Soft Colloidal Arrangements of Iron Oxide Nanocube Building Blocks: the Key to Improving Magnetic Hyperthermia Performance

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Abstract

Magnetic hyperthermia (MH) based on magnetic nanoparticles (MNPs) is a promising adjuvant therapy for cancer treatment. Particle clustering leading to complex magnetic interactions affects the heat generated by MNPs during MH. The heat efficiencies, theoretically predicted, are still poorly understood because of lack of the control of the fabrication of such clusters with defined geometries and thus their functionality. This study aims to correlate the heating efficiency under MH of individually coated iron oxide nanocubes (IONCs) vs. soft colloidal nanoclusters made of small groupings of nanocubes arranged in different geometries. The controlled clustering of alkyl stabilized IONCs is achieved here during the water transfer procedure by tuning the fraction of the amphiphilic copolymer, poly(styrene-co-maleic anhydride) cumene terminated, to the nanoparticle surface. It is found that increasing the polymer-to-nanoparticle surface ratio leads to the formation of increasingly large nanoclusters with defined geometries. When compared to the individual nanocubes, we show here that controlled grouping of nanoparticles—so-called “dimers” and “trimers” comprised of two and three nanocubes, respectively—increases

specific absorption rate (SAR) values, while conversely, forming centrosymmetric clusters having more than four nanocubes leads to lower SAR values. Magnetization measurements and Monte-Carlo based simulations support the observed SAR trend, and reveal the importance of the dipolar interaction effect and its dependence on the details of the particle arrangements within the different clusters.

**Keywords:** controlled colloidal clustering, iron oxide nanocubes, specific absorption rate, poly(styrene-co-maleic anhydride), magnetic hyperthermia, annealing, Monte-Carlo simulation

Magnetic hyperthermia (MH) is a novel non-invasive treatment, now undergoing clinical trials on patients with brain or prostate tumors,\(^1\) that exploits the heat generated by magnetic nanoparticles (MNPs) when exposed to an alternating magnetic field.\(^2\)–\(^4\) The use of MNPs as heat mediators in MH treatment impairs the monitoring of the tumor progression by magnetic resonance imaging (MRI)\(^1\) since it requires a substantial dose of MNPs to achieve the clinically relevant heating efficiency, incompatible with MRI imaging. Although several research studies have aimed at the design of optimal heat mediators that would allow reduction of the MNP dose, while maintaining the required heating performance, the low heating efficiency remains among the current limitations of MNPs used in clinical trials.\(^5\)–\(^7\) In parallel to the direct synthesis of nanoparticles with optimized heat performances, the research focus was also directed towards the assembly of the same building blocks into controlled clusters in order to maximize their heating performance.\(^8\)–\(^11\) The aim behind this strategy, is to achieve higher magnetic hyperthermia performances of defined MNPs used as building blocks by controlling the specific configuration of the MNPs in the final assembly.

The heating efficiency of the magnetic nanoparticles is expressed by their specific absorption rate (SAR). The SAR value is defined as the power absorbed per mass of the heat mediator in the case of MNPs. SAR depends on various factors, among them: (i) the applied magnetic field characteristics (frequency and amplitude), (ii) the intrinsic magnetic properties (i.e. saturation magnetization, anisotropy) that depend on MNP features such as size, shape, composition, and arrangement, and (iii) the characteristics of the dispersing medium (i.e. viscosity, concentration, heat capacity).

Controlled or uncontrolled aggregation in a centrosymmetric 3D configuration—a bead-like assembly—was reported to lower SAR values.\(^12\)–\(^15\) On the contrary, controlled aggregation in chain-like structures driven by anisotropic interactions of magnetic nanoparticles was reported to improve SAR values. For instance, bacterial magnetosome chains that are \(ca.\) 50 nm cubic-shape iron oxide nanoparticles individually coated with a lipid shell—naturally aligned in chain-like morphologies on
protein filaments—are currently state-of-the-art in terms of hyperthermia performance.\textsuperscript{16} Similar findings were demonstrated by Martinez-Boubeta \textit{et al.}\textsuperscript{8} who have investigated the influence of dipolar interactions on the hysteresis loops in magnetic nano-assemblies by means of the Monte-Carlo simulations. Their Monte-Carlo computational model predicted an increase in the area of the hysteresis loop by increasing the chain length as the key factor to improve SAR values. Alongside their mathematical calculations, their experimental calorimetric measurements—on 44 nm ferromagnetic spherical magnetite nanoparticles forming micrometer long chains in agarose upon applying 0.12 T magnetic fields—demonstrated the importance of chain alignment on the heating efficiency.\textsuperscript{8}

Their model also showed how centrosymmetric assemblies comprised of eight nanoparticles led to smaller hysteresis loops compared to the corresponding chain like configuration.\textsuperscript{8} This indicates the importance of obtaining elongated assemblies of MNPs. Magnetic dipole-dipole interactions leading to the formation of chain-like structures under the action of external magnetic fields were also exploited by other groups to showcase the effect of the arrangement at the nanoscale on magnetic hyperthermia. Compared to the non-aligned samples, 40 nm magnetite nanoparticles—dispersed in agarose gel matrix and magnetically aligned in 40 mT fields—presented SAR values enhanced by a factor of two.\textsuperscript{10}

However, only relatively few studies have investigated the formation of particle arrangements of defined geometries—1D, 2D, or 3D structures—colloidally stable in a solution without the application of an external field, and their correlation with magnetic hyperthermia measurements. In the work of Andreu \textit{et al.},\textsuperscript{9} in order to build clusters of different geometries, different encapsulating materials were exploited. Magnetic nanoparticles were embedded in silica nanoworms to obtain 1D chain arrangements, while poly(D,L-lactide-co-glycolic) acid (PLGA) was used for small 2D grouping of nanoparticles enwrapped in polymer spheres, showing that their magnetic properties and the hyperthermia response were governed by nanoparticle arrangement. The 1D and 2D nano-objects displayed an improved SAR behavior compared to single nanoparticles or agglomerates of NPs.\textsuperscript{9}

Besides using PLGA polymer, known to be biocompatible and non-cytotoxic,\textsuperscript{17} also many other polymers including dioleate-modified polyethylene glycol,\textsuperscript{18} poly(\(\epsilon\)-caprolactone)-b-poly(ethylene glycol) (PCL-b-PEG),\textsuperscript{19} poly(trimethylammonium ethylacrylate methyl sulfate)-b-poly(acrylamide),\textsuperscript{20} poly(ethylene oxide-b-acrylate) (H\(_2\)N-PEO-b-PAA),\textsuperscript{21} poly(\(lactic\)-co-glycolic acid)-b-poly(ethylene glycol) (PLGA-b-PEG),\textsuperscript{22} and even triblock copolymers such as poly(ethylene imine)-b-poly(\(\epsilon\)-caprolactone)-b-poly(ethylene glycol) (PEI-b-PCL-b-PEG)\textsuperscript{23} were used in the literature to form polymeric colloidal clusters of nanocrystals. These soft colloidal nanocrystal
clusters—a term introduced by Bakandritsos et al.\textsuperscript{24}—have been evaluated as contrast agents for MRI, while no hyperthermia studies have been reported.\textsuperscript{18-23}

In this study, by using one type of nanocube, one specific amphiphilic polymer and by adjusting the polymer-to-nanoparticle parameter we controlled the formation of colloidally stable (i) single particles, (ii) dimer and trimer assemblies, and (iii) centrosymmetric structures. We then studied the evolution of SAR with the size and spatial arrangement of clusters and the corresponding magnetic parameters of the various soft colloidal clusters. The experimental SAR results are here supported by the theoretical simulations carried out by means of a kinetic Monte-Carlo computational model on the clusters. We demonstrate that the primary factor responsible for the enhancement of SAR is in fact not the variation of $M_S$, but rather the dipolar interaction effect induced by the arrangement of nanocubes into dimers, trimers, and centrosymmetric clusters. This work clearly shows that when working with one single type of MNP while promoting the anisotropic assembly of the MNPs, structured nanomaterials with enhanced heat performance are obtained.

