"Near-Perfect" Finite-Cardinality Generalized Space-Time Shift Keying

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Abstract-Two decades of full-diversity high-rate MIMO research has created perfect Space-Time Block Codes (STBCs) including the Golden code. However, the major stumbling block of their wide-spread employment is their limited energy-efficiency. On one hand, the superposition of their signals results in a high Peak-to-Average Power Ratio (PAPR). On the other hand, the total number of equivalent Inter-Antenna Interference (IAI) contributions that the receiver has to deal with is increased to $IAI = M^2$ upon using M Transmit Antennas (TAs), which is a substantial extra price compared to the IAI = M of V-BLAST. Against this background, we propose a new family of Finite-Cardinality Generalized Space-Time Shift Keying (FC-GSTSK). More explicitly, the proposed FC-GSTSK is capable of outperforming both V-BLAST and STBC, which is the ultimate objective of full-diversity high-rate MIMO design. Furthermore, following the index modulation philosophy, the proposed FC-GSTSK replaces the signal-additions by the data-carrying signalselection process. As a benefit, the FC-GSTSK substantially reduces the PAPR of signal transmission. As a further advantage, the equivalent IAI imposed on signal detection is reduced back to the same level as that of V-BLAST. Moreover, the proposed FC-GSTSK is even capable of consistently outperforming the perfect STBCs in terms of its Peak Signal to Noise-power Ratio (PSNR) that takes into account the power consumption at the transmitter. As a further advance, the reduced-RF-chain based version of FC-GSTSK is also capable of outperforming both Generalized Spatial Modulation (GSM) and Space-Time Block Coded Spatial Modulation (STBC-SM) without increasing the PAPR and the equivalent IAI.

Index Terms—Space-time block code, perfect STBC, Golden code, generalized space-time shift keying, finite-cardinality, peak-to-average power ratio, inter-antenna interference, energy-efficiency, bandwidth-efficiency, power-efficiency, full-RF-chain,

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I. INTRODUCTION

Following the recent digital and analog circuit breakthroughs in processing massive-bandwidth millimeter-wave signals, the next-generation mobile network is envisioned to achieve the ambitious goal of 1000 times higher capacity and 10-fold reduced roundtrip latency [1]. As a benefit of the substantial new available bandwidth, billions of powerhungry devices may be ubiquitously connected to the evolving Internet-of-Things (IoT), where the employment of energyefficient schemes associated with low-complexity transceivers is increasingly favorable. Against this backdrop, the invention of Spatial Modulation (SM) [2]-[4] harnessed the Index Modulation (IM) philosophy in the spatial domain, which inspired a paradigm shift from spectral-efficiency to energy-efficiency. More explicitly, the base-line SM activates a single one out of M Transmit Antennas (TAs) in order to transmit a modulated L-PSK/QAM symbol. As a result, since only a single RF chain is required, the power consumption of the transmitter is substantially reduced [5]-[9]. Furthermore, the activation of a single TA effectively eliminates the Inter-Antenna Interference (IAI), which facilitates low-complexity single-stream-based detection [10], [11]. However, despite their attractive advantages in energy-efficiency, the IM design generally suffers from a reduced bandwidth-efficiency. For instance, the overall SM throughput is given by $R = \log_2 M + \log_2 L$, which is inferior to the V-BLAST throughput of $R = M \log_2 L$ that grows linearly with M.

In the recent years, the IM philosophy has been intensively applied to a variety of scenarios [5]-[9] including Orthogonal Frequency-Division Multiplexing (OFDM) [12]-[14], Faster-Than-Nyquist (FTN) [15]-[17] and differential Multiple-Input Multiple-Output (MIMO) systems [18]-[21], where the concept of energy-efficiency is not exclusively limited to the reduction of RF chains. In fact, the implementation of the single- and reduced-RF-chain designs still faces a number of practical challenges. First of all, the power amplifier of the single activated RF chain has to deliver M times higher power than its counterparts operating in the full-RF mode. Secondly, the antenna switching time has to be substantially lower than the symbol period [22], and the time limit on pulse-shaping is also more strictly bounded, because the transmission of a whole symbol has to be completed over the activated symbol period [7]. Thirdly, the single- and reduced-RF designs are

generally limited to the single-carrier systems, owing to the fact that the simultaneous activation of OFDM subcarriers would result in full-RF transmission.

Regardless of the number of activated RF chains, the actual signal constellation and the associated Peak-to-Average Power Ratio (PAPR) predetermine the power consumption of each RF chain. To this end, the diversity-aided IM schemes of Space-Time Shift Keying (STSK) and Generalized STSK (GSTSK) [23]–[27] that invoke arbitrary signals may not be deemed energy-efficient for the following reasons. First of all, the products of the communication industry typically use standardized PSK/QAM signals rather than arbitrary signals. The signal conversion from arbitrary signals to the Finite-Cardinality (FC) fixed-point representation of PSK/QAM is subject to VLSI hardware constraints. Secondly, transmitting arbitrary signals undermine the low-PAPR advantage of singlecarrier systems. Thirdly, when a multi-carrier OFDM system is considered, typically the classic PSK/QAM constellations are used for frequency-domain modulation. Although the Inverse Fast Fourier Transform (IFFT) potentially increases the PAPR at the transmitter, a variety of practical techniques - including active constellation extension, selected mapping, tone injection and tone reservation [28]-[31] - are capable of reducing the time-domain OFDM signal's PAPR, but all of them operate based on the classic PSK/QAM input constellations before the IFFT.

Similar to STSK, the signal constellation typically becomes almost arbitrary when aiming for full-diversity high-rate MIMO design. Specifically, the family of perfect STBCs [32]-[35] including the Golden code [36] is capable of achieving unprecedented performance advantages over both V-BLAST and STBC relying on orthogonal [37], [38], on Amicable-Orthogonal (AO) [39], [40] and on Quasi-Orthogonal (QO) [41], [42] designs. More explicitly, the perfect STBC partitions the $(M \times M)$ space-time signal matrix into M layers, where each layer disperses a total number of M modulated QAM/HEX [32] symbols. The beneficial cubic shaping property [32] ensures that the total power of each layer remains unchanged. Moreover, the state-of-the-art nonvanishing determinant property [32] further enhance the diversity gain. Despite the fact that the Golden code was included in the IEEE 802.16e-2005 WiMAX standard [43], the family of perfect STBCs is not sufficiently energy-efficient for next-generation MIMO systems. On one hand, owing to the superposition of their signals within each layer during the dispersion process, the associated constellation expansion and the increased PAPR impose extra constraints both on the Digital-to-Analog Converter (DAC) and on the power amplifier at the transmitter. On the other hand, in addition to the M interfering elements within each layer, the space-time transmission of the M layers also induces cross-layer IAIs. As a result, the total number of equivalent IAIs that the receiver has to deal with is increased to $IAI = M^2$, which is a substantial extra price compared to the conventional IAI = M of V-BLAST. To alleviate the high-PAPR, the so-called integer STBC arrangement was developed in [44], [45], where the transmitted signals are limited to an expanded L^2 -QAM constellation. Moreover, in order to mitigate the excessive receiver complexity, the fast decoding algorithm and the so-called Silver code [43], [46], [47] endeavored to separate the in-phase and quadrature evaluations in the Sphere Decoder (SD). However, these solutions still suffer from both an increased PAPR compared to the single-stream *L*-QAM and from a performance loss over the optimal perfect STBC.

Against this background, we propose a new FC-GSTSK design, which is capable of outperforming both V-BLAST and STBC without increasing the PAPR, while the equivalent IAIs is reduced back to the moderate IAI = M value of V-BLAST. Explicitly, the novel contributions of this paper are:

- 1) First of all, instead of using the irrational coefficients such as the Golden number of the Golden code, the dispersion elements of the new FC-GSTSK operate based on the L_{DM} -th root of unity $[w_{L_{DM}} = \exp(j\frac{2\pi}{L_{DM}})]$. Secondly, following the IM philosophy, the signal-superposition form of $(\sum_{q=1}^{\overline{Q}} s_{\overline{q}} w_{L_{DM}}^{\overline{q}})$ is replaced by the signal-selection operation of $s^l w_{L_{DM}}^{\overline{q}}$, where both the modulation index l and the activation index \overline{q} carry source information. Thirdly, in order to maximize the diversity gains, the dispersion elements are appropriately rotated by the integers of $\{u_m\}_{m=1}^M$, as denoted by $\{w_{L_{DM}}^{u_m\overline{q}}\}_{m=1}^M$ in order to cater for the different MIMO setups. As a result, the benefits of the resultant full-RF FC-GSTSK are summarized in the following aspects:
 - (A) **Energy-Efficiency**: Thanks to the new dispersion elements and the IM design, the FC-GSTSK does not increase the PAPR of signal transmission. Moreover, the signal-selection process also eliminates the interference imposed on each layer. As a result, the total number of equivalent IAIs imposed on signal detection is reduced back to the V-BLAST's IAI = M.
 - (B) **Bandwidth-Efficiency**: The FC-GSTSK throughput is given by $R = \log_2 \overline{Q} + \log_2 L$, which is higher than that of the family of STBCs [37]–[42]. We note that \overline{Q} denotes the number of dispersion elements in each layer. Our analysis demonstrates that the bandwidth-efficiency of FC-GSTSK grows logarithmically with \overline{Q} towards the full MIMO capacity, where increasing \overline{Q} does not impose any extra hardware cost in terms of TAs, Receive Antennas (RAs) or RF chains.
 - (C) Power-Efficiency: As a full-diversity high-rate design, the FC-GSTSK massively outperforms STBCs [37]–[42], especially as N and R increase, where N denotes the number of RAs. Moreover, the FC-GSTSK distinctly outperforms V-BLAST owing to its beneficial diversity gain. The improved power-efficiency of FC-GSTSK manifests itself in terms of its reduced power consumption required for achieving a certain target performance. Specifically, the FC-GSTSK is even capable of consistently outperforming the Golden code in terms of its Peak Signal to Noise-power Ratio (PSNR), which takes into account the practical power consumption of the transmitter.
 - (D) Deployability: The diversity gain optimization is

conducted in an off-line fashion and all the FC-GSTSK parameters are integers. Therefore, the transceiver is only required to store integer parameters instead of dispersion matrices or full signal matrices.

- 2) In this work, we are particularly interested in the FC-GSTSK using the *L*-PSK modulation, which exhibits the perfect 0 dB PAPR. Nonetheless, in order to achieve a further improved performance at high throughputs, we conceive the Single-Element Amplitude Shift Keying (SE-ASK) as well as Multi-Element ASK (ME-ASK) for star QAM signalling. In particular, the ME-ASK arrangement achieves a substantially improved throughput at the cost of a slightly eroded diversity order. However, our simulation results confirm that the maximized diversity gain among a subset of FC-GSTSK codewords is sufficient to ensure the consistently superior performance of FC-GSTSK at high throughputs.
- 3) Moreover, in order to simplify the FC-GSTSK signal construction for using an increased number of M TAs at high throughputs R, we additionally propose a Diversity-Rate (DR) tradeoff based arrangement. More explicitly, for an integer of V = M/T, where T represents the number of time slots of a FC-GSTSK block, a $(T \times M)$ -element FC-GSTSK is constructed by V number of smaller $(T \times T)$ constituent FC-GSTSK. The resultant transmit diversity order is reduced to $[\min(M, T) = T = M/V]$, but the throughput is improved to $[R = V(\log_2 \overline{Q} + \log_2 L)]$.
- 4) As a further advance, we develop the reduced-RF-chain version of FC-GSTSK, where a subset of M_A out of M TAs are activated. Our simulation results demonstrate that the reduced-RF FC-GSTSK is capable of outperforming both Generalized SM (GSM) and its diversity-oriented counterpart of Space-Time Block Coded Spatial Modulation (STBC-SM) [48]–[51] without increasing the PAPR and the equivalent IAIs.
- 5) Finally, the proposed FC-GSTSK scheme is examined in conjunction with a low-complexity Binary Convolutional Coding (BCC) scheme, which is the channel coding arrangement of the IEEE 802.11a/n/ac/ah standard family. The powerful analytical tool of EXtrinsic Information Transfer (EXIT) charts [52]–[55] is employed for analysing the convengence behaviour of iterative demapping and decoding. Our simulation results confirm the unequivocal performance advantages of the proposed FC-GSTSK scheme in the practical channel coded systems.

The new FC-GSTSK subsumes the single-RF STSK [21], which was proposed in the differential MIMO scenario and was shown to outperform Differential SM (DSM) [18], [19], [56], [57] and its diversity-oriented counterparts [20], [58]–[63]. Moving forward from [21], this work activates multiple RF chains and further improves the methodology of the diversity gain optimization, so that the new FC-GSTSK becomes capable of achieving the best MIMO performance.

The rest of this paper is organized as follows. The pre-

1	4	3	2
2	1	4	3
3	2	1	4
4	3	2	1

Fig. 1: Examples of the TAST layout [67] associated with M = T = 4.

liminaries and system model are introduced in Sec. II. The signal construction of FC-GSTSK is proposed in Sec. III, while its further extensions to star QAM, DR and reduced-RF arrangements are conceived in Sec. IV. Our performance results and conclusions are offered in Sec. V and Sec. VI, respectively.

The following notations are used throughout the paper. The operation \otimes represents the Kronecker product, while tr(·), $rank(\cdot)$ and det(·) take the trace, rank and determinant of a matrix, respectively. Moreover, for a generic MIMO scheme, the notations M, N, T and Q represent the numbers of TAs, RAs, transmission time slots and modulated symbols, respectively, while L and R represent the modulation alphabet size and throughput, respectively.

