





Physical Chemistry Chemical Physics

Accepted Manuscript

This article can be cited before page numbers have been issued, to do this please use: G. R. Bacanu, G. Hoffman, M. Amponsah, M. Concistre, R. J. Whitby and M. H. Levitt, *Phys. Chem. Chem. Phys.*, 2020, DOI: 10.1039/D0CP01282C.



This is an Accepted Manuscript, which has been through the Royal Society of Chemistry peer review process and has been accepted for publication.

Accepted Manuscripts are published online shortly after acceptance, before technical editing, formatting and proof reading. Using this free service, authors can make their results available to the community, in citable form, before we publish the edited article. We will replace this Accepted Manuscript with the edited and formatted Advance Article as soon as it is available.

You can find more information about Accepted Manuscripts in the <u>Information for Authors</u>.

Please note that technical editing may introduce minor changes to the text and/or graphics, which may alter content. The journal's standard <u>Terms & Conditions</u> and the <u>Ethical guidelines</u> still apply. In no event shall the Royal Society of Chemistry be held responsible for any errors or omissions in this Accepted Manuscript or any consequences arising from the use of any information it contains.





ARTICLE TYPE

Cite this: DOI: 00.0000/xxxxxxxxxxx

Fine structure in the solution state 13 C-NMR spectrum of C_{60} and its endofullerene derivatives †

George Razvan Bacanu*a, Gabriela Hoffmana, Michael Amponsaha, Maria Concistrèa, Richard J. Whitbya and Malcolm H. Levitta

Received Date
Accepted Date

This article is licensed under a Creative Commons Attribution-NonCommercial 3.0 Unported Licence.

Open Access Article. Published on 13 May 2020. Downloaded on 5/13/2020 9:48:08 AM.

DOI: 00.0000/xxxxxxxxxx

The 13 C NMR spectrum of fullerene C_{60} in solution displays two small "side peaks" on the shielding side of the main 13 C peak, with integrated intensities of 1.63% and 0.81% of the main peak. The two side peaks are shifted by -12.6 ppb and -20.0 ppb with respect to the main peak. The side peaks are also observed in the 13 C NMR spectra of endofullerenes, but with slightly different shifts relative to the main peak. We ascribe the small additional peaks to minor isotopomers of C_{60} containing two adjacent 13 C nuclei. The shifts of the additional peaks are due to a secondary isotope shift of the 13 C resonance caused by the substitution of a 12 C neighbour by 13 C. Two peaks are observed since the C_{60} structure contains two different classes of carbon-carbon bonds with different vibrational characteristics. The 2:1 ratio of the side peak intensities is consistent with the known structure of C_{60} . The origin and intensities of the 13 C side peaks are discussed, together with an analysis of the 13 C solution NMR spectrum of a 13 C-enriched sample of C_{60} , which displays a relatively broad 13 C NMR peak due to a statistical distribution of 13 C isotopes. The spectrum of 13 C-enriched C_{60} is analyzed by a Monte Carlo simulation technique, using a theorem for the second moment of the NMR spectrum generated by J-coupled spin clusters.

1 Introduction

The 13 C solution NMR spectrum of C_{60} fullerene is widely believed to contain a single peak. Indeed the observation of a single 13 C peak in the solution NMR of C_{60} was one of the key pieces of evidence for its highly symmetrical structure 1,2 . All sixty 13 C sites are chemically equivalent and have an identical chemical shift, as opposed to less symmetrical fullerenes such as C_{70} which displays 5 peaks in the 13 C spectrum 1 .

Nevertheless, close examination of the high resolution ^{13}C spectrum of C_{60} in solution reveals two small additional peaks at a slightly lower chemical shift with respect to the main peak, in an intensity ratio of 2:1 (Fig. 1). Pairs of side peaks are also observed in the ^{13}C solution NMR spectrum of endofullerenes, in which the C_{60} cages encapsulate guest molecules such as H_2 and H_2O (Fig. 2). The ^{13}C chemical shifts of the fullerene cage sites are perturbed by the endohedral guests within the cavity of C_{60} , leading to two main peaks (for empty and filled fullerene molecules) and two pairs of small side peaks, each with an amplitude ratio

of 2:1.

The pairs of side peaks may be attributed to minor isotopomers of C_{60} with two 13 C nuclei in neighbouring carbon sites. The substitution of the abundant 12 C isotope at a particular site by the heavier 13 C isotope leads to secondary isotope shifts in the resonance frequencies of neighbouring 13 C sites $^{3-8}$. This shift arises since the vibrational wavefunctions of the participating nuclei are perturbed by the introduction of a nuclide with an increased mass. Since the structure of C_{60} contains two different classes of carbon-carbon bond with different vibrational characteristics, the 13 C spectrum of C_{60} and its derivatives contains two side peaks. As discussed below, the 2:1 intensity ratio of the two side peaks reflects the relative abundance of the C-C bond types in C_{60} . Note that the side peak structure is *not* caused by $^{13}C_{-}^{-13}$

The aim of this paper is to provide an interpretation of the observed spectral structure in the ^{13}C NMR of C_{60} fullerene and its endofullerene derivates. The ^{13}C NMR spectrum of ^{13}C -enriched C_{60} is also presented, and analyzed using an approximate Monte Carlo simulation method exploiting a theorem for the second moment of the NMR spectra of J-coupled spin clusters.

^a Departament of Chemistry, University of Southmapton, Southampton SO17 1BJ, UK. Tel: +44 23 80596753; E-mail: g.r.bacanu@soton.ac.uk; mhl@soton.ac.uk

 $[\]dagger$ Electronic Supplementary Information (ESI) available: Fitting procedure, spin-lattice relaxation, chemical shift referencing, mass spectrometry. See DOI: 10.1039/cXCP00000x/

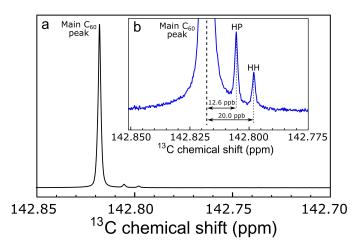


Fig. 1 (a) ^{13}C NMR spectrum of 25 mM C_{60} in deuterated orthodichlorobenzene (ODCB-d₄), at a magnetic field of 16.45 T and a temperature of 295 K (sum of 856 transients). The main C_{60} peak is at 142.818 ppm relative to TMS. (b) Expanded view of the base of the main C_{60} peak, showing the assignment of the side peaks to ^{13}C pairs sharing either a HP (hexagon-pentagon) or a HH (hexagon-hexagon) bond. The secondary ^{13}C isotope shifts are $^{1}\Delta \simeq$ 12.6 ppb for a HP $^{13}\text{C}_2$ pair and $^{1}\Delta \simeq$ 20.0 ppb for a HH $^{13}\text{C}_2$ pair.

