# The radius of the quiescent neutron star in the globular cluster M13

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#### ABSTRACT

X-ray spectra of quiescent low-mass X-ray binaries containing neutron stars can be fit with atmosphere models to constrain the mass and the radius. Mass-radius constraints can be used to place limits on the equation of state of dense matter. We perform fits to the X-ray spectrum of a quiescent neutron star in the globular cluster M13, utilizing data from ROSAT, Chandra and XMM-Newton, and constrain the mass-radius relation. Assuming an atmosphere composed of hydrogen and a 1.4M $_{\odot}$  neutron star, we find the radius to be  $R_{\rm NS}=12.2^{+1.5}_{-1.1}$  km, a significant improvement in precision over previous measurements. Incorporating an uncertainty on the distance to M13 relaxes the radius constraints slightly and we find  $R_{\rm NS}=12.3^{+1.9}_{-1.7}$  km (for a 1.4M $_{\odot}$  neutron star with a hydrogen atmosphere), which is still an improvement in precision over previous measurements, some of which do not consider distance uncertainty. We also discuss how the composition of the atmosphere affects the derived radius, finding that a helium atmosphere implies a significantly larger radius.

 $\mathbf{Key\ words:}\ globular\ clusters:$ general – globular clusters: individual: M13– stars: neutron – X-rays: binaries

## 1 INTRODUCTION

One of the unanswered questions in astrophysics concerns the interior physics of neutron stars (NSs), primarily the equation of state (EOS) of dense matter. The EOS, which also defines the relationship between mass and radius, is universal across all NSs (Lattimer & Prakash 2001). However, constraining this relation is difficult due to the complications involved with measuring NS radii. It is possible to derive constraints on the radius of a NS ( $R_{\rm NS}$ ) from spectral fits to their thermal X-ray emission, for example through spectroscopic observations of thermonuclear bursts (e.g. Özel et al. 2009, 2012; Poutanen et al. 2014; Özel et al. 2016a; Nättilä et al. 2017). Pulse profile modelling of rotation-powered pulsars can also provide an independent, non-spectroscopic method of constraining  $R_{\rm NS}$  (Watts et al. 2016; Özel et al. 2016b). One key method of deriving EOS constraints has been

through the fitting of X-ray spectra of quiescent low mass X-ray binaries (qLMXBs) containing NSs.

These systems typically exhibit soft X-ray spectra consisting of a thermal, blackbody-like component, sometimes with a harder, non-thermal component (Campana et al. 1998). The nature of the thermal component has been debated over the last few decades. Brown et al. (1998) claimed that the soft X-ray component can be explained by the 'leakage' of heat deposited in the core during accretion episodes. This 'deep crustal heating' model can predict the thermal spectrum of many qLMXBs (e.g. Rutledge et al. 2001a), though not for those which exhibit short accretion episodes, in which case the heat must be released at a shallower depth (Degenaar et al. 2011). Some qLMXBs may continue to accrete at a low level, somewhat mimicking the spectrum of deep crustal heating (Zampieri et al. 1995).

Regardless of the mechanism powering the soft component, the X-rays originate from the atmosphere of the NS. After accretion ceases, the elements stratify very quickly,

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leaving the lightest at the top (Alcock & Illarionov 1980; Romani 1987). Thus, studies of qLMXBs have often found that the soft X-ray spectra can be well described by a hydrogen atmosphere (e.g. Rutledge et al. 2001a,b; Heinke et al. 2006) and can therefore provide valuable constraints on NS masses and radii.

However, the derived radius constraints are heavily dependent on distance measurements, which are not well known for many LMXBs. Instead, we turn to qLMXBs located in globular clusters, whose distances are known to within  $\sim 5 - 10\%$  (Brown et al. 1998; Rutledge et al. 2002a). With accurate distance measurements, constraints on the NS EOS have been derived from studies of a number of globular cluster qLMXBs. Of the  $\sim$  50 known qLMXBs in globular clusters, a relatively small fraction have sufficient flux, and low enough extinction for dedicated studies of the NS EOS. These include qLMXBs in 47 Tuc (X5 and X7; Heinke et al. 2003, 2006; Bogdanov et al. 2016), M13 (Gendre et al. 2003b; Webb & Barret 2007; Catuneanu et al. 2013),  $\omega$  Cen (Rutledge et al. 2002b; Gendre et al. 2003a; Webb & Barret 2007; Heinke et al. 2014), M28 (source 26; Becker et al. 2003; Servillat et al. 2012), NGC 6397 (U24; Grindlay et al. 2001; Guillot et al. 2011a; Heinke et al. 2014), NGC 6304 (Guillot et al. 2009a,b, 2013), NGC 2808 (Webb & Barret 2007; Servillat et al. 2008), NGC 6553 (Guillot et al. 2011b) and M30 (Lugger et al. 2007; Guillot & Rutledge 2014).

