

**3GPP TSG RAN WG1 Meeting #87**  
**Reno, Nevada, USA, 14th – 18th November 2016**

**R1-1612308**

**Agenda item:** 7.1.5.1

**Source:** AccelerComm

**Title:** BLER performance of list decoding for enhanced turbo codes

**Document for:** Discussion

## I. INTRODUCTION

This paper presents Block Error Ratio (BLER) performance results for the list decoding of the enhanced turbo code of [1]. The list decoding technique of [2] is employed, as implemented in the attached Matlab code. Here, a list Viterbi decoder [3] is employed to identify a list comprising the  $L$  most likely paths through the trellis of the upper component code. Following this  $L$  replicas of the iterative turbo decoding process are performed. During the first iteration of each replica, a different set of transitions are pruned from the trellis of the upper component code, in order to force a different starting point for the turbo decoding process. At the completion of the  $L$  turbo decoding processes,  $L$  different decoded bit sequences are typically obtained. Therefore, the complexity of list turbo decoding is equal to the  $L$  times the complexity of conventional turbo decoding, plus the complexity of a list Viterbi decoder.

The BLER results presented in this paper quantify the ratio of information blocks that do not exist within the list of  $L$  decoded candidates.

## II. EMBB DATA CHANNEL

Figures 1 – 3 provide BLER results for block lengths of  $K \in \{96, 400, 992\}$  bits, when using Quaternary Phase Shift Keying (QPSK) modulation for transmission over an Additive White Gaussian Noise (AWGN) channel. Likewise, Figure 4 provides BLER results for a block length of  $K = 96$  bits, when using QPSK modulation for transmission over an uncorrelated narrowband Rayleigh fading channel. Figure 5 provides BLER results for a block length of  $K = 96$  bits, when using 64-ary Quadrature Amplitude Modulation (64QAM) modulation for transmission over an AWGN channel. Figure 6 provides BLER results for a block length of  $K = 96$  bits, when using 64QAM modulation for transmission over an uncorrelated narrowband Rayleigh fading channel.

In all plots,  $I = 8$  iterations of scaled-Max-Log-MAP decoding is assumed for coding rates of  $R \in \{1/5, 1/3, 2/5, 1/2, 2/3, 8/9\}$  and list sizes of  $L \in \{32, 16, 8, 4, 2, 1\}$ .

## III. EMBB CONTROL, URLLC AND MMTC CHANNELS

Figures 7 – 9 provide BLER results for block lengths of  $K \in \{32, 80, 208\}$  bits, when using QPSK modulation for transmission over an AWGN channel. Likewise, Figures 10 – 12 provide BLER results for block lengths of  $K \in \{32, 80, 208\}$  bits, when using QPSK modulation for transmission over an uncorrelated narrowband Rayleigh fading channel. Figures 13 and 14 provide BLER results for block lengths of  $K \in \{32, 80\}$  bits, when using 64QAM modulation for transmission over an AWGN channel. Likewise, Figures 15 and 16 provide BLER results for block lengths of  $K \in \{32, 80\}$  bits, when using 64QAM modulation for transmission over an uncorrelated narrowband Rayleigh fading channel.

In all plots,  $I = 8$  iterations of scaled-Max-Log-MAP decoding is assumed for coding rates of  $R \in \{1/12, 1/6, 1/3, 1/2, 2/3\}$  and list sizes of  $L \in \{32, 16, 8, 4, 2, 1\}$ .

#### IV. CONCLUSIONS

This paper has presented BLER performance results for the list decoding of the enhanced turbo code of [1].

**Observation 1: List decoding of turbo codes provides greater coding gains when employing (a) higher list sizes  $L$ , (b) higher coding rates  $R$ , (c) shorter information block lengths  $K$  and/or (d) fading channels.**

**Observation 2: Relative to conventional turbo decoding, list decoding can provide coding gains of around 2 dB, when employing  $L = 32$ ,  $R = 2/3$ ,  $K = 32$  and an uncorrelated Rayleigh fading channel.**

#### REFERENCES

- [1] Orange and IMT, "R1-1612938 Enhanced Turbo Codes for NR: Performance Evaluation for eMBB and URLLC," in *3GPP TSG RAN WGI #87*, Nov. 2016.
- [2] A. Akmalhodzhaev and A. Kozlov, "New iterative turbo code list decoder," in *Proc. Int. Symp. Problems of Redundancy in Information and Control Systems*, June 2014, pp. 15–18.
- [3] N. Seshadri and C. E. W. Sundberg, "List Viterbi decoding algorithms with applications," *IEEE Trans. Commun.*, vol. 42, no. 234, pp. 313–323, Feb 1994.