2 Methods

Fullerene C_{60} was purchased from Materials Technologies Research Ltd. (Cleveland, Ohio, USA) and purified by sublimation in house. A solution was prepared by dissolving 23.4 mg of sublimed C_{60} powder in ~ 1.1 mL of ortho-dichlorobenzened4 (ODCB-d4, Sigma-Aldrich), adding $\sim 10~\mu L$ of tetramethylsilane (TMS) for chemical shift referencing and $\sim 100~\mu L$ of tris(trimethylsilyl)silane for temperature calibration 9 . The solution was filtered to remove any undissolved impurities and degassed by bubbling O_2 -free N_2 gas through the solution for 10 min

The endofullerenes $H_2@C_{60}$ and $H_2O@C_{60}$ were prepared by molecular surgery techniques $^{10-14}$. Figure 2(a) shows the ^{13}C NMR spectrum of $H_2@C_{60}$ in ODCB-d₄, with a "filling factor" (i.e. fraction of filled cages) of 87.7%. The solution of $H_2O@C_{60}$ in ODCB-d₄ used for Fig. 2(b) contained $H_2O@C_{60}$ with a filling factor of 78.6%.

The $^{13}\text{C}\text{-enriched}$ fullerene was purchased as 20-30% $^{13}\text{C}\text{-enriched}$ powder from MER Corporation (Tucson, Arizona, USA) and sublimed in-house. 15.5 mg of sublimed powder was dissolved in 1 mL of ODCB-d₄ plus \sim 10 μL of TMS. The solution was filtered to remove undissolved impurities and degassed by O₂-free N₂ bubbling for 10 mins.

All NMR experiments were performed at a field of 16.45 T in a Bruker Ascend 700 NB magnet fitted with a Bruker TCI prodigy 5 mm liquids cryoprobe and a Bruker AVANCE NEO console.

3 Results

The ^{13}C solution NMR spectrum of C_{60} is shown in figure $\,$ 1. The two side peaks are at $\Delta\delta_1=-12.6\,\text{ppb}$ and $\Delta\delta_2=-20.0\,\text{ppb}$ relative to the main ^{13}C peak. In all measurements presented the widths of peaks (main and side peaks) at half-maximum

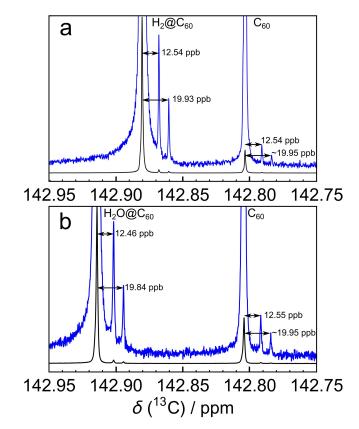


Fig. 2 13 C NMR spectra of \sim 25 mM solutions of (a) H₂@C₆₀ (filling factor 87.7%, sum of 416 transients) and b) H₂O@C₆₀ (filling factor 78.6%, sum of 272 transients) in ODCB-d₄ at a temperature of 298 K. For each species, a pair of side peaks on the shielding side of the main 13 C peak is clearly visible.

height are between 0.128 Hz and 0.272 Hz, the bulk of measurements having line widths under 0.200 Hz. The integrated amplitudes of the side peaks, relative to the main $^{13}\mathrm{C}$ peak, are $a_1/a_0=1.63\pm0.15\,\%$ and $a_2/a_0=0.81\pm0.08\,\%$ respectively (see the ESI† for the fitting procedure). The ratio of the integrated amplitudes for the two side peaks is given by $a_1/a_2=2.02\pm0.01.$ Solutions of endofullerenes display an identical fine structure in their $^{13}\mathrm{C}$ NMR peaks, as shown in figure 2.

The shifts of the side peaks relative to the main peak have a weak temperature-dependence, as shown in figure 3. The temperature-dependent shifts fit well to a linear model over the explored temperature range, of the form $\Delta \delta_i = \Delta \delta_i^0 + (\mathrm{d}\Delta \delta_i/\mathrm{d}T)T$ with $i \in \{1,2\}$. The fit parameters for C₆₀ and two endofullerenes are given in Table 1. The outer side peak has a stronger temperature dependence than the inner peak and is slightly more affected by the presence of an endohedral molecule.

Enrichment of C_{60} with ^{13}C obscures the side peak structure. A ^{13}C NMR spectrum of a solution of 20%-30% ^{13}C -enriched C_{60} in ODCB- d_4 is shown in figure 4(b). Instead of two discrete side peaks, a relatively broad lineshape is observed with a width of about 40 ppb. The broad peak exhibits a distinct shoulder on the deshielding ("downfield") side of the peak, at a chemical shift corresponding to the main ^{13}C peak in natural-abundance C_{60} (see ESI† for chemical shift referencing).

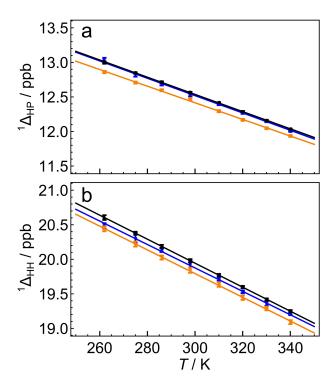


Fig. 3 Temperature dependence of secondary 13 C isotope shifts for C_{60} (black), $H_2@C_{60}$ (blue) and $H_2O@C_{60}$ (orange), for (a) HP the first side peak, and (b) HH the second side peak. The solid lines are best linear fits of the form $^1\Delta(T) = ^1\Delta^0 + (d^1\Delta/dT)T$, where the fit parameters are given in Table 1. The side peak shifts $\Delta\delta_1$ and $\Delta\delta_2$ are related to the isotope shifts by a sign change (see equation 3).

The 13 C relaxation time constants T_1 were also measured (see ESI†). The 13 C T_1 of the natural- abundance C_{60} sample was determined to be 16.6 ± 0.3 s at a temperature of 295 K and magnetic field of 16.45 T. The 13 C T_1 of the 20-30% 13 C-enriched sample was found to be slightly shorter under the same conditions $(14.8\pm0.2 \text{ s})$.

4 Discussion

4.1 Natural abundance spectra

The molecular structure of C_{60} is composed of sixty carbon atoms at the vertices of a truncated icosahedron (see figure 5). The carbon atoms are arranged in 20 hexagonal and 12 pentagonal rings. There are two distinct types of carbon-carbon bonds, with different bond lengths $^{15-18}$. There are 30 carbon-carbon bonds which are on the shared edges of two hexagons, and which are called here HH bonds 19,20 . The HH bonds are significantly shorter than the 60 bonds which are shared between a hexagon and a pentagon, and which are called here HP bonds 19,20 .

The internuclear distances for the two bond types are estimated to be $r_{\rm HH}=139.5\pm0.5\,{\rm pm}$ and $r_{\rm HP}=145.2\pm0.2\,{\rm pm}$, as determined by X-ray diffraction ¹⁵, gas-phase electron diffraction ¹⁶, solid-state NMR ¹⁷, and neutron diffraction ¹⁸.

