Controlling Lateral Buckling of Subsea Pipeline with Sinusoidal Shape Pre-Deformation

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Abstract

It is common for subsea pipelines to operate at high pressures and high temperatures (HPHT) conditions. The build-up of axial force along the pipeline due to temperature and pressure differences from as-laid conditions coupled with the influence of the seabed soil that restricts free movement of the pipeline can result in the phenomenon called 'lateral buckling'. The excessive lateral deformation from lateral buckling may risk safe operation of the pipeline due to local axial strains that potentially could be severe enough to cause fracture failure of welds or collapse of the pipeline. Engineered buckles may be initiated reliably during operation by using special subsea structures or lay methods which are expensive. This paper introduces and exemplifies a novel method that involves continuously deforming the pipeline prior to or during installation with prescribed radius and wavelength to control lateral buckling that could be a valuable modification of the practical design of offshore pipelines. Previous published work has shown that installation of a pipeline with such continuous deformations is feasible. The results from an example pipeline case described here show that the pipeline can be installed and operated safely at elevated temperatures without the need for other expensive buckle initiation methods.

Keywords

Subsea pipeline novel design, Pipeline Lateral Buckling, Pre-deformed Pipeline (PDP), High Pressure

- High Temperature (HPHT), Pipeline – Soil Interaction (PSI), Pipeline failure modes

1. Introduction

The demand for gas in recent times has driven the offshore industry into exploration and production at extreme conditions, due primarily by high pressure high temperature (HPHT) drilling. An accepted HPHT definition is when a gas reservoir temperature exceeds 300°F (149°C) and pressure exceeds

10,000 psi (690 bar) (Shadravan and Amani, 2012). This often implies that subsea pipelines, used to transport hydrocarbons, are also required to operate at HPHT conditions.

When a subsea pipeline, carrying a hydrocarbon gas, is operated at high temperatures and pressures there is a consequential tendency for the pipeline to expand longitudinally. The longitudinal expansion is resisted by the axial friction mobilised against the seabed soil, creating high compressive axial forces.

When the compressive axial forces increases in the pipeline to a certain level, the pipeline has the natural tendency to move laterally on the seabed to reduce the axial force and to achieve a lower strain energy state. Similar to beam or column buckling, the lateral deflection of the structural member as a result of axial compressive force leads to bending of the column, i.e. change of mode, due to the instability of the member.

Buckling can occur quite suddenly and the large lateral displacements induced by this uncontrolled phenomenon, sometimes called 'global buckling', may result in high local stresses and strains in the pipe wall that exceed code limits such as those specified in DNV OS F101 (Det Norske Veritas, 2013). Cyclic fatigue and fracture of girth weld between pipeline joints may also be at risk of failure due to pipeline lateral buckling caused by conditions that cycle between start-up and shutdowns during the pipeline's design life.

In order to understand the lateral buckling of subsea pipelines, it is required that we understand the concept of effective axial force. The concept of effective axial force is the heart of subsea pipeline design and has been extensively discussed (Fyrileiv and Collberg, 2005; Sparks, 1984). Effective axial force (taking compression as negative) is the pipeline steel wall force augmented by the pressure induced force as shown in Eq. (1):

$$S_{eff} = N - P_i A_i + P_e A_e \tag{1}$$

where:

N = pipeline axial steel-wall force

P_i = pipeline internal pressure

A_i = pipeline internal cross-sectional area

P_e = pipeline external pressure

A_e = pipeline external cross-sectional area

It is generally accepted that global buckling of pipelines is governed by the effective axial force (Det Norske Veritas, 2013). Following installation of a pipeline on the seabed, the steel-wall force of the

pipeline is simply the residual lay tension and the external pressure force, P_eA_e . When the pipeline is operated, the steel-wall force is given by the restrained thermal expansion (- $A_s\alpha\Delta TE$) and the longitudinal stress due the hoop stress and Poisson's effect ($v\sigma_hA_s$) during the application of the gas temperature and pressure. As the external pressure of the pipeline due to the hydrostatic pressure of water depth is the same for as-laid and operation conditions, the external pressure term is cancelled. Substituting the steel-walled force into Eq. (1), the fully restrained pipeline effective axial force can be defined using Eq. (2).

$$S_{eff} = H - \Delta P_i A_i (1 - 2\nu) + A_s E \alpha \Delta T \tag{2}$$

where

H = residual lay tension

 ΔP_i = internal pressure difference relative to as-laid

v = Poisson Ratio

 A_s = cross-sectional area of the pipe

E = Young's Modulus of Elasticity

 α = thermal coefficient of expansion

 ΔT = temperature difference relative to as-laid

The fully restrained force is shown as Case A in Fig. 1. In practice, a pipeline on the seabed is not fully restrained from expansion movement. Axial movement during operation is restrained by the seabed soil and the axial resistance force over a length L of a pipeline is given by Eq. (3).

$$F_{ax} = \mu_a W_s L_x \tag{3}$$

where

 μ_a = axial friction coefficient

W_s = pipeline submerged unit weight

 L_x = length along pipeline

The pipeline ends are usually free to expand, for example through the provision of low-friction mechanical sliders on the termination structure (see the case study in Jayson et al. 2008, for example). This means that the effective axial force for a pipeline at the free-ends is zero and gradually

increases due to the axial friction resistance force between the pipeline and the seabed. Given sufficient length of the pipeline, there will be a limiting position along the pipeline where the axial friction force equals the expansion force of the pipeline. This position is called the anchor point where the axial strain of the pipeline is zero and the force at this point is the fully restrained force given in Eq. (2). This behaviour of the effective axial force is represented by Case B in Fig. 1 and is called 'long pipeline' is called 'long pipeline' behaviour. If however, due to low axial friction resistance between seabed and pipeline, or if the length of pipeline is insufficient, the pipeline does not attain the fully restrained condition. This is shown in Fig. 1 as Case C and is called 'short pipeline' behaviour. The anchor point is then formed at the mid length of the pipeline. The effective axial force in the pipeline may be well below the fully constrained force but it could be sufficient to buckle the pipeline. A pipeline is susceptible to lateral buckling when the compressive effective axial force exceeds the 'critical buckling force' above which the pipeline becomes unstable laterally. The critical buckling force is highly dependent on the lateral pipe-soil resistance and to the local out-of-straightness (OOS) of the installed pipeline. When a pipeline buckles, the pipeline axial force decreases significantly with the axial expansion feeding into the buckle. This is shown as Case D in Fig. 1. A 'long pipeline' is more susceptible to lateral buckling due to high effective axial force than a 'short pipeline'.

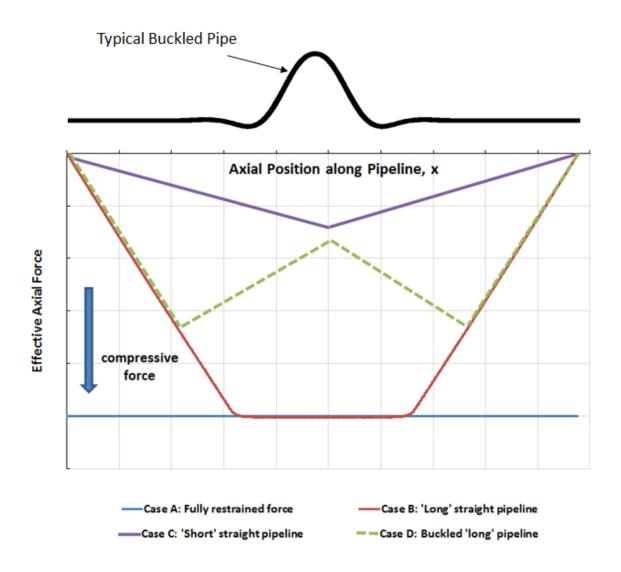


Fig. 1. Pipeline Lateral Buckling Phenomenon

An important aspect to be considered by pipeline engineers is to determine this critical buckling force that could cause lateral buckling. Early studies carried out by Hobbs (Hobbs, 1981; Hobbs and Liang, 1989) have proved an analytical solution for the critical buckling force, P_o for a perfectly straight pipeline laid on a rigid flat seabed shown in Eq. (4) for a mode 3 buckle, which is a commonly encountered mode of subsea pipeline buckling:

$$P_o = \frac{34.06 \cdot E \cdot I}{(L)^2} + 1.294 \cdot \mu_a \cdot w_s \cdot L \cdot \left[\left(1 + 1.668 \times 10^{-4} \frac{E \cdot A_s \cdot \mu_l^2 \cdot w_s L^5}{\mu_a \cdot (E \cdot I)^2} \right)^{0.5} - 1 \right]$$
(4)

The buckle amplitude is calculated using Eq. (5) (Hobbs, 1981; Hobbs and Liang, 1989).

$$y = \frac{1.032 \times 10^{-2} \cdot \mu_l \cdot W_s}{E \cdot I} L^4 \tag{5}$$

where

L = buckle length

I = Second Moment of Pipe Area

 μ_a = axial friction coefficient

 μ_{l} = lateral friction coefficient

y = buckle amplitude

If the pipeline effective axial force exceeds the Hobbs critical buckle initiation force, lateral buckling will occur. This method however has two major limitations; the first is that Hobbs equations are for an idealised, or perfect pipeline buckling phenomena which does not account for any initial out-of-straightness; secondly, pipe-soil friction is assumed to be fully mobilised throughout the analysis.

In practice, a perfectly straight pipeline does not exist as a practical pipeline would inherit imperfections from the processes of pipe manufacturing, pipe laying and also the seabed topography. Taylor and Gan (Taylor and Gan, 1986) modified the Hobbs formulation for Mode 1 and 2 conditions to include the effect of imperfection in lateral buckling of pipeline and deformation-dependent axial friction resistance.

Although analytical equations mentioned above provide a simple solution to predict lateral buckling of pipelines due to operating temperature and pressure and pipe-soil interaction, there are significant uncertainties with soil resistance and the as-laid out-of-straightness. Therefore, it is necessary to address the uncertainties inherent in lateral buckling prediction as more and more pipelines now operate in HPHT environment. Bruton et al. (2005; 2007; 2008) discussed the SAFEBUCK JIP guideline where researchers and industry have collaborated to developed methods to control buckling using deterministic and probabilistic methods where the pipeline initiation is deliberately applied in a controlled manner (Bruton et al. 2005; Bruton et al. 2007; Bruton et al. 2008). Controlled or planned buckling means that the pipeline is caused to buckle such that lateral displacements do not become a failure risk and excessive local deformations in the areas of high bending that do not lead to local buckling, wrinkling of pipe wall, or fracture at girth welds are considered to be acceptable.

