Sediment microstructure and the establishment of gas migration pathways during bubble growth

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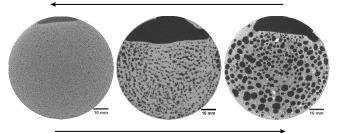
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TOC graphic

Increasing pore throat radii, enhanced bubble connectivity and gas transport



Smaller populations of larger bubbles

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Abstract

Soft sediments exhibit complex and varied deformation behavior during in situ bubble growth, however, the sediment microstructure is often neglected when predicting bubble networking or fracture propagation dynamics. This study considers three chemically similar Mg(OH)₂-rich sediments, which differ slightly in their particle size distributions and morphologies, but exhibit significant differences in their porosity, stiffness and pore throat dimensions at equivalent yield strengths. At low yield strengths, microstructure greatly influenced the size distribution and connectivity of spherical bubble populations, with narrow sedimentary pore throats promoting coarser bubbles with diminished connectivity. Increased connectivity of the bubble population appeared highly significant in limiting bed expansion, either by establishing pathways for gas release, or by dissipating excess internal bubble pressure thereby diminishing further growth. During in situ gas generation, each sediment demonstrated a critical fracture strength which demarcated the populations with high void fractions (0.27 $< \nu < 0.4$) of near spherical bubbles from a fracturing regime supporting reduced void fractions ($\nu \approx 0.15$) of high aspect ratio cracks. However, critical fracture strengths varied significantly (in the 60-1000 Pa range) between sediments, with coarser-grained and higher porosity sediments promoting fracture at lower strengths. Fracture propagation greatly enhanced the connectivity and diminished the tortuosity of the void networks, thereby augmenting the continuous gas release flux.

21 Introduction

In situ gas generation and retention has significant environmental implications for numerous natural and industrial waste sediments. Methanogenesis within natural water systems such as shallow marine sediments, lakes and dredging sludge ¹ represents a considerable, but poorly quantified, contribution to the the global carbon budget and thus represents a significant source of uncertainty for climate change models. Conversely, carbon dioxide sequestration into deep (> 800 m) sedimentary basins has been suggested as an option for balancing this budget ². A lesser known example of trapped sedimentary gases is encountered within historic nuclear waste sludge ³. Corrosion of metallic uranium fuel and nuclear cladding materials, supplemented by radiolytic breakdown of water by soluble fission products (primarily Cs¹³⁷ and Sr⁹⁰) generates flammable hydrogen. Protecting the environment from various radioactinides inherent to these wastes within nuclear storage ponds, tanks and silos, requires that potential acute hydrogen releases are understood and effectively managed to prevent breach of containment.

In natural sediments, an ebullient flux of methane is promoted by elevated winds⁴, tides
and atmospheric pressure fluctuations⁵, which effectively reduce the critical diameter necessary for a bubble to achieve buoyancy⁶. However, under quiescent conditions, both theoretical models⁶ and x-ray computed tomography (CT) imaging³ have shown the critical bubble diameters required for bubble ebullition to be prohibitively large, even under low yield
strength conditions of < 10 Pa. Instead, a recent study by the current authors⁷ proposed
that gas migration and release from quiescent sediments is better explained by transport
through connected networks of partially coalesced bubbles and cracks. Furthermore, this
mechanism of enhanced gas transport is greatly augmented in the case of sediments prone
to fracture during in situ bubble growth⁷.

Comparison of sandy, silty and clay-like sediments has shown that significant disparities in particle and pore size distributions greatly influence the capacity for gas retention, bubble size distribution, bubble morphology and the retained gas profile with depth⁸. While significant

nificant modeling studies have used linear elastic fracture mechanics (LEFM) to mathematically describe the growth and propagation of fractures ⁹⁻¹¹, such models do not account for pore-scale sediment structures which can influence whether the sediment supports fractures, spherical or dendritic bubbles. Little is known of how subtle differences in microstructure (the size, shape and orientation of particles and pore networks¹²) between predominantly fine-grained sediments can influence the gas retention behavior, including the tendency to fracture and the establishment of avenues for gas release. In this study, gas generation is investigated within three chemically similar, fine-grained Mg(OH)₂-rich sediments, complemented by x-ray CT imaging of the retained bubble populations at steady state gas holdup. A two-phase Monte Carlo (MC) gas transport model is also presented in order to analyse the significance of the range, connectivity and geometry of networks of coalesced bubbles in determining the gas release dynamics.

60 2 Materials and methods

Three Mg(OH)₂-rich test materials are used throughout this study as non-active analogues for the Magnox legacy waste found at Sellafield and various Magnox reactor sites across the UK. The first is a commercial Mg(OH)₂ powder called Versamag¹³ (Martin Marietta Specialities, USA), synthesized by the calcination, hydration and precipitation of dolomitic lime; water is added for a prescribed solids concentration before thorough agitation with an overhead stirrer. For brevity, this test material is referred to as magnesium hydroxide powder sludge (MHPS). Two alternative test materials, corroded magnesium sludge (CMgS) and corroded Magnox sludge (CMS), are each manufactured by the UK's National Nuclear Laboratory by corroding raspings of magnesium metal and Magnox alloy respectively in heated water baths doped with sodium chloride. The solids concentrations of CMS and CMgS samples are determined from the loss in mass following 24 h drying at 80 °C. Characterization of the particle size distributions, elemental and crystalline composition, and shear deformation and dynamic mechanical behavior are included in the supporting information (SI).