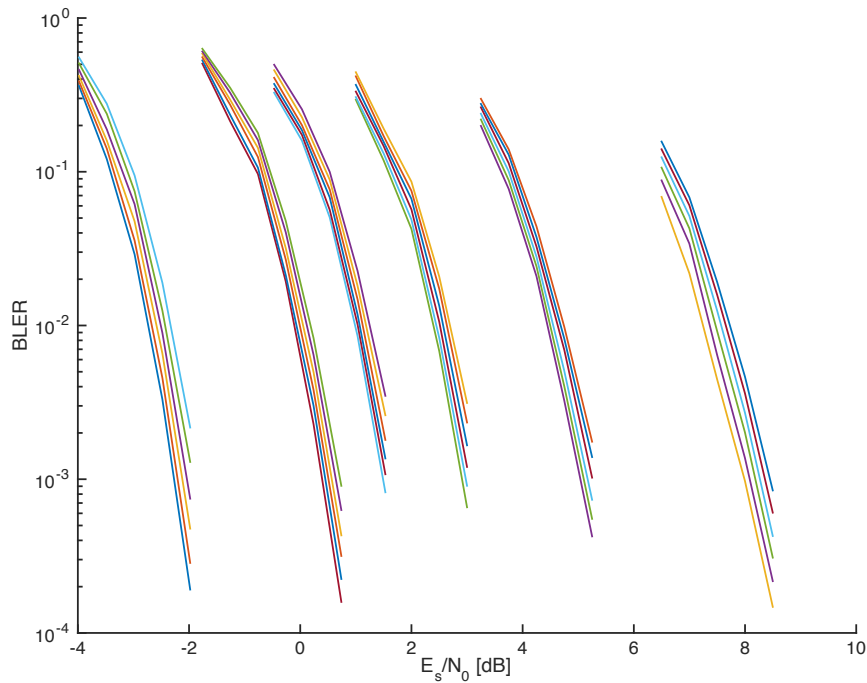


Fig. 1.  $K = 96$ .  $R \in \{1/5, 1/3, 2/5, 1/2, 2/3, 8/9\}$  from left to right.  $L \in \{32, 16, 8, 4, 2, 1\}$  from left to right. QPSK modulation. AWGN channel.  $I = 8$  iterations of scaled-Max-Log-MAP decoding.

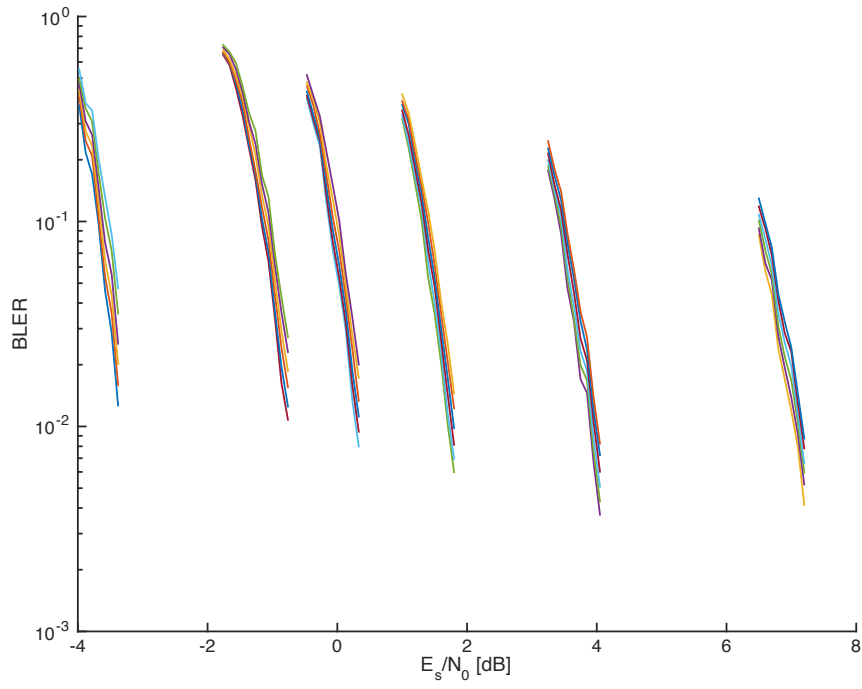


Fig. 2.  $K = 400$ .  $R \in \{1/5, 1/3, 2/5, 1/2, 2/3, 8/9\}$  from left to right.  $L \in \{32, 16, 8, 4, 2, 1\}$  from left to right. QPSK modulation. AWGN channel.  $I = 8$  iterations of scaled-Max-Log-MAP decoding.

