# Joint Hybrid and Passive RIS-Assisted Beamforming for MmWave MIMO Systems Relying on Dynamically Configured Subarrays

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Abstract—Reconfigurable intelligent surface (RIS) assisted millimeter-wave (mmWave) communication systems relying on hybrid beamforming structures are capable of achieving high spectral efficiency at a low hardware complexity and low power consumption. In this paper, we propose an RIS-assisted mmWave point-to-point system relying on dynamically configured subarray connected hybrid beamforming structures. More explicitly, an energy-efficient analog beamformer relying on twin-resolution phase shifters is proposed. Then, we conceive a successive interference cancelation (SIC) based method for jointly designing the hybrid beamforming matrix of the base station (BS) and the passive beamforming matrix of the RIS. Specifically, the associated bandwidth-efficiency maximization problem is transformed into a series of sub-problems, where the sub-array of phase shifters and RIS elements are jointly optimized for maximizing each sub-array's rate. Furthermore, a greedy method is proposed for determining the phase shifter configuration of each sub-array. We then propose to update the RIS elements relying on a complex circle manifold (CCM)-based method. The proposed dynamic sub-connected structure as well as the proposed joint hybrid and passive beamforming method strikes an attractive trade-off between the bandwidth efficiency and power consumption. Our simulation results demonstrate the superiority of the proposed method compared to its traditional counterparts.

Index Terms-RIS, mmWave, hybrid beamforming, dynamic sub-connected structure.

#### I. Introduction

EXT-generation wireless communication systems tend to aim for Gigebit per and in the communication systems tend to aim for Gigabit-per-second data transmission rates [1]-[3] and millimeter-wave (mmWave) techniques are indeed capable of supporting such high data rates given their abundant bandwidth [4]-[7]. For compensating the high pathloss of mmWave signals, multi-input multi-output (MIMO) techniques are widely used [8]-[11]. For instance, beamforming is capable of achieving a high directional gain. However, due to the high directivity, beamformed mmWave signals can be easily blocked by obstacles [12]. As a remedy,

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reconfigurable intelligent surfaces (RISs) can be employed for reflecting the incident signals by intelligently tuning the passive elements embedded into their surfaces [12]-[21]. Note that full-duplex relaying is also capable of compensating the significant attenuation of mmWave signals [22]-[24]. It can also be employed for improving the system's converge without reducing the transmission rate [25]. However, compared to full-duplex relays, RIS does not need an active transmitter module and only reflects the received signals in a passive way, which incurs no transmit power consumption [15]. Moreover, full-duplex relays require sophisticated self-interference cancellation, while a RIS naturally operates in full-duplex mode without self-interference or without introducing extra thermal noise [26]–[28]. Moreover, since the mmWave channel exhibits a sparse channel impulse response (CIR), this may be readily exploited for reducing the complexity by hybrid beamforming structures at the base station (BS) [29]-[31]. Explicitly, upon appropriately designing the hybrid beamforming at the BS and the passive beamforming at the RIS, RIS-assisted mmWave communication systems exhibit excellent performance at low hardware cost and low power consumption.

# A. Literature overview

There is now quite a bit of literature on the joint active and passive beamforming design conceived for maximizing the system's bandwidth efficiency, where fully-digital structures are considered at the BS. The authors of [32]-[36] propose to jointly design the active and passive beamforming matrices of both RIS-assisted single-input single-output (SISO) and multiuser multi-input single-output (MU-MISO) systems. Specifically, Guo et al. [32] propose a fractional programming (FP)based framework for joint active and passive beamforming design, while Ma et al. [33] use FP for solving the bandwidthefficiency-maximization problem. As a further advance, Yan et al. [34] advocate a sample average approximation (SAA)based iterative algorithm for their passive beamforming design. Li et al. [35] exploit the characteristics of RIS elements in a wideband scenario and propose a Lagrangian multiplier based method for jointly designing the active and passive beamforming matrices. By contrast, Zhou et al. [36] conceive a pair of algorithms under the majorization-minimization (MM) algorithmic framework for maximizing the bandwidth efficiency of RIS-assisted multi-group multi-cast MISO systems. Furthermore, the authors of [37]–[40] focus their attention on RIS-assisted MIMO systems, where both the BS and the