⁷⁴ 2.1 Sediment microstructure characterization

The sediment microstructure was characterized using a combination of cryogenic-focused 75 ion beam/scanning electron microscopy (cryo-FIB/SEM) and low-field nuclear magnetic resonance (LFNMR) analysis of the pore dimensions. Prior to imaging, samples were rapidly 77 frozen by quenching with slush nitrogen before the temperature was increased to and maintained at -90 °C (under vacuum) for 8 min in order to sublime away the majority of the pore-water. This approach has shown positive results in preserving the microstructure of $soils^{14,15}$ and $gels^{16}$ for imaging, demonstrating excellent agreement with mercury intrusion 81 porosimetry (MIP) 15 and NMR 16 data respectively. A Helios G4 CX DualBeam microscope (FEI, USA) was used to capture images of (1) the topography of a fractured surface of frozen sediment and (2) the interior wall of a borehole etched from the sample by the FIB, or FIB 84 cross-section. 85 LFNMR is a powerful tool for investigating the internal structures of aqueous sedi-86 ments^{8,17}, profiting from the proportionality between the rate at which the protons com-87 prising the pore water lose their magnetic spin, or transverse relaxation time, T_2 , and the pore body radii, $r_{pb}^{18,19}$. Analysis was conducted in accordance with the method outlined 89 in Johnson et al. 7, using mercury intrusion porosimetry (MIP) data for dried samples and LFNMR data for dried and re-wetted samples to calibrate a corrected transverse relation

sions, $r_{th} = \rho_2^* T_2^{7,20}$, where r_{th} is the pore throat radius. MIP and LFNMR tests were undertaken using a 413 MPa Autopore IV porosimeter (Micromeritics, USA) and a MARAN Ultra benchtop NMR analyser (Oxford Instruments, UK) respectively.

strength, ρ_2^* , enabling the relaxation times to be translated to more relevant length dimen-

$_{96}$ 2.2 X-ray CT imaging of $in \ situ$ bubble populations

Bubbles were generated within the sediment by introducing 4.4 mL 35 % w/w hydrogen peroxide solution (Merck Chemicals, Germany), per liter of sediment, which decomposes to a volume of oxygen equivalent to 60% of the initial bed volume over the course of around 8 h⁷. The hydrogen peroxide solution was thoroughly distributed throughout the sediment 100 at the start of each test by 60s of homogenization with an impeller controlled by an over-101 head stirrer. Tests were performed at 0.35, 1 or 6.5 L scales, with the smallest scale tests 102 imaged by x-ray CT. The 1 L tests were performed within 118 mm diameter cylinders, while 103 the 0.35 and 6.5 L tests were performed within 150 mm long sideways mounted cylinders of 104 81 and 300 mm diameter respectively (designed for axisymmetric x-ray attenuation within 105 clinical CT scanners⁷). Gas holdup, or void fraction, was determined, for a broad range of 106 sediment conditions (30 $< \tau < 1112 \,\mathrm{Pa}, \, 1270 < \rho < 1700 \,\mathrm{kg \, m^{-3}}$) above the liquid limit²¹, 107 by monitoring volumetric bed swell ($\nu = 1 - V_{in}/V_{max}$, where V_{in} and V_{max} are the initial 108 and maximum bed volumes respectively)³. 109

Sedimentary bubbles are frequently generated experimentally by *in situ* chemical⁷ or biological⁵ reaction, high pressure injection through a nozzle²² or depressurization^{23,24}. *In situ* reaction was deemed preferable as (1) it ensures that gas generation is global throughout the bed, (2) bubble growth occurs on a realistic time-scale of several hours, and (3) bubble nucleation and growth commence at the pore-scale, which is critical to investigating the role of microstructure on bubble growth. Hydrogen peroxide decomposition has been shown to provide repeatable kinetics independent of the Mg(OH)₂ solids concentration or yield strength conditions³.

Previous work by the current authors³ has shown that this method of *in situ* gas generation results in steady state gas holdup, bubble populations and bubble dimensions within the first 6 h of gas generation and thus the bubbles can be considered *mature*²⁵ after 6 h.

Under these steady state gas holdup conditions, the retained bubble populations within four 350 mL-scale sediment tests were visualized using high resolution x-ray CT, including each

of the test sediments at $\approx 30 \,\mathrm{Pa}$ yield strength, and an additional higher strength sample of \approx 130 Pa CMS. The MHPS and CMgS sediments were imaged using an Inveon dual positron 124 emission tomography(PET)/CT scanner (Siemens, Germany) in accordance with the method 125 outlined in Johnson et al. 7. A similar XTremeCT (Scanco Medical, Switzerland) scanner 126 was used to investigate the CMS test material. Both scanners use cone-beam x-ray sources, 127 capturing 180 projections at 1° intervals, achieving voxel resolutions in the order of 50 µm 128 after reconstruction. The imaging protocols are further summarized in Table S1. 129

A combination of FIJI ImageJ²⁶, DigiUtility (Structure Vision Ltd., UK)²⁷ and Matlab 130 v. R2017a (Mathworks, USA) were used to diminish image artefacts, threshold and extract 131 quantitative bubble size information during post-processing⁷. Bubble size analysis for inter-132 connected bubble populations was achieved by measuring three perpendicular chord lengths 133 at 1×10^8 random sites within the void network and applying an ellipsoidal chord length to 134 diameter transformation algorithm^{7,28} in Matlab. 135

Monte Carlo modeling of gas migration 2.3 136

Extensive networking between partially coalesced bubbles enables gas transport to be inves-137 tigated on timescales of seconds, in contrast to the much slower process of aqueous diffusion 138 through pore-water⁷. A Monte Carlo model (MCM) originally used to study aggregation 139 and sedimentation dynamics²⁹, and later gas diffusion⁷, was further adapted to simulate gas 140 migration through sediments with complex void geometries. Such complex void geometries 141 could include sediments containing discrete, non-ebullient (static) bubble networks, for which 142 long-range gas transport through the sediment is not possible without (1) mass exchange at 143 the bubble-pore water interface, and (2) transport of volatiles in the aqueous phase. This 144 is particularly relevant to immature or low voidage bubble populations where long range 145 networks have not had time to form, or within sediments where bubble armoring inhibits partial bubble coalescence³⁰. A detailed description of the principles underlying the MCM are included in the SI; however, in brief, the adapted model mimics Fick's second law of

diffusion within the aqueous (pore water) and gaseous (void) phases through random motion between neighboring voxels in the reconstructed CT images, while Henry's law is used to 150 dictate the rate of mass exchange between the voidage and ambient pore water. The rele-151 vant diffusion coefficients ^{31,32} and the dimensionless Henry's law coefficient ³³ employed by 152 the model are detailed in Table 1.