The structure of C_{60} provides a ready *qualitative* interpretation of the natural abundance ¹³C spectrum. The three species contributing most of the intensity to the natural abundance ¹³C spectrum are denoted [¹³C₁]- C_{60} , [HP-¹³C₂]- C_{60} , and [HH-¹³C₂]- C_{60} (see figure 5). [¹³C₁]- C_{60} molecules contain ¹³C sites with no im-

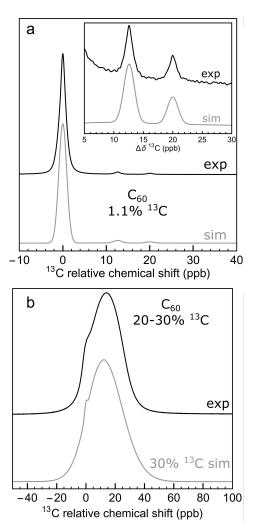


Fig. 4 (a) 13 C NMR spectrum of 25 mM solution of C_{60} in ODCB-d₄ (sum of 856 transients); (b) 13 C NMR spectrum of 20 mM of 13 C-enriched C_{60} (20-30% 13 C) in ODCB-d₄ (sum of 16 transients). Spectra are taken at 16.45 T and 295 K. Black lines show experimental data. The grey lines show the results of Monte Carlo simulations using a 13 C abundance of (a) 1.1% and (b) 30%. The horizontal axes depict the 13 C chemical shift relative to that of the main C_{60} peak.

mediate ^{13}C neighbours, while [HP. $^{13}\text{C}_2$]-C60 and [HH. $^{13}\text{C}_2$]-C60 molecules contain $^{13}\text{C}_2$ pairs separated by a HP bond and a HH bond respectively. On average, there are twice as many [HP. $^{13}\text{C}_2$]-C60 molecules as [HH. $^{13}\text{C}_2$]-C60 molecules, since there are twice as many HP bonds as HH bonds.

The [$^{13}C_1$]- C_{60} isotopomer contributes a single ^{13}C peak to the ^{13}C spectrum, at the main peak chemical shift (figure 5 d). The $^{13}C_2$ pairs in the [HP- $^{13}C_2$]- C_{60} and [HH- $^{13}C_2$]- C_{60} isotopomers also contribute a single peak each (see figure 5 e, f), since the ^{13}C sites are magnetically equivalent by symmetry. The ^{13}C - ^{13}C J-coupling between magnetically equivalent spins has no direct spectral consequences in isotropic solution 21 . The spectral contribution from each [HP- $^{13}C_2$]- C_{60} molecule is twice as large as the contribution from each [$^{13}C_1$]- C_{60} molecule.

The frequencies of the $[HP^{-13}C_2]$ - C_{60} and $[HH^{-13}C_2]$ - C_{60} peaks are influenced by secondary isotope shifts. The substitution of a ^{12}C nucleus by a more massive ^{13}C nucleus modifies the vibra-

Table 1 Linear regression parameters for the temperature dependence of the secondary 13 C isotope shifts for C_{60} and the endofullerenes $H_2@C_{60}$ and $H_2O@C_{60}$ (Fig. 3). The side peak shifts $\Delta\delta_1$ and $\Delta\delta_2$ are related to the isotope shifts by a sign change (see equation 3).

parameter	C ₆₀	$H_2@C_{60}$	$H_2O@C_{60}$
¹ Δ _{HP} (298 K)/ppb	12.56 ± 0.01	12.54 ± 0.03	12.46 ± 0.02
$^{1}\Delta_{\mathrm{HP}}^{0}/\mathrm{ppb}$	16.28 ± 0.05	16.29 ± 0.11	16.03 ± 0.06
$({\rm d}^1 \Delta_{\rm HP}/{\rm d}T)$ / $10^{-3}~{\rm ppb}~{\rm K}^{-1}$	$\textbf{-12.47} \pm \textbf{0.15}$	$\textbf{-12.56} \pm \textbf{0.34}$	$\textbf{-12.04} \pm \textbf{0.20}$
¹ Δ _{HH} (298 K)/ppb	19.98 ± 0.02	19.93 ± 0.05	19.84 ± 0.04
$^{1}\Delta_{\mathrm{HH}}^{0}/\mathrm{ppb}$	25.16 ± 0.10	24.96 ± 0.18	24.94 ± 0.14
$(d^{1}\Delta_{\rm HH}/dT) / 10^{-3} \ \rm ppb \ K^{-1}$	-17.38 ± 0.30	-16.96 ± 0.58	-17.17 ± 0.44

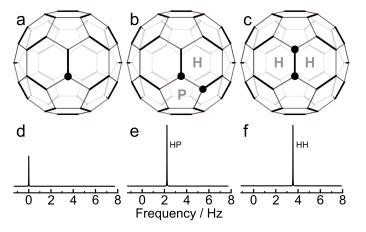


Fig. 5 Three isotopomers of C_{60} , with the positions of ^{13}C sites marked by a filled circle: (a) $[^{13}C_1]$ - C_{60} ; (b) $[HP^{-13}C_2]$ - C_{60} ; (c) $[HH^{-13}C_2]$ - C_{60} . The hexagonal and pentagonal carbon rings are marked. (d-e) Simulations of the associated ^{13}C spectra at a magnetic field of $16.45\,\mathrm{T}$, using artificial Lorentzian lineshapes and secondary isotope shifts taken from experiment (Fig. 1). The spectral amplitudes contributed by each $^{13}C_2$ molecule is twice as large as for each $^{13}C_1$ molecule. The $^{13}C^{-13}C$ J-coupling does not influence the spectra of the $^{13}C_2$ isotopomers, since the ^{13}C nuclei are in magnetically equivalent sites.

tional wavefunctions of the molecule and influences the chemical shift of neighbouring ¹³C nuclei. The primary mechanism of secondary isotope shifts is as follows 3-7: The chemical shift of a nucleus depends on the molecular electronic wavefunction which is a function of internuclear distances; the distances between bonded atoms oscillates because of vibrational motions and, within the Born-Oppenheimer approximation, the electronic wavefunction adjusts rapidly to the changing positions of the nuclei. The observed chemical shift is an average over the internuclear distances explored by the nuclear vibrational wavefunction. However, nuclear vibrational wavefunctions depend on the nuclear mass; heavier nuclei possess wavefunctions which are more strongly localised towards the potential minimum of the vibrational coordinate whereas lighter nuclei explore a wider range of vibrational coordinates. If the vibration is anharmonic, the mean nuclear position also depends on the nuclear mass. Hence, onebond isotope shifts depend on the frequency and anharmonicity of the relevant vibrational mode. Since the two types of bonds in C₆₀ have different bond lengths and vibrational frequencies, it is not surprising that the associated isotope shifts are different as well. The experimental results indicate that the secondary isotope shift is larger for two 13 C nuclei separated by the shorter HH bond, than when the nuclei are separated by the longer HP bond.

Unfortunately, the most widely used definition of the secondary isotope shift 6 suffers from a counter-intuitive sign convention. Nevertheless, we persist with it in this article. The secondary isotope shift of a 13 C site induced by swapping the "light" isotope L A of a neighbouring atom A with a "heavy" isotope H A is defined as follows 6 :

$${}^{1}\Delta^{13}C(A) = \delta^{13}C({}^{L}A) - \delta^{13}C({}^{H}A)$$
 (1)

The following condensed notation is introduced for the one-bond secondary isotope shifts in fullerenes:

$$^{1}\Delta_{HP} = \delta^{13}C([^{13}C_{1}]-C_{60}) - \delta^{13}C([HP^{-13}C_{2}]-C_{60})$$

$$^{1}\Delta_{HH} = \delta^{13}C([^{13}C_{1}]-C_{60}) - \delta^{13}C([HH^{-13}C_{2}]-C_{60})$$
(2)

The chemical shifts of the two side peaks, relative to the main ¹³C peaks, are therefore given by

$$\Delta\delta_{1} = -{}^{1}\Delta_{HP}$$

$$\Delta\delta_{2} = -{}^{1}\Delta_{HH}$$
 (3)

The HP and HH peak assignments are shown in figures 1 and 5. The amplitudes of the two side peaks are in the ratio 2:1 since C_{60} contains twice as many HP bonds as HH bonds. This is in agreement with experiment.