user are equipped with multiple antennas. Specifically, Ning et al. [37] propose a sum-path-gain maximization (SPGM)based method for designing the passive beamforming matrix. As another valuable contribution, Zhang et al. [38] derive the closed-form solution of RIS beamforming and propose an alternating optimization (AO)-based method for jointly designing the fully-digital beamforming matrix and the RIS elements. To elaborate further, Pan et al. [39] propose a joint active and passive beamforming design for IRS-assisted simultaneous wireless information and power transfer (SWIP-T) systems, where they design the active beamforming by the classic Lagrangian multiplier method, while the passive beamforming is optimized by MM-based and complex circle manifold (CCM)-based methods. In a further treatise, Pan et al. [40] propose to jointly design the fully digital beamforming matrices at the BSs and the RIS elements for their RIS-assisted multi-cell systems, while Zhang et al. [41] exploit the FP for jointly designing the active and passive beamforming matrices of RIS-assisted cell-free MIMO systems.

Moreover, considering the hybrid beamforming structures at the BS, Ning *et al.* [45] propose a codebook-based beam training and hybrid beamforming design method for RIS-assisted multi-user MIMO systems. In their recent contribution, Wang *et al.* [12] minimize the Euclidean distance between the hybrid beamforming matrix and the optimal fully-digital solution derived by singular value decomposition (SVD), and they propose a manifold optimization (MO)-based passive beamforming method for RISs. Typically fully-connected hybrid beamforming structures are considered in most of the literatures. However, the hardware complexity of the fully-connected hybrid beamforming structure is relatively high.

The optimization of different metrics characterizing RIS-assisted systems were also considered. The total transmit power minimization problem was investigated in [15], [16], while the energy efficiency maximization problems of different RIS-assisted systems were considered in [46], [47]. Some authors considered the joint optimization of different performance metrics, or striking the best trade-off between bandwidth efficiency and energy efficiency [48]. Robust beamforming designs were considered in [49]–[55] in terms of different optimization targets, while the concept of simultaneously transmitting and reflecting RIS (STAR-RIS) was proposed in [56]. As a further evolution, the active RIS philosophy was proposed in [57], while a hybrid RIS structure was conceived in [58].

For hybrid beamforming, one of the important research objectives is to reduce both the hardware complexity and the power consumption of the analog beamformer by using low-resolution phase shifters. In this context, Sohrabi and Yu [59] propose an iterative hybrid beamforming algorithm for fully-connected hybrid structures having low-resolution phase shifters. They further extend the proposed method to wideband scenarios in [60]. As another state-of-the-art (SoA) contribution, Wang *et al.* [61] jointly design the beamformer and combiner relying on low-resolution phase shifters. Chen *et al.* [62] propose a hybrid beamforming matrix in conjunction with low-resolution phase shifters, where an iterative training-based method is proposed, which converges to the dominant

steering vectors that are aligned with the direction of the highest channel gain. As a further development, Li et al. [63] propose a Lagrangian multiplier combined with the penalty dual decomposition (PDD) method for designing a hybrid beamforming matrix realized by low-resolution phase shifters in wideband mmWave systems. By relying on both highand low-resolution phase shifters, in our recent work [42] we propose a fully-connected hybrid structure relying on twinresolution phase shifters, where we also conceive a dynamic hybrid beamforming method. However, the fully-connected analog beamformer suffers from high hardware complexity. For mitigating this problem, Gao et al. [43] conceive a pioneering sub-connected analog beamformer conceived with a successive interference cancelation (SIC) based hybrid beamforming method. As a beneficial evolution, Park et al. [44] propose a dynamic sub-connected analog beamformer, where the connection between the radio-frequency (RF) chains and all the phase shifters can be flexibly set by their greedy method. In Table I we boldly and explicitly contrast our contributions to the SoA, emphasizing that our goal is to develop RIS-assisted mmWave systems relying on a lowcomplexity and energy-efficient hybrid structure, harvesting a joint hybrid and passive beamforming design method.

