

1 **TITLE**

2 **Column tests investigating the liquefaction of partially saturated loose non-plastic soils**

3

4 **AUTHORS**

5 **K.A Kwa¹, Y. Hu¹, J. Chen¹, Z. Chen² & D.W Airey¹**

6 **¹School of Civil Engineering, University of Sydney**

7 **²School of Civil Engineering, Shaoxing University, Shaoxing, Zhejiang 312000, China**

8

9 **ABSTRACT**

10 This study reports data and findings from shake table tests performed on **loosely compacted** unsaturated
11 well graded materials containing a wide range of particle sizes and significant fines contents of 18 to
12 28%. The results are useful for understanding the fundamental cyclic liquefaction behaviour of these
13 unsaturated well graded materials when subjected to vertical cyclic loading conditions relevant to
14 repetitive transport loading or during bulk cargo shipping transportation. Liquefaction was observed in
15 all the shake table tests performed on the well-graded materials, which were prepared at relative
16 densities of 50 to 60% and degrees of saturation ranging from 50% to 70%. Large settlements were also
17 observed in the columns of the well-graded materials, which resulted in significant increases in the
18 degree of saturation towards fully saturated states. Migration of fines throughout the well-graded
19 materials was also observed, which also contributed to settlement and resulted in different local
20 densities and fines contents throughout the column. The resulting build-up in pore pressures, settlements
21 and accompanying increases in degree of saturation and movement of moisture throughout are
22 presented and compared with shake table tests performed on columns of partially saturated clean sand
23 for which liquefaction was not observed.

24 **1. INTRODUCTION**

25 There is relatively limited data that describes the cyclic response of partially saturated soils as studies
26 have mainly focused on the cyclic response of either fully dry or fully saturated materials. Traditionally,
27 the worst cyclic soil responses are expected when the soil is either fully dry, and large settlements occur,
28 or the soil is completely saturated, and there is a large build up in pore pressure and decrease in effective
29 stress. The consensus that soils with intermediate degrees of saturation result in less critical behaviour
30 due to the role of matric suctions, has lately been questioned (Ghayoomi and McCartney, 2012). In
31 recent years there has been increasing interest in the seismic response of partially saturated soils as
32 during earthquake events they have been associated with significant compression (Stewart and Whang,

2003, Duku et al, 2008, Ghayoomi et al, 2011) and have been involved in liquefaction failures (Uzuoka et al, 2014; Okamura & Soga, 2006; Unno et al, 2008). Given that partially saturated soils also underlie much of the world's infrastructure, there is an evident need for well documented laboratory and field data to better understand their behaviour and to support rigorous risk assessment. Although there have been many recent studies of the cyclic behaviour of unsaturated soils in simple shear and triaxial tests there are limited data suitable to assess and validate the response of sophisticated numerical models for dynamic unsaturated behaviour. To address this deficiency, shake table tests on columns of partially saturated material have been performed in this study.

Background

It is well known that particle grading has an important influence on the susceptibility to liquefaction and that sands and silty sands are the most prone (Tsuchida, 1970). A large number of element tests, specifically investigating the effect of fines on the saturated cyclic liquefaction response of silty sands have been performed in the triaxial and simple shear apparatuses (Bouckovalas et al., 2003; Dash & Sitharam, 2009; Polito & Martin, 2011; Sadek & Saleh, 2007; Sadrekarimi 2013; Xenaki and Athanasopoulos, 2003; Carrera et al., 2011). There has been much less focus on the cyclic liquefaction behaviour of well-graded materials containing larger gravel sized particles, as these materials do not tend to liquefy as often as sands and silty sands. This is because these materials typically have higher permeabilities and therefore, are able to dissipate pore water pressures more quickly.

Nevertheless, a number of triaxial tests have been performed on saturated and unsaturated well-graded materials (Kimoto et al., 2011; Okamura & Soga, 2006; Unno et al, 2006; 2008, Uzuoka et al, 2014 Wang et al., 2015; Kwa & Airey, 2017; 2019), with a few specifically investigating the effect of fines on the cyclic liquefaction response of unsaturated well-graded materials (Unno et al, 2006; Kwa & Airey, 2017, 2019). If a significant amount of fines is present, the fines have been known to decrease these materials' drainage potential, resulting in cases where materials, containing gravel sized particles, used for reclaimed fill purposes have liquefied during earthquakes (Harder, 1997; Andrus, 1995; Cubrinovski et al, 2003, 2017). The migration of fines from the subgrade into railway ballast and highway pavements due to train and car traffic cyclic loading conditions is also known to reduce the drainage potential of ballast and pavement material, resulting in ballast and pavement degradation and large settlements of the infrastructure above (Alobaidi et al., 1996; Indraratna et al., 2011 Duong et al., 2014; Ebrahimi et al., 2014). Metallic ore bulk cargoes are another material containing a wide range of particle sizes from gravels down to silts and significant fines contents, as high as 28%, that are susceptible to liquefaction during shipping transportation when subjected to rocking motions from sea waves (IMSBC, 2013; Kwa & Airey, 2019). Due to the loading process, these metallic ores are in a relatively loose and in a partially saturated state when placed in the hold of the ship. If they liquefy during transportation, they can cause the ship to progressively tilt, become unstable and then capsize.

68 The mechanics leading to liquefaction of these unsaturated, well-graded materials, which are widely
69 used as reclaimed fill materials, railway ballast, pavement subbase materials, and are also similar in
70 grading to a number of shipped metallic ores, is not well understood. One of the main challenges is in
71 understanding the settlements, associated increases in the degree of saturation and migration of moisture
72 throughout the partially saturated material when they are subjected to cyclic loads.

73 Shake table tests are relatively simple model tests that have been widely used to model the 1g saturated
74 behaviour of sands when subjected to seismic loading conditions. In particular, shake tables have been
75 used to investigate the pore pressure responses and 1D settlements in sands (Yanagisawa, 1995; Yegain
76 et al., 2006, 2007; Ueng et al., 2006, 2010, 2017; Pathak et al., 2010, 2013) and to model the
77 displacements and strains of embankments and shallow foundations in sands (Koga et al., 1990; Toyota
78 et al., 2004; Sadrekarimi, 2013). In all of these shake table studies, increases in pore water pressures
79 and significant settlements were measured and reported once liquefaction had occurred. Some studies
80 also measured and observed an upwards flow of water and propagation of pore water pressures
81 throughout column of soil towards the surface once liquefaction had occurred (Ueng et al., 2017; Yang.,
82 2017). Some studies, including those performed by Kokusho (1999), Kokusho et al. (2002) and Ozener
83 et al. (2009), used shake table apparatuses to investigate pore water pressure generation in sand with
84 silts. However, in these studies, shaking was horizontal, and the silt and sand were separated into layers
85 and the effects of interlaying silt within a column of sand were investigated to determine their effect on
86 the upward flow of pore water.

87 Very few shake table tests have been reported on well-graded materials containing a mixture of particles
88 sizes from gravels down to silts. Shaking has also typically been applied to samples in the horizontal
89 direction, which is less relevant when modelling the cyclic soil response underneath pavements and
90 railway ballast subjected to repetitive vertically acting transport loading conditions, or in metallic ore
91 cargoes during shipping transportation. Some shake table tests and numerical analyses have been
92 performed on unsaturated well-graded samples of iron ore fines (TWG, 2013, Munro & Mohajerani,
93 2016, Ju et al., 2016) to observe whether the material lost its strength and flowed when subjected to
94 cyclic loads relevant to ship rocking motions, but only limited experimental pore pressure and
95 displacement data have been reported.

96 More 1g model tests that are better instrumented are required to gain a better understanding of the cyclic
97 liquefaction response of well-graded materials, that contain a wider range of particle sizes than sands
98 and are also prone to liquefaction. This study continues to investigate the cyclic unsaturated liquefaction
99 response of well-graded materials which contain significant fines contents. To gain a more holistic
100 understanding of the build-up in pore pressures, settlements and accompanying increases in the degree
101 of saturation and movement of moisture throughout the material, shake table tests will be performed on
102 columns of **loosely compacted**, unsaturated well-graded materials containing 18% and 28% fines. This

103 study follows on from other tests which investigated ship cargo liquefaction on well graded materials
104 with a significant fines content, similar in grading and relative densities to iron ore fines (Kwa & Airey,
105 2019) and the results have been supplemented by tests using a clean sand.

106

107 2. METHOD

108 2.1 Materials

109 Tests have been performed using Sydney Sand and reconstituted well-graded materials consisting of
110 angular basalt aggregates ranging in particle size from 9.5mm down to 0.015mm mixed with feldspar
111 fines. Grading curves for the sand, feldspar fines and the reconstituted materials are shown in Figure 1.
112 Fines contents of 18% and 28% were used for the reconstituted materials to produce grading curves
113 representative of the lower and upper bound grading curves for iron ore fines (TWG, 2013) and they
114 were also similar in grading to the gravelly fills that were reported to liquefy in Cubrinovski et al. (2003,
115 2017). The critical state soil parameters and specific gravities for these materials that were obtained in
116 a previous study (Kwa et al., 2019, 2017), are summarised in Table 1.

117 2.2 Experimental Set up and Sample Preparation

118 A photograph of the shake table apparatus and Perspex column used to contain the soil are shown in
119 Figure 2. The shake table used in this study is normally used for minimum and maximum density tests
120 according to Australian Standard AS1289.5.5.1 and has a fixed frequency of 50Hz and produces a
121 regular pulsed waveform with peak vertical accelerations of approximately 0.4g, similar to the peak
122 accelerations measured in the cargo of bulk ore carriers. An accelerometer was attached to the base of
123 the shake table. A typical displacement waveform derived from the acceleration data is shown in Figure
124 3. A 500mm tall by 140mm diameter Perspex column was also fastened onto the shake table and three
125 pressure transducers and three ECHO EC-5 moisture content probes were located at depths of 125mm,
126 250mm and 375mm from the top of the column. The pressure transducers, moisture content probes and
127 accelerometer were connected to a Vishay System 6000 data acquisition system, capable of measuring
128 up to 4000 readings per second and data were displayed and recorded on a computer.

129 The pressure transducers were calibrated using a GDS pressure controller. They were cleaned and filled
130 with de-aired water before each test and then were screwed horizontally into the side of the column.
131 Coarse gauze was also placed over the aperture of the transducers to prevent fines from flowing into
132 the transducer. After each test was completed, the transducers were also observed to be filled with clean
133 water, suggesting that they remained saturated throughout the test. Calibration of the moisture content
134 probes was conducted to determine the relation between voltage and moisture content. Tests were
135 performed over the range of expected void ratios and moisture contents for both materials. Figure 4
136 summarises the calibration curves for the Echo EC-5 moisture content probes in sand and in the well-

137 graded materials tested in this study. The calibration curve for Sydney Sand was consistent with the
138 calibration curves previously obtained in other studies (Campbell, 2001; Tehrani, 2016). However, the
139 calibration curve for the well-graded material was noticeably different, particularly at higher moisture
140 contents. The calibration in the well-graded materials was obtained by using two different methods
141 labelled as wetting and drying in Figure 4. The moisture content within the material was either increased
142 by adding and mixing known amounts of water into the soil (wetting), or they were decreased through
143 allowing the soil to dry out and the mass of water which evaporated out of the soil was measured
144 (drying). The calibration was not sensitive to whether the well-graded materials was subjected to
145 wetting or drying, and the calibration was also not observed to vary significantly with changes in the
146 density of the well-graded materials, as can also be seen in Figure 4.

147 An unsaturated column of soil was prepared by initially mixing the dry material with water at the
148 required moisture content. Once the moist material was well mixed, it was divided by mass into 10
149 equal portions. Each portion or layer was subsequently compacted into the column using the same
150 compaction energy per layer to achieve the target relative densities and degrees of saturation for the
151 unsaturated sample. In the columns of pure sand, samples were prepared at void ratios from 0.57 to 0.82
152 and degrees of saturation ranging from 29% to 68%. In the well-graded materials, the target relative
153 densities and degrees of saturation were relevant to those that have been measured in metallic ore bulk
154 cargoes when loaded into the hold of a ship (TWG, 2013). This corresponded to target void ratios of
155 0.38 to 0.55 for the well-graded materials containing 18 and 28% fines and degrees of saturation ranging
156 from 50 to 70%. **The effects of independently varying the initial dry densities of samples on the**
157 **unsaturated liquefaction response of these materials were not investigated in this study.** Table 2
158 summarises the individual test conditions, including their global initial and final void ratios, moisture
159 contents and the resulting degrees of saturation and relative densities. In some of the tests, coloured
160 sand was placed between the compacted layers around the container boundary to enable settlement
161 profiles with time to be tracked using photography. Once the column was filled, the shake table was
162 turned on and the soil was subjected to shaking, with drainage only from the upper surface, for 5 to 10
163 minutes, until the settlement and pore pressures were observed to stabilise.

