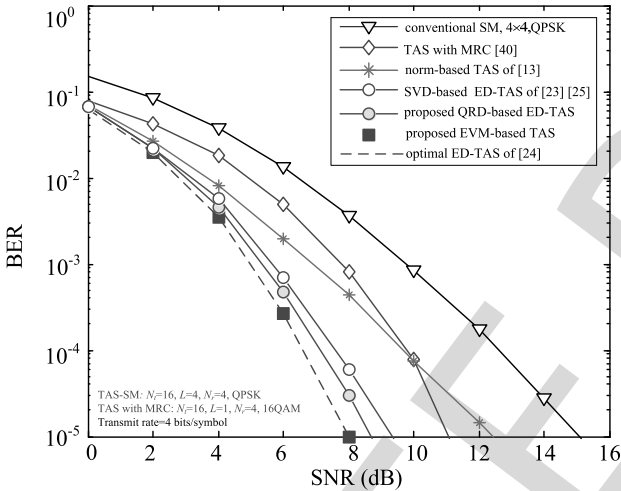


Fig. 6. BER comparison at $m = 4$ bits/symbol for the proposed TAS-SM schemes, the existing TAS-SM schemes and the classic TAS/MRC scheme having $N_t = 16$ and $L = 4$.

throughput as our SM-based schemes. Note that this benefit depends on the particular MIMO setups. To be specific, as noted in [23], the TAS-SM and the TAS/MRC schemes exhibit different BER advantages for different system setups. However, similar to the results achieved in [23], our new TAS-SM schemes strike an attractive tradeoff between the complexity and the BER attained. The above-mentioned trends of these proposed TAS-SM schemes are also confirmed in Fig. 6, where the number N_t of TAS increases from 8 to 16.

In Fig. 7, a spatially correlated MIMO channel model characterized by $\mathbf{H}^{corr} = \mathbf{R}_r^{1/2} \mathbf{H} \mathbf{R}_t^{1/2}$ [24], [41] is considered for the proposed QRD-based ED-TAS and EVM-based TAS ($K = 3$) schemes, where $\mathbf{R}_t = [r_{ij}]_{N_t \times N_t}$ and $\mathbf{R}_r = [r_{ij}]_{N_r \times N_r}$ are the positive definite Hermitian matrices that specify the transmit and receive correlations, respectively. In Fig. 7, the components of \mathbf{R}_t and \mathbf{R}_r are calculated as $r_{ij} = r_{ji}^* = r^{j-i}$ for $i \leq j$, where r is the correlation coefficient ($0 \leq r \leq 1$). Here, the simulation parameters are the same as those of Figs. 2 and 4

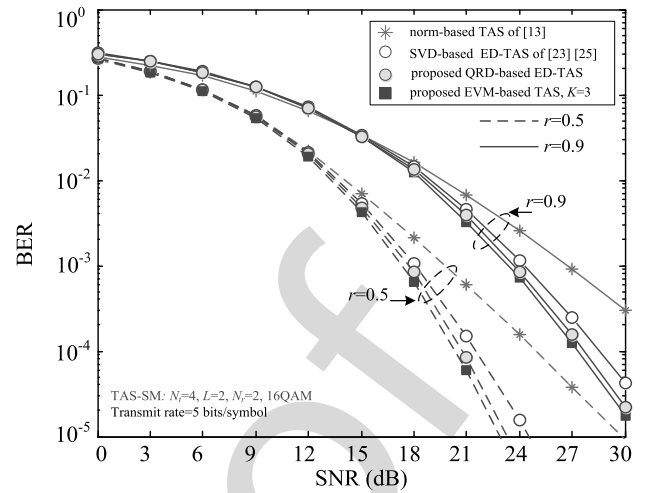


Fig. 7. BER comparison of different TAS algorithms for SM systems in correlated Rayleigh fading channels.

