Airplane-Aided Integrated Next-Generation Networking

Muralikrishnan Srinivasan¹, Sarath Gopi², Sheetal Kalyani², Xiaojing Huang³, Lajos Hanzo⁴

Abstract—A high-rate yet low-cost air-to-ground (A2G) communication backbone is conceived for integrating the space and terrestrial network by harnessing the opportunistic assistance of the passenger planes or high altitude platforms (HAPs) as mobile base stations (BSs) and millimetre wave communication. The airliners act as the network-provider for the terrestrial users while relying on satellite backhaul. Three different beamforming techniques relying on a large-scale planar array are used for transmission by the airliner/HAP for achieving a high directional gain, hence minimizing the interference among the users. Furthermore, approximate spectral efficiency (SE) and area spectral efficiency (ASE) expressions are derived and quantified for diverse system parameters.

I. INTRODUCTION

Next-generation wireless standards are expected to cope with increased traffic demands and support emerging applications even in remote locations such as rural hinterlands, mountains, deserts and even for vessels such as cruise-ships in the oceans [1]. However, the operational fifth-generation (5G) standards have predominantly been designed for terrestrial communications. One of the promising techniques of augmenting cellular communication is through air-based platforms such as unmanned aerial vehicles (UAV) or high-altitude platforms (HAP). Hence, extensive research has been dedicated to the design, channel modelling, and security of UAV-based cellular communications [2]–[5], as well as to their performance analysis [6]–[15]. Sakaee and Jamalipour [16] along with Kato [17] showed as early as 2006 that the probability of finding at least two But potentially up to dozens of aircraft capable of establishing an AANET above-the-cloud is close to 100%. It was inferred by investigating a snapshot of flight data over the United States (US). They also proposed a quality of service (QoS) based so-called multipath Doppler routing protocol by jointly considering both the QoS and the relative velocity of nodes in order to find stable routing paths.

Integrating the aerial networks with the terrestrial networks has the potential of increasing both the data rate and the coverage quality of terrestrial networks [18]–[23]. There have also been some attempts to integrate the space networks with terrestrial networks or to provide Internet coverage for airliner [24]–[31]. The applicability of these prior contributions are tabulated in I. However, most of these contributions rely on reusing the existing long-term evolution (LTE) bands, which are already congested in the sub-6GHz bands [32], [33]. Therefore, the creation of a high-capacity integrated space terrestrial network (ISTN) or a space-air-ground integrated network (SAGIN) is still elusive at the time of writing both due to the bandwidth limitation of aerial backbones and owing to the limited area spectral efficiency (ASE) of the air-to-ground (A2G) systems, given their large footprint on the ground. Therefore, it is imperative to explore new architectures integrating the existing terrestrial networks with space networks.

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TABLE I INTEGRATED AERIAL-TERRESTRIAL NETWORKS IN SUB-6GHZ BAND

A. Related Contributions:

A critical cornerstone of the next-generation systems is the potential exploitation of millimetre wave (mmWave) carrier frequencies to benefit from their broad unused spectrum. Hence the authors of [34]–[39] have investigated the challenges of mmWave based A2G and air-to-air (A2A) communications. For example, the two-ray propagation model’s applicability in different scenarios employing UAVs was explored in [34]. The pros and cons of UAV-BS in complementing the mmWave backhaul were demonstrated in [35]. The concept of mmWave A2A networks was first explored by Cuvelier and Heath [37], while mmWave based HAPs in terrestrial transmissions were studied in [38], [39].

As a further development, Huang et al. [1] have proposed the ISTN concept relying on civil airliner networks and mmWave communication to form a high-capacity yet low-cost A2A and A2G communications backbone employing high-gain antenna arrays. In this concept, the airliners act
as an efficient network-provider for terrestrial users, since the distance from the planes to the ground is much shorter than that from the satellite. Furthermore, to provide A2G cellular coverage for small cells that can support high ASE, adaptive beamforming is proposed. In areas where the civil-airliners cannot be used, dedicated HAPs would be used as the backbone. A similar topology is presented in [40, Fig 1].

B. Design challenges:

To actually design such a high-capacity airline-aided integrated network, several challenges have to be addressed. For example, a cruising airliner maintains an altitude of at least 10 km from the ground, while solar-charged unmanned aircraft are envisioned to circle above 20 km for avoiding civilian planes. The mmWave channel suffers from substantial pathloss owing to raindrops, high-absorption and other atmospheric effects, especially at a carrier frequency of 73.5 GHz. Another challenge to overcome is the huge channel estimation overhead, which results from the rapidly fluctuating high-Doppler channel between the cruising airliner and ground users. Hence, a careful selection of the channel model, antenna dimensions, Rician factor and other system parameters is required for investigating a realistic stand-alone model.

C. Contributions

To overcome the above-mentioned challenges, we design a high-performance system having a high data-rate and ASE and provide theoretical performance guarantees with the aid of approximate expressions. We consider a planar-array aided stand-alone airliner/HAP in a macro-cell communicating with the terrestrial BS/users. Although a strong line-of-sight (LoS) component exists between the airplane and the ground users, the non-line-of-sight (NLoS) component fluctuates drastically over time. Hence, to achieve a high directional gain while minimizing the users’ interference, we propose three different channel-agnostic transmit precoding schemes for avoiding the massive pilot overhead required for estimating the channel-state information (CSI) or the NLoS component. Explicitly, our Transmit Precoders (TPC) rely only on the users’ position relative to the airliner and they are quite robust to incorrect Doppler compensation and position vector mismatches.

