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The Endofullerene HF@C₆₀: Inelastic Neutron Scattering Spectra from Quantum Simulations and Experiment, Validity of the Selection Rule and Symmetry Breaking

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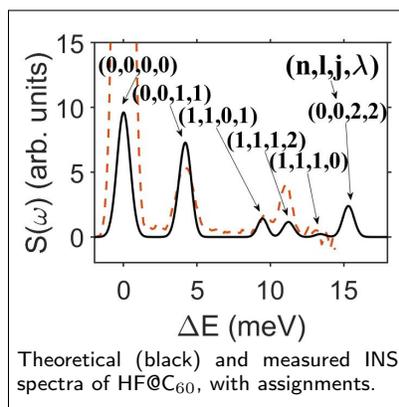
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Abstract

Accurate quantum simulations of the low-temperature inelastic neutron scattering (INS) spectra of HF@C₆₀ are reported, for two incident neutron wavelengths. They are distinguished by the rigorous inclusion of symmetry-breaking effects in the treatment, and having the spectra computed with HF as the guest, rather than H₂ or HD, as in the past work. The results demonstrate that the precedent-setting INS selection rule, originally derived for H₂ and HD in near-spherical nanocavities, applies also to HF@C₆₀, despite the large mass asymmetry of HF and the strongly mixed character of its translation-rotation eigenstates. This lends crucial support to the theoretical prediction [Xu, M.; et al. *J. Phys. Chem. Lett.* **2015**, 6, 3721] that the INS selection rule is valid for any diatomic molecule in near-spherical nanoconfinement. The selection rule remains valid in the presence of symmetry breaking, but is modified slightly in an interesting way. Comparison is made with the recently published experimental INS spectrum of HF@C₆₀. The agreement is very good, apart from one peak for which our calculations suggest a reassignment. This reassignment is consistent with the measured INS spectrum presented in this work, that covers an extended energy range.

Graphical TOC Entry



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3 Light-molecule endofullerenes have molecules such as H_2 , H_2O , HF , and CH_4 , character-
4 ized by small masses and large rotational constants, encapsulated inside the cages of C_{60} , C_{70}
5 and other fullerenes.^{1,2} Their synthesis has been accomplished utilizing the approach known
6 as molecular surgery, in which a hole is created in the fullerene cage through a sequence of
7 chemical reactions allowing the insertion of the guest molecule into the cavity, followed by
8 reforming the pristine fullerene shell with the guest molecule trapped in its interior.³⁻⁶ Inside
9 C_{60} , the entrapped molecules are under the conditions unlike any other studied previously -
10 confined in the highly symmetric and nonpolar nanoscale cage and, in the case of HF and
11 H_2O , isolated and unable to form hydrogen bonds to other molecules.

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21 Another distinguishing feature of light-molecule endofullerenes, one that has motivated
22 a large number of experimental and theoretical studies, is the dominance of quantum effects
23 in the dynamics and spectroscopy of the guest molecules.^{1,2,7} These species exemplify many
24 of the fundamental, textbook principles of quantum mechanics to the degree and with the
25 clarity that are unmatched among molecular systems amenable to experimental investiga-
26 tions. One source of quantum effects is the quantization of the translational center-of-mass
27 (c.m.) degrees of freedom (DOFs) of the encapsulated molecules (particle-in-a-box effect).
28 Tight confinement gives rise to translational eigenstates whose energy differences are large
29 relative to kT (k being the Boltzmann constant). The same holds for the quantized rotational
30 states of the light molecules. The quantized translational and rotational DOFs of the guest
31 molecule are coupled by the confining potential of the fullerene interior, resulting in a sparse
32 and intricate translation-rotation (TR) energy level structure.^{1,7}

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45 The endofullerene $\text{HF}@C_{60}$, where the fullerene cage is occupied by a single dipolar
46 HF molecule, is of considerable interest to experimentalists and theorists alike. Among its
47 attractions is the opportunity that electric-dipole-coupled arrays of close-packed $\text{HF}@C_{60}$
48 moieties provide for investigating the many-body correlations between the highly quantum
49 molecular dipoles confined in the C_{60} cages, and the possible emergence of dipole-ordered
50 phases and ferroelectricity at low temperatures.⁸ The inelastic neutron scattering (INS)
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3 and far- and mid-infrared (IR) spectra have revealed quantization of the translational and
4 rotational DOFs of the encapsulated HF.⁵ Moreover, both the rotational transitions and the
5 intramolecular stretch fundamental of the caged HF are shifted to lower energies relative to
6 those in the gas phase, evidence for the softening of the HF intramolecular potential caused
7 by the guest-host interaction.⁵ Finally, in the far- and mid-IR spectra of solid HF@C₆₀ at low
8 temperature (5 K),⁵ the rotational $j = 0 \rightarrow 1$ transition is split by 3.9 cm⁻¹, signaling that
9 the symmetry of the environment felt by the guest HF must be lower than I_h , the symmetry
10 of an isolated C₆₀ molecule. Symmetry breaking was previously observed in solid H₂@C₆₀^{9,10}
11 and H₂O@C₆₀¹¹⁻¹³ at low temperatures.