164 3. RESULTS & DISCUSSION

165 3.1 Sand

166 The settlements measured in the columns of sand during shaking were small and consistent with results
167 from shaking table tests on saturated sand (Ozener et al., 2008). Figure 5 shows the moisture contents
168 measured at the top, middle and bottom of the columns of unsaturated sand during shaking. The initial
169 moisture contents measured at the bottom of the sand column were higher than the moisture contents
170 used during preparation of the sand column and they were also significantly higher than the moisture
171 contents measured at the top of the soil column. This is because water tended to redistribute towards

172 the bottom of the column during preparation as sand is a relatively free draining material. After the
173 water redistributed towards the bottom of the column, the moisture contents remained relatively
174 constant during shaking and liquefaction was not observed despite large numbers of cycles. However,
175 only a limited range of relative densities and initial degree of saturation have been tested and
176 liquefaction may have occurred if the columns of sand with low relative density had been tested at
177 higher degrees of saturation.

178 *3.2 Well graded materials*

179 *3.2.1 Settlements*

180 Liquefaction was observed in all the shake table tests performed on the well-graded materials containing
181 18% and 28% fines. Total settlements of 50mm to 75mm were observed in the columns of the well-
182 graded materials with initial degrees of saturation from 50% to 70%. Additional tests prepared with the
183 same compaction energy at higher initial degrees of saturation, and hence density, resulted in lower
184 settlements (Hu and Chen, 2017). In all tests shaking resulted in decreases in the global void ratios and
185 increases in degree of saturation, towards fully saturated states, with the final water level observed to
186 be at, or above, the surface of the soil. Figure 6 shows settlement profiles during shaking for a test with
187 28% fines, 28Sr60b. These profiles were obtained by measuring the changes in height of the coloured
188 sand layers as the test progressed. It shows that settlement in the first 30 seconds occurs mostly in the
189 upper 150 mm of the column and as shaking continues the zone where settlement dominates moves
190 downwards. In the first 120 seconds, minimal settlement occurs in the bottom 100 mm, however
191 between 120 and 300 seconds most of the settlement derives from this zone. The coloured layers of
192 sand became difficult to distinguish as the material liquified and after 20 minutes of shaking could not
193 be seen so only the position of the column surface is shown in Figure 6 at the end of the test.

194 All tests with a given fines content approached similar ultimate states with the final settlement
195 experienced by the soil column dependent on the initial density, a reduction in the initial density resulted
196 in larger settlements.

197 *3.2.2 Pore pressures*

198 Figures 7 and 8 show typical, average pore pressure responses during shaking measured at the top,
199 middle and bottom of the column containing the well-graded materials with 18% and 28% fines. The
200 detailed pore pressure responses could not capture the initial matric suctions and show variable and
201 erratic responses which may have been affected by the cylinder walls and possibly fines slowing down
202 the responses. Nevertheless, these effects do not appear to have influenced the mean pore pressures
203 which rise rapidly once shaking commences. As expected, the highest average pore water pressures
204 were measured at the bottom of the column, followed by the middle and top. Larger oscillations in the
205 pore water pressures were measured in the material containing 18% fines, particularly towards the end

206 of the test, which are believed to be a result of the material being more dilative and having a larger
207 friction angle than the material containing 28% fines (Kwa and Airey, 2017). The average pore
208 pressures during shaking measured at the middle and bottom of the column approached values that were
209 slightly, 0.5 to 3kPa, higher than hydrostatic pressure, taking the water level at the surface of the soil
210 column, implying an upwards flow of water. The pore pressures rose more quickly in samples prepared
211 at higher degrees of saturation and tended closer toward the estimated total stress (calculated assuming
212 material saturated), possibly because there was less air present in the soil.

213 At all depths the average pore pressures increased and approached the estimated total stresses, which
214 are indicated on the Figures. The rate of pore pressure increase depends on the magnitude of cyclic
215 stresses, increases with the degree of saturation and is limited by drainage. Initially, as a result of the
216 air present in the upper part of the column, the ability of water to flow upward is limited, contributing
217 to the increase of water pressures within the column. As a result, the effective stresses within the soil
218 column tended towards zero and the soil became liquefied. This state of very low effective stress was
219 reached early in the shaking process at the base of the column and migrated upwards as the saturation
220 front rose through the column, which is also evident in the moisture content responses.

221

222 *3.2.3 Moisture contents*

223 Typical moisture content variations during shaking of the column for material with 28% fines are shown
224 in Figure 9. The initial values indicate moisture redistribution has occurred with moisture contents in
225 the top of the column lower than the as-compacted state. Once shaking commences, there is a small
226 delay before the moisture contents increase at the middle sensor, and after a further delay upper sensor,
227 as the saturation front progressively moves towards the top of the column. This is consistent with the
228 pore pressure increases and accompanying decreases in effective stress which approached zero
229 throughout the whole column once the saturation front reached the surface of the column. Air bubbles
230 in the soil column were also observed to move towards the top of the column during shaking. Spikes in
231 the moisture content readings were caused by small voids forming underneath the moisture content
232 probes which restricted settlements in the surrounding material. This was most noticeable at the top of
233 the column where most of the settlements occurred rapidly at the beginning of the test. However, as the
234 test progressed more constant moisture contents were measured as the saturation degree increased and
235 the material liquefied so that it was able to flow more easily around the probes. The final moisture
236 contents measured at the end of the tests have been summarised in Table 3 and it is evident that the
237 moisture contents measured at the top of the sample were consistently higher than the moisture contents
238 measured at the middle and bottom of the column. This behaviour can be contrasted with the sand tests
239 where moisture content increased with depth following equilibration and then remained essentially
240 unchanged during shaking.

241 By combining the volume changes for test 28Sr60b and the moisture content responses for test 28Sr62,
242 shown in Figures 6 and 9 respectively, schematic moisture and density paths for the soil at the lower
243 and upper moisture sensor locations can be estimated as shown in Figure 10. The densities associated
244 with e_{max} and e_{min} and the modified Proctor compaction curve, which had a maximum dry density of
245 2.17t/m^3 , are also shown on Figure 10 to aid interpretation. Initially the soil is compacted into the
246 column at a known moisture content (11.5%) to a controlled density with $S_r \approx 61\%$, which is represented
247 by point 1. Moisture redistribution then occurs with water moving to the base of the column with
248 minimal change in volume so that the soil states move to points 2 and 5 for the lower and upper sensor
249 elevations, respectively. There is a smaller decrease in the moisture content measured at the bottom
250 transducer where the moisture content dropped to 9% (point 2) compared to the top transducer, where
251 the moisture content dropped to 3% (point 5).

252 When shaking commences the moisture content at the bottom transducer location increases rapidly to
253 about 14% in 5 seconds and then remains approximately constant. This peak can be interpreted as the
254 passing of the saturation front. As indicated by the settlement profiles this is not associated with
255 significant volume change and the soil state moves from point 2 to point 3 where it remains for
256 approximately 120 seconds until the saturation front reaches the top of the column. Subsequently water
257 flowed from the base and this was accompanied with a volume strain of 0.125 in the bottom third of the
258 column, resulting in the state moving from point 3 to point 4. The final density is greater than given by
259 e_{min} as a result of an upwards migration of fines associated with the flow of water, discussed further
260 below. At the top transducer location, the column initially experiences unsaturated compression, and
261 within 30 seconds of shaking, the upper one third of the column has an average volume strain of ~ 0.12 ,
262 and the soil state moves from point 5 to point 6 without significant change in moisture content. The
263 rising saturation front then causes a gradual rise in moisture content to around 12% at 200 seconds,
264 which is accompanied by a slight loosening in the soil and the soil state moves from point 6 to point 7.
265 As the test progressed, the moisture content gradually continued to rise, and the soil loosened due to the
266 upward flow of water and increasing fines content until the end of the test, at point 8.

267 Similar trends were observed in the other tests. More rapid rises of the saturation front and increases in
268 the degrees of saturation were observed in tests performed with higher initial degrees of saturation. This
269 can be seen, for example, in comparison of Figure 9a where the initial degree of saturation was 62%
270 and Figure 9b, where initial degree of saturation was 72%.

271 3.2.4 Migration of fines

272 The fines in the well-graded materials were observed to migrate towards the surface of the column and
273 a thin layer of fines could be seen lying at the top of the soil column after shaking as shown in Figure
274 11. A sieve analysis was performed after shaking on four sub-samples that were cut from different parts
275 of the soil column and the resulting grading curves for each sub-sample, labelled as A, B, C and D, are

276 shown in Figure 12. The resulting distributions of fines throughout the column after shaking have been
277 summarised in Figure 13 and the thin layer of fines observed at the top of the column has been plotted
278 as a layer with 100% fines. From the grading curves and final distribution of fines throughout the
279 column in Figures 12 and 13, it is evident that the material at the top of the column was finer than the
280 material towards the bottom of the column. There was also more variation in the fines content in the
281 layers of the well-graded material containing 28% fines than 18% fines.

282 The movement of fines throughout these well-graded materials is not unexpected. The flow of water
283 through soils is known to cause fines within the material to migrate and this process, termed suffosion,
284 is an internal stability phenomenon in which fine particles are transported through a non-plastic soil,
285 resulting in the collapse of the soil structure (Chapuis, 1992; Fannin et al., 2014). For suffosion to occur,
286 the hydraulic gradient needs to exceed a critical value and the soil itself needs to be unstable. Both
287 requirements have been found to depend on the grading of the soil (Kenny et al., 1985, Li & Fannin,
288 2008, 2012, Hunter & Bowman, 2018). In this study, the pore pressure build-up measured during
289 shaking resulted in hydraulic gradients close to the critical values required for suffosion to occur. The
290 well graded materials containing 18% and 28% fines can also be classified as potentially unstable soils
291 (Kezdi, 1979; Kenny et al., 1985) and they are similar in grading to materials which have demonstrated
292 suffosion (Kenny et al., 1985; Li, 2008).

293 As already noted during the shaking of the well-graded materials the soil columns settled significantly,
294 the fines accumulated at the column surface, and the final water level was at, or just above, the soil
295 surface. Allowing for the settlement enables the average post-shaking void ratios ($e_{average}$) and degrees
296 of saturation ($S_{r,corrected}$) to be calculated as reported in Table 2. It can be seen that significant decreases
297 in void ratio have occurred and the final relative densities ($D_{r,final}$) are apparently well above 1. Given
298 that all the initially unsaturated material had liquefied the average degrees of saturation would be
299 expected to be between 0.9 and 1 and this is confirmed by the values in Table 2. However, if the final
300 degrees of saturation are calculated from the local moisture contents for the well-graded material with
301 28% fines using the final average void ratios ($e_{average}$) and a constant value for specific gravity of 2.82,
302 unreasonable degrees of saturation are calculated ($S_{r,calculated}$), as indicated in Table 3. Values greater
303 than 1 result at the top of the soil column and unreasonably low values are estimated at the base. More
304 reasonable degrees of saturation, within $\pm 2\%$ of the measured final global degrees of saturation
305 ($S_{r,corrected}$), can be determined if the inhomogeneity within the soil column is considered. The
306 distribution of fines within the column was used to estimate the local specific gravities, which varied
307 with fines migration because the specific gravities of feldspar fines and coarser basalt were 2.6 and 2.9,
308 respectively. Assuming a constant degree of saturation throughout the column, within $\pm 2\%$ of the
309 measured global value, the local void ratios could be calculated from the moisture contents measured
310 at the top, middle and bottom of the column. These calculated void ratios are included in Table 3,
311 labelled as e , and the distribution of void ratios with column depth have been plotted in Figure 14. As

312 expected, the void ratios were higher towards the top of the column. To estimate the void ratio of the
313 thin, close to fully saturated layer of fines at the top of the soil column, a known mass of dry fines was
314 pluviated into a measuring cylinder filled with water. The fines were left to settle for a few hours until
315 the height of the settled and submerged fines layer could be accurately measured.