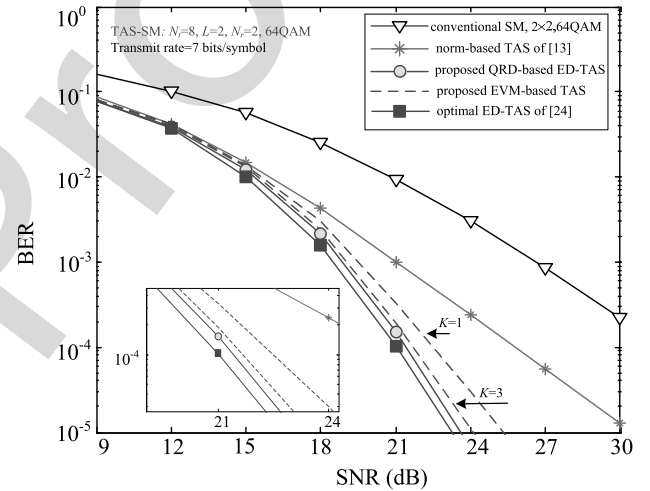


Fig. 8. BER comparison at $m = 7$ bits/symbol for the proposed QRD-based ED-TAS and EVM-based ED-TAS with 64-QAM.

for 5 bits/symbol transmissions. We found that the BER curves of the EVM-based TAS schemes and of the optimal ED-TAS are almost overlapped (similar to the results seen in Fig. 4), hence for clarity in Fig. 7 we simply provide the BER curves for the EVM-based TAS schemes only. Compared to the BER curves in Figs. 2 and 4 for the correlation coefficient $r = 0$, we observe in Fig. 7 that the BER performance of all schemes is substantially degraded by these correlations. However, the proposed schemes remain capable of operating efficiently for the correlated channels.

In Fig. 8, we further compare the proposed QRD-based ED-TAS scheme and the proposed EVM-based TAS schemes for a higher modulation order, where the 64-QAM scheme is employed. Observe in Fig. 8 that the proposed QRD-based ED-TAS scheme outperforms the EVM-based TAS scheme in conjunction with $K = 1$ and the corresponding performance gain is seen to be about 1 dB. Similar to the results in Figs. 2 and 4, the EVM-based TAS associated with $K = 3$ provide an improved BER compared to that scheme with $K = 1$. At

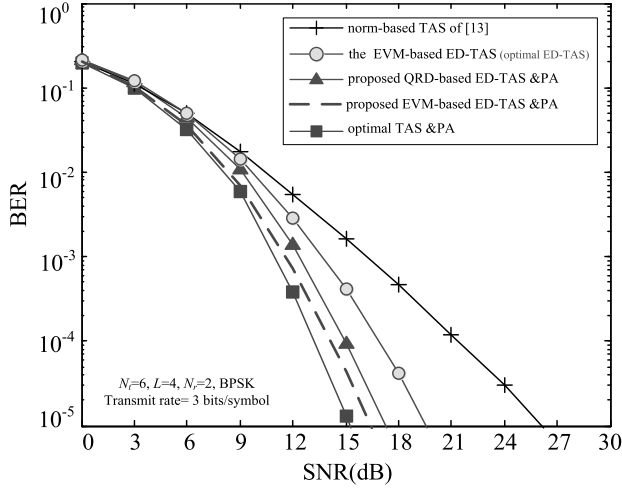


Fig. 9. BER performance comparison of the TAS algorithms and of the proposed TAS &PA algorithms in SM systems, having the transmit rate of 3 bits/symbol.

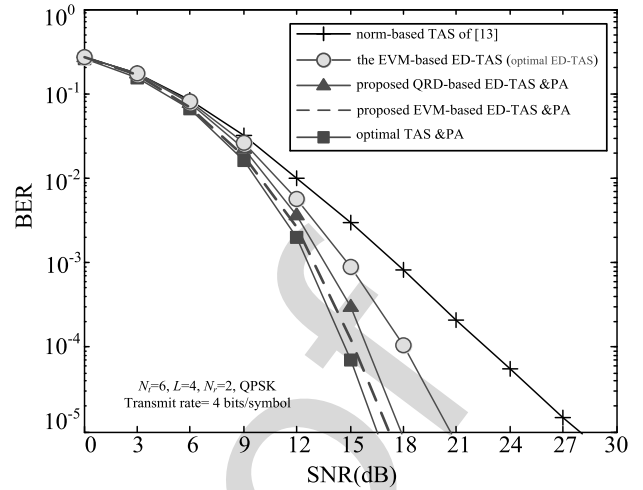


Fig. 10. BER performance comparison of the TAS algorithms and of the proposed TAS &PA algorithms in SM systems, having the transmit rate of 4 bits/symbol.

