# Strong light-matter coupling in microcavities characterised by Rabi-splittings comparable to the Bragg stop-band widths

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**Abstract.** The vacuum Rabi splitting of polaritonic eigenmodes in semiconductor microcavities scales with the square root of the oscillator strength, as predicted by the coupled oscillator model and confirmed in many experiments. We show here that the square root law is no more applicable if the Rabi splitting becomes comparable or larger than the stop-band width of the Bragg mirrors forming the cavity. Once the oscillator strength becomes large enough, the material hosting excitons hybridises with the quasi-continuum microcavity Bragg modes lying outside of the stop-band, thus forming a novel kind of polaritonic resonance. We study this physics considering both two- and three-dimensional excitonic materials embedded in the microcavity. We highlight the varied phenomenology of those polaritons and develop a theoretical understanding of their most peculiar features.

## 1. Introduction

Quantum wells embedded in semiconductor Bragg microcavities have been one of the first systems in which the resonant mode splitting between light and matter has been observed [1]. The study of exciton-polaritons, the hybrid light-matter excitations of such heterostructures, have blossomed in an extremely rich field of research, with proposed applications spanning optoelectronics [2], superconductivity [3], analog simulations [4], quantum technologies [5], optical computing [6], and machine learning [7].

Most studies to date have focused on an idealised system in which a single excitonic resonance couples to a single discrete photonic mode. Such an approach is adequate when the coupling between light and matter is larger than the intrinsic resonance linewidth, but otherwise much smaller than all the other energy scales. It instead breaks down when, exploiting a number of advances in the design of both resonators and quantum emitters [8], the coupling becomes comparable to other energy scales, ushering us into a zoology of non-perturbative coupling regimes [9, 10].

In particular, when the coupling becomes comparable to the energy difference between different matter resonances [11], the interaction between light and matter doesn't cause only Rabi oscillations between the bare light and matter excitations, but it can modify the electronic wavefunction of the system [12]. In this way polaritonics becomes a tool to modify the underlying electronic properties of the material [13]. The impact of such physics becomes even greater when the effect of the ionization continuum is taken into account, causing not only renormalization of the system's parameters [14, 15], but also the possibility of creating novel bound excitons kept together by photon exchange [16, 17].

In this work we investigate the dual case in which the interaction energy between a discrete excitonic resonance and a microcavity exceeds the width of the microcavity stopband, thus coupling to the complex quasi-continuum structure of Bragg-modes. To this aim we consider two model systems, schematised in Fig. 1. In Fig. 1(a), a thin layer of dipoles is placed at the center of a microcavity. For definiteness we will refer to this layer as a quantum wells (QWs) [18, 19], but it could as well describe other 2-dimensional materials embedded in the microcavity [20, 21, 22]. In Fig. 1(b) instead the cavity is completely filled by a bulk homogeneous excitonic material, as organic molecules [23] or polar dielectrics hosting bulk optical phonons.

In a rigorous semiclassical framework we consider the vacuum Rabi frequency, quantifying the light-matter coupling strength, as an adjustable parameter, varying from zero to the frequency of the bare optical transition. Note that although achievable couplings in inorganic excitonic microcavities are substantially smaller [8], interesting effects become apparent already for values of the coupling comparable with the microcavity stopband width. Such a regime can be achieved by combining microcavities with narrow index contrast with samples with multiple QWs [12], or 2D material layers [24]. Organic microcavities are instead characterised by much larger light-matter coupling strengths when compared to their inorganic counterparts [25, 26], allowing to