Controlling lateral buckling can be achieved using various methods such as utilizing a subsea structure that acts as buckle initiator commonly called a sleeper (shown in Fig. 2), use of route

bends, snake-laying (Sinclair et al. 2009) and utilising a textured pipeline in place of a cylindrical pipeline, based on a study by Karampour and Albermani (2016). Sleepers are manufactured on land then transported and installed along the pipeline. This is costly and time consuming. In route bends and snake-lay, due to the radius of the bends being limited by the pipe-soil friction and lay tension, these methods may not achieve the required high reliability required in planned buckling while the textured pipeline system is still in research phase. An alternative practice is to place large weights or structures on the seabed around which the pipeline is bent during installation. The objective is to increase the pipe local curvature along the pipeline to initiate a lateral buckle with a high level of reliability.

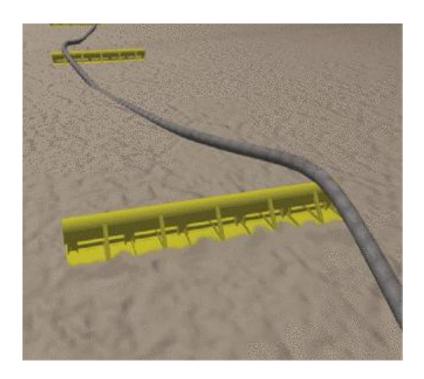


Fig. 2. Use of sleeper for controlling lateral buckling (Kristiansen et al., 2005)

The use of deterministic and probabilistic analysis discussed in (Bruton et al. 2005; Bruton et al. 2007; Bruton et al. 2008) centres around the concept of virtual anchor points or VAS. VAS is simply the feed-in length to a buckle. When a buckle is formed in a pipeline, the axial force decreases and pipe on each side of the buckle feed-in the required length for the buckle formation. When multiple buckles are formed, the pipeline divides itself into a series of 'short pipelines' that consist of its own feed-in length which are fully constrained at their ends. This end constraint is where the direction of the pipe axial displacement changes as they are involved in axial movement feeding into two adjacent buckles.

Fig. 3 illustrates the post-buckled effective axial force of the pipeline where the buckled pipeline behaves like a series of 'short' pipelines. The closer the buckles are to each other the less is the axial feed-in length to the buckle, lowering the lateral deflection. This produces a solution in which the expansion strain is shared between each site, leading to manageable strain within each buckle.

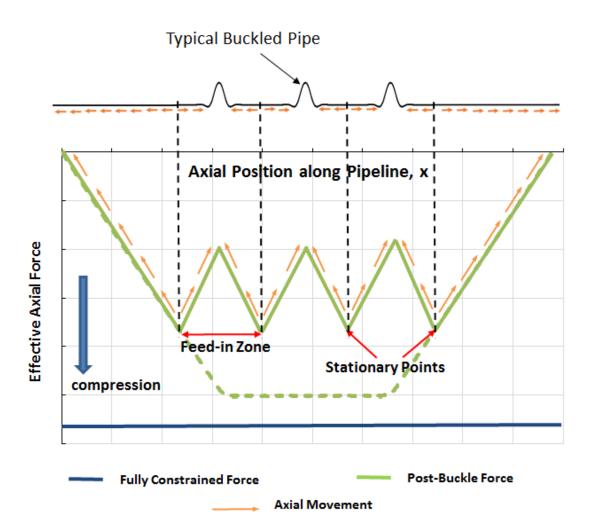


Fig. 3. Concept of Post-Buckle Feed-In 'Short' Pipeline Behaviour

Although the use of deterministic and probabilistic methods detailed in researches by Bruton et al. (2005; 2007; 2008) in controlled lateral buckling are safer and more cost-efficient compared to assessing buckling using Hobbs followed by trenching and burying the pipeline to eliminate buckling as mentioned in (Hobbs, 1989), the cost of controlling buckling, i.e. installing subsea structures and snake-laying the pipeline, is still significant.

This paper proposes a new concept in which the pipe is continuously deformed into specific wavelength and amplitude prior to installation on the seabed for controlling lateral buckling and

eliminating the use of subsea structures. Pre-installation out-of-straightness deformations reduce the axial stiffness of the pipeline sufficiently to allow the pipelines to operate without the need for subsea structures for controlling lateral buckling could reduce overall cost of installing pipelines and structures.

2. Pre-Deformation of Pipeline

A pre-deformed pipeline has been successfully installed for controlling lateral buckling. Endal et al. (2014) and Endal and Nystrom (2015) published a paper detailing the use of the straightener on the reel-lay barge during reel-lay installation to create residual curvature at specified sections along the dual 14/16inch pipeline designed for operating temperature up to 95°C for the Skuld Project before it was laid on the seabed.

In reel-lay installation, the welding together of pipe sections is carried out onshore and then reeled onto a large drum. The pipeline is plastically bent during the process of reeling. The pipeline is then unreeled from the drum and the residual bending strains are removed by a straightener system before leaving the reel ship and laid on the seabed. The method is patented by Statoil (2002) and takes advantage of the hydraulically adjustable straightener to bend the pipe at specified section to create specified levels and variations of residual curvature at specific isolated locations along the pipeline.

Fig. 4 shows the image taken from (Endal et al., 2014). It shows a local curvature created on the pipeline by the straightener using three-point bending to 0.2% to 0.25% along a 40m length. Implementation of this method at 25 locations for the Skuld Project in 2012. Approximately one per km of pipeline length was reported to only cost additional of 10 - 20 minutes per location (Endal et al., 2014). This is a relatively small cost compare to time spent implementing other methods of controlling buckling such as sleepers (which require a separate installation campaign) nor snake-laying (which requires frequent interruptions to the laying process). Fig 5 shows the residual curvature described in Fig. 4 (Endal et al., 2014; Endal and Nystrom, 2015) located every km along the installed Skuld pipeline.

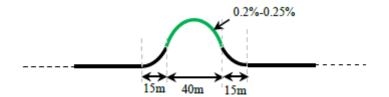


Fig. 4. Local Curvature Patented by Statoil (2002) taken from (Endal et al., 2014)

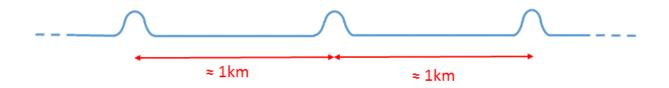


Fig 5. Distance between Local Curvatures in Skuld Project (Endal et al., 2014)

The concept of pre-deformation introduced in the present paper differs from (Endal et al., 2014; Endal and Nystrom, 2015) as the pipeline considered in the development below is pre-deformed continuously rather than being pre-deformed at specific positions along the pipeline.

Continuous pre-deforming pipeline was used previously to control upheaval buckling of 5.7inch pipeline with operating temperature of 280°F (137.8°C) for Mobile Bay Fairway Field Project in 1990 (Lanan and Barry, 1992). A continuous zig-zag configuration was obtained by pre-deforming each pipe joint into a constant radius 8° bend at mid-length and welding the 2 bend joints together in alternating directions. Fig. 6 presents the pipeline geometry in the Fairway Field Project. In practice the pipeline operated at the required high temperature without any evident lateral buckling. However, this method of continuous pre-deforming pipeline has not been verified as being suitable for controlling lateral buckling at higher temperatures, or relating the required bend angles to various pipe diameters and operating temperatures.

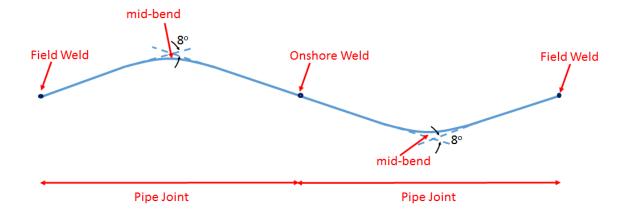


Fig. 6. Use of Regular Expansion Bend in Fairway Field Project (Lanan and Barry, 1992)

It is the objective of this paper to discuss the feasibility of using the concept of continuous predeforming pipeline to control lateral buckling. A pre-deformed pipeline reduces the axial force in the pipeline significantly, meaning that the effective axial force build up in the pipeline at elevated operating temperatures will not attain the buckle initiation temperature, hence, instability will not occur during operation of the pipeline. The interest in the present investigation is that if, however, due to variations of pipe properties and occurrence of elevated temperatures, the pre-deformed pipeline might develop a local instability, would it naturally develop a series of 'short' pipelines, therefore, reducing the lateral deformation of the buckles, limiting the strain, making it safe, robust and costeffective way for practical lateral buckling control?

3. Analytical Calculation of Axial Stiffness of Pre-deformed Lobe

This section presents a numerical analysis of how the axial stiffness of a pipe can be decreased due to the pre-deformation. The analytical solutions here is purely to compare the axial stiffness of the pre-deformed pipeline with a 'straight' pipeline; therefore, simple linear elastic formulation is used and both end boundary conditions are assumed to be fully fixed for both 'straight' and pre-deformed pipeline. The comparison is exemplified for a length of pipe, L_T , deformed into one lobe (or wave shape) shown graphically in Fig. 7 and a simple chosen shape, i.e. that follows a sinusoidal wavelength shape given by the Eq. (6). As the length of the pipe consist of only one lobe, the wavelength, L_w is equal to the length of the pipe, L_T .

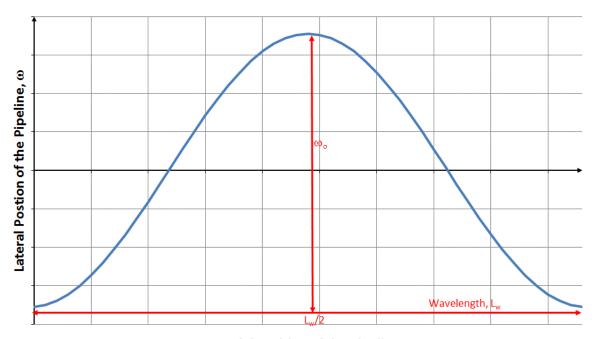
$$\omega = \frac{\omega_0}{2} \left[\sin\left(\frac{2\pi x}{L_w}\right) \right] \tag{6}$$

where

 ω = lateral position along the pipeline relative to the straight configuration

x = axial position along the pipeline

 ω_0 = maximum lateral amplitude along the pipeline (at L_w/2)



Axial Position of the Pipeline, x

Fig. 7. Pre-deformed shape of one lobe

For a pre-deformed pipeline under axial force, P_{ax} , the change in strain energy relative to the unstressed state, $d\Phi$ along the pipeline is given by Eq. (7):

$$d\Phi = \frac{EI}{2} \int_0^{L_W} \left(\frac{d^2 \omega}{dx^2}\right)^2 dx - \frac{P_{ax}}{2} \int_0^{L_W} \left(\frac{d\omega}{dx}\right)^2 dx \tag{7}$$

Any increased in P_{ax} , will caused an increase in energy and the system will be statically unstable. The system will deflect and\or deform to minimise the energy. This force will be called the critical force and be defined as P_{cr} . The critical force, $P_{cr} = \frac{4\pi^2 EI}{L_w^2}$, is obtained from $\frac{d\Phi}{d\omega} = 0$.

