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Cavity Flow Noise Predictions

by

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Abstract

The near and far pressure fields of three-dimensional turbulent cavity flow are studied by time-accurate simulations coupled with aeroacoustic predictions. A large-eddy simulation (LES) method is applied to a cavity with a 5:1:1 length-to-depth-to-width ratio at high Reynolds number (6.8 million based on cavity length) and compared with experiment. A good agreement is found for Rossiter mode amplitudes for all but the first mode, a finding that is in agreement with other numerical simulations. A detached eddy simulation (DES) is carried out at a lower Reynolds number of 45000. For the DES simulation, results from both coarse and fine grids have no obvious differences, suggesting that a grid of one million cells is sufficient. A low-storage Ffowcs Williams-Hawkings (FW-H) solver for far field noise prediction is validated for both closed and open integration surfaces. For three-dimensional calculations it is found that spanwise integration lengths of at least 20 cavity depths give the most accurate far field predictions. For the high Reynolds number cavity peak radiation is found in the range of 57 to 60 degrees (with angles measured relative to the upstream direction). For the lower Reynolds number cavity both fine and coarse grid cases predict a peak radiation angle of 54 degrees. Noise attenuation is studied by placing a liner on the inner cavity walls. It is found that liners have a positive effect for the broadband noise reduction. Optimum noise reduction is found with complete coverage of the cavity floor and walls.

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1. Introduction

1.1 M219 cavity and *Re_D*=45000 cavity cases

In a project on Turbulence Modelling for Military Application Challenges (TurMMAC) [1] a number of M219 cavity experiments were carried out in the QinetiQ wind tunnels; the resulting experimental pressure data can be used as a benchmark to improve turbulence modelling for flow problems. In this report one of the M219 cavity configurations is utilised, namely the M219 cavity without door and with length (*L*) of 20 inches, width (*W*) of 4 inches and depth (*D*) of 4 inches. The M219 cavity is immersed in a subsonic flow with conditions shown in Table 1.1.1. The M219 cavity is simulated with a newly developed DES code and an existing LES code with improvements in non-reflecting boundary conditions.

Length (L)	20 (inches)
Depth (D)	4 (inches)
Width (W)	4 (inches)
Mach number (M)	0.85
Total pressure	14.6444 (Psi)
Freestream static pressure	9.1286 (Psi)
Freestream dynamic pressure	4.6190 (Psi)
Reynolds number (Re)	13.353×10^6 (m ⁻¹)
Total temperature	309.3 (K)

Table 1.1.1

In the experiment twenty seven kulite transducers were placed on the cavity ceiling, on the front plate and on the rear plate as shown in Figure 1.1.1. Ten unsteady pressure histories with a 6 *kHz* sample rate at the K20 to K29 transducer positions, fixed on the cavity ceiling from *x/L*=0.05 to 0.95 with increment of 0.1*D*, were provided for comparison. Therefore overall or band-limited root-mean-square (RMS) pressure distributions can be calculated along the cavity ceiling and be compared with numerical results. There are recommended criteria [1] for a good simulation:

- A. Tone frequency prediction error < 5%.
- B. Tone amplitude prediction error $\leq 5\%$.
- C. Progress achieved in the understanding of issues such as:
	- adverse mesh convergence of the computed solution (i.e. mesh divergence);
	- influence on RANS solutions of an incomplete separation of scales;
	- minimum resolution of scales sufficient for the computation of adequate solutions.

There have been a number of investigations [3-6] on the M219 cavity configuration. Larcheveque [3] used an LES model consisting of a $2nd$ order spatial scheme, a $2nd$ order implicit temporal scheme and a mixed scale turbulence model on a $3.2x10^6$ cell grid. The predicted mode amplitude errors to the experimental data were -3, -14, 2 and -4 *dB* respectively. The $3rd$ mode was predicted to be dominant while the $2nd$ mode was dominant in the experimental data. Only the $4th$ mode frequency was predicted within the 5% error limit. There was an unusual mode prediction at 7.5 *kHz*. Mendonca *etc.* [4, 5] used a 2nd order mixed upwind and central spatial scheme and *k-ε* turbulent DES model to investigate the M219 cavity flow on a $1.1x10^6$ hexahedral cell grid. Details of the temporal scheme were not provided. The typical near wall y^+ value was about 300. Therefore the near wall physics was not captured. No quantitative comparisons of mode frequency and amplitude were given except the power spectrum densities. Mendonca [5] also gave a comparison between a coarse grid (1.1x10⁶ cells) simulation and a fine grid (2.8x10⁶ cells) simulation. In [4], a bandlimited RMS pressure calculation was introduced through a FFT technique. From the presented figures there was no improvement in the RMS pressure prediction on a fine grid. Ashworth $\overrightarrow{6}$ used a Fluent DES model with a 2nd order spatial scheme, a 2nd order implicit temporal scheme and a Spalart-Allmaras (S-A) turbulent model to simulate the M219 cavity flow on a $1.68x10^6$ cell grid. Comparisons between the URANS and the DES predictions showed that the $2nd$ mode was missing from the URANS prediction but was captured by the DES model.

The M219 cavity case is a high Reynolds number case with a flow speed close to sonic conditions and thus a fine grid has to be used in order to resolve free shear layer and to simulate near wall flow physics. A newly developed SotonCAA code uses a high order spatial scheme and an explicit temporal scheme, which requires smaller time step than the lower order schemes and longer integration time for fine grids. Thus the full scale case is very expensive to compute. An alternative cavity case with a low Reynolds number of 45000 was therefore proposed in order to complete the target of the project [1], which is to develop an efficient numerical method to complete flow simulations from near CFD flow field to far field acoustic noise propagation. Although low Reynolds number cavity simulations have no experimental data to compare with, a semi-empirical formula proposed by Rossiter [2] provides a good estimation of mode frequencies with engineering accuracy for a cavity flow in a Mach number range of 0.4 to 1.2 [30]. Importantly it can be done within reasonable time schedule. One of intentions for this low Reynolds number flow simulation is to study mesh

convergence through two three-dimensional (3-D) grids with different sizes. The flow conditions for the proposed cavity are listed in Table 1.1.2.

1.2 LES and DES models

A. LES model

An LES code, SBLI V3.4, was initially employed to run the M219 cavity flow simulations while the DES model was under development. The numerical model is a compressible flow LES model $[8-10]$. A 4th order central finite-difference scheme is employed for the spatial discretization. To improve the nonlinear stability, a split high-order entropy-conserving scheme of Gerritsen and Olsson [11] is used in the Euler equation discretization. In the situation of high Reynolds number flows such as the M219 cavity flow, a weighted five-point filter is applied every ten time steps to strengthen the stability. The time integration scheme is a 3rd order Runge-Kutta scheme [12]. A mixed-scale turbulent model [9] is chosen as subgrid model in the simulations since it requires no averaging in its execution. This code has been parallelized and optimized for many computing platforms. By placing a buffer-zone combined together with Giles [13] characteristic condition as a non-reflecting boundary condition (NRC) in inflow and outflow regions this code performs better than without buffer zone conditions.

In Cartesian coordinates, the Favre filtered equations are [10],

$$
\begin{cases}\n\frac{\partial \overline{\rho}}{\partial t} + \frac{\partial \overline{\rho} \widetilde{u}_{i}}{\partial x_{i}} = 0, \\
\frac{\partial \overline{\rho} \widetilde{u}_{i}}{\partial t} + \frac{\partial \overline{\rho} \widetilde{u}_{i} \widetilde{u}_{j}}{\partial x_{j}} = -\frac{\partial \overline{p}}{\partial x_{i}} + \frac{\partial}{\partial x_{j}} (\widetilde{\tau}_{ij} - \widetilde{\tau}_{ij}^{s}), \\
\frac{\partial \widetilde{E}_{t}}{\partial t} + \frac{\partial}{\partial x_{i}} [\widetilde{u}_{i} (\widetilde{E}_{t} + \overline{p})] = -\frac{\partial}{\partial x_{i}} (\widetilde{q}_{i} - \widetilde{q}_{i}^{s}) + \frac{\partial \widetilde{u}_{j} \widetilde{\tau}_{ij}}{\partial x_{j}} - \widetilde{u}_{i} \frac{\partial \widetilde{\tau}_{ij}^{s}}{\partial x_{j}},\n\end{cases}
$$
\n(1.2.1)

where symbols overbar, tilde and superscripts denote Reynolds, Favre filtered quantities and sub-grid scale quantities respectively. ρ , u_i , p , T , E_t , τ_{ij} and τ_{ij}^s are density, velocity components, pressure, temperature, total energy, viscous stress tensor and sub-grid stress tensor respectively. There are auxiliary relations:

$$
\overline{p} = \overline{\rho}R\widetilde{T},
$$

$$
\widetilde{E}_t = \frac{\overline{p}}{\gamma - 1} + \frac{1}{2}\overline{\rho}\widetilde{u}_i\widetilde{u}_j,
$$

$$
\begin{aligned}\n\widetilde{\tau}_{ij} &= \widetilde{\mu} S_{ij}, \\
\widetilde{\tau}_{ij}^s &= \overline{\rho u_i u_j} - \overline{\rho} \widetilde{u}_i \widetilde{u}_j = \widetilde{\mu}^s S_{ij} \\
\widetilde{q}_i &= -\frac{\widetilde{\mu}}{\text{Pr}} \frac{\partial \widetilde{T}}{\partial x_i}, \\
\widetilde{q}_i^s &= -\frac{\widetilde{\mu}^s}{\text{Pr}_t} \frac{\partial \widetilde{T}}{\partial x_i}, \\
S_{ij} &= \frac{\partial \widetilde{u}_i}{\partial x_j} + \frac{\partial \widetilde{u}_j}{\partial x_i} - \frac{2}{3} \delta_{ij} \frac{\partial \widetilde{u}_k}{\partial x_k},\n\end{aligned}
$$

