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Calculation of surface potentials at the silica-water interface using molecular dynamics: Challenges and opportunities

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Continuum-based methods are important in calculating electrostatic properties of interfacial systems such as the electric field and surface potential but are incapable of providing sufficient insight into a range of fundamentally and technologically important phenomena which occur at atomistic length-scales. In this work a molecular dynamics methodology is presented for the calculation of interfacial electric field and potential calculations. The silica-water interface was chosen as an example system, which is highly relevant for understanding the response of field-effect transistors sensors (FET sensors). Detailed validation work is presented, followed by the simulated surface charge/surface potential relationship. This showed good agreement with experiment at low surface charge density but at high surface charge the results highlighted challenges presented by an atomistic definition of the surface potential. This methodology will be used to investigate the effect of surface morphology and biomolecule addition; both factors which are challenging using conventional continuum models. © 2018 The Japan Society of Applied Physics

Introduction

24 Accurate calculation of the interfacial potential is vital to a 25 range of fields of study such as membrane biophysics, 1,2) 26 semiconductor-oxide³⁾ or oxide-oxide⁴⁾ interfacial dipole 27 layer physics. Changes in this electrostatic potential are also 28 crucial for interpreting, predicting and engineering the 29 response of potentiometric biosensing platforms such as 30 ion-sensitive field-effect transistors (IS-FETs)⁵⁾ and fieldeffect biosensors (BioFETs).^{6,7)}

The vast majority of BioFET models incorporate a model 33 of the electrical double layer primarily based on either the ³⁴ Poisson–Boltzmann equation^{8–18)} or the linearised Poisson– 35 Boltzmann equation, 19-22) which were first developed in the ³⁶ early 20th century.²³⁾ For example, the Grahame equation is 37 often used to model DNA response, where the DNA is essentially assumed to be part of the surface charge.^{24–26)} 39 Such predictions cannot provide quantitative accuracy for 40 biosensor response, 21,27) and sometimes provide qualitatively 41 incorrect results.²⁰⁾ Some more recent attempts at modelling 42 BioFET response treat the charges on the biomolecule 43 discretely in a continuum solvent; 20,21,28,29) such approaches 44 provide a good compromise between atomistic and contin-45 uum techniques, but neglect effects such as steric hindrance 46 of counter-ions, biomolecule dynamics, surface morphology 47 and water polarisation which are important for some systems.

Molecular dynamics calculation of electrostatic potential 49 differences has the ability to provide a significant advantage 50 over these continuum models, in that it can in principle 51 describe biomolecular systems without system-specific 52 empirical parametrisation (e.g., choice of a permittivity 53 constant for a specific system of biomolecules 30). This is 54 achieved via instead using standard transferable molecular 55 dynamics simulation parameters ("forcefield") for the atomic 56 interactions. Using molecular dynamics thus reduces the risk 57 of model overfitting when using the simulation to predict 58 response due to biomolecular analyte. A further advantage 59 of molecular dynamics simulation in this field is that steric 60 effects are modelled, which means that it can provide insight

61 into electrostatic potential changes due to, for example, ion

displacement by analyte molecules, or due to changes in the 22 silica surface morphology.

In previous work we used ab initio dynamics to provide 24 new insight into the energetics, dynamics and mechanisms of 25 proton-transfer reactions involved in the charging of silica 26 surfaces. 31) Subsequently, molecular dynamics simulations 27 were used to investigate the silica-water-(bio) inter-28 face^{7,32–35)} using the COMPASS II forcefield.³⁶⁾ This force- 29 field has the advantage of accurate simulation of water 30 dynamics, including H-O bond stretching. The study high- 31 lighted the importance of water polarisation and salt 32 concentration in controlling electrostatic properties at these 33 interfaces, 7,32-35) and demonstrated the effects of divalent 34 electrolyte, such as charge inversion. One limitation of that 35 work was that the computational expense of the COMPASS 36 II forcefield permitted simulation times potentially too short 37 to fully explore the range of conformational space involved in 38 counter-ion adsorption/desorption processes.

In this work, the less computationally expensive 40 INTERFACE forcefield is used³⁷⁾ which permits significantly 41 longer simulation duration (hundreds of nanoseconds) than 42 COMPASS II, whilst also offering the benefit of being well- 43 experimentally validated explicitly for silica-water systems. 44 A molecular dynamics methodology for accurate electrostatic 45 property evaluation is validated using a silica-water system 46 as a model system, with careful attention paid to ensuring 47 reliable results such as the choice of electrostatics evaluation 48 algorithm and model system setup. Proceeding from our 49 previous conference paper, 38) which included experimental 50 data collated for the surface potential/pH relationship at the 51 silica-water interface, we herein present simulation data for 52 comparison. This will provide a foundation for future work 53 in which the model is used to investigate the effect of 54 biomolecule addition (biosensing) and changes in surface 55 morphology (IS-FET characteristics).

The following background is split into two subsections: 57 firstly, background relating to accurate evaluation of electro- 58 statics, followed by a brief overview of relevant background 59 for charging at the silica-water interface.