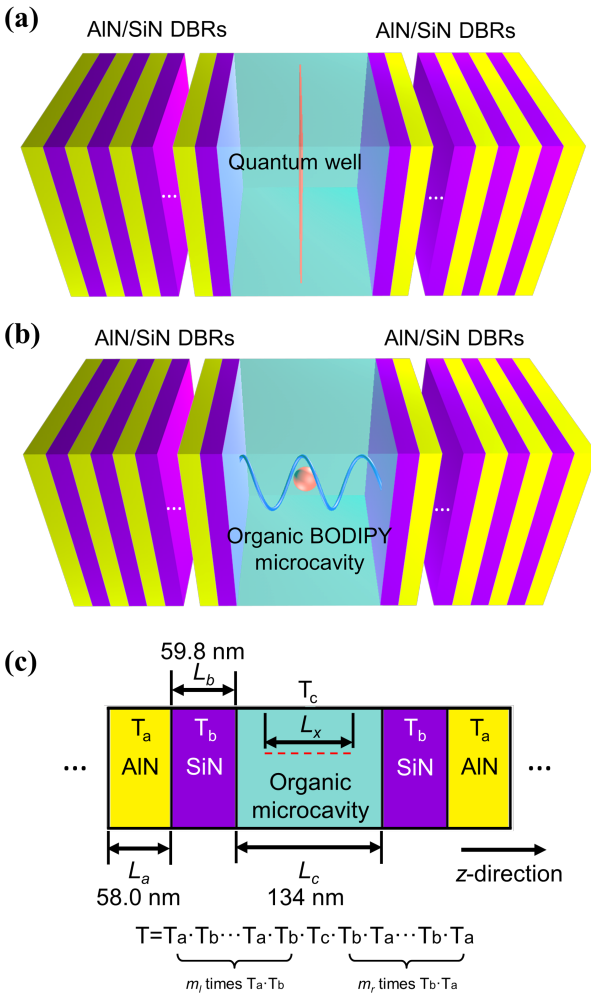


**Figure 1.** Schematic illustration of the two classes of planar optical microcavities considered in this work.
(a) The central layer between the two mirrors is filled with an optically inert material embedding a thin excitonic material in its center, e.g., a quantum well.
(b) The central layer between the two mirrors is filled with a bulk excitonic material, e.g., organic molecules with large oscillator strength like BODIPY.
(c) parameters of elementary cells in the structure. $T_a$, $T_b$ and $T_c$ in Eq. 7 stand for the transfer matrices of AlN, SiN mirror and microcavity, with length of $L_a$, $L_b$ and $L_c$, respectively. $L_x$ indicates the length of excitonic material in microcavity. The transfer matrix T across the entire structure is multiplication of elementary transfer matrix of optical layers. The expression shown is for the case $L_x = L_c$ in which the cavity is completely filled with excitonic material. $m_l$ and $m_r$ indicate the number of optical unit cells composing left and right Bragg mirror.

cover much of the parameter space considered in this paper. Moreover, the coupling strength of organic microcavities can be optically modified [27], allowing us to tune the DBR reflectivity in situ.

We start by presenting the transfer matrix semiclassical calculation of the model microcavity response which will allow us to predict a number of effects in different configurations, namely: (i) the deviation of the Rabi-splitting dependence on the exciton oscillator strength from the well-known square root law, (ii) the strong coupling of exciton with both the cavity photon mode and some of the Fabri-Perot modes confined between upper and lower surfaces of the structure (Bragg modes), (iii) a parity filtering effect that consists in the coexistence of the strong coupling regime of the exciton with Bragg modes of a certain parity and zero exciton-coupling with modes of the opposite parity, (vi) a strongly asymmetric reflectivity, due to the opening of a polaritonic Reststrahlen band. We will also verify that some of the features we observe can be reproduced with a simplified quasimode quantum approach, thus strengthening the relevance of our modal interpretation.

## 2. Theoretical framework

### *2.1. Model systems*

We consider a model structure that represents an optical microcavity sandwiched between two identical Bragg mirrors, as shown in Fig. 1, each mirror being a finite-size distributed Bragg reflector (DBR). Each DBR represents a periodic structure whose period is composed of two different layers with thicknesses $L_a$ and $L_b$ and refractive indices $n_a$ and $n_b$. The Bragg interference condition is then satisfied if $n_a L_a = n_b L_b$. The cavity is a $\lambda/2$-cavity characterised by a length $L_c$ and a refractive index $n_c$, leading to a fundamental cavity resonance of angular frequency $\omega_c = \frac{\pi c}{n_c L_c}$. The structure is surrounded by vacuum with a refractive index $n_{ext} = 1$.

The central section of the cavity, of length $L_x$, is filled with an excitonic material characterised by the non-local susceptibility

$$\chi(z, z', \omega) = \sum_j \tilde{\chi}_j(\omega) \Phi_j^*(z) \Phi_j(z'), \tag{1}$$

where $j$ indexes the normal-to-the-plane modes, with envelope functions $\Phi_j(z)$, $z$-direction is orthogonal to the planar system as shown in Fig. 1(c), $z$ and $z'$ are coordinates along $z$-axis.

$$\tilde{\chi}_j(\omega) = \frac{n_c^2 \Omega_R^2 \frac{\omega_x}{\omega_0}}{\omega_j^2 - \omega^2 - 2i\omega\gamma}, \tag{2}$$

is the local susceptibility. In Eq. 2 $\omega_j$ is the frequency of the $j^{th}$ optically active mode, $\gamma$ the intrinsic matter losses, $\Omega_R$ the resonant vacuum Rabi frequency, proportional to the square root of the oscillator strength, and $\omega_x = \frac{2\pi c}{n_c L_x}$ is the frequency of a propagating electromagnetic mode with wavelength $L_x$. Note that in this formalism the factor $\omega_x \propto L_x^{-1}$ in the numerator of Eq. 2 assures that the value of $\Omega_R$ is an

extensive property of the system, allowing us to perform a fair comparison between excitonic materials of different dimensionality, although the relation between $\Omega_R$ and the polariton splitting will involve a geometric factor of the order of 1.