#### B. Our contribution

Against this background, we propose a RIS-assisted pointto-point mmWave MIMO system relying on twin-resolution dynamic sub-connected hybrid beamforming structures. The detailed contributions of this paper are summarized as follows:

- 1) An energy-efficient and low-complexity dynamic subconnected analog beamformer realized by twin-resolution
  phase shifters is proposed, where half of the phase shifters
  in each sub-array are predefined to have high resolution,
  while others have low resolution. The connection between
  the twin-resolution phase shifters and the TAs in each
  sub-array can be flexibly determined according to the
  channel state information (CSI). The proposed analog
  beamformer has lower hardware complexity than the
  fully-connected analog beamformer of [42]. Moreover,
  it can strike a more attractive bandwidth efficiency vs.
  power consumption tradeoff than the conventional subconnected analog beamformer of [43].
- 2) We propose to maximize the bandwidth efficiency by jointly optimizing the hybrid beamforming at the BS and passive beamforming realized by the RIS elements. However, both the objective function (OF) and constant-modulus constraints imposed on each element of the analog beamforming matrix and on the RIS elements are non-convex, which makes the problem formulated challenging to solve. Inspired by the successive interference cancelation (SIC)-based algorithm, we first transform the bandwidth efficiency maximization problem into a series of sub-rate maximization problems, where the sub-array of phase shifters and RIS elements are jointly optimized. Then we propose a SIC-based joint hybrid and passive beamforming algorithm to solve them.
- For the hybrid beamforming design, the well-known SVD-based digital beamformer component is used. Then

	[12]	[32]	[38]	[42]	[43]	[44]	Proposed
Hybrid Beamforming	<b>√</b>			<b>√</b>	<b>√</b>	<b>√</b>	<b>√</b>
RIS	<b>√</b>	<b>√</b>	<b>√</b>				<b>√</b>
Fully-connected hybrid structure	<b>√</b>			<b>√</b>			
Sub-connected hybrid structure					<b>√</b>	<b>√</b>	<b>√</b>
Single-resolution phase shifters	<b>√</b>	<b>√</b>	<b>√</b>		<b>√</b>	<b>√</b>	

TABLE I
CONTRASTING OUR CONTRIBUTION TO THE LITERATURES

we design the analog beamformer component columnby-column by relying on SIC. During the design of each sub-array, we fix the RIS elements and regard the cascaded BS-RIS-user link as the effective channel. We propose a greedy method for solving the corresponding sub-problem.

Twin-resolution phase shifters

4) Having the designed sub-arrays, we propose to update the RIS elements based on CCM. Specifically, we maximize the upper bound of the bandwidth efficiency of the sub-arrays and RIS elements that have been obtained. Then, complex matrix transformations are adopted for transforming the reformulated problem into a tractable form. Then we exploit a CCM-based method for updating the passive beamforming matrix. Our simulation results demonstrate the superiority of the proposed method over its counterparts.

The remainder of this paper is organized as follows. In Section II, our downlink system model and channel model are introduced. In Section III, our twin-resolution dynamic sub-connected analog beamformer and problem formulation are presented. In Section IV, our proposed joint hybrid and passive beamforming design is introduced. In Section V, our numerical results are provided. Finally, our conclusions are drawn in Section VI.

Notation: Lower-case and upper-case boldface letters denote vectors and matrices, respectively;  $(\cdot)^*, (\cdot)^T, (\cdot)^H, (\cdot)^{-1}$  and  $(\cdot)^\dagger$  denote the conjugate, transpose, conjugate transpose, inverse and pseudo-inverse of a matrix, respectively;  $\operatorname{Tr}(\cdot)$  presents the trace function;  $\operatorname{diag}\left[a_1, a_2, \cdots, a_N\right]$  denotes a diagonal matrix with  $a_1, a_2, \cdots, a_N$  being the diagonal elements;  $\|\cdot\|_F$  denotes the Frobenius norm of a matrix; |a| is the absolute value of a scalar;  $|\mathbf{A}|$  is the determinant of a matrix;  $\mathbf{A}(i,:)$  and  $\mathbf{A}(:,j)$  represent the i-th row and j-th column of the matrix  $\mathbf{A}$ , respectively; The operator  $\circ$  represents the Hadamard product; Finally,  $\mathbf{I}_P$  denotes the identity matrix of size  $P \times P$ .

## II. DOWNLINK SYSTEM MODEL AND CHANNEL MODEL

In this section, we will introduce both the system model and channel model of our RIS-assisted point-to-point mmWave MIMO downlink system relying on twin-resolution dynamically reconfigurable sub-connected hybrid structures.