1.1 Accurate electrostatics evaluation for surface2 systems: EW3DC

3 A method for the rapid evaluation of Coulombic interactions 4 between periodic images is required for the accurate 5 calculation of the electrostatics properties of the system in 6 molecular dynamics simulations. Molecular dynamics simu-7 lation commonly operate using a three-dimensional Ewald 8 summation³⁹⁾ to model a system that is periodic in all three 9 dimensions (x, y, z). Whilst the method originated as far back 10 at the 1920s, the optimal choice of electrostatic boundary conditions remains an active research area and can have a 12 large effect on the accuracy of the result. 40) The boundary 13 conditions associated with the 3D Ewald summation have 14 resulted in some conceptual ambiguity because the total 15 electrostatic energy per unit cell ("coulombic lattice sum", U) 16 is not well defined; it is mathematically dependent upon the order in which the summation is performed, 40-42) i.e., it is a 18 conditionally convergent series. A more detailed description 19 of this topic can be found in the online supplementary data 1 http://stacks.iop.org/JJAP/57/00XX00/mmedia, but in ief, the boundary term of the Ewald summation includes boundary term, U^{IB} , in the form of a series expansion in 23 reciprocal space (k) taken at the limit $k \to 0$. At this limit in 24 reciprocal space, the behavior is dominated by the behaviour 25 at infinite distance in real space. 41)

When the term is neglected ($U^{\rm IB}=0$) we arrive at what is called the "tinfoil" or "conducting" boundary condition as it can be interpreted as embedding the lattice in a conducting medium with an infinitely large dielectric constant. ^{40,43}) The 3D Ewald summation with these tinfoil boundary conditions has become the de facto standard for handling electrostatics in molecular simulations, ⁴⁰) referred to as simply EW3D in this work. While EW3D (i.e., tinfoil boundary conditions) is accurate for systems with no net dipole moment, systems which have a dipole moment over the cell (i.e., net polarization) demonstrate unphysical coupling between replicas of the interfacial dipole. As a result, different boundary conditions are required. ¹⁾

When modelling polarised interfacial systems (such as lipid bilayers or oxide–liquid interfaces), the long-range electrostatic interactions can be most accurately evaluated using a 2D Ewald (EW2D) summation where only interactions between x, y periodic images are considered, 41,42,44) however, despite much work in optimising the implementation, this technique is often prohibitively computationally expensive.

Aside from EW2D, other approaches such as local molecular field $(LMF)^{45}$ and symmetry-preserving mean field $(SPMF)^{46}$ theory have shown promise for both accurate and efficient evaluation for interfacial systems, 40 but their implementation has not yet become widespread amongst available simulation software packages. An attractive alternative that is commonly practised is to instead simulate the interfacial system as a 2D slab which is periodically repeated in the z-axis with either a vacuum layer or a solvent layer separating each slab in order to minimise unphysical periodic interactions. Spohr increased the empty space between periodic images by increasing the size of the cell in the z-dimension (L_z) , and showed that the EW3D results converge to the EW2D results with increasing L_z , but that extremely large cell sizes are required. Even when L_z was five

times the lateral dimensions, convergence was not satisfactory. To highlight this issue, Yeh and Wallqvist showed that using EW3D for a quartz/water interface led to unphysical water polarisation and inaccurate electrostatic potentials, even when L_z was greater than eight times the lateral dimensions. To remedy this issue, Yeh and Berkowitz proposed utilising the planar vacuum boundary condition, which they considered a corrected form of EW3D and termed EW3DC. 1,47 This term is derived by performing the summation of the infinite boundary term (U^{IB}) with the xy to plane built up first $(|x| \to \infty)$ and $|y| \to \infty$ before taking the limit in the z-direction $(|z| \to \infty)$. 41,47 This can implemented by simply applying an effective electric field at each frame of the simulation corresponding to the cell polarisation:

$$E^{\text{EW3DC}} = \frac{-M_z}{\epsilon_0 V} = \frac{-P_z}{\epsilon_0},\tag{1}$$

where ϵ_0 , V, M_z , and P_z are the vacuum permittivity, the 18 volume of the unit simulation cell, the z-component of 19 the total dipole moment of the unit simulation cell, and the 20 z-component of polarisation, respectively. 1,47) Importantly for 21 the present work, without the EW3DC correction, unphysical 22 water polarisation results in an electric field in the bulk of 23 the water (i.e., electrostatic potential gradient in the bulk) 24 making accurate determination of the surface potential 25 impossible. This EW3DC methodology was further validated 26 by Gurtovenko and Vattulainen who found excellent agree-27 ment between the electrostatic potential profile of a control 28 system and an EW3DC corrected system. 2)