The interpretation of the natural-abundance 13 C spectrum of C_{60} therefore appears to be straightforward. The main 13 C peak derives from 13 C₁ isotopomers of C_{60} , while the two side peaks derive from the two types of 13 C₂ isotopomers, which have abundances in the ratio of 2:1. However, closer inspection reveals one small point that is not so easy to explain. The ratio of the integrated amplitude of the outer (HH) side peak to that of the main peak is observed to be $a_2/a_0 = 0.81 \pm 0.08\%$. What explains this intensity ratio? A naive theory runs as follows: The outer side peak is attributed solely to the [HH- 13 C₂]-C₆₀ isotopomer, and the main peak to the $[^{13}$ C₁]-C₆₀ isotopomer. Consider two neighbouring carbon sites in C₆₀, separated by a HH bond. The probability of a carbon atom having a 13 C nucleus is x, while the probability of the carbon having a 12 C nucleus is 1-x. The probability of ei-

ther one of the two sites being 13 C is therefore given by 2x(1-x). Both 13 C₁ isotopomers contribute to the intensity of the main 13 C peak. The probability of *both* sites being 13 C, on the other hand, is x^2 . The 13 C resonance of these 13 C₂ isotopomers is subject to the secondary isotope shift and hence they contribute to the intensity of the HH side peak. Since a 13 C₂ isotopomer contributes twice the spectral intensity of a 13 C₁ isotopomer, the amplitude ratio of the HH side peak to the main peak is predicted by this argument to be $2 \times x^2/2x(1-x) = x/(1-x)$. This is given approximately by x for small x. Since the natural abundance of 13 C is $x \simeq 1.1\%$, the predicted amplitude ratio is also 1.1%. However, this prediction is outside the confidence limits of the observed a_2/a_0 ratio, which is $0.81 \pm 0.08\%$. The discrepancy is significant.

As shown below, a more sophisticated theory of the spectral structure is required to explain the observed intensity ratio of the side peaks to the main peak. Alternative combinatorial approach is given in the ESI†.

Figure 3 shows that the isotope shifts $^1\Delta_{HP}$ and $^1\Delta_{HH}$ decrease as the temperature is increased. This may be attributed to the increased representation of excited vibrational states as the temperature is increased; excited vibrational wavefunctions are less influenced by the mass of the vibrating particles than the ground vibrational state 5 . It is not fully understood why the HH bond exhibits a stronger temperature-dependence than the HP bond. This may be due to the fact that the HH bond is shorter than the HP bond and has a higher force constant. The vibrational excited states of the HH bond are therefore less accessible, causing an increase in temperature to have a proportionately higher effect on the populations of excited vibrational wavefunctions.

Figure 3 and Table 1 show that the isotope shifts are slightly reduced in magnitude when an endohedral molecule is present. The larger the endohedral molecule, the larger the change in the isotope shift. The mechanism of this effect is currently unknown, but it may be associated with a modification of the C_{60} vibrational modes by the endohedral moiety, an effect which has been detected in Raman spectroscopy²².

4.2 ¹³C-enriched fullerene and spectral simulations

The 13 C NMR spectrum of 13 C-enriched C_{60} is shown in figure 4 b and displays a relatively broad lineshape with a shoulder on the deshielding side of the peak. The position of the shoulder coincides with the position of the main peak in natural abundance C_{60} (see ESI†).

There is a small difference in the spin-lattice relaxation rate constants of the natural-abundance and 13 C-enriched samples (see ESI†). This difference is presumably due to the role of 13 C- 13 C dipole-dipole couplings. However, the small relaxation rate difference is insufficient to explain the spectral broadening in the 13 C spectrum of 13 C-enriched 13 C. The broad lineshape originates from coherent interactions, such as secondary isotope shifts and 13 C- 13 C J-couplings.

A detailed understanding of this spectral structure presents a formidable theoretical and computational challenge. At an enrichment level of 30%, the most abundant isotopomers of C_{60} contain around 19 13 C nuclei 25 . An accurate simulation of even

a single spin system of this size is at the very limit of current computational techniques. An accurate simulation would require the calculation of an astronomical number of such spectra, some of which involve much larger spin systems.

Nevertheless, the rather featureless lineshape in figure 4(b) indicates that a *detailed* lineshape analysis is unnecessary in this case. It is possible to achieve a reasonable qualitative understanding of the lineshape through a Monte Carlo technique aided by plausible approximations and assumptions.

The simulation technique involves the following steps: (i) Generation of a computer representation of an ensemble of ¹³C configurations, distributed according to the desired ¹³C abundance; (ii) Identification of one or more distinct ¹³C *clusters* within each configuration; (iii) Prediction of spin interaction parameters (chemical shifts and J-couplings) for each ¹³C cluster; (iv) Calculation of the spectral lineshape for an individual ¹³C cluster with the predicted interaction parameters; (v) Summation of the simulated lineshapes over all ¹³C clusters, leading to the total NMR spectrum:

$$S(\omega) = N_{\text{config}}^{-1} \sum_{c=1}^{M} S_c(\omega)$$
 (4)

Here $S_c(\omega)$ is the simulated NMR spectrum for an individual cluster, M is the number of clusters and the total number of configurations is denoted $N_{\rm config}$.

The details of the individual steps are as follows:

- 1. Generation of an ensemble of ^{13}C configurations. The atomic coordinates and bonding network for C_{60} are set up in the *Mathematica* symbolic software platform 26 . A ^{13}C or ^{12}C nucleus is randomly assigned to each of the 60 carbon sites using a stochastic function with probability x for ^{13}C and 1-x for ^{12}C . Typical calculations involve around $N_{\rm config}=10000$ random configurations. This is far smaller than the total number of possible configurations but sufficient to define the main features of the NMR spectrum.
- 2. Identification of ¹³C clusters. The next step is to identify ¹³C clusters within each computer-generated configuration, by which we mean groups of ¹³C spins which interact sufficiently strongly with each other to be treated as distinct spin systems, while interactions between spins in different clusters are ignored. Quantum chemistry calculations on C_{60} have predicted that the J_{CC} coupling between all pairs of ¹³C nuclei separated by more than 3 bonds are smaller than $1 \, \text{Hz}^{23,24}$. Since $1 \, \text{Hz}$ corresponds to $\sim 6 \, \text{ppb}$ for $^{13} \text{C}$ in a magnetic field of 16.45 T, which is smaller in magnitude than the one-bond secondary isotope shifts, we define a ¹³C cluster as follows: A set of ¹³C nuclei for which (i) each nucleus is connected to at least one other member of the cluster by no more than 3 bonds, and (ii) for which every nucleus is at least 4 bonds away from any ¹³C nuclei which are outside the cluster. For example, the configurations sketched in figure 6(a,b) each contain one ¹³C cluster (containing 3 and 4 ¹³C nuclei respectively), while the configuration in figure 6(c) contains one cluster of 2 13C nuclei and a second cluster of 4 13C nuclei. Note that a cluster does not neces-

