

Ship speed prediction based on machine learning for efficient shipping operation

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Abstract

Optimizing ship operational performance has generated considerable research interest recently to reduce fuel consumption and its associated cost and emissions. One of the key factors to optimize ship design and operation is an accurate prediction of ship speed due to its significant influence on the ship operational efficiency. Traditional methods of ship speed estimation include theoretical calculations, numerical modeling, simulation, or experimental work which can be expensive, time-consuming, have limitations and uncertainties, or it can't be applied to ships under different operational conditions. Therefore, in this study, a data-driven machine learning approach is investigated for ship speed prediction through regression utilizing a high-quality publicly-accessible ship operational dataset of the 'M/S Smyril' ferry. Employed regression algorithms include linear regression, regression trees with different sizes, regression trees ensembles, Gaussian process regression, and support vector machines using different covariance functions implemented in MATLAB and compared in terms of speed prediction accuracy. A comprehensive data preprocessing pipeline of operational features selection, extraction, engineering and scaling is also proposed. Moreover, cross validation, sensitivity analyses, correlation analyses, and numerical simulations are performed. It has been demonstrated that the proposed approach can provide accurate prediction of ship speed under real operational conditions and help in optimizing ship operational parameters.

Keywords: Ship speed prediction, Ship energy efficiency, Machine learning, Regression, MATLAB

1. Introduction

With more than 80% of the world trade handled by shipping, more stringent regulations are introduced by the International Maritime Organization (IMO) to improve ships operational efficiency and reduce its greenhouse gas (GHG) emissions. However, in spite of implementing stricter regulations, the total GHG emissions from ships as well as the shipping share percentage to the global emissions have increased by 9.6% and 4.7% respectively between 2012 and 2018 according to the latest IMO GHG study (Faber et al., 2020). Therefore, in order to control and reduce these emissions, IMO has adopted mandatory operational and technical measures which include the Energy Efficiency Design Index (EEDI) for new ship design and the Ship Energy Efficiency Management Plan (SEEMP) for all ships. The EEDI targets a minimum CO₂ emissions per cargo carried for newly built ships through implementing design-based solutions. Meanwhile, the SEEMP seeks to improve the operational energy efficiency of ships using operational strategies and practices of ship management (Rehmatulla et al., 2017; Bazari and Longva, 2011).

Among the various EEDI and SEEMP measures available, the speed based measures are increasing in popularity for improving ships energy efficiency and reducing GHG emissions (Capezza et al., 2019). This is mainly due to the fact that, a small speed adjustment can result in a significant improvement to the ship fuel

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39 consumption and energy efficiency (Smith et al., 2011). Moreover, applying speed based EEDI and SEEMP
40 measures such as speed optimization, voyage execution, or speed reduction for new and existing ships does
41 not require an upfront capital or investment costs and payback periods. However, it should be noted that
42 altering ship speed can impact the voyage duration and associated costs which affects the ship productivity
43 and total income (Capezza et al., 2019; Smith et al., 2011). Therefore, predicting ship speed in design stage
44 and during operation is an essential element in evaluating the efficiency of EEDI and SEEMP measures.

45 Ship speed prediction is of significant importance in the decision making processes and has many
46 implementations in the maritime industry. For example, for more accurate fuel consumption and emissions
47 calculations, ship speed is the most principal operational parameter to be determined Bialystocki and
48 Konovessis (2016). In addition, it has been shown that ship operating speed is a trend key driver of
49 emissions and its growth rate (Faber et al., 2020). Moreover, in ship routing and voyage planning problems,
50 an accurate ship speed prediction is essential to estimate the ship expected time of arrival (ETA) and satisfy
51 the calling ports time windows constrains (Zis et al., 2020). Also, ship speed is a key factor in developing
52 and operating ship trajectory planning and collision avoidance strategies for safer navigation especially in
53 narrow channels or heavy traffic areas (Cockcroft and Lameijer, 2003).

54 The overall concept of the ship energy system can be explained as the fuel energy is converted into
55 useful thrust by the propeller through the propulsive machinery to overcome the ship total resistance at
56 a specific ship speed. Therefore, ship speed prediction and calculation depend on the characteristics of
57 the ship hull, propulsion machinery, propeller, and the surrounding environment (Molland et al., 2011;
58 Journée, 1976). This issue can be approached in different ways; experimentally using ship model tests or full
59 scale ship speed trails (ITTC, 2014a,b), numerically by modeling the flow field around the ship hull using
60 various computational fluid dynamic (CFD) techniques (Choi et al., 2009), from in-service propeller shaft
61 measurements (Dalheim and Steen, 2021), or statistically using for example regression based methods to
62 learn and estimate the relations between ship speed/power and other hull, operational, and environmental
63 parameters. Measurements of these parameters can be obtained from model and full scale tests as in Holtrop
64 work (Holtrop, 1984) or recorded during normal ship operation over a period of time using measuring
65 instruments (Mao et al., 2016).

66 The recent advancement in sensor technologies, data acquisitions and storage systems enables the
67 monitoring of ship operational performance to be more efficient and reliable owing to the higher data
68 quality and integrity (Shenoi et al., 2015). The proper processing and analysis of this data can provide a
69 deeper insight into the ship operational performance, extract valuable information from it, and uncover the
70 correlation and patterns between the measured data. For these purposes, machine learning and statistical
71 approaches have gained substantial momentum in shipping industry in the recent decades (Petersen et al.,
72 2012a; Soner et al., 2019). This is because statistical and data-driven models can deal with high-dimensional
73 and non-linear data such as the ship operational data without a priori knowledge of the ship underlying basic
74 physics (Coraddu et al., 2017, 2015). Also, due to their nature, statistical and machine learning approaches
75 have more prediction robustness and easier information extraction from sensor data compared to theoretical
76 and parametric approaches (Coraddu et al., 2015; Soner et al., 2019).

77 The literature review in the area of ship operational performance monitoring through data analysis is
78 dominated by modeling, predicting, and optimizing of the ship fuel consumption for economic as well as
79 environmental reasons (Soner et al., 2018; Gkerekos et al., 2019; Uyanık et al., 2020; Parkes et al., 2018);
80 however, there have been a few studies that investigated ship speed prediction based on available ship
81 operational data. For monitoring and analyzing the operational performance of a ferry in terms of ship speed
82 and fuel consumption, Gaussian Processes (GP) and neural network models were compared in (Petersen
83 et al., 2012a). Based on the same dataset, the Ridge and LASSO regression models were also compared in
84 (Soner et al., 2019). Moreover, tree based regression models were proposed in (Soner et al., 2018) for the
85 same ship showing a comparable performance with the aforementioned models. Meanwhile, the operational
86 performance of a containership was modeled in terms of ship speed and and engine power using GP model in
87 (Yoo and Kim, 2019). In another study for speed prediction of a container ship, a preliminary investigation of
88 the linear regression, autoregressive and the mixed effects models was conducted in (Mao et al., 2016) using
89 a limited amount of operational data. Linear regression was also compared to the generalized additive and
90 projection pursuit regression models for speed prediction in (Brandsæter and Vanem, 2018). Furthermore,

91 speed prediction through regression was proposed for weather routing optimization study in (Krata and
 92 Szlapczynska, 2018), for modeling ship maneuverability in (Wang et al., 2015), and for navigation safety
 93 and collision avoidance of ice class ships in (Similä and Lensu, 2018).

94 From the above, it can be seen that ship speed prediction is of great concern for different purposes with
 95 different approaches being considered. Although ship speed can be predicted mathematically during design
 96 stage or be measured directly during operation using satellite based technologies such as global positioning
 97 or automatic identification systems, the purpose of this work is to predict ship speed based on measured
 98 real ship operational data as inputs to a machine learning model. This can be extended to provide deeper
 99 insights into the relation between ship speed and other ship operational parameters which is essential for
 100 operational optimization and decision support purposes. As a result, helping decisions makers and shipping
 101 companies to move towards more efficient operation environmentally and economically.