Given the importance of Ewald methods for molecular 30 simulation, other authors have extended upon the aforemen- 31 tioned methods. A more computationally efficient 3D Ewald 32 summation than EW3DC has been proposed for the case of 33 simulating electrolyte confined between infinite charged 34 walls. 48) A efficient method for incorporating the polarisation 35 contribution for systems confined between planar polarisable 36 walls has also been developed. 49) When simulating systems 37 with a net charge on the simulation cell, a further background 38 charge correction is required because M_7 in Eq. (1) then 39 becomes dependent on the choice of origin of the unit cell.⁵⁰⁾ 40 The Ewald 3D summation has also been recast in terms of a 41 sum of pairwise additive interactions, which does not provide 42 an efficient algorithm for computation but instead can be used 43 to help physical interpretation of more efficient Ewald 3D 44 summations. 41,51)

1.2 Surface charging at the silica-water interface

Chemical reactions at the surface of silica between reactive 47 silanol groups (Si–OH) and $^{+}$ /OH $^{-}$ in water are thought to 48 be the primary surface charging mechanism for hydrated 49 silica, 52) with electrolyte effects having a measurable but less significant effect. 53) Silica is negatively charged at physiological pH (pH 6–9), with a point-of-zero charge (i.e., the 52 pH for which the net charge of the surface is zero) of 53 approximately pH 2– $^{454-60}$ 0 and only gathers a positive 54 charge at extremely acidic conditions (47 PL). 61,62 0 55

The density of silanol groups is important in determining 66 the surface electrodynamic properties. In this work, ~ 5 OH 57 nm $^{-2}$ was used, as it has been used by other authors to 58 successfully reproduce experimental IS-FET data, 63) is often 59 used in IS-FET modelling 64) and has been reported as the 60 density of fully hydrated silica. 65,66)

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2. Computational methods and validation

3 2.1 Forcefield and molecular dynamics setup

4 The INTERFACE forcefield (v1.5) was used for this 5 molecular dynamics simulation work. 37,67-70) One of many 6 available forcefields, the INTERFACE forcefield is one of 7 the only forcefields parameterised to treat charged silica-8 water interfaces and likely represents the state-of-the-art for 9 accurate molecular dynamics simulation of the electrified 10 silica-water interface. Under physiologically relevant conditions (i.e., pH ~6-9), the surface is highly charged and 12 most silica-water forcefields do not have parameters to 13 describe the negatively charged silanolate groups at the 14 surface. The INTERFACE forcefield shows excellent agree-15 ment with experiment for a large range of experimental data such as water contact angle, adsorption energy of peptides (at 17 20% surface ionization), water adsorption isotherms, immer-18 sion energy in water and the cell parameters of quartz.³⁷⁾ The 19 forcefield has been used to simulate protein binding, showing 20 good agreement to measured binding isotherms. ⁶⁹⁾

The NAMD simulation software⁷¹⁾ was used for this work, 22 using 2 fs timesteps, NVT Langevin dynamics at 298.15 K with the SETTLE algorithm for all hydrogen atoms.⁷²⁾ The 24 particle mesh Ewald (PME) method is used for efficient 25 electrostatics evaluation with periodic boundary conditions, 26 using a 1 Å grid spacing and 1×10^{-6} tolerance and a local 27 interaction distance of $12 \, \text{Å}$.

Over the duration of the simulation (320 ns), several water molecules were found to evaporate into the vacuum layer and cross the z-periodic boundary and so a simple repulsive potential was employed to prevent this [Eq. (2)]. More specifically, a list of atoms which were at a z coordinate greater than that of the wall ($z_0 = 120 \text{ Å}$) was generated and updated every 100 steps (200 fs), and every step a force, F, was applied to atoms in the list:

$$F = -k(z - z_0), \tag{2}$$

where k is a harmonic force constant of $-1 \text{ kcal mol}^{-1} \text{ Å}^{-2}$.

39 2.2 Molecular model

⁴⁰ The model of the silica surface used in this work was based on the crystalline model supplied with the INTERFACE forcefield. The model, shown in Fig. 1, is derived from the (10 $\bar{1}$) cleavage plane of α-cristobalite and has Q³ isolated silanols groups of density 4.807 OH per nm⁻², with a surface area of 33.4076 × 34.8705 Ų and a slab thickness of ~25 Å. Silica atoms within ~11 Å of the bottom were rigidly constrained. The model was fully hydroxylated on both top and bottom, but in order to generate systems with surface charge, randomly selected silanol groups on the top surface were replaced with negatively charged silanolate groups as discussed in the following.

As the pH becomes increasingly alkaline, the negative surface charge density increases resulting in a more negative surface potential. The relationship between surface charge density and surface potential can be obtained by potentiometric titration of colloidal silica particles. This relationship is non-linear, but to a first order approximation can be treated as a linear relationship. In this work the linear empirical relationship presented by Emami et al.^{67,68)} is used in order to compare simulated systems of a given surface charge density to the corresponding effective pH. Specifically,

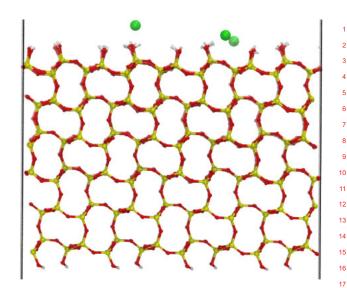


Fig. 1. (Color online) Side-on view of the periodic slab used to model the 18 silica surface in this work. Green, red, yellow, and grey atoms are sodium, 19 oxygen, silicon, and hydrogen respectively. Snapshot taken from trajectory of the $-0.09 \,\mathrm{Cm^{-2}}$ models, with the sodium ions shown introduced to maintain charge neutrality. For the crystalline system, the negative silanolate charges are all located randomly within the first atomic layer.