# A. RIS-assisted Point-to-point MmWave MIMO Downlink Model

As shown in Fig. 1, the BS communicates with the user through the reflected link (BS-RIS-user), since the direct link

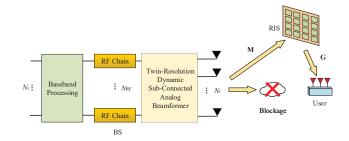


Fig. 1. Illustration of the RIS-assisted mmWave MIMO systems relying on twin-resolution dynamic sub-connected hybrid structure.

(BS-user) is assumed to be blocked. The BS is equipped with hybrid beamforming relying on  $N_t$  transmit antennas (TAs) and  $N_{\rm RF}$  RF chains. At the user, the fully-digital structure having  $N_r$  receive antennas (RAs) is adopted. The transmit signal at the BS has  $N_s$  data streams, which is defined as  $\mathbf{s} = [s_1, s_2, \cdots, s_{N_s}]^{\rm T} \in \mathbb{C}^{N_s \times 1}$  and has the normalized power of  $\mathbb{E}\left[\mathbf{s}\mathbf{s}^{\rm H}\right] = \mathbf{I}_{N_s}$ . At the BS, the transmit signals are firstly precoded by the baseband digital beamformer  $\mathbf{F}_{\rm BB} \in \mathbb{C}^{N_{\rm RF} \times N_s}$ . Without loss of generality, we assume  $N_s = N_{\rm RF}$  [43], [64]. Then the signals  $\mathbf{F}_{\rm BB}\mathbf{s}$  are precoded by the analog beamformer  $\mathbf{F}_{\rm RF} \in \mathbb{C}^{N_t \times N_{\rm RF}}$ , which will be introduced in detail in Section III-A. The phase shifters in the analog beamformer have the same amplitude of  $\frac{1}{\sqrt{M}}$  with  $M = \frac{N_t}{N_{\rm RF}}$  representing the number of phase shifters in each sub-array. Hence, we have

$$\mathbf{F}_{\mathrm{RF}} = \begin{bmatrix} \mathbf{f}_{\mathrm{RF},1} & \mathbf{0} & \cdots & \mathbf{0} \\ \mathbf{0} & \mathbf{f}_{\mathrm{RF},2} & \cdots & \mathbf{0} \\ \mathbf{0} & \mathbf{0} & \cdots & \mathbf{f}_{\mathrm{RF},N_{\mathrm{RF}}} \end{bmatrix},$$
 (1)

where  $\mathbf{f}_{\mathrm{RF},j} \in \mathbb{C}^{M \times 1}$  and  $\mathbf{f}_{\mathrm{RF},j}\left(i\right) = \frac{1}{\sqrt{M}}e^{j\theta_{i,j}}$  with  $\theta_{i,j}$  denoting the discrete phase shift caused by the limited-resolution phase shifters. The total transmit power constraint is set to  $\left\|\mathbf{F}_{\mathrm{RF}}\mathbf{F}_{\mathrm{BB}}\right\|_{\mathrm{F}}^2 = N_{\mathrm{RF}}$ . The transmitted signal after hybrid analog and digital beamforming is expressed by

$$\mathbf{x} = \sqrt{\frac{P_t}{N_s}} \mathbf{F}_{RF} \mathbf{F}_{BB} \mathbf{s}, \tag{2}$$

where  $P_t$  is the transmit power.

Then, the transmitted signals pass through the cascaded BS-RIS-user channel, which is defined as  $\mathbf{H}_{\mathrm{eff}} = \mathbf{G} \mathbf{\Phi} \mathbf{M}$ , where  $\mathbf{M} \in \mathbb{C}^{N_{\mathrm{RIS}} \times N_t}$  is the BS-RIS channel,  $\mathbf{G} \in \mathbb{C}^{N_r \times N_{\mathrm{RIS}}}$  is the RIS-user channel, and  $\mathbf{\Phi} = \mathrm{diag}\left[e^{j\phi_1}, e^{j\phi_2}, \cdots, e^{j\phi_{N_{\mathrm{RIS}}}}\right] \in \mathbb{C}^{N_{\mathrm{RIS}} \times N_{\mathrm{RIS}}}$  is the RIS matrix having  $N_{\mathrm{RIS}}$  passive elements. It is assumed that the channel state information (CSI) is