For the QW case, see Fig. 1(a), we consider that modes beyond the lowest one (e.g., higher order excitons) are out of resonance and only retain the lowest ($j = 0$) optically-active mode, with frequency $\omega_0$. Here, we introduce the reflection and transmission coefficients containing resonant excitonic contributions, to describe a QW. We consider the case where light is incident normally on a planar structure. We denote the amplitudes of incident, reflected and transmitted light as $A_1^+$, $A_1^-$ and $A_2^+$, respectively. The reflection coefficient $r$ is defined as the ratio of amplitudes of reflected light and incident light, $r = A_1^-/A_1^+$. The transmitted coefficient $t$ is defined as the ratio of amplitudes of transmitted light and incident light, i.e. $t = A_2^+/A_1^+$. The QW layer is characterized by a reflection coefficient $r_{QW}$ and transmission coefficient $t_{QW} = 1+r_{QW}$. Following Ref. [18] they can be expressed in the form

$$r_{QW}(\omega) = \frac{\frac{i\omega}{2n_c c}\tilde{\chi}_0(\omega)\left[\int \Phi_0(z)\cos(kz)dz\right]^2}{1-\frac{i\omega}{2n_c c}\tilde{\chi}_0(\omega)\left[\int \Phi_0(z)\cos(kz)dz\right]^2}, \tag{3}$$

with $\omega = \frac{ck}{n_c}$ and $c$ the speed of light in vacuum. Assuming that the excitation profile is uniform across the layer of width $L_x \ll 1/k$ we then arrive at the expression for the amplitude reflection coefficient of the QW [28]

$$r_{QW} = \frac{i\pi\Omega_R^2}{\frac{\omega_0}{\omega}(\omega_0^2-\omega^2) - 2i\omega_0\gamma - i\pi\Omega_R^2}. \tag{4}$$

Using different boundary conditions and excitation envelope functions would lead to analogous results (e.g., the Pekar boundary conditions would lead to a reduction of the vacuum Rabi frequency by a factor $\approx 0.9$). Note that in order to be able to take into account arbitrary coupling strengths, we went beyond the usually employed single-pole approximation for the QW reflectivity [18] and used instead the full form of the susceptibility from Eq. 2.

In the bulk case, shown in Fig. 1(b), we consider instead the excitations to be dispersionless (that is $\omega_j = \omega_0 \ \forall j$ ). This is usually a good approximation for bulk active resonances as optical phonons, bulk excitons, or organic microcavities, although the effect of dispersion can lead to observable non-local effects in sub-wavelength structures [29, 30, 31]. Neglecting the frequency dispersion of the exciton resonance and, as a consequence, neglecting the spatial dispersion in the cavity layer allows us to simplify the non-local susceptibility exploiting the orthonormality condition $\sum_j \Phi_j^*(z)\Phi_j(z') = \delta(z-z')$, leading to a local polarization function

$$\mathbf{P}(\omega) = \epsilon_0\tilde{\chi}_0(\omega)\mathbf{E}(\omega), \tag{5}$$

where $\mathbf{E}(\omega)$ is the local electric field. The local dielectric function can be derived from Eq. 5 and written as