316 It is evident that the void ratio of the fines is significantly higher than estimated for the well-graded
317 material. A weighted average ($e_{average}$) of the calculated local void ratios, based on the approximate
318 thicknesses of the soil layers, as shown in Figure 15, was calculated in Table 3, to check the
319 reasonableness of the calculated void ratios. These values are close to the global average values given
320 in Table 2 and are not particularly sensitive to uncertainty in the thicknesses of the soil layers. This
321 analysis suggests that it is reasonable to assume a constant degree of saturation throughout the liquefied
322 column, and this is associated with densification at the base of the column, loosening at the top, upwards
323 fines migration and the development of a loose fines layer on the column surface. It may also be noted
324 that the presence of fines on the surface also reduced the permeability and contributed to keeping the
325 soil in a liquefied state until shaking of the soil stopped.

326 *3.3 Application of the findings and limitations*

327 The results presented in this paper describe the fundamental liquefaction behaviour of unsaturated well
328 graded materials, which are widely used as fill materials, in railway ballast and as pavement materials.
329 The well graded materials also have gradings within the range of liquefiable shipped metallic cargoes.
330 These tests have clearly demonstrated the potential for large settlements, fines migration and the
331 development of very low effective stresses within a large number of cycles and at the amplitudes
332 thought to be relevant for ships passing through storms. However, they have been conducted in a column
333 of 0.5m height, with vertical excitation at a very high frequency of 50 Hz, which is more relevant to
334 cyclic loading conditions on train ballast and highway pavements. Nevertheless, cyclic triaxial tests
335 performed on the same well-graded unsaturated material showed similar trends in settlement
336 accumulation and rapid pore pressure build up at lower frequencies when drainage was prevented (Kwa
337 & Airey, 2019). Similar trends in pore pressures have also been observed in shake table tests performed
338 on saturated and partially saturated sands that have liquefied, when cyclically loaded at lower, more
339 realistic frequencies of between 0.1 to 8 Hz (Yegain et al., 2006, 2007; Ueng et al., 2006, 2010, 2017;
340 Pathak et al., 2010, 2013). Although similar trends in behaviour may be observed, the susceptibility to
341 liquefaction of the partially saturated well graded materials would be difficult to predict with existing
342 models and understanding and there is a need for more well controlled and instrumented tests to develop
343 and validate models.

344 The shake table used in this study is normally used to perform maximum density tests according to
345 AS1289.5.5.1. (Similar to ASTM D4253). The minimum and maximum densities for the well graded
346 materials tested in this study were also determined according to the standard AS1289.5.5.1, however,

347 according to the standard, maximum density tests should not be performed on materials containing non-
348 plastic fine contents greater than 12% (15% in ASTM D4253) because the fines can segregate. This
349 was observed during the column tests in the well-graded materials containing 18% and 28% fines. Once
350 the fines migrate, the material is no longer homogeneous and the measured global density in the column,
351 which is significantly taller than the standard container used in the maximum density tests, is not
352 representative of the local densities throughout the material. This resulted in an overestimation of the
353 true relative densities of the material. It can be anticipated that tests to measure maximum density using
354 wet samples that satisfy suffosion criteria for unstable soils are likely to be affected by fines migration
355 and lead to unreliable maximum density values. The need for improved standards to measure maximum
356 dry unit weight has recently been discussed (Lunne et al., 2019) and from our column tests it appears
357 that tests should be performed dry to avoid internal instability.

358

359 4. CONCLUSION

360 This study investigated the cyclic unsaturated liquefaction responses of **columns of loosely compacted**
361 well-graded materials that contain a wider range of particle sizes than more commonly tested sands and
362 silty sands, and that have similar gradings to other soils that have been known to liquefy. Liquefaction
363 was observed in all of the shake table tests performed on the well-graded materials containing 18 and
364 28% fines and prepared at degrees of saturation ranging from 50 to 70%. Prior to shaking moisture
365 redistributed, decreasing at the surface and increasing at the base. When shaking started large
366 settlements were observed in the upper partly saturated part of the column, whereas at the base very
367 little settlement occurred and a saturation front could be seen to move upwards. As shaking continued
368 the saturation front moved up to the column surface and the pore pressures increased to equal the total
369 stress and the soil reached a liquefied state. The liquefied state was reached first at the bottom of the
370 column, partly as a result of air in the upper parts restricting water flow, and settlement in the lower
371 part of the column did not occur until the saturation front reached the surface. The fines in the well-
372 graded materials also migrated towards the surface of the column due to the upward hydraulic gradient.
373 Due to the migration of water and fines, the soil in the column was not homogeneous and as a result,
374 the local densities also varied. The void ratios were found to increase at the top and decrease at the
375 bottom.

376 The shake table used in this study vibrated in a vertical direction at higher frequencies and for a larger
377 number of cycles than typically used in normal seismic liquefaction studies. This paper reports data and
378 findings which are useful for understanding the fundamental cyclic liquefaction behaviour of
379 unsaturated well graded materials when subjected to similar vertical cyclic loading conditions including
380 during repetitive transport loading or in cargoes during shipping transportation. In addition to this, the

381 data can also be used to validate finite element numerical models with dynamic unsaturated constitutive
382 models that seek to predict the response of unsaturated soils to dynamic events.

383

384 5. ACKNOWLEDGEMENTS

385 The authors acknowledge the support provided by the Australian Research Council Discovery
386 Scheme (grant DP150103083).

387

388 REFERENCES

389 Alobaidi, I. and Hoare, D.J., 1996. The development of pore water pressure at the subgrade-subbase
390 interface of a highway pavement and its effect on pumping of fines. *Geotextiles and geomembranes*,
391 14(2), pp.111-135.

392 Andrus, R. (1995). In situ characterization of gravelly soils that liquefied in the 1983 Borah peak
393 earthquake (Idaho). PhD thesis, University of Texas at Austin.

394 ASTM (2012). ASTM Designation D4253 Standard Test Methods for Maximum Index Density and
395 Unit Weight of Soils Using a Vibratory Table. American Society for Testing and Materials

396 Bouckovalas, G. D., Andrianopoulos, K. I., and Papadimitriou, A. G. (2003). A critical state
397 interpretation for the cyclic liquefaction resistance of silty sands. *Soil Dynamics and Earthquake*
398 *Engineering*, 23(2):115–125.

399 Bowman, E., & Hunter, R. P. (2017). Visualisation of seepage induced suffusion and suffosion within
400 internally erodible granular media. *Géotechnique*.

401 Campbell, G.S. (2001). Calibration and evaluation of the low-cost EC-5 soil moisture sensor. Retrieved
402 from metergroup.com/environmental/articles/calibration-evaluation-ec-5-soil-moisture-sensor

403 Carrera, A., Coop, M. R., & Lancellotta, R. (2011). Influence of grading on the mechanical behaviour
404 of Stava tailings. *Géotechnique*, 61(11), 935.

405 Chapuis, R. P. (1992). Similarity of internal stability criteria for granular soils. *Canadian Geotechnical*
406 *Journal*, 29(4):711–713.

407 Cubrinovski, M., & Ishihara, K. (2003). Liquefaction-induced ground deformation and damage to piles
408 in the 1995 Kobe Earthquake.

409 Cubrinovski, M., Bray, J., de la Torre, C., Olsen, 4. M., Bradley, B., Chiaro, G., ... & Wotherspoon, L.
410 (2017). Liquefaction effects and associated damages observed at the Wellington Centreport from the
411 2016 Kaikoura earthquake.

412 Dash, H. and Sitharam, T. (2009). Undrained cyclic pore pressure response of sand–silt mixtures: effect
413 of nonplastic fines and other parameters. *Geotechnical and Geological Engineering*, 27(4):501–517.

414 Duku, P. M., Stewart, J. P., Whang, D. H., & Yee, E. (2008). Volumetric strains of clean sands subject
415 to cyclic loads. *Journal of geotechnical and geoenvironmental engineering*, 134(8), 1073-1085.

416 Duong, T.V., Cui, Y.J., Tang, A.M., Dupla, J.C., Canou, J., Calon, N. and Robinet, A., 2014.
417 Investigating the mud pumping and interlayer creation phenomena in railway sub-structure.
418 *Engineering Geology*, 171, pp.45-58.

419 Ebrahimi, A., Tinjum, J.M. and Edil, T.B., 2015. Deformational behavior of fouled railway ballast.
420 *Canadian Geotechnical Journal*, 52(3), pp.344-355.

421 Fannin, R. and Slangen, P. (2014). On the distinct phenomena of suffusion and suffosion. *Géotechnique*
422 *Letters*, 4(4):289–294.

423 Ghayoomi, M., & McCartney, J. S. (2011). Measurement of small-strain shear moduli of partially
424 saturated sand during infiltration in a geotechnical centrifuge. *Geotechnical Testing Journal*, 34(5), 503-
425 513.

426 Ghayoomi, M., McCartney, J. S., & Ko, H. Y. (2012). Empirical methodology to estimate seismically
427 induced settlement of partially saturated sand. *Journal of Geotechnical and Geoenvironmental*
428 *Engineering*, 139(3), 367-376.

429 Harder, JR, L. F. (1997). Application of the Becker Penetration Test for evaluating the liquefaction
430 potential of gravelly soils. Technical report.

431 Hu, Y. (2017). Liquefaction of unsaturated soil under cyclic loading. Bachelor’s thesis, The University
432 of Sydney.

433 IMSBC, (2013). International maritime solid bulk cargoes code. International Maritime Organization.

434 Indraratna, B., Salim, W., Rujikiatkamjorn, C., 2011. *Advanced Rail Geotechnology - Ballasted Track*,
435 CRC Press.

436 Ju, L., Vassalos, D., & Boulougouris, E. (2016). Numerical assessment of cargo liquefaction potential.
437 *Ocean Engineering*, 120, 383-388.

438 Kenny, T. and Lau, D. (1985). Internal stability of granular soils. *Canadian Geotechnical Journal*,
439 21:634–643.

440 Kezdi, A. (1979). Soil physics – selected topics. Amsterdam, the Netherlands: Elsevier Scientific
441 Publishing Co.

442 Kimoto, S., Oka, F., Fukutani, J., Yabuki, T., and Nakashima, K. (2011). Monotonic and cyclic
443 behaviour of unsaturated sandy soil under drained and fully undrained conditions. *Soils and*
444 *foundations*, 51(4):663–681.

445 Kokusho, T. (1999). Water film in liquefied sand and its effect on lateral spread. *Journal of Geotechnical*
446 *and Geoenvironmental Engineering*, 125(10), 817-826.

447 Kokusho, T., & Kojima, T. (2002). Mechanism for postliquefaction water film generation in layered
448 sand. *Journal of geotechnical and geoenvironmental engineering*, 128(2), 129-137.

449 Kwa, K. A., & Airey, D. W. (2017). Effects of fines on liquefaction behaviour in well-graded materials.
450 *Canadian Geotechnical Journal*, 54(10), 1460-1471.

451 Kwa, K. A., & Airey, D. W. (2019). Effects of fines on the cyclic liquefaction behaviour in unsaturated,
452 well-graded materials. *Soils and Foundations*

453 Li, M., & Fannin, R. J. (2008). Comparison of two criteria for internal stability of granular soil.
454 *Canadian Geotechnical Journal*, 45(9), 1303-1309.

455 Li, M., & Fannin, R. J. (2012). A theoretical envelope for internal instability of cohesionless soil.
456 *Géotechnique*, 62(1), 77-80.

457 Lunne, T., Knudsen, S., Blaker, O., Vestgarden, T., Powell, J.J.M., Wallace, C.F., Krogh, L., Thomson
458 N.V., Yetginer, G., and Ghanekar, R.K. (2019) Methods used to determine maximum and minimum
459 dry unit weights of sand: Is there a need for a new standard? *Canadian Geotechnical Journal*, 56: 536-
460 553

461 Munro, M. C. and Mohajerani, A. (2016). Moisture content limits of iron ore fines to prevent
462 liquefaction during transport: review and experimental study. *International Journal of Mineral*
463 *Processing*, 148:137–146.

464 Okamura, M. and Soga, Y. (2006). Effects of pore fluid compressibility on liquefaction resistance of
465 partially saturated sand. *Soils and Foundations*, 46(5):695–700.