II. PRELIMINARIES AND SYSTEM MODEL

First and foremost, it is important to portray our contributions in a historical perspective. Before the MIMO's space-time diversity era, the lattice-based multidimensional constellation design [64]–[66] endeavored to attain a beneficial diversity gain over the Single-Input Single-Output (SISO) systems. More explicitly, a sequence of T dispersed symbols is given by:

$$\bar{\mathbf{s}} = \frac{1}{\sqrt{T}} \mathbf{G}_A \mathbf{s}.$$
 (1)

The generator matrix \mathbf{G}_A is of size $(T \times T)$, which is found to be a Vandermonde matrix $\mathbf{G}_A = \text{VDM}_{T \times T}(g_1, \cdots, g_T)$ for the *L*-PSK modulation formulated as:

$$\mathbf{G}_{A} = \begin{bmatrix} \overline{a}_{1,1} & \overline{a}_{1,2} & \overline{a}_{1,3} & \dots & \overline{a}_{1,T} \\ \overline{a}_{2,1} & \overline{a}_{2,2} & \overline{a}_{2,3} & \dots & \overline{a}_{2,T} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ \overline{a}_{T,1} & \overline{a}_{T,2} & \overline{a}_{T,3} & \dots & \overline{a}_{T,T} \end{bmatrix}$$

$$= \begin{bmatrix} 1 & g_{1} & g_{1}^{2} & \dots & g_{1}^{T-1} \\ 1 & g_{2} & g_{2}^{2} & \dots & g_{2}^{T-1} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 1 & g_{T} & g_{T}^{2} & \dots & g_{T}^{T-1} \end{bmatrix}.$$
(2)

The diversity is imposed by the dispersion operation of $(\bar{s}_{\bar{t}} = \sum_{t=1}^{T} \bar{a}_{\bar{t},t} s_t = \sum_{t=1}^{T} g_{\bar{t}}^{t-1} s_t)$, where the dispersion elements $\{g_{\bar{t}}\}_{\bar{t}=1}^{T}$ are taken from a 4*T*-PSK constellation according to [64]. Therefore, instead of directly sending the modulated *L*-PSK symbols $\{s_t\}_{t=1}^{T}$ in \bar{s} of (1), the correlated symbols $\{\bar{s}_{\bar{t}}\}_{\bar{t}=1}^{T}$ in \bar{s} are transmitted over the fading channel. As a result, the receiver may successfully recover $\bar{s} = [\bar{s}_1, \cdots, \bar{s}_T]^T$, unless the whole sequence experiences a deep fade. There is no throughput loss for the SISO system given by $(R = \frac{T \log_2 L}{T} = \log_2 L)$. However, the PAPR of the transmitted symbols in \bar{s} of (1), while the dispersion process also imposes *T*-element interferences among $\{\bar{s}_{\bar{t}}\}_{\bar{t}=1}^T$.

Accordingly, in order to achieve space-time diversity in MIMO systems, the Diagonal Algebraic Space-Time (DAST) design of [68] was proposed to transmit the dispersed sequence

 $\overline{\mathbf{s}}$ of (1) mapped to the diagonal of the MIMO's space-time signal matrix as:

$$\mathbf{S} = \frac{1}{\sqrt{M}} \operatorname{diag}(\mathbf{G}_{A}\mathbf{s}) = \frac{1}{\sqrt{M}} \operatorname{diag}\left(\left[\sum_{m=1}^{M} g_{1}^{m-1} s_{m}, \sum_{m=1}^{M} g_{2}^{m-1} s_{m}, \cdots, \sum_{m=1}^{M} g_{M}^{m-1} s_{m}\right]\right)$$
(3)

The resultant throughput is also given by $(R = \frac{T \log_2 L}{T}) = \log_2 L$. In order to regain the V-BLAST throughput of $R = M \log_2 L$, the Threaded Algebraic Space-Time (TAST) arrangement [67] partitions a $(T \times M)$ -element space-time signal-matrix into M layers, where each layer transmits a dispersed sequence $\bar{\mathbf{s}}_{\tau} = {\{\mathbf{G}_A \mathbf{s}_{\tau}\}_{\tau=1}^M}$. The TAST layout is exemplified by Fig. 1. More explicitly, the signal matrix is constructed by [67]:

$$\mathbf{S} = \frac{1}{M} \sum_{\tau=1}^{M} \phi_r^{\tau-1} \operatorname{diag}(\mathbf{G}_A \mathbf{s}_{\tau}) \mathbf{G}_r^{\tau-1}.$$
 (4)

The generator matrix \mathbf{G}_A in (4) is still given by (2). The layer-switching phase rotations of $\{\phi_r^{\tau-1} = w_{L_r}^{\tau-1}\}_{\tau=1}^M$ in (4) are taken from a L_r -PSK constellation, which are invoked for the sake of retaining the full diversity order. Moreover, the layer-switching matrix \mathbf{G}_r in (4) is given by:

$$\mathbf{G}_{r} = \begin{bmatrix} 0 & 0 & \cdots & 0 & 1 \\ 1 & 0 & \cdots & 0 & 0 \\ 0 & 1 & \cdots & 0 & 0 \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ 0 & 0 & \cdots & 1 & 0 \end{bmatrix}.$$
 (5)

As a result, the TAST throughput is improved to $(R = \frac{M^2 \log_2 L}{T} = M \log_2 L)$ for M = T. However, both the DAST and TAST designs suffer from the vanishing determinant problem, where the following diversity gain tends to zero as the throughput increases:

$$\delta_{\min} = \min_{\forall \mathbf{S} \neq \mathbf{S}'} \det[(\mathbf{S} - \mathbf{S}')(\mathbf{S} - \mathbf{S}')^H].$$
(6)

Following the success of the orthogonal STBC designs [37], [38], considerable research efforts have also been dedicated to finding the MIMO schemes that may achieve both fulldiversity and high-rate. Notably, it was demonstrated in [69] that a sufficient condition for achieving both the multiplexing and diversity gains quantified in [70] is to ensure a lower bound on the diversity gain of (6), which may be solved based on division algebra [69], [71], [72]. More explicitly, when the STBC signals are allowed to take values in an infinite constellation, the diversity gain of the infinite code is given by:

$$\delta_{\inf} = \min_{\forall \mathbf{S} \neq \mathbf{0}} |\det(\mathbf{S})|^2, \tag{7}$$

which is obtained by using $(\mathbf{S}' = \mathbf{0})$ and (M = T) in (6). Naturally, the family of invertible matrices from division algebra guarantees $[\det(\mathbf{S}) \neq 0]$ for (7), which is sufficient for ensuring $(\delta_{\min} \neq 0)$ in (6). The division algebra designs generally use the following signal structure:

$$\mathbf{S} = \frac{1}{\sqrt{M}} \sum_{\tau=1}^{M} \operatorname{diag}(\mathbf{G}_A \mathbf{s}_{\tau}) \mathbf{G}_R^{\tau-1}, \tag{8}$$

where the layer-switching phase ϕ_R is incorporated into the layer-switching matrix \mathbf{G}_R as:

$$\mathbf{G}_{R} = \begin{bmatrix} 0 & 1 & 0 & \cdots & 0 \\ 0 & 0 & 1 & \cdots & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & 0 & \cdots & 1 \\ \phi_{R} & 0 & 0 & \cdots & 0 \end{bmatrix}.$$
 (9)

- (A) The cubic shaping property [32] requires \mathbf{G}_A to be unitary, so that the overall power of each layer in (8) remains unchanged as $\{\|\mathbf{G}_A\mathbf{s}_{\tau}\|^2 = \|\mathbf{s}_{\tau}\|^2\}_{\tau=1}^T$. Moreover, the average transmit power across the *M* layers also remains the same, which requires ϕ_R to have unity power of $|\phi_R|^2 = 1$.
- (B) The full V-BLAST throughput is retained for (8) as $(R = \frac{M^2 \log_2 L}{T} = M \log_2 L)$, where a total number of $Q = M^2$ symbols are transmitted over M = T times slots.
- (C) The full STBC diversity order is achieved. Furthermore, the nondiminishing determinant property guarantees that without considering the power normalization, the diversity gain δ_{inf} of (7) is a non-zero constant δ_c . More explicitly, when the modulated symbols $\{s_q\}_{q=1}^Q$ in $\{\mathbf{s}_{\tau}\}_{\tau=1}^T$ of (8) are given by Gaussian integers $\mathbb{Z}[j]$ or Eisenstein integers $\mathbb{Z}[w_3]$, where $w_3 = \exp(j\frac{2\pi}{3})$ denotes the primitive third root of unity, the perfect STBC has¹:

$$\delta_{\inf} = \frac{1}{\beta^M} \delta_c. \tag{10}$$

The factor of $\frac{1}{\sqrt{\beta}}$ normalizes the average power of unbounded signal-set $\mathbb{Z}[j]$ or $\mathbb{Z}[w_3]$ to the unity-power cardinality-*L* QAM/HEX constellations associated with $\{E(|s_q|^2) = 1\}_{q=1}^Q$.

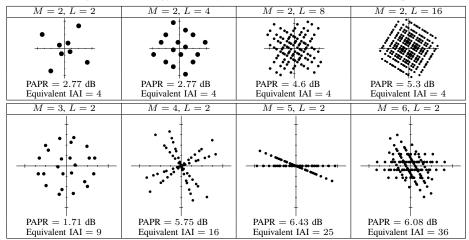
Example 1: The state-of-the-art Golden code [36] uses $\mathbf{G}_A = \frac{1}{\sqrt{5}} \begin{bmatrix} \epsilon & \epsilon \theta \\ \overline{\epsilon} & \overline{\epsilon \theta} \end{bmatrix}$ and $\phi_R = j$, where the parameters are $\theta = \frac{1+\sqrt{5}}{2}$, $\epsilon = 1+j-j\theta$, $\overline{\theta} = \frac{1-\sqrt{5}}{2}$ and $\overline{\epsilon} = 1+j-j\overline{\theta}$. As a result, the signal matrix of (8) becomes $\mathbf{S} = \frac{1}{\sqrt{10}} \begin{bmatrix} \epsilon(s_1+\theta s_2) & \epsilon(s_3+\theta s_4) \\ j\overline{\epsilon}(s_3+\overline{\theta} s_4) & \overline{\epsilon}(s_1+\overline{\theta} s_2) \end{bmatrix}$, which uses M = 2 TAs to convey Q = 4 symbols $\{s_q\}_{q=1}^4$ over T = 2 time slots. Given the relationships of $(\theta\overline{\theta} = -1)$, $(\theta + \overline{\theta} = 1)$ and $(\epsilon\overline{\epsilon} = 2+j)$, we have $\det(\mathbf{S}) = \frac{2+j}{10} [(s_1^2 + s_1 s_2 - s_2^2) - j(s_3^2 + s_3 s_4 - s_4^2)]$, which results $\ln^2 \delta_{\inf} = \frac{1}{20\beta^2}$ for (7), where the minimum is given by $s_1 = \frac{1}{\sqrt{\beta}}$ and $s_2 = s_3 = s_4 = 0$.

Although the cubic shaping property normalizes the layer power in the perfect STBC design, the PAPR of each transmitted symbol is inevitably increased due to the signals being multiplied and added together by $G_A s_{\tau}$ in (4). The associated constellation expansion is exemplied in Table I. As a result, it was shown in [44], [73] that the employment of realistic finite-precision DACs may impose a severe performance loss on the Golden code. Furthermore, Table I also shows that the perfect STBCs impose an equivalent IAI = M^2 on the signal detection at the receiver. More explicitly, the transmitted

¹We note that owing to the power normalization for ensuring $E[tr(\mathbf{SS}^H)] = T$ in the MIMO systems design, the diversity gain of the perfect code still declines as the throughput increases.

²Once again, owing to the normalization factors of $\frac{1}{\sqrt{\beta}}$ for $\{E(|s_q|^2) = 1\}_{q=1}^Q$ and $\frac{1}{\sqrt{M}}$ in (8) for $E[tr(\mathbf{SS}^H)] = T$, the diversity gain derived in this work is smaller than the one originally claimed in [36].

TABLE I: Constellation diagrams and energy-efficiency measures of Golden code [36] and perfect STBCs [32]-[35].



signals of (8) may be expressed in the form of the Linear Dispersion Code (LDC) [74] as:

$$\mathbf{S} = \sum_{\tau=1}^{M} \sum_{m=1}^{M} s_{\tau,m} \mathbf{A}_{\tau,m} = \sum_{q=1}^{Q} \overline{s}_{q} \overline{\mathbf{A}}_{q}, \tag{11}$$

where we have $\overline{s}_q = s_{\tau,m}$ and $\overline{\mathbf{A}}_q = \mathbf{A}_{\tau,m} = \frac{1}{\sqrt{M}} \operatorname{diag} \{ \mathbf{G}_A (:, m) \} \mathbf{G}_R^{\tau-1}$, while $\mathbf{G}_A (:, m)$ denotes the *m*-th column in \mathbf{G}_A . The relationship between indices is given by $[q = m + (\tau - 1)M]$. Moreover, the signal received by the *N* RAs over *T* times slots may be modeled as:

$$\mathbf{Y} = \mathbf{S}\mathbf{H} + \mathbf{V},\tag{12}$$

where the $(T \times M)$ -element matrix **S** and the $(T \times N)$ element matrix **Y** represent the input and output signals of the MIMO channels, while the $(M \times N)$ -element **H** and $(T \times N)$ -element **V** model the Rayleigh fading channels and the AWGN, respectively. As a result, vectorizing **Y** of (12) leads to the following LDC signal model:

$$\overline{\mathbf{Y}} = \overline{\mathbf{S}}\overline{\mathbf{H}} + \overline{\mathbf{V}},\tag{13}$$

where we have the $(1 \times TN)$ -element $\overline{\mathbf{Y}} = \operatorname{rvec}(\mathbf{Y})$ and $\overline{\mathbf{V}} = \operatorname{rvec}(\mathbf{V})$. The equivalent $(1 \times Q)$ -element transmitted signal vector $\overline{\mathbf{S}}$ is given by:

$$\overline{\mathbf{S}} = \underbrace{[s_{1,1} \cdots s_{1,M}}_{\tau=1} \underbrace{s_{2,1} \cdots s_{2,M}}_{\tau=2} \cdots \underbrace{s_{M,1} \cdots s_{M,M}}_{\tau=M}].$$
(14)

The $(Q \times TN)$ -element channel matrix is $\overline{\mathbf{H}} = \overline{\chi}(\mathbf{I}_T \otimes \mathbf{H})$, where we have the $(Q \times TM)$ -element $\overline{\chi} = [\operatorname{rvec}(\overline{\mathbf{A}}_1)^T, \cdots, \operatorname{rvec}(\overline{\mathbf{A}}_Q)^T]^T$. As a result, the signal detection of the perfect STBC is equivalent to that of a V-BLAST scheme associated with $Q = M^2$ TAs and TN RAs. Hence the total number of equivalent IAIs that the receiver has to mitigate is increased to IAI = M^2 .