perfectly known at the BS, noting that both the accurate channel estimation and the robust joint hybrid and passive design relying on partial CSI constitute rather specific problems in RIS-assisted systems relying on dynamically configured subarrays [65]–[69]. Then the signal  $\mathbf{y} \in \mathbb{C}^{N_r \times 1}$  received by the user can be expressed as

$$\mathbf{y} = \sqrt{\frac{P_t}{N_s}} \mathbf{G} \mathbf{\Phi} \mathbf{M} \mathbf{F}_{RF} \mathbf{F}_{BB} \mathbf{s} + \mathbf{n}, \tag{3}$$

where  $\mathbf{n} \sim \mathcal{CN}\left(0, \sigma^2 \mathbf{I}_{N_r}\right) \in \mathbb{C}^{N_r \times 1}$  denotes the additive white Gaussian noise. We can further express the achievable bandwidth efficiency as [12]

$$R = \log_2 \left( \left| \mathbf{I}_{N_r} + \frac{P_t}{\sigma^2 N_s} \mathbf{G} \mathbf{\Phi} \mathbf{M} \mathbf{F}_{RF} \mathbf{F}_{BB} \cdot \mathbf{F}_{BF}^{H} \mathbf{F}_{RF}^{H} \mathbf{M}^{H} \mathbf{\Phi}^{H} \mathbf{G}^{H} \right| \right). \tag{4}$$

# B. Channel Model

In this paper, we adopt the multi-path mmWave channel model for both the BS-RIS channel M and the RIS-user channel G, which are defined by [29]

$$\mathbf{M} = \sqrt{\frac{N_t N_{\text{RIS}}}{L}} \sqrt{A_{\text{BR}}} \sum_{\ell=1}^{L} \alpha_{\ell} \mathbf{a}_{\text{RIS}} \left( \phi_{\ell}^{\text{r}}, \theta_{\ell}^{\text{r}} \right) \mathbf{a}_{\text{BS}}^{\text{H}} \left( \phi_{\ell}^{\text{t}}, \theta_{\ell}^{\text{t}} \right),$$
(5)

$$\mathbf{G} = \sqrt{\frac{N_{\mathrm{RIS}}N_r}{P}} \sqrt{A_{\mathrm{RU}}} \sum_{p=1}^{P} \beta_p \mathbf{a}_{\mathrm{MS}} \left(\phi_p^{\mathrm{r}}, \theta_p^{\mathrm{r}}\right) \mathbf{a}_{\mathrm{RIS}}^{\mathrm{H}} \left(\phi_p^{\mathrm{t}}, \theta_p^{\mathrm{t}}\right),$$
(6)

where L and P denote the total number of paths in the BS-RIS link and RIS-user link, respectively. Symbols  $A_{\rm BR}$  and  $A_{\rm RU}$  represent the path-loss in the BS-RIS link and RIS-user link, respectively. The variables  $\alpha_l, \beta_p \sim \mathcal{CN}\left(0,1\right)$  denote the complex gain in the BS-RIS link and RIS-user link, respectively. The variables  $\phi_\ell^t$  ( $\phi_\ell^{\rm r}$ ) and  $\theta_\ell^{\rm t}$  ( $\theta_\ell^{\rm r}$ ) are the azimuth and elevation angles of departure (arrival) associated with the BS-RIS link,  $\phi_p^{\rm t}$  ( $\phi_p^{\rm r}$ ) and  $\theta_p^{\rm t}$  ( $\theta_p^{\rm r}$ ) represent the azimuth and elevation angles of departure (arrival) associated with the RIS-user link. Vector  $\mathbf{a}_o, o \in \{\mathrm{BS}, \mathrm{RIS}, \mathrm{MS}\}$  stands for the beam steering vectors at the BS, the RIS or the user. Uniform planar arrays (UPAs) of antennas are employed at the BS, the RIS and the user. Thus, the typical beam steering vector of UPA antennas can be expressed by

$$\mathbf{a}_{o}\left(\phi,\theta\right) = \frac{1}{\sqrt{WH}} \left[ 1, \cdots, e^{j\frac{2\pi}{\lambda}d(m\sin\phi\sin\theta + n\cos\theta)}, \cdots, e^{j\frac{2\pi}{\lambda}d((W-1)\sin\phi\sin\theta + (H-1)\cos\theta)} \right]^{\mathrm{T}}, \tag{7}$$

where  $m \in \{0, 1, \dots, W-1\}$  and  $n \in \{0, 1, \dots, H-1\}$  with W and H denoting the number of antennas in the horizontal and vertical directions.