where constants $\gamma=1.4$, *R*=287.05, *Pr*=0.72 and *Pr_t* =1. The molecular viscosity $\tilde{\mu} \propto T^{0.75}$ and eddy viscosity $\tilde{\mu}^s$ is modelled by sub-grid (SGS) models. In a mixed-scale SGS model [9],

$$
\widetilde{\mu}^{s} = C_{MTS} \overline{\rho} k_{es} T_{s},
$$
\n
$$
k_{es} = (\widetilde{u}_{k} - \widehat{\widetilde{u}}_{k})^{2},
$$
\n
$$
T_{s}^{-1} = \left(\frac{\overline{\Delta}}{\sqrt{k_{es}}}\right)^{-1} + \left(\frac{C_{T}}{|S|}\right)^{-1},
$$

where $\overline{\Delta} = (\Delta x \Delta y \Delta z)^{1/3}$, $|\overline{S}| = \sqrt{\overline{S}_{ij} \overline{S}_{ij}} / 2$, $\overline{S}_{ij} = \partial \widetilde{u}_i / \partial x_j + \partial \widetilde{u}_j / \partial x_i$, $C_{MTS} = 0.05$, and C_T =10. Advantages of mixed-scale model are no artificial averaging and wall-damping function required.

B. Spalart-Allmaras (S-A) RANS and DES models

For high Reynolds number flows, the LES model is not a practical tool to simulate near wall physics due to the huge computing cost associated with fine grids. Detached eddy simulation is an alternative way of solving this kind of problems and it uses RANS turbulent models in solid wall area to cut computing cost down. In this project the S-A turbulent model is employed in the DES model and is written as in references [14, 15]:

$$
\left(\frac{\partial}{\partial t} + \widetilde{u}_i \frac{\partial}{\partial x_i}\right) \hat{v} = c_{b1} (1 - f_{i2}) \hat{S} \hat{v} - \left(c_{w1} f_w - \frac{c_{b1}}{\kappa^2} f_{i2} \right) \left(\frac{\hat{v}}{d}\right)^2 \n+ \frac{1}{\sigma} \left\{\frac{\partial}{\partial x_i} \left[(v + \hat{v}) \frac{\partial \hat{v}}{\partial x_i} \right] + c_{b2} \left(\frac{\partial \hat{v}}{\partial x_i}\right)^2 \right\} + f_{i1} \Delta U^2,
$$
\n(1.2.2)

where \hat{v} is a working variable, v is the kinematic molecular viscosity and *d* is the distance to the closest wall. *U* is a velocity component in the streamwise direction and ∆*U* is the difference between the velocity at a field point and that at the trip [14]. If laminar and transitional regions are not in consideration those terms with subscript *t* can be dropped (i.e.

 f_{tl} =0, f_{t2} =0). The kinematic eddy viscosity \tilde{v}^s is obtained from,

$$
\widetilde{v}^s = \frac{\chi^3 \widehat{v}}{\chi^3 + c_{\nu 1}^3}, \quad \chi = \frac{\widehat{v}}{v}.
$$

Other parameters are:

$$
\hat{S} = S + \left(1 - \frac{\chi}{1 + f_{v1}\chi}\right)\frac{\hat{v}}{\kappa^2 d^2}, \quad S = \sqrt{\Omega_{ij}\Omega_{ij}}, \quad \overline{\Omega}_{ij} = \partial \widetilde{u}_i / \partial x_j - \partial \widetilde{u}_j / \partial x_i,
$$
\n
$$
f_{t2} = c_{t3} \exp(-c_{t4}\chi^2),
$$
\n
$$
f_w = g \left(\frac{1 + c_{w3}^6}{g^6 + c_{w3}^6}\right)^{1/6}, \quad g = r + c_{w2}(r^6 - r), \quad r = \frac{\hat{v}}{\hat{S}\kappa^2 d^2},
$$
\n
$$
f_{t1} = c_{t1}g_t \exp\left[-c_{t2} \frac{\omega_t^2}{\Delta U^2} (d^2 + g_t^2 d_t^2)\right], \quad g_t = \min\left[0.1, \frac{\Delta U}{\omega_t \Delta x_t}\right],
$$
\n
$$
c_{w1} = \frac{c_{b1}}{\kappa^2} + \frac{1 + c_{b2}}{\sigma}.
$$

Constants are c_{b1} =0.1355, σ =2/3, c_{b2} =0.622, κ =0.41, c_{w2} =0.3, c_{w3} =2, c_{v1} =7.1, c_{v2} =5. In the trip function f_t , d_t is defined as the distance from the field point to the trip, which is on a wall, ω_t is the wall vorticity at the trip and Δx , is the grid spacing along the wall at the trip. Other constants are c_{t} ^{$=$ 1}, c_{t} ^{$=$ 2}, c_{t} ^{$=$}^{$=$ 1}.1 and c_{t} $=$ ².

The DES model uses the S-A model with a new distance \tilde{d} to replace *d*: $\tilde{d} = min(d, c_{DES} \Delta)$. Δ is the maximum distance between the neighbouring cells. A constant c_{DE} =0.65 is defined for homogeneous turbulence. Therefore away from the cavity flat plates/ceilings the DES model will produce solutions similar to LES with a Smagorinsky sub-grid model.

1.3 SotonCAA code

The SotonCAA code consists of two parts. The first part is for the simulation of acoustic mode propagation through the solution of the modified linearised Euler equations (LEE) [16, 17] while the second part is for CFD flow simulation by solution of the Navies-Stokes (N-S) equations coupled with a DES/S-A turbulence model for sub-grid eddies. In order to maintain a capacity for aeroacoustic noise prediction the code uses high order temporal and spatial schemes to keep wave dissipation and dispersion low. A compact finite-difference scheme ($6th$ order) of Hixon [16] or a 4th order pre-factored scheme [19] is used for spatial derivative calculation. Time integration uses a low storage, low dispersion and dissipation Runge-Kutta (LDDRK) [20] scheme which is a $4th$ order 4-6 stage scheme. Other low order $(2nd - 3rd)$ temporal schemes are also available to enable rapid establishment of flow fields, i.e. running to an approximate solution before starting the main calculation. Explicit filtering [21] from $2nd$ to $10th$ order accuracy is also used to filter out numerical noise and to improve computing stability. The code is portable across many computing platforms with FORTRAN 90 and MPI installed. Figure 1.3.1 shows a result of parallel scaling test on HPCx computer using 28, 56 and 112 processors for a grid consisting of $1.05x10^6$ cells. Compared with ideal

speedup line (straight line), a quasi-linear speedup is achieved and with high number of processors, such as 56 processors, computing efficiency is improved.

Figure 1.3.1: parallel scaling of SotonCAA code

Non-dimensional values of flow variables and coordinates are used in the SotonCAA code. The dimensional reference values are characteristic length L^* , free-stream density ρ^*_{∞} and free-stream sound speed *C* [∞]*. The corresponding non-dimensional values are as follows:

$$
x = x^*/L^*, \quad y = y^*/L^*, \quad z = z^*/L^*,
$$

\n
$$
t = t^* * C_{\infty}/L^*,
$$

\n
$$
\rho = \rho^*/\rho^*_{\infty},
$$

\n
$$
u = u^*/C^*_{\infty}, \quad v = v^*/C^*_{\infty}, \quad w = w^*/C^*_{\infty},
$$

\n
$$
T = T^*/R/C_{\infty}^{*2},
$$

\n
$$
p = p^*/(\rho^*_{\infty}C^*_{\infty}),
$$

where an asterisk stands for a dimensional value and *t* and *T* are non-dimensional time and temperature respectively. *R* and γ (= C_p/C_v) are the ideal gas constant and the ratio of specific heats and have values of 287.05 JK_g⁻¹K⁻¹and 1.4 respectively. Therefore nondimensional free-stream values for flow velocity components, density, pressure and temperature are M_x , M_y , M_z , 1.0, 1.0/ γ and 1.0 where *M* is Mach number. In this report, the cavity depth *D* is chosen as the characteristic length L^* .

1.4 Target

To improve understanding and modeling of turbulent flow phenomena of importance for industrial aerospace applications, this project aims to use a high order DES code, in Southampton University, coupled with an efficient far field noise prediction method and apply it to cavity flow simulations [1]. Along with the DES simulation, the LES code is employed to simulate the 3-D M219 cavity flow. Experience from this computation is then utilised when the SotonCAA DES code is available for use.

In conjunction with simulation using the SotonCAA DES code and implementation of a low storage Ffowcs Williams-Hawkings (FW-H) solver, other code modifications have also been attempted to extend the capability of the SotonCAA code and to finish the project in time. Not all of these were successful due to limitations of the numerical method (such as high order implicit temporal schemes [29]) or the limitation of the project time (such as validations of three-dimensional (3-D) open FW-H integration surface due to *z* length variations). Cavity flow control is studied through acoustic treatments on inner cavity walls/ceilings. In the analysis of unsteady pressure oscillations on the cavity ceiling, a calculation of the band-limited RMS pressure uses the FFT technique to extract single mode information so that single mode contribution can be studied. Llower and upper limits of the band-width are defined as the mid-point of adjeccent mode frequencies shown in Table 1.4.1. For example the 1st mode band-width is from 76 to 261 *Hz* for the M219 cavity case. Those mode amplitudes inside each mode band-width are reserved and others are set to null. Pressure history recovered from the spectral space will present mode contributions to the pressure field and the RMS pressure pattern. Through band-limited pressure analyses, mode contribution to the unsteady pressure oscillations would be clear.