III. INDEX MODULATION ASSISTED FULL-DIVERSITY HIGH-RATE SIGNAL CONSTRUCTION

In this section, we propose the novel FC-GSTSK in Sec. III-A, where the schematic descriptions are summarized in Sec. III-B. The bespoke diversity gain maximization is presented in Sec. III-C, and our analysis of the bandwidthand power-efficiency is offered in Sec. III-D.

A. The Energy-Efficient Finite-Cardinality Design

Following the IM philosophy, all the signal additions in (4) and (8) may be replaced by data-carrying signal-selection. First of all, we propose to rewrite the τ -th layer in (4) and (8) as:

where the generator matrix \mathbf{G}_A is revised to be an $(M \times \overline{Q})$ -element Vandermonde matrix as:

$$\mathbf{G}_{A} = \mathbf{V}\mathbf{D}\mathbf{M}_{M \times \overline{Q}}(w_{L_{DM}}^{u_{1}}, \cdots, w_{L_{DM}}^{u_{M}})$$

$$= \begin{bmatrix} 1 & w_{L_{DM}}^{u_{1}} & w_{L_{DM}}^{2u_{1}} & \cdots & w_{L_{DM}}^{(\overline{Q}-1)u_{1}} \\ 1 & w_{L_{DM}}^{u_{2}} & w_{L_{DM}}^{2u_{2}} & \cdots & w_{L_{DM}}^{(\overline{Q}-1)u_{2}} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 1 & w_{L_{DM}}^{u_{M}} & w_{L_{DM}}^{2u_{M}} & \cdots & w_{L_{DM}}^{(\overline{Q}-1)u_{M}} \end{bmatrix}, \quad (16)$$

while the $(\overline{Q} \times 1)$ -element IM vector \mathbf{s}_{τ} is given by:

$$= \begin{bmatrix} 0 \cdots 0 & s^{t_{\tau}} & 0 \cdots 0 \end{bmatrix}^{T}.$$

$$\stackrel{\uparrow}{\underset{q_{\tau}}{\uparrow}} \qquad (17)$$

We note that the choice of \overline{Q} becomes flexible, which is independent of the hardware parameter of the number of TAs, RAs and RF chains. As a result, the activation index \overline{q}_{τ} and the modulation index l_{τ} carry $\log_2 \overline{Q}$ and $\log_2 \overline{L}$ information bits, respectively. Following this, we propose to construct the FC-GSTSK based on the TAST signal structure of (4) as:

$$\mathbf{S} = \frac{1}{\sqrt{M}} \sum_{\tau=1}^{M} \phi_r^{\tau-1} \operatorname{diag}(\mathbf{G}_A \mathbf{s}_{\tau}) \mathbf{G}_r^{\tau-1}, \qquad (18)$$

where the layer-switching phase is given by $\phi_r = w_{L_r}$, while the layer-switching matrix \mathbf{G}_r is given by (5). The integer rotation-parameters $\mathbf{u} = [u_1 \cdots u_m]$ are introduced in order to maximize the diversity gain, which will be detailed in Sec. III-C. In summary, the overall FC-GSTSK throughput is given by $[R = \frac{M(\log_2 \overline{Q} + \log_2 L)}{\overline{Q}} = \log_2 \overline{Q} + \log_2 L]$ for M = T, which is higher than that of STBCs from orthogonal [37], [38], AO [39], [40] and QO [41], [42] designs.

Furthermore, the LDC form [74] for the FC-GSTSK of (18) may be expressed as:

$$\mathbf{S} = \sum_{\tau=1}^{M} s^{l_{\tau}} \mathbf{A}_{\tau, \overline{q}_{\tau}} = \sum_{q=1}^{Q} \overline{s}_{q} \overline{\mathbf{A}}_{q}, \tag{19}$$

where the symbols $\{\overline{s}_q\}_{q=1}^Q$ are given by:

$$\overline{s}_q = \begin{cases} s^{l_\tau}, & \text{for } q = \overline{q}_\tau + (\tau - 1)\overline{Q} \\ 0, & \text{for all the other } q \end{cases},$$
(20)

while the dispersion matrices are expressed by:

$$\overline{\mathbf{A}}_{q} = \mathbf{A}_{\tau,\overline{q}} \\
= \frac{1}{\sqrt{M}} \phi_{r}^{\tau-1} \operatorname{diag}([w_{L_{DM}}^{(\overline{q}-1)u_{1}}, w_{L_{DM}}^{(\overline{q}-1)u_{2}}, \cdots, w_{L_{DM}}^{(\overline{q}-1)u_{M}}]) \mathbf{G}_{r}^{\tau-1}.$$
(21)

The relationship between the indices is given by $[q = \overline{q} + (\tau - 1)\overline{Q}]$. It is readily seen that the PAPR of $s^{l_{\tau}}$ remains unchanged, since the *m*-th signal on the τ -th layer in the FC-GSTSK signal matrix of (18) is given by $\frac{1}{\sqrt{M}}s^{l_{\tau}}w_{L_{DM}}^{(\overline{q}_{\tau}-1)u_m}w_{L_{\tau}}^{\tau-1}$. Furthermore, the equivalent LDC received signal model is also given by (13), where the equivalent $(1 \times Q)$ -element transmitted signal vector $\overline{\mathbf{S}}$ is now given by:

$$\overline{\mathbf{S}} = \begin{bmatrix} \overline{q}_1 & \overline{q}_2 & \overline{q}_M \\ \downarrow & \downarrow \\ \tau=1 & 0 \\ \tau=2 & \tau=M \end{bmatrix} \cdots \underbrace{q}_{\tau=M} \underbrace{q}_M \\ 0 \\ \cdots \\ 0 \\ \tau=M \end{bmatrix} \cdots \underbrace{q}_{\tau=M} \underbrace{q}_M \\ 0 \\ \tau=M \end{bmatrix} (22)$$

As a result, the FC-GSTSK signal detection is equivalent to that of a GSM scheme associated with $Q = M\overline{Q}$ TAs and Mactivated RF chains. Thanks to the IM design, the equivalent IAI is reduced to IAI = M in (22).

Remark 1 (Parameters): The FC-GSTSK scheme of (18) is unambiguously specified by the integer parameters of $(M, N, T, \overline{Q}, L, L_{DM}, L_r, \mathbf{u})$, where we have M = T and $Q = \overline{Q}M$. Given a MIMO setup of M TAs and N RAs, the diversity gain maximization process detailed in Sec. III-C is responsible for finding the best parameters of $(L_{DM}, L_r, \mathbf{u})$ that determine \mathbf{G}_A and ϕ_r for each specific throughput target of $[R = \log_2 \overline{Q} + \log_2 L]$.

Remark 2 (RF chains): Owing to the simultaneous activation of all layers in (18), the default mode of FC-GSTSK is the full-RF transmission with IAI = M. Nonetheless, if " $\sum_{\tau=1}^{M}$ " in (18) is replaced by " $\sum_{\tau=1}^{M_A}$ ", a subset of M_A out of Mlayers is activated, which results in a reduced number of M_A activated RFs associated with IAI = M_A . For the special case of $M_A = 1$, the FC-GSTSK of (18) becomes the single-RF and IAI-free STSK design of [21].

Remark 3 (Complexity): According to [26], the ML detection complexity of FC-GSTSK that activates M out of Q dispersion matrices is in proportional to the full ML complexity within a factor of M/Q for the LDCs of (4) and (8) in Sec. II. When the suboptimal GSM detectors of [49], [50] are considered, a MMSE detector or a SD of the equivalent M-IAI V-BLAST may be invoked \overline{Q}^M times for all the activation combinations in (22). In this work, the ML detectors of [26], [27] are assumed in order to verify the performance analysis of FC-GSTSK.

B. Schematic Description

The schematics of Goden code and FC-GSTSK are explicitly visualized in Fig. 2. As demonstrated by Fig. 2(a), the diversity advantage of Goden code [36] is achieved at the substantial extra cost for the transceiver to deal with the increased PAPR and IAI, which constitutes the major stumbling block of the practical deployment of perfect STBCs

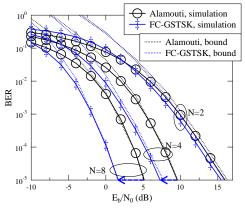


Fig. 3: BER comparison between Alamouti's G2 STBC and the new FC-GSTSK, when we have (M = T = 2), $N = \{2, 4, 8\}$ and R = 3.0. The parameters can be found in Sec. V.

[32]–[36]. By contrast, the proposed FC-GSTSK conceived based on the TAST and IM philosophies is capable of offering the following exclusive advantages:

- (A) The IM design eliminates the signal superpositions in TAST, as demonstrated by Fig. 2(b). As a result, when specifically considering *L*-PSK signalling for s^l_τ, the perfect 0 dB PAPR is retained for all of the FC-GSTSK signals of {s^{l_τ} w^{(q_τ-1)u_m} w^{τ-1}_{L_r}}_{π=1}.
 (D) The IM design of the second seco
- (B) The IM design eliminates the intra-layer IAI, as demonstrated by Fig. 2(b). As a result, the total IAI of the FC-GSTSK is reduced back to the same level as the V-BLAST's IAI = M.
- (C) The FC-GSTSK throughput is given by $R = \log_2 \overline{Q} + \log_2 L$, where increasing \overline{Q} does not impose extra hardware cost in terms of more TAs, RAs or RF chains. The FC-GSTSK capacity will be further analysed in Sec. III-D.
- (D) The FC-GSTSK retains the non-diminishing high diversity gain by appropriately adjusting the integer parameters of $(L_{DM}, L_r, \{u_m\}_{m=1}^M)$ in order to cater for the different MIMO setups, which will be further elaborated on in Sec. III-C.

C. Diversity Gain Maximization

The averaged BER of a generic MIMO scheme is given by: [55], [75]

$$\overline{P}_{e,bit} \le \mathbb{E}\left[\sum_{i=0}^{I-1} \sum_{i'=0}^{I-1} \frac{d_H(i,i')}{I \log_2 I} p(\mathbf{S}^i \to \mathbf{S}^{i'})\right],$$
(23)

where $d_H(i, i')$ refers to the Hamming distance between the bit-mappings of \mathbf{S}^i and $\mathbf{S}^{i'}$. The Pairwise Error Probability (PEP) is upper bounded by: [55], [75]

$$p(\mathbf{S}^{i} \to \mathbf{S}^{i'}) \le \mathbb{E}\left\{Q\left[\frac{\sqrt{\|(\mathbf{S}^{i} - \mathbf{S}^{i'})\mathbf{H}\|^{2}}}{2N_{0}}\right]\right\},$$
 (24)

where $Q(\cdot)$ represents the integral form of the Q-function. The BERs of the Alamouti's G2 STBC and the proposed FC-GSTSK are exemplied in Fig. 3, which verifies the advantages of FC-GSTSK in terms of both simulation and the theoretical bound of (23). Furthermore, in order to formulate the Objective

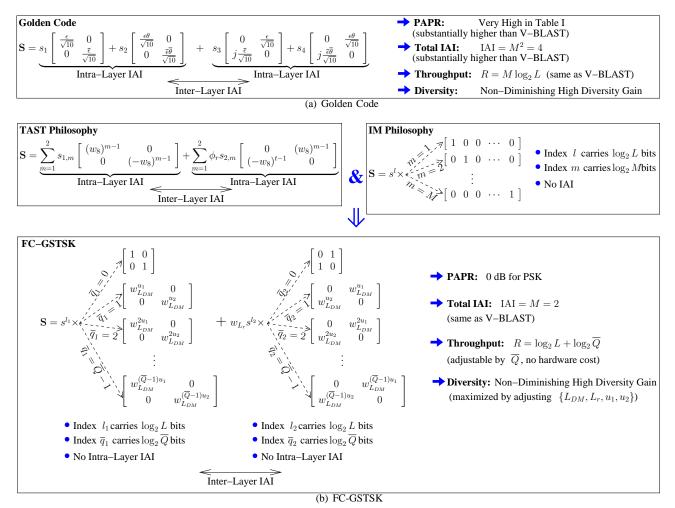


Fig. 2: Schematic descriptions of Golden code [36] seen in Example 1 and the proposed FC-GSTSK (M = T = 2).

