

1 **Asymmetric transfer of CO₂ across a broken sea surface**

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10 **Abstract**

11 Most estimates of the climatically-important transfer of atmospheric gases into, and out
12 of, the ocean assume that the ocean surface is unbroken by breaking waves. However
13 the trapping of bubbles of atmospheric gases in the ocean by breaking waves introduces
14 an asymmetry in this flux. This asymmetry occurs as a bias towards injecting gas into
15 the ocean where it dissolves, and against the evasion/exsolution of previously-dissolved
16 gas coming out of solution from the oceans and eventually reaching the atmosphere.
17 Here we use at-sea measurements and modelling of the bubble clouds beneath the ocean
18 surface to show that the numbers of large bubbles found metres below the sea surface in
19 high winds are sufficient to drive a large and asymmetric flux of carbon dioxide. Our
20 results imply a much larger asymmetry for carbon dioxide than previously proposed.
21 This asymmetry contradicts an assumption inherent in most existing estimates of ocean-
22 atmosphere gas transfer. The geochemical and climate implications include an enhanced
23 invasion of carbon dioxide into the stormy temperate and polar seas.

24

25 **Introduction**

26 The role of the ocean in contributing to climate control and change has been recognized
27 for many years. One aspect of that role is as a significant sink of anthropogenic carbon
28 dioxide^{1,2} and a major source or sink of several other climatically-important gases.
29 Calculations of air-sea flux of each gas depend on the estimation of exchange
30 coefficients, whose values depend on wind-driven processes at the air-sea interface.
31 Most estimates implicitly assume stirring across an intact sea surface³⁻⁵, but the broken
32 surface (Fig. 1), characterized primarily by bubbles under breaking waves, should be
33 considered⁶⁻⁹. Bubble-mediated transfer is inherently asymmetric^{10,11} with a bias
34 towards injection into the ocean. Here we show that the numbers of large bubbles found
35 metres below the sea surface in high winds are sufficient to drive a large and
36 “asymmetric” flux of carbon dioxide in contradiction to previous studies. Extrapolation
37 of this finding is shown to imply a substantial effect annually and globally.

38

39 **Gas flux**

40 Estimates of the net flux of a gas across the sea surface³⁻⁵ generally assume an
 41 equilibrium based on Henry's Law and the application of a Fickian diffusion equation,
 42 usually written in the form:

$$43 \quad F = K (C_a - C_w) . \quad (1)$$

44 Here a net air-to-sea flux, F , of a gas species is proportional to the difference between
 45 the concentration of that species dissolved in the upper ocean (C_w) and C_a (the liquid-
 46 phase concentration in equilibrium with the atmosphere, a feature which eliminates
 47 solubility from this and succeeding equations). For poorly soluble gases, the diffusion
 48 across the marine microlayer (the sub-millimetre layer of liquid immediately adjacent to
 49 the absolute sea surface) determines the exchange rate^{5, 12, 13}. In a steady state most of
 50 the concentration difference is across this layer, implying that the molecular diffusion
 51 coefficient of the dissolved gas and the related non-dimensional Schmidt number, Sc ,
 52 are key factors. Since there are few measurements of air-sea gas transfer velocities, K ,
 53 most models of air-sea gas transfer¹⁴ assume a simple wind-speed dependence, scaling
 54 with Schmidt number (usually $K \sim Sc^{-0.5}$) and a strict proportionality to air-sea
 55 concentration difference as implied by equation (1).