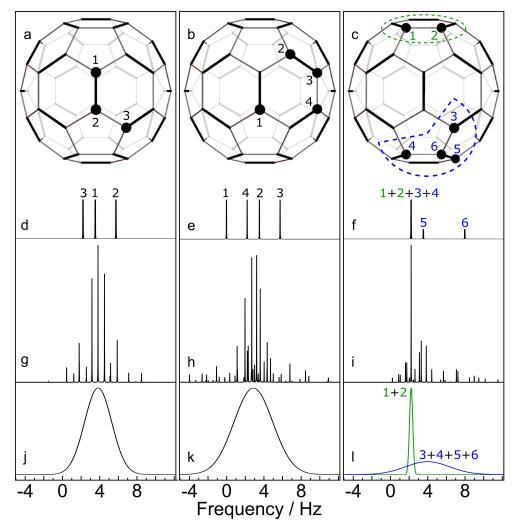


Fig. 6 Simulated NMR spectra for three selected C_{60} configurations, at a magnetic field of 16.45 T. 13 C nuclei are shown by filled circles. Cases (a) and (b) contain a single 13 C cluster. Case (c) contains two 13 C clusters. (d-f) Stick spectra showing the predicted 13 C chemical shifts, perturbed by the one-bond secondary isotope shifts from neighbouring 13 C nuclei; (g-h) Accurate spin dynamical computations of the NMR spectra, including the predicted chemical shifts and J-couplings from quantum chemistry calculations 23,24 . (i-l) Approximate simulations of the NMR spectra for each cluster using equation 7. All vertical scales are arbitrary.

sarily consist of 13 C atoms which are directly bonded to each other. The number of 13 C nuclei in an individual cluster c is denoted N_c .

3. Spin interaction parameters for a 13 C cluster. Simulation of the NMR spectrum of a 13 C cluster requires knowledge of the spin interaction parameters (chemical shifts and J-couplings). For the J-couplings between pairs of 13 C in the cluster we use the results of published quantum chemistry calculations 24 . For the chemical shifts, an additive model is assumed for the one-bond secondary isotope shifts. Suppose that a given 13 C site i has $n_{\rm HP}(i)$ 13 C neighbours separated by a HP bond, where $n_{\rm HP}(i) \in \{0,1,2\}$, and $n_{\rm HH}(i)$ 13 C neighbours separated by a HH bond, where $n_{\rm HH}(i) \in \{0,1\}$. The total secondary isotope shift of the given 13 C site is assumed to be given by

$$^{1}\Delta_{i} \simeq n_{\rm HP}(i)^{1}\Delta_{\rm HP} + n_{\rm HH}(i)^{1}\Delta_{\rm HH} \tag{5}$$

where the values $^1\Delta_{HP}=12.6\,\mathrm{ppb}$ and $^1\Delta_{HH}=20.0\,\mathrm{ppb}$ are assumed in the calculations. All two-bond and higher secondary isotope shifts are ignored. The total secondary isotope shift has a maximum value of $2^1\Delta_{HP}+^1\Delta_{HH}=45.2\,\mathrm{ppb}$, and a minimum value of 0. These two values approximately bound the lineshape of the ^{13}C -enriched sample of C_{60} , shown in figure 4(b).

The isotope shift of each 13 C site i may be converted into a frequency shift relative to the main 13 C peak by using the relationship

$$\Omega_i = -{}^{1}\Delta_i \times \boldsymbol{\omega}^0 \tag{6}$$

where the (signed) 13 C Larmor frequency is $\omega^0 = -\gamma B^0$, γ is the magnetogyric ratio of 13 C and B^0 is the magnetic field 21 . Equation 6 takes into account the non-intuitive sign convention for the secondary isotope shift (equation 3) 6 .

4. *Spectral lineshape for a* ¹³*C cluster.* Having identified a ¹³C cluster and estimated all chemical shifts and J-couplings, the

This article is licensed under a Creative Commons Attribution-NonCommercial 3.0 Unported Licence

Open Access Article. Published on 13 May 2020. Downloaded on 5/13/2020 9:48:08 AM.

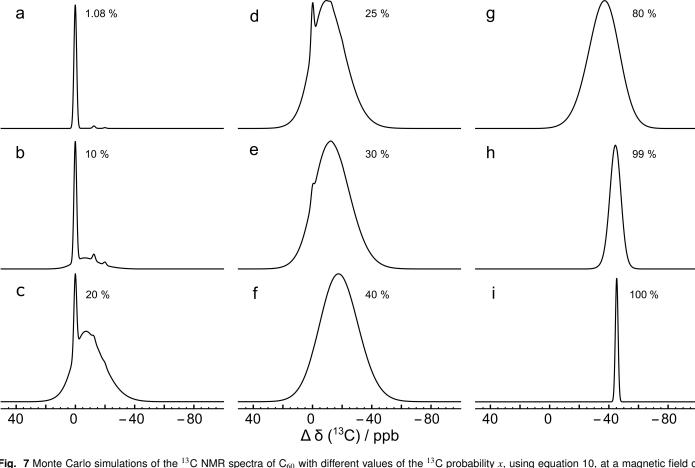


Fig. 7 Monte Carlo simulations of the 13 C NMR spectra of C_{60} with different values of the 13 C probability x, using equation 10, at a magnetic field of $B^0 = 16.45$ T. Each simulation was performed by analyzing 10000 random C_{60} configurations. The spectra are normalised to the same peak height for clarity. Simulations for more values of x are shown in the ESI†.

next step is to simulate the ¹³C spectrum.

In the case of small cluster dimension N_c , it is possible to use accurate simulation techniques, such as those used in the *SpinDynamica* software package ²⁷. Some results are shown in the middle row of figure 6. In each case the simulations show a complex spectrum containing many individual peaks.

Accurate simulations of this type are not feasible for large values of N_c , and in any case this level of spectral detail is unresolved in the experimental spectra of 13 C-enriched C_{60} . We therefore use an approximate expression for the 13 C cluster spectrum $S_c(\omega)$, which derives from a moment analysis of the NMR spectrum, as described in the Appendix. The cluster spectrum is approximated by the following Gaussian function:

$$S_c^{\star}(\omega) = N_c (2\sigma_c)^{-1/2} \exp\left\{-\frac{(\omega - \overline{\Omega}_c)^2}{2\sigma_c}\right\}$$
 (7)

where the standard deviation of the Gaussian function is as follows:

$$\sigma_c = N_c^{-1} \sum_{i=1}^{N_c} (\Omega_i - \overline{\Omega}_c)^2$$
 (8)

and the mean resonance offset frequency of a cluster is

given by

$$\overline{\Omega}_c = N_c^{-1} \sum_{i=1}^{N_c} \Omega_i \tag{9}$$

Equation 7 evaluates very rapidly even for large cluster dimension N_c .

Figure 6 compares some cluster spectra simulations using equation 7 (lower row) with exact spin-dynamical simulations (middle row). The approximate method omits the fine details of the spectra but represents the centre frequency and width of the cluster spectra accurately. The great advantage of this approximation technique is that it is computationally feasible for large numbers of clusters each containing many ¹³C nuclei, which is out of the question for accurate spin-dynamical techniques.

Equation 8 predicts a zero-width Gaussian when all 13 C nuclei in the cluster have identical chemical shifts (magnetic equivalence). A small empirical line-broadening term is included in this case, matching the experimental linewidth of the natural-abundance C_{60} peak.