Table 1: Parameters used in the MCM to determine composite hydrogen diffusion through voids and porewater

$$\frac{D_{H_2,H_2} \text{ (m}^2 \text{ s}^{-1}) \quad D_{H_2,H_2O} \text{ (m}^2 \text{ s}^{-1}) \quad K_{H,cc}}{1.604 \times 10^{-4} \quad 4.50 \times 10^{-9} \quad 1.96 \times 10^{-2}}$$

This approach for simulating gas migration benefits from very simple front-end imple-154 mentation in comparison to continuum-based flow modeling. The model can be implemented directly using real tomographic datasets of complex void geometries without the need for 156 meshing. In this study, the calculations were performed using 600³ voxel CT reconstructions of $\approx 30 \,\mathrm{Pa}$ yield strength samples of the three test materials and a higher strength 132 Pa CMS sample, each after 6 h in situ gas generation. The primary disadvantage is that the 159 simulations themselves can be time consuming to undertake. Four tomography datasets were 160 simulated using individual 3 GHz CPU Intel i5 processors with 2×8 Gb RAM due to issues 161 with conserving mass when running the simulation across multiple cores. Consequently, one 162 minute of real diffusion required around four weeks of simulation time. 163

3 Results and Discussion

3.1 Sediment microstructure characterization 165

Light scattering analysis (Figure S2) revealed each of the test materials to be largely fine-166 grained with modal particle diameters in the order of 3-4 µm. The PSDs indicate largely 167 silt-like (2 $< d_p < 63 \,\mu m$) sediments with up to 21 % clay-sized ($< 2 \,\mu m$) fractions. The 168 principle differences in PSD lie in the fact that MHPS exhibits few sand-sized particles $(0.2\% > 63\,\mu\text{m})$, while the CMS and CMgS are richer in coarse silt and medium sand-sized grains respectively.

Energy dispersive x-ray spectroscopy (EDX) and x-ray powder diffraction (XRD) analysis (Figure S3) revealed very similar compositions. Each of the test materials was found to contain almost exclusively brucite (Mg(OH)₂) with only trace amounts (< 1%) of aluminum, silicon and calcium. For the CMgS, these elements were attributed to traces of crushed slate contaminants, while the aluminum within the CMS derives from the 0.8% Al content present in the Magnox alloy from which it was synthesized.

In spite of the apparent compositional similarity, cryo-FIB/SEM imaging (Figures 1a-c) 178 revealed a distinct structure in the case of the CMS, with high aspect ratio acicular, or needle-179 like, crystals resembling the carbonated brucite seen in Maher et al. 34, contrasting the more 180 common hexagonal platelet brucite structure³⁵ of the MHPS and CMgS. The nuclear waste 181 sediments exhibit an open structure, with high void ratio, which is analogous to a range of 182 natural sediments, including clay-dominated sediments at very shallow depths ¹², calcareous 183 sediments³⁶, and organo-mineral agglomerations (mixtures of particles formed by organisms 184 such as faecal pellets, and mineral grains) that form in areas with rapid sedimentation that 185 induces significant organic matter decomposition³⁷. In particular, acicular crystals observed in the CMS sediment are highly analogous to calcareous sediments dominated by aragonite $needles^{36}$. 188

This distinctive CMS crystal morphology has some significant implications for the sed-189 iment microstructure and shear deformation behavior. The high aspect ratio crystals en-190 able the CMS to form a continuous solid skeleton, or qel, at reduced solids concentrations 191 $(\omega < 0.2 \,\mathrm{kg \, kg^{-1}})$, see Figure S4b). Correspondingly, the CMS has a significantly greater 192 porosity and water content than the CMgS or MHPS at an equivalent yield strength. In the 193 instance of 30 Pa yield strength sediments, the CMS will be around 18 % higher in porosity 194 and 11% lower in bulk density than the CMgS and MHPS. However, weak inter-granular 195 contacts between needle-like crystals give the CMS skeleton a reduced stiffness at low strains 196

(see Figures S4c-d). CMS of $\approx 30 \,\mathrm{Pa}$ yield strength has a storage modulus, G', in the order of $10^4 \,\mathrm{Pa}$, around an order of magnitude lower than the MHPS and CMgS.

Figure 1d presents the pore throat size distributions for three CMS samples of different 199 yield strength; 84-91 % of the total detected pore volumes for each sample are connected by 200 pore throats in the $0.1 < r_{th} < 0.6 \,\mu\mathrm{m}$ range, around an order of magnitude smaller than 201 the modal particle sizes demonstrated in Figure S2. The remaining pore volume is almost 202 entirely accounted for by a small number of large $\approx 2\,\mu\mathrm{m}$ scale pores. Given that $\approx 99\,\%$ 203 of the porosity is connected by throats of at least 100 nm³⁸, these soft sediments can safely 204 be characterized as macro-porous, punctuated by a small number of micron-scale fracture 205 sites 39 , or *cleats*. 206

In addition to enhancing the sediment bulk yield strength, increasing the solids con-207 centration (usually achieved by dewatering the sediment under compression) also causes 208 the majority of pore throats to constrict. This contraction is consistent with observations 209 from discrete element modeling for coarser, non-cohesive sandy sediments in Mahmoodlu 210 et al. 40. Pore throat constriction increases the resistance to a non-wetting fluid (such as 211 hydrogen bubbles) intruding into adjacent pore-space by capillary invasion 41 and is further 212 demonstrated by Figure 1e which presents modal pore throat radii as a function of shear yield strength for the three test materials. Curiously, the hierarchy of pore throat radii (MHPS>CMS>CMgS) finds the CMS to have intermediate sized pore throats, despite its 215 apparently distinct particle morphology and elevated porosity at comparable yield strength. 216 However, the pore dimensions likely represent a complex product of particle size distribution, 217 crystal morphology, porosity and the strength of inter-particle interactions, and are thus far 218 from trivial to predict. Logically, if the CMS has a significantly larger total porosity and 219 more constricted pore throats than the MHPS, a larger pore body to throat ratio would be 220 anticipated. However, the pore body to throat ratio is not easily characterized without first 221 drying the sediment 20 and the microstructure is unlikely to be preserved during the drying 222 process. 223