21 These experimental findings have stimulated a number of theoretical studies of the quan-
22 tum TR dynamics and spectroscopy of HF@C₆₀. Quantum-five dimensional (5D) bound-
23 state calculations for the isolated HF@C₆₀ (treating both HF and C₆₀ as rigid)^{14,15} employing
24 the recent *ab initio* 5D PES of the system¹⁴ have revealed that, despite the large mass asym-
25 metry of HF, its TR eigenstates exhibit many of the salient features of the TR level structure
26 of H₂@C₆₀ (apart from spin isomerism), elucidated by theory previously.^{7,16-19} These include
27 the use of (i) the principal and orbital angular momentum quantum numbers n and l , re-
28 spectively, of the 3D isotropic harmonic oscillator (HO) for the translational c.m. excitations
29 of HF, (ii) the quantum number j of a linear rigid rotor for the HF rotational excitations,
30 (iii) and the total angular momentum quantum number λ , arising from the vectorial cou-
31 pling of the orbital angular momentum l associated with the translational motion of HF and
32 the rotational angular momentum j of the molecule. In addition, the recently developed
33 first-principles electrostatic quadrupolar model²⁰ has been shown to account quantitatively
34 for the effects of symmetry breaking on both the $j = 1$ level of HF²⁰ and its excited TR
35 eigenstates¹⁵ (as well as the corresponding TR levels of the caged H₂ and H₂O).