56 If the surface is broken (e.g. by the generation of bubbles in breaking waves) then
 57 there will be a parallel pathway across these additional surfaces as gases transfer across
 58 the bubble wall. Moreover, the concentration difference driving this flux is different,
 59 since it depends on partial pressures in the bubbles, which will generally be raised due
 60 to the hydrostatic pressure on the bubbles and the effect of surface tension. In this case,
 61 equation (1) is invalid for a bubble-mediated flux, but it is proposed¹⁰ that the following
 62 modified flux equation is suitable for the bubble-mediated flux, F_b :

$$63 \quad F_b = K_b [(1 + \delta) C_a - C_w] . \quad (2)$$

64 Here, K_b is the contribution of bubbles to the air-sea transfer velocity of the gas, while δ
 65 describes an asymmetry in that transfer (see Supplementary Section S1 for a thorough
 66 explanation of the formulations used in this study). This bubble-mediated flux F_b occurs
 67 in addition to the flux directly across the sea surface of equation 1. There are two key

68 features of the model of equation (2), which invalidate widely-held assumptions. Firstly,
69 it is not credible to assume K_b will scale simply with Schmidt number¹⁵. This point
70 implies that conventional extrapolations for one gas from another may be awry. The
71 second key feature is an inherent asymmetry (embodied in δ) that favours injection into
72 the ocean (i.e. favouring dissolution of gases into the ocean over the release of
73 previously-dissolved gas from the ocean into the atmosphere)^{8,10,11}. This point is
74 potentially more far reaching, since the basic formula, equation (1), used for most
75 estimates of gas transfer is strictly incorrect and instead equation (2) should be used for
76 the bubble-mediated flux.

77 We validate equation (2) and give estimates for the transfer coefficients K_b and δ
78 by combining a model of subsurface bubble cloud evolution with measurements in the
79 open ocean of the bubble size distribution (BSD, the histogram of bubble
80 concentrations, as a function of radius) from a free-floating instrumented buoy (Fig. 2).

81 **Results**

82 The bubble size distributions measured in this study are presented together with some
83 historical data sets in Fig. 3 (the technical and environmental parameters for each study
84 are summarised in the Supplementary material). Much higher concentrations of bubbles
85 have been measured in the surf zone^{20,21}, but all the other studies report broadly
86 comparable distributions. The novel observation is that substantial numbers of large (i.e.
87 substantially larger than 100 μm radius) bubbles penetrate to 1 and 2 metres depth. The
88 large values of δ reported below follow substantially from this observation.

89 To quantify K_b and δ for individual atmospheric gases, the evolution of bubbles
90 clouds under breaking waves and the resulting gas flux, was modelled. This modelling
91 extends earlier work¹⁰ to apply more recent observations²⁴ of the initial bubble size
92 distribution (BSD) and the injection process. After the injection, the BSD changes over
93 time as bubbles dissolve, expand or contract, as buoyancy and oceanic turbulence and
94 circulation moves them to greater or lesser depths. Calculations of gas transfer across
95 the surface of the bubbles are made for gases of interest. Outputs include instantaneous
96 and time-averaged “modelled” BSDs. The time-averaged modelled and observed BSDs

97 at various depths in the Atlantic measurements are merged to calculate the bubble-
 98 mediated gas transfer. Tuning of the model to the measurements is summarised under
 99 Methods and further detail is provided in Supplementary Section S3. The measured and
 100 modelled BSDs are shown in Fig. 4. Note especially that the measurement of bubbles is
 101 dependent on subtraction of a “baseline”, the attenuation of acoustic signals in the
 102 absence of bubbles. Uncertainty in that baseline carries through first to the measured
 103 BSDs and on to the modelled BSDs and gas fluxes. Generally, the fit of the model to the
 104 data after calibration is satisfactory, but is relatively poor for radii greater than $200 \mu\text{m}$.
 105 That remaining discrepancy is significant to the accuracy of our results and is
 106 considered in the Discussion.