466 Özener, P. T., Özyaydın, K., & Berilgen, M. M. (2009). Investigation of liquefaction and pore water
467 pressure development in layered sands. *Bulletin of Earthquake Engineering*, 7(1), 199-219.

468 Pathak, S. R., Dalvi, R. S., & Katdare, A. D. (2010). Earthquake Induced Liquefaction using Shake
469 Table Test.

470 Pathak, S. R., Kshirsagar, M. P., & Joshi, M. S. (2013). Liquefaction triggering criterion using shake
471 table test. *Int. J. Eng. Tech*, 5, 4439-4449.

472 Polito, C. P. and Martin II, J. R. (2001). Effects of nonplastic fines on the liquefaction resistance of
473 sands. *Journal of Geotechnical and Geoenvironmental Engineering*, 127(5):408–415.

474 Proceedings of the 6th International Symposium on Deformation Characteristics of Geomaterials, IS-
475 Buenos Aires 2015, 15-18 November 2015, Buenos Aires, Argentina, volume 6, page 299. IOS Press.

476 Report 3, Technical Working Group (TWG).

477 Sadek, S. and Saleh, M. (2007). The effect of carbonaceous fines on the cyclic resistance of poorly
478 graded sands. *Geotechnical and Geological Engineering*, 25(2):257.

479 Sadrekarimi, A. (2013). Influence of fines content on liquefied strength of silty sands. *Soil Dynamics
480 and Earthquake Engineering*, 55:108–119.

481 Stewart, J. P., & Whang, D. H. (2003). Simplified procedure to estimate ground settlement from seismic
482 compression in compacted soils. In *Proc. 2003 Pacific Conference on Earthquake Engineering*.

483 Tehrani, K. (2016). Developing a new instrumented soil column to study climate-induced ground
484 movement in expansive soil (Doctoral dissertation, Queensland University of Technology).

485 Tsuchida, H. (1970). Prediction and countermeasure against the liquefaction in sand deposits. In
486 *Abstract of the seminar in the Port and Harbor Research Institute*, pages 31–333.

487 TWG (2013). TWG 3rd report and Imperial College review- Proctor Fagerberg (PF) Test.

488 Ueng, T. S., Wang, M. H., Chen, M. H., Chen, C. H., & Peng, L. H. (2006). A large biaxial shear box
489 for shaking table test on saturated sand. *Geotechnical Testing Journal*, 29(1), 1-8.

490 Ueng, T. S., Wang, Z. F., Chu, M. C., & Ge, L. (2017). Laboratory tests for permeability of sand during
491 liquefaction. *Soil Dynamics and Earthquake Engineering*, 100, 249-256.

492 Ueng, T. S., Wu, C. W., Cheng, H. W., & Chen, C. H. (2010). Settlements of saturated clean sand
493 deposits in shaking table tests. *Soil Dynamics and Earthquake Engineering*, 30(1-2), 50-60.

494 Unno, T., Kazama, M., Sento, N., and Uzuoka, R. (2006). Cyclic shear behavior of unsaturated volcanic
495 sandy soil under various suction conditions. In *Unsaturated Soils 2006*, pages 1133–1144.

496 Unno, T., Kazama, M., Uzuoka, R., and Sento, N. (2008). Liquefaction of unsaturated sand considering
497 the pore air pressure and volume compressibility of the soil particle skeleton. *Soils and Foundations*,
498 48(1):87–99.

- 499 Uzuoka, R., Unno, T., Sento, N., and Kazama, M. (2014). Effect of pore air pressure on cyclic behavior
500 of unsaturated sandy soil. In Proceedings of the 6th International Conference on Unsaturated Soils,
501 UNSAT, pages 783–789.
- 502 Wang, H., Koseki, J., Sato, T., and Tantian, J. (2015). Experimental evaluation of liquefaction resistance
503 of unsaturated sandy soils. In Deformation Characteristics of Geomaterials:
- 504 Xenaki, V. and Athanasopoulos, G. (2003). Liquefaction resistance of sand–silt mixtures: an
505 experimental investigation of the effect of fines. *Soil Dynamics and Earthquake Engineering*, 23(3):1–
506 12.
- 507 Yanagisawa, E., & Jafarzadeh, F. (1995). Behaviour of Saturated Sand Models under Principal Stress
508 Axes Rotation in Shake Table Tests.
- 509 Yegian, M. K., Eseller, E., & Alshawabkeh, A. (2006). Preparation and cyclic testing of partially
510 saturated sands. In *Unsaturated Soils 2006* (pp. 508-518).
- 511 Yegian, M. K., Eseller-Bayat, E., Alshawabkeh, A., & Ali, S. (2007). Induced-partial saturation for
512 liquefaction mitigation: experimental investigation. *Journal of Geotechnical and Geoenvironmental*
513 *Engineering*, 133(4), 372-380.

TABLES

Table 1: Material parameters

Material	ϕ_{cs} (°)	G_s	e_{min}	e_{max}
Sydney Sand	32	2.65	0.60	0.81
Feldspar Fines	37	2.6	0.38	0.57
Well-Graded 18% Fines	42	2.85	0.34	0.52
Well-Graded 28% Fines	40	2.82	0.39	0.72

Table 2: Summary of shake table tests and the average moisture and density state values

Name	Material	$e_{initial}$	$Dr_{initial}$	$mc_{initial}$	$Sr_{initial}$	e_{final}	Sr_{final}	Dr_{final}
SydSSr29	Sydney Sand	0.82	-0.05	0.09	0.29	No Change		
SydSSr56	Sydney Sand	0.57	1.15	0.12	0.56	No Change		
SydSS68	Sydney Sand	0.60	0.7	0.17	0.68	No Change		
18Sr50	18% Fines	0.51	0.06	0.088	0.50	0.3	0.84	1.22
18Sr60	18% Fines	0.43	0.53	0.089	0.60	0.27	0.96	1.39
18Sr70	18% Fines	0.38	0.78	0.093	0.71	0.275	0.97	1.36
28Sr56	28% Fines	0.55	0.52	0.11	0.56	0.34	0.91	1.15
28Sr60	28% Fines	0.54	0.55	0.115	0.60	0.34	0.95	1.15
28Sr60b	28% Fines	0.51	0.63	0.107	0.60	0.31	0.96	1.24
28Sr62	28% Fines	0.51	0.64	0.115	0.62	0.34	0.95	1.15
28Sr65	28% Fines	0.50	0.67	0.115	0.65	0.34	0.95	1.15
28Sr72	28% Fines	0.45	0.81	0.115	0.72	0.34	0.95	1.15

Table 3: Summary of the final moisture contents, degrees of saturation and void ratios at the top, middle and bottom of the column of the well-graded material with 28% fines

Name	Layer	$m_{c,measured}$	$S_{r,calculated}$	G_s	Layer thickness	e	$S_{r,corrected}$
28Sr56	fines	-	-	2.60	10	1.5	-
	top	0.112	0.902	2.77	82.5	0.34	0.912
	middle	0.109	0.878	2.80	130	0.33	0.925
	bottom	0.1	0.806	2.82	187.5	0.31	0.911
					$e_{average}$	0.351	
28Sr60	fines	-	-	2.60	10	1.5	-
	top	0.125	1.037	2.78	82.5	0.36	0.965
	middle	0.105	0.871	2.80	130	0.31	0.948
	bottom	0.1	0.829	2.82	187.5	0.3	0.941
					$e_{average}$	0.345	
28Sr62	fines	-	-	2.60	10	1.5	-
	top	0.125	1.037	2.78	82.5	0.36	0.979
	middle	0.12	0.995	2.80	130	0.34	0.988
	bottom	0.11	0.912	2.82	187.5	0.31	0.995
					$e_{average}$	0.359	
28Sr65	fines	-	-	2.60	10	1.5	-
	top	0.13	1.078	2.78	82.5	0.37	0.977
	middle	0.11	0.912	2.80	130	0.32	0.963
	bottom	0.105	0.871	2.82	187.5	0.31	0.956
					$e_{average}$	0.354	
28Sr72	fines	-	-	2.60	10	1.5	-
	top	0.125	1.037	2.77	82.5	0.35	0.993
	middle	0.12	0.995	2.80	130	0.34	0.998
	bottom	0.102	0.829	2.82	187.5	0.30	0.941
					$e_{average}$	0.352	

