LES Prediction of an Installed Jet Flow and Noise with Experimental Validation

Zhong-Nan Wang^{1*}, Anderson Proenca^{2†}, Jack Lawrence^{2‡}, Paul G. Tucker^{1 §}

and Rod $\mathrm{Self}^{2\P}$

¹Department of Engineering, University of Cambridge, Cambridge, CB2 1PZ, UK

²Institue of Sound and Vibration Research, University of Southampton, Southampton, SO17 1BJ, UK

Extra noise is generated when jets are installed beneath solid surface. In this paper, Large-Eddy Simulation (LES) has been used to investigate these jet installation effects. The simulations were performed on two jet configurations: an isolated jet and a jet installed below a horizontal flat plate. The LES is compared with experimental data from measurements using hot wires, unsteady surface pressure sensors and far-field microphones. Good agreement has been achieved between LES and experimental measurements on flow statistics, space-time correlations, and both near-field and far-field sound spectra. The installed effects are discussed from the perspective of flows and acoustics in the validation process.

Nomenclature

 $A_{ij}^{c,n}$ Jacobi matrix of $F_{ij}^{c,n}$

- c_0 sound speed of ambient fluids, m/s
- D Nozzle diameter, m
- $F_{ij}^{c,n}$ Numerical convective flux between control volume *i* and *j*
- H Distance between nozzle centre line and plate lower surface, m
- L Distance between nozzle exit and plate trailing edge, m
- M_j Jet Mach number, U_j/c_0

^{*}Research Associate, Department of Engineering, University of Cambridge, and AIAA Member.

[†]Research Fellow, Institute of Sound and Vibration Research, University of Southampton, and AIAA Member.

[‡]Research Fellow, Institute of Sound and Vibration Research, University of Southampton, and AIAA Member.

[§]Rank Professor of Engineering, Department of Engineering, University of Cambridge, and AIAA Associate Fellow.

[¶]Professor of Aeroacoustics, Institute of Sound and Vibration Research, University of Southampton, and AIAA Member.

- Q_i conservative variables at control volume i, $[\rho, \vec{u}, \rho E]$
- r Radial distance from nozzle centre line, m
- R_{ij} Space-time correlation of velocities u_i and u_j
- St Strouhal number
- u_i instantaneous velocity in the direction i, m/s
- U_i Maximum axial velocity along nozzle centre line, m/s
- U, V Time-averaged axial, radial velocity, m/s
- W Half plate width, m
- **x** Coordinates [x, y, z], m
- τ_{ij} Reynold stress tensor
- ϕ Observer polar angle, °
- ζ Spatial separation distance $[\xi, \eta, \phi], m$
- au Time delay, s

Subscript

j jet

Superscript

- n surface normal
- c convective

I. Introduction

As global air traffic volume continues to grow, currently by about 8% per year, aircraft noise becomes of great concern to residents living around airports. Jet noise from aeroengines is still one of the dominant components when an aircraft is taking off. High bypass ratios, used to increase engine efficiency, significantly reduces jet noise by decreasing the effective jet velocity U_j , as jet mixing noise scales with $U_j^{8,1}$. However, the increased bypass ratio enlarges engine diameters, which in turn results in the engine installation much closer to the wing. This intensified jet-wing interaction introduces a significant low-frequency noise source, referred to as installed jet noise.² Especially for the next-generation ultra-high bypass ratio (UHBP) aeroengine, the small gap between the engine and wing will further increase installed jet noise. It is, therefore, important to predict, understand and then reduce installed jet noise.

In over 60 years of research, considerable progress has been made on isolated jet noise. However, the understanding of installed jets and their acoustics is still limited. Historically, the extra noise due to the wing installation was first noticed by Bushell³ when comparing an in-flight installed jet with a static isolated jet for a full-scale aircraft. The acoustic characteristics of installed jets have been extensively studied in the mid-1970s by experimentalists.^{2,4} The directivity of installation noise is found to be dipole-like and be sensitive to the distance from the jet centre line to the solid surface and from the jet exit to the surface trailing edge. To understand the noise mechanism, Ffowcs Williams and Hall observed that the far-field low frequency noise is amplified when a turbulent flow is installed close to a surface.⁵ They attributed this amplification to the scattering of the hydrodynamics pressure field near the solid surface edge. Lyu and Dowling confirmed this theory and developed a reliable prediction model⁶ based on the hydrodynamic wave scattering. This model demonstrated that the far-field sound amplification can be accurately predicted by incorporating the scattering of near-field hydrodynamic evanescent waves using Amiet's approach.⁷ However, comprehensive unsteady flow data of installed jets is currently not available for development and validation of low-order acoustic source models. High-fidelity numerical simulation is therefore used to fulfill this mission, since it is relatively difficult to achieve time-accurate flow measurements.