As the axial load increases, there is a change of energy of pre-deformed lobe due to a change in amplitude and shortening of the axial length. Eq. (8) shows the shortening of the axial length, Δ_S of the pipeline feeding into the lateral deflection of the pre-deformed shape is simply:

$$\Delta_{s} = \frac{\pi^{2} \left[\left(\frac{\omega_{o}}{1 - \frac{P_{ax}}{P_{cr}}} \right)^{2} - \omega_{o}^{2} \right]}{4L_{w}}$$
(8)

The total axial displacement, Δ_{Tot} is displacement of the pipe wave without lateral deflection and the shortening due to lateral deflection. This is shown in Eq. (9).

$$\Delta_{Tot} = \frac{\pi^2 \left[\left(\frac{\omega_o}{1 - \frac{P_{ax}}{P_{cr}}} \right)^2 - \omega_o^2 \right]}{4L_w} + \frac{P_{ax}L_w}{EA_s}$$

$$\tag{9}$$

Stiffness of the pre-deformed wave, K_p is therefore $\frac{1}{d\Delta_{Tot}/dP_{av}}$ and is given by Eq. (10):

$$K_{p} = \frac{1}{\frac{L_{T}}{EA} - \frac{\pi^{2}\omega_{o}^{2}}{2L_{w}P_{cr}\left(\frac{P_{ax}}{P_{cr}} - 1\right)^{3}}}$$
(10)

The second term on the denominator controls the fall in axial stiffness of the pre-deformed wave relative to the straight pipe case, and as $\omega_0 \to 0$ the solution reverts to a straight pipe. For a specified wavelength, L_w and amplitude of a lobe, ω_0 , an increased in axial force, P_{ax} causes the stiffness, K_p to decrease. Fig. 8 presents the calculated ratio of stiffness (stiffness of pre-deformed wave, and since uniform conditions are considered along the pipeline, the stiffness of the full length of the pipeline from Eq. (10), K_p divided by the stiffness of straight pipeline, K_s (= EA/L_T), for example pipeline with properties presented in Table 1 against the axial force. At infinitesimal axial force, the axial stiffness of the pre-deformed pipeline is slightly less than half the stiffness of the straight pipeline. As the applied axial force is increased, the ratio of stiffness decreases and approaches zero at about 1MN of axial force for the example case. This is because the stiffness of pre-deformed pipeline reaches a constant value after 1MN of applied force while the stiffness of the straight pipeline keeps increasing with applied axial force. Also included in Fig. 8 is the non-dimensional axial force of the pre-deformed wave, $P_{ax}/(K_p^*L_w)$. As the axial force increases, the axial stiffness of the pre-deformed wave

decreases, therefore, the ratio of $P_{ax}/(K_p^*L_w)$ increases significantly with the axial force, P_{ax} . The axial force comparison is made using FEA and as it is seen in the graph, the results are identical.

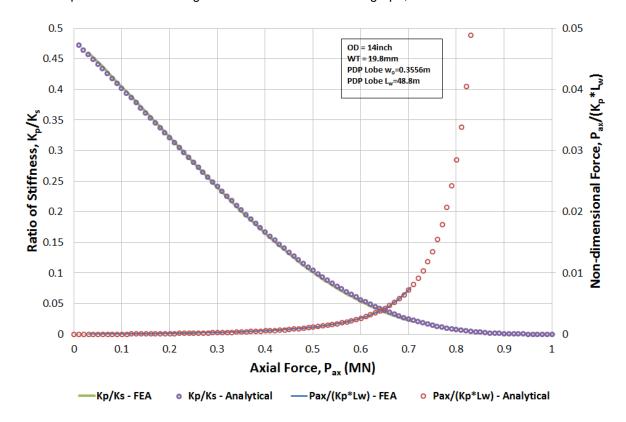


Fig. 8. Ratio of Stiffness Plot

Fig. 9 shows the effect of the reducing stiffness of the pre-deformed pipeline on the fully restrained effective axial force of the same example pipeline. This shows the decrease in fully restraint effective axial force for the example pre-deformed pipeline is significant compare to a perfectly 'straight' pipeline.

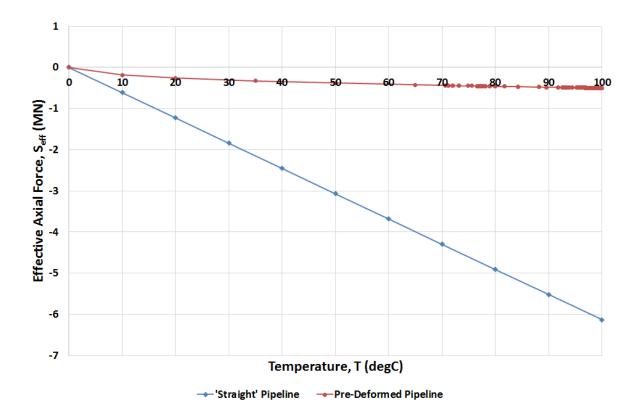


Fig. 9. Fully Restraint Effective Axial Force of a Perfectly 'Straight' and Pre-Deformed Pipeline with temperature

Based on the above discussion, a small but practical level of regular sinusoidal pre-deformation has a significant influence on the axial stiffness of a pipeline. The next step is to determine if the effect of the reduced axial stiffness of the pre-deformed pipeline is applicable in an example subsea pipeline in field condition, i.e. with non-linear variables such as material properties, complex pipe-soil interaction and random imperfections. In order to do this, FEA modelling is utilized.

4. Pipe-Soil Interaction (PSI)

The pipe-soil interaction used in this paper is the 'equivalent' friction coefficient between pipe and seabed soil which is defined as the maximum resistance of the soil divided by the submerged weight of the pipe. Therefore, all friction values presented in this paper are based on the 'equivalent' friction concept as is the usual practice in pipeline design (Bruton et al., 2007; Bruton et al., 2008, DNV 2017).

The example lateral and axial soil friction factors used in this paper is assumed to have captured the interaction between vertical embedment of the pipeline and the characteristic of the seabed soil. Typically, the more the pipeline penetrate into the soil, the higher the lateral and axial resistance. The

prediction of the axial and lateral resistance of the pipe-soil interaction based on penetration depth into the seabed soil and its uncertainty can be found in (White and Randolph, 2007). With this assumption, the coupling between flowline embedment and PSI is not taken into account in the FEA model in this paper. Therefore, the seabed surface is modelled as a flat, hard surface with very high vertical stiffness (~10⁶N/m²).

For all the FE calculations performed, soil modelling is based on uncoupled axial and lateral coulomb friction. Extensive work had been done to establish the uncoupled behaviour of axial and lateral soil acting on the pipeline during lateral buckling analysis (Bruton et al., 2007; Bruton et al., 2008; White and Cheuk, 2008). Separate values are assigned to the axial and lateral equivalent friction factors, hence, the failure surface which determines when sliding occurs is rectangular (see Fig. 10). This results in axial and lateral friction behaviours that are independent of each other.

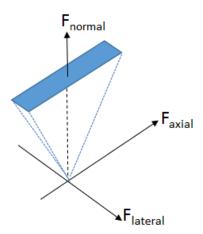


Fig. 10. Failure Surface for PSI

A simple bi-linear axial response of a pipeline on the seabed is assumed in this paper and is shown in Fig. 11. This assumption is applicable for pipeline with axial displacement that occurs slowly, with no excess pore pressure generation. Potential changes in axial friction due to consolidation effects between episodes of movement are ignored for simplicity. Fig. 12 shows the lateral response of a pipeline on the seabed. Due to as-laid embedment of the pipeline, during the first loading, the partially embedded pipeline undergoing lateral movement, needs to 'break-out' and rises as it moves laterally, mobilising an initial peak in resistance. The lateral resistance for break-out is usually high. The lateral resistance then reduces to a steady residual resistance (White and Cheuk, 2008). Therefore, the PSI response for the first start-up is a tri-linear behaviour. During the first shutdown, the pipeline displaces in a reverse direction compared to start-up. However, the pipeline does not displace back to its

original position due to reversal of the axial resistance along the feed-in section and lateral resistance at the buckle lobe (White and Cheuk, 2008). In the subsequent start-up and shutdown cycles, the pipeline is only resisted by constant lateral friction, i.e. similar to lateral residual friction from first loading with the assumption that the pipeline is not subjected to prolonged shutdown in a stationary position that causes it to be partially embedded. Experiments reported in (White and Cheuk, 2008) show that during cyclic pipeline lateral displacement, soil is swept ahead each cycle, causing a build-up of berms at the extremes of the pipe displacement. However, this soil berm accumulation effect is not taken into consideration in this paper.

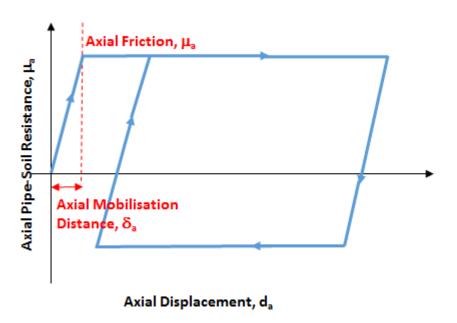


Fig. 11. Pipe-Soil Axial Friction Modelling in FE

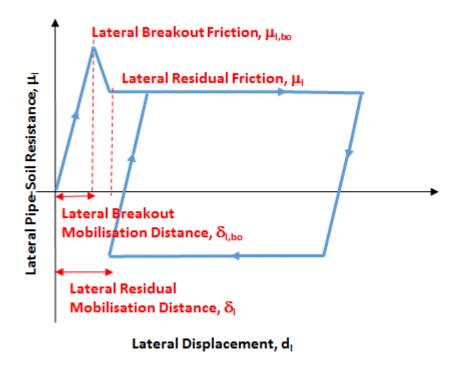


Fig. 12. Pipe/Soil Lateral Friction Modelling in FE

5. Description of Example Case Study

A typical case, shown in Table 1, comprising pipe, pipeline and operating conditions is selected to study the characteristic properties of a pre-deformed pipeline subjected to high operating temperature and pressure. The 14inch with diameter/thickness (D/t) ratio of 18 is selected as it is a common size in subsea gas pipelines that can be installed by conventional means, i.e. S-lay, Reel-lay. The operating temperature and pressure are applied simultaneously with respect to the reference pipeline initial temperature and internal pressure of 0°C and 0bara respectively for simplicity. No external pressure is applied in the modelling as external pressure has minimal effect on lateral buckling as the build-up of effective axial force shown in Eqn. (2) is due to the internal pressure and temperature relative to as-laid condition. The effect of residual lay tension is also ignored in the present work.