Many previous studies have assumed that the atmosphere of the NS in a qLMXB is purely hydrogen (e.g. Guillot et al. 2013, and references therein). This is a reasonable assumption for typical LMXBs with main sequence donors, as once accretion stops the accreted elements will stratify (Alcock & Illarionov 1980; Romani 1987). However, it has been noted that between 28 and 44% of observed bright globular cluster LMXBs are ultracompact sources (i.e. they have orbital periods < 1hr; see Bahramian et al. 2014), suggesting that they require degenerate white dwarf companions devoid of hydrogen, as main sequence stars are not compact enough to exist in such a small orbit. If this fraction transfers to the quiescent population, then it is likely that a significant number of qLMXBs in globular clusters contain NSs with atmospheres composed of heavier elements (He, C, O).

If this is the case, then an X-ray spectrum incorrectly modelled with a hydrogen atmosphere will underestimate the radius, as spectral fits with heavier element atmospheres give larger radii than H atmospheres (Ho & Heinke 2009). The atmosphere of the NS therefore has important consequences for the EOS and must be considered (e.g. Servillat et al. 2012; Steiner et al. 2018). Unfortunately, it is difficult to determine the correct atmosphere to use without utilising optical observations to detect (or not) hydrogen in the optical spectrum of LMXBs (e.g. Haggard et al. 2004; Degenaar et al. 2010) or identifying the orbital period (e.g. Heinke et al. 2003). We note here that low-level accretion can work to prevent the stratification of elements (Rutledge et al. 2002a), which would introduce additional uncertainties in X-ray spectral models. However, the lack of variability in the majority of globular cluster qLMXBs suggests that the accretion is not a dominant process, and therefore the accretion rate is low enough to allow the atmosphere to stratify (Walsh et al. 2015; Bahramian et al. 2015).

We focus here on the qLMXB source located in the globular cluster M13, discovered by ROSAT (Fox et al. 1996; Verbunt 2001) and further studied by the XMM-Newton and Chandra X-ray observatories (Gendre et al. 2003b; Webb & Barret 2007; Servillat et al. 2011; Catuneanu et al. 2013). Since its discovery, there have been a number of attempts to constrain  $R_{\rm NS}$  through X-ray observations. This has resulted in a wide range of measurements, from a relatively compact NS ( $R_{\rm NS} \sim 9$  – 10 km Webb & Barret 2007; Guillot et al. 2013), to a much larger one ( $R_{\rm NS} \sim 12$  – 15, dependent on the chosen atmosphere; Catuneanu et al. 2013).

In this paper we utilise a new, deep observation of M13 with XMM-Newton, deriving the tightest constraints on  $R_{\rm NS}$  for this NS yet. We target M13 as the NS has a sufficiently high flux and low hydrogen absorption column  $(N_{\rm H})$  where a modest XMM-Newton observation can make the largest impact in reducing uncertainty on  $R_{\rm NS}$ . We discuss our results in the context of the NS EOS and comment on the nature of the NS atmosphere in this particular qLMXB.

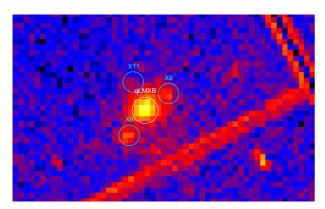
## 2 OBSERVATIONS AND DATA REDUCTION

In this work, we utilize data from ROSAT, Chandra and XMM-Newton, focusing in particular on a 2016  $\sim$  100 ks observation of M13 with the European Photon Imaging Counter (EPIC) detectors on board XMM-Newton. We also use two XMM-Newton observations of the cluster from 2002, a pair of archival Chandra observations from 2006 and a 1992 ROSAT pointing mode observation (see Table 1).