$$\epsilon_B(\omega) = n_c^2 + \tilde{\chi}_0(\omega). \tag{6}$$

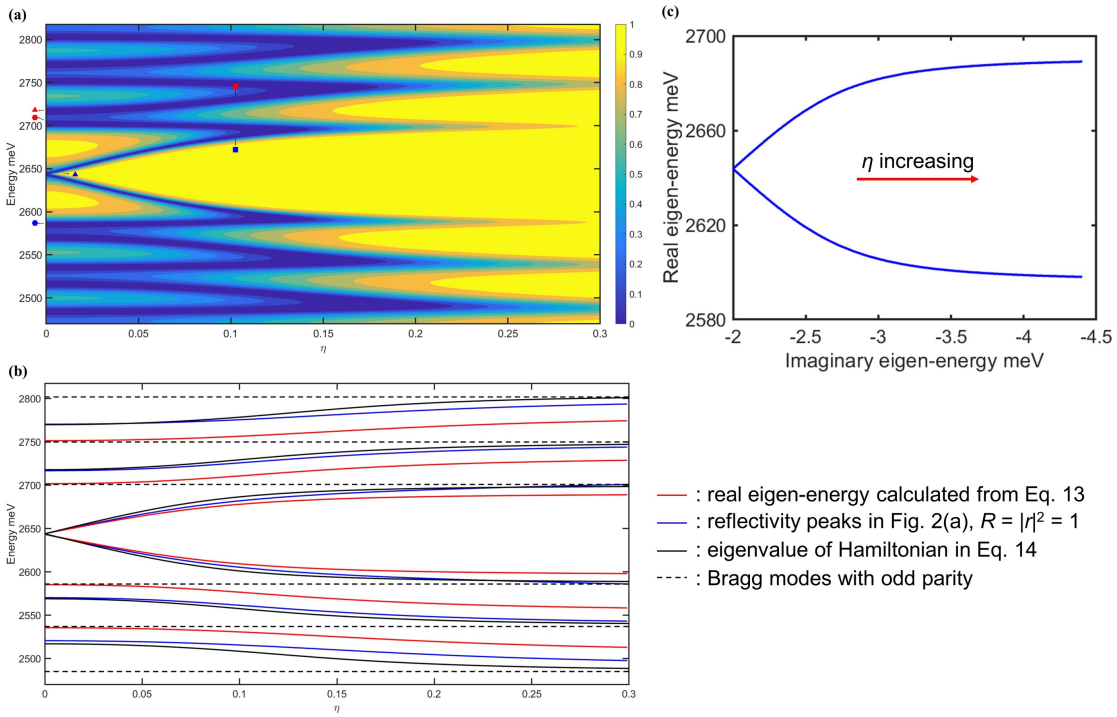


**Figure 2.** (a) Color plot of the reflectivity spectrum obtained using the transfer matrix method for a model symmetric microcavity structure with a QW embedded in its center as a function of the normalised coupling $\eta$. Hexagonal, triangle, and square symbols correspond to different electric field intensity curves in Fig. 3. (b) Photonic modes from reflectivity peaks (blue), eigenmode analysis (red), and Hamiltonian theory (black). Solid curves represent even Bragg modes, while dashed lines are modes with odd parity. (c) Eigenmode plot. The blue curve shows values taken by the complex eigen-energy of polariton modes as $\eta$ increases. The increase of the imaginary part of the eigen-energy indicates the increase of radiative decay rate of polaritons due to their strong coupling with Bragg modes.

### *2.2. The transfer matrix model*

In order to calculate the reflectivity of the full structures we apply the well-known transfer matrix method [18, 32] to study the reflectivity spectra and the complex frequencies of optical eigenmodes of the structure as functions of the vacuum Rabi frequency $\Omega_R$. The transfer matrices of layers characterised by a frequency-independent dielectric function have a generic form

$$\mathrm{T_j} = \begin{bmatrix} \cos(\omega n_j L_j/c) & i\sin(\omega n_j L_j/c)/n_j \\ i\sin(\omega n_j L_j/c) n_j & \cos(\omega n_j L_j/c) \end{bmatrix}, \tag{7}$$

with $j = \{a, b, c\}$ corresponding to the layers of Bragg mirrors and the cavity layer, respectively. For the bulk case we consider that the excitonic material completeley fills the cavity ($L_c = L_x$) and we use as refractive index $\sqrt{\epsilon_B(\omega)}$, where the dispersive dielectric function has been defined in Eq. 6.

For the QW case we use instead the transfer matrix (denoted as $\mathrm{T_{QW}}$) written in

terms of its frequency-dependent reflection and transmission coefficients. In order to derive it, we suppose first that light is incident on a symmetric QW from the left side (right side), and the amplitude of electric field of the incident light is 1. Using Maxwell boundary condition for both sides of the QW embedded in a microcavity, [18] one will have

$$\begin{aligned} \mathrm{T_{QW}}\begin{pmatrix} 1+r_{QW} \\ n_c(1-r_{QW}) \end{pmatrix} &= \begin{pmatrix} t_{QW} \\ n_c t_{QW} \end{pmatrix}, \text{for light from left side,} \\ \mathrm{T_{QW}}\begin{pmatrix} t_{QW} \\ -n_c t_{QW} \end{pmatrix} &= \begin{pmatrix} 1+r_{QW} \\ -n_c(1-r_{QW}) \end{pmatrix}, \text{for light from the right side,} \end{aligned} \tag{8}$$

where $n_c$ is the refractive index while $r_{QW}$ and $t_{QW}$ are reflection and transmission coefficients of the background microcavity. Four equations in Eq. 8 describe the propagation of light incident from the left side and right side on a QW. Solving these equations one can obtain four elements of the transfer matrix as follows:

$$\mathrm{T_{QW}} = \tfrac{1}{2t_{QW}} \cdot \begin{bmatrix} t_{QW}^2 - r_{QW}^2 + 1 & \frac{t_{QW}^2-(r_{QW}+1)^2}{n_c} \\ n_c(t_{QW}^2 - (r_{QW}-1)^2) & t_{QW}^2 - r_{QW}^2 + 1 \end{bmatrix}. \tag{9}$$