We also derive approximate expressions for the SE/ASE of the users. Furthermore, the proposed schemes are evaluated through extensive simulations, and its performance is compared to the analytically obtained values. Additionally, depending on the dimensions of the planar array and of the LoS factor, the ASE achieved by our system becomes several times higher than that of conventional terrestrial networks [50]–[53] capable of providing data rates on the order of several Gbps. The authors of [41]–[49] have considered 3D beamforming in the context of UAV communications, where most of them tended to rely either on UAVs flying at a modest altitude or on channel-aware TPCs. Specifically, the authors of [49] designed a TPC relying on the effective channel matrix between the access point (AP) and the users. Therefore, a dedicated downlink channel estimation phase is required by the TPC. By contrast, in our case, the channel between the airliner and the user is dominated by the LoS component due to the airliner’s altitude. Typically the aeronautical model for such a scenario has a strong LoS path and a much weaker NLoS ground-reflected path [54]. Hence using a TPC vector relying on the estimated channel matrix is counter-productive. Furthermore, in such a highly mobile scenario, accurate channel estimation requires a potentially excessive pilot overhead. Explicitly, compared to the pedestrian walking across a mmWave cell at 5 km/hr, a plane travelling at 1000 km/hr would require a 200 times higher pilot overhead. Even if we disregard the huge training overhead requirement, the CSI is prone to estimation error.

Against the above backdrop, we boldly contrast our novel contributions to the prior art in Table II. The theoretical analysis of the proposed system and our extensive simulations indicate that our design leads to high capacity airplane-aided integrated networks that are eminently suitable for filling the coverage-holes of next-generation wireless systems.

The rest of the paper is structured as follows. In Section II, the proposed system design is discussed in detail, along with different beamforming. In Section III, theoretical expressions are derived for the ASE/SE using the popular use and forget bound. In Section IV, our simulation results and interesting design guidelines are discussed, while in Section V, some future research directions are provided.

II. PROPOSED SYSTEM DESIGN

In this section, we design the ISTN backbone and propose a system model using various adaptive beamforming for supporting high data-rates and seamless connectivity. Consider a circular macro-cell of radius $R$ with an airliner at its centre at an altitude $H_l$. The radius $R$ is chosen to be at least 5 km, so a minimum inter-airliner distance of 10 km is maintained. In remote locations outside the regular flight path, HAPs can be installed for providing seamless connectivity to satellites. Free-space optical (FSO) links connect them to Low-Earth orbit (LEO)/medium-Earth orbit (MEO) satellites as their high-speed backhaul.

Each airliner/HAP is equipped with a planar antenna having $M \times M$ equally spaced elements. Without loss of generality, it can be assumed that the antenna elements are parallel to the ground and the centre of the antenna is the origin $(0, 0, 0)$. The macro-cell is further divided into several tightly packed micro-cells of radius $r << R$. Each micro-cell supports a single time-frequency block. The users can either be a cellular user equipment (CUE) or even an LTE base station, which in turn supports several UEs. The intended user is at position $(x_0, y_0, -H_l)$, and the micro-cell containing it is referred to as the micro-cell of interest (MCI).

Assume that there are $N_1, N_2, ..., N_J$ interfering micro-cells in the first $J$ tiers using the same time-frequency block. The centres of these micro-cells are located at distances $D, 2D, ..., JD$ from the MCI, where $D$ denotes the reuse distance. Let $N_I = N_1 + N_2 + ... + N_J$ be the total number of interfering cells and let the coordinates of these interfering users be $(x_i, y_i, -H_l) i = 1, ..., N_I$. All the users are assumed to have
a single antenna. Let \((\theta^z_i, \theta^a_i)\) represent the zenith and azimuth angle pair for the \(i^{th}\) user, which are:

\[
\theta^z_i = \tan^{-1}\left(\frac{\sqrt{x_i^2 + y_i^2}}{-H_i}\right), \quad i = 0, \ldots, N_I
\]  

(1)

and

\[
\theta^a_i = \tan^{-1}\left(\frac{y_i}{x_i}\right), \quad i = 0, \ldots, N_I.
\]

(2)

Here \(i = 0\) represents the user under consideration, while \(i = 1, \ldots, N_I\) represent the interferers. The entire system is shown in Fig. 1.

![Fig. 1](image)

Note that the typical cruising airliner altitudes are in the 9 – 12 km range. At such distances, the mmWave channels’ attenuation, say at 73.5 GHz, is significant. Existing contributions, such as [43]–[45], [47], [48], which deal with aerial mmWave networks, consider only low-flying UAVs or low altitude platforms (LAPs) and hence suffer from relatively low attenuation. In the absence of beamforming at the transmitter, the users in the macro-cell suffer from mutual interference, resulting in a reduced data-rate. Therefore, to reduce the mutual interference amongst the users and improve the spectral efficiency, some form of adaptive beamforming must be used by the airliner’s planar array. Furthermore, the adaptive beamforming schemes must be robust to incorrect Doppler compensation and position vector mismatches. We therefore propose three different beamforming or TPC schemes at the Airliner/HAP. The design of the beamforming vectors is described in the subsequent paragraphs.