Functions (OFs) of diversity gains, the PEP of (24) is extended as:

$$p(\mathbf{S}^{i} \to \mathbf{S}^{i'}) \le \left(\frac{1}{4N_{0}}\right)^{-N\operatorname{rank}(\boldsymbol{\Delta})} \left[\prod_{m=1}^{\operatorname{rank}(\boldsymbol{\Delta})} \lambda_{m}\right]^{-N},$$
 (25)

where $\{\lambda_m\}_{m=1}^M$ are eigenvalues of $[\mathbf{\Delta} = (\mathbf{S}^i - \mathbf{S}^{i'})^H (\mathbf{S}^i - \mathbf{S}^{i'})]$. Assuming the full rank [rank($\mathbf{\Delta}$) = M = T], the PEP may be further rewritten as: [76]

$$p(\mathbf{S}^{i} \to \mathbf{S}^{i'}) \le \left[1 + \sum_{m=1}^{M} \left(\frac{1}{4N_{0}}\right)^{m} \Xi_{m}\right]^{-N}, \qquad (26)$$

where $(\Xi_m = \sum_{1 \le i_1 < i_2 < \dots < i_m \le M} \prod_{k=1}^m \lambda_{i_k})$ has the special cases of $(\Xi_M = \prod_{m=1}^M \lambda_m)$ and $(\Xi_1 = \sum_{m=1}^M \lambda_m)$. Owing to the associated coefficients of $\left(\frac{1}{4N_0}\right)^M$ and $\left(\frac{1}{4N_0}\right)^1$ for Ξ_M and Ξ_1 in (26), the determinant term $[\det(\mathbf{\Delta}) = \prod_{m=1}^M \lambda_m]$ and the trace term $[tr(\mathbf{\Delta}) = \sum_{m=1}^M \lambda_m]$ dominate the PEP in the high-and low-SNR regions, respectively. Accordingly, the trend of PEP may be characterized by the *diversity product* and by the *diversity sum* as [21], [76]:

$$\Lambda_{p} = \frac{1}{2} \min_{\forall i \neq i'} \det(\mathbf{\Delta})^{\frac{1}{2T}},$$

$$\Lambda_{s} = \frac{1}{2\sqrt{T}} \min_{\forall i \neq i'} \operatorname{tr}(\mathbf{\Delta})^{\frac{1}{2}}.$$
(27)

Moreover, according to the average BER expression of (23), the *average diversity product* and *average diversity sum* are expressed as [21]:

$$\overline{\Lambda}_{p} = \frac{1}{2} \left[\frac{2}{\log_{2} I + 1} \sum_{\forall i} \sum_{\forall i' \neq i} \frac{d_{H}(i, i')}{I \log_{2} I \det(\boldsymbol{\Delta})} \right]^{-\frac{1}{2M}},$$

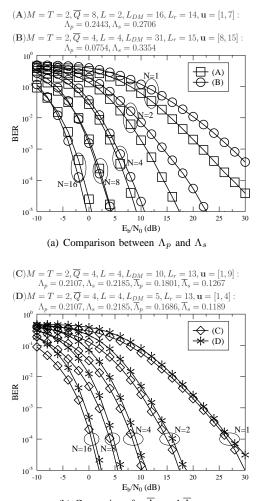
$$\overline{\Lambda}_{s} = \frac{1}{2\sqrt{M}} \left[\frac{2}{\log_{2} I + 1} \sum_{\forall i} \sum_{\forall i' \neq i} \frac{d_{H}(i, i')}{I \log_{2} I \operatorname{tr}(\boldsymbol{\Delta})} \right]^{-\frac{1}{2}}.$$
(28)

The four metrics of Λ_p , Λ_s , $\overline{\Lambda_p}$ and $\overline{\Lambda_s}$ in (27) and (28) are normalized to be within [0, 1]. Fig. 4(a) demonstrates that a higher Λ_p or Λ_s leads to better performance for smaller N ={1, 2} or larger N = {8, 16}, respectively. Moreover, Fig. 4(b) further confirms that when Λ_p and Λ_s are fixed, the higher values of $\overline{\Lambda_p}$ and $\overline{\Lambda_s}$ also lead to better performance.

Unfortunately, it is impossible to maximize all the four OFs of $\{\Lambda_p, \Lambda_s, \overline{\Lambda}_p, \overline{\Lambda}_s\}$ at the same time. Therefore, it is important to determine their priorities according to the MIMO setup. There are a total number of 4! = 24 possible arrangements of priorities, and our analysis is characterized by the following linear regression equation:

$$SNR_t = \kappa_0 + \kappa_1 \Lambda_p + \kappa_2 \Lambda_s + \kappa_3 \overline{\Lambda}_p + \kappa_4 \overline{\Lambda}_s, \qquad (29)$$

where for each construction of $\{\mathbf{S}^i\}_{i=0}^{I-1}$ according to (18), the simulation result of SNR_t is recorded at the target BER = 10⁻⁴, while the associated $\{\Lambda_p, \Lambda_s, \overline{\Lambda}_p, \overline{\Lambda}_s\}$ are



(b) Comparison for $\overline{\Lambda}_p$ and $\overline{\Lambda}_s$ Fig. 4: Performance comparison between four FC-GSTSK(M = T = 2, R = 4) associated with different parameters.

evaluated based on (27) and (28). The regression coefficients $\{\kappa_0, \dots, \kappa_4\}$ can be automatically determined by machine learning in Excel, and the descending priorities are assigned to the four OFs according to their descending coefficient values.

More explicitly, the pseudocode for the diversity gain maximization of the FC-GSTSK is provided in Table II, which summarizes four proto-type arrangements that are often encountered in our intensive simulations. The first two arrangements in Table II often produce beneficial FC-GSTSK solutions for small $N = \{1, 2\}$, while the latter two arrangements often lead to good performance for N > 2. Following this, the rest of the pseudocode in Table II aims for finding the best integer parameters $(1 < L_{DM}, L_r \leq LT\overline{Q})$ and $(1 \leq \{u_m\}_{m=1}^M < L_{DM})$ that maximize the four OFs $\{\Lambda_1, \dots, \Lambda_4\}$ in descending order of priorities. We note that the values of $\{u_m\}_{m=1}^M$ has to be relatively prime to L_{DM} , as represented by $\{\gcd(u_m, L_{DM}) = 1\}_{m=1}^M$ in Table II. Otherwise, there exist $[u_m(q-1) \mod L_{DM} = 0]$ values that result in $(\Lambda_p = 0)$.

Example 2: For the case of M = T = 2 and R = 3.0, the best FC-GSTSK we have found has the parameters of $(\overline{Q} = 4, L = 2, L_{DM} = 8, L_r = 14, \mathbf{u} = [1,3])$. This is obtained by performing full-search over all the possible combinations of $(1 < L_{DM} \le 16)$, $(1 < L_r \le 16)$ and $\{\gcd(u_m, L_{DM}) = 1\}_{m=1}^M$. The signal constructions of (16), (21) and (22) are

TABLE II: Pseudocode for the diversity gain maximization of the FC-GSTSK.

	angement I:			$\Lambda_3 = \underline{\Lambda}_p,$	
	angement II:				
	angement III:				
Arra	angement IV:	$\Lambda_1 = \overline{\Lambda}_s,$	$\Lambda_2 = \Lambda_s,$	$\Lambda_3 = \overline{\Lambda}_p,$	$\Lambda_4 = \Lambda_p$
1:	Initialize L_{DM}^{opt}	, L_r^{opt} , $\{u_m^{\text{opt}}\}$	$_{m=1}^{M}, \{\Lambda_{k}^{\text{opt}} =$	$\{0\}_{k=1}^4$	
2:	Initialize integer	s $1 < L_{DM}$,	$L_r \leq LT\overline{Q}$		
3:	Initialize integer	s $1 \leq \{u_m\}_{m=1}^M$	$< L_{DM}$, where	$e \{ gcd(u_m, L_L) \}$	$M_{M} = 1_{m=1}^{M}$
	Construct $\{\mathbf{S}^i\}$				
	Evaluate $\{\Lambda_k=0\}$			28) for $\{\{\mathbf{S}^i, \}$	${f S}^{i'}_{i \neq i'}_{i \neq i'}^{I-}_{i-}$
	if $(\Lambda_1 > \Lambda_1^{opt})$:				, t <i>+</i> t , t=
	update $L_{DM}^{\text{opt}} = I$	$L_{DM}, L_r^{opt} = L$	$_{r}, \{u_{m}^{\text{opt}}=u_{m}\}$	$M_{m-1}, \{\Lambda_{h}^{\text{opt}} = \Lambda$	$_{k}^{k}_{k-1}^{4}$
	else if $(\Lambda_1 \approx \Lambda_2)$			m=i t k	<i>k k i</i>
8:	if $(\Lambda_2 > \Lambda_2^{\text{opt}})$				
	update $L_{DM}^{opt^2}$ =	$=L_{DM}L_r^{\text{opt}}=$	L_r , $\{u_m^{opt}=u_m$	$M_{m-1} \{ \Lambda_{t}^{\text{opt}} =$	$\{\Lambda_k\}_{k=1}^4$
9:	else if $(\Lambda_2 \approx$			5 <i>m</i> =1°C <i>k</i>	$\kappa j \kappa = 1$
10:	if $(\Lambda_3 > \Lambda_3^0)$				
	update $L_{\rm D}^{\rm opt}$	$=L_D M L_r^{opt}$	$=L_r$, $\{u_m^{opt}=u\}$	$_{m}\}_{m=1}^{M}, \{\Lambda_{k}^{\text{opt}}\}$	$= \Lambda_k \}_{k=1}^4$
11:		$\approx \Lambda_3^{\text{opt}})\&(\Lambda_4)$		m j m = 1, 0 - k	k = 1
	update L_{p}^{opt}	$L = L_D M L_p^{or}$	$u_{m}^{ot} = L_r \cdot \{u_{m}^{opt} =$	$\{u_m\}_{m=1}^M, \{\Lambda\}$	$\sum_{k=1}^{n} = \Lambda_k \{ \}_{k=1}^{4}$
	end if	<i>A</i> = <i>D</i> ₁ <i>M</i> ,= <i>t</i>	_,,(~,,,	-m) _{m=1} ,($k = -\kappa J k =$
12:	end if				
13:	end if				
	go to 2&3 until				
	Output $(L_{DM}^{opt}, to (18))$.	$L_r^{\text{opt}}, \{u_m^{\text{opt}}\}_m^M$	=1) for constr	ucting $\{\mathbf{S}^i\}_{i=1}^{I-1}$	$_{=0}^{-1}$ accordin

TABLE III: Signal constructions of (16), (21) and (22) for the FC-GSTSK of *Example 2:* using $(\overline{Q} = 4, L = 2, L_{DM} = 8, L_r = 14, \mathbf{u} = [1, 3]).$