The 13 C NMR spectrum of C₆₀ may therefore be treated approximately, for any 13 C probability x, by generating a large number of configurations using a Monte Carlo method, and summing the

cluster contributions to the spectrum according to

$$S^{\star}(\boldsymbol{\omega}) = N_{\text{config}}^{-1} \sum_{c=1}^{M} S_{c}^{\star}(\boldsymbol{\omega})$$
 (10)

where the individual spectral contributions are given by equation 7.

Figure 7(a) shows the result for x = 1.1%, which corresponds to the incidence of ¹³C at natural abundance. The two side peaks are just visible, and are seen more clearly in the expanded view of figure 4(a), where the simulated and experimental spectra are compared. The correspondence is good.

Why is the ratio between the main 13 C peak and the second side peak not equal to $x \simeq 1.1\%$, as expected by a naive argument (see above)? The cluster analysis explains this by considering the role of the random 13 C occupancy of carbon sites which are 2 or 3 bonds away from the sites of interest. There are several ways to perform this analysis, all requiring care: The argument given below predicts the correct ratio using relatively few logical steps, but requires delicate reasoning. An alternative analysis is given the ESI†, this considers the relative abundances of C_{60} isotopomers containing up to three 13 C nuclei, and provides an estimate of the peak ratio which is close, but not exactly equal, to the experimental ratio. The residual discrepancy is attributed to isotopomers with more than three 13 C nuclei.

Consider the main ¹³C peak. This derives predominantly from isolated 13 C nuclei. In the C₆₀ structure, there are 3 carbon sites which are one bond away from a given site, 6 sites which are 2 bonds away, and 8 sites which are 3 bonds away. Assuming that a given carbon site is occupied by ¹³C, there is a probability of $14x \simeq 15\%$ that at least one of the sites that are 2 or 3 bonds away are also occupied by ¹³C. The two ¹³C nuclei would, by the definition used in this article, belong to the same cluster. However, the spectral consequences of these additional ¹³C nuclei are minor, since the additional nuclei will (most likely) not have direct one-bond ¹³C neighbours themselves. Hence, the additional ¹³C nucleus does not experience a significant secondary isotope shift, and the cluster of two ¹³C nuclei has the same chemical shift as an isolated ¹³C nucleus, within the approximations used here. The amplitude of the ¹³C main peak is therefore largely unaffected by random pairs of ¹³C nuclei which are 2 or 3 carbon-carbon bonds distant from each other.

The situation is different for the $^{13}\text{C}_2$ pairs that give rise to the side peaks. A $^{13}\text{C}_2$ pair separated by a HH bond has 4 carbon sites which are one bond away, 8 sites which are 2 bonds away, and 8 sites which are 3 bonds away. There is a probability of $16x \simeq 18\%$ that at least one of the sites that are 2 or 3 bonds away are also occupied by ^{13}C . Unlike the case of isolated ^{13}C nuclei, an additional ^{13}C nucleus 2 or 3 bonds away has a large effect on the spectrum. The three ^{13}C nuclei form a single cluster, which has a broadened and shifted spectrum, relative to the spectrum of the isolated $^{13}\text{C}_2$ pair. This is because the additional ^{13}C nucleus does not itself have a directly-bonded neighbouring ^{13}C (except in rare circumstances), and therefore experiences a different secondary isotope shift to the directly-bonded $^{13}\text{C}_2$ pair. Hence about 18% of the intensity of a given side peak is transferred into a broadened

and shifted resonance. The result is a depletion in the intensity of the sharp side peak by $\sim 18\%$. This argument accounts accurately for the observed ratio in the relative intensities of the side peaks and the main peak in natural abundance C_{60} .

This effect is seen more clearly in figure 7(b), which shows a simulation for a 13 C probability of x = 10%. The broad resonance between the main peaks and the side peaks is obvious in this case.

Figure 7 shows that as the 13 C probability increases, the 13 C spectrum broadens and shifts in the shielding direction, with a shoulder at the main peak position persisting up to about x=30%. The shoulder is generated by 13 C nuclei that have no directly bonded 13 C partners themselves and which are also at least 3 bonds away from directly-bonded groups of 13 C nuclei. A simulation for x=30% matches the experimental spectrum of the 13 C-enriched C_{60} well, as shown in figure 4(b). This is in agreement with the enrichment level determined by mass spectrometry, which is also $x\sim30\%$ (see ESI†).

Figure 7 shows that the simulated spectra become narrower again when x exceeds 50%. This is because the isotope shifts of the 13 C sites become more uniform when most carbon sites in C₆₀ are occupied by 13 C. In the extreme case of x = 100%, the simulated spectrum is very sharp, since all 13 C sites have three 13 C neighbours, and experience the same secondary isotope shift of $2^1\Delta_{\rm HP} + ^1\Delta_{\rm HH} = 45.2$ ppb. All sixty 13 C nuclei are magnetically equivalent in this case.

5 Conclusion

The observation of a single, sharp 13 C NMR peak for solutions of C_{60} is one of the strongest pieces of evidence for its highly symmetrical molecular structure 1 . Our observations show that the solution-state 13 C NMR of C_{60} also displays two small side peaks, in the intensity ratio of 2:1. We interpret the side peaks as the signals from 13 C₂ isotopomers, which are displaced from the main 13 C peak by secondary isotope shifts. Two peaks arise since the C_{60} structure contains two types of carbon-carbon bonds, also in the incidence ratio of 2:1. Indeed the presence of two side peaks in the solution 13 C spectrum of C_{60} proves the presence of two different types of C-C bonds – a fact which was originally established by X-ray diffraction 15 , gas-phase electron diffraction 16 , neutron diffraction 18 and low-temperature solid-state NMR of 13 C labelled material 17 .

 13 C side peaks of similar origin are also observed for other symmetrical molecular compounds, such as ferrocene 28 .

The secondary isotope shifts become smaller when the temperature is increased. The positions of the side peaks are also influenced by the presence of an endohedral molecule, with the magnitude of the perturbation roughly correlated with the size of the endohedral moiety.

The solution 13 C NMR spectrum of 13 C-enriched C_{60} is broader than that of the natural abundance material. We have developed an algorithm for the simulation of C_{60} NMR spectra at arbitrary levels of 13 C enrichment. This uses a Monte Carlo approach, combined with a cluster identification algorithm, and an approximate spectral treatment based on a second moment analysis. This technique allows rapid approximate calculations of the NMR spectra of J-coupled spin clusters, even for large numbers

This article is licensed under a Creative Commons Attribution-NonCommercial 3.0 Unported Licence.

Open Access Article. Published on 13 May 2020. Downloaded on 5/13/2020 9:48:08 AM.

of coupled spins, and might be adapted to other problems in solution and solid-state NMR. The simulations agree well with the experimental spectrum of the ^{13}C -enriched sample. This analysis also explain why the outer side peak in natural-abundance C_{60} has an amplitude of 0.81% of the main peak, instead of the natural abundance ratio of 1.1%, which would be predicted by a naive argument. We expect that the ^{13}C NMR spectra of higher fullerenes such

We expect that the 13 C NMR spectra of higher fullerenes such as C_{70} will also display additional spectral structure due to $^{13}C_2$ isotopomers. In this case, more complex phenomena are anticipated since there are several groups of chemically inequivalent sites.

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

We thank Sally Bloodworth for experimental help. This research was supported by EPSRC (UK), grant codes EP/P009980/1, EP/P030491/1, EP/K00509X/1 and EP/T004320/1.