A. Null-steered beamforming (NSB) design

NSB relies on signal processing techniques for creating transmit nulls and maxima in the undesired and desired receivers’ directions, respectively, for mitigating the interference [42], [55], [56]. For \(i = 0, 1, \ldots, N_I\), let \(e_i\) be the \(M \times 1\) vector representation of the \(i^{th}\) user’s steering vector with respect to each of the components of the planar array. The three-dimensional Cartesian co-ordinates of the \((m, n)^{th}\) component of the planar array are represented by \((x_m, y_n, 0)\), where \(x_m = \left[- \frac{M-1}{2} + \frac{(m-1)}{2}\right]\) and \(y_n = \left[- \frac{M-1}{2} + \frac{(n-1)}{2}\right]\), for \(m = 1, \ldots, M\) and \(n = 1, \ldots, M\). Note that the inter-elemental spacing is \(\lambda/2\), where \(\lambda\) is the wavelength of the carrier. Thus the entry of \(e_i\), which corresponds to the position of the user with respect to the \((m, n)^{th}\) element of the planar array, is given by \(\exp\left[\frac{2\pi}{\lambda} (x_m \psi^x_i + y_n \psi^y_i)\right]\), where we have

\[
\psi^x_i = \sin \theta^z_i \cos \theta^a_i,
\]

(3)

and

\[
\psi^y_i = \sin \theta^z_i \sin \theta^a_i,
\]

(4)

while \(\theta^z_i\) and \(\theta^a_i\) are defined in (1) and (2), respectively, which are functions of the user location. Now the null-steered beamforming vector \(\hat{e}_i\) used by the airliner is

\[
\hat{e}_i = e_i - E_i (E_i^H E_i)^{-1} E_i^H e_i, \forall i = 0, 1, \ldots, N_I,
\]

(5)
where $\mathbf{E}_i$ is the matrix whose columns are the steering vectors, except for $e_i$, which is given by:

$$
\mathbf{E}_i = \begin{bmatrix} 0 & e_2 & \ldots & e_{i-1} & e_{i+1} & \ldots & e_{N_I} \end{bmatrix}.
$$

(6)

This can be obtained by solving the following optimization problem [57]:

$$
\min_{\mathbf{e}_i} \| \mathbf{e}_i - \mathbf{e}_i \|^2
$$

such that $\mathbf{e}_i^H \mathbf{E}_i = 0$. 

(7)

NSB may also be interpreted as a zero-forcing precoder, where the precoding vectors only require the knowledge of the user location.

B. Null-Steered Beamformer with Derivative Constraints (NS-B-D)

The NSB detailed in Section II-A can be extended by adding additional derivative constraints [57, 3.7.2]. The higher order derivatives of the directional pattern in the directions of nulls are set to zero to broaden the beam-widths, to make the TPC robust to mismatches in the steering vector. In this paper, we explicitly add the following first-order derivative constraints to (7):

$$
\hat{\mathbf{e}}_i = \frac{\partial}{\partial \theta_i} \mathbf{e}_i = 0 \quad \forall \quad i = 0, 1, \ldots, N_I
$$

$$
\bar{\mathbf{e}}_i = \frac{\partial}{\partial \bar{\theta}_i} \mathbf{e}_i = 0 \quad \forall \quad i = 0, 1, \ldots, N_I.
$$

(8)

Solving the optimization problem yields the beamforming vector $\mathbf{e}_i$ as [57]:

$$
\mathbf{e}_i = \mathbf{e}_i - \bar{\mathbf{E}}_i \left( \mathbf{E}_i^H \bar{\mathbf{E}}_i \right)^{-1} \mathbf{E}_i^H \mathbf{e}_i \quad \forall \quad i = 0, 1, \ldots, N_I,
$$

(9)

where

$$
\bar{\mathbf{E}}_i = \begin{bmatrix} e_0 & e_1 & \ldots & e_{i-1} & e_{i+1} & \ldots & e_{N_I} \end{bmatrix}.
$$

Note that (9) is similar to (6) except that $\mathbf{E}$ is replaced with $\bar{\mathbf{E}}$, which includes the derivative constraints of all the users.

C. Minimum-Power Distortionless Response Beamformer (MPDRB)

Another popular beamformer is the MPDRB, where the total output power is minimized subject to a distortionless constraint [57]. In other words, one can determine the steering vectors $\mathbf{e}_i$ so that the total power $\| \mathbf{e}_i^H \mathbf{E}_i \|^2$ subject to a distortionless constraint is minimized, which is formulated as:

$$
\min_{\mathbf{e}_i} \| \mathbf{e}_i^H \mathbf{E}_i \|^2 \quad \text{such that} \quad \mathbf{e}_i^H \mathbf{e}_i = 1,
$$

(11)

where $\mathbf{E}_i = \begin{bmatrix} e_0 & e_1 & \ldots & e_{i-1} & e_{i+1} & \ldots & e_{N_I} \end{bmatrix}$. Solving the optimization problem results in [57]:

$$
\bar{\mathbf{e}}_i = \frac{\mathbf{E}_i^H \mathbf{E}_i}{\mathbf{E}_i^H \mathbf{E}_i^H} \mathbf{e}_i.
$$

(12)