$[1, \mathbf{u} = [1, 0]).$	
$\mathbf{G}_A = \begin{bmatrix} 1 & w_8 & w_8^2 & w_8 \\ 1 & w_8^3 & w_8^6 & w_8 \end{bmatrix}$	
$\overline{\mathbf{A}}_1 = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 0\\ 0 & 1 \end{bmatrix},$	$\overline{\mathbf{A}}_2 = rac{1}{\sqrt{2}} \left[egin{array}{cc} w_8 & 0 \ 0 & w_8^3 \end{array} ight],$
$\overline{\mathbf{A}}_3 = \frac{1}{\sqrt{2}} \begin{bmatrix} w_8^2 & 0 \\ 0 & w_8^6 \end{bmatrix},$	$\overline{\mathbf{A}}_4 = rac{1}{\sqrt{2}} \left[egin{array}{cc} w_8^3 & 0 \ 0 & w_8 \end{array} ight],$
$\overline{\mathbf{A}}_5 = \frac{1}{\sqrt{2}} w_{14} \begin{vmatrix} 0 & 1 \\ 1 & 0 \end{vmatrix},$	
$\overline{\mathbf{A}}_7 = \frac{1}{\sqrt{2}} w_{14} \begin{bmatrix} 0 & \overline{w}_8^2 \\ w_8^6 & 0 \end{bmatrix}$	$\left], \overline{\mathbf{A}}_8 = \frac{1}{\sqrt{2}} w_{14} \left[\begin{array}{cc} 0 & w_8^3 \\ w_8 & 0 \end{array} \right].$
$\overline{\mathbf{S}} = \begin{cases} [s^{l_1} \ 0 \ 0 \ 0 \ s^{l_2} \ 0 \ 0 \ 0], \\ [0 \ s^{l_1} \ 0 \ s^{l_2} \ 0 \ 0], \\ [s^{l_1} \ 0 \ 0 \ 0 \ s^{s_2} \ 0 \ 0], \\ [s^{l_1} \ 0 \ 0 \ 0 \ s^{s_2} \ 0 \ 0], \\ [s^{l_1} \ 0 \ 0 \ 0 \ 0 \ s^{s_2} \ 0], \\ [s^{l_1} \ 0 \ 0 \ 0 \ 0 \ s^{l_2} \ 0], \\ [s^{l_1} \ 0 \ 0 \ 0 \ 0 \ s^{s_2} \ 0], \\ [s^{l_1} \ 0 \ 0 \ 0 \ 0 \ s^{s_2} \ 0], \\ [s^{l_1} \ 0 \ 0 \ 0 \ 0 \ s^{s_2} \ 0], \\ [s^{l_1} \ 0 \ 0 \ 0 \ 0 \ s^{s_2} \ 0], \\ [s^{l_1} \ 0 \ 0 \ 0 \ 0 \ s^{s_2} \ 0], \\ [s^{l_1} \ 0 \ 0 \ 0 \ 0 \ s^{s_2} \ 0], \\ [s^{l_1} \ 0 \ 0 \ 0 \ 0 \ s^{l_2} \ 0], \\ [s^{l_1} \ 0 \ 0 \ 0 \ 0 \ 0 \ s^{s_2} \ 0], \\ [s^{l_1} \ 0 \ 0 \ 0 \ 0 \ 0 \ s^{s_2} \ 0], \\ [s^{l_1} \ 0 \ 0 \ 0 \ 0 \ 0 \ s^{s_2} \ 0], \\ [s^{l_1} \ 0 \ 0 \ 0 \ 0 \ 0 \ s^{s_2} \ 0], \\ [s^{l_1} \ 0 \ 0 \ 0 \ 0 \ 0 \ s^{s_2} \ 0], \\ [s^{l_1} \ 0 \ 0 \ 0 \ 0 \ 0 \ s^{s_2} \ 0], \\ [s^{l_1} \ 0 \ 0 \ 0 \ 0 \ 0 \ s^{s_2} \ 0], \\ [s^{l_1} \ 0 \ 0 \ 0 \ 0 \ s^{s_2} \ 0], \\ [s^{l_1} \ 0 \ 0 \ 0 \ 0 \ s^{s_2} \ 0], \\ [s^{l_1} \ 0 \ 0 \ 0 \ 0 \ s^{s_2} \ 0], \\ [s^{l_1} \ 0 \ 0 \ 0 \ 0 \ s^{s_2} \ 0], \\ [s^{l_1} \ 0 \ 0 \ 0 \ 0 \ s^{s_2} \ 0], \\ [s^{l_1} \ 0 \ 0 \ 0 \ 0 \ s^{s_2} \ 0], \\ [s^{l_1} \ 0 \ 0 \ 0 \ 0 \ s^{s_2} \ 0], \\ [s^{l_1} \ 0 \ 0 \ 0 \ 0 \ s^{s_2} \ 0], \\ \ 0 \ s^{l_1} \ 0 \ 0 \ 0 \ 0 \ s^{s_2} \ 0], \\ \ 0 \ s^{l_1} \ 0 \ 0 \ 0 \ s^{s_2} \ 0], \\ \ 0 \ s^{l_1} \ 0 \ 0 \ 0 \ s^{s_2} \ 0], \\ \ 0 \ s^{l_1} \ 0 \ 0 \ s^{l_1} \ 0 \ 0 \ 0 \ 0 \ s^{l_1} \ 0 \ 0 \ 0 \ s^{l_1} \ 0 \ 0 \ 0 \ 0 \ s^{l_1} \ 0 \ 0 \ 0 \ s^{l_1} \ 0 \ 0 \ 0 \ 0 \ s^{l_1} \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ $	$ \left. \begin{array}{c} [0 \ s^{l_1} \ 0 \ 0 \ s^{l_2} \ 0 \ 0 \ 0], \\ [0 \ 0 \ 0 \ s^{l_1} \ s^{l_2} \ 0 \ 0 \ 0], \\ [0 \ s^{l_1} \ 0 \ 0 \ 0 \ s^{l_2} \ 0 \ 0], \\ [0 \ 0 \ s^{l_1} \ 0 \ 0 \ 0 \ s^{l_2} \ 0 \ 0], \\ [0 \ s^{l_1} \ 0 \ 0 \ 0 \ s^{l_2} \ 0], \\ [0 \ s^{l_1} \ 0 \ 0 \ 0 \ s^{l_2} \ 0], \\ [0 \ 0 \ s^{l_1} \ 0 \ 0 \ 0 \ s^{l_2} \ 0], \\ [0 \ s^{l_1} \ 0 \ 0 \ 0 \ s^{l_2} \ 0], \\ [0 \ s^{l_1} \ 0 \ 0 \ 0 \ 0 \ s^{l_2} \ 0], \\ [0 \ s^{l_1} \ 0 \ 0 \ 0 \ 0 \ s^{l_2} \ 0], \\ [0 \ s^{l_1} \ 0 \ 0 \ 0 \ 0 \ s^{l_2} \ 0], \\ [0 \ s^{l_1} \ 0 \ 0 \ 0 \ 0 \ s^{l_2} \ 0], \\ [0 \ s^{l_1} \ 0 \ 0 \ 0 \ 0 \ s^{l_2} \ 0], \\ [0 \ s^{l_1} \ 0 \ 0 \ 0 \ s^{l_2} \ 0], \\ [0 \ s^{l_1} \ 0 \ 0 \ 0 \ s^{l_2} \ 0], \\ [0 \ s^{l_1} \ 0 \ 0 \ 0 \ s^{l_2} \ 0], \\ [0 \ s^{l_1} \ 0 \ 0 \ 0 \ s^{l_2} \ 0], \\ [0 \ s^{l_1} \ 0 \ 0 \ 0 \ s^{l_2} \ 0], \\ [0 \ s^{l_1} \ 0 \ 0 \ s^{l_2} \ 0], \\ [0 \ s^{l_1} \ 0 \ 0 \ s^{l_2} \ 0], \\ [0 \ s^{l_1} \ 0 \ 0 \ s^{l_2} \ 0], \\ [0 \ s^{l_1} \ 0 \ 0 \ s^{l_2} \ 0], \\ [0 \ s^{l_1} \ 0 \ 0 \ s^{l_1} \ 0 \ 0 \ s^{l_2} \ 0], \\ \end{tabular}$

presented in Table III. The resultant signal matrices S of (18) have $(\Lambda_p = 0.3917)$ and $(\Lambda_s = 0.5)$, which are substantially higher than $(\Lambda_p = 0.2706)$ and $(\Lambda_s = 0.2706)$ of Alamouti's STBC [37] using 8PSK. Hence it is expected that FC-GSTSK is capable of substantially outperforming Alamouti's STBC using M = T = 2 and R = 3.0 (see Fig. 8b).

Remark 4 (High-throughput construction): At high throughputs, the full-search of Table II may become infeasible. Alternatively, one may invoke Table II for the DAST signal model of $\mathbf{S} = \text{diag}(\mathbf{G}_A \mathbf{s})$ in order to obtain L_{DM} and $\{u_m\}_{m=1}^M$ as the first step. For example, for the case of M = T = 2 and R = 8.0, there are a total number of $(I = 2^{RT} = 65536)$ combinations for the FC-GSTSK signal matrices, but this is reduced to only $(I = 2^{RT/2} = 256)$ for the DAST. Upon obtaining L_{DM} and $\{u_m\}_{m=1}^M$, Table II may be invoked again just for L_r .

D. Analysis on Bandwidth- and Power-Efficiency

First of all, let us examine the bandwidth-efficiency with the aid of the Continuous-input Continuous-output Memoryless Channel (CCMC) capacity. More explicitly, the CCMC capacity of V-BLAST evaluated based on $[p(\mathbf{Y}|\mathbf{S}) = \frac{1}{(\pi N_0)^N} \exp(-\frac{\|\mathbf{Y}-\mathbf{SH}\|^2}{N_0})]$ is given by:

$$\mathcal{C}_{\text{MIMO}}^{\text{CCMC}}(\text{SNR}) = \max_{p(\mathbf{S})} \mathcal{I}(\mathbf{S}; \mathbf{Y}) = \text{E}\left[\log_2 \det\left(\mathbf{I}_N + \frac{\eta}{M} \mathbf{H}^H \mathbf{H}\right)\right],$$
(30)

where (SNR = $10 \log_{10} \eta$ dB), while the mutual information $\mathcal{I}(\mathbf{S}; \mathbf{Y})$ is maximized for a Gaussian input signal having $[\mathbf{E}(\mathbf{S}^H \mathbf{S}) = \frac{1}{M} \mathbf{I}_M]$.

By contrast, for the orthogonal STBCs [37]–[40], the signal construction may be generalized as $[\mathbf{S} = \sqrt{P_t} \sum_{q=1}^{Q} (\mathbf{D}_q^+ s_q + \mathbf{D}_q^- s_q^*)]$, where the power normalization factor P_t ensures $E[\text{tr}(\mathbf{SS}^H)] = T$, while $\{\mathbf{D}_q^+, \mathbf{D}_q^-\}_{q=1}^Q$ are dispersion matrices from orthogonal design. Owing to the orthogonality, the conditional probability $p(\mathbf{Y}|\mathbf{S})$ may be decoupled as $[p(\mathbf{Y}|\mathbf{S}) = \vartheta \prod_{q=1}^{Q} p(\overline{z}_q | s_q)]$, where we have $\{\overline{z}_q = \frac{MQ\sqrt{P_t}}{T||\mathbf{H}||^2} \text{tr}[\mathbf{Y}^H \mathbf{D}_q^- \mathbf{H} + \mathbf{H}^H(\mathbf{D}_q^+)^H \mathbf{Y}]\}$, $[\vartheta = \frac{(\pi \overline{N}_0)^Q}{(\pi N_0)^{NT}} \exp(-\frac{\vartheta}{N_0})]$, $[\vartheta = ||\mathbf{Y}||^2 - \sum_{q=1}^{Q} \frac{T||\mathbf{H}||^2}{MQ} |\overline{z}_q|^2]$ and $[p(\overline{z}_q | s_q) = \frac{1}{\pi \overline{N}_0} \exp(-\frac{|\overline{z}_q - s_q|^2}{N})]$, while the equivalent noise power is given by $(\overline{N}_0 = \frac{MQ}{T||\mathbf{H}||^2} N_0)$. As a result, the CCMC capacity of STBCs from orthogonal design marks a loss in bandwidth-efficiency as [55], [77]:

$$\mathcal{C}_{STBC}^{CCMC}(SNR) = \max_{\{p(s_q)\}_{q=1}^Q} \frac{1}{T} \sum_{q=1}^Q \mathcal{I}(s_q; \overline{z}_q) \\
= \frac{Q}{T} \mathbb{E} \left[\log_2 \left(1 + \frac{T \| \mathbf{H} \|^2}{MQ} \eta \right) \right], \qquad (31) \\
= \frac{Q}{T} C_{MIMO}^{CCMC}(MN, 1, \frac{NT}{Q} \eta) \leq C_{MIMO}^{CCMC}(M, N, \eta),$$

which indicates that $C_{\text{STBC}}^{\text{CCMC}}(\text{SNR})$ is equivalent to a fraction $\frac{Q}{T}$ of the full MIMO capacity of (30) with MN TAs, 1 RA and (SNR = $10 \log_{10} \frac{NT}{Q} \eta$ dB). Therefore, the orthogonal STBC only becomes capacity-optimal for the special case of Alamouti's (M = 2) scheme using (N = 1).

Moreover, for the generic LDC signal model of (13), the CCMC capacity evaluated based on $[p(\overline{\mathbf{Y}}|\overline{\mathbf{S}}) = \frac{1}{(\pi N_0)^{TN}} \exp(-\frac{\|\overline{\mathbf{Y}}-\overline{\mathbf{SH}}\|^2}{N_0})]$ is given by [55], [74]:

$$\mathcal{C}_{\text{LDC}}^{\text{CCMC}}(\text{SNR}) = \max_{p(\overline{\mathbf{s}})} \mathcal{I}(\overline{\mathbf{s}}; \overline{\mathbf{Y}}) = \mathrm{E} \left\{ \log_2 \det \left[\mathbf{I}_{NT} + \eta (\mathbf{I}_T \otimes \mathbf{H})^H \overline{\boldsymbol{\chi}}^H \overline{\boldsymbol{\chi}} (\mathbf{I}_T \otimes \mathbf{H}) \right] \right\}.$$
(32)

In particular, the family of the capacity-optimal LDCs [55], [74] including the Golden code [36] has $\overline{\chi}^H \overline{\chi} = \frac{1}{M} \mathbf{I}_{TM}$, which results in the full MIMO capacity of $[\mathcal{C}_{\text{LDC}}^{\text{CCMC}}(\text{SNR}) = \mathcal{C}_{\text{MIMO}}^{\text{CCMC}}(\text{SNR})]$.