The pipe-soil friction factors in Table 1 are assumed based on mean values of data published by Bruton et.al (2006) and Bruton et. al (2008) for several project specific test. The example mobilisation distances are also taken within the range of recommended values from paper published by Bruton et.al (2006) and Bruton et. al (2008).

Table 1 Modelling Parameters

Parameters	Unit	Value
Pipe Outer Diameter (OD)	m	0.3556
Pipe Wall Thickness (WT)	mm	19.8
Pipe Submerged Weight, W _s	N/m	610
Pipeline Total Length, L _T	km	4.88
Maximum Operating Temperature, T _{op}	°C	200
Ambient Temperature, T _{amb}	°C	0
Maximum Operating Pressure, Pop	bara	200
Pipeline Material Young's Modulus, E	GPa	205
Coefficient of Thermal Expansion, α	1/°C	1.3 x 10 ⁻⁵
Pipe-Soil Lateral Breakout Friction, μ _{l,bo}	-	1.0
Lateral Breakout Mobilisation Distance, $\delta_{\text{l,bo}}$	mm	30
Pipe-Soil Lateral Residual Friction, μ _l	-	0.5
Lateral Residual Mobilisation Distance δ_l	mm	150
Pipe-Soil Axial Friction, μ _a	-	0.5
Axial Mobilisation Distance, δ_a	mm	1.5

The pipe carbon-steel material is assumed to have a material stress-strain curve as shown in Fig. 13 and this stress-strain behavior is captured in FEA modelling by inputting the Young's Modulus of Elasticity and the yield stress vs. equivalent plastic strain. All relevant parameters from Table 1 and stress-strain characteristic from Fig. 13 are assumed to be constant with variation in temperature for simplicity at this stage in the development of the concept.

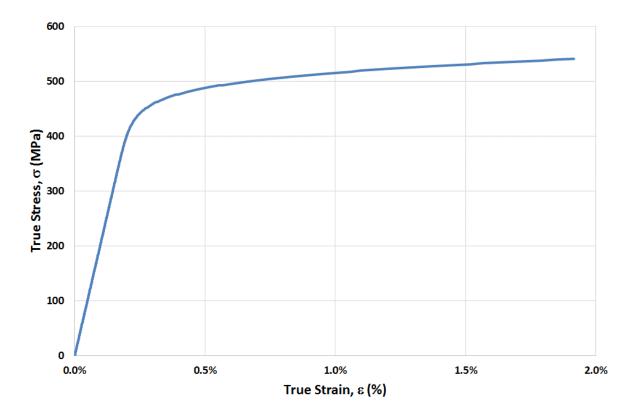


Fig. 13. Typical Stress-Strain Curve for Pipeline Carbon-Steel Material

The assumed 4.8km length of 14inch pipeline is continuously deformed in wave-like shape of 48.8m wavelength that is defined by the sinusoidal function given in Eq. (6). The amplitude of each lobe, ω_0 is 0.71m (i.e. 2 x OD of the pipeline) which is equivalent to a maximum bending strain of 0.1% at the apex of the lobe which remains in the elastic range (Fig. 13).

Fig. 14 presents the initial shape of the 4.8km length perfect pre-deformed pipeline model. The scale on the graph is highly exaggerated. The amplitudes in comparison to the pipeline length are much smaller. Considering the 2 lobes in the 1:1 scale shown in Fig. 15, the amplitude of the pre-deformation is, from a practical viewpoint, hardly noticeable.

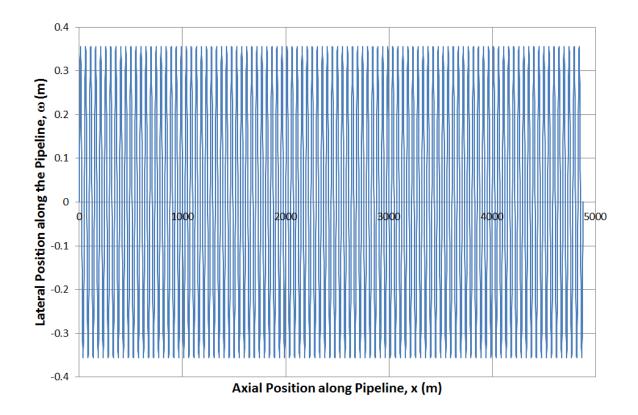


Fig. 14. Initial Shape of Perfect Pre-deformed pipeline

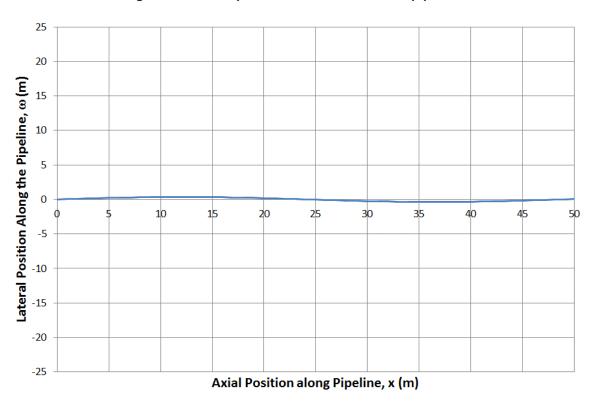


Fig. 15. Initial Shape of Perfect Pre-deformed pipeline (two lobes in 1:1 scale)

At both ends of the pipeline, two spring elements, one acting along the pipeline axial direction and one acting on the pipeline lateral direction are modelled with a linear elastic stiffness of 100kN/m to represent a typical practical stiffness of end expansion spools.

6. Finite Element Analysis (FEA) Modelling

Finite Element software ABAQUS 6.14 (Abaqus, 2014) is used to model the example of a predeformed pipe on the seabed. The FEA modelling exemplified in this section is intended to show the advantage of using a pre-deformed pipeline in controlling lateral buckling.

6.1 Pipe Elements

The pipe elements used for modelling the flowline in ABAQUS 6.14 are PIPE31H (Abaqus, 2014). This pipe element from ABAQUS is 3D two node linear pipe element with 6 DOF at each node and numerical integration of material response at 32 integration points around the circumference. PIPE31H uses Timoshenko beam formulation that allowed transverse shear deformation. 'H' at the end of the element name in ABAQUS defines hybrid formulation. Hybrid beam elements are used to improve numerical convergence of beam where the axial stiffness of the beam is much larger compared to the bending stiffness (Abaqus, 2014). This is useful especially in lateral buckling analysis of where axially rigid long beam or pipeline undergoes large rotation when it buckles.

6.2 PSI and Seabed Modelling

In all the example FEA calculations, the seabed is modelled as a flat horizontal rigid surface. Contact pairs are used to model the interaction between the flowline and the seabed surface. ABAQUS user subroutine FRIC (Abaqus, 2014) is used to capture the effect of independent axial and lateral components of the contact surface. The subroutine is also necessary to account for a tri-linear lateral resistance behaviour for the pipeline first start-up. Both axial and lateral resistance are also assumed to be independent of vertical penetration of the slave surface, i.e. the pipe element into the master surface, i.e. rigid surface. Therefore, an increase in embedment does not result in higher friction values.

6.3 Loading

The submerged weight of the pipeline is simulated by applying a uniform distributed weight on the pipe element. No external pressure is applied. Initial temperature is assumed to be 0°C. Internal pressure of the pipeline prior to operating is assumed to be 0bara. Operating temperature and pressure are simultaneously applied in constant increments.

7. Results and Discussion

7.1 Perfect Initial Sinusoidal Pre-Deformation

In this analysis case, the initial as-laid pre-deformed pipeline (PDP) has no variation in the imposed out-of-straightness, which comprises of identical equally-sized sinusoidal lobes. Each of the lobes are uniform in shape as shown in Fig. 14 and Fig. 16. Fig. 16 taken from ABAQUS presents the detailed view of the initial shape of the perfect pre-deformed pipeline (blue lines) and after application of operating temperature and pressure (red lines) respectively. It can be seen in Fig. 16 that the amplitude of each lobe increases and the pipe displaces laterally to maintain its initial sinusoidal shape. Maximum displacements at each lobe are not uniform but there is no localization of deformation of a single lobe (i.e. feed-in of deformation into one or a few lobes caused by structural instability).

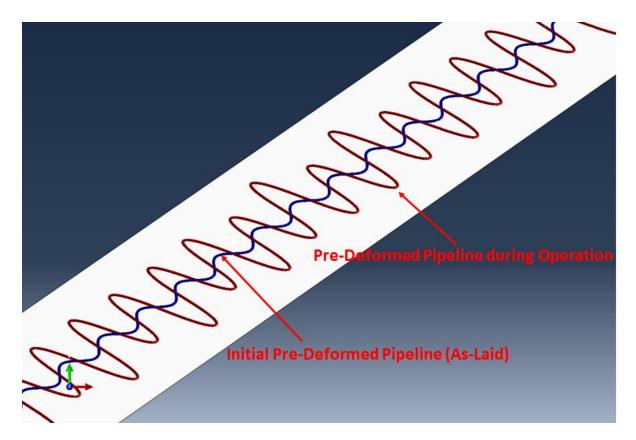


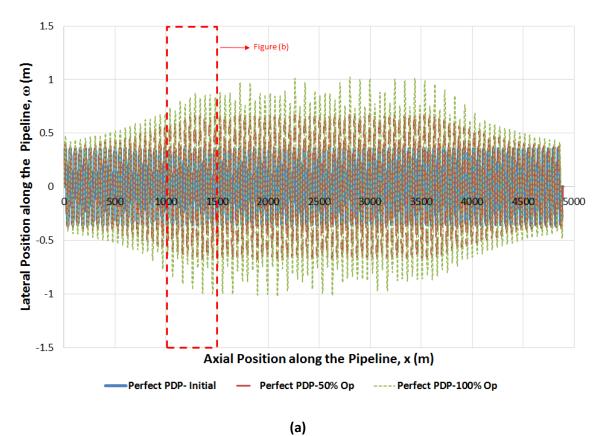
Fig. 16. Lateral Deformation of Perfect PDP during operating condition

Fig. 17 (a) presents the lateral deflection of the pre-deformed pipeline with 0% Operating Load, (i.e. ambient temperature and pressure of 0°C and 0bara), at 50% Operating Load (100°C and 100bara) and 100% Operating Load (200°C and 200bara). A section along the length from Fig. 17 (a) is expanded for a closer view of the lateral deflection and is presented in Fig. 17 (b). It can be seen that the lobes of the initial shape simply displace into higher amplitude lobes but the overall shape of the pipeline has not significantly changed.