**Results and discussion**

The overall clustering process is schematically shown in Figure 1I. FeO/Fe\textsubscript{3}O\textsubscript{4} core-shell iron oxide nanocubes\textsuperscript{25} (IONCs, with an edge length of 20.2 ± 1.5 nm, Figure S1) were first used in this study. The choice of core-shell nanocubes was dictated by their magnetically non-interacting nature, alongside their initial stability in THF as evidenced by the clear THF solution. Both conditions were considered prerequisites for a successful clustering protocol. Attempts done with non-completely soluble nanoparticles were not successful (data not shown).

In a typical clustering procedure for obtaining centrosymmetric clusters, taken as an example, as-synthesized oleic acid coated IONCs ($m_{Fe} = 0.23$ mg) were dispersed in 10 mL tetrahydrofuran (THF) together with the amphiphilic polymer poly(styrene-\textit{co}-maleic anhydride) (PScMA), cumene terminated ($M_n = 1600$ g/mol), at a ratio of 66 polymer chains/nm\textsuperscript{2} of nanoparticle surface. Subsequently, the addition of 1 mL H\textsubscript{2}O by a syringe pump (0.5 mL/minute), while sonicating the NPs-polymer solution in an ice bath followed. During this step, the solution had to remain clear as the water transfer would fail if the THF/H\textsubscript{2}O mixture became turbid during the water addition.

Interestingly, in the H\textsubscript{2}O/THF mixture (\textit{ca.} 1.5 mL) the nanocubes were not yet clustered; they still appeared as single nanocubes on the TEM grid (data not shown) and the solution was clear. As the last 0.5 mL of THF evaporated the solution became turbid. After full evaporation of THF the IONCs were already clustered and a thin layer of polymer was clearly evident on the clusters as checked by TEM characterization, even before the CHCl\textsubscript{3} addition (Figure S2a). This data suggests that the clustering was favored by the change in solubility of polymer and nanocubes as soon as the
THF evaporated in the THF/water mixture. The chloroform addition step promoted the extraction of the excess of polymer/surfactant molecules from aqueous phase into organic phase. This was clearly evident as a milky layer of polymer was found at the interface between CHCl₃ and water (Figure S3) and after CHCl₃ addition, no more extra polymer was visible on the TEM grid (Figure S2b).

To set the clustering protocol, different parameters were investigated systematically. This list included the rate of THF evaporation, the ratio of water to THF, the total solution volume, and the amount of polymer. However, the main parameter that allowed a fine tuning of the cluster size and the configuration of the nanoclusters was the number of molecules of amphiphilic polymer, poly(styrene-co-maleic anhydride) per square nanometer of particle surface. This ratio varied between 16.5 and 66 molecules/nm² corresponding to a change in size and configuration of the formed clusters. With an increase in polymer amount, the degree of clustering increased as seen in the TEM micrographs in Figure 1. As judged by the distribution of nanoparticles on the TEM grid and from the inter-particle distance (Figure 1A), with a ratio of 16.5 molecules of polymer/nm², the majority of the nanocubes were individually coated, while by doubling the amount of polymer to 33 molecules/nm², dimers and trimers were formed (Figure 1B). In this specific case, the dimer and trimer arrangements were even more evident by looking at a collection of TEM images in which isolated groups of two or three nanocubes were clearly seen. Often, on the same grid, different dimers and trimers were observed (Figure 1E-H). At 50 and 66 molecules of polymer/nm² the number of nanocubes per cluster increased respectively, forming more tetramers or grouping of centrosymmetric clusters containing more than 5 nanocubes each (Figure 1C and 1D). The corresponding hydrodynamic volume distributions, as measured by dynamic light scattering (DLS), also reflected the size increase from ca. 40 to 100 nm (Figure 2). The mean hydrodynamic diameters by volume were 38 ± 2 nm (PDI 0.12), 51 ± 3 nm (PDI 0.14), 68 ± 4 nm (PDI 0.08), and 99 ± 2 nm (PDI 0.07) for 16.5, 33, 50 and 66 PScMA/nm² respectively. Note that the very low polydispersity index (PDI) values indicate a homogeneous distribution of the clusters obtained. Once formed the cluster solutions could be kept for very long time (more than a year) without showing any sign of aggregation (DLS and TEM characterization were the same as for freshly prepared samples).
Figure 1: Scheme of the clustering protocol using 20 nm core-shell iron oxide nanocubes. Representative TEM micrographs of IONCs@PScMA in water and just after they have been prepared at a ratio of (A) 16.5, (B) 33, (C) 50 and (D) 66 polymer chains/nm² of particle surface. (E-H) a collection of TEM images at higher magnification of dimers and trimers formed at the ratio of 33. (I) Schematic representation of the formation of soft colloidal nanoclusters.
Figure 2: Tuning the mean hydrodynamic diameter of clusters by different polymer amounts. Volume distribution of hydrodynamic size $d_H$ of soft colloidal clusters measured in water starting from 20 nm IONCs. The $d_H$ was adjusted between 38 and 99 nm. No aggregation of clusters was detected as PDI values were between 0.07 and 0.14 (see inset).

Given that the hydrodynamic diameter obtained was an average value, and that TEM images provide only qualitative images of the assemblies, in an attempt to quantify the percentage of individually coated nanoparticles, dimers, trimers and clusters with more than four nanocubes for the different samples, we ran a statistical image analysis—using ImageJ software. Numerous TEM micrographs were analyzed in order to obtain a statistical distribution of individually coated nanocubes vs. 1D and 2D constructs (dimers and trimers, respectively) vs. 3D constructs (bigger colloidal nanoclusters with $n \geq 4$) so that at least 250 objects were analyzed for each sample (Figure S4). We focused on the 3 available samples—at 16.5, 33 and 66 polymer molecules/nm$^2$ samples (from now on they will be referred to as 16.5PScMA, 33PScMA, and 66PScMA, respectively) as on those samples further SAR measurements and magnetic characterizations were carried out. For sample 16.5PScMA, 255 objects were studied, corresponding to a total of 342 individual nanocubes, of which 66% were individually coated, 28% were dimers, 4% were trimers and 2% were bigger clusters (Figure 3a). For sample 33PScMA, when doubling the amount of polymer with respect to 16.5PScMA sample, out of 254 objects analyzed (Figure S4)—corresponding to 493 IONCs—70% consisted of an equal population of dimers and trimers (Figure 3b). The 30% remaining objects were
19% individually coated NPs and 11% 3D arrangements. For sample 66PScMA, when still doubling the polymer amount with respect to sample 33PScMA, almost only 3D clusters were obtained, representing 86% (Figure 3c) of the 259 objects inspected—corresponding to more than 1000 NPs (Figure S4). The remaining 14% of sample 66PScMA was equally distributed between single particles (5%), dimers (5%), and trimers (4%). Overall, we could statistically confirm that by increasing the polymer amount from 16.5, to 33, and further to 66 molecules of PScMA/nm$^2$ of NP surface, the resulting clusters evolved from a major population of individually coated nanoparticles to dimers and trimers and, lastly, to groups of more than 4 nanocubes per unit.