For the proposed FC-GSTSK, both the classic modulated symbols $\{s^{l_{\tau}}\}_{\tau=1}^{M}$ and the IM activation indices $\{\bar{q}_{\tau}\}_{\tau=1}^{M}$ in (22) carry input information, yielding:

$$\mathcal{C}_{\text{FC-GSTSK}}^{\text{CCMC}}(\text{SNR}) = \mathcal{C}_{\text{FC-GSTSK}}^{\text{CCMC-MOD}}(\text{SNR}) + \mathcal{C}_{\text{FC-GSTSK}}^{\text{CCMC-IM}}(\text{SNR}).$$
(33)

The first part in (33) is evaluated based on $[p(\overline{\mathbf{Y}}|\overline{\mathbf{S}}) = \frac{1}{(\pi N_0)^{TN}} \exp(-\frac{\|\overline{\mathbf{Y}}-\overline{\mathbf{SH}}\|^2}{N_0})]$ as:

$$\mathcal{C}_{\text{FC-GSTSK}}^{\text{CCMC-MOD}}(\text{SNR}) = \max_{\{p(s^{l_{\tau}})\}_{\tau=1}^{M}} \frac{1}{T} \mathcal{I}(\{s^{l_{\tau}}\}_{\tau=1}^{M}; \overline{\mathbf{Y}} | \{\overline{q}_{\tau}\}_{\tau=1}^{M})$$
$$= \frac{1}{T\overline{Q}^{M}} \underbrace{\sum_{\overline{q}_{1}=1}^{\overline{Q}} \cdots \sum_{\overline{q}_{M}=1}^{\overline{Q}}}_{M} \mathbb{E} \left[\log_{2} \det(\mathbf{I}_{NT} + \eta \overline{\mathbf{H}}^{H} \mathbf{J} \overline{\mathbf{H}}) \right].$$
(34)

The $(Q \times Q)$ -element $[\mathbf{J} = \mathrm{E}(\overline{\mathbf{S}}^H \overline{\mathbf{S}}) = \mathrm{diag}(\mathbf{J}_1, \mathbf{J}_2, \cdots, \mathbf{J}_M)]$ is conditioned on the IM activation indices $\{\overline{q}_{\tau}\}_{\tau=1}^M$, where the constituent $(\overline{Q} \times \overline{Q})$ -element $\{\mathbf{J}_{\tau}\}_{\tau=1}^M$ has all-zero elements

except for a single non-zero element on the \overline{q}_{τ} -th row and \overline{q}_{τ} column as:

$$\mathbf{J}_{\tau} = \begin{bmatrix} 0 & \cdots & 0 & 0 & 0 & \cdots & 0 \\ \vdots & \ddots & \vdots & \vdots & \vdots & \ddots & \vdots \\ 0 & \cdots & 0 & 0 & 0 & \cdots & 0 \\ 0 & \cdots & 0 & 1 & 0 & \cdots & 0 \\ 0 & \cdots & 0 & 0 & 0 & \cdots & 0 \\ \vdots & \ddots & \vdots & \vdots & \vdots & \ddots & \vdots \\ 0 & \cdots & 0 & 0 & 0 & \cdots & 0 \end{bmatrix}.$$
 (35)

The mutual information in (34) is maximized for the "Gaussianized" signals of $\{s^{l_{\tau}}\}_{\tau=1}^{M}$. By contrast, the IM activation indices $\{\overline{q}_{\tau}\}_{\tau=1}^{M}$ are always discrete-valued. More explicitly, the second part in (33) is evaluated based on $[p(\overline{\mathbf{Y}}|\{\overline{q}_{\tau}\}_{\tau=1}^{M}) = \frac{1}{\det(\tau \mathbf{R}_{YY})} \exp(-\overline{\mathbf{Y}}\mathbf{R}_{YY}^{-1}\overline{\mathbf{Y}})]$ relying on $[\mathbf{R}_{YY} = \mathbf{E}(\overline{\mathbf{Y}}^{H}\overline{\mathbf{Y}}) = \overline{\mathbf{H}}^{H}\mathbf{J}\overline{\mathbf{H}} + N_{0}\mathbf{I}_{NT}]$ as (36), where the mutual information is maximized for the equal-prob source of $\{p(\overline{q}_{\tau}) = 1/\overline{Q}\}_{\tau=1}^{M}$. As a result, the bandwidth-efficiency of FC-GSTSK increases logarithmically with \overline{Q} , which is evidenced by Fig. 5(a). Furthermore, Fig. 5(a) also demonstrates that as \overline{Q} grows, the CCMC capacity of FC-GSTSK improves further beyond STBC towards the full MIMO capacity. Once again, we note that increasing the parameter \overline{Q} in the FC-GSTSK signal model of (18) does not impose extra hardware cost in terms of TAs, RAs or RF chains.

The CCMC capacities of Fig. 5(a) are unbounded upon increasing the SNR. However, in reality, the power-efficiency at a specific target rate is more relevant to the overall system performance. The encountered Discrete-input Continuous-output Memoryless Channel (DCMC) capacity is evaluated based on $[p(\mathbf{Y}|\mathbf{S}) = \frac{1}{(\pi N_0)^{NT}} \exp(-\frac{\|\mathbf{Y} - \mathbf{SH}\|^2}{N_0})]$ as:

$$\mathcal{C}^{\text{DCMC}}(\text{SNR}) = \max_{p(\mathbf{S})} \frac{1}{T} \sum_{\forall \mathbf{S}} \int p(\mathbf{Y}|\mathbf{S}) p(\mathbf{S}) \log_2 \frac{p(\mathbf{Y}|\mathbf{S})}{p(\mathbf{Y})} d\mathbf{Y}$$
$$= \frac{1}{IT} \sum_{i=0}^{I-1} \mathbb{E} \left[\log_2 \frac{I \exp\left(-\frac{\|\mathbf{Y}-\mathbf{S}^i\mathbf{H}\|^2}{N_0}\right)}{\sum_{i'=0}^{I-1} \exp\left(-\frac{\|\mathbf{Y}-\mathbf{S}^{i'}\mathbf{H}\|^2}{N_0}\right)} \right],$$
(37)

which is maximized for the equal-prob source of $\{p(\mathbf{S}^i) = 1/I\}_{i=0}^{I-1}$.

As a result, it is demonstrated by Fig. 5(b) that the proposed FC-GSTSK is capable of achieving better DCMC capacities than V-BLAST and STBC, where the SNRs required for the FC-GSTSK to achieve the target rates of $R = \{2.0, 3.0, 4.0\}$ are lower, hence the better power-efficiency. Moreover, it also appears that as the throughput increases to R = 4.0, the Golden code starts to perform the best in Fig. 5(b). However, when the practical power consumption at the transmitter is taken into account by the PSNR of (PSNR = $10 \log_{10} \frac{\max |s|}{N_0} dB$), the power-efficiency of FC-GSTSK is substantially better than that of the Golden code, as distinctively marked in Fig. 5(c). Our more detailed performance comparisons will be presented in Sec. V.

IV. EXTENSIONS ON SIGNAL CONSTRUCTION

In this section, we proceed to extend the FC-GSTSK signal construction for a wider range of MIMO scenarios. First of all, the ASK design for star QAM signalling is presented in

$$\mathcal{C}_{\text{FC-GSTSK}}^{\text{CCMC-IM}}(\text{SNR}) = \max_{\{p(\overline{q}_{\tau})\}_{\tau=1}^{M}} \frac{1}{T} \mathcal{I}(\{\overline{q}_{\tau}\}_{\tau=1}^{M}; \overline{\mathbf{Y}}) = \max_{\{p(\overline{q}_{\tau})\}_{\tau=1}^{M}} \frac{1}{T} \underbrace{\sum_{\overline{q}_{1}=1}^{\overline{Q}} \cdots \sum_{\overline{q}_{M}=1}^{\overline{Q}}}_{M} \int p(\overline{\mathbf{Y}} | \{\overline{q}_{\tau}\}_{\tau=1}^{M}) \prod_{\tau=1}^{M} p(\overline{q}_{\tau}) \log_{2} \frac{p(\overline{\mathbf{Y}} | \{\overline{q}_{\tau}\}_{\tau=1}^{M})}{p(\overline{\mathbf{Y}})} d\overline{\mathbf{Y}}$$

$$= \frac{1}{T\overline{Q}^{M}} \underbrace{\sum_{\overline{q}_{1}=1}^{\overline{Q}} \cdots \sum_{\overline{q}_{M}=1}^{\overline{Q}}}_{M} \mathbb{E} \left[\log_{2} \frac{\overline{Q}^{M} p(\overline{\mathbf{Y}} | \{\overline{q}_{\tau}\}_{\tau=1}^{M})}{\sum_{\overline{q}_{1}'=1}^{\overline{Q}} p(\overline{\mathbf{Y}} | \{\overline{q}_{\tau}\}_{\tau=1}^{M})}} \right],$$
(36)

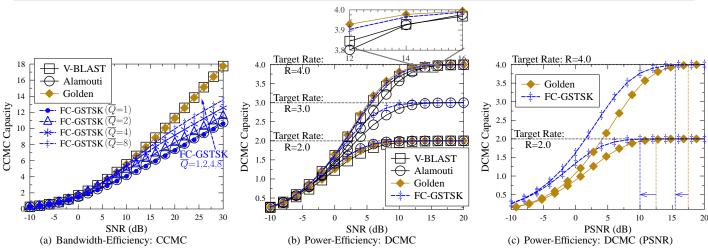


Fig. 5: CCMC and DCMC capacity comparison between V-BLAST, Alamouti's STBC, Golden code and FC-GSTSK associated with M = 2 and N = 2. The parameters for FC-GSTSK are given by Table VI in Sec. V.

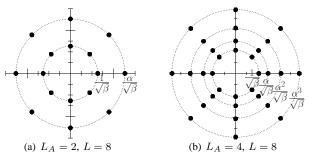


Fig. 6: Constellation diagrams for star QAM associated with $L_A = \{2, 4\}$ ASK-amplitudes and $L = \{8, 16\}$ PSK-phases.

Sec. IV-A. Secondly, the DR arrangement for higher number of TAs is conceived in Sec. IV-B. Lastly, the reduced-RF version of FC-GSTSK is proposed in Sec. IV-C.

A. Amplitude Shift Keying (ASK)

As shown in Sec. III-A, the FC-GSTSK does not increase the signal transmission PAPR. Specifically, when the square and star QAM are used for the modulated symbols in s_{τ} of (18), the constellation of the FC-GSTSK's transmitted signals in **S** of (18) is always limited to star QAM. Therefore, in this section, we explicitly conceive the design guidelines for using SE-ASK and ME-ASK for star QAM signalling, where the ASK-amplitudes are modulated independently of the phase matrix, so that the notations of Sec. III remain the same.

For the SE-ASK design, in contrast to the single-RF schemes [20], [21], [56], [57] that invoke a single ASK for the whole signal matrix, the FC-GSTSK modulates a L_A -level ASK symbol γ_{τ} for each layer as:

$$\mathbf{S} = \frac{1}{\sqrt{M}} \sum_{\tau=1}^{M} \phi_r^{\tau-1} \gamma_\tau \operatorname{diag}(\mathbf{G}_A \mathbf{s}_\tau) \mathbf{G}_r^{\tau-1},$$
(38)

TABLE IV: Parameters (\overline{Q} , L, L_{DM} , L_r , **u**) of FC-GSTSK (PSK) and parameters (\overline{Q} , L, L_{DM} , L_r , **u**, L_A , α) of FC-GSTSK (PSK,SE-/ME-ASK) used in Fig. 7.

R = 6.0	PSK:(4, 16, 64, 54, [7, 57]) SE-ASK:(4, 8, 97, 82, [5, 80], 2, 2.0) ME-ASK:(4, 4, 10, 14, [1, 9], 2, 2.0)
R = 8.0	PSK:(16, 16, 256, 7, [1, 161]) SE-ASK:(4, 16, 64, 15, [1, 49], 4, 1.4) ME-ASK:(4, 16, 64, 23, [1, 15], 2, 2.0)

where we have $\{\{\gamma_{\tau} = \frac{\alpha^{a_{\tau}}}{\sqrt{\beta}}\}_{a_{\tau}=1}^{L_{A}}\}_{\tau=1}^{M}$, while α and $\beta = \frac{\sum_{\mu=0}^{L_{A}-1} \alpha^{2\mu}}{L_{A}}$ respectively represent the ring ratio and the as-

 $E_{A} = 0$ respectively represent the ring ratio and the associated normalization factor that ensures $[E(\gamma_{\tau}^2) = 1]$. The resultant star QAM constellations are exemplied in Fig. 7. We note that the advantageous choices of ring ratios in Rayleigh fading scenarios are $\alpha = 2.0$ for $L_A = 2$ and $\alpha = 1.4$ for $L_A = 4$ [78]–[81]. In summary, the overall throughput is improved to $[R = \log_2 \overline{Q} + \log_2 L + \log_2 L_A]$.

As a further advance, the ME-ASK design [21], [56], [57] is revised to modulate a total of M different ASK symbols in each FC-GSTSK layer as:

$$\mathbf{S} = \frac{1}{\sqrt{M}} \sum_{\tau=1}^{M} \phi_r^{\tau-1} \mathbf{\Lambda}_{\tau} \operatorname{diag}(\mathbf{G}_A \mathbf{s}_{\tau}) \mathbf{G}_r^{\tau-1}, \qquad (39)$$

where we have $\Lambda_{\tau} = \text{diag}([\gamma_{\tau,1}, \cdots, \gamma_{\tau,M}])$. The further improved throughput is given by $[R = \log_2 \overline{Q} + \log_2 L + M \log_2 L_A]$. The ME-ASK design no longer retains the full diversity. For example, the two signal matrices \mathbf{S}^i and $\mathbf{S}^{i'}$ of (39) associated with a single different data-carrying ASKamplitude $(\gamma_{1,1} \neq \gamma'_{1,1})$ but the same remaining source bits have rank-1 Δ for the PEP of (25). However, \mathbf{G}_A and ϕ_r optimized from Table II for the phase matrices still offer a performance advantage for FC-GSTSK(PSK,ME-ASK) over V-BLAST, as evidenced by Fig. 7. This is due to the fact that

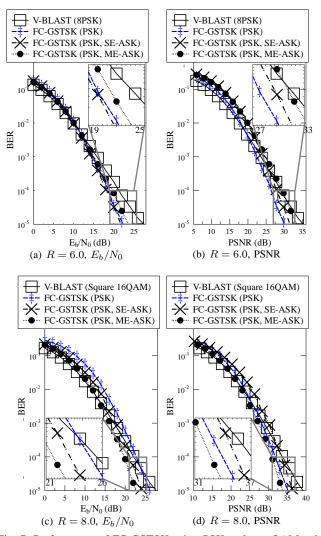


Fig. 7: Performance of FC-GSTSK using PSK and star QAM, when we have M = T = 2 and N = 2. The FC-GSTSK parameters are summarized in Table IV.

at high throughputs, the maximized diversity gain for a subset of signal matrices is sufficient to ensure a good performance.