51 Here we present rigorous quantum simulations of the low-temperature INS spectra of
52 HF@C₆₀ for two incident neutron wavelengths, utilizing the methodology developed by Bačić,
53 Xu, and co-workers.^{1,21-23} These calculations are notable for several reasons. For the first
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3 time, they include explicitly the effects of symmetry breaking on the quantum 5D TR eigen-
4 states of the encaged molecule, HF, and hence the INS spectra, since the former constitute
5 the initial and final states of the INS transitions. These simulations are also the first to
6 involve a guest molecule other than H₂ or HD. Therefore, they make it possible to establish
7 whether the first ever (and so far the only) selection rule established in the INS spectroscopy
8 of discrete molecular compounds,²⁴ and validated experimentally for H₂@C₆₀,²⁵ applies to
9 HF@C₆₀ as well, as suggested by the generalized INS selection rule.²⁶ If it does, is it modi-
10 fied in some way by the symmetry breaking? Finally, comparison is made between the INS
11 spectra computed in the present study and the experimental spectrum in the literature,⁵
12 suggesting the reassignment of one peak in the latter. This reassignment is consistent with
13 the measured INS spectrum presented in this work, that covers an extended energy range.
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25 The quantum methodology employed in this study to calculate accurately the INS spectra
26 of HF@C₆₀, with and without the inclusion of symmetry breaking, is outlined in section S1 of
27 the Supporting Information, and presented in full in ref 23. The TR levels and wave functions
28 of HF@C₆₀, that serve as input for the simulations of the INS spectra, were calculated in ref
29 15, using the approach summarized in section S2 of the Supporting Information.
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35 Table 1 shows the intensities of the INS transitions out of the ground TR state of HF@C₆₀
36 to its excited TR levels, for the incident neutron wavelength $\lambda_n = 1.65 \text{ \AA}$ (one of the two
37 wavelengths for which the INS spectra were recorded), calculated in this work for the isolated
38 endofullerene (I_0) and for the dominant P crystal orientation (I_P) of HF@C₆₀(s), respectively.
39 The P and H crystal orientations are defined in section S1 of the Supporting Information.
40 For the H orientation, the calculated symmetry-induced splittings of the TR levels are about
41 a factor of 30 smaller than the corresponding ones in the P orientation.²⁰ Also displayed in
42 Table 1 are select lower-lying TR levels of HF@C₆₀, the final states of the INS transitions
43 considered, computed for the P crystal orientation. For each level, we show its energy (ΔE_P)
44 relative to the TR ground state, its degeneracy (g_P), and the quantum numbers (n, l, j), λ ,
45 and $|m_\lambda|$. Those levels whose parentage derives from the same level of the isolated HF@C₆₀
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3 are grouped together. The energies (ΔE_0) and degeneracies (g_0) of these “parent” levels are
4 given in the first two columns of Table 1. Both sets of TR levels are from ref 15.
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7 The information presented in Table 1 allows us to ascertain if the unexpected INS se-
8 lection rule that we established²⁴ and subsequently generalized,²⁶ is valid for HF@C₆₀. The
9 discovery of this selection rule was very surprising, since it contradicted the view widely held
10 by the INS community that the INS spectroscopy of discrete molecular compounds is not
11 subject to any selection rules.^{27–30}
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17 The selection rule in question, in its original form²⁴ states that for a *para*-H₂ or HD
18 molecule confined in a near-spherical nanocavity, such as that of C₆₀, the INS transitions
19 between its ground TR state and excited TR states assigned as (n, l, j, λ) are *forbidden* for
20 $\lambda = j + l - 1$. A later derivation showed that this selection rule, and its generalized ver-
21 sion, should apply to *any* diatomic molecule, homo- or heteronuclear, inside a near-spherical
22 nanocavity.²⁶ These derivations^{24,26} involve explicit evaluation of the INS transition matrix
23 element, and a physically motivated assumption about the functional form of the radial
24 component of the TR eigenstates. HF@C₆₀ poses an important test of the generality of the
25 selection rule, and a demanding one, given the large mass asymmetry of the molecule, and
26 the fact that, as elaborated below, n, l, j are not nearly as good quantum numbers for HF
27 as they are for H₂.¹⁵ It should be pointed out that the group-theoretical derivation of these
28 selection rules³¹ is strictly applicable only to homonuclear diatomic molecules such as H₂
29 inside a spherical cavity (leaving out even I_h systems like C₆₀), and says nothing about caged
30 heteronuclear diatomics like HF (or HD³²).
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45 In Table 1, the bold-faced transitions are those that for *isolated* HF@C₆₀ should be
46 forbidden according to the above selection rule. Indeed, their intensities (I_0) are *zero* to the
47 number of significant figures shown, implying that these transitions are unobservable in the
48 INS spectra, and thus forbidden for all practical purposes. This provides a computational
49 confirmation of the validity of the INS selection rule for this system, as derived by us.^{24,26}
50 It also attests that the scope of validity of the selection rule is significantly larger than
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3 suggested by the group-theoretical considerations.³¹
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5 Table 1 also shows how the INS selection rule is affected by the symmetry breaking. It
6 is clear that symmetry breaking splits the TR levels of isolated HF@C₆₀ with the quantum
7 number λ , in the ΔE_0 column, into $\lambda+1$ sublevels shown in the ΔE_P column, each associated
8 with one value of $|m_\lambda|$. The same of course happens to the INS transitions to these TR levels.
9 Looking at each of the transitions that for isolated HF@C₆₀ is forbidden, one sees that in
10 the presence of symmetry breaking only the transition to the $|m_\lambda| = 0$ sublevel remains
11 forbidden, with the intensity that is zero to four significant figures. But, the intensities
12 of the transitions to the $|m_\lambda| > 0$ sublevels, while nonzero, are very small, and would be
13 invisible in the INS spectrum as well. The relationship between these predictions and the
14 available experimental spectra is discussed later in the paper.
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25 One important point warrants discussion here. The INS selection rule^{24,26} is expressed
26 in terms of the TR quantum numbers n, l, j and λ , that are assumed to be good quantum
27 numbers. This is certainly the case for H₂^{15,17} (and H₂O¹⁵) in C₆₀. However, as mentioned
28 above, that is *not* true for HF@C₆₀, apart from the quantum number λ .¹⁵ Let us consider two
29 TR eigenstates in Table 1 that are the respective final states of two *forbidden* INS transitions.
30 One of them, (2, 2, 1, 2) at 21.222 meV ($|m_\lambda| = 0$), is 52.1% $|2, 2, 1\rangle + 45.2\%$ $|1, 1, 2\rangle$. Given
31 such strong mixing of two sets of (n, l, j) quantum numbers, why does the INS selection rule
32 apply to this TR eigenstate? The reason is that *both* $|2, 2, 1\rangle$ and $|1, 1, 2\rangle$ *separately* satisfy
33 the selection rule condition $\lambda = j + l - 1$, with $\lambda = 2$. Likewise, the second “forbidden” TR
34 eigenstate (1, 1, 2, 2), at 24.162 meV ($|m_\lambda| = 0$), is strongly mixed as well, 52.8% $|1, 1, 2\rangle +$
35 44.8% $|2, 2, 1\rangle$. But the transition to it (from the ground TR state) is forbidden since $|1, 1, 2\rangle$
36 and $|2, 2, 1\rangle$ *separately* satisfy the condition $\lambda = j + l - 1$, for $\lambda = 2$ [the lowest-energy
37 “forbidden” eigenstate (1, 1, 1, 1), at 13.683 meV in Table 1, happens to be a remarkably
38 pure state, 97% $|1, 1, 1\rangle$].
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53 Precisely the same was established earlier for HD@C₆₀,²⁶ another system whose TR
54 eigenstates have strongly mixed character.¹⁷ Thus, we can now make a general statement
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3 about the reason why the INS selection rule applies to heteronuclear, mass-asymmetric
4 systems such as HF@C₆₀ and HD@C₆₀, whose TR eigenstates are strongly mixed and (n, l, j)
5 are not particularly good quantum numbers. The reason is that *each* basis state having
6 a significant weight in a “forbidden” TR eigenstate *individually* satisfies the selection rule
7 condition $\lambda = j + l - 1$.
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13 Figure 1 shows the INS spectrum of HF@C₆₀ computed for 0 K and the incident neutron
14 wavelength $\lambda_n = 2.22 \text{ \AA}$ and, in Figure 1a, the INS spectrum recorded at 1.6 K using the
15 same incident neutron wavelength.⁵ At these temperatures, the INS transitions, calculated
16 and observed, all originate from the ground TR state of HF, since it is the only one populated.
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Figures 1b and 1c show the stick spectra computed for the P and H crystal orientations, respectively. The theoretical spectrum in Figure 1a is a weighted sum of the P and H stick spectra, computed for a 15% contribution from the H orientation and 85% from the P orientation (corresponding to the measured abundances of the two crystal types under the experimental conditions). It is then convolved with the instrumental resolution function. The transitions are labeled with the quantum numbers (n, l, j, λ) of their final TR states.