107 To quantify K_b and δ from this model, the mass flux parameters were evaluated in
 108 the following manner. With the measured ancillary data (detailed in Supplementary
 109 material) as input, the model was run with bubble injection by successive breaking
 110 waves until the bubble cloud reached steady state (i.e. when the variation of BSD with
 111 depth no longer changed significantly with each new injection). A range of fixed
 112 intervals between successive breaking wave events was tested, for example in the
 113 sensitivity study, but it was fixed at 8 s for production of the final results. Comparison
 114 of the steady state output with the time-averaged BSD found during the 10-hour at-sea
 115 measurements confirmed the validity of the model and allowed the values of a few
 116 remaining ancillary parameters (i.e. those which could not be measured directly in the
 117 trial; see Supplementary Section S3.3.3) to be estimated by calibration. Having
 118 determined all of the input parameters, the model is run again with bubbles injected
 119 only once, at the start of the simulation. This second type of simulation was run four
 120 times for each gas species in seawater, using four varying values of the concentrations
 121 varying from 95% to 110% of the saturation, $(C_w / S p_{pw}) \times 100\%$, where S is the
 122 solubility and p_{pw} is the partial pressure of the gas in question in the water. As shown
 123 in Fig. 5, when F_b is plotted as a function of the saturation, the data follow the straight-
 124 line dependence implied by $F_b = K_b [(I + \delta)C_a - C_w]$, thereby validating equation (2).
 125 Furthermore, K_b and δ can be calculated from the gradient and intersect of the linear fit.

126 The calculated values of K_b and δ for the four gases modelled are summarised in
127 Table 1. All values are substantial in the context of typical air-sea gas transfer rates.
128 Coefficients are expected to vary among gases, since they will depend on the molecular
129 diffusion coefficient of the dissolved gas and the solubility of the gas. In particular, both
130 coefficients are expected to be lower for more soluble gases. This expectation is met by
131 the results. Nitrogen, which is the least soluble gas, has the highest values of K_b (21.5
132 cm hr^{-1}) and δ (8.27%), while CO_2 has the lowest ($K_b = 8.1 \text{ cm hr}^{-1}$ and $\delta = 1.32\%$)
133 Oxygen and argon, which are very similar in physical constants, are intermediate in
134 both values. As noted already, uncertainty in an acoustic baseline introduces uncertainty
135 and that carries through to estimates of gas flux. That implies an uncertainty in K_b that is
136 represented by the minimum and maximum values in brackets in Table 1.

137 Since the sea state grew during the complete measurement period, it was possible
138 to obtain estimates of K_b for two different sea states. Two subsets of the full data set
139 were analysed, the first one third and the remainder, corresponding to average values of
140 significant wave height of 1.9 m and 3.1 m respectively. A marked difference in
141 acoustic attenuation between these two sea states was measured, which is consistent
142 with an increasing frequency of wave breaking (Fig. S3.9). Measured and modelled
143 BSDs for these two subsets (at 1.15 m depth only) are shown in Fig. 6, in which the
144 difference is readily apparent. The estimated concentration of bubbles varied
145 substantially between the two subsets and from the full data set. In each case, the rate of
146 bubble injection was tuned to provide the best fit between measured and modelled BSD.
147 In the earlier period, injection rate was 45% of the standard set, while it was 112% for
148 the later period. This rescaling translates to the values of K_b as shown in Table 1.

149 Discussion

150 Estimates of the contribution of “bubble-mediated transfer” have previously depended
151 on a postulated population of bubbles^{6, 10, 11}. Those estimates are supported by estimates
152 of gas transfer velocity for various gases²⁵, but direct evidence of sufficient bubbles has
153 been missing. This study represents a first opportunity to calculate gas transfer
154 coefficients directly from an adequate observation of the bubbles responsible (albeit on

155 a single day and location). The results support the view that in strong winds a
156 substantial fraction of air-sea exchange is by bubble-mediated transfer and that transfer
157 is strongly asymmetric.

158 The results support the use of equation (2) to represent the asymmetric gas
159 transfer. An additional specific term to describe total dissolution of some bubbles⁸ is not
160 required, though some bubbles will have dissolved in the simulations. Table 1 includes
161 a few key estimates of transfer coefficients from the literature, calculated for wind speed
162 of 14 m/s for easy comparison with our results. The values of K_b from this study are
163 fairly high, but broadly consistent with previous estimates^{6,7} and support the hypothesis
164 that there is a substantial enhancement of the total transfer velocity of gases by bubbles.
165 The transfer velocities are sensitive to the choice of bubble-water transfer coefficients
166 and also to the treatment of injection and mixing very close to the sea surface.
167 Considering also the uncertainty of the baseline measurement (bracketed values in
168 Table 1) and the difficulty of extrapolating from a single deployment in a building sea,
169 the values of K_b generally support contemporary views of the significance of bubble-
170 mediated transfer, but cannot narrow uncertainties.