The disparity in pore throat scales demonstrated between the three test materials is 224 potentially significant to the mechanism of in situ bubble growth. Returning to the example 225 of 30 Pa yield strength sediments, the CMgS would experience 35 % greater capillary entry 226 pressures (given the Young-Laplace relationship⁴², $\Delta P_i = P_b - P_w \propto r_{th}^{-1}$, where P_b and P_w 227 are the internal bubble and pore water pressures) between the majority of its pores than 228 the MHPS or CMS. However, the narrow modal pore throat dimensions of less than 340 nm 229 observed for these fine grained test materials is likely to preclude gas invasion into adjacent 230 pore-space due to prohibitively high capillary entry pressures 1,25,43. Instead, it is anticipated 231 that bubble growth will be limited to the cavity expansion and fracture propagation growth 232 mechanisms, both of which involve deformation of the surrounding sediment skeleton. 233

3.2 Gas retention behavior

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The maximum void fractions, or gas holdup, were observed during 8 h in situ gas generation 235 within sediments at 1 and 6.5 L scales, as detailed in Section 2.2, and are presented across 236 a range of shear yield strength conditions in Figure 2. The six 6.5 L scale experiments 237 represented by open symbols in Figure 2 were deemed to demonstrate acceptable agreement 238 with the liter-scale data. The disparity in gas holdup between the test materials appears 239 significant, although a number of consistent themes emerge. Each of the test materials 240 exhibits a large holdup regime at low yield strengths, with void fractions in the order of 241 0.27-0.40. Above a critical yield strength, or narrow range of yield strengths, gas holdup 242 diminishes to maximum void fractions in the order of 0.15. For the CMS, this transition 243 occurs above yield strengths of around 60 Pa. A similar trend occurs for the CMgS above 244 120 Pa, and above around 1000 Pa yield strength for the MHPS (see the dashed vertical lines 245 in Figure 2). Unfortunately, it was not possible to adequately distribute hydrogen peroxide 246 through greater than kPa strength MHPS to observe a similar ≈ 0.15 void fraction plateau to the CMS.

The x-ray tomography studies of MHPS in Johnson et al.³,⁷ clearly indicate that the

reduction in bed swell at ≈ 1 kPa yield strength corresponded to the onset of fracture in that material. Furthermore, in van Kessel and van Kesteren¹, crack initiation within dredging sludge experiencing in situ methanogenesis was similarly observed to diminish the capacity for bed expansion. Thus, a critical fracture strength, τ_f , may demarcate a low strength regime of near spherical bubble growth by elastic/plastic cavity expansion from a regime of growth dictated by tensile fracture. The characteristics of the bubble population in the low strength cavity expansion regime and the evidence for a microstructure dependent critical fracture strength are discussed in Sections 3.3 and 3.4 respectively.

$_{58}$ 3.3 Gas retention in the cavity expansion regime

Figures 3a-c reveal the bubble populations within the three test materials at similar yield strengths of $31 \pm 1 \,\mathrm{Pa}$, each below the respective critical fracture strengths. 260 strength test material supports bubbles with a spherical geometry, 3-4 orders of magni-261 tude greater than the LFNMR measured pore dimensions, indicating bubble growth by 262 elastic/plastic cavity expansion. However, it is immediately apparent that the bubble di-263 mensions are vastly dissimilar between the three sediments, reflected by the bubble size 264 distributions (BSD) presented in Figure 3e and the bubble characteristics summarized in 265 Table 2. Two indicators suggest that the tomographic resolution of $\approx 50 \,\mu m$ is sufficient to 266 capture the entire bubble populations. First, the Gaussian distributions of each of the BSDs 267 decay to zero at bubble diameters greater than 80 µm. Second, the visible void fractions 268 determined from image analysis, summarized in Table 2, demonstrate good agreement with 260 the apparent increase in bed volume over the duration of these small-scale CT experiments, 270 and the void fractions from the liter-scale tests summarized in Figure 2. 271

The smallest bubbles retained by the CMgS are a millimeter in diameter, much larger than those within the MHPS, for which 86% of bubbles are smaller than a millimeter. The low strength CMS retains intermediate sized bubbles, with 22% of its population less than a millimeter in diameter and 10% of bubbles larger than $2.8 \,\mathrm{mm}$. In fact, the disparity in

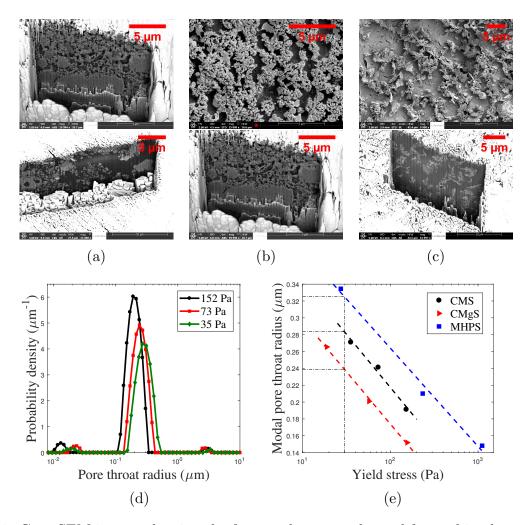


Figure 1: Cryo-SEM images showing the fractured topography and focused ion beam etched cross-sections of (a) $\omega \approx 0.4$; $\tau \approx 70\,\mathrm{Pa}$ MHPS, (b) $\omega \approx 0.42$; $\tau \approx 148\,\mathrm{Pa}$ CMgS and (c) $\omega \approx 0.27$; $\tau \approx 86\,\mathrm{Pa}$ CMS sediments, along with LFNMR analysis of (d) pore throat size distributions for CMS and (e) modal pore throat radii as a function of yield strength for the various Mg(OH)₂-rich legacy waste test materials (dashed lines represent semilog regression fits for each test material).