However, note that specific to our application, even for a $200 \times 200$ planar array, since the position vectors are of dimensions $40000 \times 1$, the dimension of the matrix $\mathbf{E}_i \mathbf{E}_i^H$ is $40000 \times 40000$, and hence ill-conditioned. To circumvent ill-conditioning, one can apply the singular value decomposition (SVD) of $\mathbf{E}_i$, to obtain the inverse in the numerator of (12). Let $\mathbf{U}$ and $\mathbf{D}$ be the left singular value matrix and diagonal matrix of singular values, respectively. Since there are $N_I + 1$ users, there will be $N_I + 1$ non-zero singular values. If $\mathbf{D}_{N_I+1}$ and $\mathbf{U}_{N_I+1}$ are the diagonal matrix of non-zero singular values and the corresponding left singular value matrix, then we can compute $\mathbf{e}_i$ in (12) as

$$
\bar{\mathbf{e}}_i = \mathbf{U}_{N_I+1} \mathbf{D}_{N_I+1}^{-2} \mathbf{e}_i.
$$

(13)

where $\mathbf{e}_i = \mathbf{U}_i^H \mathbf{e}_i$. Note that, the MPDRB relies on all the user locations in the minimization criterion, including the actual desired receiver location. Similar to the case of NSB, additional derivative constraints can be added to the MPDRB formulation to make it robust. However, evaluating the solution in this case will be time-consuming using popular software such as MATLAB, owing to the $M \times M$ dimensional $\mathbf{E}_i \mathbf{E}_i^H$.

The system’s efficacy under the different beamforming schemes is determined by a pair of popular metrics, namely the ASE and the SE, which are functions of various system parameters, like the Rician factor $K$, the array dimensions $M \times M$, or the micro-cell radius, etc. In the next section, we derive the approximate expressions of the performance metrics, followed by extensive simulation results for characterizing the system.

III. THEORETICAL APPROXIMATIONS FOR ASE/SE

It is essential for us to characterize the SINR and then derive theoretical expressions for our metrics, such as the ASE and SE. To begin with, let $\alpha_i$ $i = 0, 1, \ldots, N_I$ represent the symbol intended for the $i$th user. Without loss of generality, let $i = 0$ denote the user under consideration and $i = 1, \ldots, N_I$ denote the interferers in the other micro-cells. The symbol received by the user is

$$
y = \sqrt{P_t} \mathbf{h}_{0,Ric}^H \mathbf{e}_0 \alpha_0 + \sqrt{P_t} \sum_{i=1}^{N_I} \mathbf{h}_{0,Ric}^H \mathbf{e}_i \alpha_i + n,
$$

(14)

where $n$ represents the complex Gaussian noise having the power of $\sigma^2 = kTBN_F$, with $k = 1.374 \times 10^{-21}$ being Boltzmann’s constant, $T$ the temperature in Kelvins, $B$ the bandwidth, and $N_F$ the noise figure of the receiver. The received power is given by:

$$
P_r = \frac{P_t G_t G_r}{\nu \nu},
$$

(15)

where $P_t$ is the power transmitted from the Airliner/HAP, $G_t$ and $G_r$ are the transmitter and receiver antenna gains, while $\nu \nu$ includes the frequency-dependent atmospheric loss as well as the back-off loss of the modulation scheme. Finally, the term $\nu \nu$ represents the path-loss given by [58]:

$$
\nu = 20 \log \left( \frac{\pi d f_c}{c} \right) dB = \left( \frac{40 \pi d f_c \sigma_{GHz}}{3} \right)^2,
$$

(16)

where $c = 3 \times 10^8$ $m/s$ is the speed of the light, $d$ is the distance from the airliner/HAP to the user in meters and
\( f_c \cdot \text{GHz} \) is the carrier-frequency in GHz. The Rician fading channel between the Airliner/HAP and the user is represented by:

\[
h_{i, \text{Ric}} = \sqrt{\frac{K}{1+K}} e_i + \sqrt{\frac{1}{1+K}} h_i \mathbf{1},
\]

(17)

where \( K \) is the Rician factor and \( h_i \) is the NLoS component, while 1 is the vector of ones. Furthermore, the NLoS component \( h_i \) is a complex Gaussian random variable (RV) with zero mean and unit variance. The instantaneous SINR is now given by the following theorem.

**Theorem 1.** The instantaneous signal to interference plus noise (SINR) \( \gamma_{\text{SINR}} \), of the desired user under NSB is given by \(^1\):

\[
\gamma_{\text{SINR}} = \frac{P_r |X_s|^2}{\sum_{i=1}^{N} P_i |X_i|^2 + \sigma^2},
\]

(18)

where \( X_s \sim \mathcal{CN}(\mu, \sigma_s^2) \), with

\[
\mu = \sqrt{\frac{K}{1+K}} \left( M_0 - e_0^H \mathbf{E}_0 \left( \mathbf{E}_0^H \mathbf{E}_0 \right)^{-1} \mathbf{E}_0^H e_0 \right),
\]

(19)

and

\[
\sigma_s^2 = \frac{1}{1+K} \left\| \mathbf{1}^H \left( 1 - \mathbf{E}_0 \left( \mathbf{E}_0^H \mathbf{E}_0 \right)^{-1} \mathbf{E}_0^H \right) e_0 \right\|^2.
\]

(20)

Furthermore, still referring to (18), we have \( X_i \sim \mathcal{CN}(0, \sigma_i^2) \), where

\[
\sigma_i^2 = \frac{1}{1+K} \left\| \mathbf{1}^H \left( 1 - \mathbf{E}_i \left( \mathbf{E}_i^H \mathbf{E}_i \right)^{-1} \mathbf{E}_i^H \right) e_i \right\|^2.
\]