171 The values of equilibrium supersaturation from our study are more remarkable
172 and represent a significant new finding. We include two historical estimates^{6, 10} in Table
173 1, but note that each of these estimates needs to be put in context. Woolf and Thorpe¹⁰
174 modelled the injection of a plume dominated by small bubbles, inconsistent with newer
175 observations of the initial BSD. Significant asymmetry was found, but this is expressed
176 as an asymmetry of the total transfer, Δ (which is less than δ , in the ratio of K_b to the
177 total transfer velocity, see Supplementary Section S1). Keeling⁶ considered large
178 bubbles, but only rising from a shallow depth. Our study is the first to assess the
179 significance of large bubbles (i.e. bubbles substantially larger than about 100 μm radius)
180 advected to depths of one or two metres. The following two paragraphs outline the
181 evidence to support the hypothesis that the asymmetry reported here is a robust result
182 and should supplant previous estimates.

183 Substantial asymmetry of gas exchange has been demonstrated previously^{8,9} for
184 Noble gases and oxygen (and by implication for other very poorly soluble gases) by

185 measurement of their oceanic supersaturation. These values can also be validated by
186 measurements of the small bubbles in deep clouds¹⁰. The fact that supersaturations exist
187 indicates the importance of bubbles. Our study predicts supersaturations rising to very
188 high values (e.g., 5.72% for O₂, 5.60% for Ar), but only when bubble-mediated
189 exchange is dominant and these values are consistent with net supersaturations of ~1%
190 for more normal conditions where bubble-mediated exchange is only a fraction of the
191 total air-sea exchange. The supersaturations of slightly more soluble gases (including
192 CO₂) are expected to be lower, but extrapolation from less soluble gases⁸⁻¹¹ is inexact
193 without accurate information on BSDs; existing estimates of δ for carbon dioxide
194 assume a distribution of bubbles near the sea surface in windy conditions. It has been
195 demonstrated that many large bubbles are injected to several metres depth in hurricane
196 conditions²⁶ and that bubbles can be driven to several metres depth through Langmuir
197 circulation²⁷ (Fig. 7), but prior to our new measurements the significance of a relatively
198 deep penetration of large bubbles has not been appreciated. The concentration of
199 bubbles up to a radius of 200 μm could be simulated, but we could not find an
200 acceptable fit for even larger bubbles. The modelled concentrations are lower than the
201 acoustically-measured concentrations for the largest bubbles. Had this mismatch
202 occurred for a population where all bubbles were much smaller than a wavelength in
203 radius, then it would indicate a mismatch between the model and the real BSD.
204 However it is not possible to have the same level of confidence when the sound field
205 interacts with large bubbles, because then is it possible (but not provable given the
206 optical system was damaged) that the model continues to match the true bubble size,
207 and the actual mismatch is between the acoustically-inferred BSD and the real BSD.
208 This is because the accuracy of the estimation of BSD reduces when the sound field
209 interrogates large bubbles. A key assumption of the acoustic model which estimates the
210 BSD from the measured acoustic attenuation (the ‘inversion’), is that the bubbles are
211 oscillating in steady state, and the maximum achievable pulse length may be insufficient
212 to achieve that (see Supplementary Sections S2.1.1 and S3.4.1). Another key
213 assumption in the inversion is that the product of the largest bubble radius and highest
214 acoustic wavenumber are much less than unity^{23,28} (i.e. that all bubbles are much
215 smaller than the smallest wavelength used; see Supplementary Section S2.1.2). For 1
216 mm radius bubbles, this value (at 197 kHz) equals 0.8, and the assumption becomes