Figure 3: Statistical analysis of fractions of different objects for samples (A) 16.5PScMA, (B) 33PScMA, and (C) 66PScMA indicated the presence of (A) 32% 1D and 2D constructs (28% dimers and 4% trimers) in sample 16.5PScMA, (B) a majority of 70% (35% dimers and 35% trimers) in sample 33PScMA, and (C) only 10% (5% dimers and 5% trimers) 1D and 2D structures in sample 66PScMA, with a majority of clusters with a number of nanocubes higher than 4 (86%).

**Thermogravimetric analysis**
The nanoparticle surfactant effect: In addition to the evaporation rate of THF, polymer amount and initial stability of the nanocubes in THF, another crucial parameter for the successful water transfer and cluster formation was the surfactant amount associated with the nanocubes. We observed differences in the clustering procedure when changing the batch of core-shell IONCs (20.2 ± 1.5 nm), to a batch with a similar edge length of 20 ± 2 nm (Figure S5). Indeed, sometimes even if the initial cubes were soluble in THF, as for other batches of nanocubes, the procedure did not result in cluster formation. In order to elucidate the correlation between different batches of nanocubes and the clustering procedure, we carried out thermogravimetric analysis (TGA) on the two batches of nanocubes, as the amount of surfactant molecules, oleic acid (OA), stabilizing the nanocubes may have also contributed to cluster formation.

The thermogravimetric analysis of the IONCs sample dispersed in CHCl₃ (sample A)—for which the clustering process worked straightforwardly—showed a first weight loss of 26.4 wt% in the temperature range from 150 to 300 °C and a second weight loss of 31.2 wt% from 300 to 400 °C (Figure 4a, blue line). The first transition is mainly attributed to unbound or physisorbed OA, while the second transition is related to the oleate molecules chemisorbed on the particle surface. As a comparison, the TGA degradation profile of oleic acid is plotted showing a weight loss of ca. 90 wt% at 300 °C (Figure 4a, violet line), supporting the claim that the first weight loss is due to free oleic acid.

It should also be noted that that for this batch of IONCs the amount of oleate chemisorbed to the surface of the IONCs—ligand density (ρ_l)—was much higher than the theoretical 5 ligands/nm². The calculated ligand density was instead 27 ligands/nm², if only the second weight loss seen in TGA was considered. If instead the total weight loss of surfactant is considered—both decomposition steps between 150 and 400 °C—the surfactant density was 50 ligands/nm², with a 46% and 54% fraction corresponding to free oleic acid and oleate bound to the surface of the NPs, respectively. These results suggest a multilayer coating of surfactant on the particle (likely promoted by the hydrophobic interaction between the OA alkyl chains).

Next, TGA analysis was carried out on the core-shell IONCs batch before and after the washing step as for this batch the clustering process did not work initially (Figure 4b, sample B as-synthesized), but it did work after washing the excess of surfactant (Figure 4b, sample B washed once). For the as-synthesized sample in CHCl₃ (Figure 4b), the organic layer accounted for a mass loss of 79.6 wt%, with 11.5 wt% corresponding to free oleic acid in solution and 68.1 wt% to oleate molecules (Figure 4b, red curve). The excess amount of oleate was due to a change in the amount of OA used for the synthesis of this batch. Interestingly, after centrifuging the sample in a mixture of chloroform: methanol (1:3 v/v), on the final sample the total oleic acid amount associated to the
IONCs was assessed to be 54.8 wt% of which the oleate amount decreased to 43.3 wt% (Figure 4b, green curve). These results suggested that the amount of chemisorbed OA was crucial to the cluster formation: when too high no clusters were formed suggesting that the polystyrene branches of the amphiphilic PScMA could not intercalate with the surfactant layer, as the surfactant molecules were tightly packed close to one another. After the washing, as some of the OA molecules were stripped from the external layers, the decrease in the amount of chemisorbed OA facilitated the NP interaction with the polymer and the water transfer proceeded. It is worth mentioning that there is a range of concentration of OA per nanoparticles in which the protocol works. We noticed, for instance, that an additional second washing step on the same sample did not result in cluster formation anymore. This indicated that by decreasing the chemisorbed OA amount from 124 (as-synthesized sample) to 29 (sample washed once) ligands/nm², the hydrophobic tail of the polymer, the PS units, could intercalate with the alkyllic chain on the nanocube, while having even less oleate molecules, the interaction was no longer favorable.

Overall, the TGA data suggest that the balance between the oleate molecules chemically bound to the surface of the IONCs and the oleic acid molecules physisorbed or intercalated between the oleate molecules—forming additional outer layers of surfactant—was a crucial parameter to be controlled in order to obtain soft colloidal clusters.

![Figure 4](image_url)

*Figure 4:* (a) TGA weight-loss profiles of oleic acid capped IONCs (sample A: blue curve) and free oleic acid (violet curve) performed in air. The first weight loss in the region between 150 and 300 °C
corresponded to free oleic acid in solution, while the second weight loss in the region between 300 and 400 °C corresponded to oleate chemisorbed to the surface of the IONCs. (b) TGA weight-loss profiles of a new batch of as-synthesized oleic acid capped IONCs (sample B: red curve) and sample B after washing to remove excess of oleic acid (green curve). On sample B, before washing no clusters were obtained. Upon one washing, the amount of oleate decreased from 68.1 wt% to 43.3 wt%, re-establishing the cluster formation on sample B.

It is interesting to note that the arrangement in chain configurations of nanoparticles has been observed in many phenyl-based polymers. Polystyrene has been used for instance to cluster cobalt ferrite nanoparticles in chain assemblies of micrometer chain length and the same polymer has also been used to chain gold nanorods in a tip-to-tip configuration. Similar to the latter work, in our system the cumene terminated polymer and the nanocubes are both well soluble in THF, however, the addition of water as an antisolvent induces a different precipitation of the hydrophobic poly(styrene) moieties of the cumene terminated polymer and the oleic acid capped nanocubes. We might speculate that the polymer–polymer interaction is more favorable compared to the polymer-nanoparticle interaction, likely because of their difference in solubility in the solvent mixture. Given that the nanocubes have multiple layers of OA, this shell (OA bears a carboxyl moiety) might provide a greater solubility of the IONCs compared to that of the amphiphilic PScMA in the THF/water mixture. This would likely provide a higher nanocube-nanocube affinity and drive the slow arrangement of the nanocubes in chains while the polymer molecules would tend to interact through phenyl rings. If this is the case, we would also explain why here and in contrast to other works, an increase in the polymer amount favors the clustering rather than the individual coating of nanocubes. If we compare our procedure to a previously reported procedure, in which the authors reported that a high polymer/NP ratio favored the formation of discretely encapsulated MNPs, whereas at low ratio particle clustering was enforced by the relative depletion of polymer, we can underline that the main difference was the type of amphiphilic polymer chosen. Indeed, while we opted for the copolymer poly(styrene-co-maleic anhydride), in the work of Pössel et al. the triblock polymer poly(ethylene imine)-b-poly(ε-caprolactone)-b-poly(ethylene glycol) was used for cluster formation.