679 BER= 10^{-5} , the performance gap between the proposed EVM-
 680 based TAS with $K = 3$ and the proposed QRD-based ED-TAS
 681 becomes negligible.

682 The main conclusions observed from Figs. 2, 4 and 5–8 are:
 683 (1) the proposed EVM-based TAS and QRD-based ED-TAS
 684 schemes exhibit different BER advantages for different system
 685 setups; (2) the proposed QRD-based ED-TAS is preferred
 686 to the QAM-modulated SM schemes, since its complexity is
 687 independent of the modulation order; (3) The proposed EVM-
 688 based TAS is preferred to the PSK-modulated SM schemes,
 689 since it can achieve the performance of optimal ED-TAS at
 690 the reduced error vector set. (4) For the QAM-modulated SM
 691 schemes, the parameter K of the proposed EVM-based TAS
 692 can be flexibly selected for striking a beneficial trade-off between
 693 the complexity imposed and the BER attained.

694 *B. BER Comparisons of TAS Algorithms and TAS &PA*
 695 *Algorithms for SM*

696 In this subsection, we focus our attention on studying the
 697 BER performance of our TAS&PA algorithms. Here, for the
 698 low-complexity TAS&PA, the proposed QRD-based ED-TAS
 699 as well as the EVM-based ED-TAS algorithms are utilized and
 700 the corresponding algorithms are termed as the QRD-based
 701 ED-TAS &PA and the EVM-based ED-TAS &PA, respec-
 702 tively. Note that the EVM-based ED-TAS achieves the same
 703 performance as the optimal ED-TAS for the PSK-modulated
 704 SM schemes. The BER performances of other TAS algorithms
 705 are similar to the results seen in Figs. 2, 4 and 5–8. Hence,
 706 for clarity, when only pure TAS is considered, we simply
 707 provide the corresponding BER curves of the proposed EVM-
 708 based ED-TAS and of the conventional norm-based TAS as
 709 benchmarks.

710 Fig. 9 compares the BER performance of the proposed
 711 TAS&PA arrangement to that of other SM-based schemes. In
 712 Fig. 9, the parameter setup is $N_t = 6$, $L = 4$, $N_r = 2$ and
 713 $M = 2$. It becomes clear from Fig. 9 that the TAS&PA algo-
 714 rithms advocated outperform both the EVM-based ED-TAS and

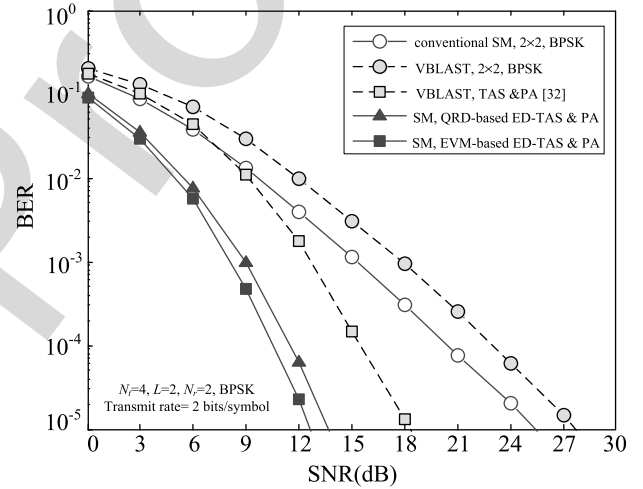


Fig. 11. BER performance comparison of the proposed TAS &PA algorithms in SM systems and the conventional identical-throughput TAS&TA algorithm in V-BLAST systems, where the throughput is 2 bits/symbol ($N_t = 4$, $N_r = 2$, $L = 2$).

the norm-based ED-TAS. At a BER of 10^{-5} , the exhaustive- 715
 search based optimal TAS&PA provides 9.5 dB and 4 dB SNR 716
 gains over the norm-based ED-TAS and over the EVM-based 717
 ED-TAS, respectively. Moreover, the low-complexity QRD- 718
 based ED-TAS &PA provides about 4 dB SNR gain over the 719
 EVM-based TAS operating without PA. 720