217 compromised, making the estimation less accurate for large bubbles. This is generally
218 true for all active acoustic measurements of bubble size, and so to offset this limitation,
219 an optical system^{29,30} of measuring bubble size was implemented on the buoy to make a
220 complementary estimate of BSD for larger bubbles (optical systems show the opposite
221 trend to that displayed by the acoustics, tending to have higher accuracy for larger
222 bubbles). The plan was to extend the measurement of the BSD to even larger bubbles
223 using this overlap, and to compare the optical and acoustic estimates in the overlapping
224 region at around 1 mm radius to obtain a better estimate than either system gives alone.
225 This planning was negated when deployment of the buoy damaged the optical system.
226 Note that the modelled bubble concentrations imply the gas transfer coefficients
227 reported in this study and if the modelled concentrations are too low, the transfer
228 coefficients are also too low.

229 Though there are remaining discrepancies between the measured and modelled
230 concentrations of large bubbles, we have shown that there are sufficient populations of
231 large bubbles to support substantial values of K_b . Moreover, we have found that many of
232 these large bubbles penetrate at least 2 metres below the sea surface in windy conditions
233 and this underpins predictions of large δ for carbon dioxide. Hydrostatic pressure (in
234 addition to a lesser contribution from surface tension and surface curvature), increases
235 the gas pressure in the bubble and is the origin of the asymmetry. One metre below the
236 sea surface, the hydrostatic pressure equals 10% of atmospheric pressure, implying an
237 associated 10% asymmetry in gas transfer by this effect alone. It can be understood
238 from this simple model that the observation of sufficient bubbles at depths of one and
239 two metres underpins the calculation that the asymmetry will be larger than previously
240 supposed. It should be noted however that the composition of bubbles will change as the
241 bubbles evolve especially in the smaller bubbles, which underlies the greater
242 significance of large bubbles and necessitates the more detailed modelling employed in
243 this study. If the model underestimates the number of very large bubbles at depth (as
244 implied by the acoustic data), then the true asymmetry will be even larger. The findings
245 from, and equipment generated by, this relatively inexpensive 2007 experiment were
246 sufficient to justify a well-supported multi-centre follow-on study³¹, currently
247 underway, part of which uses the equipment, models and reports³² produced by this

248 study. In addition, the acoustical methods are also being incorporated into a large multi-
249 centre programme on carbon capture and storage³³.

250 This study provides data only for a single 10-hour-period in the open sea at a
251 water temperature of 17 °C, when the wind speed was fairly steady at 14 ms⁻¹ and there
252 was a growing wind sea. The data and associated model provide strong evidence of
253 substantial and highly asymmetric bubble-mediated gas transfer on this occasion. The
254 data also implies that the sea state is significant, since bubble concentrations increased
255 as the waves grew. It is clearly a challenge to extrapolate the results of this study to all
256 wind speeds, water temperatures and sea states. However, it is useful to consider the
257 global implications, especially with respect to the asymmetry of the air-sea transfer of
258 CO₂, since this study radically alters understanding in this respect.

259 The global disequilibrium for CO₂ is small, currently estimated as a net flux into
260 the oceans of 1.6 PgC³ on an exchange of 80 PgC^{1, 2}. Since we have found an
261 asymmetry of >1% on a substantial part of the total flux, the climatology of carbon
262 dioxide should be revised. Bubble-mediated exchange of carbon dioxide may account
263 for a quarter of total air-sea exchange³⁴. An asymmetry of 1.32% in the bubble-
264 mediated transfer implies an asymmetry of ~0.3% in the total or an additional annual
265 downward global flux of 0.2-0.3 PgC. (This is an extrapolation from one 10 hr, high
266 wind, single-location measurement, because experimental and funding challenges
267 precluded obtaining more data (see Supplementary Section S2). The previous wisdom
268 that the asymmetry was negligible is also based on extravagant extrapolation, but of less
269 directly relevant information, as described earlier in this section). The additional flux is
270 proportional to the partial pressure in the atmosphere¹¹ and will increase with rising
271 atmospheric carbon dioxide. Regional and seasonal effects will be greatest for relatively
272 stormy localities such as the wintertime temperate and polar seas.

