Dynamic Strain Measurement Using Small Gain Stimulated Brillouin Scattering in STFT-BOTDR

Bo Li, Linqing Luo, Yifei Yu, Kenichi Soga, and Jize Yan

Abstract—A distributed dynamic strain measurement is demonstrated using small gain stimulated Brillouin scattering (SBS) in Brillouin optical time domain reflectometry based on the short-time Fourier transform algorithm. The input power limits, frequency uncertainties for given pulse durations, fiber lengths, and the number of averaging are calculated. The output signal power and the signal-to-noise ratio of the system output are enhanced by SBS. It is found that the signal processing is faster and requires fewer averaging to achieve dynamic sensing performance along the fiber under test. A 60-Hz vibration on a 6-m fiber section at the end of a 935-m fiber is detected with the spatial resolution of 4 m with a sampling rate of 2.5 kS/s.

Index Terms—Brillouin scattering, distributed fiber optic sensors, strain measurement.

I. INTRODUCTION

In recent years, structural health monitoring (SHM) is becoming critical in structural and geotechnical engineering applications [1]. Distributed fiber optic sensing technology, as an effective method of SHM, has the advantages of long sensing distance, distributed sensing information and small sensor size [2]. In particular, Rayleigh and Brillouin based distributed fiber optic sensors have been developed to monitor distributed temperature and strain information for decades [3]–[5]. With the development of smart infrastructures, distributed dynamic measurement of strain can be used in more applications, such as detection of seismic activity, perimeter security and intrusion sensing, traffic monitoring, railway monitoring, and bridge monitoring [1], [6].

Phase-sensitive optical time domain reflectometry (phase-OTDR), the most studied Rayleigh-based dynamic system, has been proved to be capable of detecting strain vibration as accurate as 0.08 με [7]. However, it can only give relative strain between two strain conditions [8], [9]. In addition, phase-OTDR has a limited strain range of as low as 2 με [8], and its linearity between phase and strain is sensitive to the intrinsic phase of the fiber [7], [8]. Brillouin based dynamic systems can measure the absolute strain with a large strain range higher than 10⁴ με. Brillouin based systems demonstrate a slow sampling rate (tens of Hz to a few hundred Hz) and a limited sensing distance from tens of meters to a few hundred meters [10]–[12].

Brillouin optical time-domain reflectometry (BOTDR) has the advantage of single-end access compared with Brillouin optical time-domain analysis (BOTDA). This means that BOTDR can work even if the optic fiber cable is broken halfway. At the construction site, this advantage brings huge benefits for the sensor deployment and testing. However, BOTDR usually needs a large number of averaging due to the weak power of spontaneous Brillouin scattering (SpBS) and the conventional frequency scanning method [13]. Recently, Short-time Fourier transform (STFT) algorithm is replacing the frequency scanning in BOTDR [12], [14]. STFT can reduce the averaging times and realize the dynamic strain measurement [12], [14], whose performance is limited by the signal-to-noise ratio (SNR) that is usually low in BOTDR [13].

Stimulated Brillouin scattering (SBS) is usually avoided in BOTDR, which weakens the injected power along long fiber under test (FUT) (tens of km) and shortens the sensing distance. For many civil engineering applications, however, the sensing distance requirement is reduced to 1km (e.g. the monitoring of piles and buildings), greatly shorter than the achievable sensing distance of BOTDR [13].

The introduction of small gain SBS in BOTDR could improve the power of Brillouin scattering and SNR. The number of averaging then can be reduced and the speed of dynamic strain measurement can be increased as well. In this paper, a small gain SBS based STFT-BOTDR is proposed and tested for the dynamic strain and vibration measurement. The input power limits, frequency uncertainties for given pulse durations, fiber lengths, and number of averaging are calculated, limited by nonlinear effects.

II. POWER LIMITATIONS

The light power of the signal injected into an optic fiber is limited by some parameters. Power depletion can occur if the input power is over the threshold, especially for a distributed fiber optic sensing system [13].