For a quantum well, $t_{QW} = 1 + r_{QW}$ and Eq. 9 can be reduced to

$$\mathrm{T_{QW}} = \begin{bmatrix} 1 & 0 \\ 2n_c r_{QW}/t_{QW} & 1 \end{bmatrix}. \tag{10}$$

We denote the transfer matrix of the entire structure as T and its reflection coefficient as $r$. Expressing $r$ through the elements of T, we obtain

$$r = \frac{n_r t_{11} + n_l n_r t_{12} - t_{21} - n_l t_{22}}{-n_r t_{11} + n_l n_r t_{12} + t_{21} - n_l t_{22}}, \tag{11}$$

where $n_r$ and $n_l$ are the refractive indices of right and left medium. In our case therefore $n_r = n_l = n_{ext} = 1.0$. The reflectivity $R$ can be now found as $R = |r|^2$. We shall focus on the optical eigenmodes of the structure that govern its optical response. One can find them imposing the boundary conditions of no light incident from right and left sides on the structure. In this case, one can represent the electric field of the light wave on the left side of the structure as $E_l = e^{-ikz}$, and the magnetic field as $B_l = -\frac{i}{ck_0}\partial_z E_l = -\frac{k}{ck_0}e^{-ikz}$, where $k$ is the wave vector of electromagnetic wave in the medium and $k_0$ is wave vector in vacuum. Since in our case the medium of environment is vacuum, $k = k_0$, therefore $cB_l = -e^{-ikz}$. Further we chose the origin of the coordinate system such as $e^{-ikz} = 1$, that yields $E_l = 1$ and $cB_l = -1$. Similarly, the electromagnetic wave on the right side of the structure may be written in form $E_r = Ae^{ikz}$ and $cB_r = Ae^{ikz}$, where $A$ is a complex coefficient. Absorbing complex $e^{ikz}$ in the coefficient $A$, electromagnetic wave on the right side can be written as $E_r = A$ and $cB_r = A$ At the normal incidence, the solutions to the left- and right-hand sides of the structure are linked by the transfer matrix of the entire structure:

$$\mathrm{T}\begin{pmatrix} E_l \\ cB_l \end{pmatrix} = \begin{pmatrix} E_r \\ cB_r \end{pmatrix} \Longrightarrow \mathrm{T}\begin{pmatrix} 1 \\ -1 \end{pmatrix} = A\begin{pmatrix} 1 \\ 1 \end{pmatrix}. \tag{12}$$

Eliminating $A$, we derive the equation for complex eigenfrequencies

$$t_{11} - t_{12} - t_{21} + t_{22} = 0. \tag{13}$$

*2.3. The second quantization model*

Polaritons are best understood as hybrid quasiparticles, linear superposition of photonic and matter excitations. As such, Hamiltonian descriptions in terms of coupled discrete light and matter modes are a powerful tool to study their physics and phenomenology. Due to the interference-based reflectors considered in this work, and to the broad and extended nature of the Bragg modes outside of the stopband, an ab-initio modal description would be nevertheless ill-suited.

In order to still develop an understanding of the transfer-matrix results for the QW case in terms of coupled oscillators, we model the system with a phenomenological Hamiltonian

$$H = \hbar\omega_0 b^\dagger b + \sum_n \hbar\omega_n a_n^\dagger a_n + \hbar\Omega_R \sum_n f_n (a_n^\dagger + a_n)(b^\dagger + b), \tag{14}$$

describing a discrete matter resonance coupled to multiple discrete photonic modes. In Eq. 14, $a_n$ and $b$ are annihilation operators respectively for the n$^{th}$ photonic mode and an exciton, obeying the bosonic commutation relations

$$\left[a_n, a_m^\dagger\right] = \delta_{nm}, \quad \left[b, b^\dagger\right] = 1. \tag{15}$$

The overlap parameters $f_n$ and the bare photonic frequencies $\omega_n$ can be used as fitting parameters. Such an Hamiltonian can be diagonalised by introducing the polaritonic annihilation operator

$$p = xb + zb^\dagger + \sum_n \left(y_n a_n + w_n a_n^\dagger\right), \tag{16}$$

where $x$, $z$, $y_n$ and $w_n$ are the complex Hopfield [33] coefficients obtained solving the eigenvalue equation

$$\omega p = \frac{1}{\hbar}\left[p, H\right]. \tag{17}$$

## 3. Numerical results and analysis

In the following, we investigate the reflectivity of symmetric model microcavity structures containing a QW or a bulk excitonic material. We vary the normalised coupling parameter $\eta = \Omega_R/\omega_0$ to study how the system resonances shift and interact. In the simulations we used step sizes of $10^{-2}$meV for energies and $10^{-4}$ for the normalised coupling $\eta$. The spatial resolution of structure geometry is 0.01nm.