102 Much of the current literature utilizes different ship types and datasets, with different data acquisition
 103 systems, processing techniques, and data scaling methods. Therefore, due to this inconsistency, it is
 104 inconclusive which model is more accurate in terms of ship speed prediction. To remedy this gap, the
 105 aim of this work is to train and validate various conventional regression models to examine and compare
 106 their prediction accuracy of ship speed using a high quality ship operational dataset. The studied machine
 107 learning regression models include Multiple Linear Regression (MLR), Regression trees with different sizes,
 108 Ensembles of trees using both bagging and boosting techniques, Gaussian Process Regression (GPR), and
 109 Support Vector Machine (SVM) models using different covariance functions and kernels. These algorithms
 110 are the most commonly used and they are chosen for their robustness, efficiency, power, and accuracy. Also,
 111 sensitivity analysis of different data preprocessing methods (Data scaling) as well as different number of
 112 data splits for cross validation are performed to assess its effect on the statistical performance of different
 113 regression models. Furthermore, a correlation analysis and computational experiments are conducted to
 114 study and examine the relation between ship speed and other ship operational parameters.

115 The paper is organized as follow; Section 2 introduces the examined ship and dataset preprocessing.
 116 Section 3 describes the used methodology, the studied regression models, and their validation and evaluation.
 117 Meanwhile, Section 4 shows the results and discussion. Finally, Section 5 presents the work conclusions,
 118 recommendation, and future work.

119 2. Ship & data description

120 This work utilizes the existing publicly available sensor data from the domestic ferry the '*M/S Smyril*'
 121 operating around the Faroe Islands. The ferry's specification is provided in Table 1. An automated on-board
 122 data acquisition system recorded for the ferry's two or three trips per day over a period of nearly two months
 123 from February 16th to April 21th 2010 completing, approximately 250 trips (Propulsion modelling, 2021;
 124 Petersen et al., 2012b). To improve the quality and representation of the collected dataset, the following
 125 data preprocessing has been undertaken as part of this study.

Table 1: Specifications of the M/S Smyril ferry

Parameter	Value
Length	123 <i>m</i>
Breadth	22.7 <i>m</i>
Draft	5.6 <i>m</i>
Passenger capacity	975
Car capacity	970 <i>m</i> / 200 cars
Service speed	21 <i>kn</i>
Main engines	4 * MAN B&W 7L32/40

126 *2.1. Data preprocessing*

127 *2.1.1. Feature selection & extraction*

128 One of the most commonly used data preprocessing technique is feature selection which is used to
129 identify the important variables within the dataset and remove the unnecessary features. This, consequently,
130 results in reducing the data dimensionality and the modeling computational cost, and improving the model
131 performance. Therefore, a correlation analysis is performed to show the interrelation between the ship speed
132 as the independent variable and other operational variables as presented in Table 2. Linear correlation is
133 usually used to express the relationship between variables as in (Uyamk et al., 2020; Gkerekos et al., 2019;
134 Brandsæter and Vanem, 2018). However, a nonlinear relationship may exist and not be captured. Therefore,
135 distance correlation is also deployed to test the nonlinear correlation between various variables. The linear
136 coefficient value ranges between 1 and -1, while distance correlation coefficient ranges from 0 to 1. For both
137 coefficients, a value of 0 indicates no correlation between variables and a value close to 1 implies a strong
138 relationship. Meanwhile, the linear correlation sign indicates the direction of the correlation trend.

Table 2: Correlation of ship speed to other operational variables

Variables	Linear correlation	Distance correlation
Port propeller pitch	0.9067	0.8832
Starboard propeller pitch	0.8862	0.8632
Port rudder angle	0.6689	0.7212
Headwind	0.1370	0.1904
Crosswind	-0.0003	0.0921
Starboard rudder angle	-0.2020	0.6099
Trim angle	-0.2392	0.3108
Draft	-0.4609	0.4011

139 According to Table 2, the port and starboard propeller pitch as well as the port and starboard rudder
140 angle have significant effect on the ship operational speed. This is due to the fact that varying the propeller
141 pitch varies the provided propeller thrust and ship speed while the altering the rudder angle affects the ship
142 resistance and, accordingly, the ship speed. As can be noticed in Table 2, the dependence power between
143 the ship speed and starboard rudder angle is detected by the distance correlation more than the linear
144 correlation due to its nonlinearity nature. Moreover, the ship trim angle and draft have a high impact on
145 the ship speed since it can affect the ship resistance and consequently the ship operational performance.
146 Therefore, a trim optimization at different draft conditions can be conducted to further improve the ship
147 operational efficiency. Likewise, for reducing the load on the engine bearings and shafting system, the impact
148 of optimizing the propeller controllable pitch on the ship speed can be examined for decision support. On
149 the contrary, headwind and crosswind variables show insignificant correlation, which is mostly due to the
150 fact that the utilized dataset covers about two months of operation alternating within a narrow range.

151 Measurements of the selected operational variables, which are used to train the ship speed prediction
152 models, were carried out as follows: the ship speed measured using a Doppler speed log, trim angle measured
153 using an inclinometer, port and starboard water level measurements measured using two radars placed on the
154 ship sides, port and starboard propeller pitch, port and starboard rudder angle, wind angle and direction
155 as presented in Table 3. These variables have the most significant effect on ship speed and operational
156 performance (Soner et al., 2018; Yoo and Kim, 2019).

157 The selected parameters were firstly extracted from the raw data and arranged into separate voyages.
158 Then, due to the different sampling frequencies of the measurements as shown in Table 3, the extracted
159 data was resampled at an average frequency of 1 Hz and averaged over 10 minutes windows or intervals
160 as suggested in (Pedersen and Larsen, 2009; Leifsson et al., 2008). The resulted total data size is 2654
161 observations of each feature for the given dataset.

Table 3: Selected parameters and measurement frequency (Propulsion modelling, 2021)

Feature	Unit	Measurement frequency (Hz)
Ship speed	Kn	1
Trim angle	degree	3
Port water level measurement	m	3
Starboard water level measurement	m	3
Port propeller pitch	$Volt$	1
Starboard propeller pitch	$Volt$	1
Port rudder angle	$Volt$	1
Starboard rudder angle	$Volt$	1
Wind angle	degree	0.5
Wind speed	m/s	0.5

162 2.1.2. Feature engineering

163 In order to improve the performance of machine learning algorithms, new features can be engineered
164 from the raw data to better represent the ship operational data. For example, the port and starboard water
165 level measurements were transformed into draft amidships as a function of the radars heights, angles, and
166 distance from the midship. Also, the inclinometer readings were corrected to have the real ship trim angle.
167 Moreover, the wind speed V_{wind} and angle θ_{wind} measurements were transformed into two new features called
168 the headwind V_{hw} and crosswind V_{cw} to eliminate the circular discontinuity issue of the wind direction when
169 it passes between 0° and 360° using Equations 1.

$$\begin{aligned} V_{hw} &= V_{wind} \cdot \cos(\theta_{wind}) \\ V_{cw} &= V_{wind} \cdot \sin(\theta_{wind}) \end{aligned} \quad (1)$$

170 Figure 1 shows the processed data after features selection, extraction and engineering against ship speed.
171 As expected and reported in the literature, there are nonlinear relationships between ship speed and other
172 ship operational parameters. It can, however, be noted that ship speed is proportional to the propeller pitch.