Increasing effective pH

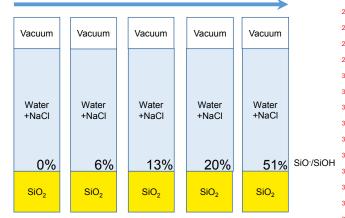


Fig. 2. (Color online) Schematic summary simulated systems, each with different surface charge density. 0, 0.0413, 0.0825, 0.1238, 0.1650, and 0.3851 C m $^{-2}$ corresponds to 0, 6, 13, 20, and 51% of silanolate to silanol groups, respectively.

approximately $0.024\,\mathrm{C\,m^{-2}\,pH^{-1}}$ was used, corresponding 45 to that measured for silica surfaces terminated by Q³ isolated 46 silanols groups, with a density of ~4.7 OH per nm⁻², at an 47 ionic strength of 0.1 to 0.3 M.

In all systems, a TIP3P water box was initialised on the 49 surface with a height of 73 Å, and NaCl was added to 50 produce a 300 mM solution (15 Na: 15 Cl ions, for this cell 51 size). Six systems were considered with surface charge 52 densities of 0, 0.0413, 0.0825, 0.1238, 0.1650, and 0.3851 53 C m⁻², corresponding to effective pH values of approx-54 imately 3, 4.7, 6.4, 8.1, 9.9, and 19, respectively. In all 55 systems, electroneutrality was maintained by introduction of 56 additional Na⁺ ions. A summary schematic of the simulated 57 systems in shown in Fig. 2. As discussed in the validation 58 section, two repeats were performed for each system with 59 different initial configurations of sodium ions, one in which 60 these additional sodium ions were initialised in proximity to 61

the surface charge, and in the other in which they were initialised randomly throughout the bulk.

2.3 Simulation analysis methodology

⁴ In order to calculate the electric potential as a function of *z*, the Poisson Equation was solved by first averaging the charge 6 density into *xy* slabs of *z* thickness δ using the VMD density 7 profile tool, ⁷³⁾ and then integrating the resulting charge 8 density using the trapezium rule, with the electric potential 9 and field set to zero at $z = 0 \text{ Å}.^{1,2)}$

For the grid-spacing convergence testing figure, a $300 \,\mathrm{mM}$ NaCl electrolyte system with silica surface charge of $0.1238 \,\mathrm{C\,m^{-2}}$ was used. The charge density was calculated over the last $90 \,\mathrm{ns}$ with $100 \,\mathrm{ps}$ between each frame used for analysis (i.e., $900 \,\mathrm{frames}$ in total). For subsequent surface potential calculation figure, the mean charge density was calculated for frames every picosecond over the last $180 \,\mathrm{ns}$. This was subdivided into three $60 \,\mathrm{ns}$ windows from which the standard error across all windows (n=3) was calculated, and multiplied by $1.96 \,\mathrm{to}$ obtain the 95% confidence intervals shown in the figure.

Unless otherwise stated, the surface potential was calculated as the potential difference between the surface and bulk water (mean value between z=80 to $85\,\text{Å}$). The bulk potential after the $180\,\text{ns}$ equilibration period was stable over time in all simulations, showing a standard deviation of $0.6\pm0.1\,\text{mV}$ (SD) across all simulations therefore not a significant source of error. The surface was defined as the deepest position at which silanolate groups (SiO⁻) were located (z=26.9 to $27.1\,\text{Å}$). To determine the specific reference point, the minima in the potential within this interval was used.

32 2.4 Validation

33 In order to accurately provide electrostatic properties from molecular dynamics simulations, careful attention must be paid to ensuring that the electrostatics are evaluated appropriately and that the simulation parameters are high enough resolution to provide the desired level of numerical precision. In this section, validation of the EW3DC method, numerical integration grid density, vacuum spacing and simulation timescale are presented. For this work, the desired precision of the calculated surface potential is within the 1–100 mV range, as detection of pH changes in IS-FET sensors involves a change in surface potential of approximately 30 mV/pH, ⁵⁶⁾ while BioFET biosensing is typically in the 1–100 mV range. ²⁷⁾

2.4.1 EW3DC validation. For this work, the EW3DC 47 correction was implemented based on the code of Yeh 48 et al.^{1,47)} and according to Eq. (1). To validate the EW3DC 49 implementation, the force acting on a pair of test charges $_{50}$ separated in the z dimension was calculated and shown in 51 Fig. 3, showing agreement with the literature. 1,44,47) The 52 correct long range limit for a 2D periodic system is such 53 that the force approaches a constant value of F_z = 54 $q_i q_i / (2\epsilon_0 L_x L_y)^{44}$ (Fig. 3, dotted black line), which shows 55 excellent agreement with the EW3DC result (Fig. 3, green 56 diamonds). This convergence to a single value is explained 57 by the fact that, as the distance between the charges increases, 58 the point-charge nature (described by Coulombs law) 59 becomes decreasingly important and the system becomes 60 increasingly akin to the interaction between charges on two 61 plates of a parallel-plate capacitor.