(21)

*Proof. For the proof, please see Appendix A.*

Assuming that the users in a cell are allocated identical bandwidths, the Area Spectral Efficiency (ASE) is defined as the sum of the maximum bit rate/Hz/unit area supported by the cell’s Airliner/HAP [50]:

\[
\text{ASE} = \frac{C}{\pi(D/2)^2},
\]

(22)

where \( C \) is the capacity of the intended user in Bps/Hz. Given \( \gamma_{\text{SINR}} \), the average channel capacity is formulated as:

\[
\bar{C}_{\text{SINR}} = \mathbb{E} \log_2 \left( 1 + \gamma_{\text{SINR}} \right)
\]

\[
\approx \int_0^\infty \log_2 \left( 1 + \gamma_{\text{SINR}} \right) f(\gamma_{\text{SINR}}) d\gamma_{\text{SINR}},
\]

(23)

where \( \mathbb{E}[.] \) represents the expectation and \( f(\gamma_{\text{SINR}}) \) denotes the pdf of \( \gamma_{\text{SINR}} \). By applying the popular use-and-forget bound of [59], the approximate average channel capacity is given by

\[
\bar{C}_{\text{app}} = \mathbb{E} \log_2 \left( 1 + \gamma_{\text{SINR}} \right)
\]

\[
\approx \log_2 \left( \frac{P_r \mathbb{E}[|X_s|^2]}{\sum_{i=1}^{N} P_i \mathbb{E}[|X_i|^2] + \sigma^2} \right),
\]

(24)

where we have \( \mathbb{E}[|X_s|^2] = \sigma_s^2 + \mu^2 \) and \( \mathbb{E}[|X_i|^2] = \sigma_i^2 \). Thus, the average ASE in bps/Hz/m\(^2\) is formulated as:

\[
\text{ASE}_{\text{app}} = \frac{4 \bar{C}_{\text{app}}}{\pi D^2}.
\]

(25)

\(^1\) Very similar expressions can be derived for the other two schemes, but omitted here given the page limit.

Similarly, the average SE of the user is given by

\[
\text{SE}_{\text{SINR}} = \bar{C}_{\text{app}}.
\]

(26)

Note that the average capacity is a function of \( \mu, \sigma_s^2 \) and \( \sigma_i^2 \), \( i = 1, \ldots, N_1 \), which are parameterized by \( \theta^c_i \) and \( \theta^a_i \) for \( i = 0, \ldots, N_1 \), the zenith and azimuth angles of all the users. Furthermore, the angles themselves are functions of the relative locations of the desired user and the interferers through (1) and (2), respectively. Therefore, the total average capacity is obtained by averaging the expressions over the user locations. Recall that the beamforming vectors are only dependent on the user positions, but not on the channel-gains. Note that, the approximations are universal, straightforward and are applicable for any value of \( K \), received power \( P_r \) and other system parameters.

**IV. Simulation Results**

![Simulation Results](image)

**TABLE III**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Macro-cell radius ( R )</td>
<td>5 – 20 km</td>
</tr>
<tr>
<td>Micro-cell radius ( r )</td>
<td>50 m, 75 m, 100 m</td>
</tr>
<tr>
<td>Vertical airliner/HAP distance ( H_t )</td>
<td>10 km, 21 km</td>
</tr>
<tr>
<td>Carrier frequency ( f_c )</td>
<td>73.5 GHz</td>
</tr>
<tr>
<td>Total Bandwidth ( B )</td>
<td>5 GHz</td>
</tr>
<tr>
<td>Reuse factor</td>
<td>7</td>
</tr>
<tr>
<td>Bandwidth per User</td>
<td>714 MHz</td>
</tr>
<tr>
<td>Dimensions of the planar array ( M )</td>
<td>200, 300, 400, 500</td>
</tr>
<tr>
<td>Rician factor ( K )</td>
<td>10, 15, 30 dB</td>
</tr>
<tr>
<td>Back-Off</td>
<td>10 dBm</td>
</tr>
<tr>
<td>Transmitter loss</td>
<td>1.8 dB</td>
</tr>
<tr>
<td>Transmitter antenna gain</td>
<td>10 log(( M^2 ))</td>
</tr>
<tr>
<td>Atmospheric and cloud loss</td>
<td>7.9 dB</td>
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<tr>
<td>Receiver antenna gain</td>
<td>60.2 dB</td>
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<tr>
<td>Receiver noise figure</td>
<td>6 dB</td>
</tr>
<tr>
<td>Other receiver loss</td>
<td>1.8 dB</td>
</tr>
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</table>

Extensive Monte-Carlo simulations have been carried out for evaluating the ASE and SE of the system, assuming that

![Simulation Results](image)

```latex
\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{Sim.png}
\caption{Average ASE of NSB vs. distance of MCI from the macro-cell centre for \( M = 500 \) and \( H_t = 10 \) km. The theoretical result is based on (25).}
\end{figure}
```
the Airliner/HAP is located at $(0, 0, 0)$. The desired UE is positioned uniformly in the MCI of radius $r$ with its centre located at $(x, y, -H_t)$. For a frequency reuse factor of 7, the reuse distance is fixed at approximately $D = 4r$. We consider the five tiers of interfering micro-cells with their centres set to $4kr, \forall k = 1, ..., 5$ from the MCI. The interfering UEs are also uniformly placed in the interfering micro-cell of radius $r$. The interferences imposed by the more distant tiers of micro-cells and macro-cells are assumed to be negligible. To represent a strong LoS component, we consider the Rician factors $K$ to be 10, 15 and 30 dB. All the other transmission parameters were proposed initially in [1] and are summarized in Table III for completeness.