173 As shown in Figure 1, the ship draft is spread between 5 and 6m while the trim angle corresponds to a
174 trim between -1.5 to 1.25m (Petersen et al., 2012a; Soner et al., 2019). Regarding the ship speed, its average
175 value varies mostly between 15 and 20Kn as shown in Figure 2. This is due to the fact that the ship slows
176 only at dock while loading and unloading. Also, the wind speed tends to increase with the ship speed as
177 shown in Figure 3 with an average headwind speed of 11m/s.

178 2.1.3. Feature scaling

179 Since different ship operational parameters have different ranges and units, features scaling is an important
180 preprocessing step. Hence, different features can be comparable to each other and contribute equally to the
181 machine learning objective functions. Standardization and normalization are two common scaling methods
182 and both are introduced into this study to test their impact on different regression models. Standardization
183 scales the features data to unit variance and removes its mean according to Equation 2. Meanwhile,
184 normalization scales the features data between 0 and 1 using min-max scaling as in Equation 3.

$$x_s = \frac{x - \mu}{\sigma} \quad (2)$$

$$x_m = \frac{x - x_{min}}{x_{max} - x_{min}} \quad (3)$$

185 where x_s and x_m are the dimensionless standardized and normalized values of the actual variable x respectively.
186 μ is the mean value of the variable x entire data, σ is its standard deviation, x_{min} and x_{max} are the minimum
187 and maximum values of the variable x respectively. The processed data is then used to train and validate
188 different predictions models as will be discussed in the following sections.

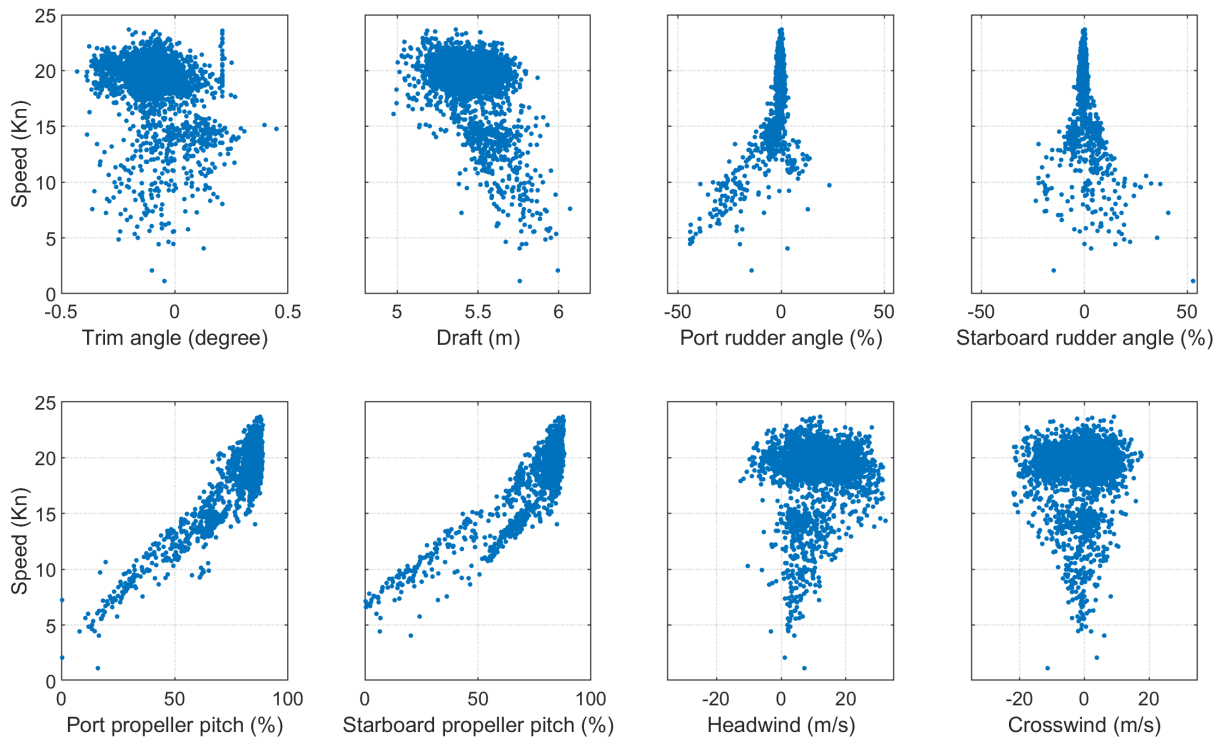


Figure 1: Scatter plots of ship speed versus processed ship operational parameter

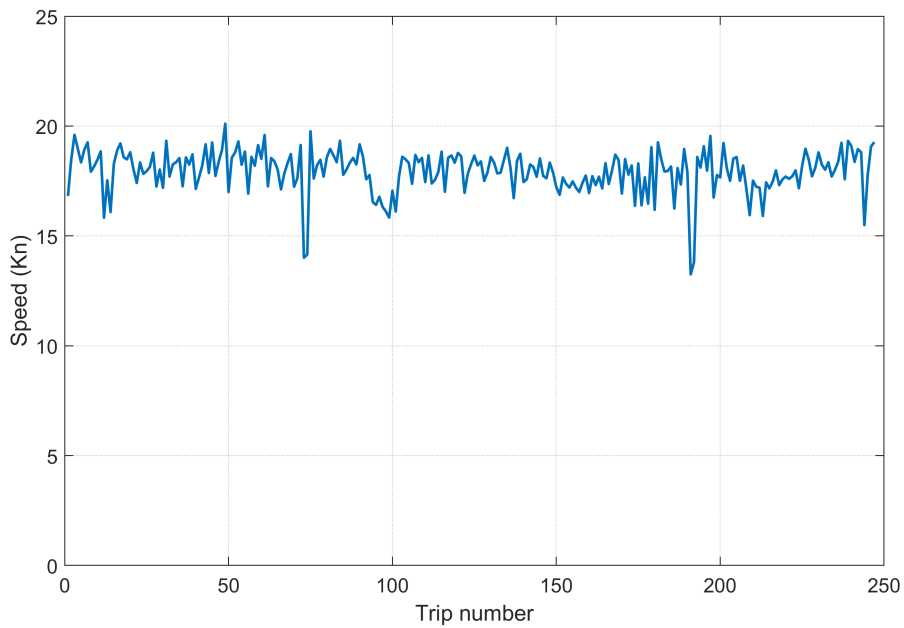


Figure 2: Average ship speed for each trip

189 **3. Prediction models**

190 In reality, ship speed is influenced by many factors including ship operational conditions (e.g. draft, trim)
 191 as well as environmental conditions which makes it difficult to be modeled using conventional approaches.

192 Therefore, machine learning regression techniques are applied in this research to predict ship speed as a
 193 function of measured ship operational parameters and surrounding environment conditions. These parameters
 194 are used to train regression models to construct a mapping function from input variables to infer the output
 195 ship speed variable, and then make prediction for new data. In the following sections, a diverse set of
 196 common regression models are described which vary in their level of complexity and accuracy. These models
 197 are then employed and compared for ship speed prediction.

198 3.1. Multiple linear regression (MLR) model

199 MLR is an extension of linear regression that assumes a linear relationship between the response variable
 200 (y_i) and the predictor variables (x_{i1} to x_{ip}) as shown in Equation 11.

$$y_i = \beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2} + \dots + \beta_p x_{ip} + \epsilon \quad (4)$$

201 where (β_0) is the constant term in the model, (β_1 to β_p) are the corresponding coefficients of the predictor
 202 variables (x_{ip}), and (ϵ) is the error term of the model. Due to its advantages of simplicity and ease of
 203 interpretation, MLR is one of the most popular parametric models and it is normally used as a reference to
 204 compare other models performance (Gkerekos et al., 2019).