Table 2: Characteristics of bubble populations in the cavity expansion regime (as determined by x-ray image analysis), including void fraction, ν , mean bubble diameter, \bar{d}_b , 90th percentile of the BSD, $d_{b,90}$, specific surface area, SSA, bubble number density, n_b , and the contribution of the largest bubble network to the total voidage, $\nu_{i,max}$.

Sediment	τ (Pa)	ν	$\bar{d}_b (\mathrm{mm})$	$d_{b,90} (\mathrm{mm})$	$SSA (mm^{-1})$	$n_b (\mathrm{cm}^{-3})$	$\nu_{i,max}$
MHPS	30	0.282	0.64	1.11	18.2	2913	0.995
CMgS	30	0.385	2.56	3.75	3.7	72	0.028
CMS	32	0.254	1.84	2.80	7.5	151	0.827

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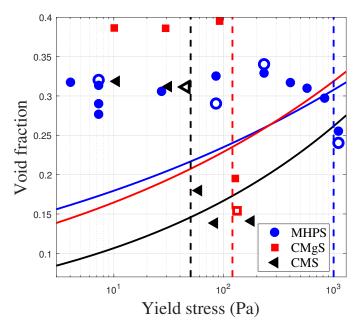


Figure 2: Maximum void fractions observed across a range of yield strength conditions for three Mg(OH)₂-rich sediments, (many of the MHPS data are reproduced from Johnson et al.³); solid and open symbols represent 1 and 6.5 L scale tests respectively, the solid line profiles represent the *neutral buoyancy* condition, whereby the sediment density reaches equilibrium with an aqueous supernatant and vertical dashed lines at $\tau = 60$, 120 and 1000 Pa indicate apparent transitions to a lower holdup regime above proposed *critical fracture strengths*.

BSD between the three test materials far outweighs the variation with yield strength for a particular test material, indicating that sediment microstructure has a greater influence on the BSD than yield strength.

The hierarchy in bubble size (CMgS>CMS>MHPS) coincides with the inverse hierarchy 279 in bubble connectivity, with coarser bubble populations manifesting in diminished connec-280 tivity. The bubble connectivity is perhaps better demonstrated by Figure 4a, which shows 281 the 16 largest networks of partially coalesced bubbles within the low strength CMgS. The 282 largest of these networks contributes only 2.8% of the total holdup, contains just 52 par-283 tially coalesced bubbles and does not traverse the width of the 32 mm wide field of view to 284 provide a continuous pathway for gas migration through the sediment. Conversely, 99.5 % of 285 bubbles within the low strength MHPS are inter-connected within the same bubble network, 286

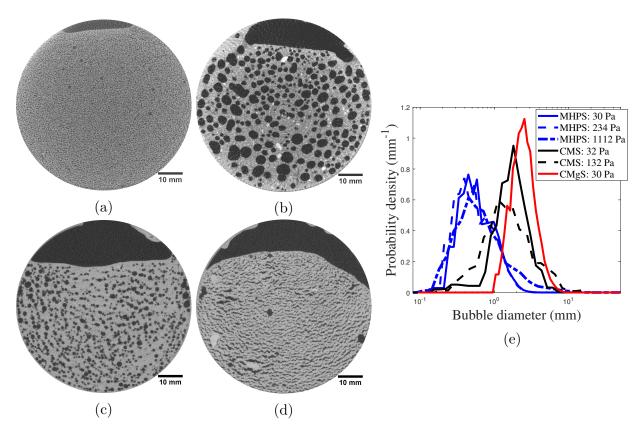


Figure 3: X-ray computed tomography slices through (a) 30 Pa MHPS, (b) 30 Pa CMgS, (c) 32 Pa CMS and (d) 132 Pa CMS following 6 h in situ hydrogen peroxide decomposition (following the cessation of bed expansion), together with (e) bubble size distributions within the three test materials.

comprised of more than 20 000 bubbles. The disparity in bubble connectivity is illustrated by Figure 4b, which presents the number of bubbles, N_i , comprising the 10 largest bubble networks in each sediment, estimated from the network volumes, V_i , and the bubble number densities, n_b , derived from the BSD probability densities, $p(d_b)$:

$$N_i = V_i n_b$$

$$n_b^{-1} = \frac{\pi}{6} \int_0^\infty \left[p(d_b) d_b^3 \right] d(d_b)$$
(1)

In one respect, the inverse correlation between bubble size and connectivity is intuitive as coalescence is a surface phenomenon and a population comprised of fewer, but coarser bubbles will present a much smaller specific surface area (SSA). However, the differences in bubble size and connectivity between the three sediments could equally be explained by their

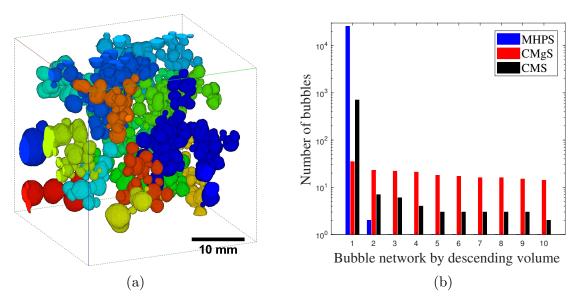


Figure 4: (a) CT reconstruction of the 16 largest bubble networks within 30 Pa CMgS, assigned different colors for visualization (with warmer colors representing reduced network volumes) and (b) a comparison of the number of bubbles comprising the 10 largest bubble networks (sorted by descending bubble volume) for the three Mg(OH)₂-rich test materials.

differences in microstructure. Recalling Figure 1e, the hierarchy of pore throat dimensions indicated by LFNMR analysis (MHPS>CMS>CMgS) resembles that of bubble connectivity.