Figs. 7(a) and 7(b) also showcase a tradeoff between bandwidth-efficiency and energy-efficiency, where the FC-GSTSK(PSK,SE-ASK) using the star QAM signaling performs better than FC-GSTSK(PSK) in Fig. 7(a) owing to the improved bandwidth-efficiency of star QAM, but this trend is reversed in Fig. 7(b) owing to the increased PAPR of star QAM. Nonetheless, at a higher R = 8.0, FC-GSTSK(PSK,ME-ASK) is capable of outperforming both FC-GSTSK(PSK) and FC-GSTSK(PSK,SE-ASK) with respect to both E_b/N_0 in Fig. 7(c) and PSNR in Fig. 7(d).

B. Diversity-Rate (DR) Tradeoff

The DR arrangement in [21], [62], [63] was originally conceived for the square-shaped signal matrix. In this work, however, we opt for using the rectangular-shaped signal matrix setup of (T < M), so that the signal construction for large Mis based on the smaller $(T \times T)$ constituent matrices. More explicitly, for an integer of (V = M/T), the DR arrangement models the $(T \times M)$ FC-GSTSK signal matrix as:

$$\mathbf{S} = \sqrt{\frac{T}{M}} [\widetilde{\mathbf{S}}_1 \ \widetilde{\mathbf{S}}_2 \ \cdots \ \widetilde{\mathbf{S}}_V], \tag{40}$$

2×2	2×2	
FC-GSTSK	FC-GSTSK	
sub-block 1	sub-block 2	
2×4 FC–GSTSK DR		

Fig. 8: Example of FC-GSTSK using the DR arrangement, when we have (M = 4), (T = 2) and (V = M/T = 2).

where the $(T \times T)$ constituent matrices $\{\widetilde{\mathbf{S}}_v = \sum_{\tau=1}^{T} s^{l_{\tau}} \widetilde{\mathbf{A}}_{\tau, \overline{q}_{\tau}} \}_{v=1}^{V}$ are all constructed by (18). The example of using (M = 4), (T = 2) and (V = M/T = 2) is portrayed in Fig. 8. Furthermore, the LDC form of (40) is expressed as:

$$\mathbf{S} = \sum_{v=1}^{V} \sum_{\tau=1}^{T} \sum_{\overline{q}=1}^{\overline{Q}} s_{v,\tau,\overline{q}} \mathbf{A}_{v,\tau,\overline{q}} = \sum_{q=1}^{Q} \overline{s}_{q} \overline{\mathbf{A}}_{q}, \qquad (41)$$

where a total of VT symbols are modulated by the V number of $(T \times T)$ constituent FC-GSTSK:

$$\overline{s}_q = s_{v,\tau,\overline{q}} = \begin{cases} s^{l_{v,\tau}}, & \text{for } \overline{q} = \overline{q}_{\tau} \\ 0, & \text{for all the other } \overline{q} \end{cases},$$
(42)

while the dispersion matrix is given by:

The relationship between indices is given by $[q = \overline{q} + (\tau - 1)\overline{Q} + (v - 1)\overline{Q}T]$. The total number of dispersion matrices in (41) is given by $(Q = VT\overline{Q})$. As a result, for the equivalent LDC received signal of (13), the $(1 \times Q)$ -element vector \overline{S} is now given by (44). In summary, the transmit diversity order of the DR design is given by the reduced value of $[\min(M, T) = T = M/V]$, but the throughput is increased to $[R = V(\log_2 \overline{Q} + \log L)]$.

C. Reduced-RF Transmission

The reduced-RF FC-GSTSK arrangement may be devised based on **Remark 2** of Sec. III-A, which retains the full transmit diversity order of M = T. However, considering that the parameter optimization in Sec. III-C becomes increasingly challenging for a high M at a higher R, we opt for invoking the alternative design of [51], where a total of $M_A = 2$ out of M TAs are activated for transmitting the (2×2) full-RF FC-GSTSK signal matrix over T = 2 time slots. The resultant throughput is given by $[R = \lfloor \log_2 \begin{pmatrix} M \\ M_A \end{pmatrix} \rfloor + \log_2 \overline{Q} + \log_2 L]$. Specifically, the signal matrices for M = 4 are given by [51]:

$$\mathbf{S} = \left\{ \begin{array}{ccccc} \begin{bmatrix} \widetilde{s}_{11} & \widetilde{s}_{12} & 0 & 0\\ \widetilde{s}_{21} & \widetilde{s}_{22} & 0 & 0\\ 0 & \widetilde{s}_{11} & \widetilde{s}_{12} & 0\\ 0 & \widetilde{s}_{21} & \widetilde{s}_{22} & 0 \end{bmatrix} e^{j\theta}, \begin{array}{c} \begin{bmatrix} 0 & 0 & \widetilde{s}_{11} & \widetilde{s}_{12}\\ 0 & 0 & \widetilde{s}_{21} & \widetilde{s}_{22}\\ 0 & \widetilde{s}_{11} & 0 & \widetilde{s}_{12}\\ 0 & \widetilde{s}_{21} & 0 & \widetilde{s}_{22} \end{bmatrix} e^{j\theta} \end{array} \right\}, \quad (45)$$

where $\{\{\widetilde{s}_{ab}\}_{a=1}^{2}\}_{b=1}^{2}$ are signals taken from the (2×2) full-RF FC-GSTSK signal matrix \widetilde{S} constructed by (18), while the extra phase θ is used for maximizing the $(M_A = 2)$ -order diversity gain of (6).

V. PERFORMANCE RESULTS

Firstly, the diversity product Λ_p and diversity sum Λ_s results of (27) as well as the energy-efficiency metrics of PAPR and IAI are summarized in Sec. V-A. Secondly, our results recorded for M = 2 TAs are presented in Sec. V-B, where the proposed FC-GSTSK is compared to the best-performing

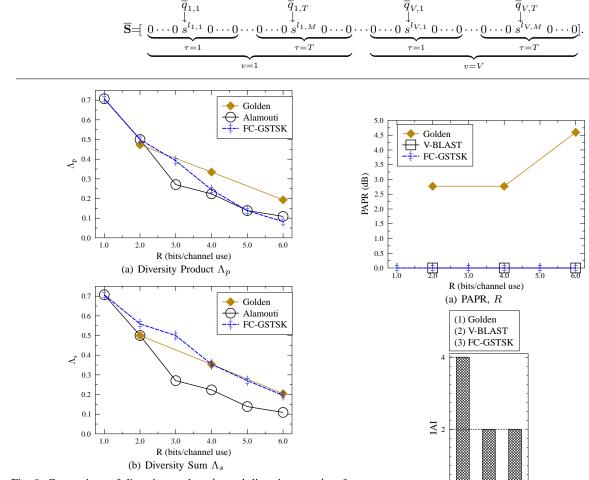


Fig. 9: Comparison of diversity product Λ_p and diversity sum Λ_s of (27), when we have (M=T=2) and $(1 \le R \le 6)$. The FC-GSTSK parameters are summarized in Table V.

TABLE V: Parameters $(\overline{Q}, L, L_{DM}, L_r, \mathbf{u})$ of FC-GSTSK (PSK) used in Fig. 9.

Fig. 9(a) $R = 1.0$: $(1, 2, 2, 4, [1, 1])$	Fig. 9(a) $R = 2.0$: $(2, 2, 4, 4, [1, 3])$
Fig. 9(a) $R = 3.0$: $(4, 2, 8, 14, [1, 3])$	Fig. 9(a) $R = 4.0$: $(8, 2, 16, 14, [1, 7])$
Fig. 9(a) $R = 5.0:(16, 2, 32, 3, [1, 15])$	Fig. 9(a) $R = 6.0$: (8, 8, 64, 19, [3, 61])
Fig. 9(b) $R = 1.0$: $(1, 2, 2, 4, [1, 1])$	Fig. 9(b) $R = 2.0$: $(4, 1, 5, 8, [1, 2])$
Fig. 9(b) $R = 3.0$: $(2, 4, 16, 8, [1, 9])$	Fig. 9(b) $R = 4.0$: $(8, 2, 18, 22, [1, 11])$
Fig. 9(b) $R = 5.0$: $(4, 8, 32, 7, [1, 9])$	Fig. 9(b) $R = 6.0$: $(16, 4, 68, 45, [1, 9])$

full-RF-based MIMO schemes. Thirdly, the performance advantages of FC-GSTSK are shown to be even more substantial for the increased number of $M = \{3, 4\}$ TAs in Sec. V-B. Finally, our results of the channel coded schemes are offered in Sec. V-D. We note that since the most up-to-date 5G standard releases [82] currently support a maximum of four and eight transmission layers for the uplink and downlink scenarios, respectively, we opt for using up to M = 4 TAs and up to N = 8 RAs in this section.

A. Characteristic Results

As a full-diversity scheme, the proposed FC-GSTSK is compared to both the Golden code and to Alamouti's G2 STBC in terms of its diversity product Λ_p and diversity sum Λ_s of (27) in Fig. 9, where the associated FC-GSTSK parameters are summarized in Table V. On one hand, Fig. 9(a) demonstrates that the diversity product Λ_p of FC-GSTSK becomes similar to Alamouti's G2 STBC as the throughput R increases, while the Golden code achieves a higher Λ_p . On

(c) IAI, M = 2 (d) IAI, M = 4Fig. 10: Comparison of the PAPR for signal transmission and the equivalent IAI for signal detection, when we have (M=T=2) and $(1 \le R \le 6)$.

(2) (3)

(1)

the other hand, Fig. 9(b) further evidences that the FC-GSTSK is capable of attaining superior diversity sums Λ_s , which are comparable to that of the Golden code at high throughputs. As discussed in Sec. III-C, the characteristics of Fig. 9 indicate that the FC-GSTSK may substantially outperform Alamouti's G2 STBC as N increases.

As a high-rate scheme, the proposed FC-GSTSK exhibits the same level of transmission PAPR and IAI as V-BLAST, as demonstrated by Fig. 10. By contrast, despite their outstanding diversity gains, the perfect STBCs including the Golden code experience substantially increased transmission PAPR in Figs. 10(a) and 10(b). Moreover, the equivalent IAI = M^2 of perfect STBC is also shown to be a substantial extra price to pay compared to V-BLAST in Figs. 10(c) and 10(d).

B. Performance Results for Two Transmit Antennas

In Fig. 11, the BER performance versus the normalized average E_b/N_0 of FC-GSTSK is compared to the best performing MIMO schemes associated with M = 2 TAs at throughputs of $(2 \le R \le 5)$. First of all, owing to the higher diversity sum Λ_s seen in Fig. 9(b), FC-GSTSK starts to outperform Alamouti's G2 STBC as N increases for the

(44)

Perfect STBC(L=2)

V-BLAST(L=2)

Μ

(1) Perfect STBC

(2) V-BLAST

(3) FC-GSTSK

(1) (2)

(3)

(b) PAPR, M

FC-GSTSK(L=2)

PAPR (dB)

16

P

4

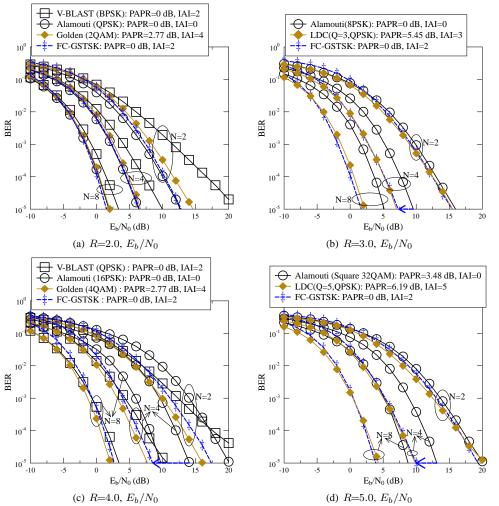


Fig. 11: BER comparison (with respect to E_b/N_0) between the proposed FC-GSTSK, V-BLAST, Alamouti's G2 STBC [37], LDC [55], [74], [75], Golden code [36], when we have (M=T=2) and $(N=\{2,4,8\})$. The FC-GSTSK parameters are summarized in Table VI.

TABLE VI: Parameters $(\overline{Q}, L, L_{DM}, L_r, \mathbf{u})$ of FC-GSTSK (PSK) and parameters $(\overline{Q}, L, L_{DM}, L_r, \mathbf{u}, L_A, \alpha)$ of FC-GSTSK (PSK,ME-ASK) used in Figs. 11 and 12.

	N = 2	N = 4	N = 8
R = 2.0	PSK:(2,2,4,4,[1,3])	PSK:(1,4,4,8,[1,1])	PSK:(4,1,5,8,[1,2])
R = 3.0	PSK:(4,2,8,14,[1,3])	PSK:(2,4,16,8,[1,9])	PSK:(2,4,16,8,[1,9])
R = 4.0	PSK:(2,8,27,13,[1,19])	PSK:(8,2,18,22,[1,11])	PSK:(8,2,18,22,[1,11])
R = 5.0	PSK:(4,8,32,29,[1,15])	PSK:(4,8,32,7,[1,9])	PSK:(4,8,32,7,[1,9])
R = 6.0	PSK:(4,16,64,54,[7,57])	PSK:(16,4,64,91,[1,45])	PSK:(16,4,68,45,[1,9])
R = 8.0	ME-ASK:(4,16,64,23,[1,15],2,2.0)	ME-ASK:(16,4,64,49,[1,37],2,2.0)	ME-ASK:(16,4,64,49,[1,37],2,2.0)

case of R = 2.0 in Fig. 11(a). More notably, Figs. 11(b)-11(d) further evidence that FC-GSTSK massively outperforms Alamouti's G2 STBC for using $(N = \{2, 4, 8\})$ at (R = $\{3.0, 4.0, 5.0\}$), as marked for N = 4 in Figs. 11(b)-11(d). Secondly, observe in Figs. 11(a) and 11(c) that owing to the beneficial diversity gain, FC-GSTSK also exhibits a distinct performance improvement over V-BLAST for $(N = \{2, 4, 8\})$ at $(R = \{2.0, 4.0\})$. However, the Golden code begins to excel in terms of its diversity gains in Fig. 11(c) as the throughput increases to (R = 4.0). Thirdly, Fig. 11(b) and 11(d) further demonstrate that FC-GSTSK associated with its perfect 0 dB PAPR is capable of achieving a comparable performance to that of the LDCs [55], [74], [75] using arbitrary signals. This verifies our energy-efficient FC-GSTSK signal construction, which achieves optimum performance without relying on arbitrary constellations.