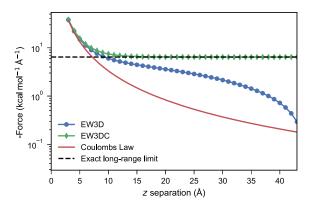


Fig. 3. (Color online) Comparison of different methods of calculating electrostatic interactions. The electrostatic z-component of the force (logarithmic axis) is shown acting upon a negative charge at position (0,0,z) 15 which is separated by z Å from a positive charge at position (0,0,0) in an x = y = 18 Å, z = 90 Å periodic cell. Forces simulated using NAMD with the standard EW3D method (blue circles) and EW3DC method (green diamonds). Coulombs law is also shown for comparison (i.e., two point charges in vacuum, non-periodic system) (red line). The correct long range limit for a 2D periodic system is such that the force approaches a constant value of $F_z = q_i q_j / (2\epsilon_0 L_x L_y)^{44}$) (dotted black line), which shows excellent agreement with the EW3DC result.

In contrast to the EW3DC and EW2D methods which 25 emulate and utilise 2D periodic boundary conditions, 26 Coulombs Law describes the behaviour of point charges 27 separated in 3D space (non-periodic), and EW3D models a 28 3D periodic system. Figure 3 demonstrates that for periodic 29 systems in which the z interactions are undesirable, such 30 as interfacial systems with 2D xy periodicity, the EW3D 31 approach for simulating long-range forces becomes highly 32 inaccurate even with large vacuum spacing between periodic 33 images. This result highlights that researchers should care- 34 fully consider the method of evaluating electrostatics 35 depending on the system of interest. The EW3DC method- 36 ology is a computationally efficient choice that can simply be 37 implemented and is presently available in many popular 38 molecular dynamics packages (e.g., GROMACS: "ewald- 39 geometry:3dc" option, LAMMPS: "kspace_modify:slab" 40 option and CASTEP: "dipole_correction").

2.4.2 Numerical integration convergence. Calculation 42 of the electrostatic potential requires double numerical 43 integration of the charge density and thus a fine mesh is 44 required for precise integration. The thickness of the grid 45 spacing upon which the charge density is discretised, δ , 46 should be suitably thin to provide sufficiently small 47 integration error. In order to investigate convergence, the 48 electric potential was calculated for $\delta = 0.001$, 0.005, 0.01, 49 0.1, and 1 Å as shown in Fig. 4. The finest grid of 0.01 Å was 50 sufficiently fine to accurately model the surface potential, as 51 demonstrated by its convergence to within 2 mV of the 52 calculated value for the 0.001 Å grid. Coarse 1 Å bins 53 provided extremely inaccurate surface potentials, highlight-54 ing the importance of such convergence studies in accurate 55 potential calculations.

2.4.3 Thermodynamic equilibrium convergence.

When calculating equilibrium properties such as the surface 58 potential, it is important to run the simulation for sufficient 59 time such that thermodynamic equilibrium can be reached. 60 This was exemplified in a study of the surface potential 61

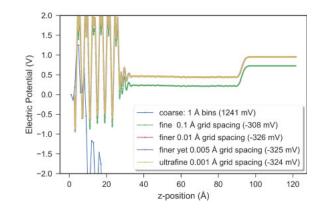


Fig. 4. (Color online) Convergence of the calculated electric potential as a function of numerical integration grid spacing. The system is a silica—water interface with the surface at ~27 Å, and surface calculated potentials are shown in brackets within the figure legend. Finer grid spacing result in more accurate integration, with 0.01 Å converged to within 2 mV of the 0.001 mesh. 1 Å bins provide extremely inaccurate surface potentials, the value being qualitatively and quantitatively inaccurate.

21 across lipid membranes which found that at least 100 ns was 22 required.²⁾ Between 3 ns^{7,32–34)} and 20 ns¹⁾ has been used in 23 the literature to calculate the surface potential at the silica–24 water interface. In this work, we significantly extend upon 25 these timeframes to investigate the long-term (to 320 ns) 26 convergence of the silica–water interface surface potential as 27 a function of time.

In order to investigate convergence as a function of time, the surface potential was calculated at time, t, based on the charge density average from t=0 to t. The time taken to reach a stable average potential is indicative of convergence and the results, shown in the online supplementary data 2 at http://stacks.iop.org/JJAP/57/00XX00/mmedia, suggested that at least 100 ns are required for an average potential which is stable within the millivolt range.