The forward stimulated Raman scattering (SRS), modulation instability (MI), and SBS are dominant factors, which limit the input pulse power in BOTDR [15]. The input threshold for each of these effects is normally defined as the input power when the induced power by the effect is as large as the input power [15]–[17].
with numerical values in (1) and (4) and using SI units, it and SRS thresholds. In fact, by substituting the parameters Fig. 1. It shows that MI thresholds are smaller than SBS SRS input threshold \( P_{th-R} \) is given by [16]

\[
P_{th-R} = \frac{16A_{eff}}{gR L_{eff}}
\]

where \( A_{eff} \) is the effective area of the fiber, \( gR \) is the Raman gain coefficient, and \( L_{eff} \) is the fiber effective length.

The SRS input threshold \( P_{th-R} \) is given by [16]

\[
P_{th=R} = \frac{4\gamma P_0}{\beta_2}
\]

where \( \beta_2 \) is the fiber dispersion coefficient, \( P_0 \) is the input power, \( \gamma \) is the nonlinear parameter by SPM, \( \omega \) is the frequency, and \( \omega_c \) is the critical frequency below which MI gain exists.

The MI gain spectrum is given by: [17]

\[
g_{MI}(\omega) = |\beta_2| \omega_c^2 - \omega^2
\]

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\]

where \( \beta_2 \) is the fiber dispersion coefficient, \( P_0 \) is the input power, \( \gamma \) is the nonlinear parameter by SPM, \( \omega \) is the frequency, and \( \omega_c \) is the critical frequency below which MI gain exists.

The MI threshold \( P_{th-MI} \) is expressed as [15]

\[
P_{th-MI} = \frac{11}{2\gamma L_{eff}}
\]

The SBS threshold \( P_{th-B} \) is quantified by [17]

\[
P_{th-B} = \frac{21A_{eff}}{gB L}
\]

where \( gB \) is the Brillouin coefficient and \( L \) is the interaction length of Brillouin scattering, which equals to the spatial resolution of BOTDR.

When the interaction length of SBS is 4m at 40ns pulse duration, conventional SBS thresholds, MI thresholds and SRS thresholds at different fiber lengths are illustrated in Fig. 1. It shows that MI thresholds are smaller than SBS and SRS thresholds. In fact, by substituting the parameters with numerical values in (1) and (4) and using SI units, it can be derived that \( P_{th-R} = 1.28 \times 10^4/L_{eff}, P_{th-MI} = 3.09 \times 10^3/L_{eff}, P_{th-B} = 67.2/L. \) And hence

\[
P_{th-R} = 4.14 P_{th-MI}
\]

\( P_{th-R} \) is always larger than \( P_{th-MI} \).

\( P_{th-MI} \) is only larger than \( P_{th-B} \) when \( L_{eff}/L < 46 \). For interaction length \( L \) of 4m, \( P_{th-B} \) becomes the dominant threshold when \( L_{eff} < 184m \). However, under this condition, \( P_{th-B} = 16.8W \), which is a high power for normal optic fiber and thermal effects might cause damage on the fiber.

Therefore for \( L_{eff}/L \geq 46 \), \( P_{th-MI} \) is the dominant threshold and determines the maximum input power for BOTDR.

III. ARCHITECTURE OF THE STFT-BOTDR

The BOTDR setup is schematically illustrated in Fig. 2. A narrow-linewidth external cavity laser provides continuous-wave (CW) light at 1550nm, followed by a 50/50 coupler (OC1) which splits the light into two branches. An electro-optic modulator (EOM) modulates one branch (the upper branch in Fig. 2) of the splitted light using a 40ns pulse at a repetition rate of 62.5kHz. The modulated light is amplified by a tunable erbium-doped fiber amplifier (EDFA). The output of the EDFA is filtered by a band pass filter (BPF) before being injected into a circulator. The FUT consists of a 920m standard single mode fiber (section S1) and a 15m single mode strain fiber (section S2 and section S3). Fiber section S2 (about 6m long) is connected to a shaker which produces vibration on the fiber.

The lower branch of the signal from OC1 is an optical local oscillator (OLO), or the reference light, of the coherent detection system. A 700kHz polarization scrambler (PS) is added on this branch to provide random polarization and to reduce polarization fading noise. The reference light OLO and the Brillouin scattered light pass through another 50/50 coupler (OC2) and mix on a photodetector (PD). The PD output signal is downconverted by a 10.5GHz local oscillator, and is electronically filtered and amplified to produce the output signal. The output signal is captured by a digitizer at 5GSa/s and is processed on a computer by the STFT method.