273 **Methods**

274 Details of the Methods are to be found in Supplementary materials, where after
275 exposition of the revised formulation for the transfer of gas across a broken ocean
276 surface (Supplementary Section S1), details are given of the sea trials (Supplementary

277 Section S2) and the bubble cloud and gas-flux modelling (Supplementary Section S3).
278 In this section, a summary of the methods used in the sea trials are followed by some
279 notes on the gas-flux modelling.

280 The BSD was measured at two depths using the acoustic attenuation between
281 three hydrophones (having depths below the mean sea surface of 0.8, 1.22 and 2.54 m)
282 vertically aligned on a 11 m long spar buoy^{29,30} deployed in the North Atlantic (43.1 °
283 N, -17.7 ° W) on 28 June 2007. The BSD was determined by inverting the acoustic
284 attenuation of a sequence of 14 tones (at frequencies ranging from 3 to 197 kHz)
285 projected upwards from the base of the buoy once every second. The BSDs reported in
286 this paper cover bubble radii from 16 to 1141 μm , the widest size range ever measured
287 at sea. The measurements of BSD are dependent on subtraction of a “baseline”, the
288 acoustic attenuation without bubbles. This baseline is an at-sea measurement, but
289 introduces uncertainty that can be followed through to the calculated BSDs and on to
290 the gas fluxes. A best guess, a minimum and a maximum baseline were identified and
291 each was used in the analysis.

292 Additional data, including wind speeds, wave heights, video observation of wave
293 breaking frequency and a segment of data from an inverted echo sounder showing the
294 structure of bubble clouds (see Supplementary Sections S2 and S3), provide context and
295 support for the measurements of BSD. During the selected period, water temperature
296 averaged 17 °C and significant wave height increased steadily (a building wind sea)
297 from <1.8 m to >3.5 m. An inferred contribution of bubbles to the measured acoustic
298 attenuation is supported by measurements from an inverted echosounder (IES). For 10
299 minutes during the 10 hour measurement period, the IES at the base of the spar buoy
300 monitored the position of the sea surface relative to the base of the buoy, and measured
301 the profile of the bubble cloud through the backscattered signal (Supplementary
302 material, Fig. S2.5). The IES revealed that the bubble clouds often penetrated deeper
303 than the hydrophones. The IES data can validate the bubble population, its variation
304 with depth and suggest the shape of bubble clouds advected across the sonar beam, but
305 the full potential of the IES was not realised in this study, owing to the relative timing
306 of measurements by hydrophones and IES. Nevertheless, as shown in Supplementary

307 Section 2, the IES does provide valuable context for the attenuation measurements. In
308 future studies, simultaneous IES and optical measurements (of large bubbles) would
309 complement acoustic attenuation measurements of BSD, providing a fuller description
310 of sub-surface evolution of the bubble clouds: although we achieved the measurement
311 of the largest range of bubble sizes achieved at sea, the absence of optical data through
312 instrument damage meant that key questions of the accuracy of the acoustically-inferred
313 BSD for large bubbles, and how it affects our conclusions, could not be answered. The
314 resulting uncertainty means that this paper sets a lower limit on the estimation of the
315 asymmetry.

316 This experiment was part of a larger cruise plan³⁰ aimed at parameterizing
317 processes that influence aerosol production and the atmospheric content of radiatively
318 important gases, including CO₂. The wind speed plateaued in the afternoon and evening
319 of 29 June 2007, fluctuating over 10 hours around an average of 14 m/s (i.e. windy, but
320 not exceptional conditions). Data exclusively from this period were analysed for this
321 study (the full set of sea trials are described in Supplementary Section S2; later studies
322 by other investigators using our instrumentation, model and codes have not yet reported
323 any data against which we can compare the results of this study).