FIGURES

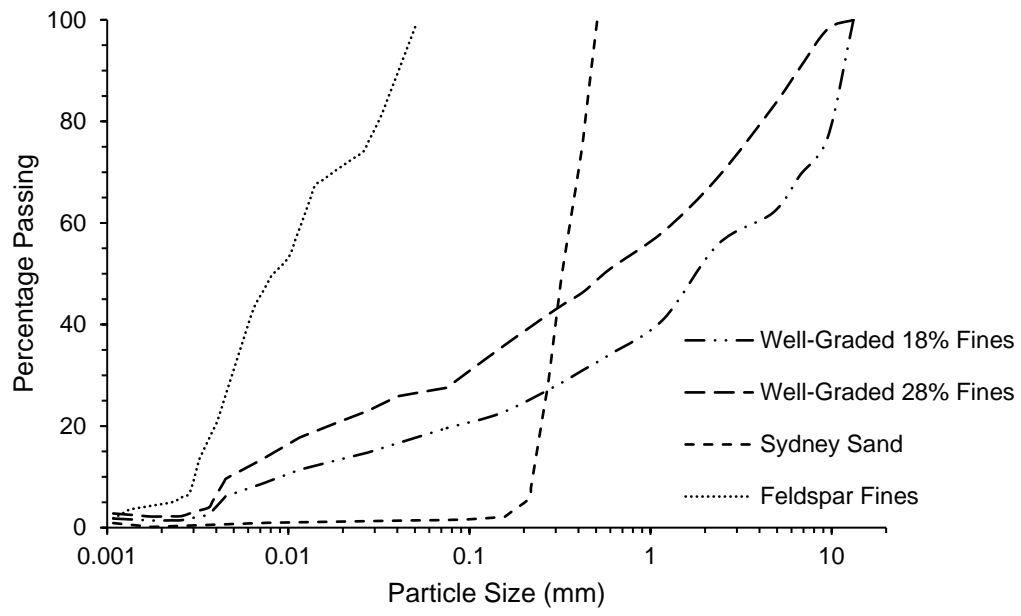


Figure 1: Grading curves

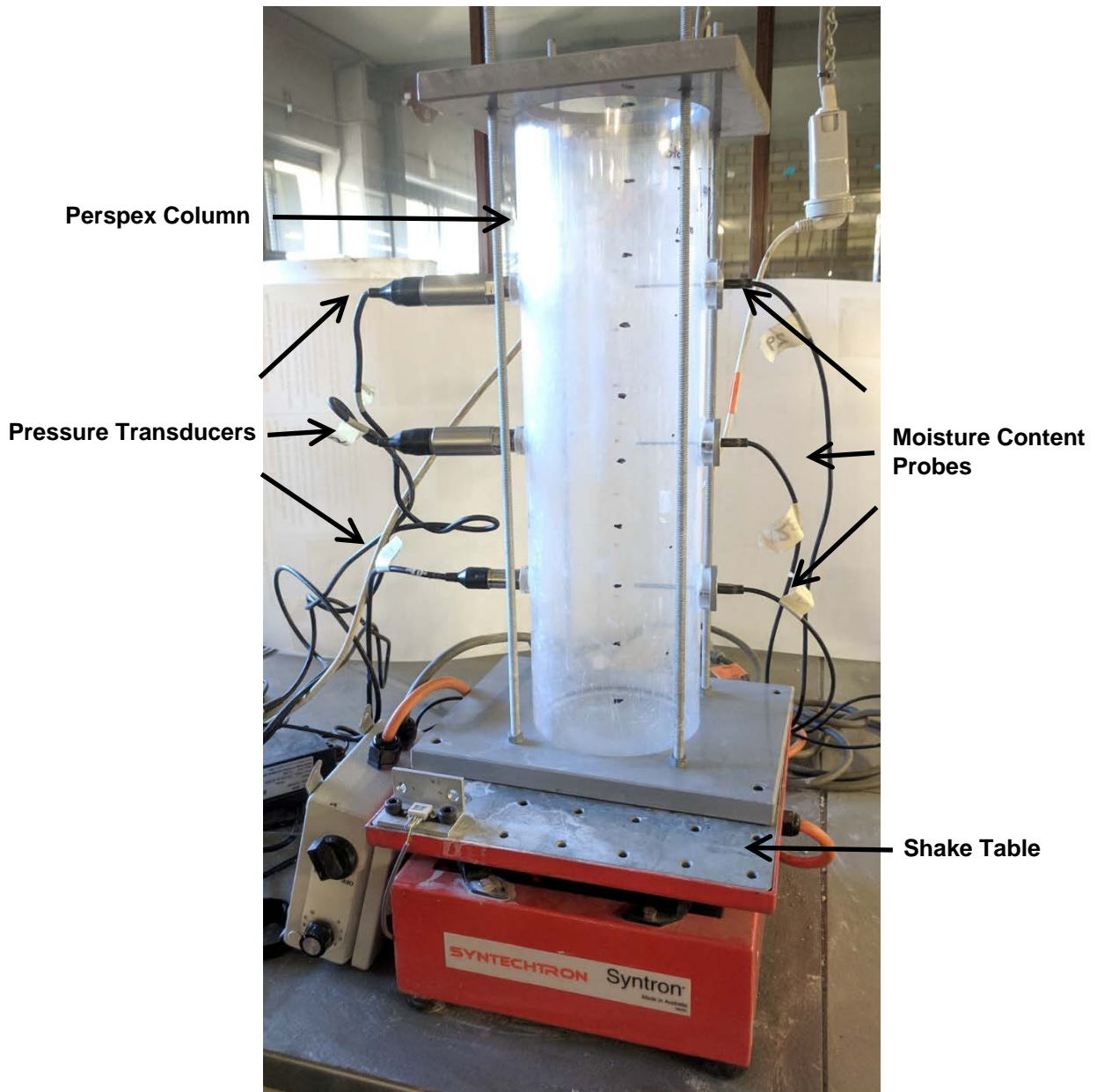


Figure 2: Shake table and soil column set up

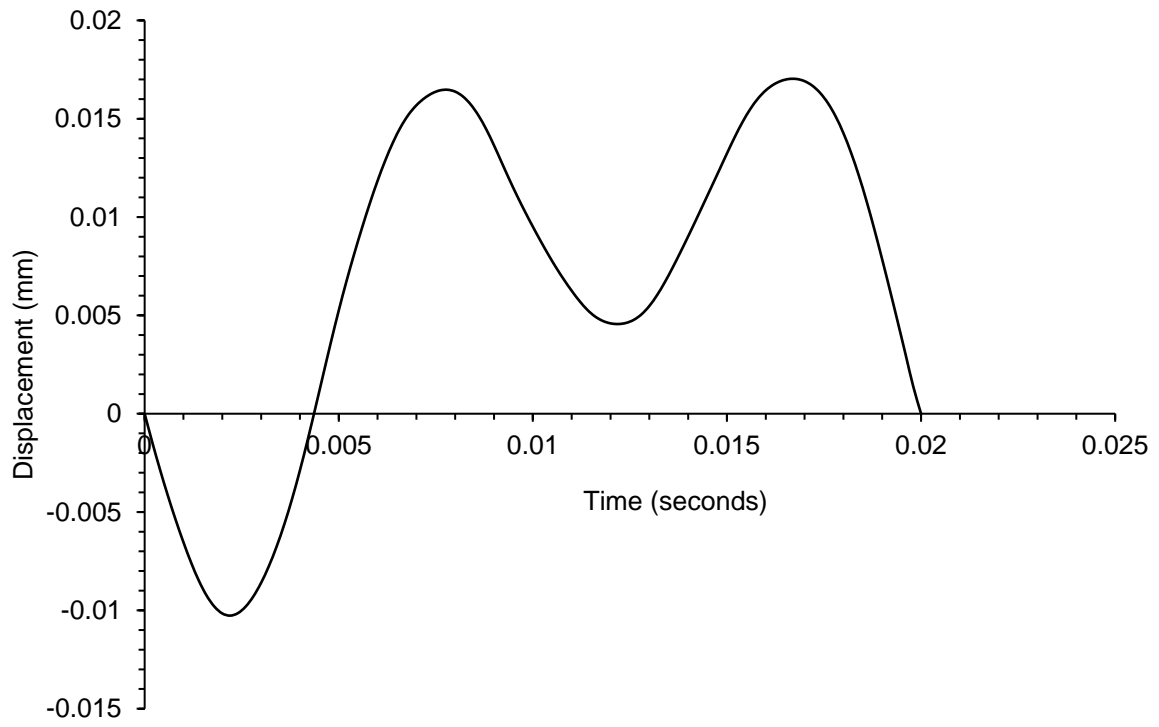


Figure 3: Typical displacement waveform produced by the shake table

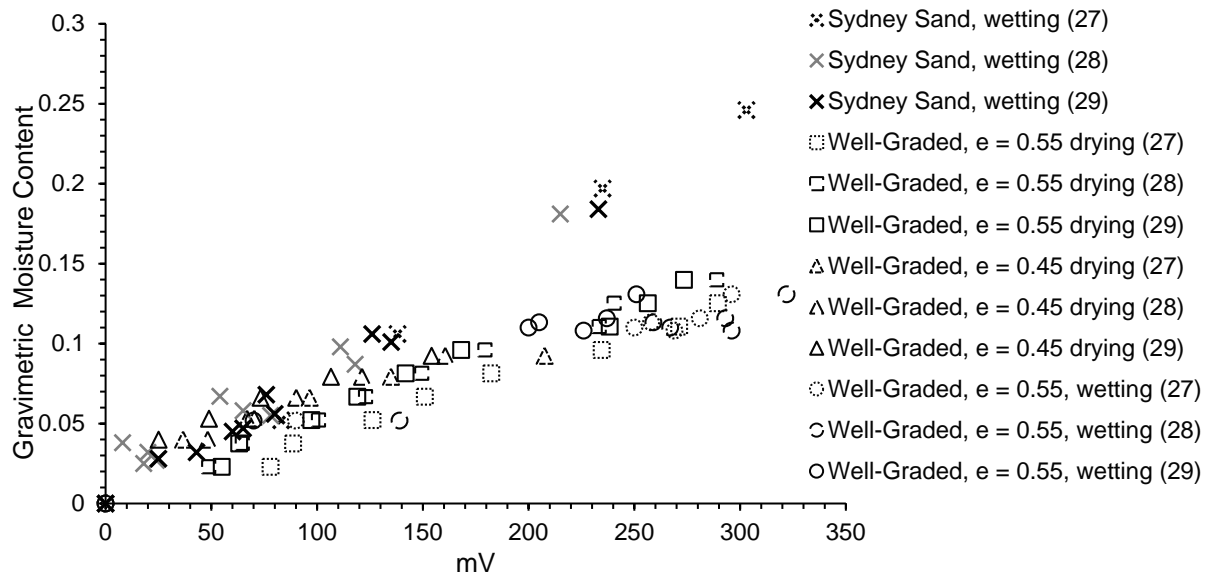


Figure 4: Calibration of moisture content probes

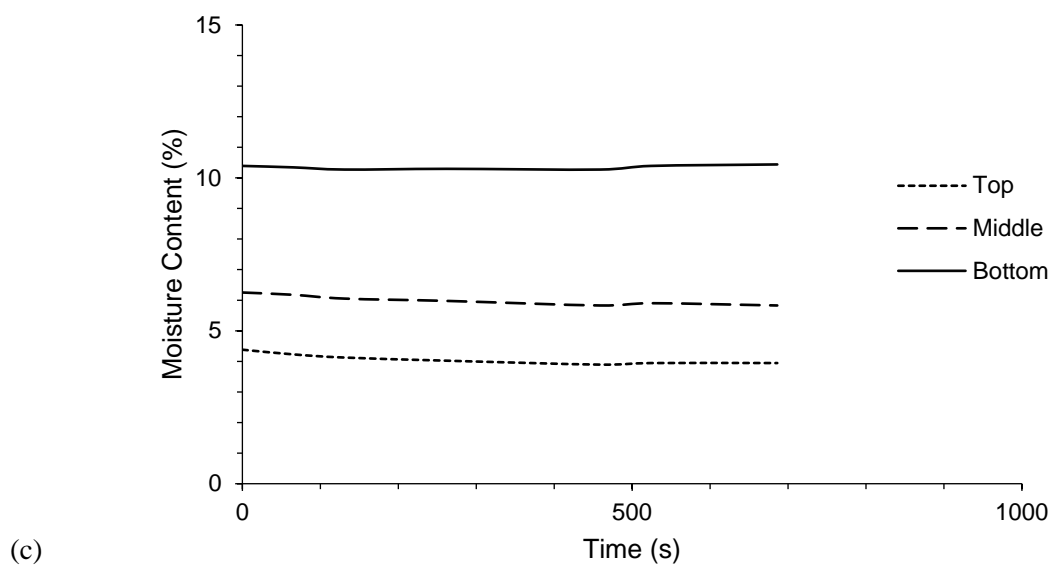
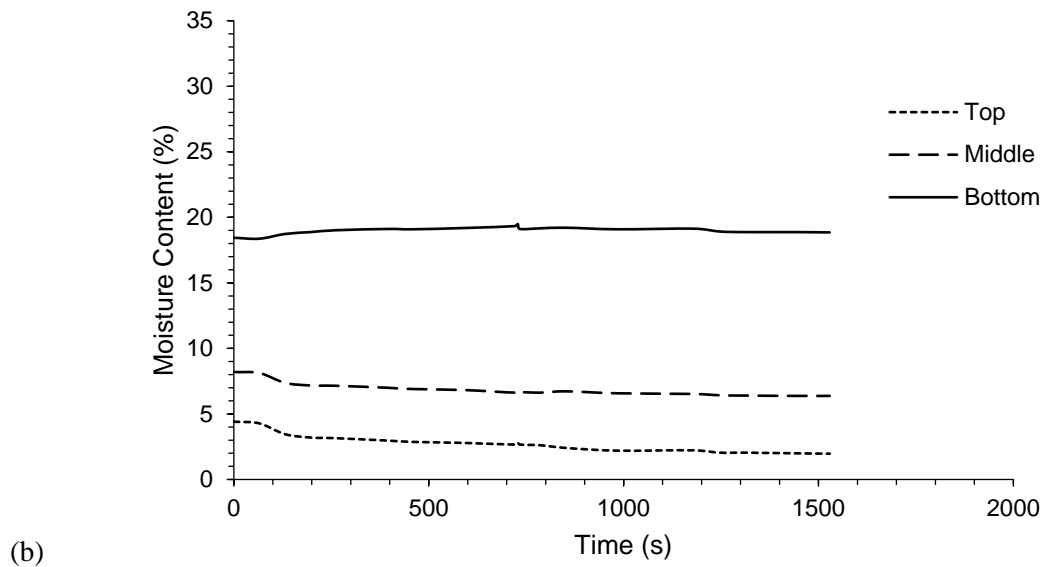
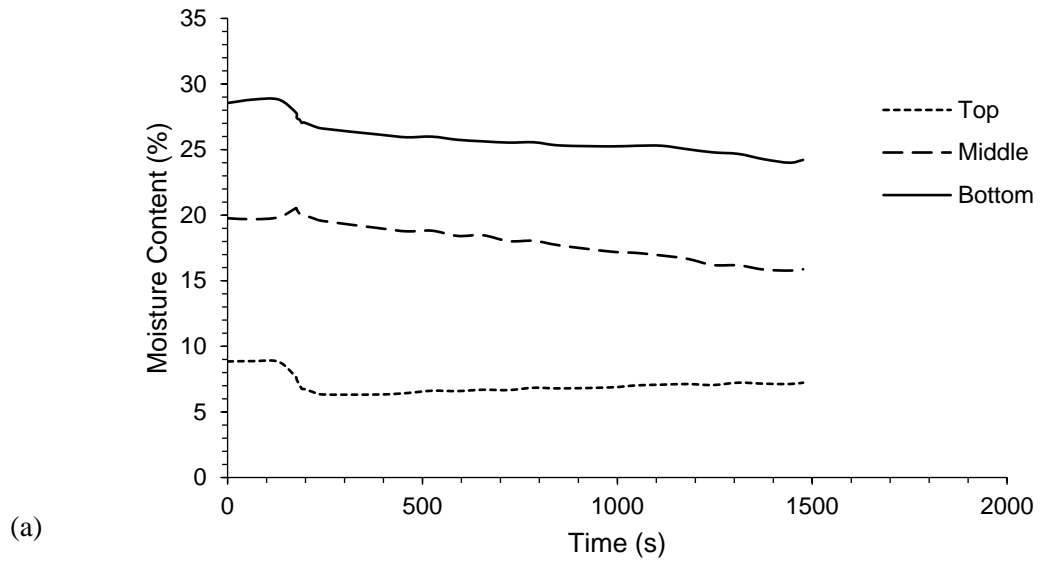