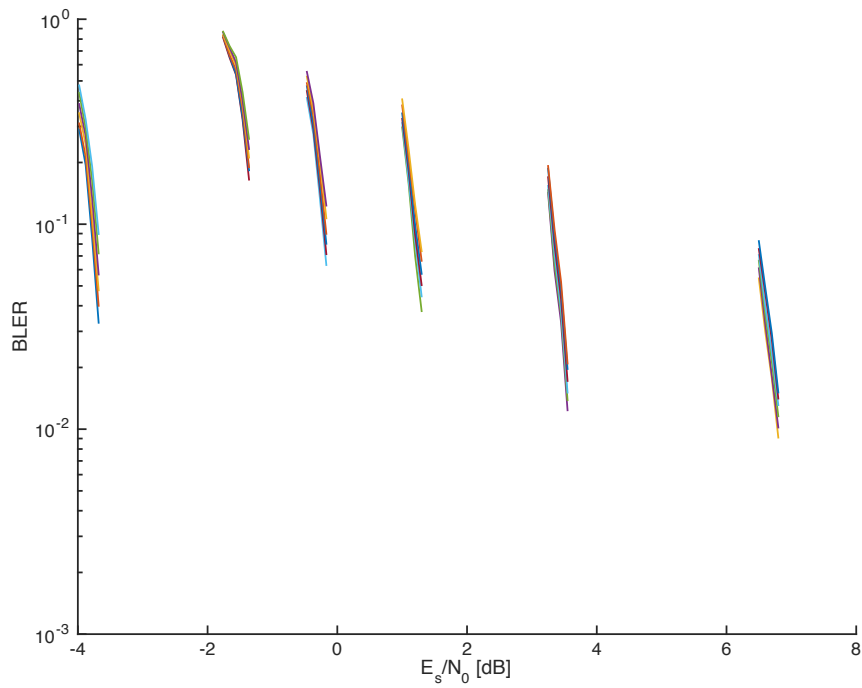


Fig. 3.  $K = 992$ .  $R \in \{1/5, 1/3, 2/5, 1/2, 2/3, 8/9\}$  from left to right.  $L \in \{32, 16, 8, 4, 2, 1\}$  from left to right. QPSK modulation. AWGN channel.  $I = 8$  iterations of scaled-Max-Log-MAP decoding.

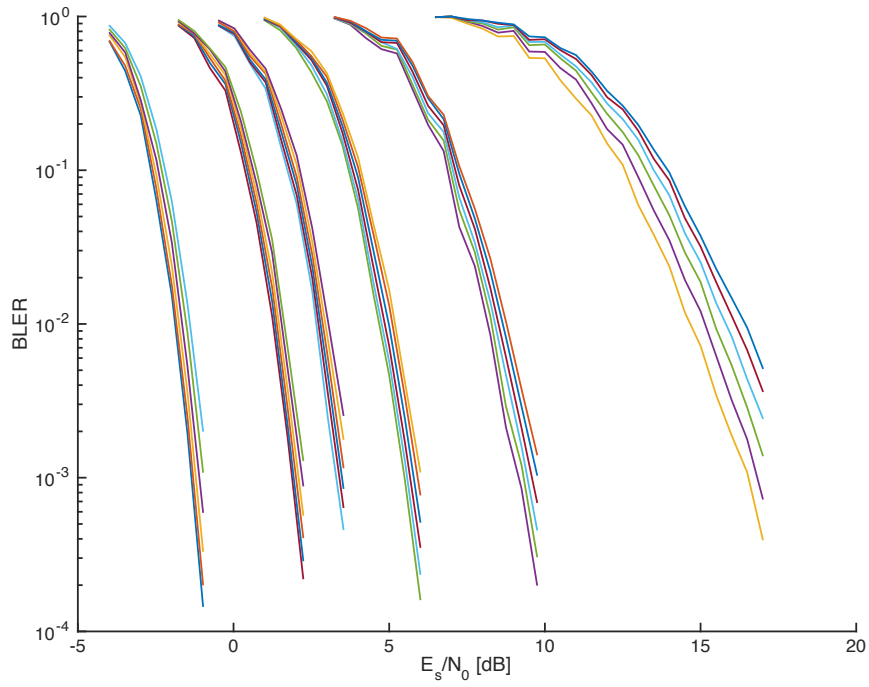


Fig. 4.  $K = 96$ .  $R \in \{1/5, 1/3, 2/5, 1/2, 2/3, 8/9\}$  from left to right.  $L \in \{32, 16, 8, 4, 2, 1\}$  from left to right. QPSK modulation. Uncorrelated narrowband Rayleigh fading channel.  $I = 8$  iterations of scaled-Max-Log-MAP decoding.

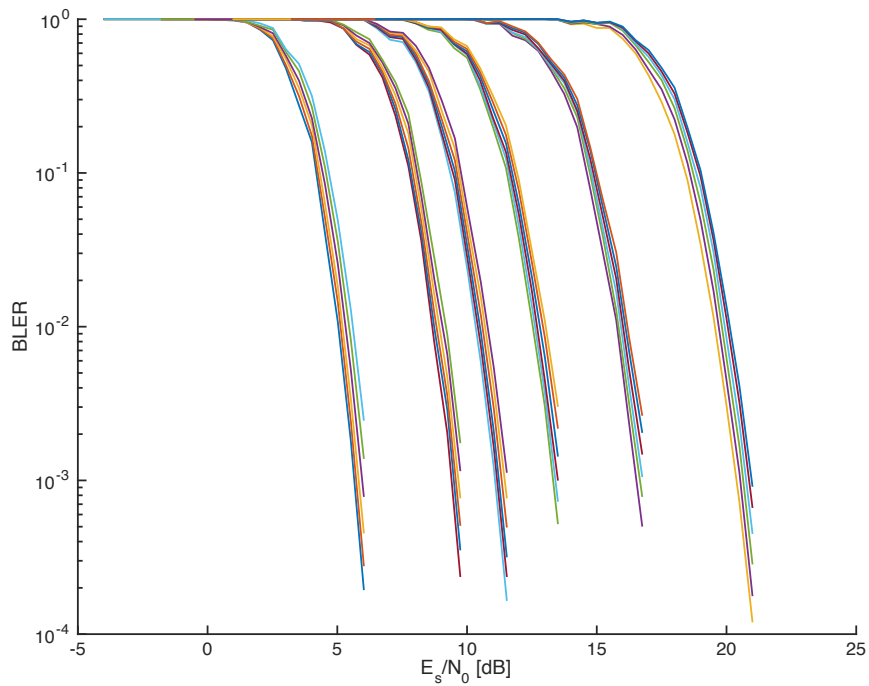


Fig. 5.  $K = 96$ .  $R \in \{1/5, 1/3, 2/5, 1/2, 2/3, 8/9\}$  from left to right.  $L \in \{32, 16, 8, 4, 2, 1\}$  from left to right. 64QAM modulation. AWGN channel.  $I = 8$  iterations of scaled-Max-Log-MAP decoding.