324

325 The experimental data are then incorporated into the model of the evolution of
326 bubble clouds beneath breaking ocean waves. The model is calibrated to the
327 measurements by modifying the rate of bubble injection and “tuning” parameters that
328 affect the penetration of bubbles to the measurement depth. Note that while we tuned
329 the model, this was restricted to maintain the integrity of the model. The initial size
330 distribution was set, since this is fairly established²⁴. Parameters that were considered
331 “tuneable” (within predefined limits) are the maximum upwelling/downwelling velocity
332 within the Langmuir circulation, the initial input jet velocity, the time for the jet velocity
333 to reach zero after injection, the insertion depth for the bubbles and the turbulent
334 diffusion coefficient, but in each case, we started at a standard value and altered the
335 values cautiously. The bubble distribution is especially sensitive to velocities within the
336 simulated Langmuir circulation. A fairly high (but sensible) maximum velocity of 0.185

337 m s⁻¹ appeared optimal. More details are described in Supplementary Section S3
338 including a tabulation of the final parameter values.

339 Variations in the measured BSD are associated both with the chosen baseline and with
340 the two subsets of data in a rising sea state. Each alternative data set was analysed in the
341 same way. The model was set to the final parameters found for the entire data set, but the
342 number of bubbles was varied to fit the specific BSD.

343 The model of the evolution of bubble clouds includes transfer of gases across the
344 surface of the bubbles. Therefore, once tuned the model also provides estimates of gas
345 flux, which with appropriate scaling provide the estimate of gas transfer coefficients.
346 Most of this part of the model is directly taken from Woolf and Thorpe¹⁰, but using
347 more capable computing technology. Again, the details are provided in Supplementary
348 Section S3.

349 The model of gas across the surface of the bubbles assumes that the process
350 depends only on molecular diffusion and the flow around the bubbles¹⁰. Among the
351 processes that are excluded is chemical reactivity. It is known that CO₂ is reactive with
352 seawater, but the initial reaction is often assumed to be slow enough compared to the
353 time scales of diffusive transfer across the sea surface to ignore³⁵, except in very light
354 winds. Since the transfer across the surface of a bubble is relatively quick (apparent by
355 comparing “individual bubble transfer velocities”¹⁰ to the typical transfer velocity at
356 the sea surface), it appears to be a safe assumption to ignore chemical reactivity in
357 bubble-mediated transfer of CO₂. However, it is worth noting that the rates of reaction
358 and CO₂ transfer at the sea surface could be raised by enzymes³⁶ and this is possible
359 also on the surface of bubbles.

360 The datasets generated during and analysed during the current study are
361 openly available from the University of Southampton repository at
362 <http://dx.doi.org/10.5258/SOTON/>[**Note to editors: The policy of the Southampton**
363 **University policy is that they grant a link for insertion once the paper is accepted to**
364 **avoid their repository referring to papers that were not published**].

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376

377 **Author contributions**

378

379 T.G.L. proposed and planned the study, was P.I. for the research, acted as co-ordinator
380 for writing the paper, main author for the Supplementary Materials and data archive, and
381 shared main authorship (with D.K.W.) of the body of the paper. T.G.L. was also main
382 supervisor for D.G.H.C., who conducted the experimental and modelling elements of this
383 study as his PhD project. D.K.W. acted as second supervisor for D.G.H.C. and expert on
384 air-sea gas fluxes and modelling of bubble cloud evolution and shared main authorship
385 of writing the body of the paper with T.G.L., M.S. acted as third supervisor for D.G.H.C.
386 and ocean-wave expert, provided the original design for the structural components of the
387 buoy and the above-surface camera (i.e. excluding the subsurface acoustical systems and
388 the optical sensors, which were designed by T.G.L. and D.G.H.C.) and organized the
389 cruise opportunities for the observations. P.R.W. advised on the bubble cloud modelling
390 and coding associated with the acoustic inversion. All authors contributed to the writing
391 of the paper.

392

393 **Competing financial interests**

394

395 The authors have no competing interests as defined by Nature Research, or other
396 interests that might be perceived to influence the results and/or discussion reported in this
397 paper.

398

399 **Figure Legends**

400

401 Figure 1. Photograph showing subsurface bubble clouds (taken by T.G.L.).

402

403 Figure 2. Photographs of the spar buoy being deployed and at sea. (a) The 11 metre
 404 long buoy being deployed from the ship (perspective makes the lower grey section
 405 appear shorter than the upper yellow section, although in reality it is nearly twice as
 406 long). (b) The buoy sitting in calm waters during the first cruise and (c) the buoy
 407 during the deployment described in this study. See also Fig. S2.3.