Finally, it should be noted that our cluster procedure can be extended to other core-shell systems prepared by other methods (see for instance Figure S6 for another core-shell nanocube having a similar edge size and Figure S7 for iron oxide nanoparticle of 18 nm diameter and spherical shape). However, the procedure did not work when using Fe₃O₄ nanocubes that did not have a core-shell structure. For instance, Fe₃O₄ nanocubes of 20 nm were not soluble in THF, the initial solvent, and therefore the procedure could not be tested. For 13 nm Fe₃O₄ nanocubes, being superparamagnetic
and thus non interacting, although the particles were soluble in THF, despite changing several reaction parameters in order to optimize them, only deformed groupings of nanocubes were obtained, but no dimers and trimers were properly formed (data not shown).

**Magnetic properties**

**Hyperthermia.** The SAR measurements were performed on clustered samples that were prepared starting from core-shell nanoparticles which were subsequently aged for one year at room temperature. Under these conditions the samples slowly changed from a core-shell structure to a quasi one-phase material. The X-ray diffraction pattern (XRD) pattern of the aged nanocubes is shown in Figure S8. The major reflections coincide with Fe$_{2.96}$O$_4$ (ICSD collection code: 82443). There exists 10-15 w% FeO phase (Fe$_{0.942}$O, ICSD: 24696) in the nanocubes.

The SAR values were obtained at the highest frequency (302 kHz) and magnetic field (23.8 kA/m) of the instrument (nB Nanoscale Biomagnetics DM100 series) as the Fe concentration of the samples was in the range of 0.65 - 3.2 g/L on a volume of 200 µL. The values were 213 ± 9, 253 ± 10, and 184 ± 8 W/g$_{Fe}$ for nanoconstructs formed at ratios of 16.5, 33 and 66 molecules PScMA/nm$^2$ of particle surface. By plotting (Figure 5) the trend observed for the different samples, we registered an increase in SAR for the mixture of dimers and trimers (33 molecules polymer/nm$^2$—Figure 1B, 1E-H) compared to both mixtures of individually coated nanoparticles (16.5 molecules polymer/nm$^2$—Figure 1A) and mixtures of soft colloidal clusters with n$\geq$4 (66 molecules polymer/nm$^2$—Figure 1D), with ‘n’ being the number of particles per cluster. When looking at the statistics, we could confirm that on the sample in which we have measured the highest SAR value—the 33 PScMA sample—the percentage of dimers and trimers was statistically higher. Individual nanocubes and clusters with n$\geq$4 were instead the predominant population for the samples 16.5PScMA and 66PScMA, respectively.

As already reported by other groups, our data also suggests that centrosymmetric clusters significantly reduced the SAR value of the nanocubes (Figure 5). The inset in Figure 5 shows results of calculations based on the kinetic Monte-Carlo modelling (see methodology section), which recovers the behavior observed experimentally for the different cluster types. Obtaining the agreement between the simulation and experiment (within the error bar) required setting the anisotropy constant value to $K = 5 \times 10^4$ erg/cm$^3$. The single-particle values of the saturation magnetization were taken directly from the experimental data and corresponded to $M_s$ of 367, 407, 407, 314 emu/cm$^3$ for the ensembles of, respectively, non-interacting, 2-particle, 3-particle, and 6-particle clusters. The low value of $K$ suggests that dipolar interactions dominate the anisotropy field of particles, as will be discussed later.
Figure 5: SAR values for soft colloidal nanoclusters after 1 year aging time, formed at ratios of 16.5, 33 and 66 molecules PScMA/nm$^2$ of particle surface ($f = 302$ kHz, $H = 23.8$ kA/m). A higher SAR value was recorded for dimers and trimers compared both to individual IONCs and clusters with $n \geq 4$. Clustering the IONCs in centrosymmetric bead-like structures decreased their heating performance. Each experimental data point was calculated as the mean value of at least three independent measurements, with error bars indicating the mean deviation. Inset: SAR values obtained from kinetic Monte-Carlo modelling of the structures as described in the text, reproducing the observed experimental trend within the error bar. Inter-particle spacing for the simulation has been set to 1 nm gap as measured on the TEM images.

**Magnetization measurements**

To gain a deeper knowledge about the magnetic properties of the fabricated constructs and also in an attempt to correlate static magnetic properties with dynamic features, here specifically the SAR, applied field and temperature dependent magnetization measurements were carried out on all three samples. The magnetization hysteresis loops $M$ vs. $H$ recorded at 298 K and 10 K are shown in Figure 6. The formation of dimers is expected to enhance a collective magnetic behavior owing to
the anisotropic alignment of nanoparticles and results in a significant enhancement of the hysteresis loop area. On the contrary, larger clusters \((n \geq 4)\), and also trimers, experience a demagnetization effect due to their specific particle configuration with the tendency to form flux closure domains, thus causing a weakened coupling to external magnetic fields, \textit{i.e.} narrow hysteresis loops (see also our simulations Figure S13). At \(T = 298\) K both single nanoparticles and dimers and trimers reveal an identical remanent magnetization \(M_r\) and coercive field \(H_c\) (Figure 6b), while \(M_r\) and \(H_c\) decrease significantly in the 3D clusters (clusters with \(n \geq 4\)). These results are supported by our numerical simulations, which show significant differences in the shape of dynamic hysteresis loops for different particle cluster structures (see Figure S13 and S14). Different behavior is observed at 10 K where the variation of \(H_c\) and \(M_r\) with clustering state vanishes. This suggests that the increased anisotropy field and coercivity at the low temperature is sufficient to overcome the effects of interactions: an observation consistent with the interpretation of the room temperature magnetic properties in terms of different cluster structures. We also confirmed by using numerical simulations that increasing the values of \(M_S\) in magnetic nanostructures can lead to an improved overall heating performance, however, the dependence is non-trivial and significantly dependent on the particle cluster geometry (Figure S15-S16).

It is tempting indeed to assume that large \(M_S\) values give rise to higher SAR since given that the maximum magnetization of the system is directly proportional to \(M_S\) and then, intuitively, higher \(M_S\) should imply a higher hysteresis loop area. However, a simple physical picture based on the Stoner-Wohlfarth particle theory suggests that given that the coercive field is inversely proportional to \(M_S\), \textit{i.e.} \(H_c \propto 1/M_S\), and the hysteresis loop area is related to \(M_S \cdot H_c\) apart from a proportionality factor, the dependence of the loop area on \(M_S\) is eliminated (see (1) in the left columns in Figures S15, S16). However, the value of \(M_S\) contributes to the heat dissipation indirectly – through determining the coercive field which relative to the amplitude of the applied magnetic field affects the size of minor or major hysteresis loops and thereby may induce significant differences in the heating output.\(^{37}\) The value of \(M_S\) also determines the strength of the dipolar interactions, which also affects SAR and the interaction effect may even dominate over the single-particle properties as suggested previously,\(^{38,39}\) and also by the present study (Figures 5, S15, S16). Our numerical simulations assuming the same \(M_S = 450\) emu/cm\(^3\) for all types of cluster structures clearly display the same quantitative trend in SAR (Figure S15D-E). Moreover, at fixed \(K\), varying the value of \(M_S\) in the range between 300 and 500 emu/cm\(^3\) preserves the overall trend of SAR for the different cluster types with minor difference between SAR \textit{vs.} clusters for different \(M_s\) values (Figure S16). These data support only a minor dependence on SAR of clusters over \(M_s\) and support the interpretation that
the inter-particle interactions and their dependence on the details of the particle arrangement within the clusters are an important factor in determining SAR.