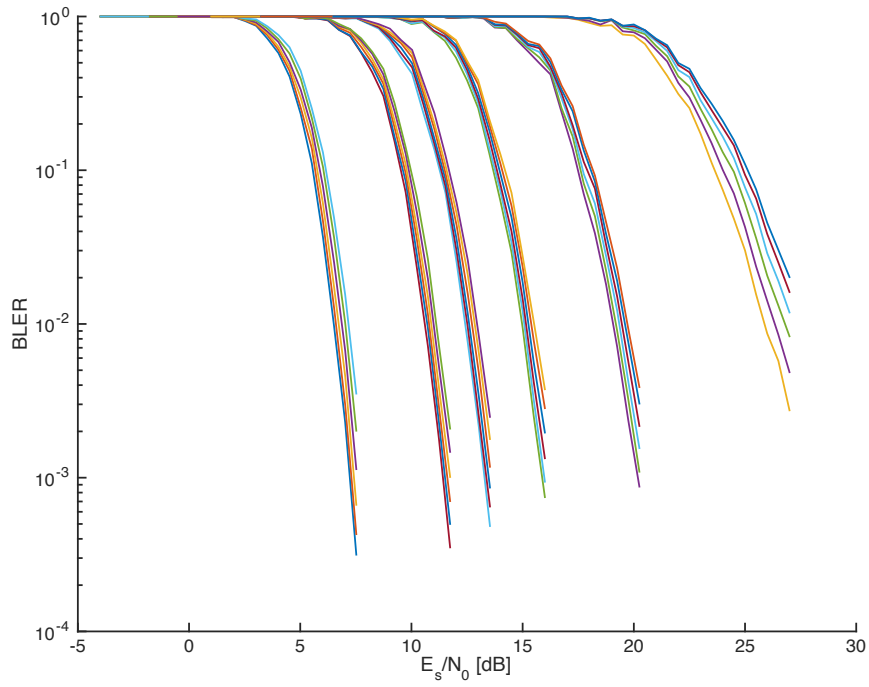


Fig. 6.  $K = 96$ .  $R \in \{1/5, 1/3, 2/5, 1/2, 2/3, 8/9\}$  from left to right.  $L \in \{32, 16, 8, 4, 2, 1\}$  from left to right. 64QAM modulation. Uncorrelated narrowband Rayleigh fading channel.  $I = 8$  iterations of scaled-Max-Log-MAP decoding.

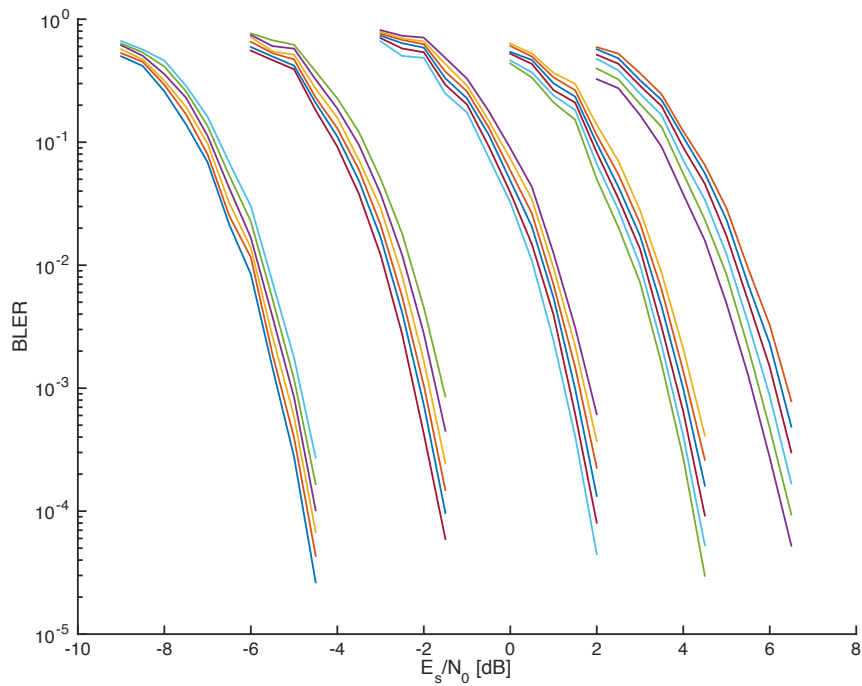


Fig. 7.  $K = 32$ .  $R \in \{1/12, 1/6, 1/3, 1/2, 2/3\}$  from left to right.  $L \in \{32, 16, 8, 4, 2, 1\}$  from left to right. QPSK modulation. AWGN channel.  $I = 8$  iterations of scaled-Max-Log-MAP decoding.