LES, as a high-fidelity simulation method, has been successfully used to predict the noise generated from isolated turbulent jet flows.⁸ Recent growth of computational power and development of numerical algorithms has enabled the simulation of industrial-level propulsive jets with complex geometries by resolving large-scale turbulent motions.⁹ Recently, the flow and noise from an UHBP engine installed under a wing was well simulated using a hybrid LES-RANS method.¹¹ The far-field noise was successfully predicted and agreed with the far-field acoustic measurements. However, it is difficult to completely separate the overall installation effects for such complex configuration, including the scattering of the linear hydrodynamic instability wave, the changes of jet mixing noise source and any effects due to unsteady wing lift. In this context, simulations on simplified canonical cases are necessary in order to isolate these installation effects and to better understand the individual noise mechanisms. Furthermore, near-field flow and pressure measurements also exist to validate such numerical computations in detail.

In this paper, LES has been performed on two jet configurations: an isolated jet and a jet installed below a flat plate. The plate is placed in the linear hydrodynamic region of the jet flow,¹⁰ which avoids nonlinear flow interactions. This is intended to include the installation noise only from the scattering of hydrodynamic instability waves. The simulation data has been compared with the experimental measurements following the validation metrics proposed by Bridge and Wernet.¹² The installation effects are then discussed from the aerodynamic and acoustic points of view.

II. Jet Configurations and Operating Conditions

To isolate jet installation effects, a canonical case was designed to be a single stream jet beneath a flat plate. The configuration is shown in Fig. 1 with a three-dimensional view of a x-y plane for jet flows and acoustics with coordinates system illustrated. Three parameters are used to control the position of the jet relative to the flat plate: H represents the vertical distance from jet nozzle centre line to plate surface and Lrepresents the distance from nozzle exit plane to plate trailing edge. The nozzle is located in the middle span of the plate and W is the half span length. The jet operates at a Mach number of 0.6, which is the typical bypass flow speed of future UHBP aeroengines. The Reynolds number based on nozzle diameter and jet velocity is around 7×10^5 . For this configuration, the jet flow barely scratches the trailing edge of the plate without touching the plate underneath surface. Flow impingement is avoided, such that the downstream jet mixing noise sources remain unaffected. Additional noise source is introduced by the scattering of linear hydrodynamic wave from the plate trailing edge. For comparison, an isolated jet was chosen with the same nozzle geometry and is operated at the same flow Mach number. The operating conditions and jet configurations are summarized in Table 1.



Figure 1. Installed jet configuration with a x-y plane cutting through the plate and jet flow

jet config.	M_j	L/D	H/D	W/D
installed jet	0.6	4	1	7
isolated jet	0.6	-	-	-

Table 1. Jet configuration and operating conditions

III. Numerical Methods

A. Flow Solver

The solver⁹ is a compressible, finite volume and edge-based solver utilizing dual meshes. It solves the unsteady Navier-Stokes equations on unstructured meshes and, hence, is capable of modelling complex geometries of any shape using a variety of cell topologies. The spatial discretisation is achieved using a second order kinetic-energy preserving (KEP) scheme¹³ with a 4th order numerical smoother adapted for convective fluxes,

$$F_{ij}^{c,n} = F_{ij,KEP}^n - \frac{1}{2}\varepsilon |A_{ij}^{c,n}| [L(Q_j) - L(Q_i)]$$
(1)

where $F_{ij,KEP}^n$ is the kinetic energy preseving fluxes $[\bar{\rho}\bar{u}^n, \bar{\rho}\bar{u}\bar{u}^n + \bar{p}\bar{n}, \bar{\rho}\bar{H}\bar{u}^n]$, and the overbar represents the arithmetic averaging operator using the values in the adjacent mesh elements *i* and *j*. The KEP scheme itself is numerically stable and non-dissipative, which is suitable for LES computation. Previous tests using homogeneous decaying turbulence with hexahedral, tetrahedral, and prism elements showed that the KEP scheme was less sensitive to grid types, which enables LES to be performed on hybrid structured-unstructured meshes. The second term in Eq. 1 is the numerical smoother. The parameter ε is used to control numerical smoothing in the simulation. This is minimized in the jet flow zone and is increased along with the grid expansion to form a sponge zone near the boundaries to prevent wave reflections. Second-order backward differencing is used for physical time marching. Implicit physical time stepping is made possible through the use of dual time stepping. A 4th order Runge-Kutta method is used in each pseudo time step with CFL = 1. The physical time step is 0.0016 D/U_j . The total sampling time is 293 D/U_j .