We have also investigated using simulations the dependence of SAR on the inter-particle edge to edge spacing as a way to control the dipolar interaction strength. Figure S17 suggests that while SAR is independent of the inter-particle spacing for non-interacting particles, it decays monotonically with the spacing distance for dimers. This is expected because dipolar interaction weakens as particles are brought further apart. Interestingly, however, the spacing dependence of SAR is non-monotonic for trimers and hexamers, which can be attributed to the effect of magnetic frustration and the collective magnetization behavior relevant for small spacing distances when particles are close and dipolar interactions strong. In addition, we have also used simulations to explore the cluster shape dependence of SAR, by considering 6-particle clusters arranged into statistically different geometries quantified by a variable fractal dimension (Figure S18). The values of SAR are the largest for statistically chain-like structures, and continually decrease with the increasing degree of geometrical symmetry. Spherical cluster geometries lead to the lowest values of SAR. This confirms that tuning the cluster shape has profound consequences on SAR values.

It is well known that such antiferromagnetic-ferrimagnetic (AFM-FiM) core-shell nanoparticles show so-called exchange bias identified by a shifted hysteresis loop $H_E = \frac{-\left(H^+ + H^-\right)}{2}$, towards the opposite direction of the applied field in a field-cooled (FC) measurement. All three cluster samples, measured after 1 year aging time, show a slightly shifted loop with $H_E$ of around 6 mT (Figure 6c). This means that all the samples have virtually the same phase composition and yet after a year, show a small AFM-FiM interface volume. This feature was also confirmed by XRD data (Figure S8). The XRD pattern of aged nanocubes in CHCl₃, is identical to the nanocubes forming the clusters, as shown in Figure S8. The major reflections coincide with Fe₂₉.96O₄ (ICSD: 98-008-2443). Likely, the existence of 10-15 wt% FeO phase (Fe₀.₉₄₂O, ICSD: 98-002-4696) in the particles, together with the structural defects can account for the persistence of $H_E$. In a previous work, we have found that similar core-shell nanocubes which underwent thermal annealing at 130 °C, thus fully transformed to the spinel phase, were still showing $H_E$ of 5 mT. This was related to the existence of structural defects such as anti-phase boundaries (APBs) as was also reported by other groups.
Figure 6: Magnetization hysteresis loops measured at room temperature (a) and (b), after cooling to 10 K in 5 T magnetic fields (c), and temperature dependent zero-field-cooled and field-cooled magnetization measurements performed on aqueous suspension of nanoclusters after a year of aging time, solidified in gypsum matrix recorded at 50 Oe magnetic fields (d): 16.5PScMA (blue line—individual IONCs), 33PScMA (red line—dimers and trimers), and 66PScMA (green line—clusters with n ≥ 4).

Broadly speaking, the magnetic energy barrier $KV$ distribution, with $K$ the magneto-crystalline anisotropy constant and $V$ the nanoparticle magnetic volume, can be qualitatively judged by looking at the steepness of zero-field-cooled (ZFC) curves as well as field-cooled (FC) ones (Figure 6d). A steeper ZFC curve corresponds to a narrower $KV$ distribution. At a first glance, it is seen that the dimers and trimers (33PScMA) and 3D constructs (66PScMA) show the steepest and the most gradually rising ZFC curve, proportional to the narrowest and broadest $KV$ distribution, respectively. The superparamagnetic blocking temperature $T_b$, estimated from the maximum of ZFC curves, rises from 346 K to 355 K and then to 379 K for singly coated particles, to dimers and trimers, and
ultimately to 3D clusters, respectively. To a first approximation, knowing the $T_b$, the anisotropy constant is estimated by exploiting the Néel relaxation formula given by $KV = 25k_B T_b$ (only valid at zero magnetic field, no magnetic interaction, and assuming typical measurement time at SQUID of 100 s) and $K \propto T_b/V$ holds with both $T_b$ and $V$ increasing as dimers/trimers and 3D clusters are formed, it is plausible to assume that $K$ constants of all three samples are comparable. Note that having assigned an identical $K$ value ($K = 5 \times 10^4 \text{ erg/cm}^3$) to all three samples in the Monte-Carlo simulations, a good numerical reproduction of the SAR results was achieved (Figure 5 inset and S15).

**SAR values improvement by annealing.**

Having chosen FeO/Fe$_3$O$_4$ core-shell nanoparticles as starting materials, questions arose whether (i) the clusters, once formed, would be stable against a thermal oxidation transforming the initial biphasic core-shell system into a single phase material in a much shorter time, in comparison to the case of spontaneous room temperature oxidation discussed above, and (ii) whether the trend in SAR values of individual IONCs vs. dimers and trimers and vs. bigger soft colloidal clusters ($n \geq 4$) would still be maintained.

We chose a freshly synthesized sample of core-shell iron oxide nanocubes with an edge length of $20 \pm 2 \text{ nm}$ (sample B, Figure S5) similar in size to the previous one studied for the clustering (Table S1). The XRD pattern of this sample reveals reflections of both Fe$_{2.96}$O$_4$ (ICSD: 82443) and Fe$_{0.942}$O (ICSD: 24696) phases, however dominated by the latter one (Figure S9a). Once the clusters were obtained (Figure S9b), the FeO core was oxidized to magnetite by thermal annealing in an oven at $80^\circ\text{C}$ for different time periods, each of them with an overnight duration up to a total of 52 hours (Figure S9b). Hyperthermia experiments were carried out before and after each step of the annealing process, alongside with XRD, DLS, and TEM characterization to follow the evolution of the phase composition, the morphology, and the colloidal stability of the clusters (Figure 7 and S10).

The SAR values before annealing were below 50 W/g$_{Fe}$ (Figure 7a, Table 1), which was expected for core-shell iron oxide nanocubes, due to nearly non-contributing paramagnetic FeO core and small magnetite domains oriented differently on the outer layers.$^{25}$ As the first oxidation of the core by heat treatment started, the SAR values gradually increased up to a factor of 3.7 to 131 ± 5, 179 ± 1, and 97 ± 4 W/g$_{Fe}$ for individual IONCs, dimers/trimers, and bigger clusters, respectively (Table 1). The dimers and trimers sample showed highest SAR values compared to the other two samples after only 18 hours of annealing. The trend was maintained throughout the whole annealing process, up to 52 hours (Figure 7a, Table 1). After 52 hours, the SAR values for all the samples did not improve any further. The XRD pattern of the 52 hours annealed sample is dominated by the Fe$_{2.96}$O$_4$ (ICSD: 82443) phase, yet there is a detectable fraction of FeO (Figure S9b). It seems that in
order to obtain completely oxidized particles, harsher oxidative conditions (e.g. higher temperatures, oxygen purging) have to be applied, compromising the stability and shape of the particles. In our previous work, we have observed that long time oxidation on individually coated nanocubes at 130 ºC results in a full oxidation to maghemite, having a lower $M_s$ and more aggregated state, with a marginal SAR improvement.\textsuperscript{25}

Remarkably, all the samples were stable during the annealing process as confirmed by DLS measurements (Figure S10). For example, for the sample of clusters with $n \geq 4$ the volume weighted hydrodynamic diameter remained unchanged during the whole annealing process, with $Z$-average of 98.1 ± 0.6 nm (PDI 0.07) before annealing and 96.5 ± 0.2 (PDI 0.08) after 52 hours of annealing.