This report is structured as follows. Firstly the M219 cavity flow simulations are described. In Section 2.2 the two-dimensional (2-D) LES and DES simulations are discussed. Threedimensional (3-D) simulations using LES and DES models are discussed in Section 2.3. In order to complete the project target in time, a low Reynolds number $(Re_D=45000, M=0.8)$ cavity flow case is simulated using the SotonCAA DES/S-A model and results are discussed in Sections 2.4 and 2.5. Section 3 focuses on implementation and application of a low storage FW-H solver and sensitivity tests of the FW-H integration surface. Results of far field cavity flow noise prediction using either low storage or high storage FW-H solver are shown. A 2-D cavity flow oscillation control study is reported in Section 4. Summary of the works and some discussions are given in Section 5. To summarise the cavity cases Table 1.4.2 lists all cases with key parameters included. The cavity length-to-depth-to-width ratio for all cavity cases remains 5:1:1. The total computational domain lengths in the *x*, *y* and *z* directions are shown as *TL*, *TD* and *TW* and the Reynolds number based on the cavity depth *D* is shown as *ReD*.

Table 1.4.2: All cavity cases and key parameters

Model	M	Re _D	Grid number	TL:TD:TW	Total time (sec)
2-D LES	0.85	1358000	$7.20x10^4$	11:4	0.159
3-D LES	0.85	1358000	5.74×10^{6}	15:7:2	0.151
2-D DES	0.85	1358000	$8.17x10^4$	14:6	0.209
3-D DES	0.85	1358000	$1.05x10^{6}$	24:14:2	0.05
2-D DES	0.8	45000	$8.09x10^{4}$	24:14	0.107
3-D DES (coarse)	0.8	45000	$1.05x10^{6}$	24:14:2	0.088
3-D DES (fine)	0.8	45000	$4.08x10^{6}$	24:14:2	0.055

2. Cavity near field CFD simulations

2.1 Introduction of M219 cavity simulations

3-D simulation using explicit high order temporal and spatial schemes is an expensive operation in terms of time and computing resources. Therefore a 2-D simulation of the M219 cavity is performed to provide an initial solution with an aim of shortening the flow transient period in the 3-D simulation. The 2-D DES simulation also serves as a validation case to find potential problems during the SotonCAA code development. Although the 2-D simulation is not entirely suitable for DES, results can be used a reference to compare with the 3-D simulation. In addition a sensitivity test of FW-H integration surface placement can also be done in the streamwise (x) and normal (y) directions using results of the 2-D simulation. Simultaneously with the development and validation of the SotonCAA DES code, an existing LES code is utilised to simulate the 2-D and 3-D M219 cavity flows.

2.2 M219 cavity 2-D simulations

2.2.1 2-D LES simulation

Figure 2.2.1.1: A schematic of 2-D grid, unit in D.

Figure 2.2.1.1 shows the 2-D computational domain and stretched grid. SBLI LES code was used to run the 2-D cavity flow simulation on an SGI Origin-3000 computer. Total length in the streamwise direction (along the *x* axis pointing right) was 11*D* from *x/D*=-1 to 10 and total length in the normal direction (along the *y* axis) was 4D from $v/D=0$ to 4. Total cell number was 72000. There were 17 cells from $y/D=1$ to 1.1 and 38 cells from $y/D=1$ to 1.3 to ensure sufficient grid resolution in the free shear layer. The first cell was 0.005*D* away from the plate. A characteristic boundary condition and a buffer-zone boundary condition were applied at the inflow and outflow boundaries to filter out reflected acoustic waves. The buffer zone width was 10 cells. A steady flow profile at the inflow boundary was obtained from a turbulent flat plate computation and the turbulent boundary thickness was set at 0.1*D* at cavity leading edge according to an estimation of $0.37xRe_x^{-0.2}$ since no experimental boundary layer parameters were available. Small time-varied disturbances were added in the inflow profile to trigger the cavity flow oscillation and they were turned off when flow oscillations started and became strong so that the spectrum analysis would not be affected. The wall temperature was fixed at the value of total temperature and a no-slip condition was applied to all cavity inner walls and the flat plates upstream and downstream of the cavity. A non-dimensional time step of $2.4x10^{-3}$, corresponding to a real time step of $8.7x10^{-7}$ sec, was used to advance the solutions. Figure 2.2.1.2 shows pressure history at the K29 position. The

pressure oscillation is already fully developed from 0.03 *sec* showing that the self-sustained flow oscillation starts very quickly.

Figure 2.2.1.2: Pressure history at K29.

Table 2.2.1.1: Mode prediction

Modes	- SU	γ nd	2 rd	4 tn	
Rossiter's formula	159 Hz	371 Hz	582 Hz	794 Hz	
Experiment	151 Hz	370 Hz	605 Hz	773 Hz	
(0.1 sec)	156 dB	158 dB	155dB	144dB	
2-D LES	167 Hz	341 Hz	506 Hz	675 Hz	
	175 dB	171 dB	164 dB	152 dB	

Table 2.2.1.1 lists the predicted frequencies using a 0.129 *sec* long pressure data from 0.03 to 0.159 *sec* with a sample rate of 10 *kHz*. The Rossiter's formula [2] can be written as,

$$
f = \frac{MC_{\infty}^*}{5D} \frac{m - \gamma_1}{M + 1/\kappa_1},
$$
\n(2.1)

where *f* is the resonance frequency and *m* is the mode number. Constants $\gamma_1 = 0.25$ and $\kappa_1 = 0.57$ are phase delay and ratio of the averaged perturbation convective speed to the freestream velocity respectively. It is noticed that the mode frequencies calculated from equation (2.1) are all within 5% of the experimental values. Therefore the Rossiter's formula predicts this case well. The numerically predicted frequencies are 167, 341, 506 and 675 *Hz* at the K29 position and the relative errors compared to the experimental values listed in Table 2.2.1.1 are $+11\%$, -8% , -16% and -13% respectively. The mode frequencies are under predicted except for the 1st mode and all relative errors are over the 5% error limit. The mode amplitudes are also not predicted well. Figure 2.2.1.3 gives a visualisation of the SPL departures. The 1st mode amplitude is 19 \overrightarrow{dB} higher than the experimental one. Form Table 2.2.1.1, the errors of the mode amplitudes are +19, +13, +9 and +8 *dB* respectively. The predicted dominant mode is the $1st$ mode. It will shown from later 3-D simulations that flow three-dimensionality is essential for the correct mode amplitude prediction. Over-prediction of the amplitudes also affects on the RMS pressure predictions shown in Figure 2.2.1.4. The RMS pressure discrepancy between the experiment and the 2-D LES results is significant. It is also observed from Figure 2.2.1.5 that the $1st$ mode is predominant.

Figure 2.2.1.5: Modal RMS pressure.

2.2.2 2-D DES simulation

Figure 2.2.2.1: 2-D computational domain and stretched grid.

As shown in Figure 2.2.2.1 in this simulation the 2-D computational domain was extended so that the buffer-zone conditions were placed further away from the free shear layer, where strong flow nonlinear interaction occurs, because the Giles [13] characteristic condition had not been implemented in the SotonCAA code. The total length in the x direction was 14*D* from x/D =-2 to 12 and in the y direction was 6*D* from y/D =0 to 6. The total cell number was

81650. At the time of this simulation the grid was extracted from a 3-D grid with a plan to complete the 3-D DES simulation within the time schedule and within the capacity of the computing resources, the y_1^+ , defined as y^+ at the first interior grid point near the cavity wall, was chosen to be about 90 ($y_1/D=0.003$). The solution would not be able to capture near wall physics such as flow separation as y_1^+ was not small enough to resolve the viscous sub-layer. In a similar situation, Mendonca *et al.* [4, 5] used y_1^+ \sim 300 in their 3-D DES M219 cavity simulation. As described later in section 2.3, we were able to use $y_1^{\dagger} \sim 1$ for the 3-D DES M219 cavity flow simulation for 0.05 *sec*. In this configuration there were 24 cells from $y/D=1$ to 1.1 and 45 cells from $y/D=1$ to 1.3. Boundary conditions were the same as the previous case. A non-dimensional time step of $2.59x10^{-4}$, corresponding to a real time step of $8x10^{-8}$ *sec*, was used to advance the solutions.

Figure 2.2.2.2 shows the pressure history at the K29 position. The pressure oscillation is fully developed from 0.089 *sec* showing that the self-sustained flow oscillation period has started. With a pressure history of 0.12 *sec* from 0.089 to 0.209 *sec*, mode predictions are shown in Table 2.2.2.1. Mode errors to the experimental values are +16%, -8%, -9% and -11% for the mode frequencies and +20, +13, +10 and +10 *dB* for the mode amplitudes respectively. In the 2-D DES computation, the mode prediction, as shown from Figures 2.2.2.3 to 2.2.2.5, are very similar to those of the 2-D LES solutions. However although the DES/S-A model is not actually suitable for a 2-D flow it does give a reasonable prediction of the mode frequencies and at least it validates the SotonCAA code.

Figure 2.2.2.2: Pressure history at K29.

Modes	1 st	2 nd	3^{rd}	4^{th}
Rossiter's formula	159 Hz	371 Hz	582 Hz	794 Hz
Experiment	151 Hz	370 Hz	605 Hz	773 Hz
(0.1 sec)	156 dB	158 dB	155dB	144dB
2-D LES	167 Hz	341 Hz	506 Hz	675 Hz
	175 dB	171dB	164 dB	152 dB
2-D DES	175 Hz	340 Hz	518 Hz	691 Hz
	176 dB	171dB	165 dB	154 dB

Table 2.2.2.1: Mode frequency comparisons at K29

Figure 2.2.2.3: SPL spectrum at K29.