205 3.2. Regression trees

206 Tree-based regression model is one of the advanced and accurate non-parametric statistical model which is
 207 suitable for non-linear parameters such as ship operational datasets (Soner et al., 2018). Building a regression
 208 tree for prediction involves two main steps; dividing the predictor variables into distinct non-overlapping
 209 regions (R_1 to R_j). Then, predictions are made from the mean response values of the training observations
 210 for every observation in different regions $R_{(1..j)}$ (James et al., 2013). Meanwhile, the main goal is to find
 211 the regions that minimizes the Residual Sum of Square (RSS) shown in Equation 5.

$$\text{RSS} = \sum_{j=1}^J \sum_{i \in R_j} (y_i - \hat{y}_{R_j})^2 \quad (5)$$

212 where \hat{y}_{R_j} is the training observations mean response within the j th region and $j = 1, 2, \dots, p$ and p
 213 represents the number of regions or leaves of the tree. The number of these regions or leaves defines the
 214 regression tree size and its level of accuracy, flexibility, and robustness. Whilst a fine regression tree can
 215 produce more accurate results, the overfitting risk increases. In contrast, a coarse regression tree has lower
 216 training accuracy but it is more robust with lower variance (James et al., 2013). Consequently, choosing
 217 the regression tree size is essential to have balance between the model complexity, speed, accuracy, and
 218 overfitting risk.

219 3.3. Ensembles of trees

220 Despite the advantages of regression tree models, they can suffer from high variance, bias and overfitting.
 221 Therefore, multiple regression trees can be combined to build an ensemble of trees to improve the predictive
 222 performance of the model (James et al., 2013). Two of the most popular ensemble techniques to aggregate
 223 many regression trees are bagging and boosting. Bagging or bootstrap aggregating uses multiple separate
 224 training sets from the original training dataset randomly with replacement to train different regression
 225 trees. The predictions of different trees ($\hat{f}^{*1}(x)$ to $\hat{f}^{*B}(x)$) are then calculated and averaged as follows
 226 which reduces the variance compared to a single regression tree (James et al., 2013).

$$\hat{f}_{bag}(x) = \frac{1}{B} \sum_{b=1}^B \hat{f}^{*b}(x) \quad (6)$$

227 where $\hat{f}_{bag}(x)$ is the average prediction of all the regression trees and B is the number of the separate
 228 training sets and trees. On the other hand, boosting technique grows the number of trees B sequentially
 229 where each tree utilizes a modified version of the whole dataset using information from the previously grown

230 tree (James et al., 2013). The learning process improves the prediction performance of each tree from $\hat{f}^1(x)$
 231 to $\hat{f}^B(x)$ by updating the observations' weights of the training dataset without bootstrap sampling and the
 232 boosted model output $\hat{f}_{boost}(x)$ is given as follows:

$$\hat{f}_{boost}(x) = \sum_{b=1}^B \lambda \hat{f}^b(x) \quad (7)$$

233 where λ is the shrinkage parameter which controls the rate of the boosting learning process. The shrinkage
 234 parameter and the B number of trees for both bagging and boosting methods are determined by cross-validation
 235 as explained later.

236 3.4. Gaussian process regression (GPR) models

237 Implementing a Gaussian process (GP) for regression purposes has been proposed considerably due to
 238 its power, efficiency, and accuracy. Also, GP-based regression models can describe the uncertainty and
 239 non-linearity between the dataset parameters through a nonparametric approach (Rasmussen and Williams,
 240 2006). Therefore, GPR models are proposed for ship operational data analysis and ship speed prediction
 241 (Yoo and Kim, 2019; Petersen et al., 2012a).

242 A GP is a collection of random variables where any finite collection of which are described by a joint
 243 Gaussian probability distribution. Whereas in GPR, the function of variables $f(x)$ is assumed to be
 244 distributed as a GP which is defined by its mean function $m(x)$ and covariance function $k(x, x')$ as follows.

$$f(x) \sim GP(m(x), k(x, x')) \quad (8)$$

245 One of the most popular covariance function and commonly used is the squared exponential (SE) or
 246 the radial basis function (RBF) (Rasmussen and Williams, 2006; Yuan and Nian, 2018). This covariance
 247 function $k_{SE}(r)$ or $k_{SE}(x, x')$ is very smooth due to its infinitely differentiable nature and it can be written
 248 as follows.

$$k_{SE}(r) = \exp\left(-\frac{r^2}{2l^2}\right) = \exp\left(-\frac{|x - x'|^2}{2l^2}\right) \quad (9)$$

249 where x and x' are the training and testing points pairs respectively and l defines the characteristic
 250 length-scale for the input values. It should, however, be noted that the assumed SE smoothness may not be
 251 realistic to model some physical systems. Therefore, the Matérn class of Gaussian process is recommended
 252 because it includes a parameter (ν) that can control the learned function smoothness (Rasmussen and
 253 Williams, 2006; Stein, 1999). One type of the Matérn class functions is the exponential covariance function
 254 obtained when $\nu = 1/2$ which is a continuous but not differentiable function as the SE function and it can
 255 be defined as follows:

$$k_{\nu=1/2}(r) = \exp\left(-\frac{r}{l}\right) \quad (10)$$

256 Both functions, the exponential and squared exponential, are common and widely used and they are
 257 implemented in this study to be compared in terms of their accuracy of ship speed prediction.

258 3.5. Support vector machine (SVM) models

259 Due to its robustness, accuracy, power, and generalization ability, SVM is one of the most attractive
 260 supervised learning model proposed for many fields which can be used for classification and regression
 261 (Uyanik et al., 2020; Awad and Khanna, 2015). In regression problems, SVMs are built as regressors which
 262 try to fit a hyperplane or a function that predicts a continuous target value within a tolerance margin or
 263 a decision boundary based on the training samples. The objectives of adjusting this margin is to minimize
 264 the prediction error and balance it with the model complexity and robustness.

265 SVM is also a kernel based technique which extends its functionality by using different kernel functions
 266 depending on the data type. Therefore, SVM can be a parametric model using a linear kernel or a

267 non-parametric model using an RBF kernel. Popular kernel functions include: linear kernel in Equation 11,
 268 polynomial kernel in Equation 12, and Gaussian kernel in Equation 14.

$$k(x, x') = x^T x' \quad (11)$$

$$k(x, x') = (1 + x^T x')^d \quad (12)$$

$$k(x, x') = \exp(-\gamma \|x - x'\|^2) \quad (13)$$

269 where d is the polynomial degree of kernel and γ is the Gaussian kernel scale hyperparameters which can be
 270 adjusted to enhance the SVM model performance. Therefore, different polynomial degrees and kernel scales
 271 are investigated in this study to find the optimal model configuration.

272 3.6. Prediction performance evaluation

273 In order to examine the predictive accuracy of the employed models and measure its effectiveness,
 274 prediction performance indices can be used. However, training the prediction models and testing its
 275 performance using the same dataset can give overoptimistic results (Arlot et al., 2010). Therefore, a
 276 validation scheme is implemented to split the dataset into a training dataset to train the prediction models,
 277 and a test dataset to validate its performance after training. Then, a number of performance measures can
 278 be used to compare all the models performance as explained in the following subsections.

279 3.6.1. Cross validation

280 Validation reduces the risk of overfitting and ensures the generalization capabilities of the trained
 281 prediction models and the robustness of its hyperparameters' values. However, partitioning the available
 282 data into training and test datasets reduces the available data for training as well as for validating the
 283 models. To address this issue, cross validation is applied in the form of K-folding which is widely used and
 284 preferred in the literature (Uyanık et al., 2020; Gkerekos et al., 2019).