Fig. 18 presents the effective axial force along the pipeline for both initially 'perfect' pre-deformed pipeline (PDP) and 'straight' pipeline for comparison. 'Perfect' pre-deformation means that the lateral amplitudes and wavelengths for each lobes are identical along the pipeline. The axial force at both ends of the pipelines are non-zero due to the assumed stiffness of the spring element used to simulate the end expansion spools as mentioned in Section 5. The end expansion of the straight pipeline is 6.1m at 100% loading whereas the PDP imposes only 2.1m of expansion at the termination. This reduction in end expansion is a further benefit of the PDP approach since it reduces the severity of the end expansions that must be tolerated at the termination structure

It can be seen that the maximum effective axial force of the 'straight' pipeline is more than double that of the PDP. This is because the axial stiffness of the PDP is so much lower than the 'straight' pipeline. Another significant difference is that the effective axial force profile for the perfect 'straight' pipeline behaves as a 'short pipeline' where the fully constrained effective force is not attained while the PDP behaves as a 'long pipeline' where it reaches the fully restrained force which is much lower compared to fully restrained effective force of the 'straight' pipeline (as shown in Fig. 9).

No changes in mode shape of the lobes or effective axial force profile of the pre-deformed pipeline occur. This is confirmed by Fig. 19, which is the plot of effective axial force against the percentage of operational loading taken at mid length of the PDP and the perfectly 'straight' pipeline. It can be seen that the effective axial force for both PDP and perfectly 'straight' pipeline in Fig. 19 keeps increasing with temperature and pressure loading with no drop in the axial force as no mode changes occur in both the pipelines. However, the effective axial force of the 'straight' pipeline increases linearly with operating load while the rate of change of effective force for PDP is decreasing with operating load. The change of slope of the axial force against operating load for the straight pipeline that occurs at about 15% of the operating load is due to the pipeline changing from being a 'long pipeline' with fully restrained section to 'short pipeline' with only partially restrained section. This is because at about 15% operating load, the axial resistance of the soil is no longer able to resist the axial expansion of the pipeline.



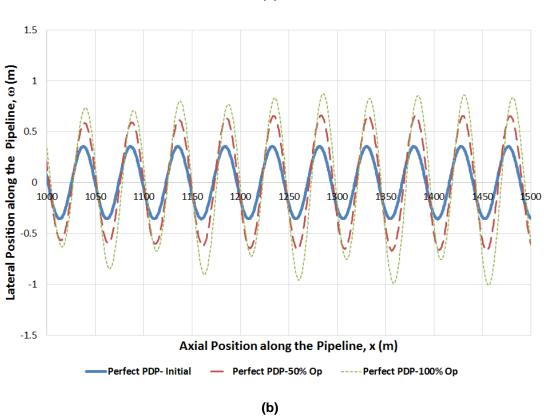


Fig. 17. Lateral Deflection for Perfect Pre-Deformed Pipeline

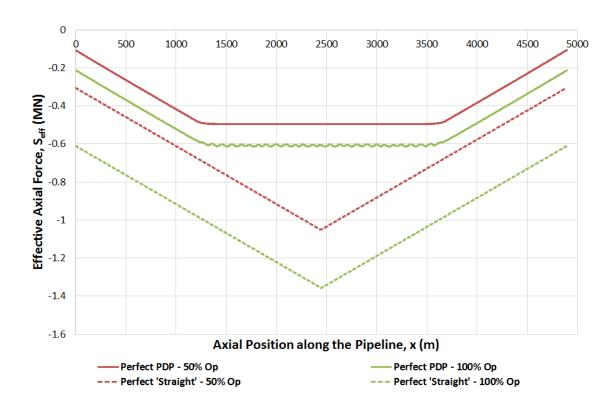


Fig. 18. Effective Axial Force for Perfect Pre-Deformed and 'Straight' Pipeline

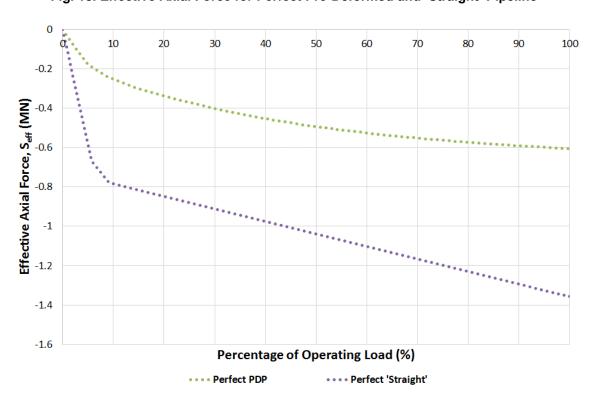


Fig. 19. Variation of Effective Axial Force with Operating Load at mid length of Perfect Pre-Deformed and 'Straight' Pipeline

Increasing the temperature and pressure to 100% of operating load shows that there is no localisation of any of the lobes. At 50% and 100% operating load, the maximum longitudinal strain along the pipeline is 0.22% and 0.41% respectively as shown in Fig. 20. The maximum longitudinal strain for the perfectly 'straight' pipeline is 0.14% and 0.26% at 50% and 100% operating load respectively. The longitudinal strain for the pre-deformed pipeline is higher due to the bending strain of the pre-deformed lobes while the longitudinal strain of the perfectly 'straight' pipeline has only axial component with no bending.

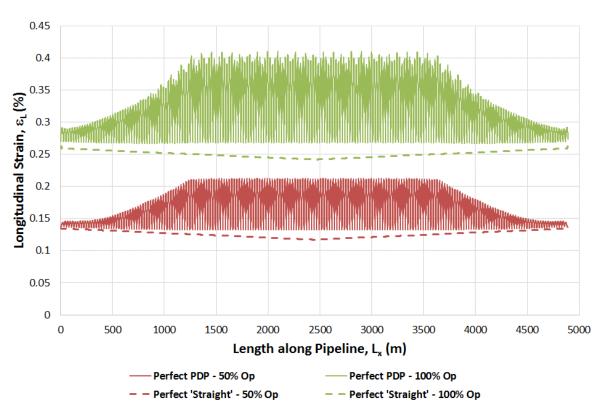


Fig. 20. Longitudinal Strain for Perfect Pre-Deformed and 'Straight' Pipeline

7.2 Imperfect Initial Sinusoidal Pre-Deformation

The analysis results from Section 7.1 are based on a perfect as-laid pre-deformed pipeline where all initial sinusoidal lobes are geometrically identical, i.e. with no imperfections or additional out-of-straightness. In reality, during the process of pre-deformation and laying of the pipeline, there are likely to be tolerances in deforming the pipeline. Variation of lateral amplitude up to a maximum of +/-0.1m is assumed to occur among the lobes. The 'imperfect' lobe maximum magnitude, ω_0 , within the assumed tolerances, is applied randomly to individual lobes.

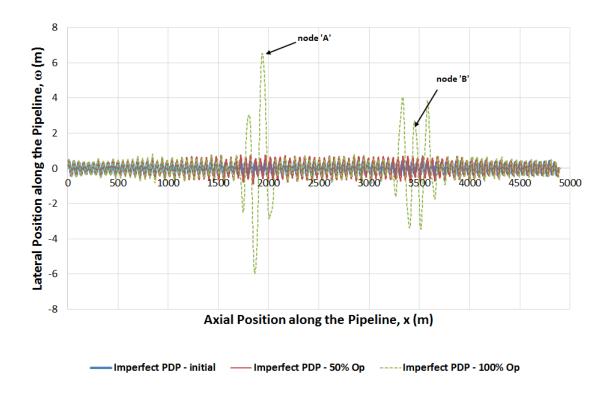
Fig. 21(a) shows the results of applying temperature and pressure to the randomly defined lobe amplitudes of the pre-deformed pipeline. It can be seen that two areas of buckling occur for this example case. "Buckling" is defined here as the occurrence of structural instability resulting in a dynamic or quasi-static change of geometry of the structure. The first buckle occurs at 1800m along the pipeline and as the temperature further increases the second buckle occurs at about 3500m along the pipeline, thus splitting the pipeline into a series of 'short pipelines' with limited feed-in length which are self-induced without the use of structural buckle initiators. This means that the axial feed-in lengths are shorter, thus, limiting the axial forces to accumulate in the buckled lengths of the pipeline. This process ultimately decreases the lateral deflection of the buckles compared to a single buckle 'straight' pipeline.

Node 'A' (at 1800m) and 'B' (at 3500m) on Fig. 21(a) are locations at two buckles along the pipeline that are used for plotting the effective axial force variation with operating load presented in Fig. 23.

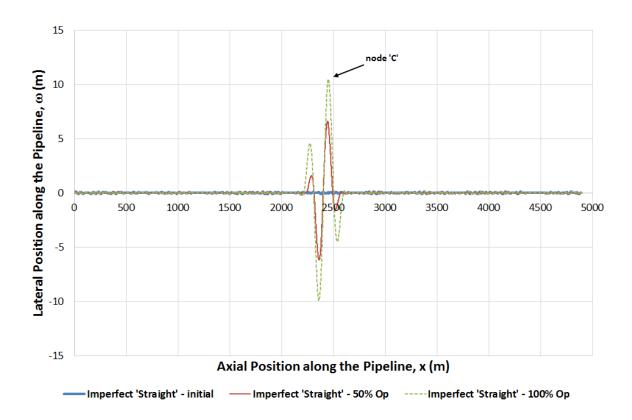
To illustrate the difference in the effect of random out-of-straightness features on a PDP and a conventional 'straight' pipeline, Fig. 21(b) shows the results of applying temperature and pressure to a 'straight' pipeline incorporating identical levels of random lateral deformation amplitudes as for the PDP (i.e. sinusoids of amplitude selected randomly in the range +/-0.1m every 48.8m). For the 'straight' pipeline only one buckle occurs in the middle at about 2500m along the pipeline. Increasing the temperature and pressure above the buckle initiation of the imperfect 'straight' pipeline increases the deflection of this buckle as the axial force keeps feeding into the deformed area. Node 'C' on Fig. 21(b) is a location at the buckle that is used for plotting the effective axial force variation with operating load presented in Fig. 23.