Similar static magnetic measurements have been performed on these samples (Figure S11). $H_E$ of all three sample is ca. 6 mT (Figure S11c), similar to the other clusters (Figure 6c). This means that for all the colloidal assemblies the building block nanocubes have a similar phase composition, as also deduced from the XRD patterns (Figure S8, S9b). Temperature dependent magnetization curves reveal some interesting features (Figure S11d). It can be discerned that the dimers and trimers have the steepest ZFC curve rise, implying the narrowest $KV$ distribution amongst all the samples. Strikingly, individual particles show a higher $T_b$ (ca. 400 K) than dimers and trimers (i.e. 370 K), being presumably caused by magnetic dipole-dipole interactions. It is known that slight particle-particle interactions can significantly shift $T_b$ towards higher temperatures.\textsuperscript{41}

Figure S15 shows results of simulations using the kinetic Monte-Carlo modelling for variable value of effective anisotropy constant $K$. We set $M_s = 450$ kA/m of bulk Fe$_3$O$_4$. The right column of Figure S15 shows data similar to Figure 7, where Figure S15D resembles the 18 hour annealed data well. This points to low effective anisotropy of particles $K = 5 \times 10^4$ erg/cm$^3$, as the trend is in qualitative disagreement for higher value of the anisotropy constant. For this low effective anisotropy value the dipolar interactions dominate the anisotropy and therefore the differences in SAR can be attributed to the presence of dipolar interactions, in agreement with previous studies.\textsuperscript{35} They found significant reduction of the value of the effective anisotropy $K$ with respect to the nominal value expected for cubic anisotropy $K_C = 1.1 \times 10^5$ erg/cm$^3$. This is also supported by previous analysis, which estimates equivalent value of the effective uniaxial $K$ to be equal to about 70% of $K_C$. The left column plots (a)-(d) in Figure S15 show the SAR before mixing the different fractions of the clusters according to Figure 3, which allows to compare contributions to SAR from the distinct populations (i.e. only single cubes, only dimers, etc.).

Overall, these data suggest that for core-shell nanoparticles the assembly can be easily performed when the particles are in a non-interacting state, while their transformation to a more heat efficient material by annealing at moderate temperatures can occur after having obtained the clusters
without losing their arrangement and colloidal stability. It is also worth highlighting that clustering the core-shell MNPs followed by the oxidation of the core is a promising method to achieve the highest yield of soft clusters with higher SAR values.

It may be worth to mention here that other anisotropic nanomagnets, as for example nanowires or nanorods, could offer similar enhanced heating performances (with easier to tune aspect ratio). Furthermore, such anisotropic structures can have also magneto-mechanical actuation properties exploitable for cell damage. However, it must be emphasized that the discrete nature of the dimers and trimers, reported by us, makes easier their disassembling and elimination after use, an important aspect to consider for clinically-aimed approaches.

Figure 7: Evolution of SAR values of soft colloidal nanoclusters by annealing in an oven at 80 °C. (A) SAR values (with standard deviation) for soft colloidal nanoclusters during the annealing process: individual IONCs—blue bars, dimers and trimers—red bars, and clusters with \( n \geq 4 \)—green bars. Only after 18 hours of annealing time the sample of dimers and trimers showed higher SAR values. The trend was maintained up to 52 hours of annealing. (B) Schematic representation of the oxidation of the FeO core for clusters of different sizes in an oven at 80 °C.

Table 1: SAR values of soft colloidal nanoclusters at 302 kHz frequency and 23.8 kA/m magnetic field

<table>
<thead>
<tr>
<th></th>
<th>Individual IONCs@GaPEG</th>
<th>Dimers and trimers</th>
<th>Bigger clusters (( n \geq 4 ))</th>
</tr>
</thead>
<tbody>
<tr>
<td>SAR [W/g Fe]</td>
<td>SAR [W/g Fe]</td>
<td>SAR [W/g Fe]</td>
<td></td>
</tr>
<tr>
<td>Before annealing</td>
<td>46 ± 2</td>
<td>48 ± 3</td>
<td>42 ± 2</td>
</tr>
<tr>
<td>After 18 h annealing</td>
<td>131 ± 5</td>
<td>179 ± 1</td>
<td>97 ± 4</td>
</tr>
<tr>
<td>After 35 h annealing</td>
<td>180 ± 5</td>
<td>216 ± 1</td>
<td>142 ± 9</td>
</tr>
</tbody>
</table>
Conclusions

We have shown here that SAR values of core-shell IONCs were enhanced by forming anisotropic structures compared to both individually coated nanocubes and centrosymmetric clusters. The controlled clustering occurred during the water transfer of IONCs in presence of the amphiphilic poly(maleic anhydride) polymer having as hydrophobic chains poly(styrene) groups. A few parameters were crucial to the cluster formation: while the anisotropic structures were dictated by the amount of amphiphilic polymer per nanoparticle surface, the rate of THF evaporation alongside the amount of surfactant was determining the reproducibility of the protocol. The 1D and 2D structures formed with two and three IONCs, so-called dimers and trimers formed at the ratio of 33 molecules polymer per nanometer square of particle surface, showed higher SAR values than the individually coated nanoparticles and the centrosymmetric clusters, highlighting the importance of the arrangement of the nanoparticles at the nanoscale. For this study we have selected freshly synthesized FeO/Fe₃O₄ core-shell nanocubes that, after cluster formation, underwent structural transformation in aqueous solution from FeO/Fe₃O₄ core-shell structure to mainly Fe₃O₄ phase either by slow aging at room temperature (timescale of a year) or by faster annealing process in an oven at 80 °C (timescale of few days). Remarkably, even in the latter case, the grouping of nanocubes in dimers and trimers presented higher SAR values than single cubes and centrosymmetric clusters, while their aqueous stability was not compromised upon annealing treatment. We also observed a variation of $M_S$ between the different cluster structures, where the highest values of $M_S$ correspond also to the dimer and trimer cluster structures. Although this might suggest that the variation of $M_S$ correlates with the observed enhanced values of SAR for dimer and trimer cluster structures, we demonstrated by means of a kinetic Monte-Carlo computational model that the primary factor responsible for the enhancement of SAR is in fact not the variation of $M_S$ but rather the magnetic dipolar effect induced by the particular arrangement of nanocubes into dimers, trimers, and centrosymmetric clusters (compare Figure S15 and S16). Finally, using the Monte-Carlo simulation to numerically reproduce the high experimental values of SAR observed for the different cluster types required setting a rather low anisotropy constant $K = 5 \times 10^4$ erg/cm$^3$ (Figure S15). This value agrees with the K value found experimentally for iron oxide nanocubes of 19 nm cube edge.$^5$ Increasing the value of K leads to a gradually diminishing effect of the clustering of nanocubes, and ultimately to no real clustering-induced gain in SAR (Figure S15).
This work presents a versatile and smart strategy to use the same nanoparticle building blocks and achieve higher heat performances first by their controlled arrangement into anisotropic constructs made of two to three particles and second by promoting their phase transformation to Fe$_3$O$_4$.