Conventionally BOTDR systems use SpBS instead of SBS. For long sensing distances, SBS can cause large power depletion. For short fiber lengths (<1km for civil engineering applications), small SBS does not generate large power depletion and loose the constraint of the input pulse power threshold. Therefore, small gain SBS can be utilized in short sensing.
fibers to enhance the SNR, which determines the detectability and accuracy of a BOTDR system [19]–[21]. The processing time can be reduced by SNR improvement and reduction of averaging times. The SNR calculation of the sensing system is given as [22]

$$SNR(dB) = 10\log_{10} \left( \frac{2R^2PBPOLO}{4kTB/R_L + 2eRP_OLOB + (RP_OLO)^2RINB} \right) - NF_{E-noise}$$ (7)

where $R$ is the responsivity of the photodetector, $PB$ is the Brillouin scattering power, $POLO$ is the power of the local oscillator branch from the laser, $N$ is the number of averaging, $k$ is the Boltzmann constant, $T$ is the temperature, $B$ is the detected bandwidth, $R_L$ is the load resistance, $e$ is the electron charge, $RIN$ is the relative intensity noise, and $NF_{E-noise}$ is the total noise figure of electronic components.

The power of the OLO branch is much higher than the Brillouin scattering signal. So the shot noise and the RIN noise (the second and the third terms of the denominator) can be approximated to be only related with $POLO$. Therefore, the thermal noise (the first term of the denominator), the shot noise and the RIN noise are independent of the Brillouin scattering power. Furthermore, for the BOTDR setup in this study, a total calculated electronic noise figure (NF) of 2.11dB is added onto the system, which is independent of the Brillouin power as well. The filtered noise by the EDFA seen on the PD can be neglected, as it is much smaller than the shot noise and thermal noise. Hence, the SNR is mainly influenced by the numerator. With the same setup, the increase of the Brillouin scattering power can enhance the numerator of (7) and the SNR.

IV. CALCULATION OF THE SYSTEM PERFORMANCE

SpBS is a linear process. The Stokes and anti-Stokes signals are located symmetrically on both sides of the Rayleigh signal on the optical spectrum with similar power for the SpBS. The SpBS power $P_{SpBS}$ induced in an optic fiber can be calculated as [8]:

$$P_{SpBS} = TPulseS\gamma_{SpBS}P_0$$ (8)

where $TPulse$ is the pulse duration, $S$ is the capture fraction, and $\gamma_{SpBS}$ is the SpBS coefficient.

SBS occurs as the input peak pulse power increases. The SBS is a nonlinear process, whose Stokes signal power is exponentially amplified by increased input power. The Brillouin single-pass gain $GB$ of SBS is expressed as [23]

$$GB = \frac{gB \gamma_0L}{\Delta_1\nu}$$ (9)

Considering the pulse duration adopted in BOTDR, the SBS induced Stokes power by SBS generator on optic fiber can be calculated as [23]

$$PB = \begin{cases} \frac{PNe^{GB}}{\sqrt{\pi \nu_s B T_{pulse} + 2\sqrt{2eGB^2B T_{pulse}}} \times B T_{pulse} > GB/2} \\ \frac{PN e^{-2\Gamma_B T_{pulse} + 2\sqrt{2eGB^2B T_{pulse}}}}{\sqrt{\pi \nu_s B T_{pulse} + 2\sqrt{2eGB^2B T_{pulse}}} \times B T_{pulse} < GB/2} \end{cases}$$ (10)

where $PN$ is the noise that initiates the SBS process and $\Gamma_B$ is the phonon damping rate. $PN$ is usually calculated as a fixed fraction of the injected light power [17]. A typical phonon lifetime $1/\Gamma_B$ of optic fiber is 5ns [17].

As is derived in (7), the Brillouin power is a main factor that influences SNR. The detected spectral resolution ($\delta\nu_B$) of BOTDR is related with SNR, the frequency step ($\sigma$) and the Brillouin bandwidth ($\Delta\nu_B$) as given by [24]:

$$\delta\nu_B = 0.67 \times \sqrt{\frac{\sigma \times \Delta\nu_B}{SNR}}$$ (11)

Hence, a higher SNR leads to a better spectral resolution for the system.

The Brillouin bandwidth is typically about 30MHz (as a function of phonon damping factor) for SpBS and small gain SBS. It becomes narrower with larger Brillouin gain. For the FUT used, the Brillouin bandwidth is about 60MHz.