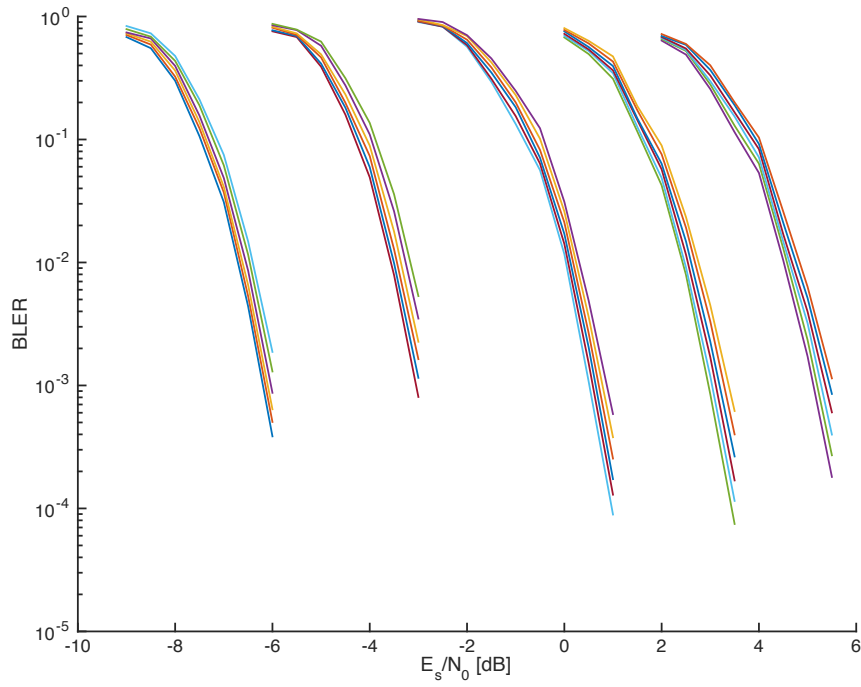


Fig. 8.  $K = 80$ .  $R \in \{1/12, 1/6, 1/3, 1/2, 2/3\}$  from left to right.  $L \in \{32, 16, 8, 4, 2, 1\}$  from left to right. QPSK modulation. AWGN channel.  $I = 8$  iterations of scaled-Max-Log-MAP decoding.

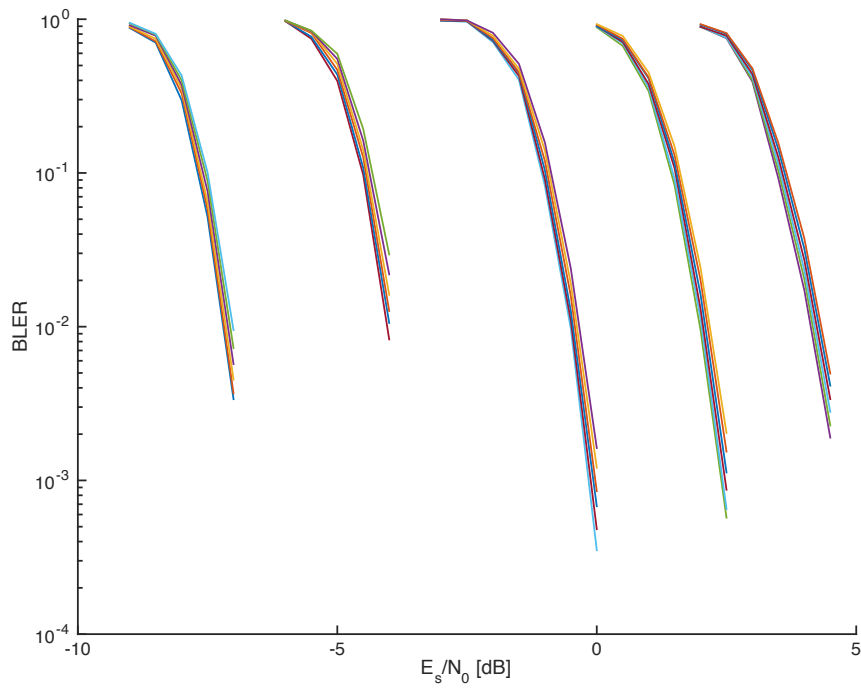


Fig. 9.  $K = 208$ .  $R \in \{1/12, 1/6, 1/3, 1/2, 2/3\}$  from left to right.  $L \in \{32, 16, 8, 4, 2, 1\}$  from left to right. QPSK modulation. AWGN channel.  $I = 8$  iterations of scaled-Max-Log-MAP decoding.