2.3 M219 cavity 3-D simulations

2.3.1 3-D LES simulation

The same LES code used in the 2-D simulation was used for a 3-D simulation of the M219 cavity. A periodic boundary condition was applied in the *z* direction. Based on experiences gained in the previous 2-D cavity flow simulations, a wider computational domain was adopted using a 5.74x10⁶ cell grid. There were $0.88x10^6$ cells (250x80x44) inside the cavity and $4.86x10^6$ cells ($450x150x72$) above the cavity. A schematic of 3-D computational domain and some 2-D grid slices are illustrated in Figures 2.3.1.1 and 2.3.1.2. The minimum cell volume size was 0.0075*D* x 0.005*D* x 0.0075*D* with 17 cells clustered in a 0.1*D* range near the plate and 37 cells from $y/D=1.0$ to 1.3. In this larger computational domain the nonreflecting boundary condition can be placed further away from the strong non-linear flow interaction area, while the stretched grid near the outflow boundaries provides extra damping to reduce the acoustic reflections. Because of the low dissipation and dispersion errors of the high order schemes unsteady 3-D disturbances were added to provide an unsteady turbulent inflow profile and they were turned off when flow oscillations started and became strong so that the spectral data would not be affected. A fixed non-dimensional time step of 2.4×10^{-3} ,

corresponding to a real time step of 8.7×10^{-7} sec, was used to advance the solutions. The total computational time was 0.151 *sec* and data were recorded for a 0.1 *sec* time duration from 0.051 to 0.151 *sec*. Results of the mode frequency prediction were compared using two identical time periods, 0.051 to 0.101 *sec* and 0.101 to 0.151 *sec*, to show that sufficient computational time was used. Predicted results were also compared with the experimental data with 0.1 *sec* time duration. Jobs were submitted on the HPCx parallel computer and 128 processors were used with a run time of 12 hours per job.

Figure 2.3.1.1: A schematic of 3-D computational domain.

A. Pressure histories and RMS pressure patterns

Figures 2.3.1.3 and 2.3.1.4 show the perturbation pressure histories recorded at three positions along the cavity ceiling. From these data it can be observed that flow oscillation is fully developed from 0.05 *sec* and the flow field is in a self-sustained oscillation stage. As shown in Figure 2.3.1.5 the pressure fluctuation level reaches its maximum at the rear cavity wall. There are other two features in Figure 2.3.1.5. In comparison with the experimental RMS pressure (black line), the LES values are higher (by 0 to 1700 *Pa*) with large differences in the near wall regions. Inspection of the flow fields finds two flow vortices in the middle of the front and rear walls and their movements have large impacts on the pressure fluctuations around the cavity corners, resulting in the higher RMS pressure. In comparison with the LES data for two identical periods (0.051 to 0.101 *sec* and 0.101 to 0.151 *sec*) no apparent differences are observed suggesting current pressure oscillations are well developed after 0.051 *sec* and no further computation beyond 0.151 *sec* would be needed.

In Figures 2.3.1.6 and 2.3.1.7 the mode contributions to the RMS pressure are illustrated. For the experimental RMS pressure contributions, the $2nd$ mode contributes the most. Contribution from the 1st mode is mainly in the rear part of cavity. A detailed study reveals that for the first three modes there are three RMS pressure peaks, of which two peaks are

fixed at x/L =0.05 and 0.95 and for the 4th mode there are four peaks located at x/L =0.05, 0.25, 0.55 and 0.95. In the LES simulation the RMS peaks are determined by their mode number and it is not necessary to have a peak at $x/L=0.05$, such as in the patterns of the 3rd and 4th modes. The 1st mode has a major impact on the whole pattern. In comparison to the experimental pattern the simulation of the $1st$ mode is poor, resulting in higher RMS pressure distribution.

B. SPL comparison at cavity ceiling

In comparison with experimental data at the K29 position, as shown in Table 2.3.1.1, the LES under-predicts the mode frequency in first three modes and the errors to the experimental data are -13%, -10%, -9% and +3% respectively. Inadequate computing time may be a reason for the unsatisfied mode frequency prediction especially for the $1st$ mode, as its accurate prediction should require long integration time. However comparisons in two identical time periods have shown sufficient integration time for the prediction, this may not be the reason for the 2nd and 3rd modes and should be explored in future. For the mode amplitude prediction the 3-D LES prediction has a significant improvement over the 2-D LES prediction. The errors to the experimental data are +8, +2, +2 and +5 *dB* respectively. Compared to the 2-D results the SPL improvements are 11, 9, 7 and 3 *dB* respectively. The mode amplitude prediction can generally be regarded as good although the dominant mode is not the $2nd$ mode, which is a common problem in current numerical simulations [3-6].

Modes	1 st	2^{nd}	3^{rd}	$4^{\rm th}$
Rossiter's formula	159 Hz	371 Hz	582 Hz	794 Hz
Experiment	151 Hz	370 Hz	605 Hz	773 Hz
(0.1 sec)	156 dB	158 dB	155dB	144dB
2-D LES	167 Hz	341 Hz	506 Hz	675 Hz
	175 dB	171dB	164 dB	152 dB
3-D LES	131 Hz	332 Hz	553 Hz	794 Hz
	164 dB	160 dB	157 dB	149 dB

Table 2.3.1.1: Mode frequency comparisons at K29

Figures 2.3.1.8 to 2.3.1.17 show the SPL comparisons between the LES results and the experimental data (left-hand figure) and two LES results for the two identical periods (righthand figure) at the cavity ceiling. For mode predictions at all positions from K20 to K29, the LES under-predicts the 1st modes by 20 *Hz* but over-predicts the amplitude by 8 *dB*. For the $2nd$ mode, the prediction (332 *Hz* at seven out of ten positions) under-predicts the mode frequency by 38 *Hz* and the amplitude differences are between 0 to 5 *dB* with maximum value at the K26 position. For the 3rd mode, the mode frequency prediction is lowered by 52 *Hz* (in eight out of ten positions) and the amplitude predictions are within 1 *dB* in six out of ten positions with the maximum difference of -7 dB at the K20 position. For the 4th mode, the LES predictions are smeared over a band of frequencies and close to the experimental data. The amplitude is over-predicted by 0 to 9 *dB* depending on location. In conclusion, the LES under-predicts the mode frequency but over-predicts the mode amplitude. For higher frequencies, it can be observed from figures 2.3.1.8 to 2.3.1.17 that the LES predictions match the experimental data quite well.

Figure 2.3.1.18: SPL spectrum at *x/L*=0.5, *y/D*=1.0, *z/D*=1.5 (Mid-cavity).

This LES simulation also has pressure recordings at a high sampling rate of 700 *kHz* at two monitored positions. Figure 2.3.1.18 shows a SPL spectrum at a position in the shear layer (middle of the cavity) and there is no dominant amplitude peak in high frequency range over 1 *kHz* in this LES simulation as compared to the one predicted at 7 *kHz* in one published paper [3], which is now believed to have been a numerical artifact.

To conclude the comparison shows that the mode predictions in both periods are almost the same. Therefore there is no need to continue the computation for a longer period. In comparison with the experimental data, reasonable predictions of the modes are observed except for the $1st$ mode amplitude. This departure from experimental results is consistent with other numerical simulations [4-6].

2.3.2 3-D DES simulation

A schematic of the 3-D mesh is shown in Figure 2.3.2.1. The total cell number was $1.05x10^6$ and the minimum cell volume size was $0.0006D(x) \cdot 0.0002D(y) \cdot 0.006D(z)$. There were 30 cells clustered in a 0.1*D* space near the flat plate to ensure $y^+ \sim 1$ and 37 cells from *y*/D=1.0 to 1.3 to ensure enough grid resolution in the free shear layer. It was possible to simulate the 3-D DES M219 cavity flow for 0.05 *sec* on the HPCx computer using 112

processors. Boundary conditions and inflow turbulent profile were the same as those used in the 3-D LES simulation. A fine grid $(4.2x10⁶)$ was established but could not be used in the M219 cavity flow simulation due to insufficient computing power and project time constraint.

Modes 1^{st} 2^{nd} 3^{rd} 4^{th} Rossiter's formula $\begin{array}{|c|c|c|c|c|c|c|c|} \hline \end{array}$ 159 Hz $\begin{array}{|c|c|c|c|c|c|c|c|} \hline \end{array}$ 582 Hz $\begin{array}{|c|c|c|c|c|c|} \hline \end{array}$ 794 Hz Experiment (0.1 sec) 151 Hz 156 dB 370 Hz 158 dB 605 Hz 155dB 773 Hz 144dB $3-D$ LES 131 Hz 164 dB 332 Hz 160 dB 553 Hz 157 dB 794 Hz 149 dB $3-D$ DES 145 Hz 173 dB 378 Hz 158 dB 524 Hz 150 dB 669 Hz 149 dB

Table 2.3.2.1: Mode frequency comparisons at K29

Kulite 29

As shown in Figure 2.3.2.2 the pressure oscillation at the K29 position develops after 0.02 *sec* and only narrowband frequencies can be observed. Table 2.3.2.1 shows the mode frequency comparisons using the K29 pressure data from 0.027 to 0.062 *sec*. For this short period only the $2nd$ mode frequency prediction seems better than the LES results. After 0.05 *sec* integration time the flow solutions are transferred back to the Iridis2 parallel computer at the Southampton University and the simulation was continued using 56 processors for a period of five months. It Apoears from a zoom view of the streamwise velocity contours shown in Figure 2.3.2.6 that the broadband turbulent features have not developed. Figures 2.3.2.3 to 2.3.2.5 show the mode FFT analysis and the RMS pressure at the cavity ceiling. They all indicate an initial stage of the self-sustained flow oscillations as only the $1st$ mode is predominant and the 2nd mode and higher modes are not properly developed.