The first peak of the calculated INS spectrum in Figure 1a corresponds to a closely spaced pair of rotational transitions to the $|m_\lambda| = 0$ and 1 sublevels resulting from the 1:2 splitting of the $j = 1$ level $(0, 0, 1, 1)$ of HF (visible in Figure 1b). The splitting of 0.461 meV is not resolved in either the calculated (convolved) or measured INS spectrum. The energies of the two transitions, 3.88 and 4.34 meV (Table 1), agree well with the measured peak centered at 4.1 meV, confirming its assignment as the rotational $j = 0 \rightarrow 1$ transition.⁵

The next higher-energy peak in the calculated spectrum arises from the transition to the HF translational fundamental $(1, 1, 0, 1)$, whose $|m_\lambda| = 0$ and 1 sublevels are split by only 0.02 meV.¹⁵ The two (unresolved) transitions at 9.45 and 9.47 meV, respectively, are in good agreement with the peak in the experimental spectrum at 9.75 meV. This peak was tentatively assigned to the fundamental translational transition,⁵ and our calculations support this assignment.

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3 The peak visible at 11 meV in both the computed and measured spectra was assigned by
4 Krachmalnicoff *et al.*⁵ to the $j = 0 \rightarrow j = 2$ rotational transition. However, as can be seen
5 in Table 1, the *only* calculated transitions near this energy are those to the $\lambda = 2$ sublevel
6 of the $n = 1, j = 1$ multiplet $(1, 1, 1, 2)$ (triplet in I_h symmetry), split by the symmetry
7 breaking into three components corresponding to $|m_\lambda| = 0, 1,$ and $2,$ respectively, in the
8 energy range 11.06 - 11.45 meV. These three transitions are visible in the stick spectrum in
9 Figure 1b. The transition to the $\lambda = 0$ sublevel $(1, 1, 1, 0)$ at 13.41 meV has a low intensity,
10 and appears in the calculated spectrum only as a slight bump. Unfortunately, the measured
11 INS spectrum presented in Figure 3a of ref 5 ends abruptly beyond 11 meV, precluding the
12 comparison with the calculated spectrum at higher energies.