In an inorganic microcavity, tuning of the exciton oscillator strength may be achieved with use of external electric or magnetic fields, while in an organic cavity it can be done either by changing the molecular density [26] or by optically modifying the dipolar strength of the optically active transition [27]. For the sake of comparison,

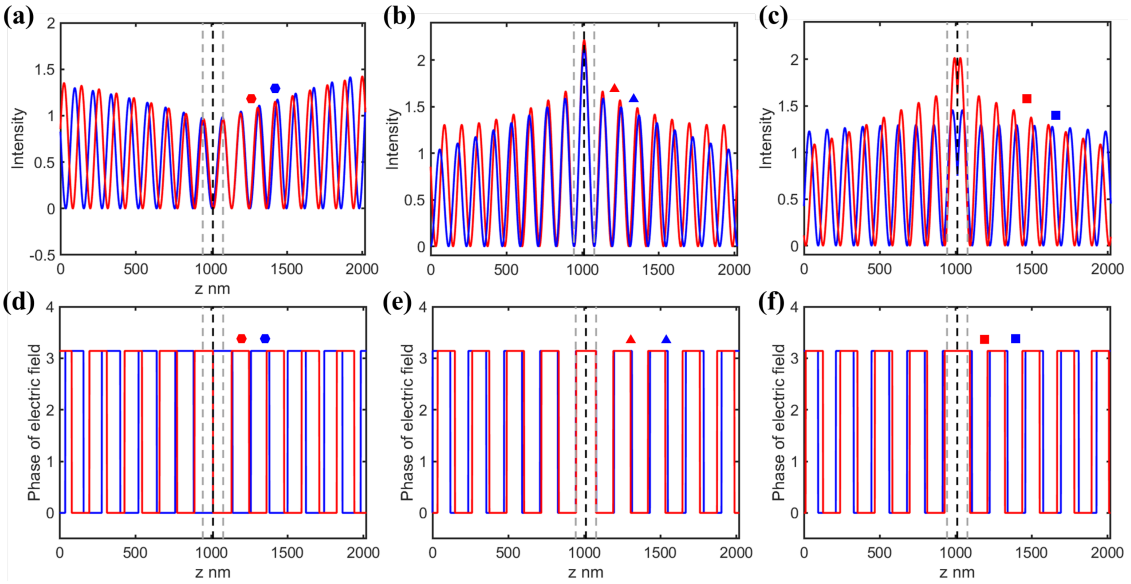


**Figure 3.** The electric field intensity profiles of the optical eigenmodes from Fig. 2(a), the black dashed line indicates the QW location, and the grey dahsed lines indicate the interface of microcavity and Bragg mirrors. (a) The intensity of electric field ($I = |E|^2$, $I$ is the intensity, $E$ is the electric field) in the odd eigenmodes; (b) and (c) electric field distributions for even modes at $\eta = 0$, $\eta = 0.1$. (d), (e) and (f): phase of electric field corresponding to (a), (b) and (c) respectively.

**Table 1.** Comparison of several organic microcavities

| Material | Exciton energy eV | Oscillator strength cm$^{-2}$ | $\eta$ | $\epsilon$ |
|---|---|---|---|---|
| BODIPY [34] | 2.66 | $1\times10^{15}$ | 0.05 | 1.75 |
| 4TBPPZn [23] | 2.88 | $2\times10^{15}$ | 0.03 | 1.75 |
| NTCDA [35] | 2.70 | - | 0.06 | 1.6 |
| Cyanine/PVA [36] | 1.84 | $9\times10^{14}$ | 0.08 | 2.15 |
| U3 [37] | 1.57 | - | 0.02 | - |

in both types of model structures we assume identical dielectric Bragg mirrors composed by eight periods, each consisting of the pair of dielectric layers aluminum nitride (AlN, layer a) and silicon nitride (SiN, layer b), with refractive indices $n_a = 2.02$ and $n_b = 1.96$ respectively.

In order to allow for an easy comparison between the results obtained in the QW and bulk cases, we used the same cavity parameters, with length $L_c = 134.0$nm and $n_c = 1.75$. The lowest resonance of the $\lambda/2$ cavity is thus resonant with the optically active transition $\hbar\omega_0 = 2664.0$meV. Note that in this configuration $\omega_x = 2\omega_0$. Detailed parameters for several organic microcavity candidates are listed in Table I.