Fig. 9 also shows that the EVM-based ED-TAS &PA outper- 721
 forms the QRD-based ED-TAS&PA and is capable of achieving 722
 almost the same BER performance as the optimal TAS&PA. 723
 The performance advantages of our schemes are attained as 724
 a result of exploiting all the benefits of MIMO channels. The 725
 above-mentioned trends of these TAS&PA algorithms recorded 726
 for SM are also visible in Fig. 10, where a SM system using 727
 $N_t = 6$, $L = 4$, $N_r = 2$ and QPSK modulation is considered. 728

In Fig. 11, the BPSK-modulated V-BLAST scheme and its 729
 TAS&PA-aided counterpart [32] associated with zero-forcing 730
 successive interference cancellation (ZF-SIC) are compared to 731

TABLE II
COMPLEXITY COMPARISON OF DIFFERENT TAS-SM ALGORITHMS IN DIVERSE CONFIGURATIONS

TAS algorithm	Configuration 1 ($N_t = 4, N_r = 2$ $L = 2, 16\text{QAM}$)	Configuration 2 ($N_t = 8, N_r = 4$ $L = 4, \text{QPSK}$)	Configuration 3 ($N_t = 8, N_r = 2$ $L = 2, 64\text{-QAM}$)
Exhaustive ED-TAS [13]	13824	8512	1032192
Maximum-norm based TAS [21]	12	56	24
Conventional QRD-based ED-TAS [24]	2060	6029	38253
SVD-based ED-TAS [25]	102	588	444
Proposed QRD-based ED-TAS	82	596	340
Proposed EVM-based ED-TAS	$\begin{cases} 84, K = 1 \\ 180, K = 3 \end{cases}$	756	$\begin{cases} 360, K = 1 \\ 808, K = 3 \end{cases}$
Exhaustive TAS&PA	4626	46340	256788
Proposed QRD-based ED-TAS&PA	853	1004	9511
Proposed EVM-based ED-TAS&PA	$\begin{cases} 855, K = 1 \\ 951, K = 3 \end{cases}$	1164	$\begin{cases} 9531, K = 1 \\ 9979, K = 3 \end{cases}$

our TAS&PA based schemes. For maintaining an identical-throughput, in Fig. 11 we let $N_t = 4, N_r = 2, L = 2$ and use BPSK for all schemes. Observe in Fig. 11 that our TAS&PA based SM schemes outperform the TAS&PA aided V-BLAST schemes by about 5-6 dB SNR at the BER of 10^{-5} .

C. Complexity Comparison

Table I shows the complexity comparison of various TAS algorithms conceived for SM, where the total number of floating point operations is considered. The Appendix provides the details of our computational complexity evaluations for the proposed TAS algorithms list in Table I. The complexity estimation of the existing TAS algorithms can be found in [15], [23] and [24]. Moreover, our complexity analysis is similar to that of [23] and [24].

Explicitly, in Table II, the quantified complexity of different TAS algorithms for some specific configurations are provided. As shown in Table I, the proposed QRD-based ED-TAS has a similar complexity order to that of the low-complexity SVD-based ED-TAS of [23], while exhibiting a lower complexity compared to the conventional QRD-based ED-TAS of [24]. For example, the proposed QRD-based ED-TAS imposes an approximately 168 times and 25 times lower complexity than the exhaustive ED-TAS and the conventional QRD-based ED-TAS for configuration 1. This is due to the fact that it is capable of avoiding the high-complexity QRD operation by directly computing the bound parameters of Eq. (27). Moreover, as shown in Tables I-II and Figs. 4-8, the EVM-based ED-TAS advocated is capable of striking a flexible BER vs complexity trade-off by employing the parameter K for diverse M -QAM schemes. Furthermore, the proposed low-complexity TAS&PA schemes impose a lower complexity than the exhaustive-search based TAS&PA and only impose a slightly increased complexity compared to the proposed EVM-based TAS and QRD-based TAS schemes. By considering the BER vs complexity results of Tables I-II and Figs. 9-11, the proposed low-complexity TAS&PA is seen to provide an improved BER performance at a modest complexity cost.