Materials and Methods

Chemicals. All reagents were obtained from commercial suppliers and used without further purification. Iron pentacarbonyl Fe(CO)$_5$ (98%), 1-octadecene (1-ODE, 99%), oleic acid (OA, 90%), triethylamine (99%), chloroform (CHCl$_3$), ethanol (EtOH), dichloromethane (DCM), poly(styrene-co-maleic anhydride), cumene terminated ($M_n = 1\ 600$ g/mol), $\alpha,\omega$-aminopropyl-poly(ethylene glycol) ($M_n = 2\ 000$ g/mol), gallic acid, phosphate buffered saline (PBS) (150 mM NaCl, pH 7.4), sodium hydroxide were purchased from Sigma-Aldrich. Sodium oleate (97%) were obtained from TCI. THF was purchased from Carlo Erba Reagents.

Synthesis of nanocubes. Core-shell iron oxide nanocubes with an edge length of $20.2 \pm 1.5$ nm were synthesized following a recently published procedure$^{25}$ with a slight modification in order to obtain bigger nanoparticles. Briefly, in a typical synthesis of 20 nm nanocubes (Figure S1, Sample A), oleic acid (OA) (1.6 g, 5.7 mmol), sodium oleate (0.939 g, 3 mmol), and 1-octadecene (5 mL) were added to a 50 mL three-neck flask connected to a reflux condenser and degassed for 30 min at 90 °C (the amounts for Sample B were: oleic acid (2.6 g, 9.2 mmol), sodium oleate (0.939 g, 3 mmol), and 1-octadecene (3 mL)). Subsequently, the solution was cooled down to 60 °C and put under N$_2$ flux. Then the precursor solution Fe(CO)$_5$ (0.597 g, 3 mmol, dissolved in 1 mL 1-ODE) was injected and the mixture was heated, within 20 min, to 320 °C. The solution reaction was stirred vigorously at 320 °C and as nucleation started (the solution turned black) it was kept at that temperature for another 1.5 h, then was cooled down to room temperature. Finally, the IONCs were collected by centrifugation at 8000 rpm for 10 minutes and washed in a mixture of chloroform : methanol : acetone (1:6:1). The cleaning process was carried out three times and the IONCs were finally dispersed in chloroform (CHCl$_3$).

Controlled clustering. For the formation of soft colloidal nanoclusters with hydrodynamic diameters around 100 nm, corresponding to 66 PScMA molecules/nm$^2$ for sample A, in a 20 mL vial, to 9 mL THF solution was added 1 mL of stock solution of poly(styrene-co-maleic anhydride), cumene terminated (PScMA, $M_n = 1\ 600$ g/mol) polymer (obtained by dissolving 35 mg of polymer in 10 mL THF resulting in a $[\text{PScMA}] = 2.19$ mM ). For 33 PScMA, to 9.5 mL THF 0.5 mL polymer stock solution was added. Instead for 16.5 PScMA, to 9.75 mL THF 0.25 mL polymer stock solution was
added. It followed the addition of 35 µL of iron oxide nanocubes solution ([Fe] = 6.09 g/L in CHCl₃, 0.33 µM in Fe) with a cube edge length of 20 nm. Subsequently, 1 mL H₂O was added by a syringe pump, at the rate of 0.5 mL/minute, while sonicating the solution in ice bath. Next, the solution was placed on a horizontal shaker rotating at a speed of 100 rpm and the vial was left uncapped overnight at room temperature (25 °C) to slowly evaporate the THF. The following day, the remaining 0.8-1 mL of solution was transferred to a 2 mL Eppendorf and an equivalent volume of CHCl₃ was added. The Eppendorf vial was vigorously stirred at room temperature and the two phases were left to separate for a couple of hours. Once the upper aqueous phase became clear, showing no sign of turbidity, it was transferred into a 1 mL HPLC vial. More in detail, to remove THF allowing the final IONC dispersion in water, several evaporation methods were tried including (i) evaporation under reduced pressure (for roughly one hour), (ii) atmospheric pressure evaporation of THF, while stirring the solution with a magnetic stirrer in an open beaker under the fume hood (for several hours), and (iii) nitrogen bubbling of the solution (for a couple of hours). When using evaporation under reduced pressure and nitrogen bubbling, although the clusters could be obtained, the reproducibility of the experiments was poor. This suggested that the rate of THF evaporation was crucial for cluster formation. Indeed when slowly evaporating THF over 24 hours by placing a 20 mL vial (without lid) on a horizontal shaker at a speed of 100 rotations per minute, the clusters were formed and the reproducibility of the cluster formation was significantly improved. At the last step, CHCl₃ was added to form a well-defined two-phase system, with the top layer being the aqueous phase containing the nanoclusters (colored phase on top, Figure S2).

**Dynamic Light scattering (DLS).** Particle hydrodynamic size measurements were carried out using a Malvern Zetasizer Nano series instrument, operated in a 173° backscattered mode on diluted aqueous solutions of nanoclusters. The measurements were performed at 25°C. An equilibration time of 2 minutes was allowed before each measurement and at least three measurements were performed on each sample. The DLS sample was prepared by adding 25 µL of cluster sample to 0.4 mL water.

**X-ray diffraction (XRD).** X-ray diffraction analysis was carried out on a Rigaku SmartLab diffractometer, equipped with a 9kW CuKα rotating anode and operating at 40 kV and 150mA. The patterns were acquired in Bragg-Brentano geometry, using a D\text{tex} Ultra 1D silicon strip detector set in X-ray fluorescence reduction mode. The samples were prepared by drying concentrated drops of particle suspensions on zero diffraction silicon wafer.
Transmission electron microscopy (TEM). Conventional TEM images were obtained using JEOL JEM 1011 electron microscope, working at an acceleration voltage of 100 kV and equipped with a W thermionic electron source and a 11Mp Orius CCD Camera (Gatan company, USA). Samples were prepared by placing a drop of sample onto a carbon coated copper grid which was then left to dry before imaging.

Thermogravimetric analysis (TGA). The weight loss of the oleic acid coated nanoparticles was determined using a TA Instruments Hi-Res TGA 2950 thermogravimetric analyzer under air atmosphere (60 cm³/min). The samples (5-10 mg) of the surfactant coated nanocubes were heated from room temperature to 50 °C and an isotherm was applied for 15 mins, then heated to 700 °C at a heating rate of 10 °C/min.

The formula used for the calculation of ligand density (\(\rho_l\)) was described by Tong et al.\(^{46}\):

\[
\rho_l = \frac{w_l N_{Av}}{M_{w,l}} \cdot \frac{m_{NP}}{w_{NP} A_{NP}},
\]

wherein \(w_l\) is the weight fraction of the ligand, \(N_{Av}\) is the Avogadro’s number, \(M_{w,l}\) is the molecular weight of the ligand, \(m_{NP}\) is the mass of one nanoparticle, \(w_{NP}\) is the weight fraction of the iron oxide nanoparticles, and \(A_{NP}\) is the surface area of one nanoparticle. The edge length of one nanocube was taken as 20 nm for area and volume calculations. For the nanoparticle mass calculation the density of bulk magnetite was considered (5.18 g/cm³).

