THE VOLUMETRIC RATE OF CALCIUM-RICH TRANSIENTS IN THE LOCAL UNIVERSE

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ABSTRACT

We present a measurement of the volumetric rate of ‘calcium-rich’ optical transients in the local universe, using a sample of three events from the Palomar Transient Factory (PTF). This measurement builds on a detailed study of the PTF transient detection efficiencies, and uses a Monte Carlo simulation of the PTF survey. We measure the volumetric rate of calcium-rich transients to be higher than previous estimates: $1.21^{+1.13}_{-0.39} \times 10^{-5}$ events yr$^{-1}$ Mpc$^{-3}$. This is equivalent to 33–94% of the local volumetric type Ia supernova rate. This calcium-rich transient rate is sufficient to reproduce the observed calcium abundances in galaxy clusters, assuming an asymptotic calcium yield per calcium-rich event of $\sim 0.05 M_\odot$. We also study the PTF detection efficiency of these transients as a function of position within their candidate host galaxies. We confirm as a real physical effect previous results that suggest calcium-rich transients prefer large physical offsets from their host galaxies.

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1. INTRODUCTION

Over the last decade, all-sky optical time-domain surveys have uncovered a new class of so-called ‘Ca-rich’ transients (Perets et al. 2010; Kasliwal et al. 2012; Valenti et al. 2014; Lunnan et al. 2017). These events have properties intermediate to those of supernovae (SNe) and novae, with characteristics that set them apart from the classical SN population: absolute magnitudes in the range of $-15$ to $-16.5$ mag, a rapid photometric evolution with rise times of 10–15 days, photospheric velocities of 6000–11000 km s$^{-1}$, and a fast spectroscopic evolution to calcium-dominated nebular spectra.

The number of published events remains small: Lunnan et al. (2017) considered a combined sample of 8 events with good photometric coverage. These objects all occurred in the outskirts of early-type galaxies, at $\sim$8–80 kpc from the centers, and a tentative preference for cluster environments. This suggests a metal-poor (and perhaps also old) explosion environment, ruling out a massive-star origin if they are formed in situ. Yuan et al. (2013) showed that their locations are consistent with globular cluster distributions. However, photometric searches for globular clusters at the positions of known Ca-rich transients have, on the whole, been unsuccessful (Lyman et al. 2014; Foley 2015; Lyman et al. 2016; Lunnan et al. 2017).

Several progenitor scenarios have been suggested to explain the physical origin of Ca-rich events. These include helium-shell detonations (without core detonations) on the surface of low-mass carbon-oxygen (CO) white dwarfs (Waldman et al. 2011), collisions in binary systems involving a He donor and a CO or ONe white dwarf (García-Berro et al. 2017), and suggestions that they may result from the tidal disruption of CO white dwarfs by intermediate-mass black holes (Rosswog et al. 2009; Metzger 2012; Sell et al. 2015).

Ca-rich transients may also play an important role in other areas of astrophysics. A long-standing puzzle is the origin of the observed Ca/Fe over-abundance in the intra-cluster medium (ICM; de Plaa et al. 2007; Mernier et al. 2016a), which cannot be explained by the yields of traditional SN classes such as core-collapse SNe and SNe Ia. Mulchaey et al. (2014) showed that a contribution from Ca-rich transients could provide a source of calcium to match the ICM measurements. The remote locations would also make them efficient at polluting the ICM, since their ejecta does not have to escape a galaxy potential (Zaritsky et al. 2004). The source of Galactic positrons has also been suggested to be due to faint thermonuclear SNe that produce the positron emitter $^{44}$Ti, with the decay of $^{44}$Ti leading to the production of $^{44}$Ca, either through the merger of two white dwarfs (Crocker et al. 2017), or as a natural by-product of He-shell detonation (Waldman et al. 2011).

However, the rate of Ca-rich transients is uncertain due to the small numbers discovered to date. This is a byproduct of the faintness and speed of their light curves which makes them difficult to detect. Absolute volumetric rates have not been calculated for a homogeneous sample of Ca-rich transients before; rather, rates relative to type Ia supernovae (SNe Ia) have been inferred. Perets et al. (2010) inspected the spectra of objects in the Lick Observatory Supernova Search (LOSS) (Filippenko et al. 2001) for possible Ca-rich candidates. An incompleteness assumption was made to produce a sample of 2.3 Ca-rich transients and 31 SNe Ia in the same search. They concluded the Ca-rich rate is some 7% of the SN Ia rate. Similarly, (Kasliwal et al. 2012) placed a lower-limit on the Ca-rich rate by comparing the number of Ca-rich events discovered in the Palomar Transient Factory (PTF; Rau et al. 2009) to the number of SNe Ia in the same volume. Without any assumption of PTF’s incompleteness, they estimated that the Ca-rich transient rate must be $>2.3\%$ of the SN Ia rate. A proper treatment of the survey incompleteness will also help explain the apparent preference for remote locations due to a potential for selection biases in their discovery (for example, it is easier to discover transients on fainter backgrounds away from galaxies).