In Fig. 2, the simulated and approximate ASE of NSB are plotted vs. the horizontal distance of the MCI from the airliners, for several Rician factors $K$ and micro-cell radii $r$. Naturally, upon increasing $K$, the ASE/SE increases. Since the ASE is inversely proportional to the cell-radius, it decreases upon increasing the micro-cell radius $r$. However, the ASE fails to reach its maximum, when the MCI is directly below the airliner, namely when the MCI is at the macro-cell centre. The ASE is a function of both the MCI distance from the airliners as well as of $K$ and of the micro-cell radius $r$. For example, for $r = 50$ m and $K = 30$ dB, an ASE as high as $1200 \text{bps/Hz/km}^2$ is achieved when the user is at a distance of 5 km from the macro-cell centre. At the macro-cell centre, the ASE is reduced to $600 \text{bps/Hz/km}^2$.

When the desired user is at the macro-cell centre, the interferers are distributed in all the quadrants; hence their azimuth angles are uniformly distributed in $[0, 360]$ degrees. Even if we choose $M = 500$, the power consumption does not exceed 0.8 kW for a Tx power of 5 dBm.

Now, as the desired user moves away from the macro-cell centre, there are two effects. Firstly, the range of azimuth angles of the interferers decreases because the first five tiers of interferers we consider are concentrated in a single quadrant. Secondly, the absolute value of the zenith angles ($\theta_z$) of the interference increases from $0^\circ$ as we move away from the macro-cell centre. Both these effects increase the correlation between the desired and interfering users’ steering vectors, hence reducing the power of the null-steering vectors. Therefore, both the signal and interference powers are reduced as the micro-cell centre moves away from the macro-cell centre. Near the macro-cell centre the reductions of both the signal and interference powers become similar and hence the ASE fluctuates. However, as the micro-cell centre moves further away, the interference power reduction is more substantial than the signal power reduction and hence the ASE increases. Further away, the desired power reduction becomes substantial and hence the ASE decreases. The SE variations vs. the distance can also be explained using similar reasoning. Furthermore, for higher altitudes of the airliner, the SINR of the users decreases owing to their higher path-loss. Therefore, the ASE decreases, as observed in Fig. 3. Note that the ASE achieved by the massive MIMO scheme of [51] is on the order of 10 $\text{bps/Hz/km}^2$, while our scheme achieves in the order of $1000 \text{bps/Hz/km}^2$, which is comparable to the ASE achieved by the HetNet and DenseNet of [52] and [53], respectively. The transmit (Tx) power at each of the antenna elements needs to be carefully chosen depending on the noise power, the number of antenna elements, and the power consumption allowed at the transmitter. For a Tx power of 30 dBm, power consumption of 40 kW is incurred for $M = 200$. Whereas for a Tx power of 5 dBm, power consumption of only 0.126 kW is incurred, without any drop in the ASE. Even if we choose $M = 500$, the power consumption does not exceed 0.8 kW for a Tx power of 5 dBm.

2The number of interfering tiers to be chosen is based on an engineering trade-off that varies with the distance from the macro-cell centre. For example, for MCI at the centre of macro-cell (directly below the airliner), considering three tiers of interferers is sufficient. In the case of the macro-cell edge, 5 tiers of interferers are needed for $r = 50$ m.

3The signal and interference powers are approximately of the order of $10^6$ and $10^{-6}$ respectively. At a reuse distance $D = 200$ m, the SE and ASE are $38 \text{bps/Hz}$ and $1200 \text{bps/Hz/km}^2$ approximately.

4Though a smaller Tx power can be chosen with no drop in the ASE, we have chosen 5 dBm to account for unforeseen practical losses.
The ASE and SE variations of NSB vs. M are portrayed in Fig. 4 and 5. An array dimension of $500 \times 500$ provides the highest ASE. For an antenna element spacing of $\lambda/2$, where $\lambda = 4$ mm is the career wavelength, the array dimensions will not exceed $1 \ m^2$. The increase in ASE vs. $M$ remains marginal compared to that vs. the Rician factor $K$. For example, for an increase in $M$ from 200 to 500, the ASE improves from approximately 300 to 400 bps/Hz/km$^2$ respectively. On the other hand, for an increase in $K$ from 10dB to 30dB, the ASE improves from 300 to 550 bps/Hz/km$^2$, respectively. With an increase in micro-cell radius, we observe a SE reduction in Fig. 5. However, the reduction is only marginal compared to the ASE reduction seen in Fig.2.

In Fig. 6, the simulated ASE is plotted vs the horizontal distance of the MCI from the airliners for various beamforming techniques. We can observe that NSB-D performs nearly as well as NSB, provided that the MCI is near the macrocell centre. However, recall that as the distance of the MCI increases, the correlation between the desired and interfering users’ steering vectors increases, hence reducing the beamforming vectors’ power. Coupled with the widening of beam by the derivative constraints, a drastic output SINR, and ASE reduction, is observed. For example, for an MCI at a distance of 10 km from the macrocell centre, the ASE of NSB-D is nearly half of that of NSB. A similar trend can be observed in SE for different $K$ values, as seen in Fig. 7. On the other hand, MPDRB provides the lowest ASE of the three beamformers. For example, for an MCI at a distance of 2.5 km from the macrocell centre, the ASE of MPDRB is nearly third of that of NSB. However, note that MPDRB is more robust to variations in the distance of the MCI from the macrocell centre. The correlation between the desired and interfering users’ steering vectors does not contribute to a significant ASE reduction because it does not explicitly create nulls in the interfering users’ directions, unlike NSB and NSB-D.