The longitudinal strain results along the imperfect pre-deformed and imperfect 'straight' pipeline are plotted in Fig. 22. It can be seen that at 50% of the operating load, the 'straight' pipeline with imperfection has already buckled and the maximum strain peaks at 0.29% at the buckle. For the pre-deformed pipeline, there is no buckle occurring at 50% of the operating load. The strain is distributed fairly uniformly at 0.23% along the fully restrained section (1000m to 4000m) of the pre-deformed pipeline. At 100% of operating load, the buckle strain from the imperfect 'straight' pipeline has grown to 0.48% while the maximum strain of the buckles is 0.46% for the PDP.

In practice, it would not be acceptable to assume the lateral buckling would occur due to small initial deformation and structures would be placed along the 'straight' pipeline to induce larger initial deformation.



(a) Imperfect PDP



(b) Imperfect 'Straight' Pipeline

Fig. 21. Lateral Deflection for Imperfect Pre-Deformed and Straight Pipeline

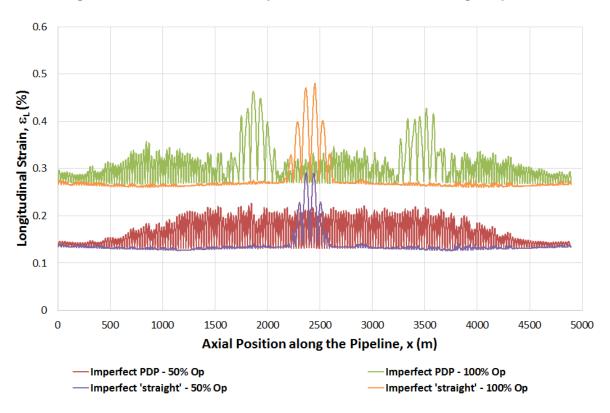


Fig. 22. Longitudinal Strain for Imperfect Pre-Deformed Pipeline and 'Straight' Pipeline

The physics of buckling along the pipelines is evidently controlled by the temperature (and pressure) at which buckling occurs. In order to determine the buckle initiation forces, and the stability conditions at various values of operating load, the effective axial force of the pre-deformed pipeline is plotted against the operating loads and is shown in Fig. 23. The locations where the effective axial force variation is taken is at Node 'A' and 'B' for PDP on Fig. 21(a) and Node 'C' on Fig. 21(b). These represent the nodes at which the maximum deflection and longitudinal strain occur. Also plotted in Fig. 23 are the effective axial force variations for perfect PDP and 'straight' pipe from Fig. 19.

It can be seen in Fig. 23 that the FEA modelling of a 'straight' pipeline with random imposed imperfection has a sudden drop of effective axial force consistent with the occurrence of a buckle at 16.2% of the operating load, which is 32.3°C (with corresponding pressure of 32.3bara). For the predeformed pipeline, tracing the effective axial force with increasing operating load at Node 'A' shows that the pre-deformed pipeline with random imperfections first buckles at this location (approximately 1800m along pipeline) at 74.8% operating load, which is 149.6°C (with corresponding pressure of 149.6bara). A second buckle was formed at Node 'B' (approximately 3500m along pipeline) and tracing the effective axial force variation at this location shows the buckle initiates at about 83.0% of the operating load, or 166.0°C (with the corresponding pressure of 166.0bara).

This is a significant increase in the operating loads at which onset of buckling occurs for the imperfect PDP compared to the 'straight' pipeline with random imperfection. This means that if this example pipeline with the specified out-of-straightness in the pre-deformed shape, is operating at differential temperature of 149.6°C and below, unplanned lateral buckling is very unlikely to occur. Assuming the average ambient temperature of 20°C, the operating temperature of the pipeline has to be about 170°C to initiate a buckle if the method of pre-deformation is used in controlling lateral buckling with the assumed levels for random 'imperfections'.

Another notable point that is that the use of Hobbs analytical method from Eq. (1) predicts lateral buckling for an initially perfect 'straight' pipeline to initiate at 6.0% of the operating load, i.e. about 12°C and 12bara. This shows that using Hobbs for calculation of lateral buckling is extremely conservative for this example case. A much higher temperature can be applied before buckling occurs.

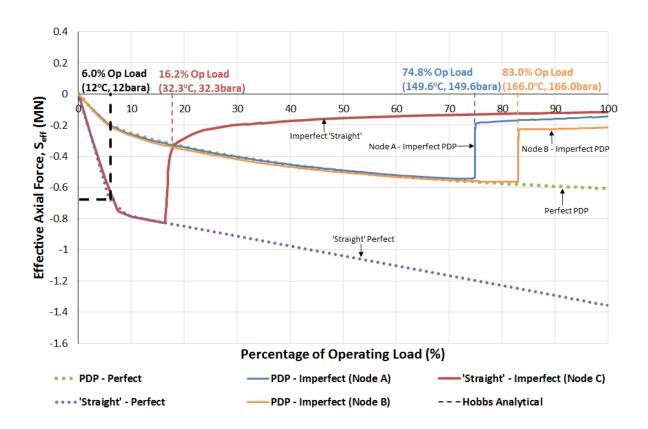


Fig. 23. Effective Axial Force vs Operating Load

Fig. 24 presents the changes in the effective axial force profile along the pre-deformed pipeline as the pipeline buckles when subjected to various increments of the operating load. Fig. 24 shows the effective axial force profile reaching about -0.55MN of fully restrained effective axial force between 1200m and 3800m prior to buckling at about 74.8% of operating load (i.e. 149.6°C and 149.6bara). Increasing the temperature and pressure slightly to 74.8% operating load initiates a buckle at 1800m and it can be seen that the effective axial force at that location drops significantly to -0.38MN.

Increasing the temperature and pressure further to 83.0% operating load as shown in Fig. 24 shows

that the effective axial force at buckle location, i.e. 1800m, is significantly reduced to about -0.17MN. A slight increase of operating load to 83.0% cause another buckle occur to at 3500m. At the end of the analysis, at applied temperature of 200°C, as shown in Fig. 24, the effective axial force profile consists of two effectively 'short pipeline' sections. The feed-in length of the buckle at 1800m is about 1880m and the feed-in length of the buckle at 3500m.

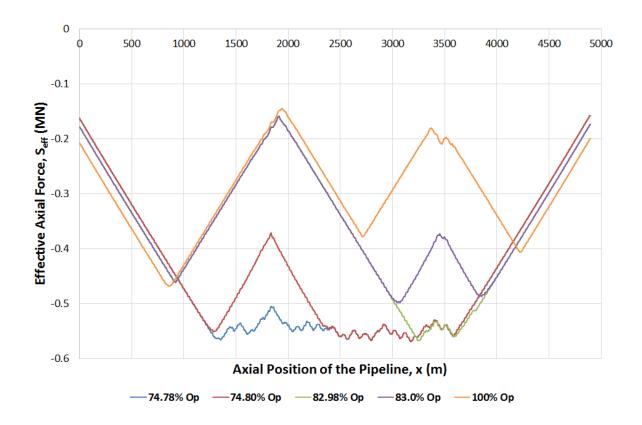


Fig. 24. Effective Axial Force Profile along Imperfect Pre-Deformed Pipeline

Fig. 25 shows how the effective axial force profile for the 'straight' pipeline with random imperfections behaves. The pre-buckle effective axial force for the 'straight' pipeline behaves as a 'short pipeline' where the drop of effective axial force occurs at about 16.3% operating load which is equivalent to 32.3°C and 32.3bara and as the temperature is increased to 100% operating load, the effective axial force keeps decreasing as the buckle develops. Feed-in length to the buckle at 200°C is 3180m.

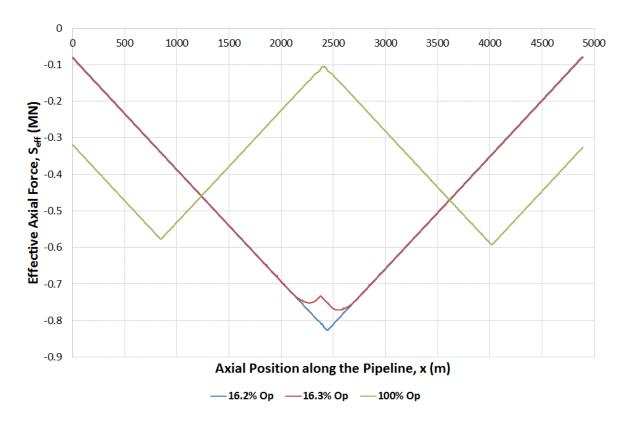


Fig. 25. Effective Axial Force Profile along Imperfect 'Straight' Pipeline

Fig. 26 presents the strain energy plot against the operating load. From the energy point of view, the system of pre-deformed pipeline tries to attain a lower energy state twice. The first initiation of instability located at 1800m occurs at 74.8% operating load, i.e. 149.6°C and 149.6bara. As the temperature and pressure increases, the second instability occurs at 83% operating load. This is shown by the two step changes in the curve as the temperature increased. In comparison with the strain energy of a 'straight' pipeline that laterally buckled, step change in strain energy during instability initiation is much more pronounced. For a 'straight' pipeline at 16.2% operating load, a lateral buckle initiates at the mid-length of the pipeline. The reduction in strain energy is almost negligible because all the axial expansion deformation is fed into a single buckle.

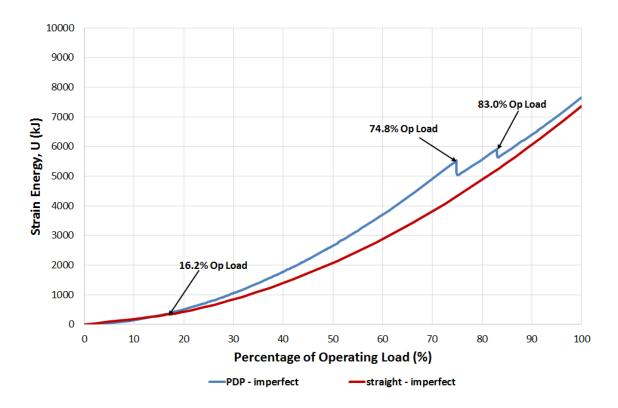


Fig. 26. Strain Energy vs. Operating Load for Imperfect Pre-Deformed Pipeline and 'Straight' Pipeline

Fig. 27 and Fig. 28 shows a detailed view of the lateral deflection of the buckle of a PDP. As a buckle develops, a few lobes will take part in the localization, hence sharing the axial load. The amplitude of deformation therefore is much lower as groups of lobes are formed instead of all the axial expansion deformations feeding into a single lobe. This phenomenon is much clearer in results from the cyclic loading of temperature and pressure which will be discussed next in Section 7.3.