*3.1. Thin optical layer*

The reflectivity spectrum of the symmetric microcavity structure with a QW embedded in its center is shown in Fig. 2(a). The QW intrinsic dissipation has been neglected ($\gamma = 0$) because of the long intrinsic exciton lifetimes in QWs and of the fact the radiative damping term (the $i\pi\Omega_R^2$ in the denominator of Eq. 4) is dominant in the regime of interest for us. Multiple interesting features are worth highlighting. Already in the stopband (from 2.59 to 2.70 eV), the two polaritonic resonances, whose splitting is usually proportional to the square root of $\eta$, strongly deviates from such a behaviour. This deviation can be documented already for relatively small values of the normalised coupling, saturating to the upper and lower edges of the main DBR stopband. Note the effective increase of the stop-band reflectivity and widening of the high reflectivity region with increase of the exciton-photon coupling strength that is apparent in Fig. 2(a). These effects are characteristic of the considered regime of interplay between the polariton Rabi-splitting and the Bragg stop-band width and linked with the optical metallization of dielectrics at large coupling strengths studied in Ref.[28]. In panel 2(c) we plot the real and imaginary part of the two polaritonic resonances in the stopband, varying the normalised coupling $\eta$. From such an image we can see that as the real polariton frequencies saturate, they also acquire an imaginary part, hybridising with the broad Bragg modes, which become a loss channel for the polariton energy.

Looking beyond the stopband in Fig. 2(a) we can see the emergence of a modal structure in which some modes are decoupled, and thus not influenced by the light-matter coupling $\eta$, while others do continuously and monotonously shifts from one decoupled photonic mode for $\eta = 0$ to the neighboring one for large $\eta$. This behaviour of the shifting modes was already observed in the case of a 2D optically active layer coupled to multiple photonic modes. This phenomenon was explained as a consequence of the metallization of the optical response of the QW for large enough values of the coupling [28], but it can be also interpreted as a general consequence of the eigenmode structure of the linear light-matter coupling Hamiltonian [38].

This result strongly suggests the shifting resonances can be correctly identified as Bragg polaritons, resulting from the coupling of the QW exciton with the Bragg modes of the DBR. One unexplained feature remains in this picture, that is the presence of flat resonances, independent of $\eta$, within each the $\eta = 0$ Bragg modes. We interpret these uncoupled resonances as a peculiar feature of the photonic continuum, which can be more correctly described as an ensemble of narrow continuum bands [39]. Within each of these bands there are even and odd modes, the former coupled to the quantum well, the latter decoupled, as their electric field vanishes at the location of the QW in our symmetric structure. The modal structure is shown in Fig. 2(b), where we plot the peaks extracted from Fig. 2(a) (blue), and compare them with the ones obtained by the eigenmode analysis (red) and with a quasi-mode quantum theory fitted to the extracted peaks (black). We can see that the three models give qualitatively similar results, with even modes (solid) shifting and odd ones (dashed) uncoupled. The good agreement

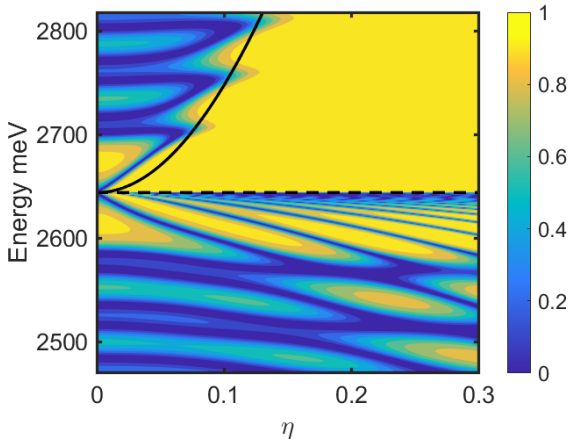


**Figure 4.** Color plot of the reflectivity spectrum obtained using the transfer matrix method for a model symmetric microcavity structure filled with a bulk optical material hosting excitons as a function of the normalised coupling $\eta$. The dashed black line represents the transverse frequency $\omega_T$ and the solid black line the longitudinal one $\omega_L$. In the area between these two lines the excitonic material is highly reflective and microcavity effects vanish.

of such a simple model with the full transfer matrix calculation further supports our interpretation of each Bragg mode as a pair of broadened Fabri-Perrot modes having opposite parities. Note that the results obtained with the three approaches are not identical, and their difference increases moving further away from the stopband. This is expected because, as originally shown by Savona *et al.* in Ref. [40], the results of a modal calculation and the reflectivity peaks do not coincide, and their difference increases with losses.