The reduction of the ROSAT data and subsequent extraction of the spectrum is described by Webb & Barret (2007) and Catuneanu et al. (2013). However, we reprocessed the Chandra and XMM-Newton data using a more recent calibration. The Chandra data were reduced using CIAO (Chandra Interactive Analysis of Observations) v4.9 and the Chandra Calibration Database (CALDB) v4.7.3 (Fruscione et al. 2006). The data were reprocessed with the chandra\_repro script to apply the latest calibration updates and bad pixel files. We filtered the data in the energy range 0.3–10 keV and found no evidence for background flaring. The spectra were extracted from circles of radius 2" centred on the qLMXB using the CIAO script specextract which also generated the corresponding response matrices.

The XMM-Newton data were processed with the Science Analysis System (SAS) v15.0.0. For all observations, we extracted events from the EPIC pn (Strüder et al. 2001) and MOS (Turner et al. 2001) detectors using epproc and emproc, respectively. All three XMM-Newton observations revealed signs of background flaring and were therefore filtered to remove the data affected by the periods of the strongest flaring activity. We use filters of 1, 2 and 0.25 count s<sup>-1</sup> (MOS) and 4.5, 5 and 0.4 count s<sup>-1</sup> (pn), for the 2002 Jan 28, Jan 30 and 2016 Feb 2 observations, respectively.

Circular regions with radii of 9".5 were used to extract the spectra of the NS qLMXB. This ensured that photons from nearby X-ray sources (X6, X9 and X11; Servillat et al. 2011) were excluded (Fig. 1). Response matrices were generated using rmfgen and arfgen and the spectra were grouped such that they contained at least 20 counts per bin. To achieve better statistics, the two MOS spectra from each observation were combined using the HEASOFT v6.19



**Figure 1.** 2016 *XMM-Newton* EPIC pn image of the qLMXB in M13. The white circle represents the region used to extract the source spectrum. The cyan circles highlight the *Chandra* positions of three nearby X-ray sources, X6, X9 and X11 (Servillat et al. 2011).

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#### 3 DATA ANALYSIS AND RESULTS

#### 3.1 Spectral fits

All spectral fits were performed using XSPEC v12.9.1p (Arnaud 1996) which uses the  $\chi^2$  minimisation technique to determine the best fit model. The interstellar absorption is accounted for by the tbabs model with Wilms et al. (2000) abundances and photo-ionisation cross-sections described by Verner et al. (1996). In all models we assume a distance to M13 of d = 7.7 kpc (McLaughlin & van der Marel 2005). We choose this distance as it is consistent with (and between)  $d = 7.65 \pm 0.36$  kpc as calculated by Sandquist et al. (2010) and  $d = 7.8 \pm 0.1$  kpc determined by Recio-Blanco et al. (2005), as well as to be able to draw comparisons with Webb & Barret (2007) and Catuneanu et al. (2013), who both use d = 7.7 kpc. We used a normalization constant to account for the cross-calibration differences between each detector, allowing the constant to vary relative to the MOS detectors, for which it was fixed to unity. In all fits, in addition to the relevant NS atmosphere model, we also included a thermal bremsstrahlung model for the fit to the ROSAT data, to account for the cataclysmic variable (CV) source X6 (Servillat et al. 2011), which was not resolved as an individual point source by ROSAT. We fixed kT of the bremsstrahlung model to 4.5 keV (Webb & Barret 2007; Catuneanu et al. 2013). All uncertainties are quoted at the 90% confidence level, unless otherwise stated.

## 3.1.1 Hydrogen atmosphere model

We fit the XMM-Newton, Chandra and ROSAT spectra simultaneously with an absorbed hydrogen atmosphere model nsatmos (Heinke et al. 2006). The spectra are plotted in Fig. 2 and the best-fit model parameters are displayed in Table 2, assuming a fixed NS mass of  $M_{\rm NS}=1.4{\rm M}_{\odot}$ . The resulting absorption column is consistent with  $N_{\rm H}=(1.74\pm0.87)\times10^{20}$ 

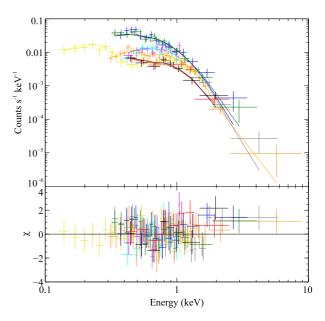


Figure 2. Spectra of the qLMXB in M13, fit with an absorbed hydrogen atmosphere model. Plotted are the 2002 XMM-Newton MOS spectra (black and red), 2002 pn spectra (green and blue), 2016 MOS and pn spectra (orange and grey, respectively), 2006 Chandra spectra (cyan and magenta) and 1992 ROSAT spectrum (yellow). The ROSAT data has been fit with an additional bremsstrahlung component to account for the unresolved CV M13 X6. The best-fit model is plotted as a solid line for each spectrum. The bottom panel shows the  $\Delta\chi$  residuals.