LES is used to resolve the turbulent jet plume with under-resolved scales modelled by the WALE SGS model.¹⁴ Boundary layers near the nozzle wall are modelled using the standard SA (Spalart Allmaras) RANS turbulence model.¹⁵ The RANS stress tensor τ_{ij}^{RANS} is hybridized with the SGS stress tensor τ_{ij}^{SGS} using a blending function f based on modified wall distance.⁹

$$\tau_{ij}^{turb} = f\tau_{ij}^{SGS} + (1-f)\tau_{ij}^{RANS} \tag{2}$$

Turbulent flow profiles are therefore generated inside the nozzle by RANS without turbulent velocity fluctuations in streak structures resolved near the wall. The steep velocity gradient of turbulent profiles introduces strong Kelvin-Helmholtz instabilities, which naturally trigger rapid transition into three dimensional structures downstream of the nozzle lip within 0.1D. No significant effects on near/far-field acoustics are observed except a tonal component introduced by the transition process. The solver has been extensively validated on a range of jet flows.⁹ Parallel performance is achieved using MPI and ParMetis grid partition-

ing, showing almost linear scaling over 10,000 cores. The parallel I/O is also made efficient by using HDF5 library, each core can visit the same file simultaneously without blocking.

B. Computational Domain and Mesh

Figure 2 shows the computational domain. It is of conical shape with a radial size of $30D_j$ at the inlet plane at $x = -15D_j$, and $50D_j$ at the outlet plane at $x = 100D_j$. It contains two zones: LES and sponge zones. The LES zone starts from $3D_j$ upstream and extends to $30D_j$ downstream of the nozzle exit in the axial direction, with a radial size of $7D_j$. The rest of the domain is filled with sponge zones, where a high level of smoothing is applied to reduce any numerical reflections from computational boundaries. Total temperature and pressure are imposed at the nozzle inlet. Far-field conditions are specified at the upstream boundary and side cylindrical boundary surfaces while static pressure is specified at the downstream boundary.



Figure 2. Computational domain of jet simulation

Hexahedral cells are used for the isolated jet simulation. The grid line aligns with the shear-layer trajectories to provide better resolution. The grid gradually expands in the axial direction following jet spreading rate. The mesh resolution along the lipline is shown in Table 2. The y^+ is around 1 near the nozzle wall and x^+ is around 7 at the nozzle exit. For the installed jet simulation, the same hexahedral cells are maintained in the jet plume. The plate surface is meshed with a quad-dominant mesh from where prism layers are extruded. Further refinement on the plate surface mesh is made near the nozzle and jet plume because the small-scale turbulence and high-frequency acoustics are generated there. Outside of the jet plume, tetrahedral cells are used to resolve the near-field acoustics. The position of the interface between the hex-meshed jet plume zone and the tet-meshed acoustics zone are carefully adjusted. The adjustment is based on the criterion the aspect ratio of the hexahedral mesh on the interface is close to 1, as the tetrahedral cells connected to the interface are isotropic. The interface radius R are chosen to be $R\Delta\theta \approx \Delta R \approx \Delta x$. This makes a smooth transition in size from jet plume hexahedral mesh to acoustics tetrahedral mesh. The hybrid mesh is shown in Fig. 3. The mesh statistics is listed in Table 3. The current grid density is chosen according to our best practice guidelines¹⁶ obtained by simulating a large number of jets from canonical to industrial complexity levels. The grid independence and azimuthal grid spacing sensitivity have been tested in previous research.¹⁷ The total number of grid points varied from 18 to 50 million and the azimuthal grid number varied from 120 to 180. They showed the gird independent results in flow statistics and far-field acoustics. This grid independence is also confirmed by other researchers,¹⁸ from 10 to 64 million. Therefore, the current mesh size should be enough to fulfil the task in the current simulation.