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15 If the peak observed, and calculated, around 11 meV arises from transitions to the $n =$
16 $1, j = 1$ multiplet $(1, 1, 1, 2)$, then where is the peak associated with the $j = 0 \rightarrow j = 2$
17 rotational transition? According to the calculations, Table 1 and Figure 1a, the transition
18 to the $j = 2$ rotational level $(0, 0, 2, 2)$ of HF, that is split into three components with
19 $|m_\lambda| = 0, 1,$ and $2,$ respectively (see Figure 1b), appears in the range 15.17 - 15.50 meV. But,
20 as mentioned above, the measured INS spectrum in ref 5 terminates around 11 meV.

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23 Fortunately, the INS spectrum of HF@C₆₀, recorded at 1.6 K but with a shorter incident
24 neutron wavelength $\lambda_n = 1.60 \text{ \AA}$ is available, and is shown in Figure 2. The INS mea-
25 surements were conducted on the IN4C thermal time-of-flight spectrometer located at the
26 Institut Laue Langevin in Grenoble (France). Additional information is available in section
27 S3 of the Supporting Information. This spectrum, extending beyond 11 meV, does exhibit a
28 prominent peak around 16 meV, that agrees well with our calculated transition to the $j = 2$
29 rotational level $(0, 0, 2, 2)$. One may be surprised by the rather high energy of this TR level,
30 given that the $j = 0 \rightarrow 1$ transition is around 4 meV. But as pointed out above, (n, l, j) are
31 not very good quantum numbers for HF@C₆₀. Thus, the TR eigenstate $(0, 0, 2, 2)$ is only
32 62% $|0, 0, 2\rangle$, so its assignment as the $j = 2$ level is not to be taken literally.

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35 The broad asymmetric band with the maximum at 11 meV in Figure 2 covers the energy
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3 range from 8 to 12 meV. Hidden underneath are the peaks around 9.75 and 11 meV that are
4 resolved for $\lambda_n = 2.22 \text{ \AA}$ (Figure 1a). The former is assigned, by experiment and theory, to
5 the transitions to the HF translational fundamental, and the latter (by us in this study) to
6 the $n = 1, j = 1$ multiplet, respectively. The peak around 4 meV matches that recorded for
7 $\lambda_n = 2.22 \text{ \AA}$ (Figure 1a) and has been already assigned to the transitions to the symmetry-
8 split $j = 1$ rotational level of HF.
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15 Figure 3 displays the INS spectrum of HF@C₆₀ computed for 0 K and the incident
16 neutron wavelength $\lambda_n = 1.65 \text{ \AA}$, that can be thought of as the theoretical counterpart
17 to the measured INS spectrum in Figure 2. What this simulated spectrum shows is that
18 beyond 16 meV there are no intense transitions, so that in this energy range the measured
19 INS spectrum should have few, if any, distinctive features.
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25 Can the two experimental INS spectra that are currently available be used to validate
26 the predictions of the INS selection rule presented earlier in the paper? The lowest-energy
27 (bold-faced) transition in Table 1 predicted to be forbidden, to the $|m_\lambda| = 0$ component of
28 the $n = 1, j = 1$ doublet (1, 1, 1, 1), lies at 13.68 meV. This is beyond the range of the INS
29 spectrum measured in ref 5, but not of that in Figure 2. The latter spectrum appears to
30 show a dip, or absence of any features, between 13 and 15 meV, which is consistent with
31 the selection rule. However, a better resolved and less noisy INS spectrum is needed for a
32 definitive experimental confirmation of the validity of the selection rule for HF@C₆₀.
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41 In summary, we have presented rigorous quantum simulations of the low-temperature
42 INS spectra of HF@C₆₀, employing the methodology developed several years ago.²¹⁻²³ They
43 are distinctive in a number of ways. The effects of symmetry breaking^{15,20} are included
44 explicitly for the first time in the calculations of the INS spectra. Also for the first time in
45 the INS calculations for light-molecule endofullerenes,¹ the guest molecule, HF, is not H₂ or
46 one of its isotopologues. This has allowed us to test the prediction²⁶ that the INS selection
47 rule initially derived for H₂ or HD in a near-spherical nanocavity^{24,32} applies to a much
48 broader class of diatomic molecules in such a confinement. HF presents a challenge, owing
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3 to its large mass asymmetry and because n, l, j are not nearly as good quantum numbers as
4 they are for H_2 .¹⁵ Nevertheless, the INS selection rule completely passed the (computational)
5 test, both for the isolated $\text{HF}@C_{60}$, without symmetry breaking, and when the symmetry
6 breaking is taken into account (modifying the selection rule in a particular way). The
7 measured INS spectrum that encompasses the lowest-energy computed forbidden transition
8 is not inconsistent with this band being forbidden. But, an unambiguous verification of the
9 theory requires an experimental INS spectrum of $\text{HF}@C_{60}$ that is better resolved and less
10 noisy. Our calculations agree with the assignments of two out of three peaks visible in the
11 published INS spectrum of $\text{HF}@C_{60}$.⁵ For the third peak measured at 11 meV and assigned
12 to the $j = 0 \rightarrow j = 2$ rotational transition,⁵ we suggest its reassignment to the closely spaced
13 $n = 1, j = 1$ multiplet. The calculations predict that the transitions to the $j = 2$ rotational
14 level, split by symmetry breaking, are in the range 15.17 - 15.50 meV. This is in good
15 agreement with the the INS spectrum of $\text{HF}@C_{60}$ recorded over an extended energy range,
16 in which a peak around 16 meV figures prominently. Evidently, the close interaction between
17 high-level theory and experiment, that has been the hallmark of this field, continues to be
18 stimulating and productive, leading to deeper understanding of these intriguing systems. In
19 particular, the results of this study support the contention made by us previously,²⁶ that
20 the INS selection rule applies to any diatomic molecule in near-spherical confinement. This
21 fundamental topic should be pursued further by experiment and theory.
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Supporting Information Available