VII. CONCLUSIONS

In this paper, we have investigated TAS algorithms conceived for SM systems. Firstly, a pair of low-complexity

ED-TAS algorithms, namely the QRD-based ED-TAS and the EVM-based ED-TAS, were proposed. The theoretical analysis and simulation results indicated that the QRD-based ED-TAS exhibits a better BER performance compared with the conventional SVD-based ED-TAS, while the EVM-based ED-TAS is capable of striking a flexible BER vs complexity trade-off. To further improve the attainable performance, the proposed TAS algorithms were amalgamated with PA. A pair of beneficial joint TAS-PA algorithms were proposed and our simulation results demonstrated that they outperform both the pure TAS algorithms and the TAS&PA algorithm designed for spatial multiplexing systems.

APPENDIX

Computational complexity of the proposed TAS algorithms designed for SM systems.

A. The Proposed QRD-Based ED-TAS

As detailed in Section IV-A, the calculation of the QRD-based bound of Eq. (27) only depends on the elements of the matrix $\mathbf{H}^H \mathbf{H}$, which incurs a complexity in the order of $\text{comp}(\mathbf{H}^H \mathbf{H}) = 2N_t^2 N_r - N_r^2$. Then, we can calculate the values of $\tilde{R}_{k,k}(\mathbf{\Pi}_m)$, ($m = 1, 2, k = 1, 2$) in Eqs. (30)-(33) by reusing these elements for the different TAS candidates \mathbf{H}_u . Specifically, the calculation of $\sqrt{\|\mathbf{h}_u(j)\|_F^2}$, $j = 1, \dots, N_t$ for estimating $\tilde{R}_{1,1}(\mathbf{\Pi}_m)$, $m = 1, 2$ in Eqs. (30) and (32) requires N_t flops. Moreover, to calculate the values of $\tilde{R}_{2,2}(\mathbf{\Pi}_m)$, $m = 1, 2$ in Eqs. (31) and (33), we have to consider $\binom{N_t}{2}$ possible combinations (i, j) for computing the value of $\sqrt{\frac{\|\mathbf{h}_u(i)\|_F^2 + \|\mathbf{h}_u(j)\|_F^2 - 2\Re\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\}}{\|\mathbf{h}_u(j)\|_F^2}}$. For each combination, the complexity imposed is 5 flops. Hence, the complexity of computing $\tilde{R}_{2,2}(\mathbf{\Pi}_m)$, $m = 1, 2$ is $5\binom{N_t}{2}$ flops. The overall complexity of the proposed QRD-based ED-TAS is

$$\begin{aligned} C_{\text{PQRD}} &= 2N_t^2 N_r - N_r^2 + N_t + 5\binom{N_t}{2} \\ &= 2N_t^2 N_r + \frac{3}{2}N_t(N_t - 1). \end{aligned} \quad (47)$$

Note that based on Eq. (28), $d_{\min}^{\text{Modulus}}$, d_{\min}^{APM} and d_{\min}^{all} are constants for a specific APM scheme and the calculation of d_{\min}^{signal} and $d_{\min}^{\text{spatial}}$ can also exploit the common elements, such as $\|\mathbf{h}_u(i)\|_F^2 + \|\mathbf{h}_u(j)\|_F^2 - 2\Re\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\}$, $\|\mathbf{h}_u(i)\|_F^2$, in the

807 calculation of the bound of d_{\min}^{joint} , as shown in Eqs. (15) and
808 (16). Hence, the complexity imposed can be deemed negligible.