285 In K-fold cross validation method, the dataset is split into k subsets or folds where $K-1$ subsets are
 286 combined and used to train the prediction models and the remaining subset is used for validation. This
 287 process is repeated for K times where each time, one of the K folds is used as a validation subset. Finally,
 288 the average validation error of all the K runs are obtained. By using this technique, most of the data is used
 289 for training as well as for validation which reduces the bias and variance and gives a good estimation of the
 290 predictive accuracy of the studied models. Nevertheless, different suitable values of K are reported in the
 291 literature including 4 in (Uyanık et al., 2020; Leifsson et al., 2008), 5 in (Yan et al., 2020; Hu et al., 2019),
 292 10 in (Soner et al., 2018, 2019), 20, 30, and 50 in (Brandsæter and Vanem, 2018; Coraddu et al., 2017).
 293 Therefore, a sensitivity analysis of different K values is made in this study.

294 3.6.2. Coefficient of determination R^2

295 The coefficient of determination R^2 explains the variation of the measured response variable y_i as a
 296 function of the response variable prediction made by the trained model \hat{y}_i and the average value of the
 297 response variable \bar{y}_i as follows

$$R^2 = 1 - \frac{\sum_{i=1}^n (y_i - \hat{y}_i)^2}{\sum_{i=1}^n (y_i - \bar{y}_i)^2} \quad (14)$$

298 where n is the number of samples. R^2 value varies normally from 0 to 1 where a higher value means a better
 299 fit of the trained model to the data.

300 *3.6.3. Mean squared error (MSE)*

301 This index measures the mean of the square of all errors between the predicted and the measured values
302 of the response variable as shown in the following equation.

$$\text{MSE} = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2 \quad (15)$$

303 By squaring the errors, MSE is always positive and it gives more weight to high errors. The lower the
304 MSE, the better the prediction model performance.

305 *3.6.4. Root mean square error (RMSE)*

306 RMSE is the most commonly used and easily interpreted statistic, as it has the same unit of the studied
307 variable that better reflects the prediction models performance. It is calculated by taking the square root
308 of the MSE as shown in the following equation.

$$\text{RMSE} = \sqrt{\frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2} \quad (16)$$

309 *3.6.5. Mean absolute error (MAE)*

310 This criterion is similar to the RMSE. However, it is more robust and less sensitive to data outliers
311 compared to the MSE. MAE corresponds to the average of all the absolute errors and can be calculated as
312 follows.

$$\text{MAE} = \frac{1}{n} \sum_{i=1}^n |y_i - \hat{y}_i| \quad (17)$$

313 *3.6.6. Methodology implementation & parameters*

314 The discussed prediction models as well as the examined ferry dataset are modeled mathematically and
315 implemented in MATLAB environment in order to compare the performance of these models in terms of
316 its accuracy of predicting the ship speed. First, the dataset collected from the ferry 'M/S Smyril' is loaded
317 into the MATLAB workspace, the selected parameters are extracted, resampled, averaged, and engineered
318 as explained in 2. Regarding the data scaling, a quantitative analysis is performed to study the sensitivity
319 of various prediction models to different scaling techniques. Therefore, the examined regression models are
320 trained with the raw, standardized, and normalized versions of the ferry dataset to show its impact on the
321 performance and results of different models. These datasets are then split into training and testing datasets
322 to validate the prediction models according to the K-fold cross validation method where K values of 5, 10, 30,
323 and 50 are used to study the effect of this parameter on the the performance of different models. Moreover,
324 to get more consistent results, models training is repeated 10 times as suggested in (Gkerekos et al., 2019)
325 and results are averaged. Finally, the performance metrics are computed to evaluate and compare different
326 models in terms of prediction accuracy of ship speed.

327 For the tree-based regression model, three different regression tree sizes are studied to investigate the
328 trade-off between the tree model accuracy and complexity. A minimum leaf size, that indicates the number
329 of variable observations in a tree leaf, of 4, 12, and 36 are used which corresponds to fine, medium, and
330 coarse regression trees respectively as suggested in (MATLAB, 2021). For the ensembles of trees model,
331 the two most popular techniques of aggregating regression trees, which are bagging and boosting, are
332 investigated with a shrinkage parameter or learning rate of 0.1 and a minimum leaf size of 8 as recommended
333 in (MATLAB, 2021). Regarding the SVM regression model hyperparameters, the polynomial kernel degree
334 d is set to 2 and 3 for the quadratic and the cubic SVM models respectively which are compared to the
335 linear SVM model. For the SVM Gaussian kernel scale, γ is set to $\sqrt{P}/4$, \sqrt{P} , and $4\sqrt{P}$ which correspond
336 to fine, medium, and coarse Gaussian SVM models respectively where P is the number of the trained model
337 predictors (MATLAB, 2021). The aforementioned models are integrated in the 'Regression Learner App' of

338 MATLAB’s Statistics and machine learning toolbox. In this study, MATLAB R2019b is used on a desktop
339 computer (Intel Core i7, 3.4 GHz, Memory 16 GB).

340 4. Results & analysis

341 As shown in Table 4, the GPR model with the the Matérn class or exponential kernel yields the best
342 results with an R^2 of 0.91 and RMSE of 0.91 kn utilizing the raw dataset. This indicates that controlling
343 the smoothness behavior of the stochastic processes realization as in the Matérn class can be beneficial for
344 modeling realistic physical systems. The GPR model with the squared exponential kernel and the bagged
345 trees ensemble model provide accurate results with an R^2 of 0.88. On the other hand, the SVM model
346 using a fine Gaussian kernel performs the lowest estimation with an R^2 of 0.51 due to its small-scale kernel
347 function. It follows that a rapid variations in the SVM response function which causes the model to overfit
348 and doesn’t perform accurately in the low ship speed region as illustrated in Figure 3. By increasing
349 the Gaussian kernel scale value γ , a less complicated SVM model can be obtained with better prediction
350 performance as demonstrated by the medium Gaussian SVM model. However, the prediction errors start
351 to increase again for large γ value which results in a rigid SVM response function with higher probability of
352 underfitting as shown in Table 4 and Figure 3 for the coarse Gaussian SVM model.

Table 4: Performance measures for different machine learning approaches using 5-fold cross validation

	Raw data				Standardized data				Normalized data			
	RMSE	R^2	MSE	MAE	RMSE	R^2	MSE	MAE	RMSE	R^2	MSE	MAE
<i>Linear</i>	1.17	0.86	1.37	0.92	0.38	0.86	0.142	0.295	0.052	0.86	0.0027	0.0406
<i>Regression trees:</i>												
Fine tree	1.19	0.86	1.41	0.87	0.39	0.85	0.154	0.291	0.053	0.85	0.0028	0.0396
Medium tree	1.14	0.87	1.29	0.84	0.37	0.86	0.138	0.278	0.051	0.86	0.0026	0.0383
Coarse tree	1.16	0.86	1.35	0.87	0.38	0.86	0.142	0.285	0.052	0.86	0.0027	0.0395
<i>Trees Ensemble:</i>												
Boosted trees	1.31	0.82	1.72	1.04	0.34	0.89	0.115	0.259	0.057	0.83	0.0033	0.0448
Bagged trees	1.06	0.88	1.12	0.78	0.34	0.88	0.117	0.252	0.047	0.86	0.0022	0.0348
<i>GPR:</i>												
SE	1.06	0.88	1.11	0.80	0.34	0.89	0.114	0.257	0.046	0.89	0.0022	0.0353
Exponential	0.91	0.91	0.84	0.68	0.29	0.91	0.086	0.220	0.041	0.91	0.0017	0.0305
<i>SVM:</i>												
Linear	1.18	0.86	1.38	0.91	0.38	0.86	0.143	0.294	0.052	0.86	0.0027	0.0405
Quadratic	1.14	0.87	1.30	0.85	0.37	0.86	0.136	0.276	0.051	0.86	0.0026	0.0379
Cubic	1.54	0.76	2.37	0.86	0.40	0.84	0.159	0.274	0.061	0.80	0.0037	0.0380
Fine Gaussian	2.17	0.51	4.71	1.25	0.70	0.51	0.492	0.406	0.097	0.51	0.0093	0.0560
Medium Gaussian	1.11	0.87	1.23	0.80	0.36	0.87	0.126	0.256	0.049	0.87	0.0024	0.0354
Coarse Gaussian	1.13	0.87	1.28	0.87	0.36	0.87	0.132	0.280	0.050	0.87	0.0025	0.0386