Table 2. Grid spacing distribution along lip line

x/D	0	1	2	5	10	20	30
D/dx	80	75	70	50	35	20	10
D/dr	591	450	350	200	100	60	50



Figure 3. Computational mesh of the installed jet

Table 3. Mesh statistics $(\times 10^6)$

	N_{tex}	N_{pyr}	N_{prism}	N_{hex}	N_{cell}
Isolated jet	0	0	0	34.94	34.94
Installed jet	30.46	0.26	0.02	17.89	48.64

C. Far-Field Sound Prediction

Sound at far-field observer locations is predicted by performing surface integration at a retarded time, which accounts for the propagation time spent from source to observer, following the Ffowcs William-Hawkings (FW-H) equation. A general convective FW-H formulation¹⁹ is used in this paper by setting ambient fluid velocity to zero. The volume integration is removed by enclosing all the quadrupole sources within the FW-H surfaces. The FW-H surfaces are placed in the irrotational hydrodynamic region to prevent any nonlinear hydrodynamic contaminations on acoustic predictions. The placement follows the proposed criterion: turbulent intensity less than 0.25% and normalised vorticity magnitude less than 0.05% at the FW-H surfaces.⁹

Figure 4(a) shows the FW-H surface placement in the flow and acoustic field of installed jets. To assure a robust and convergent far-field sound prediction, three sets of FW-H surfaces (shown in blue, red and green) are placed at different radial distances in the irrotational region away from turbulent jet plume. Axisymetrical conical surfaces are used for the isolated jet, while additional surfaces are devised around the flat plate for installed jets to enclose the extra sound sources introduced by jet-surface interactions. Figure 4(b) shows that the conical surfaces merge with the plate-wrapping surfaces, forming the complete set of FW-H surfaces for the installed jet. Unstructured elements are used to discretise the FW-H surfaces. In the simulation, unsteady flow data is recorded on the centroids of these surface elements for acoustic postprocessing. This far-field sound prediction procedure has been widely tested in our previous jet noise simulations.^{9,11}



(a) FW-H surfaces in flow and acoustic fields

(b) FW-H surface configurations



IV. Experimental Techniques

The experiments were performed in the anechoic Doak Laboratory (DOAK) within the Institute of Sound and Vibration Research, at the University of Southampton, UK. The DOAK jet facility is approximately $11m \times 7m \times 6m$ in size and is anechoic down to 400 Hz, shown in Fig. 5.

Near-field acoustic measurements were made using a traversable azimuthal near-field array, containing eight equally-spaced 1/4-inch microphones. They were positioned at eight different axial locations along the



Figure 5. Anechoic Doak Laboratory jet facility

jet $(0 \le x/D \le 7)$. Both polar and azimuthal measurements of the acoustic far-field were performed using a semi-circular traversable array populated with five equally-spaced microphones at 45° intervals located at a minimum distance of 50D from the nozzle exit (i.e. when the array was positioned at $\phi = 90^{\circ}$). The polar observer angles ranged between $40^{\circ} \le \phi \le 130^{\circ}$ at 10° intervals. The far-field acoustic data were corrected to 1 m-lossless values to account for spherical propagation and atmospheric attenuation.²⁰ More detail about acoustic test setup can be found in the thesis of Lawrence.²¹

Velocity measurements were carried out using a constant temperature anemometry (CTA) system. Dantec 55P11 single-probes were used to record the unsteady velocity. Axial and radial traverses using only one sensor were performed to survey the jet single-point statistical moments. To measure the joint moments, two hot-wire (HW) probes were mounted on two independent traverse systems. A more detailed description of the CTA system, the traverse setup and the instrumentation used in the aerodynamic experiments are provided by Proenca et al.^{22,23}

V. Results

A. Overview of Flow Field

Figure 6 shows instantaneous Q-criterion surfaces of the installed jet with acoustic waves in the background from the LES. The flow and acoustics are well resolved in the simulation. Hairpin vortices roll up in the jet plume and grown in size as they move downstream. When a plate is installed near the jet, interactions occur in both hydrodynamics and acoustics. The hydrodynamic interactions are relatively weak for the current configuration: the installed jet flow slightly scrapes the plate trailing edge without significant modification of flow structures, as seen in the close-up view. This weak impact on jet hydrodynamics will be further analysed in the sections of flow statistics and space-time correlations by comparison with the isolated jet. However, strong interactions are observed in acoustics. First, jet noise generated by shear layer near the nozzle is shielded above and reflected under the plate. Second, a new sound source is introduced around the trailing edge (TE). This is because near-field evanescent hydrodynamic waves are scattered by the plate TE and converted into propagating acoustics. The TE scattering noise propagates into the forward arc, as seen in Fig. 4(a) and 6. These acoustic effects will be discussed quantitatively in the sections of near-field spectra and far-field acoustics.