In order to validate our intuition on the origin of the coupled and uncoupled modes, in Fig. 3 we plot the photonic wavefunctions of the polaritonic resonances marked by respectively red and blue dots in Fig. 2(a). We can see how, consistently with our interpretation, the coupled Bragg modes are even while the decoupled ones are odd.

Note that Bragg polaritons have peculiar spatial extensions. In contrast to the cavity modes they penetrate far into the Bragg mirrors and couple to both surfaces of the structure. This greatly facilitates their coupling with external light modes, optical excitation and read-out. Moreover, hybrid Bragg modes in the strong coupling regime may be used to link vertically separated cavities in multiple-cavity structures that are currently discussed for applications as hyperbolic meta-materials [41] and double-qubit logic gates [42].

### *3.2. Bulk material*

The reflectivity spectrum of a bulk organic microcavity system is presented in Fig. 4. The parameters of the model cavity have been chosen matching to those of the organic material 4,4-difluoro-4-bora-3a,4a-diaza-s-indacene (BODIPY) [34]. The linewidth of

the excitonic material is taken $\gamma = 5$meV [8]. Frenkel excitons in such material can be considered as infinitely heavy, thus providing a good model system. As the excitonic material is extended over half-wavelength of flight, parity selection rules are relaxed in bulk microcavities, so that excitons can couple with both even and odd optical modes in this case [43]. This spoils the parity-filtering effect seen in the QW case, where only even photon modes are able to couple with a quantum well exciton [44], and it leads to the appearance of a fan of higher-order polariton modes for $\omega < \omega_0$.

The absence of higher order modes for $\omega > \omega_0$, as well as the overall strong spectral asymmetry of Fig. 4, can be understood by noticing that the dielectric function in Eq. 6 is negative between the transverse ($T$) and longitudinal ($L$) frequencies

$$\begin{aligned} \omega_T &= \omega_0, \\ \omega_L &= \sqrt{\omega_0^2 + \Omega_R^2 \frac{\omega_x}{\omega_0}}. \end{aligned} \tag{18}$$

These frequencies are plotted in Fig. 4 with dashed and solid black lines, respectively. In such a frequency region, referred to as Reststrahlen band when the oscillator is an optical phonon, the excitonic material is strongly reflective. All cavity-induced effects thus disappear, because light can not reach the second mirror.

These results demonstrate the existence of extended Bragg polaritons outside of the Reststrahlen band also in bulk materials. They also highlight a continuum transition between the strong coupling physics of organic molecules in a Bragg microcavity, and the optics of a single Bragg mirror over a highly conductive surface. The effective optical metallization of the organic semiconductor shown by our simulation, with the appearance of a broad Reststrahlen band in which the electromagnetic field cannot propagate, can be seen as the bulk equivalent of the decoupling effect predicted [28] and observed [45] in ultra-strongly coupled quantum wells.

## 4. Conclusions

We have examined theoretically a peculiar regime of light-matter coupling in a microcavity where the standard two-coupled oscillator model fails to capture the behaviour of polariton and photon modes. This regime is achieved if the Rabi-splitting of polariton modes becomes comparable to the width of the stop-band of Bragg mirrors surrounding the cavity and offers an interesting and highly original phenomenology including the deviation of the Rabi-splitting from the predictions of a two-coupled oscillator model, the strong coupling of cavity polariton modes with Bragg modes of the corresponding parities, and the pronounced parity filtering effect of Bragg modes. The considered regime could become important for organic polariton lasers [46]. Our analysis has shown that this regime manifest itself as a continuous transition of the cavity polariton lasing mode into a Bragg polariton. Such a device would be characterised by a different mode volume and quality factor and, presumably, different threshold power and eventual topological properties. Our results thus broaden the parameter region of interest for recently developed organic polariton lasers. Further studies will investigate

the specific lasing properties of the Bragg polaritons we described in this manuscript, and will investigate their technological usefulness. Furthermore, the considered light-matter coupling regime can be important for cavity-based frequency filters. We show that a cavity mode can be entirely removed from the stop band, which would enable one to switch on and off selective spectral filtering by acting upon excitons in microcavities with external electric fields. This effect could also find its applications in liquid crystal microcavities [47]. We expect that some of these phenomena may be observed in the reflectivity spectra of specially designed microcavities where the light-matter coupling strength may be tuned, e.g., with use of the photochemically induced conformational changes in organic molecules [27] or pumping an electron gas in the excitonic material [48]. These results open the new path for band engineering in photonic structures. They have a significant fundamental interest as they shed light on the light-matter coupling beyond the two-coupled oscillator model.

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