Figure 5: Moisture content measurements in sand for tests (a) SydSS68, (b) SydSS56 and (c) SydSS29

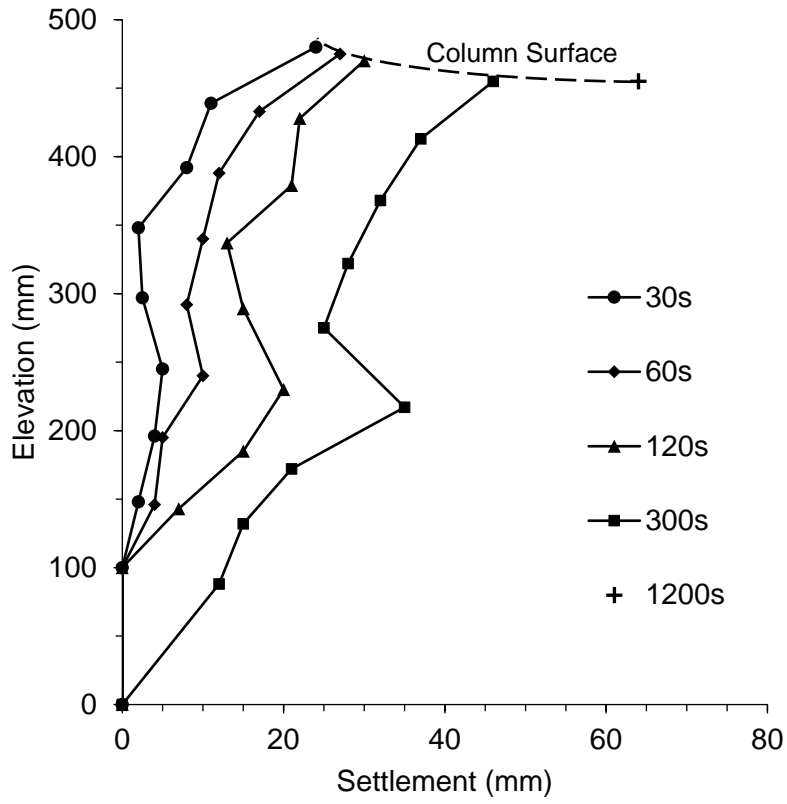
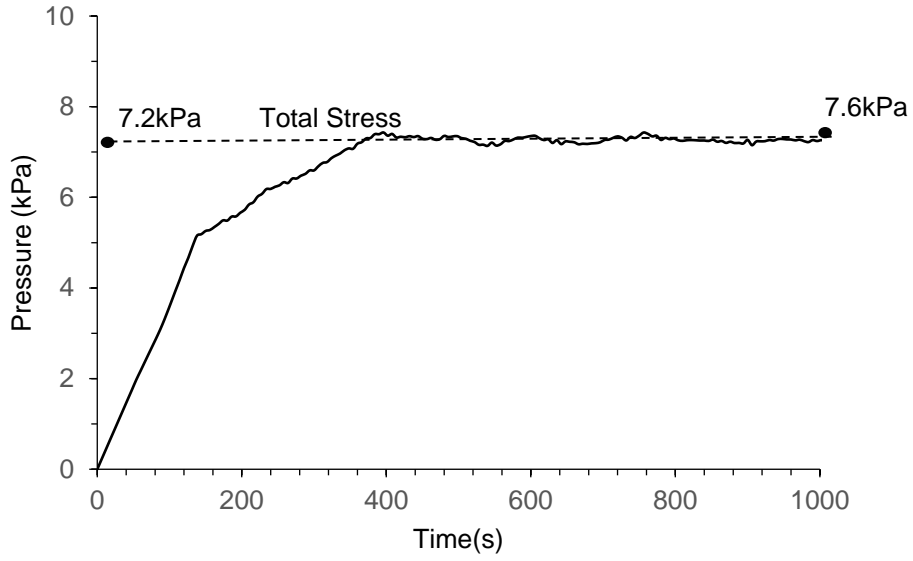
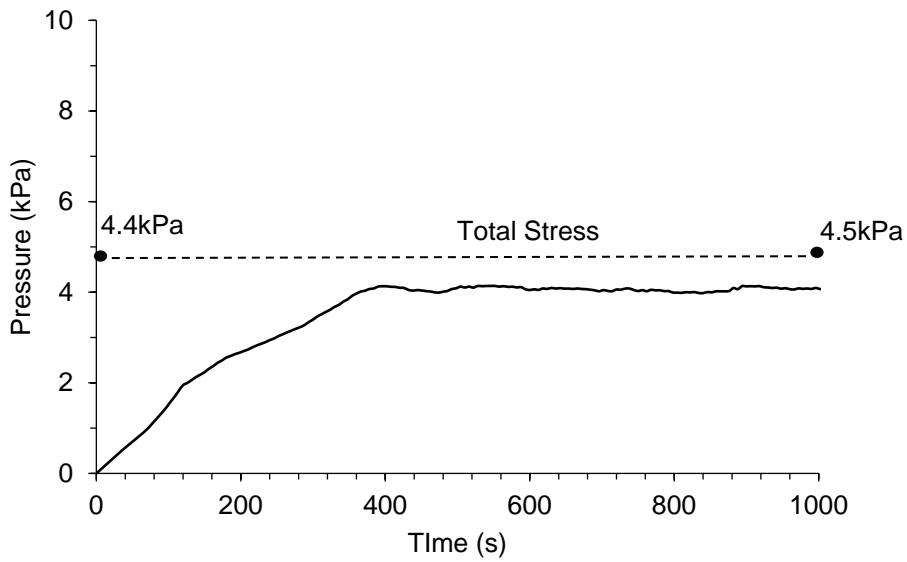


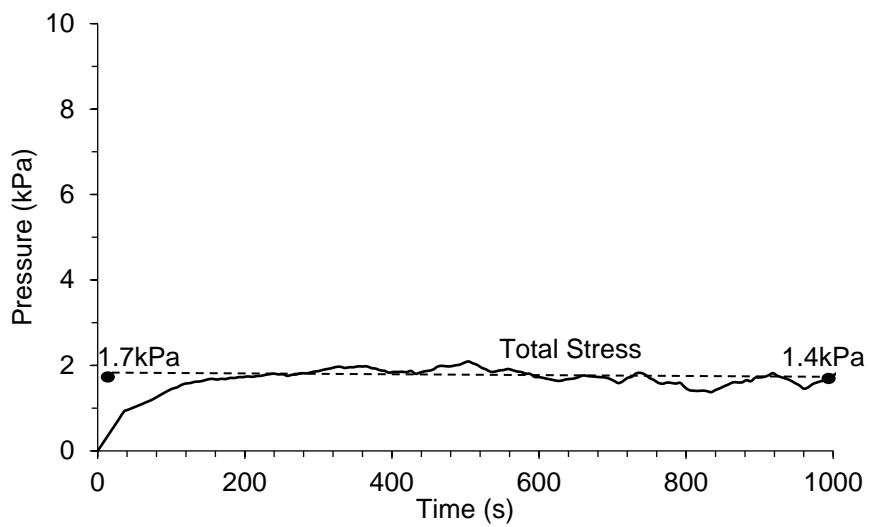
Figure 6: Change in settlement profiles during shaking (28Sr60b)



(a)



(b)



(c)

Figure 7: Typical pore pressures in the well-graded materials with 18% fines (18Sr70) measured at the (a) bottom, (b) middle and (c) top