Figure 6. Instantaneous flow and acoustics in installed jets from the LES: Q-criterion iso-surfaces coloured by axial velocity with time derivative of pressure as background contours

B. Flow Statistics

Figure 7 shows the radial profiles of both isolated and installed jet mean velocities at different axial locations in the upper x-y plane, where the difference between installed and isolated jets are available. The LES prediction achieves a good agreement with the axial component of velocity measured by the hot wires, shown in Fig. 7(a). The plate installation appears to have a negligible effect on axial velocity. A slight acceleration is seen to occur around the plate trailing edge (at $x/D_j = 4$) and immediately downstream of the trailing edge in Fig. 7(a). Figure 7(b) shows the radial velocity profiles at various axial locations. Negative radial velocity out of jet plume (r/D > 1) indicates that ambient flows are entrained into the jet plume for the isolated jet. For the installed jet, the radial velocity above the plate (x/D < 4 and r/D > 1) becomes zero. The jet entrainment is restricted by the presence of the plate and a radial expansion occurs around the plate trailing edge (x/D = 4 and 0.5 < r/D < 1).

Figure 8 shows the radial profiles of the velocity fluctuation rms. Again, the LES agrees well with hot wire measurements, shown in Fig. 8(a). The turbulent fluctuations are slightly suppressed by the plate due to the acceleration seen near the plate trailing edge. The magnitude of the radial fluctuations is also reduced



Figure 7. Radial profiles of time-averaged velocities at x/D = 0, 2, 4, 6, 8, 10 for both isolated and installed jets: red circles, Hot wire data for the isolated jet; blue squares, Hot wire data for the installed jet; red solid lines: LES data for the isolated jet; blue dashed lines: LES data for the installed jet.

under the plate due to the restricted nature of the flow. Finally, slightly higher turbulence fluctuations are observed downstream of the plate at $x/D_j = 6, 8, 10$ compared to the isolated jet. This is caused by the flow acceleration upstream of the trailing edge and the subsequent radial expansion downstream of the plate TE.



Figure 8. Radial profiles of velocity fluctuations at x/D = 0, 2, 4, 6, 8, 10 for both isolated and installed jets: red circles, Hot wire data for the isolated jet; blue squares, Hot wire data for the installed jet; red solid lines: LES data for the isolated jet; blue dashed lines: LES data for the installed jet.

C. Space-Time Correlations

As suggested by Bridge and Wernet,¹² the LES has also been validated by exploring the 2nd order space-time correlation of velocity field, mathematically defined as,

$$R_{ij}(\mathbf{x},\zeta,\tau) = \frac{\overline{u'_i(\mathbf{x},t)u'_j(\mathbf{x}+\zeta,t+\tau)}}{\sqrt{u'^2_i(\mathbf{x})}\sqrt{u'^2_j(\mathbf{x}+\zeta)}}$$
(3)

The turbulence integral scales are calculated from these correlations and can be used to inform future turbulence and acoustic modelling. Figure 9(a) shows the comparison of space-time correlations of axial velocity for different axial separations $\zeta = (\xi, 0, 0)$ at x/D = 8 and r/D = 0.5, where the experimental measurements are available. For both the isolated and installed jets, the peak locations of each axial separation are well captured by the LES despite the peak value being lower for some of the separations. The underprediction of the peak values could be caused by the short sampling length of the LES (the sampling length is only around 1/100 of the measurement) or the subgrid dissipation. Since these correlations along the nozzle lip line can be collapsed well by scaling with the shear layer width δ_{β} and jet velocity U_j ,²³ experimental measurement at a single axial location is therefore sufficient to validate the simulation quality at different axial locations in the shear layer. Figure 9(b) demonstrates this scaling of correlations $R(\mathbf{x}, \zeta = (\xi, \mathbf{0}, \mathbf{0}), \tau = \mathbf{0})$ using shear layer width δ_{β} with the LES data, while a best-fit curve from the isolated jet measurement is shown for reference. Comparing the installed and isolated jets, the plate effects do not appear to affect the jet significantly for this configuration. The correlations at x/D = 4 and x/D = 8 collapse onto one curve for both installed and isolated jets and are slightly lower than the experimental best-fit curve. This indicates that the predicted length scale is smaller than the $0.31\delta_{beta}$ value provided by the experiment. Overall, an encouraging agreement is found between the hot wire measurement and the LES prediction of space-time correlations.