353 In the same way, the medium regression tree model performs better than the fine and coarse tree models
354 as shown in Table 4. This is due to the fact that there is a trade-off between the regression tree size and
355 the model performance. Therefore, a coarse regression tree with fewer large leaves results in spreading the
356 speed predictions over fewer large regions compared to the medium and fine tree models as shown in Figure
357 3. Meanwhile, a very leafy fine tree can result in overfitting and lower its generalization capability. It should
358 be also mentioned that the studied prediction models also perform similarly to Figure 3 when utilizing the
359 standardized and normalized versions of the dataset.

360 Regarding the ensemble of trees models, the bagging technique provides better results than the boosting
361 technique using the raw and normalized datasets as detailed in Table 4. Meanwhile, by standardizing
362 the dataset before training, the boosted trees model performance gets better and provides comparable
363 performance to the bagged trees model. This can be explained by the fact that data standardization
364 improves the data consistency which enhances the sequential learning process of the boosted trees model.

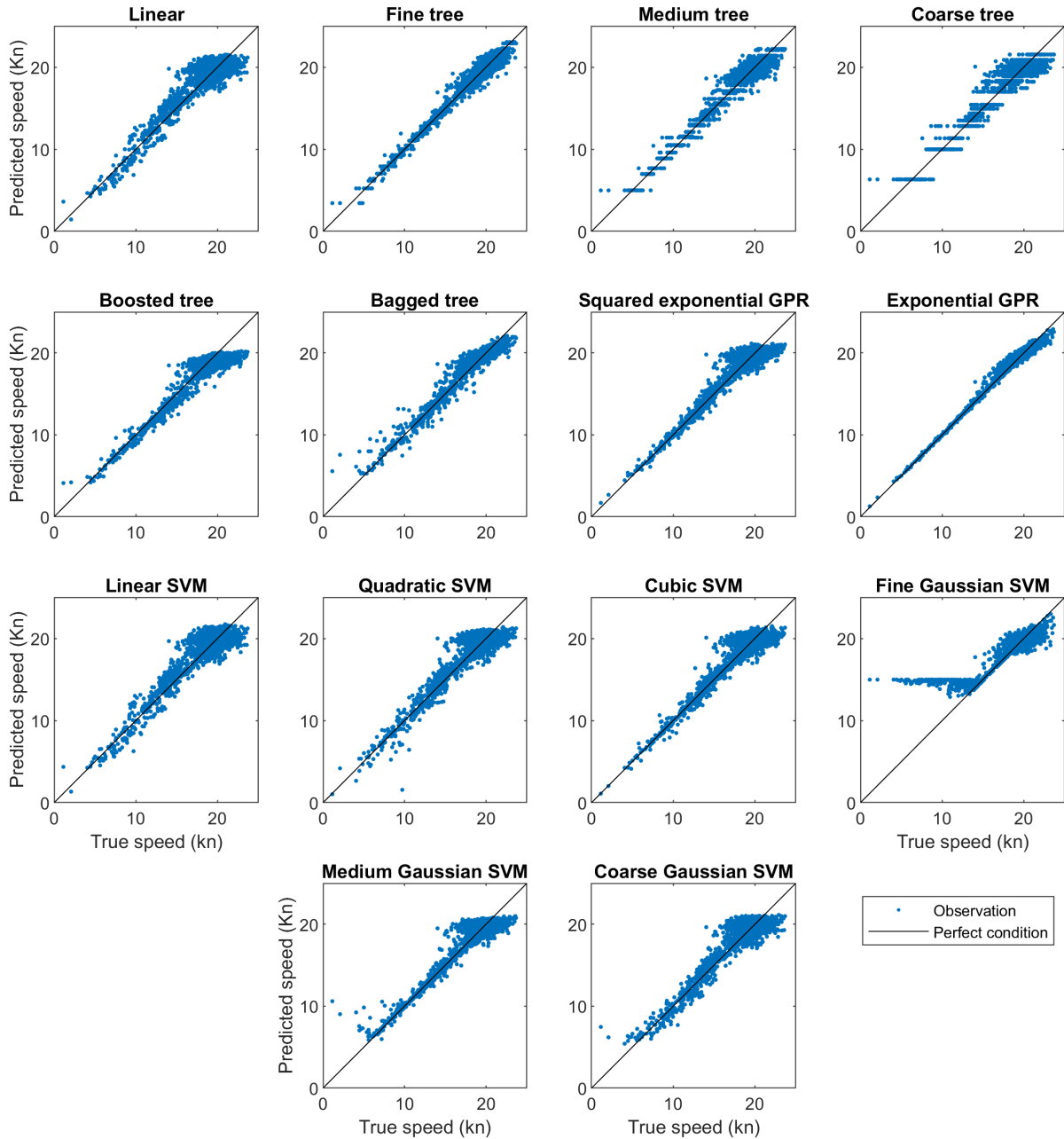


Figure 3: Predicted ship speed versus actual ship speed measurements for different machine learning approaches using raw data and 5-fold cross validation

365 Therefore, this indicates that the boosted trees model is more sensitive to the dataset variables range and
 366 feature scaling than the bagged trees model.

367 In order to study the sensitivity of other regression models to the dataset scale and appropriately compare
 368 their performance, the RMSE value index is calculated for different models using the raw, standardized, and
 369 normalized versions of the dataset. The value index number is calculated as a percentage of the RMSE of
 370 different models compared to the lowest RMSE as a base value as shown in Figure 4.

371 Since the exponential GPR model achieves the lowest RMSE, it is used as a baseline with a value index

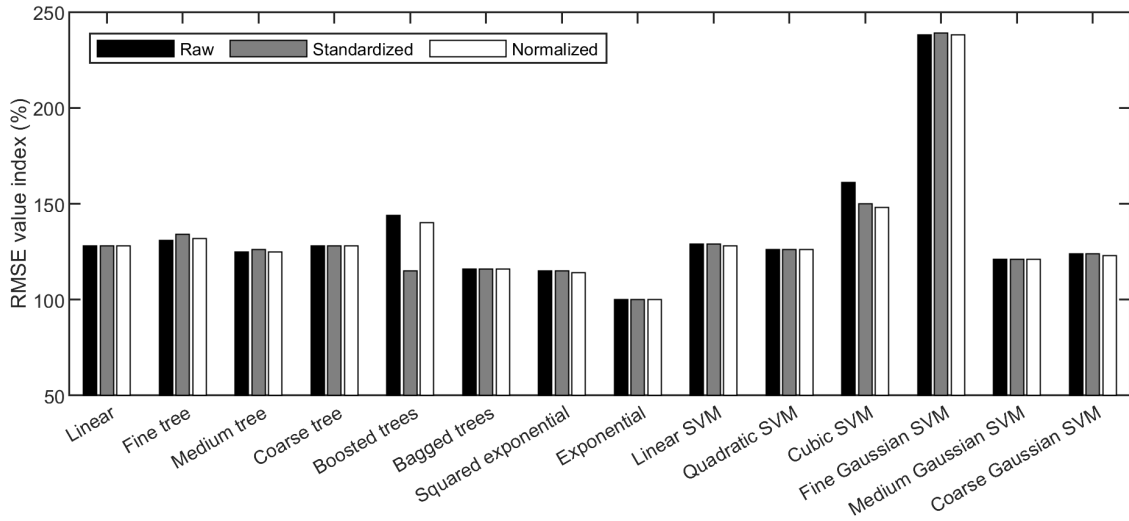


Figure 4: RMSE index value percentage of different machine learning approaches change from the base value using 5-fold cross validation

372 of 100%. As can be found in Figure 4, algorithms such as the boosted trees and the SVM model with cubic
 373 kernel are more sensitive to the range of their input values than other models. Accordingly, standardizing
 374 the dataset before training the boosted tree instead of using the raw dataset can reduce the RMSE value
 375 index by 20%. Meanwhile, normalizing the dataset before training the cubic kernel SVM can reduce the
 376 RMSE value index by 8% compared with using the raw dataset as well. Regarding other models, a slight
 377 accuracy improvement can be achieved by suitably processing the dataset before training the regression
 378 models.