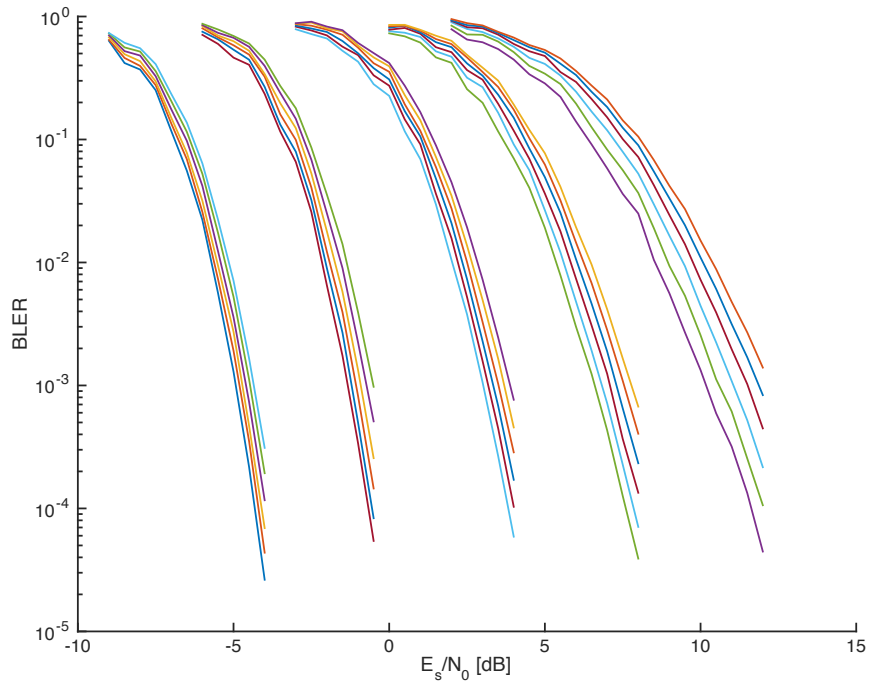


Fig. 10.  $K = 32$ .  $R \in \{1/12, 1/6, 1/3, 1/2, 2/3\}$  from left to right.  $L \in \{32, 16, 8, 4, 2, 1\}$  from left to right. QPSK modulation. Uncorrelated narrowband Rayleigh fading channel.  $I = 8$  iterations of scaled-Max-Log-MAP decoding.

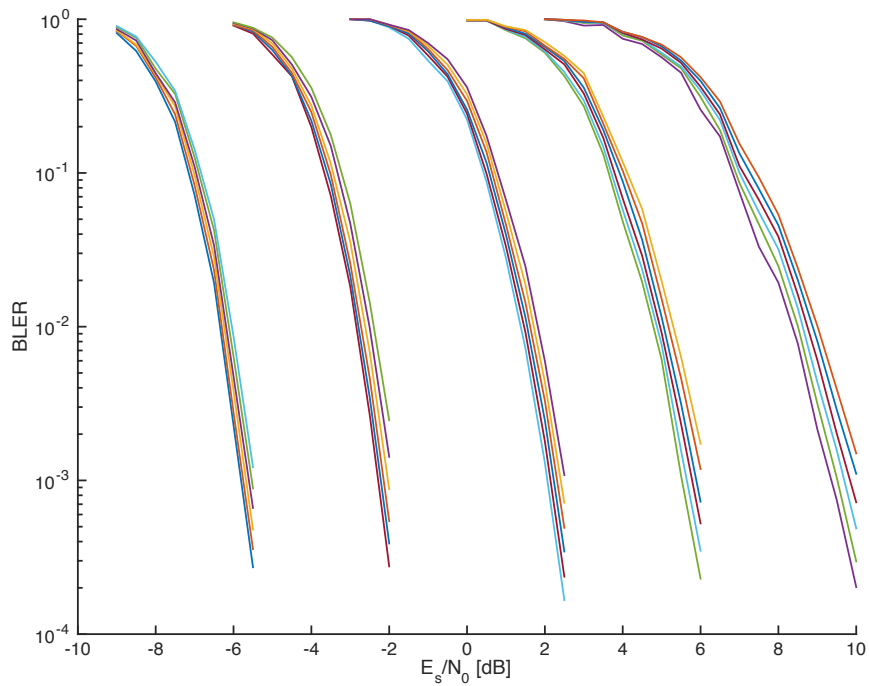


Fig. 11.  $K = 80$ .  $R \in \{1/12, 1/6, 1/3, 1/2, 2/3\}$  from left to right.  $L \in \{32, 16, 8, 4, 2, 1\}$  from left to right. QPSK modulation. Uncorrelated narrowband Rayleigh fading channel.  $I = 8$  iterations of scaled-Max-Log-MAP decoding.