(a) R_{11} with axial separations ξ at x/D=8 and r/D=0.5



(b) R_{11} with axial seprations ξ at $\tau = 0$

Figure 9. Comparison of axial-velocity space-time correlation R_{11} between hot wire and LES data

To further examine the installation effects on jet turbulence, space-time correlations are explored for both axial velocities, shown in Fig. 10, and radial velocities, shown in Fig. 11. The reference point is located at x/D = 4 and r/D = 0.5 inside the shear layer directly under the plate trailing edge, where the largest differences bewtween the isolated and installed jets are expected. Both axial and radial separations are investigated based on this reference point. For the axial separations, axial and radial velocity correlations of the installed jet increases slightly above that of the isolated before $\xi/D = 0.5$. This is because flow accelerates around the plate trailing edge. The velocity correlation decays slightly faster in installed jets for radial separations, because jet spreading is confined by the plate. In general, no significant difference in the turbulent structures is seen between the isolated and installed jets, indicating negligible non-linear hydrodynamic interactions. However, noticeable modifications to the linear hydrodynamic and acoustic waves can be seen from near-field pressure spectra, which are discussed in the next section.



Figure 10. Axial-velocity space-time correlation R_{11} at x/D = 4 and r/D = 0.5 for isolated and installed jets



Figure 11. Radial-velocity space-time correlation R_{22} at x/D = 4 and r/D = 0.5 for isolated and installed jets

D. Near-Field Spectra

Comparisons are made between the experimental measurements and LES predictions to validate both the near-field velocity and pressure for the isolated jet. The velocity is normalised by the nozzle exit jet velocity for LES and experiment. Two velocity spectra are plotted in Fig. 12(a) at the two locations x/D = 2 and 8 along the nozzle lip line r/D = 0.5: one before and the other after the potential core end. The two velocity

spectra cross at around St = 0.25. This is because large-scale turbulence structures are generated after the jet potential core collapses, leading to an increase of low-frequency energy. The decay exponents of these turbulence spectra are around -5/3 at high frequencies. This indicates that this flow has an inertial range that is close to the scaling of isotropic turbulence. The LES captures this spectral shape and the same crossing point as those of the hot-wire measurements.

The near-field pressure spectra at x/D = 2 for two radial positions r/D = 1 and 2 are compared for the isolated jet in Fig. 12(b). Excellent agreement is achieved between microphone measurements and LES predictions. There are two regimes in these pressure spectra. The hump at low frequencies (St < 1) is caused by hydrodynamic evanescent waves, whereas the high-frequencies (St > 1) corresponds to acoustics. As they move out radially, the hydrodynamic evanescent waves decay exponentially and the acoustic waves decays with $1/r^2$.



Figure 12. Velocity and pressure spectra in the near-field of isolated jet

For the installed jet, pressure spectra on the lower side of the plate surface are shown in Fig. 13. The LES predictions are compared with experimental measurements at three probe locations. Overall, encouraging agreement is found between the LES and experimental measurements. The spectra shape and the trends of spectra shape change with probe location are well captured by the LES. Figure 13(b) shows a wavenumber decomposition of pressure fluctuations for each frequency along the plate surface centre line. Clearly, two propagation regimes can be seen from the plot, separated by a sonic line. As indicated by the acoustic dispersion relationship between wavenumber and frequency,²⁴ the energy above the sonic line corresponds to the waves of a phase speed larger than the sound speed c_0 . These waves are acoustic, which are able to propagate to the far field. The energy under the sonic line corresponds to waves with a subsonic phase velocities, which are related to the evanescent hydrodynamic waves.