Appendix. Approximate NMR spectrum of Jcoupled spin clusters

Consider a cluster c containing N_c J-coupled spins-1/2, with chemical shifts δ_i and J-couplings J_{ij} , where $i, j \in \{1...N\}$. The rotating-frame spin Hamiltonian in isotropic solution is given by

$$H = H_{CS} + H_J \tag{11}$$

where the chemical shift and J-coupling terms are given by

$$H_{CS} = \sum_{i=1}^{N_c} \Omega_i I_{iz}; \quad H_J = \sum_{i < i}^{N_c} 2\pi J_{ij} \mathbf{I}_i \cdot \mathbf{I}_j$$
 (12)

and the resonance offset frequencies by

$$\Omega_i = -\gamma B^0 (\delta_i - \delta_{ref}) \tag{13}$$

The Hamiltonian may be written as follows:

$$H = H_0 + H_1 \tag{14}$$

where H_0 is defined as follows:

$$H_0 = \overline{\Omega}_c I_z \tag{15}$$

and the mean offset frequency for the cluster is defined in equation 9.

The term H_1 is given by

$$H_1 = H_J + \sum_{i=1}^{N_c} \Delta \Omega_i I_{iz}$$
 (16)

where $\Delta\Omega_i$ are resonance offsets with respect to the mean cluster frequency:

$$\Delta\Omega_i = \Omega_i - \overline{\Omega}_c \tag{17}$$

The NMR signal for the cluster (free-induction decay) is given

by

$$s_c(t) = (Q_{\text{obs}}|\exp(-i\hat{H}t)\rho(0))$$
 (18)

where \hat{H} is the commutation superoperator of the hamiltonian H, and the Liouville bracket is defined ²⁹:

$$(A|B) = \text{Tr}\{A^{\dagger}B\} \tag{19}$$

Since the Hamiltonian terms H_0 and H_1 commute, the cluster NMR signal may be written

$$s_c(t) = \left(Q_{\text{obs}} \exp(+i\hat{H}_0 t) \middle| \exp(-i\hat{H}_1 t)\rho(0)\right) \tag{20}$$

The spin density operator at the start of signal detection is denoted $\rho(0)$ and the observable operator is denoted $Q_{\rm obs}$. In an ordinary single-pulse NMR experiment, using quadrature detection, it is convenient to define these operators as follows²¹:

$$\rho(0) = -I_{y}$$

$$Q_{\text{obs}} = -iI^{-}$$
(21)

With this choice of observable operator the following commutation relationship holds:

$$\hat{H}_0|Q_{\rm obs}) = -\overline{\Omega}_c|Q_{\rm obs}) \tag{22}$$

and hence

$$\exp(-i\hat{H}_1t)|Q_{\text{obs}}) = \exp(+i\overline{\Omega}_c t)|Q_{\text{obs}})$$
 (23)

This leads to the following expression for the cluster NMR signal:

$$s_c(t) = g_c(t) \exp(i\overline{\Omega}_c t)$$
 (24)

where the function $g_c(t)$ is defined as follows:

$$g_c(t) = \left(Q_{\text{obs}} \middle| \exp(-i\hat{H}_1 t)\rho(0)\right) \tag{25}$$

The NMR spectrum of the cluster is given by the one-sided Fourier transform of the NMR signal:

$$S_c(\omega) = \int_0^\infty s_c(t) \exp(-i\omega t) dt$$
 (26)

which may be written as follows:

$$S_c(\omega) = G_c(\omega - \overline{\Omega}_c) \tag{27}$$

where the function $G_c(\omega)$ is the Fourier transform of $g_c(t)$:

$$G_c(\omega) = \int_0^\infty g_c(t) \exp(-i\omega t) dt$$
 (28)

Equation 27 shows that the cluster spectrum $S_c(\omega)$ may be derived from the function $G_c(\omega)$ by a simple frequency shift. The function $G_c(\omega)$ is centred around $\omega = 0$, while the spectrum $S_c(\omega)$ is centered around the mean resonance offset $\overline{\Omega}_c$.

An approximate expression for $G_c(\omega)$ is developed by a moment analysis. The use of spectral moments is known to be a powerful technique in broad-line solid-state NMR ³⁰, but has rarely been used for solution NMR. The *n*th moment $M_c^{(n)}$ of the real

$$M_c^{(n)} = \int_{-\infty}^{\infty} \operatorname{Re}\{G_c(\omega)\} \omega^n \, d\omega \tag{29}$$

From the properties of the Fourier transform³¹, the nth moment of the real part of the spectrum is proportional to the nth derivative of the time-domain signal at the time origin:

$$M_c^{(n)} = (-i)^n \left(\frac{d^n}{dt^n} g_c(t)\right)_{t=0}$$
 (30)

Repeated differentiation of equation 25 leads to the expression

$$\frac{\mathrm{d}^n}{\mathrm{d}t^n} s_c(t) = (-i)^n \left(Q_{\text{obs}} \middle| \hat{H}_1^n \rho(t) \right) \tag{31}$$

and hence a compact form for the *n*th spectral moment of $G_c(\omega)$:

$$M_c^{(n)} = -i(-1)^n (I^- | \hat{H}_1^n I_y)$$
(32)

For example, the n = 0 moment, which is equal to the integral of the spectrum, evaluates to:

$$M_c^{(0)} = -i(+i)(I_y|I_y) = N_c 2^{N_c-2}$$
 (33)

using equation 25.

This article is licensed under a Creative Commons Attribution-NonCommercial 3.0 Unported Licence.

Open Access Article. Published on 13 May 2020. Downloaded on 5/13/2020 9:48:08 AM.

The expression for the first moment of $G_c(\omega)$ involves the following terms:

$$\hat{H}_1 | I_y \rangle = \hat{H}_J | I_y \rangle + \sum_{i=1}^{N_c} \Delta \Omega_i \hat{I}_{iz} | I_y \rangle$$
 (34)

The first term vanishes since the J-coupling Hamiltonian commutes with the total angular momentum operator along an arbitrary axis:

$$\left[\mathbf{I}_{i} \cdot \mathbf{I}_{j}, I_{iy} + I_{jy}\right] = 0 \tag{35}$$

The commutation properties of the angular momentum operators lead to the following expression for the second term:

$$\hat{H}_1|I_y\rangle = \sum_{i=1}^{N_c} \Delta\Omega_i \hat{I}_{iz}|I_y\rangle = -i\sum_{i=1}^{N_c} \Delta\Omega_i |I_{ix}\rangle$$
 (36)

Hence the first spectral moment is given by

$$M_c^{(1)} = \sum_{i=1}^{N_c} \Delta \Omega_i (I^- | I_{ix}) = 0$$
 (37)

The first moment of $G_c(\omega)$ vanishes since each bracketed term is identical, and the sum of the resonance offsets, relative to the mean frequency of the cluster, is zero by definition:

$$\sum_{i=1}^{N_c} \Delta \Omega_i = 0 \tag{38}$$

The second moment is conveniently evaluated by rearranging equation 32 for n = 2:

$$M_c^{(2)} = -i(I^- \hat{H}_1 | \hat{H}_1 I_v)$$
 (39)

All terms involving the J-coupling term H_J vanish through the commutation relationship in equation 35. This leads through

equation 36 to the expression

$$M_c^{(2)} = \sum_{i,j=1}^{N_c} \Delta \Omega_i \Delta \Omega_j (I_{ix} | I_{jx})$$
(40)

Since the angular momentum operators of different spins are orthogonal, we get

$$M_c^{(2)} = 2^{N_c - 2} \sum_{i=1}^{N_c} \Delta \Omega_i^2$$
 (41)

The normalized second moment, defined as the ratio of the second and zeroth moments, is given by

$$\mathscr{M}_{c}^{(2)} = \frac{M_{c}^{(2)}}{M_{c}^{(0)}} = N_{c}^{-1} \sum_{i=1}^{N_{c}} \Delta \Omega_{i}^{2}$$
 (42)

which is equal to the mean-sum-square of the resonance offsets for all spins in the cluster, relative to the mean resonance offset.