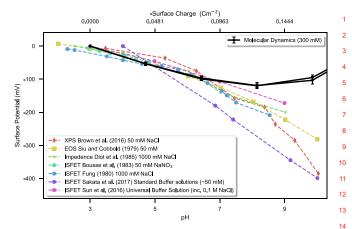
Based on this result, simulations were performed for $320 \, \text{ns}$, with the final $180 \, \text{ns}$ used for analysis. In order to quantify error from temporal fluctuations, the mean surface potential was calculated over three $60 \, \text{ns}$ windows and the standard error across these (n=3) windows was calculated. In order to further ensure thermodynamic equilibrium has been achieved, two separate simulations were run for each system with different initial conditions: both simulations should reach the same surface potential if converged to thermodynamic equilibrium.

46 **2.4.4 Vacuum layer validation and convergence.** A vacuum layer is used to minimise undesirable periodic 48 interactions between periodic *z* images. For the EW3DC 49 correction, elongation of the simulation cell to include empty

space to the extent of 3–5 times the xy dimensions of the box has been recommended in the literature $^{41,44,47)}$ which would correspond to a cell z dimension of 200 to 285 Å in this work. A z cell size of 150 Å was found to be unstable so larger cell sizes were used. Convergence testing (online supplementary data 3 at http://stacks.iop.org/JJAP/57/00XX00/mmedia) showed that z = 265, 300, and 335 Å were all stable, and surface potentials were converged to within 1 mV of each other, so 265 Å was used in this work.

Over the duration of the simulation (320 ns), several water molecules were found to evaporate into the vacuum layer and cross the *z*-periodic boundary. This "water noise" prohibits

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(Color online) Experimental silica-water surface potential as a function of pH (dashed lines, lower axis), compared to molecular dynamics simulated surface potential as a function of surface charge (black line, upper axis). The simulated surface potentials are presented relative to the system with no surface charge by subtraction of the surface potential for the zero surface-charge system. Literature data is displayed with the electrolyte used 19 in the legend, and were measured by methods indicated by marker: • X-ray 20 photoelectron spectroscopy (XPS),⁵⁷⁾ ■ electrolyte-on-insulator (EOS),⁵⁸⁾ ★ impedance, 60 and • ion-sensitive field-effect transistor (ISFET). 54-56,59) The bottom x-axis corresponds to the pH for the experimentally measured surface potential, whereas the top axis corresponds to the surface charge density used in the simulated system. These axes are aligned according to the 24 empirical relationship between surface charge density and pH for this silica 25 system as described in the methods section. For the simulated system, two repeats with different initial conditions were performed for each data point and showed good agreement, with differences only discernible at this scale at high surface charge ($\geq 0.1650 \,\mathrm{C\,m^{-2}}$). For the simulated result, error bars shown are for each simulation, and calculated as 1.96 multiplied by standard ²⁵ error between three 60 ns window averages (95% confidence interval). The 30 graph is limited to the range available for experimental data (up to pH 10). 31 The simulated data point at extremely high surface charge density $(0.1650\,\mathrm{C\,m^{-2}})$ showed a showed potential value of 396 \pm 20 mV. Lines are drawn to guide the eye.

accurate calculation of the electrostatic potential of the 36 system²⁾ and therefore, similar to other literature,⁷⁴⁾ a simple 37 repulsive potential was employed to prevent this [Eq. (2)]. 38

3. Results and discussion

In this section, the results of the simulated surface potential as 41 a function of pH are presented and discussed in the context of 42 experimental data for this system.

Figure 5 shows various literature experimental surface 44 potential measurements⁵⁴⁻⁶⁰⁾ as a function of solution pH for 45 silica surfaces from pH 2-10, shown as dotted lines. 46 Experimental potentiometric data does not generally extend 47 beyond pH 10 as silica is known to significantly dissolve 48 under such alkaline conditions⁷⁵⁾ and high pH is less 49 technologically relevant. From this data, a non-linear 50 response is seen which is approximately linear at physio- 51 logical/biosensing conditions (pH 5-9) and showed a pH 52 sensitivity of approximately 30–40 mV/pH. While most of 53 these samples were generated using thermal oxidation or 54 native oxide, the recent work of Sakata et al. was generated 55 by sputtering silica and showed an anomalously high pH 56 sensitivity around 60 mV/pH, which is the theoretical 57 "Nernst limit" for systems in which simple proton exchange 58 reactions occur. 76) In the popular site-binding model of pH 59 sensitivity, the variation between different experiments is 60 typically attributed primarily to either (a) surface hydroxyl 61

density^{64,77)} or (b) variation in the acid-base equilibrium constant of the hydroxyl groups (p K_b –p K_a). Changes in the pre-treatment of the silica are expected to significantly vary (a),⁶⁶⁾ however the extent to which (b) is relevant when comparing different silica samples is unclear as determination of p K_b /p K_a values of silica remains a challenging area of active research.^{31,62,78,79)} Interference from cation exchange from the electrolyte (due to different electrolytes and ionic strengths used between experiments) can also affect the measured surface potential shift.^{33,55)}

Figure 5 also presents the simulated surface potential as a function of surface charge density, shown as solid black lines. In agreement with experiment, with increasing surface charge density (or effective pH) up to 21% surface ionisation (0.1650 C m $^{-2}$) the surface potential decreased, with quantitative agreement for low surface charge density. Error was quantified where possible: deviation in the calculated surface potential between repeat simulations was approximately 1 to 2 mV below 0.1650 C m $^{-2}$. Error due to the stability of the potential in the bulk water was approximately 1 mV. Such errors were therefore small compared to the changes in potential with surface charge (e.g., $\sim\!\!65\,\text{mV}$ per 0.05 C m $^{-2}$).