Thus, the more constricted the sedimentary pore throats prior to the onset of gas generation, the less likely bubbles occupying adjacent pores are to interact and partially coalesce.

It has been established that the mature bubbles visible in Figure 3 are orders of magnitude larger than the sediment pore throat dimensions. At a very early stage of bubble growth the bubble occupies the pore body and begins to deform the surrounding sediment matrix ⁴¹. Just as Figure 1e demonstrated constriction of the pore throats with increased consolidation, this period of cavity expansion is likely to induce widening of the pore throats in unison with the pore body expansion, thereby diminishing the capillary invasion pressure ⁴⁴. Eventually, the capillary invasion pressure may drop sufficiently to enable the bubble to intrude through the pore throat and either (1) occupy multiple adjacent pores, or (2) approach another bubble occupying an adjacent cavity and coalesce.

Invasion into adjacent pore bodies would induce a drop in the internal bubble pressure ⁴² and diminish the driving force for further bubble growth. Likewise, two partially coalesced

bubbles will require a greater increase in internal pressure to induce further cavity expansion than the two discrete bubbles with elevated Laplace pressures. Thus, the sediment 311 microstructure may dictate the termination condition for bubble growth by cavity expan-312 sion in some instances, rather than exhaustion of the diffusive supply due to (1) diminishing 313 source strength or (2) elevated internal bubble pressures extinguishing the concentration 314 gradient and inducing a no growth condition 11. For cavity expansion growth limited by ei-315 ther coalescence or capillary invasion, a sediment with narrow pore throats could undergo a 316 prolonged period of cavity expansion before growth is terminated, resulting in a population 317 of larger bubbles and reduced connectivity, consistent with the inverse correlation observed 318 between BSD and pore throat radii. 319

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Over longer timescales than these relatively short-duration laboratory-scale tests, a second phenomenon which may contribute towards creating a smaller population of larger bubbles, or bubble coarsening, is Ostwald ripening 45,46. The inverse relationship between internal bubble pressure and bubble volume makes smaller bubbles more soluble, driving diffusive transfer from small bubbles towards proximate larger bubbles. Adjacent bubbles therefore grow competitively, with large bubbles growing at the expense of their smaller neighbors, generating a thermodynamically favorable reduction in total surface energy over time 47. This indicates how a poorly connected bubble population, such as that supported by the CMgS in Figure 3b, might have evolved over time. Conversely, when bubbles are partially coalesced in a network, or particles are agglomerated within a larger aggregate particle, Ostwald ripening manifests as a widening of the necks between adjacent bodies 48, indicating an alternative ripening regime for populations consistent with the low strength MHPS in Figure 3a.

Physical properties of the sediment can also influence the rate at which the bubble population evolves due to Ostwald ripening. It is generally acknowledged that the process is rate limited by diffusion ^{47,49}. Sediment microstructures dictate the tortuosity of the diffusion pathways for volatiles in solution ⁵⁰ and could thereby impact the rate of bubble coarsening. Subtle differences in particle size distribution (PSD) can also impact the structure and

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effectiveness of monolayers which armor bubbles and inhibit Ostwald ripening 46 .

338 3.4 Transition to a fracturing regime above a $critical\ fracture$ 339 strength

The sharp reduction in gas holdup, demonstrated for each test material above a characteristic, material dependent yield strength in Figure 2, was observed at around 60 Pa in the case of CMS. Figure 3c and Figure 3d present x-ray tomography revealing the retained bubble 342 populations at 32 and 132 Pa respectively, either side of this transitional yield strength. The uniform spherical bubbles with aspect ratios close to unity at 32 Pa become laterally oriented high aspect ratio fractures at 132 Pa, punctuated by large spherical bubbles, closely resembling the behavior of kPa strength MHPS⁷. Thus, the reduction in gas holdup coincides with 346 the onset of fracture propagation. Crack formation was similarly linked with a reduction 347 in bed swell in Johnson et al. 7 and van Kessel and van Kesteren 1, however it is not clear 348 why the *critical fracture strength*, at which this transition in bubble growth behavior occurs, 349 varies so significantly between the three Mg(OH)₂-rich test materials in this study. 350 To understand the existence of, and variation in, critical fracture strength it is necessary 351 to review the mechanisms for bubble growth. The resistance to uniform, spherical bubble 352

$$\Delta P_e = P_b - \sigma = \frac{4}{3}\tau \left(1 + \ln \left| \frac{G}{\tau} \right| \right) \tag{2}$$

where $P_b - \sigma$ is the difference between the internal bubble pressure and the mean ambient sediment stress normal to the bubble surface²⁵. For typical shear modulus to shear strength ratios in the 50-100 range⁵², the expression approximates to $\Delta P_c \approx (7.1 \pm 0.5)\tau$. Conversely, materials with high tensile strength, σ_y , (approximately double the shear yield strength) are often more prone to fracture as they are less likely to deform plastically, thereby dissipating

growth, quantified by the excess internal bubble pressure required for cavity expansion, ΔP_e ,

scales with sediment yield strength and the ratio of shear modulus, G, to yield strength: 1,51

energy, at a crack tip than low-strength ductile materials ⁵³. For natural cohesive sediments, fracture toughness appears to increase marginally with increased shear strength, $K_{1c} = k\tau$, with low multipliers reported as k = 0.13 - 0.21 in Winterwerp and van Kesteren ⁵² and $k \approx 0.09$ for Canadian clay-like silts in Johnson et al. ⁵⁴. The critical pressure for fracture, ΔP_f , is, in turn, proportional to the fracture toughness raised to the power of 6/5 according to LEFM: ^{9,55}