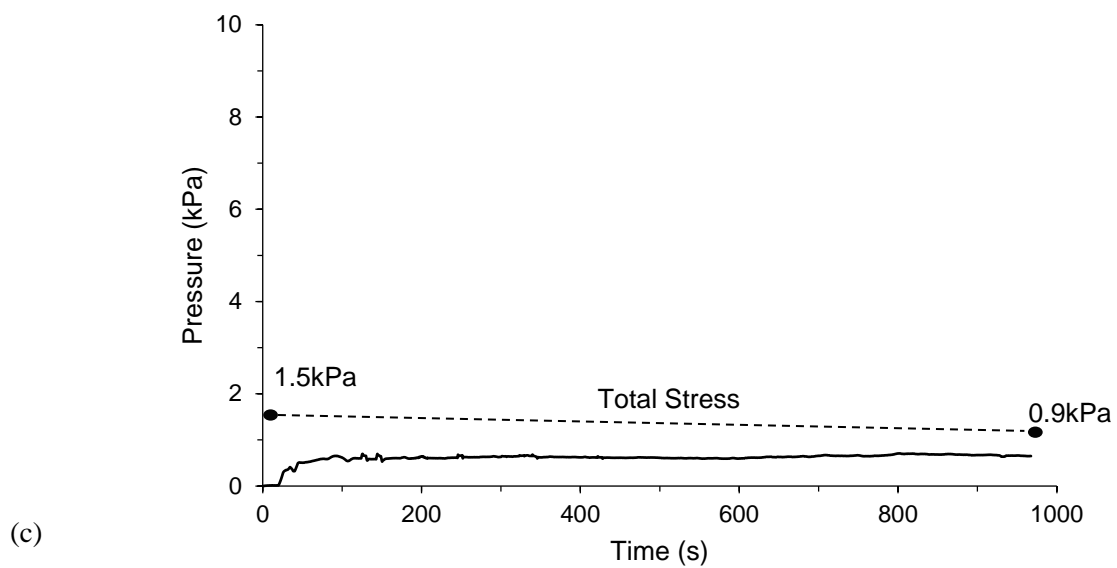
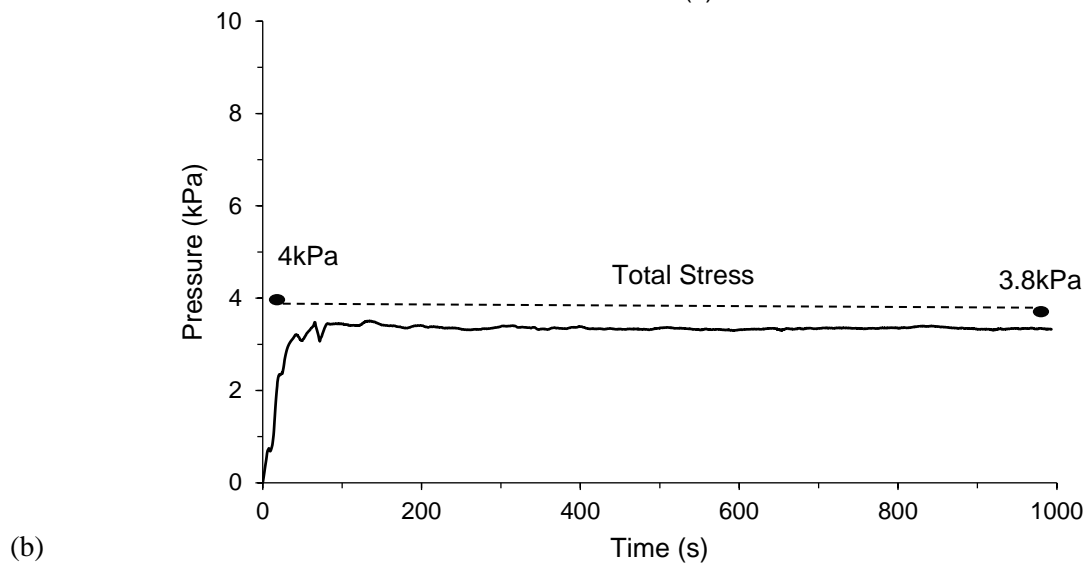
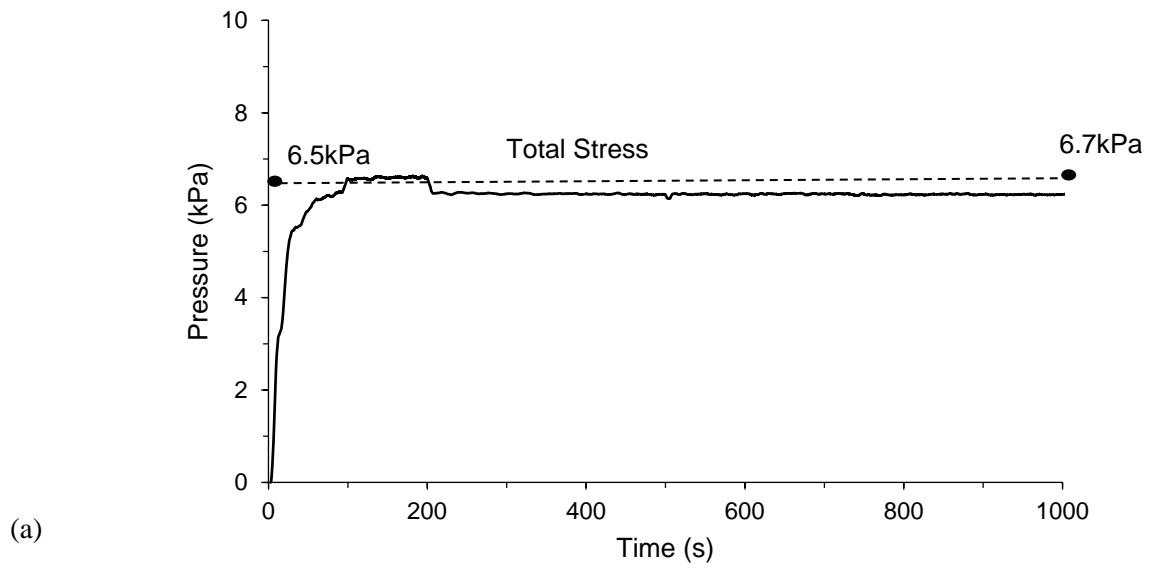
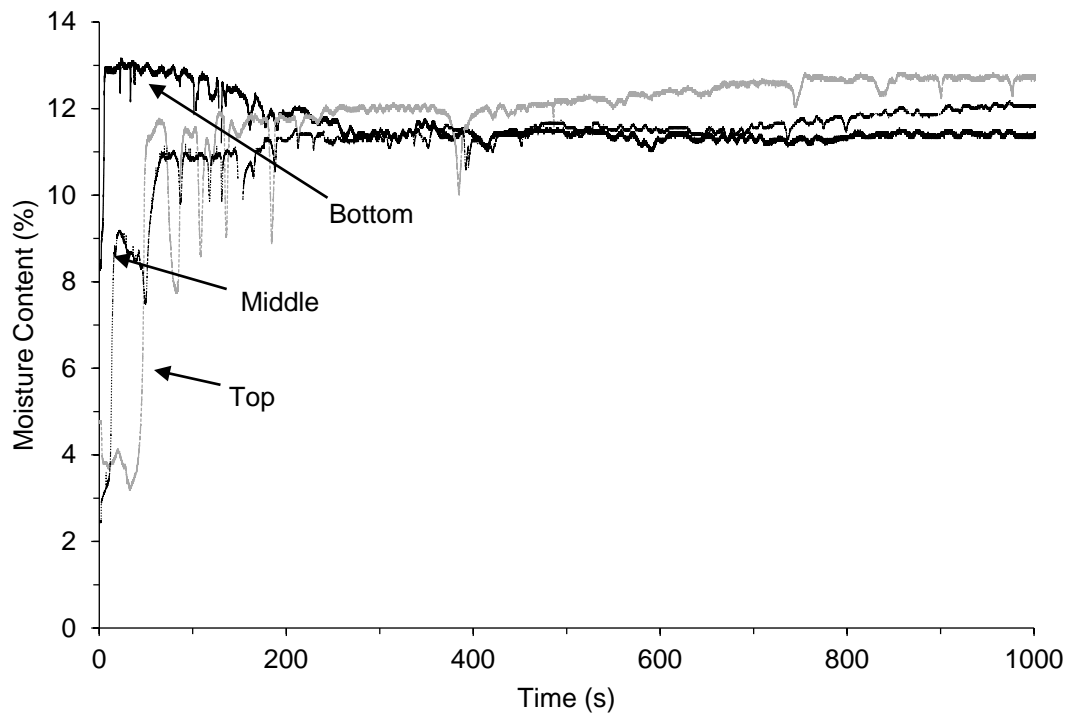


Figure 8: Typical pore pressures in the well-graded materials with 28% fines (28Sr62) measured at the (a) bottom, (b) middle and (c) top



(a)

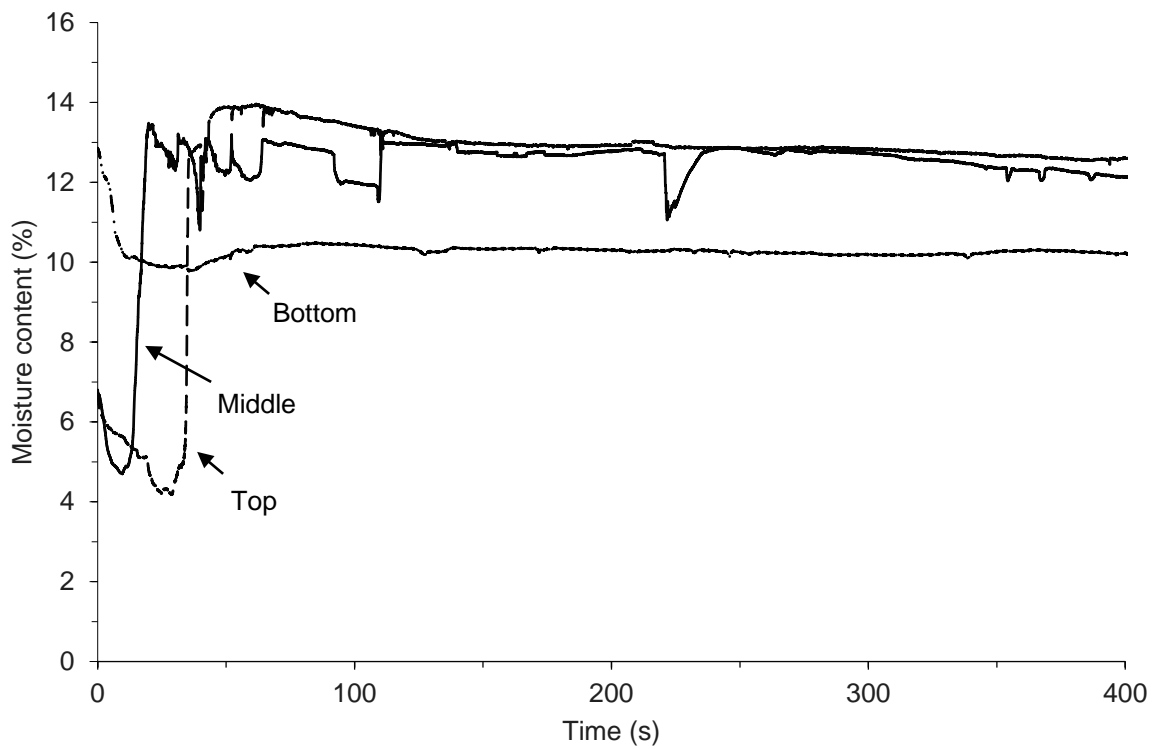


Figure 9: Comparison of moisture contents measured at the bottom, middle and top of samples (a) 28Sr62 and (b) 28Sr72

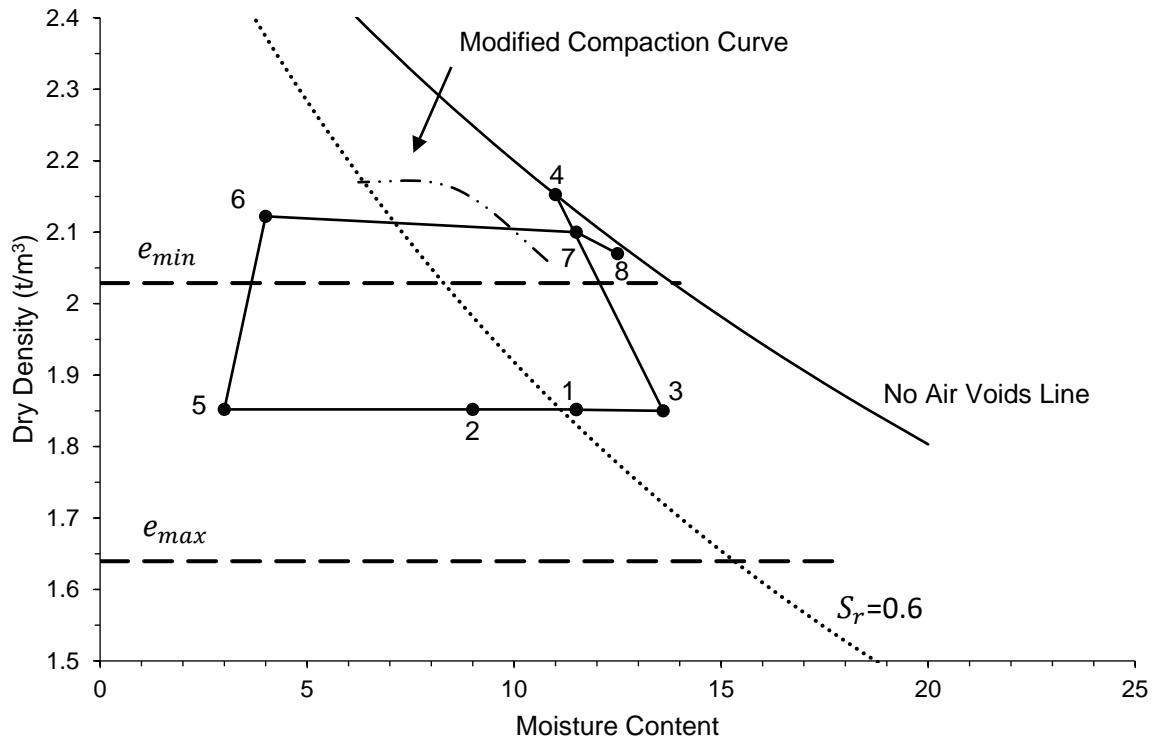


Figure 10 Schematic showing typical moisture and density paths at bottom and top moisture content probe locations during shaking (28Sr62).