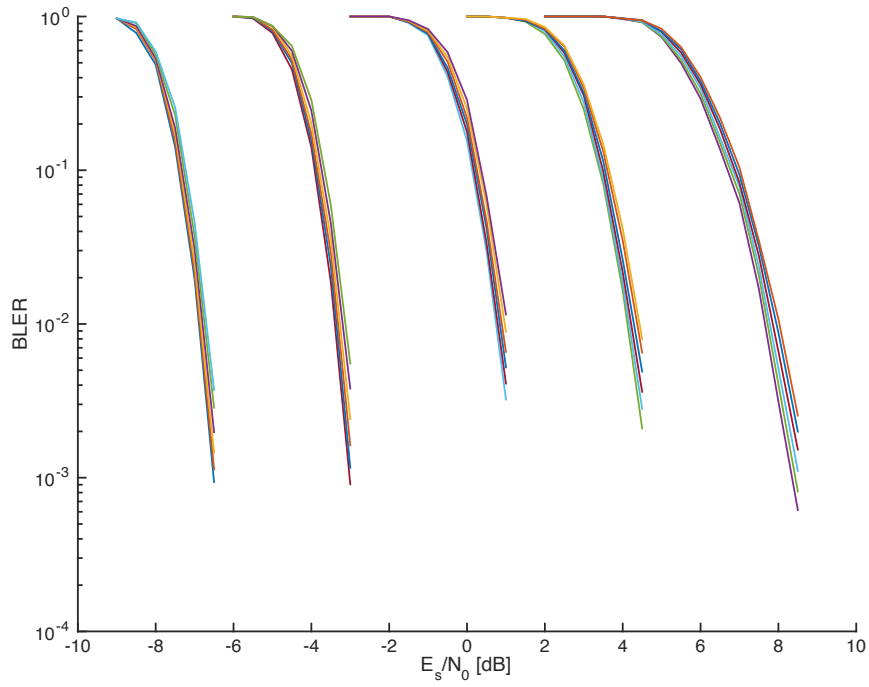


Fig. 12.  $K = 208$ .  $R \in \{1/12, 1/6, 1/3, 1/2, 2/3\}$  from left to right.  $L \in \{32, 16, 8, 4, 2, 1\}$  from left to right. QPSK modulation. Uncorrelated narrowband Rayleigh fading channel.  $I = 8$  iterations of scaled-Max-Log-MAP decoding.

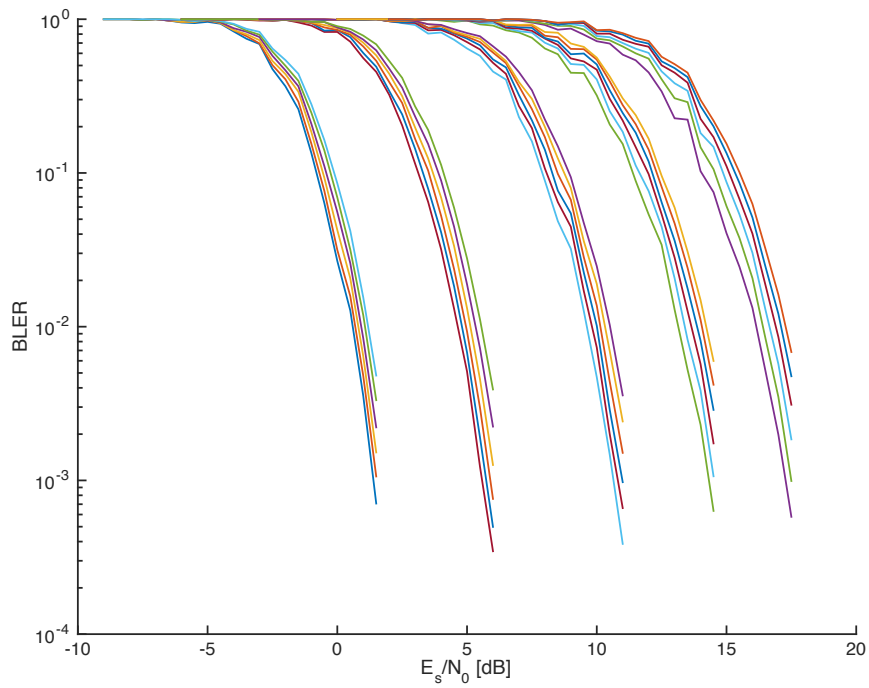


Fig. 13.  $K = 32$ .  $R \in \{1/12, 1/6, 1/3, 1/2, 2/3\}$  from left to right.  $L \in \{32, 16, 8, 4, 2, 1\}$  from left to right. 64QAM modulation. AWGN channel.  $I = 8$  iterations of scaled-Max-Log-MAP decoding.



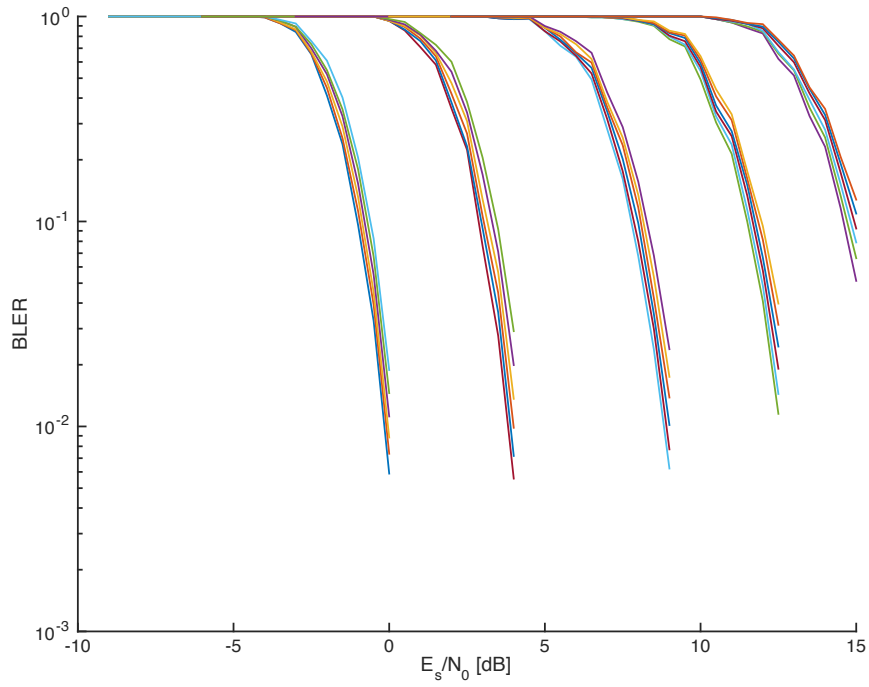


Fig. 14.  $K = 80$ .  $R \in \{1/12, 1/6, 1/3, 1/2, 2/3\}$  from left to right.  $L \in \{32, 16, 8, 4, 2, 1\}$  from left to right. 64QAM modulation. AWGN channel.  $I = 8$  iterations of scaled-Max-Log-MAP decoding.