$$\Delta P_f = P_b - \sigma = \frac{K_{1c}^{6/5} \pi^{3/5} (1 - k_\nu^2)}{12^{1/5} (EV_b)^{1/5}}$$
(3)

where k_{ν} and E are Poisson's ratio and the Young's modulus respectively and V_b is the bubble volume. The $K_{1c}^{6/5}$ and $E^{-1/5}$ dependence of the fracture pressure, combined with the very mild increase in fracture toughness with yield strength, indicates that fracture pressure increases much less rapidly with increased yield strength than the cavity expansion pressure. To illustrate this point, for a theoretical soft sediment with fracture toughness $K_{1c} = 0.17\tau^{52}$, shear modulus $G = 75\tau^{52}$, Young's modulus $E = 2G(1 + k_v)$ and Poisson's ratio of $k_{\nu} = 0.45^{56}$, the derivatives of the two critical pressures with respect to yield strength approximate as follows:

$$\frac{d\Delta P_f}{d\tau} \approx 0.048 V_b^{-1/5}
\frac{d\Delta P_e}{d\tau} \approx 7.1$$
(4)

Hence, for any bubble greater than 300 µm in equivalent spherical diameter, increasing the 374 yield strength of this theoretical sediment will increase the cavity expansion pressure more 375 than it will increase the fracture pressure. Bubble dimensions in the order of 300 µm are 376 around three orders of magnitude larger than the pore dimensions but relatively small in 377 comparison with the mature bubble dimensions observed in Figure 3, potentially indicating 378 an initial period of cavity expansion prior to fracture. Thus, for most realistic sediment 379 conditions, consolidation, or increasing yield strength, will increase proclivity for fracture, 380 giving credence to a critical strength at which fracture growth begins to dominate. One 381

particular advantage of a critical yield strength is that fracture toughness characterization remains a relatively immature field for soft materials and can require fairly complex bespoke 383 equipment for measurements in the field 54,55. Conversely, yield strength can be characterized 384 remotely using slump tests⁵⁷, which, in a nuclear context, reduces exposure of workers to 385 radiation. 386

The significant variation in critical fracture strength between the three Mg(OH)₂-rich 387 test sediments still requires explanation. The sediment microstructure will influence the 388 propensity for fracture by (1) provision of interstitial crack sites particularly vulnerable to 389 fracture nucleation and (2) the influence of microstructure on bulk mechanical properties. 390 Both effects are reflected by the LEFM model in Equation (3), which demonstrates that 391 the requisite fracture pressure will depend not only on the sediment's mechanical properties, 392 such as fracture toughness and Young's modulus, but also the bubble or initial crack dimen-393 sions, with a $V_b^{-1/5}$ dependency ^{9,55}. Fractures are therefore most likely to nucleate at, and 394 propagate along the major axis of, large microstructural defects ⁵⁸, such as the small number 395 of micron-scale pores observed from the LFNMR analysis of the CMS (Figure 1d). The fact 396 that the MHPS shows no evidence of these micron scale cleats⁷ may well contribute to the 397 absence of fracturing at sub-kPa yield strengths.

However, fracturing is observed globally in Figure 3d rather than solely at the largest 399 pores, indicating a disparity in the bulk mechanical and fracture resistance properties be-400 tween the test materials. Equation (3) identifies the particular significance of fracture tough-401 ness and, to a lesser extent, stiffness in determining the requisite fracture pressure. One prin-402 cipal difference between the test materials, revealed by vane rheology in Figure S4b, was that 403 the CMS qels at lower solids concentrations, or higher porosity. The, relatively limited, data 404 on fracture toughness of soft sediments 54,59 have shown exponential reductions in fracture 405 toughness with increased porosity, $K_{1c} = a \exp(-b\phi)$, where $a > 10^4$ and $7 < b < 16^{59}$, which 406 may well contribute to its diminished critical fracture strength. Furthermore, an inverse, or 407 inverse square, correlation exists between fracture toughness and average grain radius 43,54 .

An average grain size is not a particularly adequate representation of the complex bi- or trimodal PSDs for these Mg(OH)₂-rich sediments, however the particularly fine grained MHPS 410 $(d_{50} = 4.4 \,\mu\text{m})$ demonstrates the greatest critical fracture toughness and the coarsest grained 411 CMS ($d_{50} = 8.2 \,\mu\text{m}$) the weakest. 412 The sediment stiffness also appears in LEFM models with an $E^{-1/5}$ dependence. Young's 413 modulus is typically reported as the measure of sediment stiffness, where dynamic mechanical 414 analysis of the linear viscoelastic region may be more appropriate for viscoelastic solids (see 415 Figures S4c-d). Better measures of stiffness would be the norm $(|G^*| = \sqrt{G'^2 + G''^2})$ of the 416 complex shear modulus ($G^* = G' + iG''$) or the storage modulus itself, which are practically 417 equivalent for dominantly solid like materials ($G'/G'' \ge 10$). At yield strengths of $\approx 30 \,\mathrm{Pa}$, 418 the storage modulus is a factor of 5-6 lower for CMS than the MHPS and CMgS. A reduction 419 in stiffness actually implies an increase in fracture pressure according to LEFM, although the 420 stiffness dependence is weak in comparison to the $K_{1c}^{6/5}$ dependence on fracture toughness 421 and so the influence of the reduced porosity outweighs that of stiffness. Given the apparent 422 significance of microstructure on fracture behavior, there would be tremendous advantages 423 in extending grain-scale models of bulk mechanical properties 43 to microstructures of more

The influence of bubble geometry on gas transport dynamics 3.5 426

complex cohesive sediments with multi-modal PSDs and alternative particle morphologies.