809 *B. The Proposed EVM-Based ED-TAS*

810 Similar to the proposed QRD-based ED-TAS, the com-
811 putational complexity of EVM-based ED-TAS is also domi-
812 nated by computing d_{\min}^{joint} . Specifically, we also first have to
813 evaluate the elements $\|\mathbf{h}_u(i)\|_F^2$, $\|\mathbf{h}_u(j)\|_F^2$ and $\mathbf{h}_u(i)^H \mathbf{h}_u(j)$,
814 which incurs a complexity of $2N_t^2 N_r - N_t^2$ flops. Then,
815 for M -PSK, the simplified version of d_{\min}^{joint} is given in
816 Eq. (40), which has to consider $\binom{N_t}{2}$ legitimate TA com-
817 bination (i, j) . For each combination (i, j) , the computa-
818 tion of the term $m_{M\text{-PSK}}(\mathbf{H}_u)$ of Eq. (39) has to consider
819 $(\frac{M}{4} + 1)$ possible θ_n values. For each θ_n , the complexity of
820 evaluating $|\Re\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\} \cos \theta_n - \Im\{\mathbf{h}_u(i)^H \mathbf{h}_u(j)\} \sin \theta_n|$ is
821 4 flops. Moreover, for a specific $m_{M\text{-PSK}}(\mathbf{H}_u)$ and a fixed
822 combination (i, j) , the computation of $\|\mathbf{h}_u(i)\|_F^2 + \|\mathbf{h}_u(j)\|_F^2 -$
823 $2m_{M\text{-PSK}}(\mathbf{H}_u)$ in Eq. (40) requires 3 flops. Hence, the overall
824 complexity of the M -PSK modulated EVM-based ED-TAS is

$$\begin{aligned} C_{\text{EVM}} &= 2N_t^2 N_r - N_t^2 + \binom{N_t}{2} \{4(\frac{M}{4} + 1) + 3\} \\ &= 2N_t^2 N_r - N_t^2 + \frac{1}{2} N_t (N_t - 1) (M + 7). \end{aligned} \quad (48)$$

825 For the M -QAM scheme, this complexity depends on the
826 parameter K . Specifically, the simplified versions of d_{\min}^{joint}
827 are different for different values of K . In general, for a given K ,
828 we first characterize all possible combinations of $|s_a|^2$ and $|s_b|^2$
829 by using the method of Section IV-B. Let us assume that the
830 number of these combinations is G . For each combination, we
831 can simplify Eq. (37) similar to the process of Eqs. (43)-(44),
832 which corresponds to G simplified equations and each requires
833 15 flops, as shown in Eq. (37). Since $\binom{N_t}{2}$ legitimate TA com-
834 binations (i, j) should be considered in Eq. (37), we arrive at a
835 complexity of $15G \binom{N_t}{2}$ for all possible combinations. Overall,
836 the complexity of the EVM-based TAS for M -QAM modulated
837 SM is

$$C_{\text{EVM}} = 2N_t^2 N_r - N_t^2 + 15G \binom{N_t}{2}. \quad (49)$$

838 Note that the complexity of Eq. (49) is an approximate result,
839 which can be further refined based on the specific simplified
840 version of d_{\min}^{joint} . For example, based on Eqs. (41) and (43)
841 derived for $K = 1$ and $K = 3$, similar to the complexity anal-
842 ysis of M -PSK, the computational complexity orders of the
843 EVM-based TAS for $K = 1$ and $K = 3$ are

$$C_{\text{EVM-TAS}} = 2N_t^2 N_r - N_t^2 + 6 \binom{N_t}{2}, \quad (50)$$

844 and

$$C_{\text{EVM-TAS}} = 2N_t^2 N_r - N_t^2 + 22 \binom{N_t}{2}. \quad (51)$$

845 *C. The Proposed PA & TAS*

846 The exhaustive-search based TAS&PA algorithm has to cal-
847 culate all legitimate PA matrix candidates. According to Section

V, there are $N_U = \binom{N_t}{L}$ legitimate PA matrix candidates \mathbf{P}_u ($u =$ 848
849 $1, \dots, N_U$), which can be obtained by using the method pro-
850 posed in [29]. The complexity of computing each PA matrix is
851 C_{PA} (Eq. (22) in [29]) flops. Hence, the associated complexity
852 of the exhaustive-search based TAS&PA algorithm is $N_U C_{\text{PA}}$
853 flops. By contrast, the low-complexity TAS&PA algorithm first
854 selects the optimal TA subset and then calculates the PA matrix
855 for the selected set. Hence, the associated complexity order of
856 the low-complexity TAS&PA algorithm is $C_{\text{TAS}} + C_{\text{PA}}$ flops,
857 where C_{TAS} is the complexity of the TAS algorithm employed,
858 i. e. C_{EVM} or C_{PQRD} .

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