In order to take into account the practical power consump-

tion, the BER comparison (with respect to PSNR) between the proposed FC-GSTSK and the best-performing Golden code is further portrayed in Fig. 12. As expected, owing to its beneficial low-PAPR design, the proposed FC-GSTSK unequivocally outperforms the Golden code with respect to its PSNR, as demonstrated by Fig. 12.

C. Performance Results for Three and Four Transmit Antennas

For using $M = \{3, 4\}$ TAs, Figs. 13(a) and 13(b) demonstrate that the FC-GSTSK consistently outperforms both V-BLAST and STBCs. Furthermore, the FC-GSTSK is even capable of outperforming the perfect STBCs for (M = N = 3, R = 3.0) and (M = N = 4, R = 4.0), as evidenced by Figs. 13(a) and 13(b), respectively. We note that owing to its substantially reduced PAPR, the advantage of FC-GSTSK over perfect STBC is further augmented versus the PSNR, which is not portrayed for Fig. 13 due to space limit. In summary,

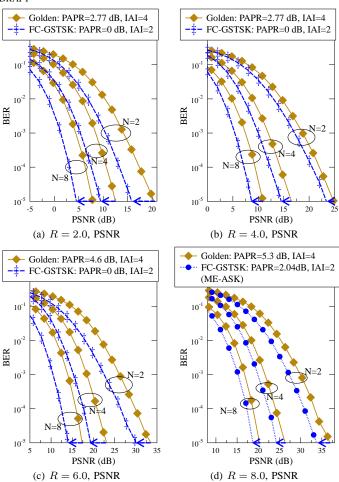


Fig. 12: BER comparison (with respect to PSNR) between the proposed FC-GSTSK and Golden code [36], when we have (M=T=2), $(N = \{2, 4, 8\})$. The FC-GSTSK parameters are summarized in Table VI.

the impressive performance of FC-GSTSK is attributed to the diversity gain maximization proposed in Sec. III-C.

Moreover, for the case of M = N = 4 at high throughputs of $R = \{6.0, 8.0\}$, the DR arrangement of FC-GSTSK proposed in Sec. IV-B constructs the signal matrix for M = 4based on two constituent (2×2) FC-GSTSK signal matrices, which is shown to outperform both STBCs and V-BLAST in Figs. 13(c) and 13(d), respectively.

As a further advance, Fig. 14 demonstrates that when a reduced number of $(M_A = 2)$ out of (M = 4) TAs are activated, the reduced-RF version of FC-GSTSK devised in Sec. IV-C also achieves an improved performance compared to its conventional counterparts of GSM [9] and STBC-SM [51] over a wide-range of throughputs of $(R = \{4.0, 5.0, 6.0, 7.0\})$.

D. Performance Results for Channel Coded Systems

The Serially Concatenated Code (SCC) constituted by BCC and MIMO is portrayed in Fig. 15, where the iterative demapping and decoding is invoked at the two-stage turbo receiver. More explicitly, the source bits are passed through the BCC encoder and a interleaver before MIMO mapping at the SCC transmitter. At the turbo receiver, both the MIMO demodulator and BCC decoder accept and produce soft-bit decisions in the form of Log Likelihood Ratios (LLRs). The extrinsic LLRs $L_{M,e}$ produced by the MIMO demodulator are de-interleaved

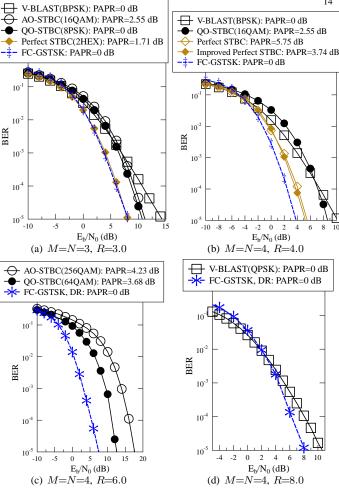


Fig. 13: BER comparison (with respect to E_b/N_0) between the proposed FC-GSTSK, V-BLAST, AO-STBC [39], QO-STBC [42], perfect STBC [32], [33] and the improved perfect STBC [34]. The parameters $(\overline{Q}, L, L_{DM}, L_r, \mathbf{u})$ of FC-GSTSK (PSK) associated with $(M = N = T = \{3, 4\})$ and $(R = \{3.0, 4.0\})$ in (a) and (b) are given by (2, 4, 18, 16, [1, 7, 13]) and (4, 4, 16, 27, [1, 5, 9, 13]), respectively. The parameters $(\overline{Q}, L, L_{DM}, L_r, \mathbf{u})$ of FC-GSTSK, DR (PSK) associated with (M = N = T = 4), (T = 2, V = 2) and $(R = \{6.0, 8.0\})$ in (c) and (d) are given by (2, 4, 16, 8, [1, 9]) and (8, 2, 18, 22, [1, 11]), respectively.

and fed into the BCC encoder as the *a priori* LLRs $L_{D,a}$. Hence the *extrinsic* mutual information $\mathcal{I}_{M_E} = I(L_{M,e}; b_m)$ at the output of the MIMO demodulator becomes equal to the *a priori* mutual information $\mathcal{I}_{D_A} = I(L_{D,a}; b_c)$ at the input of the BCC decoder. Symmetrically, the extrinsic LLRs $L_{D,e}$ produced by the BCC decoder are interleaved and fed into the MIMO demodulator as the *a priori* LLRs $L_{M,a}$, which indicates that $\mathcal{I}_{D_E} = I(L_{D,e}; b_c)$ becomes equal to $\mathcal{I}_{M_A} = I(L_{M,a}; b_m)$ as seen in Fig. 15. The idealistic error-free detection may become achievable, when the full $\mathcal{I}_{D_E} = 1.0$ is recovered by the BCC decoder.

According to the IEEE 802.11a/n/ac/ah standard family, the BCC scheme invoked in this work is specified by the generator polynomials of $g_0 = 133_8$ and $g_1 = 171_8$ as well as the constrain length of K = 7. The coding frame length is set to 10 000 bits. The BCC rate is adjustable by puncturing, and we use $R_c = \{1/2, 3/4, 5/6\}$. In order to avoid ambiguity, the MIMO throughput is still represented by R, hence the overall coded system throughput is now given by $R_c R$. Moreover, without having to access the source bits at the transmitter, the turbo receiver may evaluate the mutual information in an

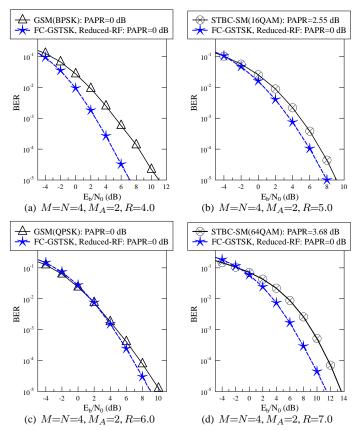


Fig. 14: BER comparison (with respect to E_b/N_0) between the proposed FC-GSTSK, the reduced-RF GSM [9] and STBC-SM [51]. The parameters ($\overline{Q}, L, L_{DM}, L_r, \mathbf{u}, \theta$) of reduced-RF FC-GSTSK (PSK) associated with (M=N=4), ($M_A=T=2$) and ($4.0 \le R \le 7.0$) used in Figs. 14(a)-(d) are given by (2, 4, 16, 8, [1, 9], 1.04 rad), (2, 8, 27, 13, [1, 19], 1.18 rad), (8, 4, 32, 51, [1, 25], 0.18 rad) and (16, 4, 68, 45, [1, 9], 0.1 rad), respectively

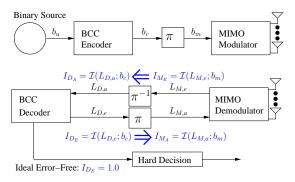


Fig. 15: Schematic of BCC coded MIMO scheme and its two-stage turbo decoder.

"on-line" fashion [52]-[55] as:

$$\mathcal{I}(L;b) = 1 + E\left[\frac{e^L}{1 + e^L}\log_2\left(\frac{e^L}{1 + e^L}\right) + \frac{1}{1 + e^L}\log_2\left(\frac{1}{1 + e^L}\right)\right],$$
(46)

so that the iterations may be terminated when no more information can be gleaned. In this work, we configure the maximum number of iterations between MIMO demapper and BCC decoder to a small number of 4.

The convergence behaviour of the turbo receiver is visualized by the EXIT charts in Fig. 16. Notably, Fig. 16(a) evidences that compared to the conventional MIMO schemes of V-BLAST, STBC and Golden code, the proposed FC-

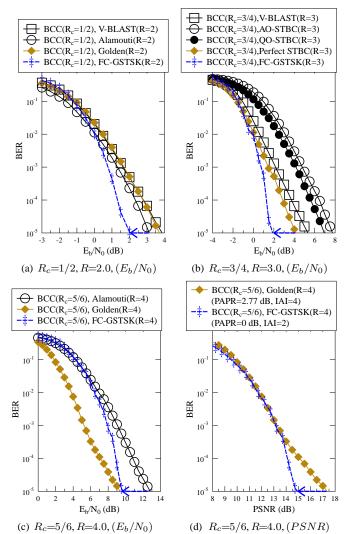


Fig. 17: BER comparison (with respect to E_b/N_0 and PSNR) between the proposed FC-GSTSK, V-BLAST, Alamouti's G2 STBC [37], AO-STBC [39], QO-STBC [42], Golden code [36] and perfect STBC [32], [33] in BCC coded systems. The parameters $(M, N, T, \overline{Q}, L, L_{DM}, L_r, \mathbf{u})$ of FC-GSTSK associated with $R = \{2.0, 3.0, 4.0\}$ are given by (2, 2, 2, 2, 2, 4, 4, [1, 3]), (3, 3, 3, 2, 4, 18, 16, [1, 7, 13]) and (2, 2, 2, 4, 4, 32, 32, [1, 19]), respectively

GSTSK exhibits an enhanced iteration gain. This is due to the fact that instead of only mapping to the Gray coded PSK/QAM symbols, the FC-GSTSK maps the source bits to both the modulated symbol index and the dispersion matrix IM index, which offers additional degree of freedom. As a result, Fig. 16(b) demonstrates that the ideal error-free condition of $\mathcal{I}_{D_E} = 1.0$ is achieved by the BCC FC-GSTSK scheme at $E_b/N_0 = 0$ dB, but its counterpart of Golden code can only obtain a lower $\mathcal{I}_{D_E} = 0.98$, as shown in Fig. 16(c).

The EXIT charts analysis of Fig. 16 is further confirmed by the BER results of Fig. 17. First of all, Figs. 17(a) and 17(b) once again demonstrate that the proposed FC-GSTSK is capable of unequivocally outperforming the MIMO schemes of V-BLAST, Alamouti's G2 STBC, AO-STBC, QO-STBC, Golden code and perfect STBC in BCC coded systems. Secondly, although Goden code associated with the excessive IAI = M^2 appears to perform the best at a higher throughput seen in Fig. 17(c), the substantially increased PAPR of Golden



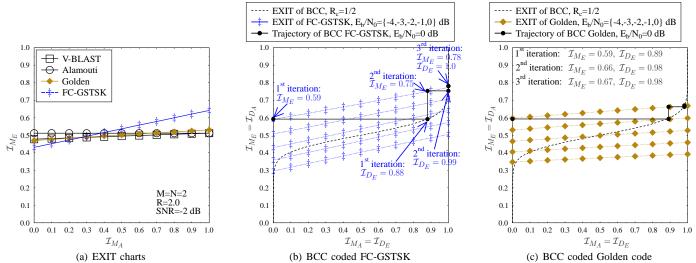


Fig. 16: EXIT charts of the MIMO schemes (M = N = 2, R = 2.0) and decoding trajectories of BCC coded FC-GSTSK and Golden code. The parameters are the same as those in Fig. 11(a).

code results in the evidently inferior performance compared to the proposed FC-GSTSK, when the PSNR takes into account the practical power consumption as shown in Fig. 17(d).

VI. CONCLUSIONS

In this work, we have proposed a new FC-GSTSK scheme. It is unprecedented in the two decades of full-diversity highrate MIMO system design that as the FC-GSTSK outperforms both V-BLAST and STBC, the PAPR of signal transmission and the equivalent IAI of signal detection are reduced to the same level as that of V-BLAST. Moreover, the reduced-RF version of FC-GSTSK also outperforms GSM and STBC-SM without increasing the PAPR and the equivalent IAI. Owing to their explicit advantages in terms of energy-efficiency, bandwidth-efficiency and power-efficiency, the proposed FC-GSTSK constitutes an attractive candidate for future wireless MIMO systems.

VII. DEDICATION

Chao Xu would like to dedicate this paper to the fond memory of Sirui Hu (1985 - 2019), who was an outstanding scientist and an inspiration in the conception of this work.

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