Figure 2.3.2.6: Instantaneous *u* velocity (zoom view).

2.4 Re_D = 45000 2-D cavity DES simulation

As stated in the introduction section, low Reynolds number 2-D/3-D cavity flows $(Re_D=45000, M=0.8)$ were simulated owing to three factors: limitation of the computing power, y_1^+ (~1) requirement and short project time. During the project, 3-D coarse grid and fine grid cases were studied to address the issue of grid sensitivity.

A 2-D cavity flow simulation was performed to provide an initial guess to start the 3-D simulation. The 2-D computational domain, which was an *x-y* cross-section of a 3-D fine grid domain, and stretched grid is shown in Figure 2.4.1. The total length in the *x* direction was 24.3*D*, from $x/D=-4.3$ to 20, and in the *y* direction 14*D*, from $y/D=0$ to 14. The total cell

number was 80940. Again the computational domain was enlarged in both directions so that the buffer-zone conditions were placed further away from the free shear layer. In this simulation no inflow turbulent profile was provided. An estimation suggested that the starting point of the computational domain at *x/D*=-4.3 would produce a 0.1*D* boundary layer thickness at the cavity edge (at $x/D=1.0$). The y₁⁺ was 1.0 (y₁/*D*=0.0037) in the flat plate. At the flat plate there were 19 cells from $v/D=1$ to 1.1 and 37 cells from $v/D=1$ to 1.3. The same boundary conditions were applied as the previous 2-D DES case. Unsteady disturbances were not added in the inflow profile in the boundary layer upstream of the cavity. A nondimensional time step of 2.23×10^{-4} , corresponding to a real time step of 2×10^{-8} sec, was used to advance the solutions.

Figure 2.4.1: Computational domain and stretched grid.

It can be observed from Figure 2.4.2 that pressure oscillation is fully developed from 0.008 to 0.107 *sec*. It seems that without the unsteady disturbances added in the inflow profile cavity flow oscillations are still triggered at an early stage. Using a time period of 0.057 *sec* from 0.05 to 0.107 *sec*, the mode predictions are shown in Table 2.4.1 and Figure 2.4.3. Although

the DES/S-A model is not suitable for a 2-D cavity it does give a reasonable prediction of the mode frequencies. Compared to the results of Rossiter's formula, the 1st mode frequency is over-predicted by 4%, the $2nd$ to $4th$ mode frequencies are under-predicted by 8%, 12% and 3% respectively. Figures 2.4.4 and 2.4.5 show the RMS pressure and the near field SPL pattern respectively. Compared to the M219 cavity case, the lower Reynolds number flow seems to produce lower RMS pressures on the cavity ceiling. Similar to the M219 2-D DES simulation the $1st$ mode has a dominant contribution to the overall RMS pressure pattern indicating that in the 2-D simulations the $1st$ mode is always over-predicted. It is noticed from Figure 2.4.5 that the most intensive flow activity happens in the shear layer close to the rear wall and the rear wall region.

2.D DES

Figure 2.4.5: SPL pattern.

2.5 $Re_D = 45000$ 3-D cavity DES simulations

2.5.1 Coarse grid

Based on the 2-D fine grid used in Section 2.4 a coarse 3-D grid used half of the cells in the *x* and *y* directions. A 2-D *y-z* slice of the 3-D computational grid is shown in Figure 2.5.1.1 with a 2-D *x-y* slice (fine grid) in Figure 2.4.1. The total cell number was 1.05×10^6 of which $0.117x10^6$ cells were inside the cavity. There were 72 computing blocks with 29x36x14 cells per block. Near the flat plate there were 10 cells from *y/D*=1 to 1.1 and 19 cells from *y/D*=1 to 1.3. The first cell was 0.0076*D* away from the plate. The freestream Mach number, freestream temperature, cavity depth and Reynolds number based on *D* were 0.8, 200*K*,

0.0254 *m* and 45000 respectively. The ratio of length-to-depth-to-width remained 5:1:1. The domain length in the *x* direction was 24.4*D*, ranging from *x/D*=-4.4 to 20, and the length in the *y* direction was 14*D*, ranging from *y/D*=0 to 14, and length in the *z* direction was 2.0*D* above the cavity, ranging from *z/D*=0 to 2. In this simulation no inflow turbulent profile was provided. A buffer-zone boundary condition was placed in the inflow and outflow regions to prevent spurious wave reflections. A periodic condition was applied at the spanwise (*z*) side computational boundaries. The wall temperature was fixed and the no-slip condition was applied to all cavity inner walls and the flat plates upstream and downstream of the cavity. By using a $3rd$ order explicit Runge-Kutta temporal scheme, a $4th$ order optimized compact spatial scheme and a $6th$ order filter in every three time step, a typical time step was $3.3x10⁻⁸$ *sec*. The data sampling rate was 10 *kHz*.

3000

2000

100

 -100

 -200

 -3000 _{0.02}

 0.03

p' (Pa)

Figure 2.5.1.2 shows the pressure history at the K29 position. The pressure oscillation amplitude falls initially and stays approximately constant after 0.04 *sec*. Data recorded from 0.049 to 0.088 *sec* are analysed, with one of the mode analyses and the RMS pressure distribution along the cavity ceiling shown in Figures 2.5.1.3 to 2.5.1.5. Compared with the 2-D DES case, shown in Figure 2.5.1.4, the RMS pressure prediction is much lower and smoother and the $1st$ mode contributes the most to the overall RMS pressure since two curves are roughly parallel and closer than the other three modes. A detailed comparison of the SPL mode prediction is listed in Table 2.5.1.1. Compared with 2-D prediction, the first three

mode amplitudes reduced by 11, 14 and 9 dB respectively and the $4th$ mode amplitude is unchanged. For mode frequencies predicted by the Rossiter's formula, the 3-D simulation under-predicts the first two modes by 8% and 3% and over-predicts the $3rd$ and $4th$ mode by 14% and 12% respectively. The 2nd mode frequency prediction is improved and accurate (in terms of the 5% error limit). The 3-D simulation is important for cavity sound pressure level and RMS pressure predictions. One possible cause for the unreasonably high SPL and RMS pressure predictions in the 2-D results is that in the 2-D domain after flow impingement on the rear wall the high acoustic energy is reflected back to the front wall without much lose creating and maintaining strong cavity flow oscillations. Detailed analyses (in the near future), such as turbulent intensity, shear layer velocity profile etc., should reveal the difference between 2-D and 3-D cavity flow simulations.

Modes	1 St	λ nd	2 rd	
Rossiter's formula	524 Hz	1223 Hz	1923 Hz	2622 Hz
2-D DES	560 Hz	1120 Hz	1682 Hz	2562 Hz
	150 dB	149 dB	140 dB	130 dB
3-D DES	469 Hz	1198 Hz	2057 Hz	2865 Hz
(coarse grid)	137 dB	136 dB	134 dB	128 dB

2.5.2 Fine grid

The fine grid was the 2-D grid stated in Section 2.4 and extended it along the *z* direction with 56 cells above the cavity from *z/D*=0 to 2, with the cavity located from *z/D*=0.5 to 1.5. The total cell number was 4.08×10^6 of which a total of 0.453×10^6 cells were inside the cavity. Therefore the fine grid case had 4 times the number of cells as the coarse grid. There were 72 computing blocks with 57x71x14 cells per block. Near the flat plate there were 19 cells from *y/D*=1 to 1.1 and 37 cells from *y/D*=1 to 1.3. The first cell was 0.0037*D* away from the plate. The numerical schemes and flow configurations used in the coarse grid case remained unchanged. In the stable flow oscillation stage, a typical time step was 3.3×10^{-8} sec which was the same as in the coarse grid case. A job of $3x10^4$ time steps took about 66 hours, which were equivalent to four jobs of the coarse grid case, on 36 processors of the Iridis2 computer and in the flow transient stage the fine grid used much smaller time steps resulting in a long waiting time for results.

Figure 2.5.2.1 shows the pressure history at the K29 position. The pressure oscillation level stabilizes after 0.028 *sec*. The pressure data at ten kulite transducer positions from K20 to K29 were recorded from 0.028 to 0.055 *sec*. To be consistent with the coarse grid case, the pressure data for a 0.021 *sec* record are analysed. One of FFT results and the RMS pressure distribution along the cavity ceiling are shown in Figures 2.5.2.2 and 2.5.2.3. The amplitudes of the 1st and 2nd modes are 139 and 138 *dB* respectively. Apart from the first two modes the $3rd$ and $4th$ modes are not easily identified due to short data length. Consistent with the SPL pattern at the K29 position, the modal RMS pressure pattern in the cavity ceiling reveals that the $1st$ mode is dominant over most of the cavity ceiling.

2.5.3 Comparison

A. RMS pattern and mode amplitudes and frequencies

Figure 2.5.3.1 shows that the RMS pressure predictions in both cases are almost the same with slightly higher values in the middle and rear corner of the cavity ceiling for the fine grid case. A similar modal RMS pressure pattern (Figure 2.5.2.4) to those of the coarse grid case

(Figure 2.5.1.4) is also observed. A detailed comparison of the mode predictions is listed in Table 2.5.3.1. The $1st$ mode amplitude is the same in both cases but the other three mode amplitudes are higher by 3, 2 and 2 dB respectively for the fine grid. The 2nd mode amplitude is now at the same level as the $1st$ mode. For mode frequency prediction, the fine grid case under predicts all four modes by 5%, 8%, 9% and 17% compared to the results of the Rossiter's formula. The modal frequency predictions in fine grid case are worse than the coarse grid case. The only improvement is in the $2nd$ mode amplitude prediction. It may be assumed that the fine grid resolution resolves the vortex structure in the shear layer and thus improves the prediction of the mode amplitudes especially the $2nd$ mode.