The aim of this paper is to determine the absolute volumetric rate of Ca-rich transients, using a sample from PTF, and to determine if they have a preference for the outskirts of galaxies. PTF was an automated optical sky survey operating at the Samuel Oschin 48 inch telescope (P48) at the Palomar Observatory, specifically designed for transient detection. This paper builds on a comprehensive study of the PTF detection efficiencies presented in Frohmaier et al. (2017, hereafter F17), and applies them to a controlled sample of PTF Ca-rich events to estimate the first absolute rate of these events. Throughout, we assume a flat $\Lambda$CDM cosmological model with $\Omega_M = 0.3$ and a Hubble constant of $H_0 = 70$ km s$^{-1}$ Mpc$^{-1}$.

2. THE CA-RICH SAMPLE

A parent sample of Ca-rich SNe in PTF was presented by Lunnan et al. (2017). This identified four likely members of the class (PTF11kmb and PTF12bho, along with PTF10iuv and PTF11bij previously identified by Kasliwal et al. 2012). Their sample also included PTF09dav (Sullivan et al. 2011). However, we have excluded this object as it displays unusual photospheric spectra, and late-time spectra that include hydrogen emission (Kasli-
3. THE RATE OF CA-RICH SNE

To determine the PTF spectroscopic completeness of Ca-rich transients, Lunnan et al. (2017) searched the PTF database for all objects that had luminosities between those of SNe and novae. They found one additional transient that may be a Ca-rich event (PTF10hcw), but its sparse light curve means it does not pass our light curve quality criteria. We note that if further objects were unconfirmed in the PTF database, this would have the effect of increasing the rate of Ca-rich transients that would be determined.

Key to this approach is the PTF detection efficiency study of F17. This study simulated around 7 million point sources in the PTF survey, and studied their detection efficiency by the PTF pipeline as a function of source magnitude, host galaxy surface brightness, and various observing conditions (the seeing or image quality, the sky brightness, and limiting magnitude). From this, multi-dimensional detection-efficiency grids were constructed, allowing the detection efficiency of any point source in any PTF image (and on any arbitrary host background) to be calculated.

Our detailed procedure is as follows. We first set the area and time period over which PTF would have been sensitive to Ca-rich events. We chose 10 observational footprints from PTF over 2010–2012 with a total of 9,428 deg$^2$ of sky. Each field was observed in a rolling cadence by PTF for between 30 and 155 days ($T_{\text{obs}}^i$). These fields each have a volume $V_i$ over the redshift range $0.0035 \leq z \leq 0.03$, inside which PTF was sensitive to calcium-rich events. This volume is determined at the lower end by the redshift at which the calcium-rich transients would saturate the PTF detector ($z = 0.0035$), and at the upper end by the redshift at which the faintest of the calcium-rich transients would no longer be detected by PTF ($z = 0.03$).

A value for $r_{\text{input}}$ is randomly chosen from the interval $1 \times 10^{-6} \leq r_{\text{input}} \leq 5 \times 10^{-5}$ events yr$^{-1}$ Mpc$^{-3}$, and used to randomly draw a number of events, $N_{\text{input}}$, from a Poisson distribution

$$P(N_{\text{input}}; \lambda) = \frac{\lambda^{N_{\text{input}}} e^{-\lambda}}{N_{\text{input}}!}$$

where $\lambda = r_{\text{input}} \sum T_{\text{obs}}^i V_i$ and the sum runs over the 10 fields. Each of these $N_{\text{input}}$ events are then randomly assigned a sky position, date of peak brightness, and redshift, such that they were uniformly distributed through the simulated volume and survey duration. Each event was then randomly assigned a Ca-rich light-curve template from Section 2, which was then scaled to the assigned redshift.