The following is available free of charge.

- Overview of (a) the methodology for quantum 5D calculation of the translation-rotation eigenstates of HF@C₆₀ including symmetry breaking, and (b) rigorous quantum treatment of the inelastic neutron scattering spectra of HF@C₆₀, as well as a brief description of the INS measurements.

This material is available free of charge via the Internet at <http://pubs.acs.org/>.

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Table 1: Intensities, in barn (bn), of the INS transitions from the ground TR state of HF@C₆₀, calculated for the isolated endofullerene (I_0) and for the P crystal orientation (I_P), respectively; incident neutron wavelength $\lambda_n = 1.65$ Å. ΔE_0 and ΔE_P (in meV) are the neutron energy transfer (level energy relative to the TR ground state) for the isolated HF@C₆₀ and the P orientation, respectively. g_0 and g_P are the respective degeneracies of these TR levels, while (n, l, j) , λ , and $|m_\lambda|$ are their quantum numbers. The bold-faced transitions are those that for isolated HF@C₆₀ are forbidden according to the selection rule stated in the text.

ΔE_0	g_0	(n, l, j)	λ	I_0 (bn)	ΔE_P	g_P	λ	$ m_\lambda $	I_P (bn)
0.00	1	(0, 0, 0)	0	10.9367	0.00	1	0	0	10.9411
4.178	3	(0, 0, 1)	1	8.0673	3.876	1	1	0	2.8716
					4.337	2	1	1	5.1935
9.466	3	(1, 1, 0)	1	1.5909	9.452	1	1	0	0.5021
					9.475	2	1	1	1.0933
11.253	5	(1, 1, 1)	2	1.8199	11.056	1	2	0	0.3897
					11.150	2	2	1	0.7410
					11.454	2	2	2	0.6695
13.407	1	(1, 1, 1)	0	0.2356	13.412	1	0	0	0.2465
13.514	3	(1, 1, 1)	1	0.0000	13.440	2	1	1	0.0450
					13.683	1	1	0	0.0000
15.319	5	(0, 0, 2)	2	5.0708	15.167	1	2	0	1.0311
					15.251	2	2	1	2.0252
					15.500	2	2	2	1.9709
...	
21.205	5	(2, 2, 1)	2	0.0000	21.207	2	2	2	0.0004
					21.222	1	2	0	0.0000
					21.264	2	2	1	0.0240
...	
24.115	5	(1, 1, 2)	2	0.0000	24.157	2	2	1	0.0093
					24.162	1	2	0	0.0000
					24.170	2	2	2	0.0145