Since near-field pressure azimuthal modes can be used to model scattering noise,⁶ they are compared



Figure 13. Frequency and wavenumber spectra of pressure on the plate surface

using the LES data of isolated and installed jets at the axial location of the plate trailing edge (x/D = 4). The azimuthal decomposition of the near-field pressure spectra is calculated as

$$\hat{p}(x,r,m,f) = \int_0^T \int_{-\pi}^{\pi} p(x,r,\theta,t) e^{i(m\theta - 2\pi ft)} d\theta dt$$
(4)

where T is the total sampling length, m is azimuthal mode number and f is frequency. The power spectral density (PSD) of the first four azimuthal modes are shown in Fig. 14 with normalisation by the reference acoustic pressure level, $p_{ref} = 2\mu Pa$. The azimuthal modes are significantly amplified in the mid frequency range 0.1 < St < 1 as the hydrodynamic waves are scattered by the plate trailing edge. The magnitude of amplification tends to increase towards the higher azimuthal modes. Figure 14(a) shows the spectra of the first four azimuthal modes. The amplitudes of azimuthal modes m = 2 and 3 of installed jets reach around the same level as those of the mode m = 0 and 1 of the isolated jets at around St = 0.4. Higher azimuthal modes of the near-field pressure spectra become important when the plate TE is introduced in the linear hydrodynamic region. This is further illustrated in Fig. 14(b), as more energy is distributed into higher azimuthal modes between St = 0.1 and 1.

E. Far-Field Sound

The far-field noise is predicted using the FW-H method for both jets. The observer angle ϕ is defined in Fig. 2. Figure 15 shows the sound spectra in the far-field at two polar observer angles $\phi = 40^{\circ}$ and 90° . The acoustic measurement of installed jet was performed at Ma = 0.5 and the mixing and scattering noise are scaled to Ma = 0.6 following Ma^8 and Ma^4 respectively at polar angle 90° and joined together at St = 3. Uncertainties from both Ma scaling and acoustic measurements are plotted in error bars. In the region between St = 0.3 - 0.5, the mixing and scattering noise contribute at a similar level, therefore simple



Figure 14. Azimuthal modes of near-field pressure at x/D = 4 and r/D = 2 for both isolated and installed jets

scaling with Ma^8 results in larger uncertainties. The predicted far-field sound agrees with the experimental measurements within the uncertainty range for installed jets at $\phi = 90^\circ$. The underprediction of isolated jet noise at low frequencies at $\phi = 90^\circ$ could be caused by inconsistent inlet turbulence levels between the LES and experiment, as well as short sampling length. This is part of our future research. Obvious installation effects are seen at $\phi = 90^\circ$ in Fig. 15(b). At low frequencies (St < 0.5), a large SPL increase at low frequencies in excess of 10dB can be observed compared to the isolated jet. This noise increase is caused by the jet-surface interaction source. LES prediction captures this jet-surface interaction noise very well. At high frequencies (St > 0.5), noise is shielded above the plate, which results in a lower SPL, while noise is reflected under the plate, which leads to a slightly higher SPL. LES predictions match the experimental data at both shielded and unshielded sides in high-frequency range (St > 0.5) with a mesh resolution limit up to around St = 2. At the lower observer angles $\phi = 40^\circ$, only isolated jet noise measurments are available. Good agreement has also been achieved between the LES and the experimental data. The jet alone noise, however, is dominant in this observation angle, and the installation effects become less obivoius as reported by other researchers.²

VI. Conclusion

In this paper, LES has been successfully performed on both the isolated and installed jets to investigate installation effects. Validation has been achieved by comparing LES thoroughly with experimental data from both hot-wire flow and microphone pressure measurements. Regarding the flow statistics, the LES shows a good agreement with experimental data in axial velocity profiles at x/D = 0, 2, 4, 6, 8 and 10. The entrainment of the jet flow is seen to be restricted by the presence of the plate and the turbulent fluctuations are slightly suppressed in the vicinity of the plate TE. It is found in general that the installation effects are



Figure 15. Far-field sound spectra at the polar angles of $\phi = 40^{\circ}$ and 90° for the isolated and installed jets

relatively small in the near-field flow statistics for this particular jet installation configuration L/D = 4 and H/D = 1. This is also confirmed by the space-time correlations of axial and radial velocities. Space-time correlations are validated by the hot-wire measurements. The LES slightly under-predicts some correlation peak values but well captures the peak locations for each spatial separation. For near-field spectra, LES captures the shape of velocity spectra and agrees well with experimentally measured pressure spectra. Using LES data, azimuthal and wavenumber decompositions were performed on the near-field pressure spectra. The azimuthal decomposition indicates that the contributions from higher azimuthal modes increase at the frequency range of 0.1 < St < 1 when the plate is present. The wavenumber decomposition along the centre line of plate under-surface distinguishes the energy distributions between the propagating acoustic and evanescent hydrodynamic waves near the trailing edge. For the far-field sound, the installation effects are obvious at the observer polar angles of $\phi = 90^{\circ}$. The LES accurately predicts the jet-surface interaction noise at the low frequencies St < 0.5 as well as the plate shielding and reflection effects at the high frequencies 0.5 < St < 2. This well-validated LES database will be used in the future to understand installed jet noise mechanisms and inform low-order model development.