Simulations were then performed, replicating the operation of PTF and matching the nightly observing conditions and cadence patterns. Each time PTF ‘observed’ an artificial Ca-rich transient, the F17 efficiencies were used to statistically assess whether PTF would have detected the event at that epoch. The recovered light curves of each simulated event were then checked to determine whether they met the light-curve quality criteria for the real sample: at least four detections over at least four nights. The number of ‘observed’ Ca-rich events,
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Figure 1. The three calcium-rich transients entering our sample, and their positions on the sky. Top left: The three light curves in apparent magnitude space, together with the Bazin et al. (2009) functional fits over-plotted. The other three panels show the PTF survey area considered in each year: 2010 (upper right), 2011 (lower left), and 2012 (lower right). In each panel, the simulated areas are shown as green boxes, and the position of the calcium-rich transients as crosses. The color-coding shows the fraction of simulated events that passed the coverage cuts.

$N_{\text{obj}}$, that met the criteria, and the associated value of $r_{\text{input}}$ for that realization, were recorded.

This process was repeated for $>1.7\times10^6$ realizations of the Ca-rich rate, at which point the statistical improvement from further simulations became negligible. This resulted in the analysis of $>3.5\times10^8$ simulated Ca-rich light curves. Clearly, this method of rate calculation is computationally expensive, but the results of the simulation are easy to understand and the uncertainties can be intuitively handled.

Figure 2 shows the fraction of our simulations that resulted in $N_{\text{obj}} = 3$ as a function of the input volumetric rate $r_{\text{input}}$. The distribution is well described by a skewed-Gaussian, and we use this functional form to estimate the most likely value of the Ca-rich rate and the region containing 68.3% of the probability. The volumetric rate of Ca-rich transients is then

$$r_V = 1.21^{+1.13}_{-0.39} \times 10^{-5} \text{ events yr}^{-1} \text{ Mpc}^{-3} h_7^3.\,$$

The volume-weighted mean redshift of the simulation was $z = 0.023$.

This represents the first direct measurement of the Ca-rich transient rate, and is equal to around $\sim 50\%$ of the SN Ia rate at a similar redshift (Frohmaier et al., in prep). Combining our rate with assumptions on the performance of the Zwicky Transient Facility (ZTF) (Bellm 2014; Laher et al. 2017), we estimate that ZTF should discover more than 20 Ca-rich transients each year. This
order of magnitude improvement on the sample statistics will revolutionize the understanding on the volumetric rates, progenitors and environments of these events.

4. THE REMOTE LOCATIONS OF CALCIUM-RICH EVENTS

We now consider the efficiencies of recovering a Ca-rich transient as a function of distance from its host galaxy. We use the real observations of each detected Ca-rich event’s location, and the survey performance around the object discovery date, to assess whether each real Ca-rich event would have been discovered had it occurred in a different (but nearby) host environment. This allows at least a partial disentanglement of the intrinsic host environmental effects (e.g., bright galaxies) from observational effects (e.g., cadence and depth), in that we are restricted to survey periods and areas where the data were known to be good enough to discover Ca-rich events.

We begin by measuring the surface brightnesses for the Ca-rich transient host galaxies using high-quality reference images of the fields. The reference images were made from $R_{P48}$ observations, uncontaminated by SN light. Each image in the stack was resampled to a common coordinate system, and co-added to produce a deep image. Potential host galaxies for our Ca-rich events were identified in the literature (Kasliwal et al. 2012; Lunnan et al. 2017) and form the sample for our study. We then measure these galaxies in the images using elliptical apertures, and construct annuli containing fractions of the integrated galaxy light out to a distance of at least 45kpc.

We then simulate each of the three Ca-rich template light curves from Figure 1 at a random position inside each of the elliptical annuli for each galaxy. The date of peak brightness for each of the real Ca-rich transients loosely sets the date of our simulated events in the field: for each simulated event, we chose a random date of peak-brightness to be within ±20 days of the real event’s peak. We record the local surface brightness and semi-major axis distance to the center of the galaxy for each simulated event. We use the infrastructure of F17 to determine whether each simulated event would have been detected, again applying the requirement of four or more detections.

The results of our simulations – the fraction of events successfully recovered in each annulus – are shown in Figure 3. We find that galaxies with the brightest cores show a reduced recovery efficiency. However, under the assumption that the $R_{P48}$-light approximately traces the galaxy stellar mass, simulated Ca-rich events contained within the outer ∼ 50% of the stellar mass are recovered with a near constant efficiency.

Furthermore, all the Ca-rich events in our sample were found at larger distances than an isophote containing 100% of the observable stellar light (i.e., where the galaxy flux becomes indistinguishable from the background).

The final two galaxies in Figure 3 (H and I) had bright cores, such that most of the luminosity was contained in an area smaller than our spatial resolution. We therefore were unable to reliably split our simulations into different elliptical annuli, and instead show the fraction of recovered events within a single boundary containing 90% of the luminosity/stellar mass.