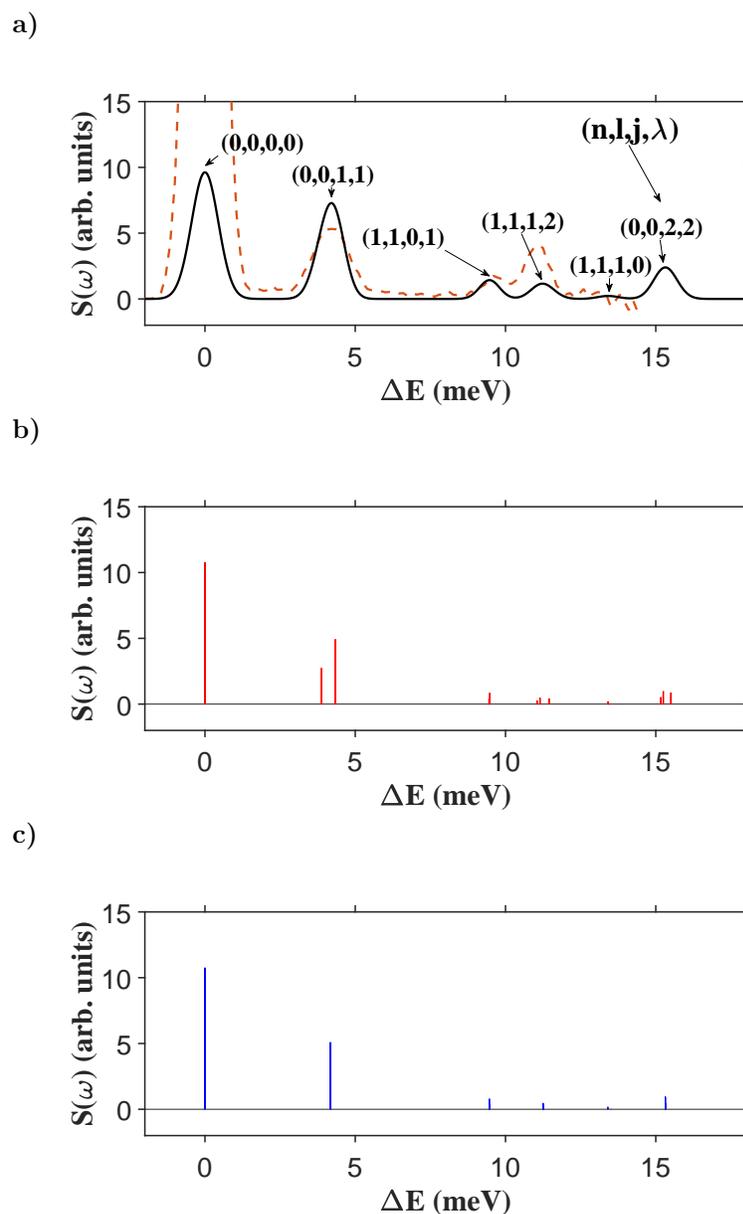


Figure 1: INS spectra of HF@C₆₀(s) computed for 0 K and the incident neutron wavelength $\lambda_n = 2.22 \text{ \AA}$. All transitions originate from the ground TR state of HF. (a) The spectrum computed for a 15% contribution from the H orientation and 85% from the P orientation. The resulting stick spectrum convolved with the instrumental resolution function is depicted with the solid black line. The calculated transitions are labeled with the quantum numbers (n, l, j, λ) of their final TR states. Dashed red line shows the experimental INS spectrum⁵ recorded at 1.6 K and for $\lambda_n = 2.22 \text{ \AA}$. (b) The computed spectrum for the P orientation. (c) The computed spectrum for the H orientation.

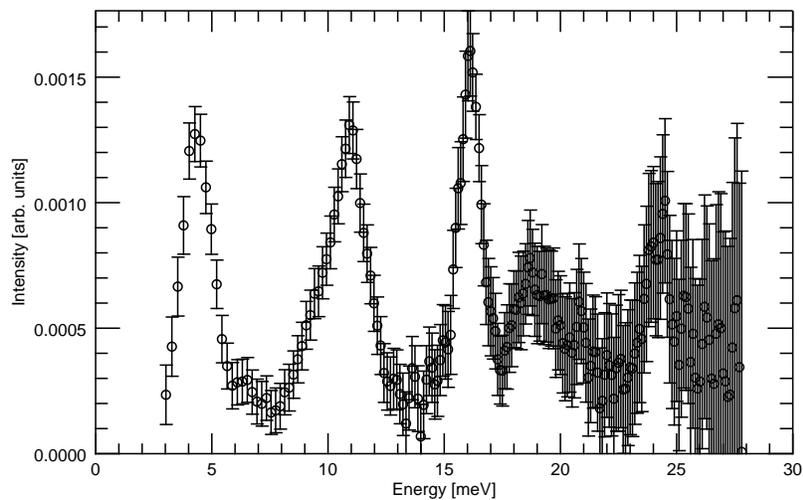


Figure 2: The INS spectrum of HF@C₆₀ recorded at 1.5 K, using the incident neutron wavelength $\lambda_n = 1.60 \text{ \AA}$.