Appendix: Experimental Uncertainty

Regarding aerodynamic CTA measurements, calibration equipment, instrumentation, and experimental conditions play a role in the uncertainty of a velocity sample. The hot-wire calibration is one of the major sources of systematic error. A dedicated, automatic calibrator was used in this work. The error associated with the calibrator unit suggested by the manufacturer is less than $\pm 0.5\%$ of the nominal velocity. Additionally, there is also uncertainty related to the linearisation of the calibration data. A quartic polynomial was used to fit the data and an error analysis was performed. It has been seen that the error is lower than

 $\pm 0.5\%$ of the nominal velocity for all points measured during the calibration procedure.

The uncertainties regarding instruments used to measure ambient and flow properties (e.g. jet and chamber static pressures, temperatures and relative humidities) are of less importance in comparison to the uncertainties discussed above. In this category, errors due to temperature variations during an experiment are dominant. Flow temperature fluctuations were measured using a thermometer mounted close to the hot-wire probe. It is expected that errors due to variations in flow and ambient properties do not exceed 1% of the sample velocity.²⁵ Therefore, the total errors intrinsic to the CTA system is taken to be within $\pm 1.5\%$ of the sample velocity. The uncertainty of the second-order moment (e.g. turbulence intensity) due to systematic errors is then $\pm 3\%$.

Probe positioning is another source of uncertainty. The traverse system and the hot-wire probe holder were aligned to the jet nozzle using a laser pointer. The laser pointer was mounted parallel to the jet nozzle and the traverse position was adjusted continuously until the hot-wire probe was seen to traverse ten jet diameters along the laser beam axis. Several mean velocity profiles ranging from the nozzle exit to ten diameters downstream were used to estimate the difference between the jet geometric axis and the measured axis. It was then seen that the difference between measured and geometric axis was 0.5° . This angle was used to correct the position of the hot-wire, so the uncertainty associated with probe positioning is small. More information about the traverse alignment procedure and definition of geometric and measured axis are presented by Proenca,²² in sections 3.1.2 and 3.2.3.

The errors discussed above are in agreement with the relative expanded uncertainty in a velocity sample equals to $\pm 1.5\%$ suggested by the CTA manufacturer. In order to verify this assumption, data from three different campaigns were compared. The three sets of data were acquired in a span of four years, but the same nozzle and traverse systems were used in all three tests. In Fig.16, mean velocity and turbulence intensity profiles from these three campaigns are shown. Data shown as black circles were acquired using a single-wire calibrated with a manual calibrator, red crosses were obtained using a cross-wire and automatic calibrator, and blue triangles used a single-wire calibrated with the same automatic calibrator. All profiles shown were measured at x/D = 8, as positioning errors are more obvious than in positions close to the jet nozzle exit. It is seen from these plots and analysis of profiles at other axial locations that the variation of the mean velocity and the root-mean-square of the velocity fluctuations are within $\pm 1.5\%$ in respect to the jet exit velocity. The uncertainties are plotted at y/D = 0 in the Fig. 7(a) and 8(a). The measurement errors are almost negligible for mean velocity.

Regarding the unsteady wall pressure data and the far-field acoustic measurement, repeat tests were conducted revealing a repeatability error of $\pm 0.5\%$ dB across the entire frequency range of interest. As for the microphone hardware itself, the systematic errors add up to less than $\pm 0.05\%$ dB. The *Ma* scaling of scattering and mixing noise leads to an uncertainty of $\pm 0.5\%$ dB. In the joint region of these two types of noise spectra, $0.3 \le St \le 0.5$, the scaling uncertainties are within $\pm 2\%$ dB. This is estimated by comparing the scaling of Ma^4 for scattering noise and Ma^8 for mixing noise.



Figure 16. (a) Mean velocity and (b) turbulence intensity of an M = 0.6 jet measured in three different experimental campaigns at the Doak Lab.

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