A. Doppler compensation

We note that all the above simulations considered an idealized setting for which the Doppler spread was neglected. However, in a practical system, it is necessary to compensate for the Doppler frequency offset (DFO) caused by the airliner’s radial velocity component with respect to the user location. Since the velocity reading of the high-speed airliner are perfectly known at the transmitter, the Doppler shift due to this motion can be pre-compensated [60]. Assuming that the airliner is heading in the $0^\circ$ azimuth-direction, the radial component of the velocity vector towards the angle pair $(\theta_i^a, \theta_i^r)$ is

$$v_r = v_a \cos \theta_i^a \sin \theta_i^r,$$

where $v_a$ is the airplane’s speed. Hence, the Doppler-induced frequency deviation in the $(\theta_i^a, \theta_i^r)$-direction is given by

$$f_D = \frac{1 - \frac{v_r}{c}}{1 + \frac{v_r}{c}} f_r,$$
where $c$ is the speed of light and $f_T$ is the carrier frequency. To pre-compensate for the spread in frequency, the airplane can transmit at a frequency of
\[
f_T = \frac{(1 + \frac{\nu_r}{c})}{(1 - \frac{\nu_r}{c})} f_c, \quad (29)
\]
so that at the user end, the received signal frequency will be $f_c$ after Doppler shift. Note that for an average airplane speed of 200 m/s and a high carrier frequency of 73.5 GHz, the Doppler offset is negligible, since $(1 \pm \frac{\nu_r}{c}) \approx 1$. In some cases, the radial component of the velocity towards the angle pair can be incorrectly estimated as
\[
\nu_r = v_a \cos \theta_i \sin \theta_i^r + \Delta \nu_r v_a \cos \theta_i^a \sin \theta_i^r, \quad (30)
\]
where $\Delta \nu_r$ is the offset/error in the estimation with $\Delta \nu_r = 0$ indicating perfect estimation. In such a case, we can observe that the pre-compensation results in the airplane transmitting at a frequency of
\[
f_T = \frac{(1 + \frac{\nu_r}{c})}{(1 - \frac{\nu_r}{c})} f_c, \quad (31)
\]
which after the Doppler spread results in
\[
f_c = \frac{(1 - \frac{\nu_r}{c})}{(1 + \frac{\nu_r}{c})} (1 + \frac{\nu_c}{c}) f_c \quad (32)
\]
at the user end. In Table IV, the average ASE is tabulated for the different beamformers operating with and without incorrect frequency offset estimation. It can be noted that even for a 50% error in estimating the offset, corresponding to $\Delta \nu_r = \pm 1$, the degradation in the ASE is moderate. The degradation is the lowest for NSB-D, because the derivative constraints increase the beam-width towards the user directions and increase the robustness to steering vector mismatches.

\begin{table}[h]
\centering
\begin{tabular}{|c|c|c|c|c|c|}
\hline
Beamformer & $\Delta \nu_r = -1$ & -0.5 & 0 & 0.5 & 1 \\
\hline
NSB & 963 & 969 & 969 & 969 & 965 \\
NSB-D & 907 & 908 & 909 & 908 & 907 \\
MPDRB & 215 & 215 & 217 & 216 & 215 \\
\hline
\end{tabular}
\caption{Average ASE expressed in $\text{bps/Hz/km}^2$ vs $\Delta \nu_r$ for $M = 200$, $K = 30 \text{ dB}$, $r = 50 \text{ m}$, $H_t = 10 \text{ km}$ and MCI at a distance of 2.5 km from the macrocell centre.}
\end{table}

**B. Position vector mismatches**

One of the essential requirements for the proposed technique is the signalling of the user locations at the airplane. The users can estimate their location using a global positioning system (GPS) and communicate it to the airplane with a local base station’s aid. A high precision technique such as real-time kinematic (RTK) processing or carrier phase differential tracking can be employed [61]. Alternatively, it is possible to continuously track the user from the airplane by periodically sending signals to the users. In other words, the established methods of precise positioning of high-speed vehicles can be used to get an accurate estimate of the user location [62], [63]. Given precise estimates of the users’ locations and the airplane’s velocity, sub-meter position accuracy can be obtained for accurate beamforming [64].

We study the performance of the beamformers for up to 5 m offset in the users’ position. Let us assume that the coordinates of the users and the interferers are incorrectly measured as $(x_i + \delta \cos \beta_i, y_i + \delta \sin \beta_i, -H_i)$, $i = 0, 1, \ldots, N_I$, where $\delta$ is the magnitude of the offset and $\beta_i$ is the random phase. The average ASE for various values of $\delta$ (in metres) is shown in Table V. We observe that NSB-D is more robust to position vector mismatches than NSB. NSB-D also outperforms NSB in the presence of position vector mismatches due to its broader beamwidth. For example, for an MCI at 3.5 km, with no position vector mismatch, i.e., $\delta = 0$, the ASE of NSB-D is 763 bps/Hz/km², and that of NSB is 1025 bps/Hz/km². For $\delta = 1$ m, the ASE is nearly halved in the case of NSB, whereas the degradation is negligible for NSB-D. Although MPDRB is also resistant to position vector mismatches compared to NSB, the overall ASE obtained still remains lower.