The first layer of molecules at the interface is expected play an important role in the electrostatic properties at 25 polarised interfaces due to accumulation of counter-ions and 26 water polarisation, therefore the first peak in the number 27 density was used to calculate the density of the first layer of 28 sodium ions, chloride ions and water molecules respectively. 29 as a function of surface charge. The density of sodium ions within the first layer was found to increase linearly with 31 surface charge density, the density of chloride was found to 32 be within 1.96 standard error of each other for all surface 33 charge densities, the exception being for the most charged 34 surface (50% surface ionisation, $0.3851\,\mathrm{C\,m^{-2}}$) which 35 showed higher chloride density due to strong electrostatic 36 attraction to the dense sodium ion layer on the surface. 37 Similarly, the water density within the first layer showed no 38 clear correlation with surface charge density. Reorientational 39 water polarisation was found to increase linearly with surface 40 charge density up to a maximum value at 21% surface 41 ionisation (0.1650 C m⁻²) after which no further reorienta-42 tional polarisation occurred. These findings suggest sodium 43 ion density and water polarisation dominated the electrostatic 44 properties of the system.

In contrast to the systems with surface charge below 0.1650 C m⁻², for higher surface charge density, the surface potential began to increase with increased surface charge, particularly for the systems at effective pH 10 and above. At such high surface charge densities, there was also increased deviation in the calculated surface potential between repeat simulations (approximately 8–15 mV) suggesting poorer convergence to equilibrium. This reversal in the direction of surface potential originates from the definition used to define the "surface", and highlights a particular challenge in the calculation of surface potentials from atomistic systems:

In this work the "surface" is defined as the z position

orresponding to the potential minima associated with the position of negatively charged silanolate groups within the simulations (z = 26.9 to 27.1 Å). This definition, however, neglects the contribution from water molecules that penetrate beyond this layer and polarise. With increasing surface

charge, two effects occurred simultaneously with led to the increasingly positive surface potential: water penetration and 2 polarisation (a) and sodium ion accumulation (b). As for (a), 3 water penetration and polarisation increased which meant that 4 at high surface charge there was a large dipolar contribution 5 from orientationally polarised water below the surface which 6 was neglected under this definition of the surface. As for 7 (b), increased sodium ion concentration near the surface⁸⁰⁾ and increased electrostatic attraction between silanolate and 9 sodium ions resulted in increased penetration of sodium ions 10 between negatively charged silanolates which had the effect 11 of reducing the mean charge density at the interfacial layer, 12 and thus making the surface potential less negative. While the 13 effect of (a) is purely methodological due to how the surface 14 is defined, the effect of (b) is a process that can occur in 15 physical systems but which is not described using conven- 16 tional 1D/2D Poisson-Boltzmann-based or capacitor based 17 models, which neglect such atomic-scale details and prohibit 18 the overlap of negative surface charges and positive counter- 19 ion charge.

The difficulty in determining the relevant reference point 21 for the surface led Lee et al. to state such surface potential 22 calculations can only be approximate. 80) In principle, 23 however, a semi-empirical model could be designed in 24 which the surface definition was calibrated to experiment. 25 Gaussian smoothing can be applied to the atomistic potential 26 distribution to obtain one which is more directly comparable 27 to continuum (mean-field) models, 4) however this technique 28 does not resolve the issue of identifying the experimentally 29 relevant "surface" reference point for surface potential 30 evaluation.

Continuum models such as the Grahame equation⁸¹⁾ or the 32 Debye-Hückel equation⁸¹⁾ describe the surface as a charged ³³ layer which is separated from counter-ion charge by an 34 infinitely thin, well-defined, surface layer. As the negative 35 surface charge increases, the counter-ion charge near the 36 surface increases, and the surface potential becomes more 37 negative, as shown in the online supplementary data 4 at 38 http://stacks.iop.org/JJAP/57/00XX00/mmedia. The differ- 39 ences and similarities between atomistic models of the 40 surface potential versus continuum models of the surface 41 potential are highlighted the schematic Fig. 6. As discussed, 42 if the definition of the surface is the z-position of the 43 negatively charged silanolate groups at the surface, atomistic 44 models show the opposite trends in surface potential at high 45 surface charge when compared to continuum models and 46 experiment. If the definition of the surface was taken to be 47 inside of the silica (i.e., below closest approach of water 48 molecules), then potential differences were found to be 49 significantly larger in magnitude than those measured in 50 experiment.