cm<sup>-2</sup> in the direction of M13, which is inferred from the extinction,  $E(B-V)=0.02\pm0.01^1$ , derived by Harris 1996 (2010 edition), and using Bahramian et al. (2015) to convert between  $A_V$  and  $N_{\rm H}$ . We determine a best fit NS radius  $R_{\rm NS}=12.2^{+1.5}_{-1.1}$  km. The determined radius is consistent with that of Catuneanu et al. (2013),  $R_{\rm NS}=11.7^{+1.9}_{-2.2}$  km, with tighter constraints. Allowing the mass to vary gives a best fit with  $M_{\rm NS}=1.7{\rm M}_{\odot}$  and  $R_{\rm NS}=11.6$  km. To visualise the derived mass-radius relationship we calculate the  $\chi^2$  contours with the steppar command in XSPEC and convert this to a probability distribution  $\mathcal{L} \propto \exp(-\chi^2/2)$ , shown in Fig. 3 (see e.g. Steiner et al. 2018).

# $\it 3.1.2 \quad Helium \ atmosphere \ model$

We also fit the spectra with an absorbed helium-atmosphere model nsx (Ho & Heinke 2009). The best-fit model parameters, assuming a 1.4M $_{\odot}$  NS, are presented in Table 2. For a 1.4M $_{\odot}$  NS, the helium atmosphere model determines a best-fit NS radius of 15.1 $_{-1.6}^{+2.0}$  km,  $\sim$  3 km larger than that implied by a hydrogen atmosphere. As with the H-atmosphere fits, the inferred absorption column is consistent with that in the direction of M13 (Harris 1996, 2010 edition). If we allow the mass to vary we find a best fit  $R_{\rm NS}=15.1$  km with a  $M_{\rm NS}=1.5{\rm M}_{\odot}$ . The mass-radius probability distribution is plotted in Fig. 4.

The helium atmosphere model provides a slightly better fit to the spectra ( $\Delta \chi^2 = 5.3$  for the same degrees of

<sup>&</sup>lt;sup>1</sup> http://physwww.mcmaster.ca/%7Eharris/mwgc.ref

Table 1. X-ray observations of M13.

Mission	ObsID	Date	Detector	GTI (s)
ROSAT XMM-Newton	RP300181N00 0085280301	1992 Sep 2002 Jan 28	PSPCB MOS1+MOS2 PN	45872 35222 14033
$XMM ext{-}Newton$	0085280801	2002 Jan 30	MOS1+MOS2 PN	30868 12032
Chandra	7290	$2006~{\rm Mar}~9$	ACIS-S	27894
Chandra	5436	2006 Mar 11	ACIS-S	26800
XMM-Newton	0760750101	2016 Feb 2	MOS1+MOS2 PN	96653 81587

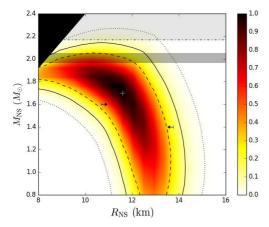
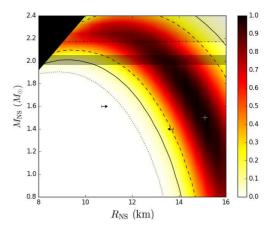


Figure 3. Mass-radius probability distribution for the hydrogen atmosphere model fit to the XMM-Newton, Chandra and ROSAT spectra of the qLMXB in M13. The dashed, solid and dotted curves represent the confidence limits at the 68%, 90% and 99% level, respectively. The black shaded section in the upper left region of the plot represents the area forbidden by causality ( $R_{\rm NS} < 2.82 GM/c^2$ ; Haensel et al. 1999). The light grey shaded region  $M_{\rm NS} > 2.17 {\rm M}_{\odot}$  may be disfavoured based on the interpretation of the NS-NS merger GW170817 (e.g. Margalit & Metzger 2017). The narrow, dark grey strip represents the most massive NS measured, PSR J0348+0432 ( $M_{\rm NS} = 2.01 \pm 0.04 {\rm M}_{\odot}$ ; Antoniadis et al. 2013). The arrows represent mass-dependent limits on  $R_{\rm NS}$  derived from GW170817 (Fattoyev et al. 2017; Bauswein et al. 2017).