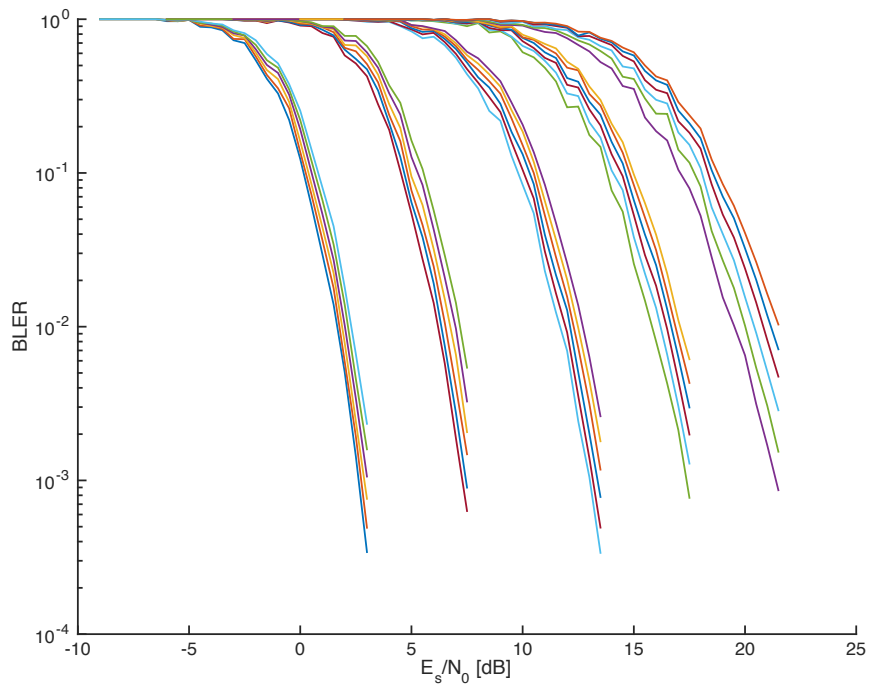


Fig. 15.  $K = 32$ .  $R \in \{1/12, 1/6, 1/3, 1/2, 2/3\}$  from left to right.  $L \in \{32, 16, 8, 4, 2, 1\}$  from left to right. 64QAM modulation. Uncorrelated narrowband Rayleigh fading channel.  $I = 8$  iterations of scaled-Max-Log-MAP decoding.

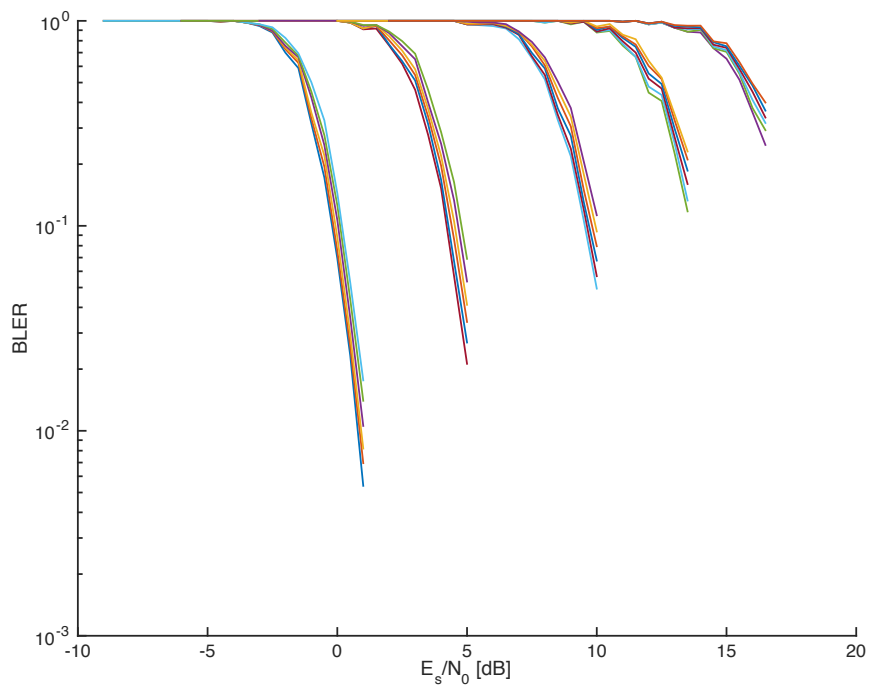


Fig. 16.  $K = 80$ .  $R \in \{1/12, 1/6, 1/3, 1/2, 2/3\}$  from left to right.  $L \in \{32, 16, 8, 4, 2, 1\}$  from left to right. 64QAM modulation. Uncorrelated narrowband Rayleigh fading channel.  $I = 8$  iterations of scaled-Max-Log-MAP decoding.