While concept of surface potential is useful for direct 52 comparison to experimental measurements, the electric field 53 (i.e., the electrostatic force) is the fundamental property of the 54 system and this property and has the advantage that it can be 55 calculated accurately from molecular dynamics simulations 56 without resorting to semi-empirical calibration or issues 57 defining the surface layer. For example, FETs operate by 58 changes in the interfacial electric field modulating the 59 electron density in a semiconducting layer below the oxide. 60 In such a system, modelling the "field-effect" would be most 61

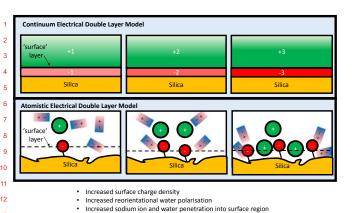


Fig. 6. (Color online) Schematic showing comparison between atomistic and continuum surface potential models. Red-blue dipolar rectangles represent the dipole from oriented water molecules. Continuum models have a clear definition for the surface and therefore a clear definition of the surface potential, but in contrast, the definition of a surface potential for atomistic models is more challenging. In continuum models, increased surface charge results in increased charge separation and more negative surface potentials. In contrast, for atomistic models, at high charge densities, charge separation between negative surface and positive counter-ions or polarised water can decrease. If the surface is defined as the layer of negatively charged silanolate groups, then this can lead to disagreement between the two models.

26 directly performed by measuring the electric field (e.g., via 27 calculating the force of a test charge below the oxide). In 28 future work, this method will be used to investigate the 29 field-effect in silica-water-biomolecule systems, with the 30 goal of improving rational design of the surface chemistry of 31 BioFETs.

To the best of the knowledge of the authors, this study 33 represents the first application of molecular dynamics to 34 simulate the surface charge-surface potential relationship for 35 silica-water systems and suggests that such a model can be 36 used to predict surface potential changes for low surface 37 charge systems. This model is not intended to supersede 38 continuum models for this application, indeed quantitative 39 accuracy of the surface charge to surface potential is highly 40 sensitive to the accuracy of the empirical relationship used 41 for pH to surface charge density (as is also often the case 42 when parameterising site-binding models for predicting pH-43 potential response), and to the definition of the surface plane. 44 This model, however, presents three key advantages over 45 conventional continuum models such as site-binding mod-46 els^{63,82,83)} and the Grahame equation for biosensing.^{24–26)} 47 Firstly, complex biomolecular systems can be incorporated 48 with relative ease and without requirement for system 49 specific parametrisation. For example, continuum-models of 50 biomolecule response often require tuning of an empirical 51 parameter specific to the experimental system such as the 52 permittivity of the biomolecule layer. 30) Secondly, experi-53 ments show potentiometric response due to binding of neutral 54 molecules such as pentane; 84) this cannot be explained by 55 continuum methods but could be explained by, for example, water polarisation effects of electrolyte displacement, both of 57 which can be modelled using this methodology. Finally, the 58 atomic-scale effects of surface morphology (e.g., roughness, 59 porosity, etc.) can be explicitly investigated. The results of 60 these applications will be presented in a future publication

61 focusing on the application of this technique.

4. Conclusions and future work

The surface charge/potential relationship for a silica-electrolyte system was calculated via molecular dynamics simu- 4 lation for the first time. Extensive validation work was 5 presented to ensure convergence of the integration density, 6 vacuum spacing and equilibrium, and to ensure accurate 7 choice of periodic boundary conditions and electrostatics 8 evaluation methodology. Error in the calculated surface 9 potential was quantified where possible, with the error 10 between repeat simulations of approximately 10 mV and 11 the error due to variation in the bulk potential of 12 approximately 1 mV. Such validation work is essential for 13 reliability and for enabling quantitative accuracy from 14 molecular dynamics simulation results. An empirical relation- 15 ship between surface charge density and pH was used to 16 provide a comparison to experimental pH/surface potential 17 measurements, and good agreement was found for low 18 surface charge density. For high surface charge density, 19 disagreement was found between the simulated surface 20 potential and that found from continuum models/experiment, 21 the reason for which was a result of the challenge of 22 presenting a rigorous atomistic definition of the surface 23 potential. For many applications, such as understanding the 24 field-effect in field-effect transistors, calculation of the 25 electric field (e.g., as the forces on a test charge) would 26 circumvent this issue while providing a more physically 27 relevant property than the surface potential.

Molecular dynamics simulation of interfacial potentials 29 presents several significant advantage over continuum 30 models for modelling interfacial electrodynamics, applications of which will be further investigated in future work. 32 Example applications include modelling the effects of 33 complex biomolecular systems, the effect of neutral analyte 34 on water polarisation and ion displacement, and also the 35 effects of surface morphology on the electric field and electric 36 potential. Given these effects are currently poorly understood, 37 insight into these would significantly improve the capability 38 for rational design of effective surface chemistry for highly 39 sensitive potentiometric biosensors.

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