**Table 2.** Best-fit parameters to the *XMM-Newton*, *Chandra* and ROSAT spectra for hydrogen (nsatmos) and helium (nsx) atmosphere models, with a NS mass fixed to  $1.4M_{\odot}$ .

Parameter	nsatmos	nsx
$N_{ m H}$ $\log_{10} T_{ m eff}$ $R_{ m NS}$ $\chi^2/{ m dof}$	$0.9^{+0.5}_{-0.4} \times 10^{20} \text{ cm}^{-2}$ $5.97 \pm 0.02$ $12.2^{+1.5}_{-1.1} \text{ km}$ 128.6/148	$1.2^{+0.6}_{-0.5} \times 10^{20} \text{ cm}^{-2}$ $5.92^{+0.02}_{-0.03}$ $15.1^{+2.0}_{-1.6} \text{ km}$ $123.3/148$



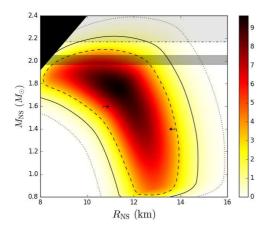
**Figure 4.** Mass-radius probability distribution for the helium atmosphere model fit to the *XMM-Newton*, *Chandra* and *ROSAT* spectra of the qLMXB in M13. The key is the same as in Fig. 3.

freedom) than the hydrogen model. However, both models are considered an acceptable fit to the data. Therefore it is not possible to determine from the fitting which atmosphere model is the correct one.

### 4 DISCUSSION

## 4.1 The effect of distance uncertainty

We have computed our spectral fits assuming a distance to M13 d=7.7 kpc (McLaughlin & van der Marel 2005). However, this did not include its associated uncertainty, which can have an effect on the inferred mass-radius relation. We can incorporate this into the probability distribution by integrating over the distance uncertainty (following the method of Steiner et al. 2018). Using a conservative uncertainty of  $\Delta d=\pm0.36$  kpc (Sandquist et al. 2010), we find  $R_{\rm NS}=12.3^{+1.9}_{-1.7}$  km and  $R_{\rm NS}=15.3^{+2.4}_{-2.2}$  km for a  $1.4{\rm M}_{\odot}$  NS with a H and He atmosphere, respectively. As expected, introducing an uncertainty on distance increases the radius uncertainties accordingly. The density distributions are plotted in Fig. 5, and show a similar increase in the mass-radius contours.



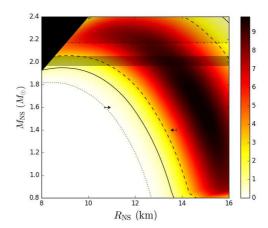


Figure 5. Mass-radius probability distribution (arbitrary normalisation) for the hydrogen (left) and helium (right) model atmosphere fits to the *XMM-Newton*, *Chandra* and *ROSAT* spectra of the M13 qLMXB, incorporating an uncertainty in the distance of  $\delta d = \pm 0.36$  kpc. The key is the same as in Fig. 3.

#### 4.2 Hydrogen vs. helium atmosphere

We have shown that the NS mass and radius constraints are highly dependent on the chosen atmosphere model. If we fix  $M_{\rm NS}=1.4{\rm M}_{\odot},$  we find that  $R_{\rm NS}$  increases by  $\sim 3$  km if the atmosphere is composed of helium versus hydrogen. It is therefore important to distinguish the nature of the companion in order to choose the correct model. Steiner et al. (2018) model the spectra of eight qLMXBs in globular clusters, and combine them to place constraints on the EOS, based on the knowledge that all NSs must have the same EOS (Lattimer & Prakash 2001). Steiner et al. (2018) calculate the probability of the qLMXB in M13 having a helium atmosphere to be < 28%, but with the tighter constraints provided by this work, this probability is likely to be even lower, despite the lower  $\chi^2$  for a helium atmosphere model (compared to hydrogen) suggesting a better fit. However, the only reliable way to distinguish between hydrogen and helium atmospheres in NS LMXBs is through direct optical/NIR observations of the counterpart.