These simulations demonstrate that if the radial distribution of Ca-rich transients follows the stellar mass of galaxies, PTF would have been capable of finding more events than it missed i.e. the recovery fraction for the speculated hosts is ∼50% or more in an annulus containing 50% of the stellar mass. Furthermore, we performed a simple Monte-Carlo simulation of Ca-rich events under the assumption they follow the host stellar light profile. We found that <8 × 10^{-5}% of the simulations would produce all 3 events beyond the contours enclosing 99% of the host light. This allows us to confidently reject any hypothesis that suggests Ca-rich transients follow the stellar light. We conclude that the PTF Ca-rich transient sample is not significantly biased due to the performance of the PTF experiment, and that the large separation between event and host-galaxy is an astrophysically real phenomenon. This confirms previous studies that show Ca-rich transients do not follow a host stellar mass profile (Yuan et al. 2013), but with a robust consideration of the efficiency of the PTF experiment.

A final consideration on the detection efficiency relates back to the rates calculated in Section 3. If indeed there are Ca-rich transients in the cores of galaxies, where our results suggest PTF has difficulty finding such events, then these objects would increase the absolute volumetric rate we find. Since we derive our Ca-rich rate from a sample of observed events, strictly speaking it should be considered as a lower limit if a significant population of Ca-rich events are later found to occur in galaxy cores.

5. INTRA-CLUSTER MEDIUM CALCIUM ABUNDANCES

In this section we discuss the implications of our rate calculation with respect to the so-called ‘Calcium Conundrum’. Observations of the ICM show a Ca/Fe over-abundance when expected elemental yields from both SNe Ia and core-collapse SNe are included in the enrichment (e.g. de Plaa et al. 2007). It has been shown
Study of the detection efficiency of the three PTF calcium-rich transients in our sample in relation to their host galaxies. Suspected host galaxies are identified in green, and their surface brightness profiles were measured. Ca-rich events were simulated in annuli containing fractions of galaxy light. In the top panel we show that if Ca-rich events followed the light profile then PTF would have recovered more events than it missed. The efficiencies hit an apparent ceiling at larger radii as a result of the different PTF cadence experiments called the ‘5-day-cadence’ (5DC) or the ‘dynamic cadence’ experiment (DyC). The median cadences of PTF10iuv, PTF11kmb and PTF12bho discovery fields were 4.95, 0.96 and 1.00 days respectively. This result demonstrates that our Ca-rich sample is not significantly bias to remote locations, and these transient preferentially occur at large radii. The bottom panel shows the normalized cumulative fraction of galaxy light, as a function of distance from the galaxy core, for the nominal hosts. The arrows show the distance of each Ca-rich transient from the host, and highlights the remote location of the explosion environment.

that a non-negligible contribution from Ca-rich SNe can potentially resolve this observed discrepancy (Mulchaey et al. 2014; Mernier et al. 2016b).

We use the latest ICM abundance measurements (Mernier et al. 2016a) of nine elements X=(O, Ne, Mg, Si, S, Ar, Ca, Fe, and Ni) from XMM-Newton observations of 44 galaxy clusters. We then build on the work of Mernier et al. (2016b), using their abunfit routine, to estimate the ratio of different SN classes that contribute to the ICM pollution. We do not attempt to definitively state the relative rates of the different SN types, rather we investigate whether the contribution of Ca-rich SNe is compatible with our rate result.

The asymptotic elemental mass yields for our SN Ia population are described by the Chandrasekhar mass (M_{Ch}) N100 models of Seitenzahl et al. (2013) and the latest sub-Chandrasekhar mass (sub-M_{Ch}) models of Shen et al. (2017). We select our sub-M_{Ch} models to have an initial metallicity of 0.5 or 1Z_{⊙} and C/O WD masses of 0.9 or 1.0M_{⊙} - which best describe ‘normal’ SNe Ia. The implementation of both the core-collapse SNe (CCSNe) (Nomoto et al. 2013) and the Ca-rich Helium shell detonation models (Waldman et al. 2011) into abunfit are described in Mernier et al. (2016b). The initial metallicities allowed for the CCSNe are Z_{int} = (0, 0.001, 0.004, 0.008, 0.02, 0.05), and a Salpeter initial mass function is assumed. The abunfit routine performs a least squares minimization to find the relative ratios of the SN classes that contribute to the X/Fe ICM abundances. The production of Mn and Ni is especially sensitive to the initial metallicity for the SNe Ia and the progenitor model used, furthermore, Ni is poorly constrained in the ICM abundance measurements, we therefore exclude Mn and Ni from our fits. In total, 336 model combinations were fit to the ICM observations, with 149 producing physically meaningful results. Results were rejected if they required non-positive contributions from any model yield.
The volumetric rate of calcium-rich transients

We find our best-fit result \((\chi^2/d.o.f \sim 2.6)\) uses a combination of the CO.5HE.2 Ca-rich model, the Z⊙ CCSN model, the N100 SN Ia model, and the Z⊙, 1M⊙ sub-M⊙ sub-M⊙ SN model. Our next best-fitting \((\chi^2/d.o.f \sim 3.9)\) Ca-rich model, CO.5HE.2N.02, requires the same CCSN and M⊙ models as before, but a different sub-M⊙ SN model (Z⊙, 0.9M⊙).