408

409 Figure 3. Bubble size distributions (BSDs) from this and historical studies. The
 410 BSDs measured in this study are shown by the broken and solid lines, measured at
 411 depths of 1.15 and 2 metres respectively. The graph compares these data with
 412 historical measurements. The historical data include the open ocean data of Breitz
 413 and Medwin¹⁶ (crosses), Phelps and Leighton¹⁷ (plus signs), Farmer and Vagle¹⁸
 414 (stars) and Johnson and Cooke¹⁹ (dots), and the surf zone data of Deane and
 415 Stokes²⁰ (diamonds), Phelps *et al.*²¹ (triangles), Meers *et al.*²² (downward pointing
 416 triangles) and Leighton *et al.*²³ (squares).

417

418 Figure 4. Bubble size distributions from the measured data (dashed line with
 419 crosses) and the model (circles). Panel (a) shows the distributions at 1.15 m depth
 420 and (b) shows them at 2 m depth. The uncertainty bars show one standard deviation
 421 from the mean within these data.

422

423 Figure 5. The modelled flux of bubble-mediated gas transfer plotted against
 424 saturation for the four gases considered. An injection of gas is predicted at
 425 saturation, while balanced at a supersaturation, δ . The fluxes have been normalised
 426 such that the values are proportional to the rate of change of saturation of each
 427 dissolved gas. Generally, both δ and the rate of change reduce with increasing
 428 solubility.

429

430 Figure 6. Measured and modelled bubble size distributions for mean significant wave
431 heights of 3.1 m (circles) and 1.9 m (triangles). Measurements are shown by open
432 circles ($H_s = 3.1$ m) and open triangles ($H_s = 1.9$ m). The model fits are shown by
433 filled circles ($H_s = 3.1$ m) and filled triangles ($H_s = 1.9$ m).

434

435 Figure 7. The bubble clouds at the end of the model run. The helical flow of the
436 Langmuir cells can be seen. The population shown here is from a run with 100000
437 bubbles in the input population, and only 1 in every 100 bubbles is plotted (the larger
438 bubbles being shown red, the smaller ones blue). Details of the input parameters can
439 be found in Supplementary Section 3.

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Tables

Gas	All data K_b (cm hr ⁻¹)	All data δ (%)	$H_s = 1.9$ m K_b (cm hr ⁻¹)	$H_s = 3.1$ m K_b (cm hr ⁻¹)	Woolf & Thorpe ¹⁰ (1991) Δ (%)	Woolf ⁷ (1993) K_b (cm hr ⁻¹)	Keeling ⁶ (1993) K_b (cm hr ⁻¹)	Keeling ⁶ (1993) δ (%)
Nitrogen	21.5 (13.8 - 31.0)	8.27	9.7	24.1	3.78	-	-	-
Oxygen	17.2 (11.0 - 24.8)	5.72	7.7	19.3	2.42	-	13.84	0.25
Carbon dioxide	8.1 (5.2 - 11.7)	1.32	3.7	9.1	0.0816	8.18	2.96	0.08-0.3
Argon	16.4 (10.5 - 23.6)	5.60	7.4	18.4	2.13	-	-	-

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Table 1. Estimates of transfer velocity (K_b) and the equilibrium supersaturation (δ) from this study and historical estimates for each of the four gases included in this study. The first two columns are the final estimates from this study. Values in brackets are the minimum and maximum values of K_b based on uncertainty in the “baseline”. Two additional values of K_b are based on subsets of the data when significant wave height averaged 1.9 m and 3.1 m respectively. Historical estimates from literature^{6,7,10} are also shown. One of the values of supersaturation is for a different definition of supersaturation¹⁰, Δ , as explained in the text. All values are for a wind speed of 14 m s⁻¹ (at 10 m above the sea surface).