## 4.3 Neutron star equation of state

Our results tighten the constraints on the mass and radius of the NS presented by Catuneanu et al. (2013), which has implications for the NS EOS. Previous studies of M13 claim tighter constraints on  $M_{\rm NS}$  and  $R_{\rm NS}$  (Gendre et al. 2003b; Webb & Barret 2007) than this work, but these results were not reproduced in later studies (Catuneanu et al. 2013; Guillot et al. 2013). Our results are consistent with Catuneanu et al. (2013) and our derived radius (for a 1.4M $_{\odot}$  NS) falls within the preferred range of 10–14 km for NSs, calculated from observations of multiple qLMXBs and taking into account the effects that a number of uncertainties (e.g. distance, atmosphere composition) have on the inferred mass-radius relation (Steiner et al. 2018).

A previous study fitting spectra of M13 and other qLMXBs by Guillot et al. (2013) preferred a smaller  $R_{\rm NS}=9.2^{+1.7}_{-2.3p}\,{\rm km}$  (where p indicates that the parameter was

pegged at the hard limit of the model) for M13. However, in that study, a smaller distance was chosen ( $d=6.5~\rm kpc$ ; Rees 1996) rather than the 7.7 kpc we utilise in this work (McLaughlin & van der Marel 2005), a distance in agreement with measurements by Recio-Blanco et al. (2005) and Sandquist et al. (2010) (see also Steiner et al. 2018). We note that if we instead choose  $d=6.5~\rm kpc$ , we find  $R_{\rm NS}=10.1\pm1.4\rm km$ , consistent with the value derived by Guillot et al. (2013).

The detection of gravitational waves (GW170817) from two merging NSs (Abbott et al. 2017a) has placed some limits on the NS EOS. The event placed an upper limit on the tidal deformability parameter ( $\Lambda$ , an intrinsic NS property sensitive to the stellar compactness). Limits on the tidal deformability obtained as the two bodies approached coalescence ( $\Lambda \leq 800$  for  $M_{\rm NS} = 1.4 {\rm M}_{\odot}$ ; Abbott et al. 2017a) can be translated into an upper limit on the radius of a  $1.4M_{\odot}$ NS  $(R_{NS} < 13.76 \text{ km}; \text{ Fattoyev et al. } 2017)$ . Information from the short gamma-ray burst that followed the merger 1.7s later (e.g. Abbott et al. 2017b; Goldstein et al. 2017; Savchenko et al. 2017) can be used to infer a limit on the maximum mass of a NS of  $\lesssim 2.17 M_{\odot}$  (Margalit & Metzger 2017; Shibata et al. 2017; Rezzolla et al. 2018). We must note, however, that these calculations, though all consistent and performed independently of one another, are heavily dependent on physical assumptions about the type of compact object formed in the merger. Finally, Bauswein et al. (2017) calculated a lower limit of  $R_{\rm NS} > 10.68$  km (for  $M_{\rm NS} = 1.6 {\rm M}_{\odot}$ ), also assuming that the merger did not result in a prompt collapse to a black hole - as suggested by the detection of a kilonova (Kasen et al. 2017; Pian et al. 2017; Smartt et al. 2017). Though the radius constraints inferred from GW170817 do not fully rule out the possibility of a He atmosphere in the M13 qLMXB, they are in agreement with Steiner et al. (2018) in that it is unlikely to be the case.

#### 5 CONCLUSIONS

We have derived NS mass-radius constraints for the qLMXB located in the globular cluster M13 using archival observations and a new, deep observation of the cluster with XMM-Newton. We provide the tightest constraints on the radius of the NS  $(R_{NS} = 12.2^{+1.5}_{-1.1})$  km assuming a H atmosphere and  $M_{\rm NS} = 1.4 {\rm M}_{\odot}$ ), which are in good agreement with the limits on the NS EOS derived by Steiner et al. (2018). We find that introducing a conservative uncertainty on distance (Sandquist et al. 2010), increases the radius uncertainties accordingly. We cannot definitively rule out a He atmosphere, but spectral fits infer a much larger  $R_{\text{NS}} = 15.1^{+2.0}_{-1.6}$ km, which overlaps with the upper edge of the  $R_{\rm NS}=10-14$ km range derived by Steiner et al. (2018). In addition, limits on  $R_{\rm NS}$  derived from the NS-NS merger GW170817 (Abbott et al. 2017a; Fattoyev et al. 2017) disfavour a He atmosphere interpretation for the qLMXB in M13. To verify the nature of the atmosphere of the NS, we require spectroscopy of the optical/NIR counterpart, which has not yet been discovered.

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