The relative elemental yields for these results are shown in Figure 5 and clearly confirm previous claims (Mulchaey et al. 2014; Mernier et al. 2016b) that the ICM measurements require a non-negligible contribution from Ca-rich SNe to explain the Ca/Fe abundance ratio.

However, we note that while a contribution from a Ca-rich model is required to produce good fits to the ICM, their relative contribution can vary significantly depending on the CCSN and SN Ia models we select. We demonstrate this by trialling different CCSN and SN Ia model combinations for a fixed Ca-rich model. We then calculate the ratio of Ca-rich SNe to SN Ia and scale the SN Ia rate evolution (Dilday et al. 2010, Frohmaier et al. in prep.) to estimate the Ca-rich rate. Our results are shown in Figure 4, where any fit utilizing the CO.5HE.2 or CO.5HE.2N.02 model, with a \(\chi^2/d.o.f < 5\) are considered. These results place the Ca-rich rate within the range of 19%–53% of the SN Ia rate. This is compatible with both our rate from Section 3, and the rate prediction of Mernier et al. (2016b). They found Ca-rich SNe made-up ~34% of their ‘thermonuclear’ population, corresponding to a rate ~51% of the SN Ia rate.

Finally, we note that directly comparing SN rates derived from ICM abundances, and SN rates from direct observations, is a limited approach. The ICM abundance SN rates only trace events that contribute to this environment, and not elemental yields trapped in a galaxy potential. This would not necessarily be a problem if the spatial distribution of all SN classes were identical. However, as we have demonstrated in Section 4, Ca-rich SNe preferentially occur at large distances from their host - making them more effective polluters of the ICM. The SN rates measured using the ICM abundance method are also very dependent on the elemental yields estimated from the various explosion models.

We have presented three results relating to Ca-rich faint-and-fast transients; (i) using detailed simulations of PTF, we have calculated the volumetric rate of Ca-rich transients to be 33–94% per cent of the SN Ia rate,

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1 The naming scheme for the Waldman et al. (2011) models represent the mass of the C/O WD core and masses of additional layers. For example, a 0.5M⊙ C/O WD with a 0.2M⊙ Helium shell is listed as CO.5HE.2.
Figure 5. The observed ICM abundances from Mernier et al. (2016a) are shown by the green points and the relative SN contributions by the various colored lines. The overall contribution from our SN models is shown by the solid black line. The top panel represents our best-fit combination of SNe and requires a dominant population of sub-M\(_{\text{Ch}}\) SNe Ia. The next best Ca-rich model is shown in the bottom panel and requires a negligible contribution from sub-M\(_{\text{Ch}}\) SNe Ia. We find that the required Ca-rich rate to explain these abundances is highly dependent on initial metallicity/mass of our other SN classes, but that in all cases a significant Ca-rich population is required.

higher than previously suggested; (ii) we confirm, using detection efficiencies from PTF, that Ca-rich events have an intrinsic preference for locations significantly offset from their host galaxy centers; (iii) we demonstrate that a non-negligible contribution from Ca-rich transients, compatible with our rate, can explain the observed ICM elemental abundances.

Attempts to unveil the intriguing nature of these transients will benefit significantly from upcoming high cadence, wide-area (ZTF) and deep (LSST) sky surveys, where a larger number of objects can be discovered. Key to this understanding will be early detections so that follow-up spectra and multi-color photometric observations can be obtained. Ultimately, studies on light curve diversity and evolution will lead to tighter constraints on the explosion models and the asymptotic elemental yields for ICM abundance analyses. Of course, large samples of Ca-rich events will also improve the statistical uncertainties associated with the rate calculations and offer better insights into the host environments of these transients.

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**Software:** astropy (Astropy Collaboration et al. 2013), astropy/photutils (Bradley et al. 2016), abunfit (Mernier et al. 2016b), Matplotlib (Hunter 2007), NumPy and SciPy (van der Walt et al. 2011), LMFIT (Newville et al. 2014)

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