379 The statistical performance of regression models can also be affected by the size of the training and test
 380 dataset which is decided by the k-fold cross validation. Therefore, different values of K is used to split the
 381 dataset into K folds to train and validate different regression models to study the impact of this parameter
 382 on their accuracy in terms of RMSE as shown in Figure 5.

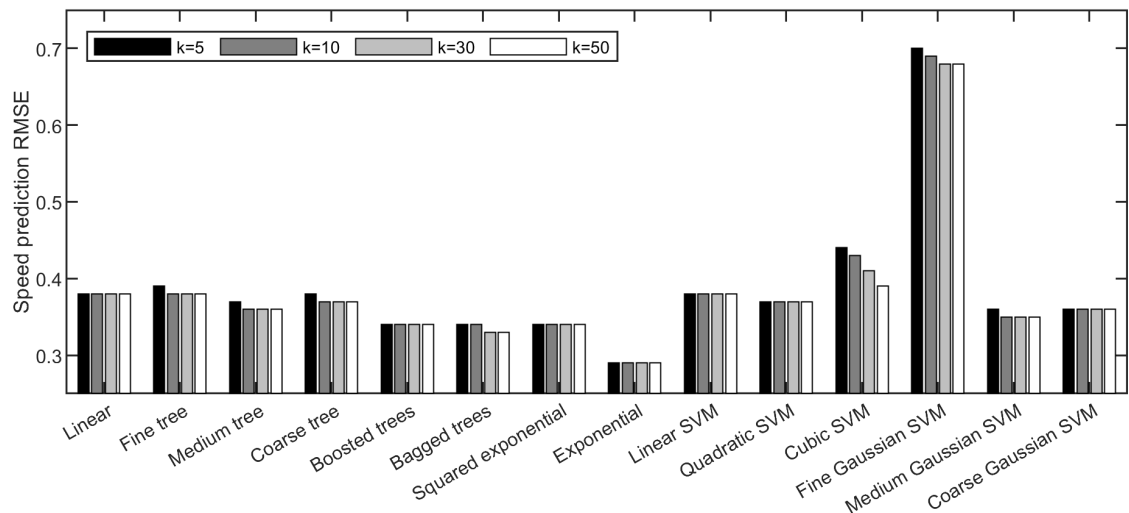


Figure 5: RMSE of different machine learning approaches using the standardized data with K values of 5, 10, 30, and 50

383 As indicated in Figure 5, increasing the number of folds K reduces the calculated RMSE of different

384 machine learning approaches. This is because, as explained earlier, using higher values of K increases the
385 size of the training dataset which improves the models statistical performance. However, this improvement
386 is more significant for the cubic and fine Gaussian SVM models which their RMSE are reduced by 11%
387 and 3% respectively by increasing K from 5 to 50. For other approaches, increasing the number of folds K
388 results in a RMSE reduction of less than 3%. Nonetheless, longer training time and higher computational
389 cost are required by hard interpretability models such as GPR, quadratic and cubic SVM models as a result
390 of increasing the number of data splits as detailed in Table 5. Therefore, a K value of 10 can be considered in
391 further studies to manage the trade-off between the models predictive quality and computational complexity.

Table 5: Required training time for different machine learning approaches with K values of 5, 10, 30, and 50

	Training time (minute)			
	K=5	K=10	K=30	K=50
Linear	<1	<1	<1	<1
Regression trees				
Fine tree	<1	<1	<1	<1
Medium tree	<1	<1	<1	<1
Coarse tree	<1	<1	<1	<1
Trees Ensemble				
Boosted trees	<1	<1	<1	<1
Bagged trees	<1	<1	<1	<1
GPR				
SE	1.3	2.4	6.4	9.7
Exponential	1.8	3.3	8.7	12.9
SVM				
Linear	<1	<1	<1	<1
Quadratic	<1	<1	1.2	1.9
Cubic	2.8	5.2	16.6	27
Fine Gaussian	<1	<1	<1	<1
Medium Gaussian	<1	<1	<1	<1
Coarse Gaussian	<1	<1	<1	<1

392 4.1. Computational experiments

393 In order to demonstrate the functionality of the proposed methodology in the optimization and decision-making
394 processes, different computational experiments are conducted to estimate the impacts of changing significant
395 operational parameters on the ship speed. Operational parameters such as the propellers pitch and ship
396 drafts are used as inputs to the trained exponential GPR model, due to their significant effect on the ship
397 speed, and the results are compared with the model predicted speed using the real ship operational data
398 and the real measured ship speed.

399 In the first case, two propellers pitch values of 95% and 70% are used instead of the real propellers pitch
400 values while using other real operational data of trim, draft, rudders angles, and environmental conditions.
401 As shown in Figure 6, increasing the propellers pitch value results in higher ship speed. However, the
402 propeller and engine rotational speeds should be taken into consideration while selecting the propeller pitch
403 for higher operational efficiency of the ship propellers and engines.

404 In the second case, two different values of ship draft of 5m and 6.5m are simulated while using other
405 real ship operational data of trim, propellers pitch, rudders angle, and environmental conditions. As shown
406 in Figure 7, increasing the ship draft reduces the ship speed as a result of increasing the ship resistance,
407 and correspondingly higher ship speed are obtained at relatively small ship draft of 5m. On the other hand,
408 lighter ship drafts may increase ship resistance at inappropriate trim angles. Therefore, optimization of ship
409 draft/trim combination should be made for more efficient ship operation.

410 Another case to further test the generalization capability of the developed ship speed prediction model
411 is conducted by adapting a new unseen test case where multiple operational parameters are changed. It

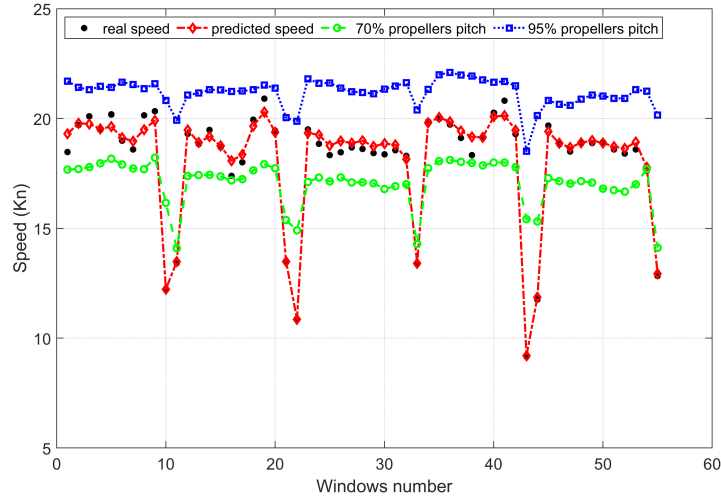


Figure 6: Real vs predicted ship speed at different values of propellers pitch using the exponential GPR model with 5-fold cross validation