SAR measurements. The calorimetric measurements to determine the specific absorption rate (SAR) value of the iron oxide nanoclusters were carried out using the Nanoscale Biomagnetics instrument (DM100) operating over the range of frequencies from 105 to 302 kHz and fields up to 40 mT and 30 mT, for 105 kHz and 302 kHz respectively. The SAR value was calculated using the formula:

\[
SAR \left(\frac{W}{g}\right) = \frac{C}{m} \times \frac{dT}{dt}
\]

where \(C\) is the specific heat capacity of dispersing medium (H₂O in most cases) per unit volume (J/K) and \(m\) is the concentration (g/L of Fe) of magnetic material in solution. The calorimetric measurements were carried out in quasi-adiabatic conditions and the slope of the curve \(\frac{dT}{dt}\) was measured by taking into account only the first 20-25 seconds of the measurement. The measurements were done on samples of 200 µl at an Fe concentration of ranging from 0.65 to 3.2 mg/mL.
Magnetic characterization. Field-dependent static magnetic measurements performed on immobilized nanoclusters were carried out by employing Magnetic Property Measurement System (MPMS-XL, Quantum Design) with EverCool technology. The samples were prepared by mixing 50 µL of nanoclusters dispersed in milli-Q water, at an iron concentration of 0.9 g/L, with 60 mg gypsum in the designated polycarbonate capsules and by drying the mixture thoroughly. The zero-field-cooled (ZFC) and field-cooled (FC) temperature dependent magnetization measurements were performed on samples prepared in the same way in the cooling field of 5 mT. The residual magnetic field in the SQUID magnets was nulled using the designated low field Hall sensor prior to ZFC measurements. All the presented magnetization data are corrected with respect to the diamagnetic and paramagnetic contributions of water and gypsum using the automatic background subtraction routine. The curves were normalized to the iron concentration as obtained from the elemental analysis.

Elemental analysis. Elemental analysis was carried out via Inductively Coupled Plasma Atomic Emission Spectroscopy (ICP-AES) on a ThermoFisher iCAP 6000 series instrument. The samples were prepared by digesting 2.5-10 µL sample in 1 mL aqua regia in a 10 mL volumetric flask, overnight. The next day, the flask was filled up to the graduation mark with milli-Q water and filtered through a 0.45 µm filter membrane prior to the measurement.

Magnetic modelling methodology. The kinetic Monte-Carlo (kMC) method used in this study systematically incorporates the complexity of realistic particle distributions, thermal fluctuations, and time varying external fields. The model assumes Stoner-Wohlfarth particles with axial anisotropy \( \hat{K}_i = K_i \hat{k}_i \) where the unit vectors \( \hat{k}_i \) for each nanocube are spherically distributed (i.e. following the uniform distribution on a unit sphere) and for simplicity \( K_i \) is set to a constant \( K \). We systematically explored the effect of the anisotropy constant \( K \) and found that the value \( 5 \times 10^3 \) J/m\(^3\) gives good qualitative agreement with the experimentally observed trends in SAR. Particles with cubic shape and cube-edge of \( a = 20 \) nm and volume \( V_i = V = a^3 \) are considered. The magnetic state of every individual particle is represented by a magnetic dipole moment \( \vec{m}_i = M_s \vec{m}_i \) positioned in the centre of its cube, where \( M_s \) is the saturation magnetization and \( \vec{m}_i \) the particle moment normalized to unity. To reflect the slight degree of misalignment of nanocubes within clusters, which can be noted from the TEM image (Fig. 1), the particle positions within elementary clusters were randomized using the fractal generating algorithm described previously\(^40\) after setting the fractal dimension \( D_f = 3 \), which produces cluster structures as illustrated in Fig. S10. The chain-like and triangular clusters can also be obtained by the algorithm after setting \( D_f = 1 \) and \( D_f = 2 \), respectively, but given the small
numbers of particles within the clusters these can be obtained equivalently by setting $D_f = 3$, which in allows to systematically generate also higher order clusters.

The Stoner-Wohlfarth energy of a cluster is:

$$E = \sum_i \left( K_i V_i \left( \vec{k}_i \times \vec{m}_i \right)^2 - V_i M_s \vec{m}_i \cdot \left( \vec{H} + \vec{H}_i^{\text{dip}} \right) \right)$$  \hspace{1cm} (1)

where the sum runs through particles $i$ inside a cluster. The effective local field acting on particle $i$ is given by the sum of the external applied field, $H$, and the dipolar interaction field described by the following equation:

$$\vec{H}_i^{\text{dip}} = \sum_{i\neq j} V_j M_s r_{ij}^{-3} \left( -\vec{m}_j + 3 \vec{r}_{ij} \left( \vec{m}_j \cdot \vec{r}_{ij} \right) \right)$$  \hspace{1cm} (2)

Thermal fluctuations are accounted in the model by assuming the Néel-Arrhenius physical picture, where fluctuations – leading to frequency dependent behavior – are described as a random hoping process over energy barriers $\Delta E$ separating the different states (magnetic moment configurations), defining the relaxation time scales as:

$$\tau = \tau_0 \exp \left( \Delta E / k_B T \right)$$  \hspace{1cm} (3)

where $\tau_0 = 10^{-9}$ s, $k_B$ is the Boltzmann constant, and $T$ is the temperature. The essence of the kinetic Monte-Carlo modelling is to solve the hopping dynamics via the Master-Equation formalism, including the interacting nature of particles as given by Eqs. (1) and (2) and with realistic timescales as given by Eq. 3. Details of the method can be found in recent studies.$^{39,40}$

Throughout the present study we consider systems of 3000 nanocubes, which were for simulation of the different ensembles split to 1500 dimers, 1000 trimers, and 500 six-particle centrosymmetric cluster. To study the non-interacting system, dipolar interactions $\vec{H}_i^{\text{dip}}$ are set to zero for all particle pairs. We choose a parameter set consistent with the experimental conditions as discussed above, i.e. the frequency of the applied field for calculations of SAR (determined from the hysteresis loop area) was set to $f = 300$ kHz, the field orientation was set along the z-axis of the coordinate system and field amplitude was set to $H_0 = 23.8$ kA/m. For Figure 5 inset, $M_s$ were set at 367, 407, 407, 314 emu/cm$^3$ for respectively single, dimers and trimers and centrosymmetric clusters by converting $M_s$ estimated from in Figure 6 from emu/g of Fe in emu/cm$^3$ of Fe$_3$O$_4$. We also developed a case-study with fixed $M_s = 450$ kA/m (450 emu/cm$^3$, i.e. bulk magnetite like particles) for all different types of cluster structures (see supplementary section, Figure S13-S15) consistent with the experiments on annealed systems (Fig. 7, Fig. S11), which allows a straightforward comparison of the dipolar effects induced by the differences of the particle arrangement within the different cluster types. The particle temperature is set to constant $T = 300$ K, thus ignoring the self-heating effect, which is equivalent to assuming infinite heat capacity of particles.
The SAR was determined by evaluating the area of hysteresis loops computed for the ensembles of isolated particles, and of 2-particle, 3-particle or 6-particle structures. Examples of the computed dynamic hysteresis loops are shown in Figure S13.

**Associated Content**
Supplementary information contains additional TEM images of nanocubes and clusters, XRD spectra of the nanocube samples and DLS characterization of soft colloidal clusters, additional squid measurements of some samples and additional images of the numerical Monte Carlo simulations.

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