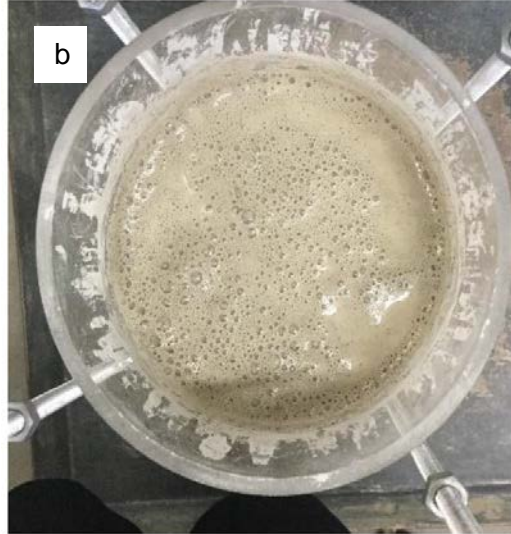
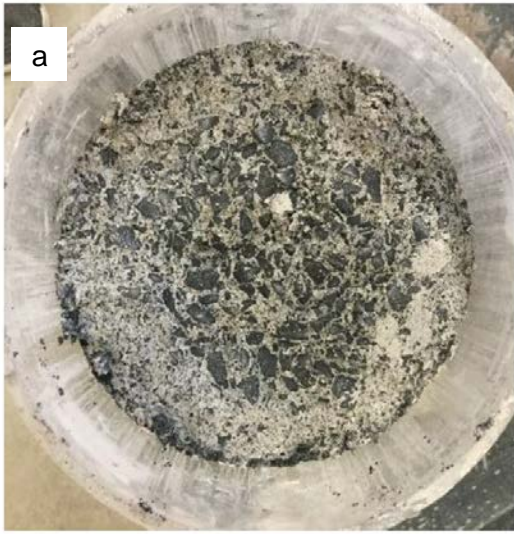
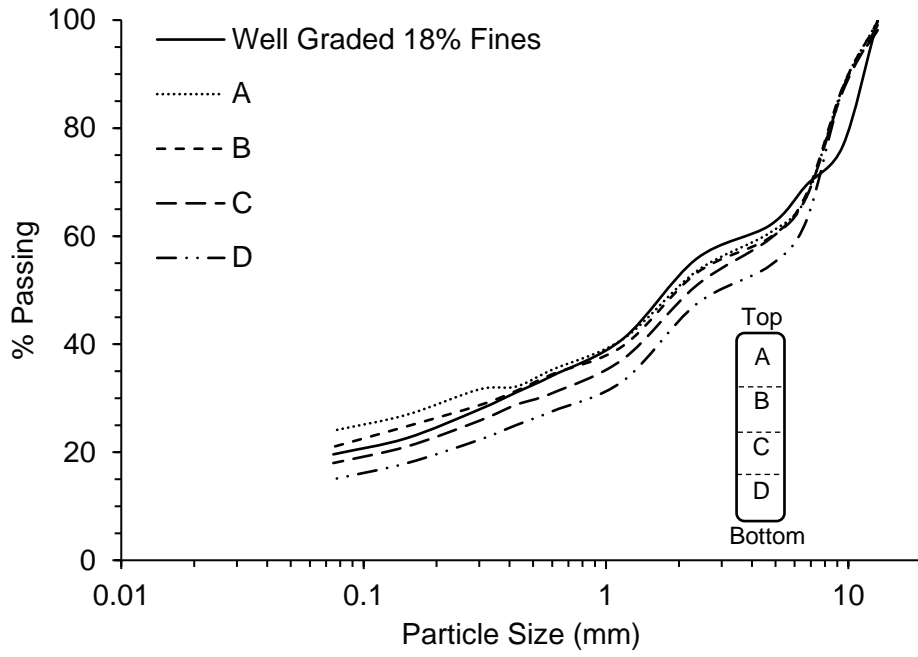
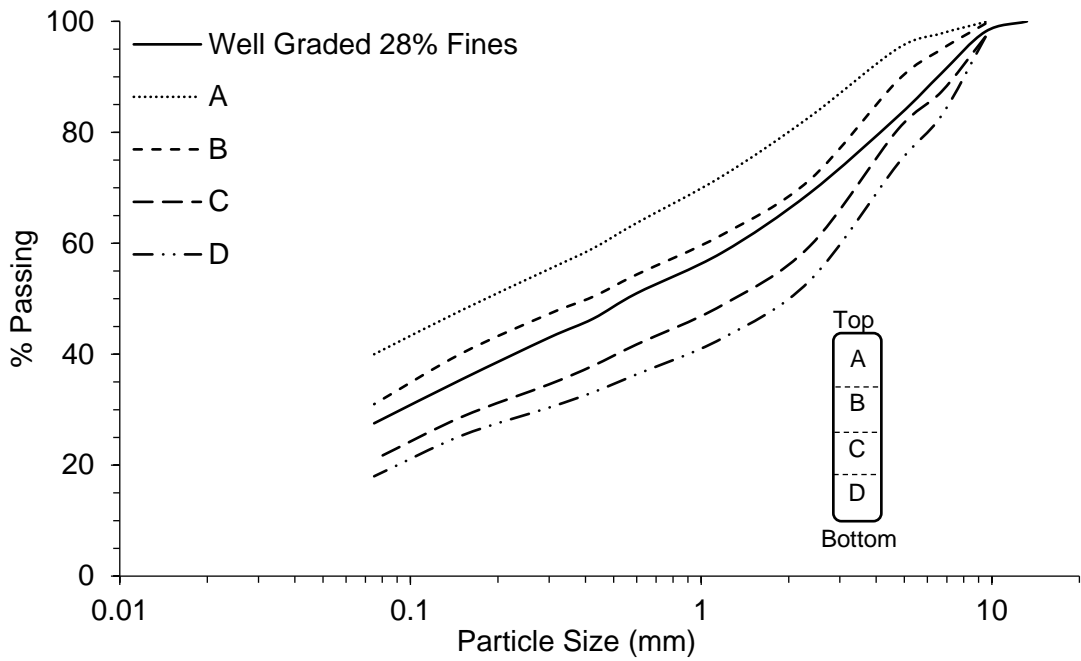


Figure 11: Photographs of the (a) bottom and (b) top of the column

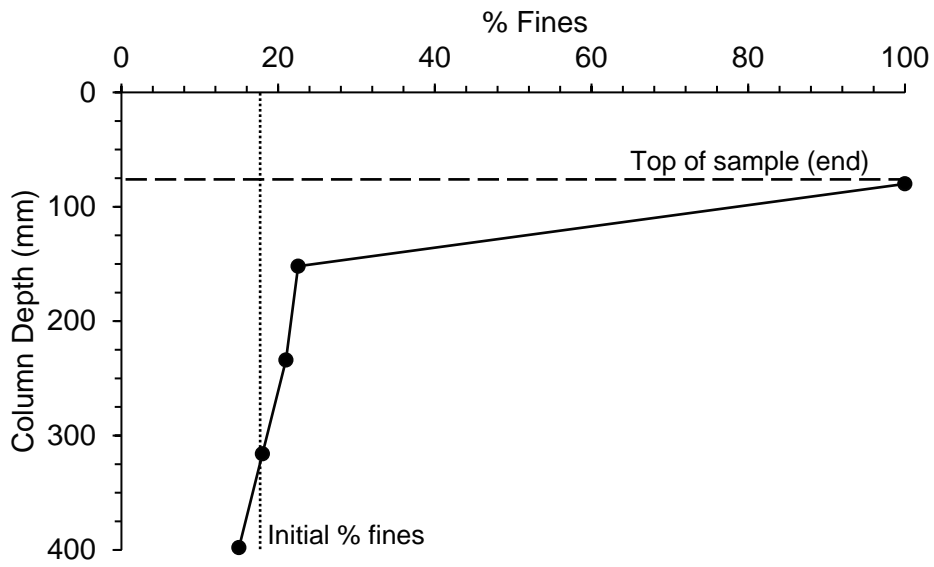


(a)

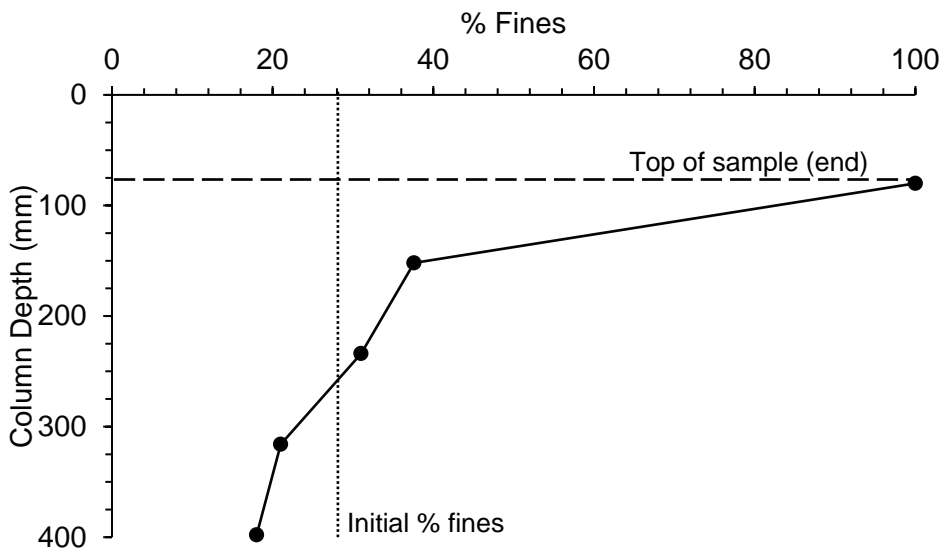


(b)

Figure 12: Sieve analysis performed on layers throughout the column containing the well-graded material with (a) 18% Fines and (b) 28% Fines



(a)



(b)

Figure 13: Typical distribution of fines throughout column after shaking in the well-graded materials containing (a) 18% fines and (b) 28% fines

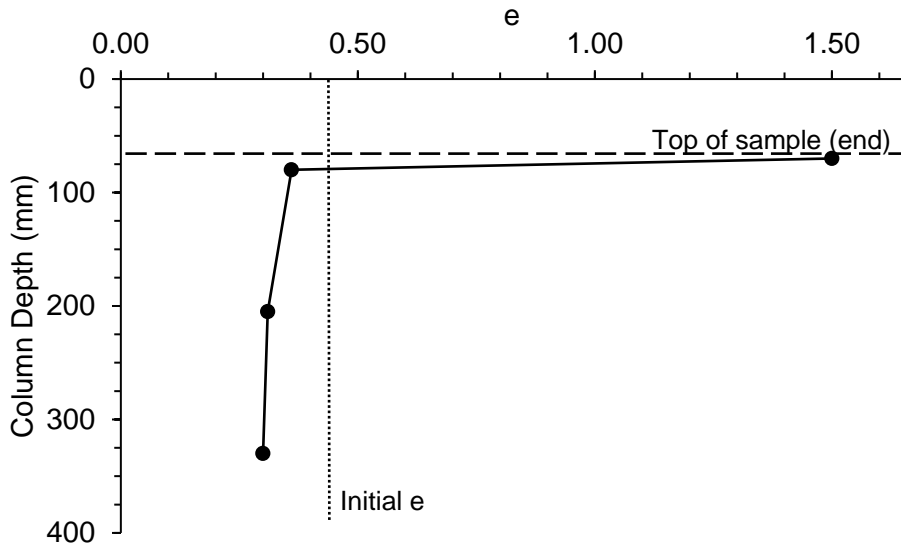


Figure 14: Typical distribution of the back calculated void ratios throughout column after shaking in the well-graded material containing 28% fines required to maintain a constant degree of saturation of within the column

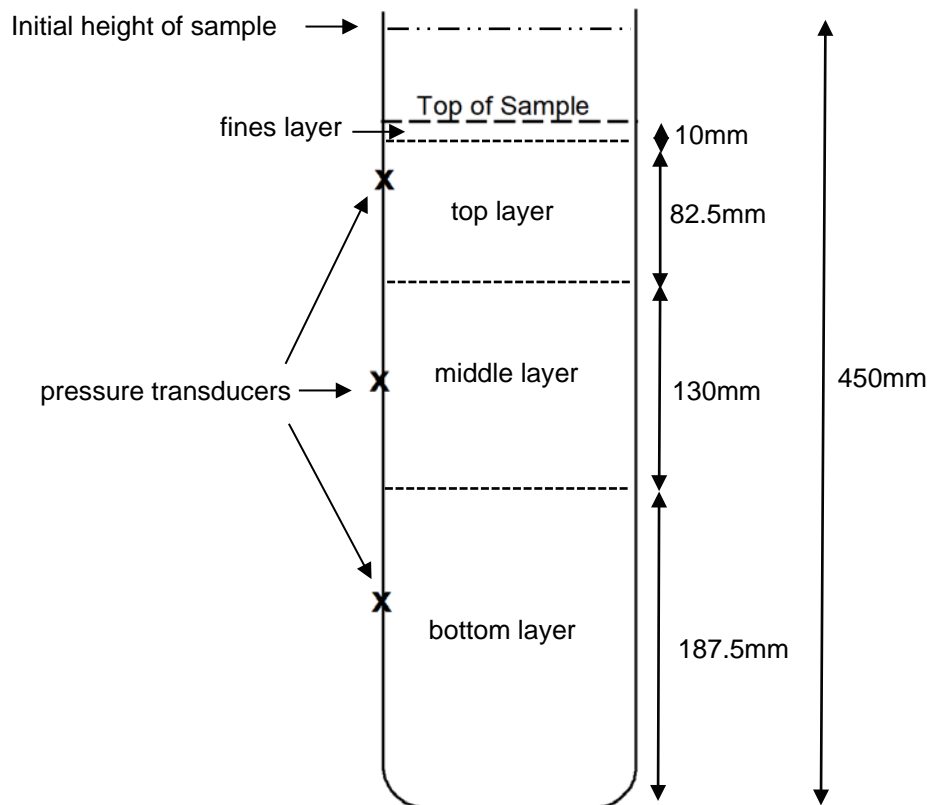


Figure 15: Diagram of column with dimensions of layers