The dynamic sampling rate of BOTDR is given by

$$fsamp = \frac{1}{T_0N}$$ (12)

where $T_0$ is the period of the input pulse and $N$ is the averaging number. $T_0$ is set to be larger than the total time ($T_{period}$) needed for the pulse to travel into and back from the FUT to eliminate overlap. The shortest time $T_0$ is given by

$$T_0 = T_{period} = \frac{2L_0}{v_g}$$ (13)

where $L_0$ is the fiber length and $v_g$ is the group velocity of light.

Using (7) and (9)-(13), the uncertainty of Brillouin frequency shift (BFS) can be theoretically modelled. Using (4), the MI threshold, i.e. the maximum input pulse power at a given fiber length, can be calculated. Consequently, the best BFS uncertainty at a given spatial resolution, fiber length and sampling frequency can be derived, as shown in Fig. 3. It shows a good spectral resolution with a fiber length below 2km.

From top to bottom, sampling frequencies of vibration are 10000Hz, 1000Hz, 100Hz and 10Hz respectively.

Fig. 3. Calculation of BFS uncertainty at different fiber lengths, spatial resolution and sampling frequency.
V. EXPERIMENTAL RESULTS OF DYNAMIC STRAIN SENSING

The dynamic strain measurement by BOTDR is experimentally verified with 60Hz vibration frequency on a shaker. The EDFA output power is tuned to produce different injected peak pulse power into FUT, at 1.2W, 2.38W and 3.12 W, respectively.

The input pulse is 40ns wide with 16μs period (62.5 kHz repetition frequency), leading to 4m spatial resolution. The output signal is captured by a digitizer for 50ms each measurement and is processed with an averaging number of 25 to derive each profile of BFS, leading to 2.5kHz sampling rate for vibration detection. According to Nyquist principle, a vibration at up to 1.25 kHz can be detected. By setting a faster pulse repetition frequency, the vibration sampling rate can be faster and reach up to 4kHz for 1km fiber under the condition of 100kHz pulse repetition for 10 μs period. The spatial sampling resolution is set to 0.4m by setting the step of STFT, which means that there is a BFS result along the fiber in every 0.4m.

The measured strain vibration over 50ms is shown in Fig. 4, by averaging the derived BFS over fiber section S2. At 3.12W input peak pulse power, a clear sine waveform can be identified. The measured peak-to-peak change of BFS is about 40 MHz, corresponding to 320 με strain change on the fiber. At 1.2W peak pulse power, the shape of the derived waveform is much more distorted. Via sine fitting, the R-square values of 0.75, 0.59 and 0.37 are derived for the peak pulse power of 3.12W, 2.38W and 1.2W, respectively. Spectra of these measured strain vibration profiles in Fig. 4 are demonstrated in Fig. 5. A frequency component at 60Hz can be seen in Fig. 5 for each input power level. Furthermore, the noise level at 1.2W is the highest among the three spectra while the spectra at 3.12W gives the lowest noise level. The experimental result at 3.12W with SBS effect gives a better detection of strain vibration at 2.5kHz sampling rate.

The corresponding profiles of BFS obtained after signal processing are illustrated in Fig. 6. From 850m to 910m, the BFS drops for about 40 MHz due to the initial condition of the fiber. The fluctuation of the measured BFS at peak pulse power of 1.2W is much larger than that at 3.12W. The corresponding frequency uncertainty for each input power level is calculated as the standard deviation of the measured BFS over time. The uncertainties are 5.1MHz, 6.3MHz, and 10.7MHz at 3.12W, 2.38W and 1.2W input peak pulse power, respectively. Fig. 7 shows the measured frequency uncertainties compared by the estimated frequency uncertainties using (7) and (9)-(13).