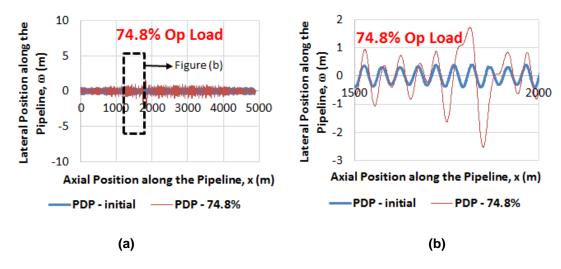


Fig. 27. Lateral Deflection of Imperfect Pre-Deformed Pipeline at 74.8% Operating Load

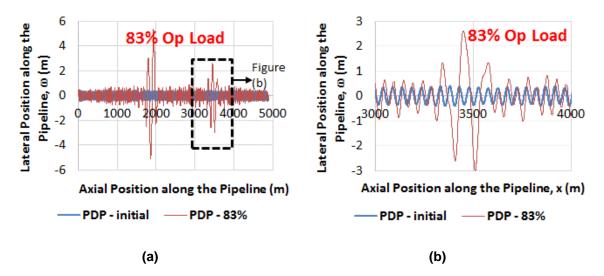


Fig. 28. Lateral Deflection of Imperfect Pre-Deformed Pipeline at 83.0% Operating Load

7.3 Cyclic Analysis

Results presented in Section 7.2 relate to the first operating cycles, i.e. the first start-up cycle. It is shown from the results of the start-up load that the pre-deformed pipeline system is highly robust and can accommodate a much higher temperature before instability occurs in comparison to a corresponding 'straight' pipeline. In this section, another important failure is considered; the fatigue limit state.

Subsea pipeline is likely to experience a number of planned and unplanned start-up and shut-down cycles of loading. These high-stress, low-cycle fatigue cycles of start-up and shut-down impose significant stress ranges on the pipeline leading to risk of fatigue or fracture failure of the pipeline girth welds.

The cyclic loading analysis presented is based on results from the same example pipeline with imperfect geometry as considered in Section 7.2. The temperature and pressure are applied and removed 10 times consecutively, simulating 10 cycles of start-up and shutdown of the pipeline. Cyclic loading and unloading analysis can be very complex due to non-linearity of the material, geometry and PSI of the analysis problem. While the pipeline goes into compression during operation, shutdown causes the pipeline to be in tension as the pipe contracts due to decrease in temperature. As shown in Fig. 29, during the first shutdown, the buckles that had formed in the pipeline during first start-up are decreased in lateral deflection but not returned to their original geometry (i.e. as-laid before first load buckling). Hence, prior to the 2nd start-up, the amplitude of the imperfections are

larger than the as-laid condition before the first start-up. This causes the buckle to occur at a lower force. The lateral deflection is also greater during the 2nd start-up in comparison to the first start-up. The lateral deflection gradually grows with the number of start-up operations. Fig. 30 presents the lateral deformations along the example pipeline during the 1st, 2nd, 5th and 10th start-up. Nodes 'A' and 'B' are the locations of the plotted variations of lateral deflections and effective axial forces for the predeformed pipeline are shown in Fig. 31 and Fig. 32.

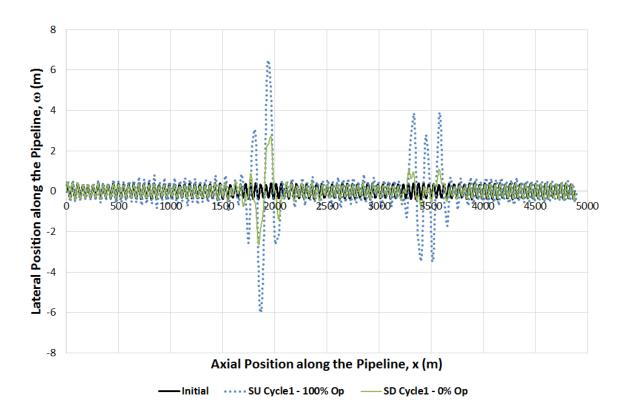


Fig. 29. Lateral Deflection of Imperfect Pre-Deformed Pipeline during the first start-up (SU) and shutdown (SD)

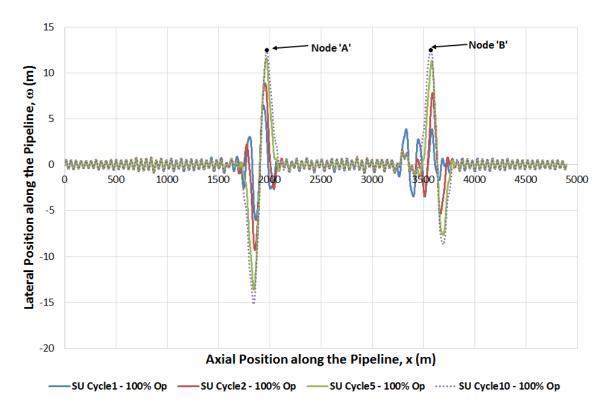
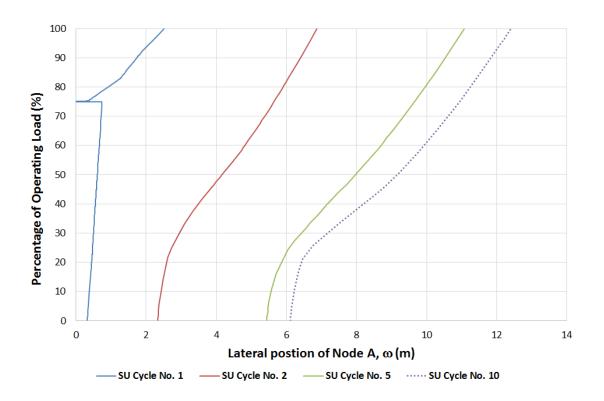
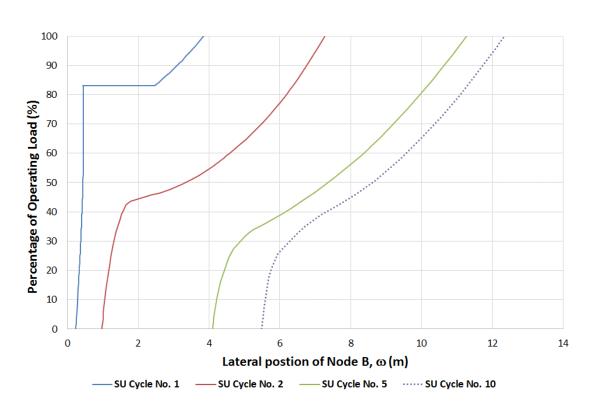


Fig. 30. Lateral Deflection of Imperfect Pre-Deformed Pipeline during 1st, 2nd, 5th and 10th Start-up (SU)

It may be seen that during the first start-up, Fig. 31(a), there is a sudden increase in lateral deflection at 74.8% Operating Load. Such a sudden increase in lateral deflection corresponding to an extremely small change in load is called 'snap buckling' (Hobbs, 1984) and is a dynamic change of pipeline geometry. As the amplitude of the imperfection at this location in the pipeline prior to the 2nd start-up is much larger than the initial as-laid imperfection, lateral buckling occurs at a much lower operating load as seen in Fig. 32 (a) and it is even arguable if this should be considered as an example of buckling. The occurrence of lateral movements is less dramatic without the 'snap buckling' effect since there is no sudden change of axial force. It is simply growth of the initial imperfection with increasing loading of the pipeline, as reported in (Hobbs, 1984; Nystrom et al., 1997). The increase in lateral deflection with operating load at Node 'B' is shown in Fig. 31(b). Similar to the buckle at location Node 'A', the amplitude of the imperfections after each shutdowns are increased, so that buckling is replaced by a continuous non-linear increase in lateral deformations due to increasing loading, as shown in Fig. 32(b).



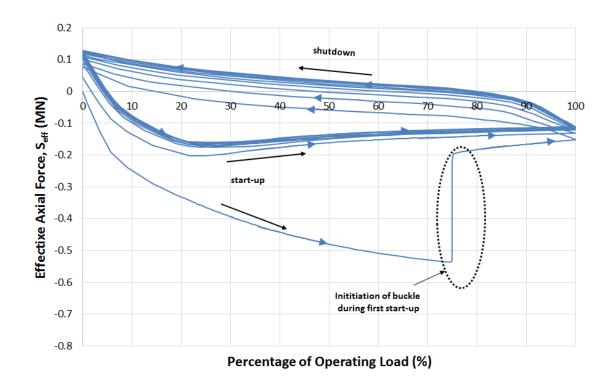




(b) Node 'B'

Fig. 31. Operating Load vs. Lateral Deflection for 1st, 2nd, 5th and 10th Start-up (SU) for Imperfect