B. Near field SPL pattern, instantaneous pressure and Q criterion

Figures 2.5.3.2 and 2.5.3.3 show the near field SPL pattern. It is observed that the rear wall region experiences the most intensive pressure fluctuations owing to the frequent flow impingements. There is another SPL peak centred in the shear layer and the middle of the cavity illustrating the 2nd mode structure and the second intensive flow activity is in the shear layer. There is no clear difference in terms of the SPL pattern between the coarse and fine grid cases. As illustrated in Figures 2.5.3.4 and 2.5.3.5 the fine grid case gives clear pressure vortex structures in the shear layer. As the dominant $2nd$ mode is excited by the flow instability in the shear layer it is expected that this mode amplitude will be predicted better in the fine grid case. Current mode prediction shown in Table 3.5.3.1 seems to verify this.

Figure 2.5.3.2: Near field SPL (coarse grid). Figure 2.5.3.3: Near field SPL (fine grid).

Figure 2.5.3.4: Instantaneous pressure (coarse grid).

Figure 2.5.3.5: Instantaneous pressure (fine gird).

Figures 2.5.3.6 to 2.5.3.9 show the vortex structure through Q criterion [31] in the shear layer region. The fine grid case produces clearer vortex structures, such as small scale vortices in the shear layer. From Figures 2.5.3.8 and 2.5.3.9 the vortex structure variation along the *z* direction is small and smooth so that small vortices are produced along the *x-y* direction and propagate mainly in the streamwise direction. The smooth flow structures may be due to the coarse grids used in the *z* direction.

Figure 2.5.3.6: Q criterion (coarse grid). Figure 2.5.3.7: Q criterion (fine grid).

Figure 2.5.3.8: Q criterion (coarse grid). Figure 2.5.3.9: Q criterion (fine grid).

3. Far field Ffowcs Williams-Hawkings (FW-H) predictions

3.1 Implementation of a low storage FW-H solver

An advanced time method for aeroacoustic predictions has been proposed recently [22]. For the same FW-H formulation developed by Farassat and Succi [23] it has a different implementation compared with a traditional retarded time method [23]. The basic idea is that at a far field observer, acoustic signals emitted from each panel of an integration surface are predicted through an FW-H solver and are gathered at different observer time levels. For an observer at a certain time only part of the acoustic pressure contribution is received. An acoustic pressure prediction will be completed when all signals from the integration surface are received. Far field directivity is calculated at a final stage. As a result of [22], the FW-H solver can now be integrated in the CFD solver and works in a parallel computing environment to provide a far field acoustic pressure prediction in line with the CFD near field prediction. This method does not require hard disk storage and hence is called a low storage FW-H solver. The low storage FW-H solver is essential for far field aeroacoustic predictions in 3-D turbulent flow simulations since usage of hard disk storage would be excessive with previous approaches.

According to [22], acoustic pressure consists of thickness noise $p'_T(x,t)$, loading noise $p'_l(x,t)$ and quadrupole noise $p'_l(x,t)$:

$$
p'(x,t) = p'_{Q}(x,t) + p'_{L}(x,t) + p'_{T}(x,t)
$$
\n(3.1.1)

where

$$
4\pi p'_T(x,t) = \left[\frac{\rho_0 (\dot{U}_n + U_n)}{r(1 - M_r)^2} + \frac{\rho_0 U_n (r\dot{M}_r + c(M_r - M^2))}{r^2 (1 - M_r)^3} \right]_{adv} dS,
$$
(3.1.2)

$$
4\pi p'_L(x,t) = \left[\frac{\dot{L}_r}{cr(1-M_r)^2} + \frac{L_r - L_M}{r^2(1-M_r)^2} + \frac{L_r(r\dot{M}_r + c(M_r - M^2))}{cr^2(1-M_r)^3} \right]_{adv} dS,
$$
(3.1.3)

$$
4\pi p'_{Q}(x,t) = \left[\frac{K_1}{c^2 r} + \frac{K_2}{cr^2} + \frac{K_3}{r^3}\right]_{adv} dV.
$$
\n(3.1.4)

Details of those parameters can be found in [22]. Note that the quadrupole noise $p'_0(x,t)$ is not included in this solver. Values of the quadrupole noise $p'_{\mathcal{Q}}(x,t)$ are small as long as the integration surface is placed away from the strong flow non-linear interaction region (source region), such as free shear layer and viscous boundary layer. Equations (3.1.2) to (3.1.4) are similar to the retarded time formulations except that the surface integral is dropped since the formulation is for an individual panel while in the retarded time method it is for all panels. The advanced time is the time at which a disturbance emitted by a source element y at time t will reach the observer x . For a subsonic observer velocity it is,

$$
t_{adv} = t + \frac{1}{c} |x(t_{adv}) - y(t)| = t + \frac{r(t)}{c} \left[\frac{M_{or} + \sqrt{M_{or}^{2}(t) + 1 - M_{o}^{2}}}{1 - M_{o}^{2}} \right].
$$
 (3.1.5)

3.2 Code validations

Two validations were made. These were un-spinning (*m*=0) and spinning (*m*>0) acoustic mode propagations through an unflanged duct. The far field directivity results are shown in Figures 3.2.1 and 3.2.2. Details of the setup can be found in [16, 17] and are not repeated here. To obtain the far field results an oval-shaped 3-D integration surface is established to enclose the source region and near field acoustic data at each panel of the integration surface are collected in time by solving a 2.5D LEE. It should be noted that the low-storage FW-H solver is not suitable for the 2.5D LEE because the acoustic data at the each panel of the integration surface can not be obtained at same time level. Figure 3.2.2 shows that the solver is also correct for spinning-mode far field prediction if near field acoustic data at the integration surface are pre-collected. From both figures it is confirmed that the low storage FW-H solver has the same prediction accuracy as the high storage FW-H solver and matches the analytic solutions. There is no integration surface sensitivity for these two LEE cases since the integration surface is an enclosed surface so that no acoustic information is missed and there is no quadrupole noise included.

Figure 3.2.1: Far field directivity for mode (0, 1) (frequency *k*=23; *M*=-0.4, Inlet problem).

Figure 3.2.2: Far field directivity for mode (13, 1) (frequency *k*=23; *M*=-0.5, Inlet problem).

3.3 Open integration surface sensitivity

3.3.1 2-D open integration surface

For a 2-D open integration surface 3-D acoustic data are obtained through data duplication along the *z* direction. It was reported, on a circular cylinder test [24], that the length of the cylinder had a strong effect on peak noise level and peak amplitude prediction from a cylinder length of 10*D* was within 2 *dB* of the experiment. Therefore a 2-D Gaussian pulse case was established as a simplification of the cavity flow case to test the surface sensitivity. As shown in Figure 3.3.1.1 the rectangular computational domain was 20*D* long and 20*D* high. A uniform mesh was used, containing $478x478$ cells to ensure sufficient mesh resolution for monitored data (collected at 0.04 non-dimensional time intervals) to compare with the FW-H prediction. A slip-wall boundary condition was placed at the bottom of the block for the Euler equation simulation and a buffer zone condition, which had a zone width of 20 cell points, was applied at the other three sides to minimize wave reflections. Mean flow properties were taken to be standard: freestream temperature, density, velocity and reference length *D* were 288.16*K*, 1.225 kg/m^3 , 0 m/s and 1.0 *m* respectively. The initial Gaussian pulse had a strength of 141.86 *Pa* (0.001^{*} $\rho_{\infty}C_{\infty}^{2}$), and was located at *x*/*D*=9 and $y/D=2$. Positions of the integration surface and three observers are shown in Figure 3.3.1.1 and they are stationary. The disturbance pressure data are collected from these three positions in order to compare with the FW-H predictions.

Figure 3.3.1.1: Illustration of computational domain.

The computation used the Euler equations and $4th$ -order LDDRK temporal integration scheme, $6th$ -order spatial compact scheme and a $10th$ -order filter in every time step. Four processors were used to ensure correct parallel implementation. The non-dimensional time step was 0.02, corresponding to a CFL condition of 0.478, and the total time steps were 1800 steps. The history data at each panel of the integration surface, which had 200 panels, were collected at 0.04 non-dimensional time intervals. In the FW-H prediction an approximately 700 *MB* memory usage was used.

Figure 3.3.1.2 shows the comparison of FW-H predictions using different integration surface *z* lengths. In comparison to CAA results at the observer two shown in Figure 3.3.1.1, a *z*length of 20*D* gives most accurate prediction. It seems that the optimized z length is case dependant since an optimized 10*D z*-length is found in a circular cylinder case [24]. With a fixed *z-*length of 20*D*, shown in Figures 3.3.1.3 to 3.3.1.5, the three FW-H predictions seem smoother than the monitored CAA data. These inconsistencies can be visualized from Figures 3.3.1.6 to 3.3.1.9, which show that the wave reflections are formed at the pulse tails. Therefore the CAA result, which can be improved, is not as good as the FW-H prediction due to the narrow buffer zone width.

Figure 3.3.1.6: Gaussian pulse at *t*= 2*D/C*∞. Figure 3.3.1.7: Gaussian pulse at *t*=4 *D/C*∞.

Figure 3.3.1.8: Gaussian pulse at $t = 6 D/C_{\infty}$. Figure 3.3.1.9: Gaussian pulse at $t=8 D/C_{\infty}$.