The vibration of strain is added onto fiber section S2 with about 150MHz (3000 με) pre-strain. The BFS profiles of S2 are enlarged in Fig. 8 (a). The difference in BFS amplitudes among different input levels is caused by the strain vibration. In Fig. 8 (a), the rising edge of BFS for the input peak pulse power of 3.12W is from 922m to 922.4m. The rising edge of detected BFS profile for the case of 2.38W peak pulse power is one sampling point (0.4m) later than that for the case of 3.12W. The rising edge for the case of 1.2W peak pulse power is further delayed. This is the distance error in time domain due to the double-peak effect of the BFS spectra in frequency domain with large BFS change [14]. With a worse SNR in the case of 1.2W, compared with that for the other two profiles, the distance error is more obvious due to the amplitude error of detected BFS by small SNR and the double-peak effect.
The BFS power profiles corresponding to each BFS profile in Fig. 8 (a) is given in Fig. 8 (b). The points in the orange rectangle are the detected Brillouin power of the sampling points on the rising edges of the BFS profiles in Fig. 8 (a). In the cases of 3.12W and 2.38W, a local minimum point can be found in the rectangular in Fig. 8 (b). At this transition point, the double peak effect splits the detected Brillouin power onto two BFS. Hence, the detected power of a single BFS drops. The spectra of the sampling points on the rising edges in Fig. 8 (a) are drawn in Fig. 8 (c). It can be seen in Fig. 8 (c) that the larger the peak pulse power is, the better the SNR is. The distance error effect can be smaller as well accordingly.

The static performance of BOTDR is measured with the shaker off.

With the same settings, the power traces of measured BFS along the FUT at different input power levels are obtained with 25 times of averaging, as shown in Fig. 9. At the input levels below 3.51W, the power attenuation is very small and can be negligible at 1.2W. In the case of 3.51W, the power depletion caused by MI can be clearly observed and it cuts down the SNR at the far end of FUT. This power level (3.51 W) can be seen as the MI threshold for this fiber length [15]. The inset inside Fig. 9 is the measured optical spectra at the far end of the FUT in the cases of 2W, 3.12W and 3.52W, respectively. In the case of 2W, no MI is observed on the spectrum. In the case of 3.12W, a small MI can be seen located on both sides of the signal frequency. This MI spectrum grows significantly when peak pulse power increases to 3.52W. By integrating the MI spectrum, the MI power is 10dB lower than the signal power in the case of 3.12W, whereas the integrated MI power equals to the signal power in the case of 3.52W, which reaches the MI threshold.

The measured Brillouin Stokes and anti-Stokes power, and the calculated SpBS power and SBS power by (8) and (10) are shown in Fig. 10. The measured Stokes power increases much faster than the anti-Stokes power and shows an exponential growth as the input peak pulse power rises. The measured Stokes power matches the calculated SBS power. The measured anti-Stokes power shows a good fit with the calculated SpBS power. As discussed by Boyd [23], the anti-Stokes SBS propagates in positive direction along the fiber and attenuates exponentially. Hence the measured anti-Stokes can be seen as SpBS. Around 1.1W, SBS and SpBS have the same power and SBS becomes dominant as the input peak pulse power continues rising. 1.2W is used as the threshold for small gain SBS in experiment, as demonstrated in Fig. 4. Apparently, even at the input peak pulse power of 4.19W, the SBS power is still below the conventional SBS threshold which is mostly defined to be 100% or 1% of input power. But small gain SBS can be clearly seen under this condition from Fig. 10.
VI. CONCLUSION

The input peak pulse power thresholds at short sensing distance are calculated. At sensing distance within 1km, peak pulse power can be raised up compared with long sensing distance. Small gain SBS is used in BOTDR system to enhance SNR and to achieve fast dynamic strain detection. A small gain SBS based BOTDR system of distributed dynamic strain vibration measurement is established with the capacity to measure as high as 1.25 kHz vibration. A vibration of 60Hz can be raised up compared with long sensing distance are calculated. At sensing distance within 1km, peak pulse power can be raised up compared with long sensing distance. Small gain SBS is used in BOTDR system to enhance SNR and to achieve fast dynamic strain detection. A small gain SBS based BOTDR system of distributed dynamic strain vibration measurement is established with the capacity to measure as high as 1.25 kHz vibration. A vibration of 60Hz can be raised up compared with long sensing distance are calculated. At sensing distance within 1km, peak pulse power can be raised up compared with long sensing distance. Small gain SBS is used in BOTDR system to enhance SNR and to achieve fast dynamic strain detection. A small gain SBS based BOTDR system of distributed dynamic strain vibration measurement is established with the capacity to measure as high as 1.25 kHz vibration. A vibration of 60Hz can be raised up compared with long sensing distance are calculated. At sensing distance within 1km, peak pulse power can be raised up compared with long sensing distance.

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