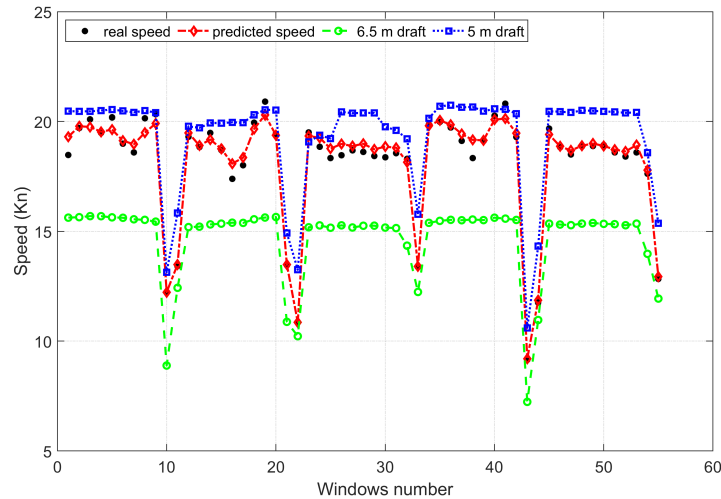


Figure 7: Real vs predicted ship speed at different values of ship draft using the exponential GPR model with 5-fold cross validation

412 is assumed that the ship is loaded to a draft of 6m sailing in a headwind of 20 m/s with an average trim
 413 angle of 0.05 degree aft. As a result, a reduced propellers pitch of 75% is selected for more efficient shipping
 414 operation by properly loading the main engines without having to increase its speed or heavily running the
 415 propellers. Then, it is assumed that the wind speed is changed during sailing to 5 m/s headwind which
 416 allows the propellers pitch to be increased to 90% gradually to avoid any operational delays. The predicted
 417 ship speed for this case is presented in Figure 8 using the exponential GPR model with the propellers pitch
 418 change given in the top plot. However, no real data is available to validate this scenario. Therefore, the
 419 exponential GPR model performance is validated with respect to the prediction of one accurate model of
 420 each regression algorithm type as illustrated in Figure 8 which also shows the response of different models
 421 to the input signals of propeller pitch, wind speed, and rudder angle.

422 According to the obtained results, the developed methodology can help ship operators and decision
 423 makers with evaluating the effect of changing the operational parameters on the ship speed. Consequently,
 424 it can help in creating more advanced models of voyage tracking and monitoring or optimization of different

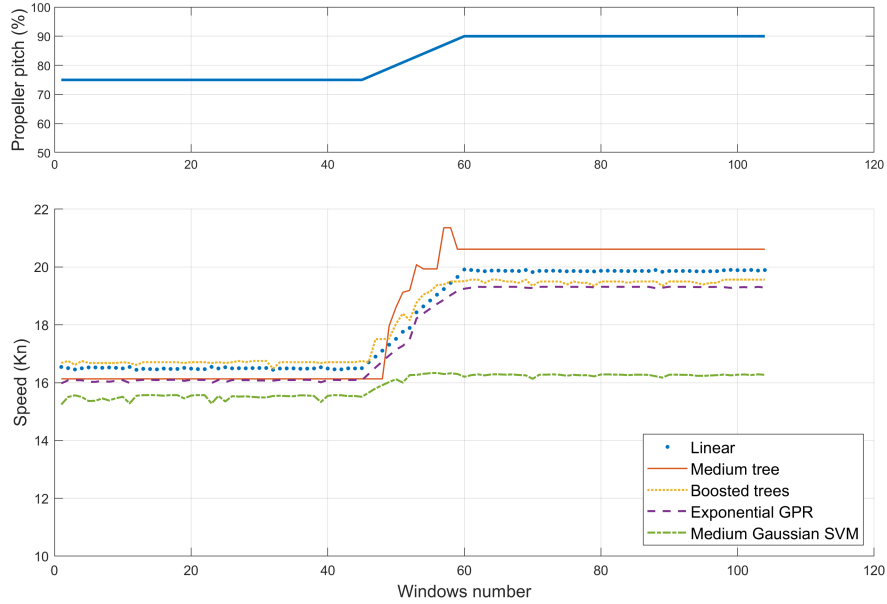


Figure 8: Predicted ship speed for the test case using the exponential GPR model with 5-fold cross validation compared to other regression models

425 ship operational parameters.

426 5. Conclusions

427 In recent years there has been a growing interest in monitoring and optimizing ship operation for better
 428 sustainability and profitability which requires accurate speed prediction. Among different approaches of ship
 429 speed prediction, machine learning and statistical methods have gained substantial momentum in shipping
 430 industry driven by the advances in computer power and the increasing operational data availability. This
 431 allows data-driven models based on machine learning to raise its responsiveness, analytical and prediction
 432 capabilities with more accuracy by extracting hidden information from the collected datasets.

433 A performance comparison of the most commonly used machine learning regression algorithms in terms
 434 of their prediction accuracy of ship speed in real operational conditions utilizing a high quality operational
 435 dataset of a ferry has been presented in this paper. For this, a framework for data preprocessing is provided
 436 which includes the selection and extraction of the operational features having significant influence on the
 437 ship speed. Moreover, new features have been engineered as well for better statistical performance of the
 438 studied models. Features transformation and scaling have been also made before training the machine
 439 learning regression algorithms. Then, cross validation has been made to avoid overfitting and assess the
 440 models generalization capability to new data. This paper also provides useful insights into the effect of
 441 different data scaling techniques on the prediction accuracy of the regression models. Also, a sensitivity
 442 analysis of different folds number and data splits for the cross validation has been made. Furthermore, the
 443 effect of changing different operational parameters on the ship speed is investigated through a correlation
 444 analysis using different techniques. The main findings can be summarized as follows:

- 445 • The studied regression models can accurately predict the ship speed with good accuracy except for
 446 the SVM with fine Gaussian kernel which had only R^2 of 0.51.
- 447 • The GPR method with the Matérn kernel function outperformed all other models in predicting ship
 448 speed with an R^2 of 0.91 but with more required training time.

- 449 • Multiple linear regression which is a considerably simpler algorithm has provided comparable accurate
450 results.
- 451 • Regression trees and trees ensemble models have yielded accurate ship speed prediction with lower
452 computational time. It should, however, be noted that the ensemble boosted trees was sensitive to the
453 data scaling technique which affected its prediction accuracy.
- 454 • The performed sensitivity analysis showed that the SVM algorithms can be sensitive to the data scaling
455 technique as well as the cross validation number of folds depending on the used covariance function.
456 An accuracy increase of 11% and 3% has been achieved in the RMSE of the cubic and fine Gaussian
457 SVM models respectively by increasing the cross validation fold number from 5 to 50.
- 458 • Other model performance hasn't improved noticeably by changing the fold number. Therefore, a
459 10-fold cross validation can be recommended for computationally efficient model performance in terms
460 of prediction accuracy and complexity.
- 461 • Computational experiments have been conducted using the proposed methodology to manage the ship
462 operational parameters and evaluate its effect on the ship speed where the simulation results were
463 rational.

464 By accurately predicting ship speed, the outcomes of this paper can help ship management companies in
465 creating further advanced models for the purposes of route optimization, ship tracking, voyage planning, etc.
466 Also, the proposed methodology can be applied without difficulty to any ship type at different operational
467 conditions or to predict or optimize other important operational parameters such as ship trim or propeller
468 controllable pitch which can be part of the future work. Performance comparison with artificial neural
469 networks should be also made in future studies considering the suitable network architecture, number of
470 layers, neurons, etc.

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