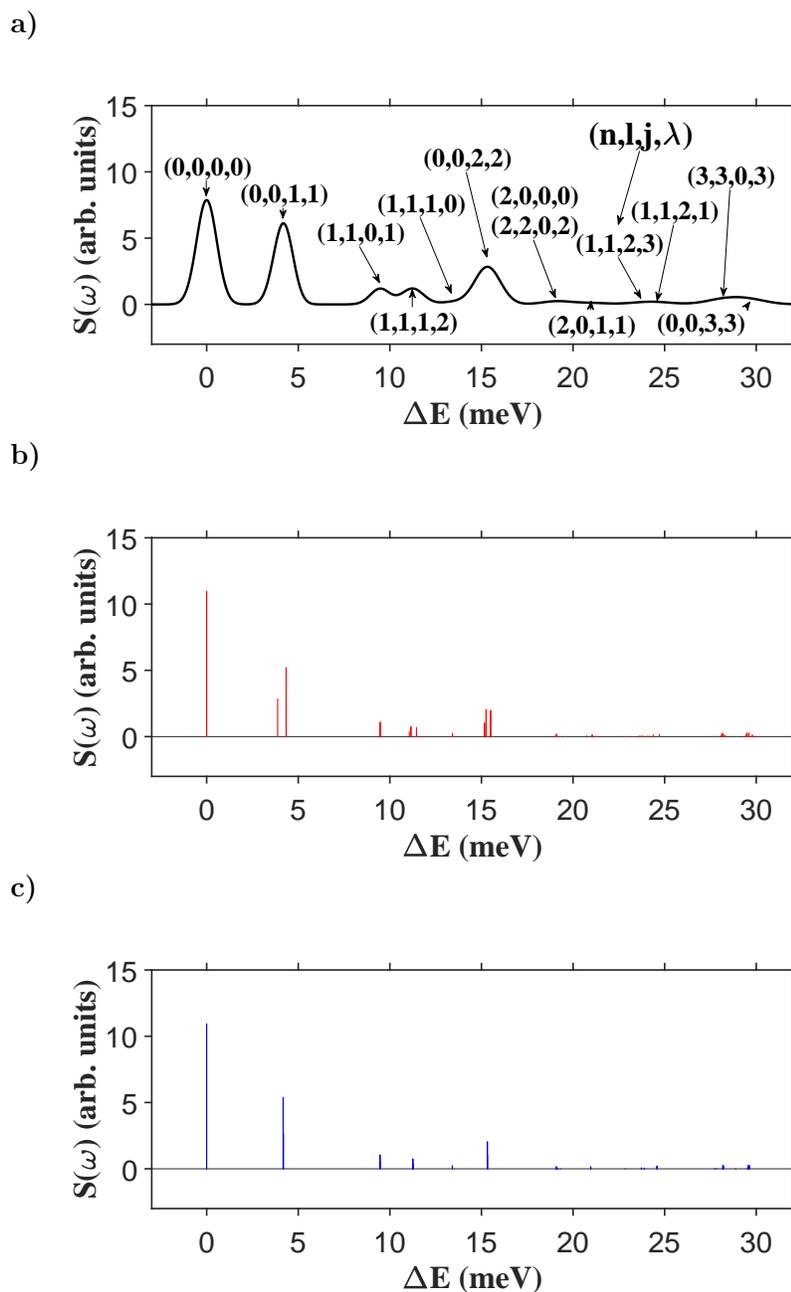


Figure 3: Calculated INS spectra of HF@C₆₀(s), for 0 K and the incident neutron wavelength $\lambda_n = 1.65 \text{ \AA}$. All transitions originate from the ground TR state of HF. (a) The spectrum computed for a 15% contribution from the H orientation and 85% from the P orientation. The resulting stick spectrum convolved with the instrumental resolution function is depicted with the solid black line. (b) The spectrum for the P orientation. (c) The spectrum for the H orientation.