In comparison with the high storage FW-H solver, this solver is efficient for non-periodic acoustic mode prediction and is part of a CFD flow field prediction procedure, which is user friendly. There is no need to calculate the time variation of the acoustic data as the CFD solver provides those values as well. However, since this solver is integrated into the main CFD solver, the integration surface has to be constructed before time integration, which may cause difficulty in verifying the effectiveness of the integration surfaces. Therefore in conducting integration surface sensitivity tests the high storage FW-H solver is preferred because it is a post-processing activity.

A sensitivity study of open integration surface placement for the 2-D Re_D =45000 cavity case has been conducted using the high storage FW-H solver. At first a *z*-length sensitivity test is established by comparing FW-H predictions with an observed SPL at a position inside the computational domain and the details are not presented here for sake of clarity. Figure 3.3.1.10 shows that the integration surface *z*-length of 7*D* or 25*D* is close to the monitored values. An extended near SPL field using the FW-H prediction together with a CFD SPL results is shown in Figure 3.3.1.11. The FW-H near field SPL peak prediction is close to the CFD values. A complete match is not expected as the stretched grid would damp high frequency noise components in coarser grid regions. As shown in Figures 3.3.1.12 and 3.3.1.13, four integration surfaces are constructed with an equal distance of 2.0*D* in the *y*

direction. The far field results at 100 *m* (centered at cavity rear edge shown in Figure 3.3.1.12) show that a consistent directivity pattern is observed at an observation angle $30<\varphi<69$ degrees, where φ is defined in Figure 3.3.1.12. The maximum SPL difference is 2 *dB*. The peak SPL value is within the area where the maximum relative difference is 1.6%. The peak SPL value is predicted at 64 degrees.

Figure 3.3.1.11: Comparison of near field SPL.

Figure 3.3.1.13: Far field FW-H predictions.

3.3.2 3-D open integration surface

For the 3-D cavity cases flow perturbation values at the integration surface outside the computation domain of *z/D*=0 to 2.0 are obtained through interpolation of the flow values inside the domain according to a periodic flow assumption in the z direction. The sensitivity study of the placement becomes difficult owing to the long integration time. Therefore to study the *z*-length effects three z-lengths are used in three cavity cases. Based on experience gained in the 2-D Gaussian pulse and the 2-D Re_D =45000 cavity cases, the lengths are chosen to be 18*D*, 30*D* and 37*D* for the 3-D M219 cavity, Re_D =45000 coarse grid and fine grid cavity cases respectively. Similar results are obtained for the near field FW-H predictions so that only one result from the M219 cavity case is shown. As shown in Figure 3.3.2.1 a perturbation pressure history is recorded from 0.2 to 0.5 *sec* at a monitoring position shown in Figure 3.3.1.12. The maximum perturbation pressure has a value of 900 *Pa*. The corresponding low storage FW-H prediction is also shown in Figure 3.3.2.2. The predicted time is actually out of the monitored time range so that both monitored and the predicted data are not able to be compared directly. Assuming the pressure has a similar pattern after 0.5 *sec* the predicted values are in a range of -1000 to 1000 *Pa*. However it is observed that high frequency components appear in the prediction. To verify this, two acoustic un-spinning mode computations are made. In the first case the low storage FW-H solver prediction starts from the beginning and in the second case three jobs are submitted with total time steps 10000 (0.08 *sec*), 2000 and 2000 steps respectively and the solver starts from the second job. The far field acoustic pressure predictions are shown in Figures 3.3.2.3 and 3.3.2.4. It is clear from Figure 3.3.2.3 that if starting from the beginning there are no high frequency components in the FW-H prediction and from Figure 3.3.2.4 that the high frequency components appear in the far field acoustic pressure history. This verifies that if the FW-H prediction starts at some stage of the computation, the observer would receive incomplete acoustic signals for a period of time, which would appear in the form of irregular and high frequency components. Figure 3.3.2.4 also confirms that once all signals are received the acoustic pressure at the observer will be regular with a correct amplitude prediction no matter how many jobs there are. From this validation it is concluded that current high frequency components in the cavity far field pressure histories are temporary phenomena and will disappear when the time integration progresses to a certain time. The whole time span depends on the first signal and last signal arriving on the observer.

Figure 3.3.2.3: FW-H prediction (0-0.8 *sec*).

Figure 3.3.2.4: FW-H prediction (0.08 to 0.11 *sec*).

Figure 3.3.2.5 shows the current far field directivity predictions, in which observers are located 100 *m* away from the cavity rear corner, for the 3-D M219 case. Two curves are shown. The first one is obtained from original pressure data and the second one is obtained from recovered pressure data in which modes are cut off if the FFT mode frequency is larger

than 3 *kHz*. It is observed that the high frequency components do not contribute to the SPL prediction significantly as there is a close match between truncated and non-truncated data from 15 to 110 degree angles. The predicted SPL level is exceptionally high with a maximum value of 156 *dB*, which is equivalent to a near field prediction. As addressed before the time schedule of this project does not leave room for completion of the simulation so that a correct far field FW-H prediction can be made. Although the SPL level prediction is not correct the directivity peak angle should be correctly predicted and it is 60 and 57 degrees for truncated and non-truncated data. Similar directivity patterns with peak angles near 60 degrees were observed from simulations [25-27], which confirm the result presented here. For the 3-D $Re_D=45000$ cases Figure 3.3.2.6 shows the far field directivity prediction comparison between the coarse and fine grids, with the high frequency components truncated after 3 *kHz*. The SPL level prediction has same problem as in the M219 case, showing the same transient period for the far field directivity prediction. Both coarse and fine grid cases predict a peak angle at 54 degrees which is 10 degree lower in comparison with the prediction of 64 degrees in the 2-D cases. Both cases are not significantly different in terms of directivity shape.

Figure 4.2.3.6: Far field directivity for *Re*_D=45000 cavity.

4. Liner and cavity flow oscillation control

An acoustic liner is implemented numerically as an impedance condition so that the solid wall becomes a 'soft' wall where the liner is placed. In the frequency domain, harmonic components of the surface pressure, \hat{p} , are related to a normal velocity component \hat{u} by an impedance *Z*,

$$
Z(\omega,\theta) = \hat{p}/\hat{u},\qquad(4.1)
$$

where ω is an angular frequency and θ is an incident angle. In reference [28], a reflective wave \hat{u}^- is related to a incident wave \hat{u}^+ by a parameter \hat{W} ,

$$
\hat{W} = \hat{u}^- / \hat{u}^+ = (1 - Z) / (1 + Z) \,. \tag{4.2}
$$

In the time domain, the convolution process is expressed as:

$$
u^{-}(t) = \int_{-\infty}^{+\infty} W(t-\tau)u^{+}(\tau)d\tau.
$$
 (4.3)

By defining a single frequency dependence,

$$
Z(\omega) = R_0 + i(X_{-1} / \omega + X_1 \omega),
$$
\n(4.4)

where resistance R_0 and reactance $X_{-1}/\omega + X_1 \omega$ can be measured through experiments and acoustic mass X_i and stiffness X_i can be calculated. Although in real flow situations, such as the cavity flow, the mode frequency is broadband, the single frequency expression is useful in determining the best frequency of a liner for noise reduction.

The chosen test case is a 2-D DES/S-A Re_D =45000 cavity flow case presented in Section 2.4. In this case a constant depth ceramic tubular liner is chosen, as its best frequency for noise reduction is 1.0 kHz and the cavity dominant mode is the $2nd$ mode with a frequency of 1.2 *kHz*. Since the cavity flow frequency is broadband, the broadband impedance condition with mean flow effects included [28] is implemented together with a single-frequency condition. Defining a parameter \hat{W} ,

$$
\overline{\hat{W}} = \hat{W} - 1 = \frac{2}{1 + Z} = \frac{2}{1 + R(\omega^2) + i\omega X(\omega^2)} = \frac{Q(i\omega)}{D(i\omega)},
$$
(4.5)

where *R* and *X* are the resistance and reactance respectively. If the denominator $D(i\omega)$ assumes form such as $(i\omega \lambda_1)$ $(i\omega \lambda_2)$... $(i\omega \lambda_m)$, the value of $\overline{\hat{W}}$ can be obtained from measured data. Detailed derivations can be found in [28] and are not repeated here.

The cavity flow oscillation is self-contained and is driven by a flow dynamic process (*i.e.* flow instability in the shear layer) and the cavity geometry. There have been a number of acoustic control studies. The methods used include porous surfaces, changing cavity leading/trailing edge shapes, blowing/sucking from holes and changing ventilations by placing an additional layer above the cavity ceiling. From the flow control point of view the

use of acoustic liners may not in itself achieve a great success, but may provide clues for better control. In the initial stage, the tests are designed to determine how successful the oscillation attenuation can be by using the impedance data (acoustic tube) available and finding a position on the cavity walls/ceilings where the noise attenuation can be effective. The dominant modes for this cavity flow are 1 to 3 which are in a range from 0.5 to 2.0 *kHz*. Therefore one impedance value corresponding to frequency from 1.0 *kHz* was used in a single-frequency test and six impedance values corresponding to frequencies from 0.5 to 3.0 *kHz* were used in the broadband-frequency test. Two liner positions were chosen as shown in Figure 4.1. One of the reasons for choosing these locations was that the rear wall region experiences the strongest pressure fluctuations and the cavity inner walls/ceilings as a whole act like a resonator. The first position (liner 1 case) was at the rear wall and the second (liner 2 case) was at all cavity inner walls/ceilings. The hard wall case was selected as a baseline configuration for comparison. In the analysis, only SPL data on the K29 position were used. The liner and baseline simulations used an existing flow solution and an integration time of 0.0106 *sec* which covered five periods of the 1st mode.