Note that the J-couplings do not appear in the expression for the second moment. The second moment of the NMR spectrum of a given J-coupled spin cluster may therefore be calculated extremely rapidly using only the chemical shift values for all spins in the cluster. The situation is different for the case of dipole-dipole coupled solids ³⁰, since a commutation relationship of the type given in equation 35 does not apply for the dipole-dipole Hamiltonian.

The algorithm used in this paper uses the following Gaussian function as an approximation to the function $G_c(\omega)$:

$$G_c^{\star}(\boldsymbol{\omega}) = N_c (2\mathcal{M}_c^{(2)})^{-1/2} \exp\left\{-\frac{\pi \boldsymbol{\omega}^2}{2\mathcal{M}_c^{(2)}}\right\}$$
 (43)

where the normalized second moment is given by equation 42. This expression omits the fine details of the NMR spectrum but has correct values for the zeroth, first, and second moments. The approximate form of the spectral function $S_c(\omega)$ for a cluster of ¹³C spins, given in equation 7, is derived from equation 43 by using the expression for the second moment in equation 42, and the frequency-shift relationship in equation 27.

References

- 1 R. Taylor, J. P. Hare, A. K. Abdul-Sada and H. W. Kroto, *J. Chem. Soc., Chem. Commun.*, 1990, 1423–1425.
- H. W. Kroto, A. W. Allaf and S. P. Balm, *Chem. Rev.*, 1991, 91, 1213–1235.
- 3 H. Batiz-Hernandez and R. A. Bernheim, *Progress in Nuclear Magnetic Resonance Spectroscopy*, 1967, **3**, 63–85.
- 4 W. T. Raynes, A. M. Davies and D. B. Cook, *Molecular Physics*, 1971, **21**, 123–133.
- 5 C. J. Jameson, J. Chem. Phys., 1977, 66, 4983-4988.
- 6 P. E. Hansen, Progress in Nuclear Magnetic Resonance Spectroscopy, 1988, 20, 207–255.
- 7 M. Saunders, K. E. Laidig and M. Wolfsberg, J. Am. Chem. Soc., 1989, 111, 8989–8994.
- 8 P. Vujanić, Z. Meić and D. Vikić-Topić, *Spectroscopy Letters*, 1995, **28**, 395–405.

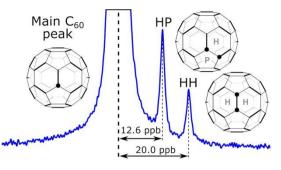
This article is licensed under a Creative Commons Attribution-NonCommercial 3.0 Unported Licence

Open Access Article. Published on 13 May 2020. Downloaded on 5/13/2020 9:48:08 AM

- 10 K. Komatsu, M. Murata and Y. Murata, *Science*, 2005, **307**, 238–240.
- 11 K. Kurotobi and Y. Murata, Science, 2011, **333**, 613–616.
- 12 A. Krachmalnicoff, M. H. Levitt and R. J. Whitby, *Chemical Communications*, 2014, **50**, 13037–13040.
- 13 A. Krachmalnicoff, R. Bounds, S. Mamone, S. Alom, M. Concistrè, B. Meier, K. Kouřil, M. E. Light, M. R. Johnson, S. Rols, A. J. Horsewill, A. Shugai, U. Nagel, T. Rõõm, M. Carravetta, M. H. Levitt and R. J. Whitby, *Nat Chem*, 2016, 8, 953–957.
- 14 S. Bloodworth, G. Sitinova, S. Alom, S. Vidal, G. R. Bacanu, S. J. Elliott, M. E. Light, J. M. Herniman, G. J. Langley, M. H. Levitt and R. J. Whitby, *Angewandte Chemie International Edition*, 2019, 58, 5038–5043.
- 15 W. I. F. David, R. M. Ibberson, J. C. Matthewman, K. Prassides, T. J. S. Dennis, J. P. Hare, H. W. Kroto, R. Taylor and D. R. M. Walton, *Nature*, 1991, 353, 147–149.
- 16 K. Hedberg, L. Hedberg, D. S. Bethune, C. A. Brown, H. C. Dorn, R. D. Johnson and M. D. Vries, *Science*, 1991, **254**, 410–412.
- 17 C. S. Yannoni, P. P. Bernier, D. S. Bethune, G. Meijer and J. R. Salem, *J. Am. Chem. Soc.*, 1991, **113**, 3190–3192.
- 18 F. Leclercq, P. Damay, M. Foukani, P. Chieux, M. C. Bellissent-Funel, A. Rassat and C. Fabre, *Phys. Rev. B*, 1993, **48**, 2748–2758.
- 19 B. Masenelli, F. Tournus, P. Mélinon, A. Pérez and X. Blase, J.

- Chem. Phys., 2002, 117, 10627-10634.
- 20 S. Díaz-Tendero, F. Martín and M. Alcamí, *Computational Materials Science*, 2006, **35**, 203–209.
- 21 M. H. Levitt, *Spin Dynamics. Basics of Nuclear Magnetic Resonance*, Wiley, Chichester, 2nd edn, 2007.
- 22 F. Cimpoesu, S. Ito, H. Shimotani, H. Takagi and N. Dragoe, *Phys. Chem. Chem. Phys.*, 2011, **13**, 9609–9615.
- 23 M. Jaszuński, K. Ruud and T. Helgaker, Molecular Physics, 2003, 101, 1997–2002.
- 24 L. B. Krivdin and R. H. Contreras, *Annual Reports on NMR Spectroscopy*, Academic Press, 2007, vol. 61, pp. 133–245.
- 25 M. S. Dresselhaus, G. Dresselhaus and P. C. Eklund, Science of Fullerenes and Carbon Nanotubes, Academic Press, New York, 1996.
- 26 S. Wolfram, *Mathematica: A System for Doing Mathematics by Computer*, Addison-Wesley, New York, 1991.
- 27 C. Bengs and M. H. Levitt, *Magnetic Resonance in Chemistry*, 2018, **56**, 374–414.
- 28 P. S. Nielsen, R. S. Hansen and H. J. Jakobsen, *Journal of Organometallic Chemistry*, 1976, **114**, 145–155.
- 29 J. Jeener, Advances in Magnetic and Optical Resonance, Academic Press, 1982, vol. 10, pp. 1–51.
- 30 M. Mehring, *High Resolution NMR Spectroscopy in Solids*, Springer-Verlag, Berlin Heidelberg, 1976.
- 31 R. N. Bracewell, *The Fourier Transform and Its Applications*, McGraw Hill, New Delhi, 3rd edn, 2014.

View Article Online DOI: 10.1039/D0CP01282C



The 13C NMR spectrum of C60 in solution showing the additional side peaks from double-13C isotopomers