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X-ray CT has demonstrated highly varied bubble populations retained by sediments with 427 subtly different microstructures and mechanical properties, from coarse spherical populations 428 with low connectivity, to sub-millimeter scale populations with extensive connectivity, and 429 vast networks of high aspect ratio fractures. It is equally important to understand how 430 each bubble population facilitates gas transport through the bed and potentially limits the 431 sediments' capacity for bed expansion. Understanding the mechanisms for gas migration is 432 particularly significant for determining when the gas flux from the sediment approaches the rate of gas generation, preventing gas accumulation and terminating growth. To this end, the results of Monte Carlo gas diffusion calculations (detailed in Sections 2.3 and S2.3) for the three low strength sediments in the cavity expansion regime ($\tau = 31 \pm 1 \,\mathrm{Pa}$) and CMS in the fracturing regime ($\tau = 132 \,\mathrm{Pa}$) are presented in Figure 5.

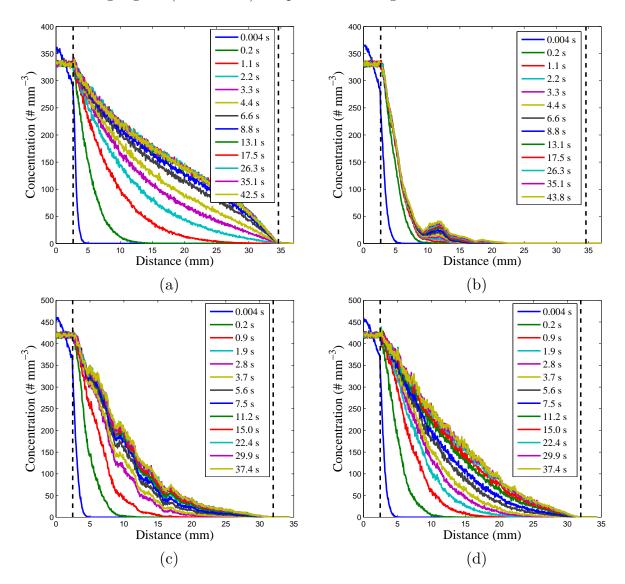


Figure 5: Evolving hydrogen concentration profiles during Monte Carlo diffusion simulations through (a) 30 Pa MHPS, (b) 30 Pa CMgS, (c) 32 Pa CMS and (d) 132 Pa CMS.

Figures 5a-c demonstrate the rate of diffusion through the three low strength ($\approx 30 \,\mathrm{Pa}$) sediments within the cavity expansion growth regime. The rate of gas transport through the sediments reveals gas diffusivity in the hierarchy of MHPS>CMS>CMgS, predictably mirroring that of the bubble connectivity in Figure 4b and Table 1. Most notably, the

CMgS demonstrates very poor gas transport dynamics. Since the bubbles supported by the
CMgS do not form a continuous network traversing the width of the domain, interfacial mass
exchange is required for a gas flux to pass through the sediment and into the sink region.

Henry's law dictates that the hydrogen concentration diminishes by a factor of 51 at 445 each bubble-pore water interface, thereby greatly hindering gas migration across the domain. 446 Furthermore, since only a very small percentage of bubble networks extend to the source 447 region, only a fraction of the voidage is effectively utilized for gas transport at the prescribed 448 boundary conditions, and so mass transport to the bulk of the void-space is limited by the 449 diffusivity of hydrogen in the pore water, which is around four orders of magnitude lower 450 than in the gas phase^{31,32}. Thus, the short range, poorly connected population of coarse 451 millimeter-scale bubbles within the CMgS results in a negligible flux of gas from the bed. 452 The negligible rate of chronic gas release in turn enables the substantial bed swell observed 453 during the 1-6.5 L scale tests to void fractions in the order of 0.40. 454

Conversely, the 83-100% connectivity amongst the MHPS and CMS bubble populations, and the provision of a completely permeable gas-pathway between source and sink regions, ensures a steady flux of gas from the bed controlled by the relatively rapid gas phase diffusion. The high connectivity also ensures that the concentration profiles exhibit the Gaussian tail shape characteristic of Fick's second law of diffusion 60. The connectivity of the bubble networks and steady flux of gas from the bed limits further bed swell and imposes a ceiling in the gas holdup capacity at the 0.25-0.28 void fractions observed in Figure 2.

Figures 5c-d contrast the gas transport dynamics for CMS under cavity expansion (32 Pa) and fracturing (132 Pa) conditions respectively. The fracturing sediment exhibits the faster gas transport dynamics, as indicated by the elevated tracer concentrations at the midpoint of the domain (roughly double those of the weaker sediment) once the equilibrium condition is attained after around 30 s. This reflects the fact that fracturing increases the connectivity of the bubble population from 83 to 94% and greatly diminishes the tortuosity of the lateral diffusion path. Significantly, the fracturing sediment demonstrates this enhanced

permeability at a reduced void fraction of 0.20, compared with 0.25 for the lower strength,

non-fracturing CMS (the void fractions within these CT sub-domains taken from 350 mL 470 scale experiments can differ slightly from the litre and 6.5 L scale tests), explaining the 471 cessation of bed expansion at reduced holdup conditions in the order of 0.15 in Figure 2. 472 The clear influence of sediment microstructure on the retained BSD, the connectivity 473 between bubbles and the tendency for fracture therefore strongly dictates the gas release 474 dynamics and capacity for gas holdup, with significant implications for both natural sedi-475 ments and active nuclear waste sediments. First, the critical fracture strength defines a lower 476 bound for yield strength at which LEFM models for fracture propagation apply. Second, it 477 dictates yield strength conditions of diminished gas holdup and enhanced rates of continuous 478 gas release. Thus, the critical yield strength provides a means of identifying natural sedi-470 ments likely to contribute substantial methane releases or radioactive waste packages posing 480 an increased risk of acute flammable gas releases and potential radioisotope release to the 481 environment. 482

Supporting information 4

An electronic supporting information document is provided including characterization of the three test materials in terms of their chemical composition, particle size distribution, rheology and dynamic mechanical behavior, along with further details of the x-ray tomographic imaging protocol and a detailed description of the Monte Carlo diffusion model.

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