Figure 4.1: Liner positions in a 2-D cavity.

A. Broadband-frequency impedance

Three comparisons are performed: domain SPL pattern, mode FFT analyses and RMS pressure patterns. Figures 4.2 to 4.4 show the SPL patterns for the baseline and both liner cases. It can be observed that the liner 2 case has better cavity flow oscillation reduction in the near field since the area of large SPL value is obviously reduced to a small area close to the rear cavity wall in comparison with the baseline case. This indicates a reduced strength of acoustic feedback and weaker flow instability excitement in the free shear layer. The liner 1 case is less effective on the flow oscillation reduction because the acoustic treatment is only done at the rear wall and acoustic feedback from the ceiling and the front wall are not affected. In both cases the maximum SPL reduction is 1.3 *dB*.

Figure 4.2: Near field SPL: Baseline.

Figure 4.3: Near field SPL: liner 1.

Figure 4.4: Near field SPL: liner 2.

Figure 4.5 shows the mode amplitude results for both liner positions. Compared to the baseline case, in the liner 1 case the first three mode amplitudes are 153, 139 and 141 *dB* and the mode frequencies are 561, 1028 and 1401 *Hz* respectively. Mode frequencies are shifted from the baseline frequencies and at the baseline mode frequency positions the amplitudes are equivalent or higher for the $1st$ and $3rd$ modes and lower for the $2nd$ mode. Both mode frequencies and amplitudes are changed. For the liner 2 case (green line), these change are ever larger. Three amplitude peaks are 153, 151 and 143 *dB* at the frequencies of 374, 748 and 1122 *Hz* respectively. It is noticed that the 2nd mode amplitude is reduced in both cases indicating the liner's selective frequency response. The RMS pressure distribution along the cavity ceiling in Figure 5.6 shows a reduced flow oscillation in most parts of the cavity ceiling in both cases and the liner 1 case performs better than the liner 2 case for the RMS pressure reduction.

B. Further study of singe-frequency impedance at 1.0 *kHz*

The single-frequency impedance study is to find how much noise reduction can be achieved if the system responds to a single-frequency only. This is done numerically assuming a new liner, which has a characteristic of single-frequency response of 1.0 *kHz*.

Figure 4.7: Near-field SPL: Liner 1 case.

Figure 4.8: Near-field SPL: Liner 2 case.

The SPL patterns in Figures 4.7 and 4.8 suggest that both liner cases achieve some kind of SPL reduction. The line 2 has better effect with the maximum reduction of 3.0 *dB*. The high

SPL value area nearly disappears in the region close to the rear wall in the liner 2 case suggesting weaker cavity flow oscillations in comparison with the corresponding SPL pattern shown in Figure 4.7. In comparison with the broadband-frequency impedance results, the single-frequency impedance has a better noise attenuation effect.

 As observed from Figure 4.9, the pressure spectrum analysis shows that the mode amplitudes are reduced at frequencies less than 2.0 *kHz* for both liner cases. A better reduction is observed for the liner 2 case. In the liner 1 case the first two mode amplitude reductions are 2.0 and 3.0 *dB* and mode frequencies are shifted to 467 and 748 *Hz* from the original 561 and 1028 *Hz* respectively. In the liner 2 case, the first two mode amplitude reductions are 10.0, and 8.0 *dB* and mode frequencies are shifted to 281 and 748 *Hz* respectively. Although the liner only responds to a single-frequency of 1.0 *kHz*, the cavity flow field experiences a change in the broadband-frequency range, suggesting close relations between the Rossiter modes. The liner 2 case gives the most noise attenuation as the amplitude values (green line) drop significantly compared with the baseline case, showing that this liner placement has a significant disruptive effect on the acoustic feedback inside the cavity. Combined with the analysis from the broadband-frequency impedance test, the liner 2 configuration should have the best noise attenuation effect. Results shown in Figure 4.10 confirm this deduction. For the liner 2 case the RMS pressure level is apparently lower and the RMS pattern is almost reversed compared with the baseline case.

5. Conclusions

In this section three parts of the work are summarized. These are the near field cavity CFD simulations, the far field aeroacoustic predictions and the cavity flow oscillation control study via linered walls. Conclusions from analyses are listed below.

- A. Near field cavity CFD simulations
	- a) In the 2-D M219 cavity simulations the LES and DES models under-predict the Rossiter mode frequencies except for the 1st mode and over-predict the mode amplitudes. Compared with experiment at the K29 position the LES model has errors of $+11\%$, -8% , -16% and -13% for mode frequencies and $+19$, $+13$, $+9$ and $+8$ *dB* for mode amplitudes respectively. The DES model has relative mode errors of +16%, -8%, -9% and -11% for mode frequencies and +20, +13, +10 and +10 *dB* for mode amplitudes respectively. Results from both models are similar and mode frequency errors are all over the target 5% accuracy limit.
	- b) In the 3-D M219 LES cavity simulation, mode predictions in two identical time periods shows no apparent differences suggesting that the sample time is long enough. The LES model under-predicts the mode frequency in first three modes and the errors are -13%, -10%, -9% and +3% respectively. The LES over-predicts the mode amplitude and the errors are $+8$, $+2$, $+2$ and $+5$ *dB* respectively. Compared to the 2-D results the SPL improvements are 11, 9, 7 and 3 *dB* respectively. In comparison with the experimental data, reasonable predictions of the Rossiter modes are observed except for the $1st$ Rossiter mode amplitude. This departure from experimental results is consistent with other numerical simulations [3-5]. In this simulation it is also noticed that there is no sign of a SPL amplitude peak at 7 *kHz*.
	- c) In the 3-D M219 DES cavity simulation, the computing time was limited to 0.062 *sec*. Self-sustained flow oscillation starts but turbulent flow features, such as broadband modal frequencies, have not yet been established. The role of the $1st$ mode is predominant.

d) Summary

Modes	1 st	2 nd	3 rd	4 th
Rossiter's formula	159 Hz	371 Hz	582 Hz	794 Hz
Experiment	151 Hz	370 Hz	605 Hz	773 Hz
(0.1 sec)	156 dB	158 dB	155dB	144dB
2-D LES	167 Hz	341 Hz	506 Hz	675 Hz
	175 dB	171 dB	164 dB	152 dB
2-D DES	175 Hz	340 Hz	518 Hz	691 Hz
	176 dB	171 dB	165 dB	154 dB
3-D LES	131 Hz	332 Hz	553 Hz	794 Hz
	164 dB	160 dB	157 dB	149 dB
3-D DES	128 Hz	386 Hz	516 Hz	902 Hz
	175 dB	159 dB	147 dB	135 dB

Table 5.1: Summary of mode predictions for M219 cavity flow

- e) In a 2-D Re 45000 cavity DES simulations the $1st$ mode frequency is over-predicted by 4%, the $2nd$ to $4th$ mode frequencies are under-predicted by 8%, 12% and 3% respectively in comparison to the results of Rossiter's formula. The mode amplitude predictions are 152, 148, 140 and 130 *dB* respectively. Clearly an improvement on the dominant $2nd$ mode amplitude prediction is needed.
- f) In a 3-D Re 45000 cavity DES simulation, results from both the coarse and fine grids are compared. Four mode amplitude and frequency predictions (see Table 2.5.3.1) for both grids have no obvious differences. Amplitude reduction is significant compared with the 2-D prediction except the $4th$ mode. The $1st$ mode amplitude is over-predicted. Longer simulation time might help to improve the $1st$ mode prediction. In terms of mode and RMS pressure predictions there are no apparent differences for both grids indicating sufficient grid resolution. For turbulent flow structure in the shear layer and inside cavity the fine grid case seems better than the coarse one as it resolves smaller scale vortices.
- B. Far field aeroacoustic predictions
	- a) A low storage FW-H solver has been established and validated for both enclosed and 2-D open integration surfaces.
	- b) In a z-length sensitivity test for a 3-D integration surface, a *z*-length of 20*D* gives most accurate prediction in far field.
	- c) It was verified that if the FW-H prediction starts from middle of the computation, the observer would receive incomplete acoustic signals for a period of time, which would appear in the form of irregular and high frequency components. Therefore current high frequency components in the cavity far field pressure histories and high

SPL value in the FW-H far field prediction are temporary and will disappear once all acoustic signals are received.

- d) For the far field directivity the M219 cavity simulation predicts a peak angle from 57 to 60 degrees. In the $Re_D=45000$ cavity simulations on both fine and coarse grid cases predict a peak angle at 54 degrees which is 10 degrees lower in comparison with the prediction of the 2-D case. However there are no significant differences in terms of directivity shape.
- C. Cavity flow oscillation control study
	- a) The 2-D cavity noise attenuation studies by placing a liner on the inner cavity walls/ceilings show that the liner has a positive effect on the broadband noise reduction. The liner 2 case, in which a liner is placed in the cavity inner walls/ceilings, has the highest cavity flow oscillation reduction.

Two tasks remain incompleted. They are the 3-D M219 cavity flow DES simulation and its far field noise predictions. High computing cost, due to a fine grid to resolve near wall flow behaviors $(y^{\dagger} < 1)$ and high order accuracy of the SotonCAA code, and limited computing power are the cause. A high order implicit temporal scheme [29] was attempted but no computing time was saved when turbulent flows were involved. However the complete prediction tool for far field noise prediction was developed and validated, which is the one of main objectives of this project and the M219 cavity flow LES simulation was successful. Two low Reynolds number cavity flow cases were proposed, with other similar flow conditions to the M219 cavity. In these two cases broadband turbulence features are observed proving the SotonCAA code capability for transonic turbulent flow simulation.

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