Pre-Deformed Pipeline



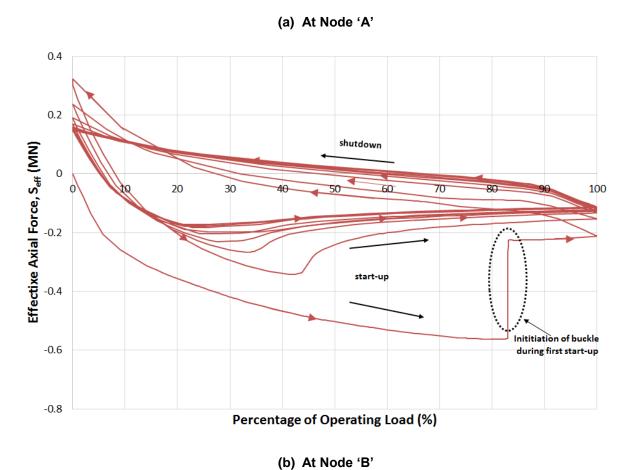
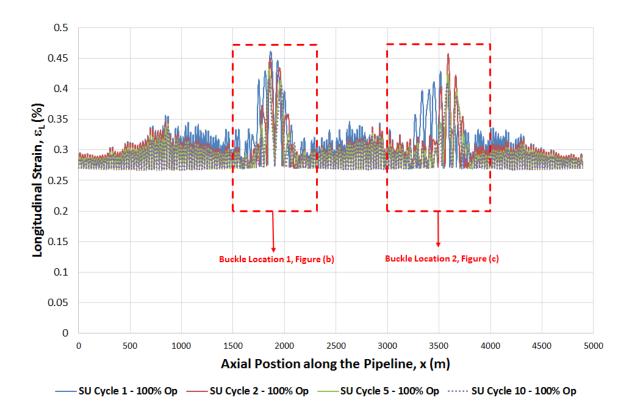
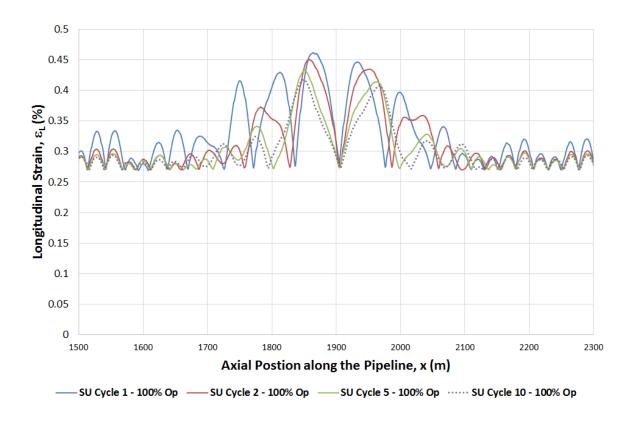


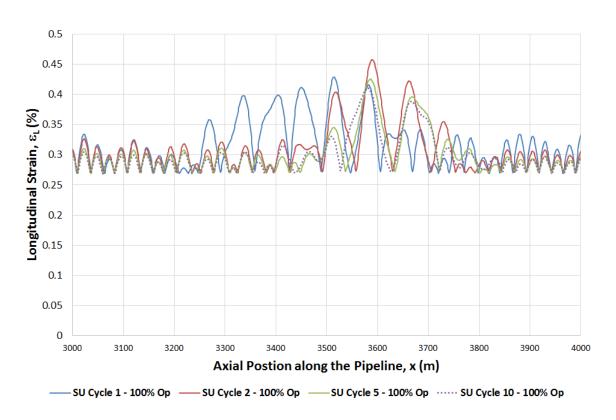
Fig. 32. Effective axial force against temperature for Imperfect Pre-deformed Pipeline

The longitudinal strain profile is shown in Fig. 33 (a) for the 1st, 2nd, 5th and 10th start-up. Fig. 33 (b) and (c) shows the expanded view of the longitudinal profile at the two locations of the buckle respectively.





(b) Expanded View along Buckle Location 1



(c) Expanded View along Buckle Location 2

Fig. 33. Longitudinal Strain for Imperfect Pre-Deformed Pipeline and 'Straight' Pipeline

The maximum strain along the PDP always occurs along the buckle location 1 and 2 as shown in Fig. 33 (a) during start-up. As the buckle location varies slightly during each start-up, the maximum longitudinal strain along the PDP at buckle location 1 from 1500m to 2300m and buckle location 2 from 3000m to 4000m at each start-up cycle is plotted instead of tracing a single point along the pipeline. This is shown in Fig. 34. The maximum strain of the PDP is highest during first start-up at 0.46%, located at buckle location 1, at maximum operating condition and gradually decreases, due to a 'shakedown' effect within the overall system of PDP lobes, to 0.42% at the end of the 10th start-up. The 'shake-down' of the strain levels along the pipeline reduces the risk of failure by fatigue at girth welds. This is an important demonstration that the PDP system has a tendency for cyclic strain ranges in the lobes to stabilise rather than grow.

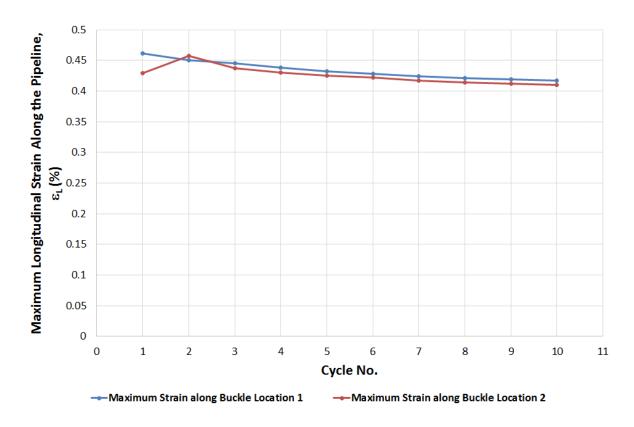


Fig. 34. Strain vs. Lateral Deflection for Imperfect Pre-Deformed Pipeline during Start-Up

Fig. 35 presents the strain energy against loading cycle for the imperfect pre-deformed pipeline. The strain energy variation during the first loading cycle is similar to Fig. 26 where the two buckles along

the pipeline occurred that lowered the energy of the system. It can be seen that a constant level of maximum strain energy is reached at start-up cycle 8.

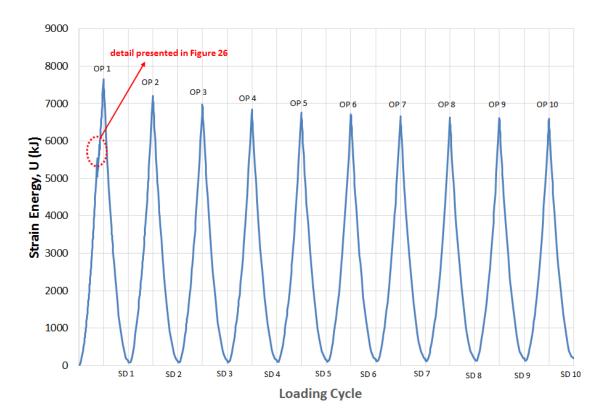


Fig. 35. Strain Energy vs. Loading Cycle for Imperfect Pre-Deformed Pipeline

8. Conclusions

Pre-deforming an initially straight pipe prior to installation into a continuous sinusoidal pre-deformed shaped pipeline has been shown to significantly reduce the axial stiffness of the pipe when installed on the seabed. This feature has the potential to control lateral buckling when the pipeline is subject to temperature and pressure loading during operation. This effect is exemplified by results from FE numerical modelling. Analytical calculations showed that for the example case of a 14inch pipeline, the PDP axial stiffness is almost half the axial stiffness of a corresponding 'straight' pipeline at infinitesimal small applied forces and the axial stiffness of the PDP decreases with applied force compared to the 'straight' pipe. This causes the effective axial force of PDP to be significantly lower than for a corresponding 'straight' pipeline. For the example 14inch pipeline case without imperfections, the maximum effective axial force for PDP at 200°C and 200bara is 45% of the maximum effective axial force for the 'straight' pipeline.

The primary conclusion drawn from the FEA modelling carried out is that pre-deforming a pipeline in the manner described here enables the pipeline to accommodate temperatures higher than typical operating temperature before lateral buckling initiates. With the example PSI properties and example random imposed out-of-straightness, a PDP pipeline initiates the first buckling only at a differential temperature, ΔT , of 150°C and differential pressure, ΔP of 150bara while a 'straight' pipeline with the same random out-of-straightness initiates at ΔT of 32°C and ΔP of 32bara. This has significant effect on the capacity of a pipeline and the practical arrangements needed to deal with thermal expansion. In fact, delaying the initiation of buckles to a much higher temperature and pressure ensures that such a pipeline would be very unlikely to buckle in maximum subsea pipeline operating temperatures of about ΔT of 100°C to 120°C. Another significant conclusion from the analysis results shown here is that the PDP initiates another buckle at ΔT of 166°C (with 166bara) at another location. This enables the formation of two sections of 'short pipelines' that limits the feed-in of axial expansions deformations to the buckled pipe length so that the maximum strain level along the pipeline is not as high as the 'straight' pipeline where the buckle localizes at one location.

This make the pre-deformed pipeline system safer and reliable as a buckle mitigation system. If in an accidental condition the operating temperature were to increase, say to 150°C compared to the design level of 120°C, the longitudinal strain of 0.46% during first load would be less than a corresponding occurrence for the nominally straight pipeline.

This study has shown that the PDP pipeline could be designed to operate at a high level of HPHT loading without the requirement of special structures installed on the seabed to control the initiation of lateral buckling and still maintain acceptable levels of axial strains. This feature has very important consequences for practical pipelines, especially long pipelines in quite deep water for which the manufacture and installation of the special structures could be very costly and have a deleterious effect on the schedule of the pipeline system.

Cyclic analysis of the PDP with 10 cycles of start-up and shutdown shows that the application of cyclic temperature and pressure loading induces a form of shake-down such that the maximum levels of strain are progressively reduced. This controls and reduces the chance of failure by fatigue.

The results to date show that the concept of pre-deforming a pipeline has potentially significant advantages for the design, installation and operation of subsea pipeline compared to corresponding

pipeline installed in a nominally straight condition. It could prove to be a valuable tool for the subsea industry as it enables the pipeline to be installed and operated safely at elevated temperatures without the need for lateral buckling design and installation of expensive structures as buckle initiators. The system is shown to be robust and able to adjust itself by geometry rearrangement to minimize the energy by creating a series of 'short pipelines'.

The objective of this paper has introduce the concept of PDP in sinusoidal shape for controlling lateral buckling in comparison with a 'straight' pipeline. Further research is underway to determine the effect of various out-of-straightness geometries and occurrence of random variations of the PSI on the PDP response of HPHT loading and to investigate the fundamental mechanics governing the buckle initiation and geometry rearrangement with analytical study. Detail studies have been done to investigate the behaviour of infinite beams on non-linear foundation by Baek et al. (2014) and Fayyaz et al. (2017) and the influence of geometric imperfections on pipeline buckling (Gao et al., 2015). These papers will serve as the basis for the next level of research. Studies are also being made to determine the optimum shape of pre-deformation to achieve reliability in controlling lateral buckling and the feasibility installation.

Abbreviations

FEA Finite Modelling Analysis

HPHT High Pressure High Temperature

OD Outer Diameter

Op Operating

PDP Pre-Deformed Pipeline

PSI Pipe-Soil Interaction

SD Shutdown

SU Start-up

VAS Virtual Anchor Spacing

WT Wall Thickness

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