Both the theory and simulations indicate substantial ASE gains for our proposed airplane-aided integrated network. However, our work only represents the first step towards realizing a high-capacity ISTN; hence it relies on some idealized simplifying assumptions to be eliminated by future research.

\begin{table}[h]
\centering
\begin{tabular}{|c|c|c|c|c|c|}
\hline
Beamformer & MCI (km) & $\delta = 0$ & $\delta = 0.5$ & $\delta = 1$ & $\delta = 5$ \\
\hline
NSB & 1 & 637 & 528 & 474 & 329 \\
 & 2.5 & 969 & 544 & 480 & 335 \\
 & 3.5 & 1025 & 538 & 478 & 332 \\
NSB-D & 1 & 580 & 580 & 580 & 550 \\
 & 2.5 & 908 & 908 & 867 & 599 \\
 & 3.5 & 763 & 763 & 746 & 496 \\
MPDRB & 1 & 221 & 221 & 221 & 220 \\
 & 2.5 & 220 & 220 & 218 & 217 \\
 & 3.5 & 215 & 215 & 214 & 214 \\
\hline
\end{tabular}
\caption{Average ASE expressed in bps/Hz/km² vs $\delta$ for $M = 200$, $K = 30 \text{ dB}$, $H_t = 10 \text{ km}$ and $r = 50 \text{ m}$.}
\end{table}

V. Conclusions and Directions for Future Research

In this treatise, we considered a planar-array aided stand-alone airliner/HAP in a macro-cell communicating with the terrestrial BS/users. To achieve a high directional gain and to minimize the interference among the users, we invoked three beamforming techniques, namely NSB, NSB with derivative constraints, and MPDRB, for transmission from the airliner/HAP and provided approximate SE and ASE expressions. We also studied the performance of the system for incorrect Doppler compensation and position vector mismatches. NSB was the least complex TPC scheme that provided maximum ASE, in the absence of position vector mismatches. However, NSB-D was more robust to position vector mismatches and MPDRB more robust to variations in the distance of the MCI from the macrocell centre.

We considered a simple system, where the airliner is the network provider for the terrestrial users. The routing protocols, traffic-offloading and optimizing the tele-traffic resources in conjunction with the existing terrestrial and space networks require careful further study. An interesting future study would
quantify the effect of the desired beam-squint encountered by the proposed schemes [65]–[67]. A possible solution to overcome this problem could be to partition the entire band into multiple narrower bands and apply a phase shift based beamformer separately. Furthermore, the hybrid beamforming techniques discussed in [67]–[73] could be adopted for overcoming the beam-squint effects and for reducing the power consumption. Another critical topic that can be explored is the impact of mobility and real flight schedule on the handovers between the different macro-cells and the existing networks. Finally, the optimal radius of micro-cells used at different distances from the macro-cell centre is another exciting future research direction.

APPENDIX A

Proof for Theorem 1

The array gain of the desired user is $X_s = h_{0,Ric}^H \tilde{e}_0$ and that of the $i$th interferer is $X_i = h_{i,Ric}^H \tilde{e}_i$. In order to determine the distribution of the SINR, we have to determine the distribution of the components in the numerator and the denominator. Upon expanding $X_s$, we arrive at,

$$X_s = h_{0,Ric}^H \tilde{e}_0 = \sqrt{\frac{K}{1 + K}} \left( e_0^H e_0 - e_0^H E_0 \left( E_0^H E_0^{-1} E_0^H e_0 \right) \right) + \frac{1}{1 + K} h_0^1 H \left( 1 - E_0 \left( E_0^H E_0^{-1} E_0^H \right) e_0 \right). \quad (33)$$

Observe that by construction, we have:

$$e_i^H e_i = \begin{cases} M^2; & i = j \\ \sin \left( \frac{1}{2} \left( \psi_i^x - \psi_j^x \right) \right) \sin \left( \frac{1}{2} \left( \psi_i^y - \psi_j^y \right) \right); & i \neq j \end{cases} \quad (34)$$

where $\psi_x$ and $\psi_y$ are defined in (3) and (4), respectively. Since, $h$ is a zero-mean Gaussian RV with unit variance, it can be readily seen that $X_s$ is a Gaussian RV with a mean given by (19) and variance by (20). Now the $i$th interference component is formulated as:

$$X_i = h_{i,Ric}^H \tilde{e}_i = \left( \sqrt{\frac{K}{1 + K}} e_i^H + \frac{1}{1 + K} h_i^1 H \right) \tilde{e}_i = \left( \sqrt{\frac{K}{1 + K}} e_i^H + \frac{1}{1 + K} h_i^1 H \right) \left( 1 - E_i \left( E_i^H E_i^{-1} E_i^H \right) e_i \right), \quad (35)$$

where the null-steering beamforming vectors $\tilde{e}_i$ are designed in such a way that $e_i^H \tilde{e}_i \approx 0$, $\forall i \neq j$. Hence, the RV $X_i$ has a negligible mean component. On the other hand, $X_s$ has a variance given by (21).

REFERENCES