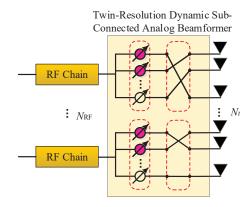


Fig. 2. Illustration of the proposed twin-resolution dynamic sub-connected analog beamformer.

# III. PROPOSED TWIN-RESOLUTION DYNAMIC SUB-CONNECTED ANALOG BEAMFORMER AND PROBLEM FORMULATION

In this section, we will firstly introduce the structure of our twin-resolution dynamically reconfigurable sub-connected analog beamformer, followed by the associated optimization problem formulation.

# A. Proposed Twin-Resolution Dynamic Sub-Connected Analog Beamformer

As illustrated in Fig. 2, we propose a twin-resolution dynamic sub-connected analog beamformer realized by twinresolution phase shifters. Specifically, we predefine half of the phase shifters in each sub-array as high-resolution ones (depicted as solid circles in Fig. 2), while the others as low-resolution ones (depicted as hollow circles in Fig. 2). Therefore, the number of high-resolution and low-resolution phase shifters in each sub-array is  $N_{\rm H}=N_{\rm L}=\frac{M}{2}$ . For achieving near-optimal performance, the connection between the M phase shifters having different resolutions and MTAs can be flexibly designed through switches according to the CSI. The phase shifter connected to the m-th TA in the j-th sub-array corresponds to the m-th element in  $\mathbf{f}_{RF,j}$ . By beneficially selecting the resolution of the phase shifter connected to each TA and designing the phase of the selected high-resolution or low-resolution phase shifter, we arrive at an attractive analog beamformer design. This procedure will be detailed in Section III-C.

The novelty of the proposed twin-resolution dynamic subconnected analog beamformer lies in two aspects. Firstly, compared to our recently proposed twin-resolution fully-connected analog beamformer [42], the twin-resolution dynamic subconnected analog beamformer has lower hardware complexity. Specifically, the total number of switches required for the hybrid beamformer is  $\left(\frac{N_t}{N_{\rm RF}}\right)^2 N_{\rm RF} = \frac{N_t^2}{N_{\rm RF}}$  in the proposed analog beamformer component. This is significantly lower than that of a twin-resolution fully-connected analog beamformer, which is  $N_t^2 N_{\rm RF}$ , especially when the number of

RF chains is large. Secondly, compared to the classical subconnected analog beamformer of [43], our proposed scheme is more energy efficient and can strike an attractive bandwidth efficiency vs. energy efficiency trade-off, since the highresolution phase shifters can attain a high beamforming gain, while the low-resolution phase shifters deployed in the analog beamformer dissipate much less energy.

#### B. Problem Formulation

In this paper, we propose to jointly optimize the hybrid beamforming matrix at the BS and the passive beamforming at the RIS for achieving the maximum bandwidth efficiency. The achievable bandwidth-efficiency maximization problem is formulated as

$$\max_{\mathbf{F}_{\mathrm{RF}}, \mathbf{F}_{\mathrm{BB}}, \mathbf{\Phi}} \qquad \qquad R \tag{8a}$$

$$|\mathbf{f}_{\mathrm{RF},j}\left(i\right)| = \frac{1}{\sqrt{M}},$$

$$\forall i = 1, 2, \cdots, M, \forall j = 1, 2, \cdots, N_{\mathrm{RF}} \quad (8c)$$

$$\theta_{i,j} \in \mathcal{Q}_{\mathrm{H}} \text{ or } \mathcal{Q}_{\mathrm{L}},$$

$$\forall i = 1, 2, \cdots, M, \forall j = 1, 2, \cdots, N_{\mathrm{RF}}$$
 (8d)

$$N_{\rm H} = N_{\rm L} = \frac{M}{2}$$
 (8e)  
 $\Phi = {\rm diag} \left[ e^{j\phi_1}, e^{j\phi_2}, \cdots, e^{j\phi_{N_{\rm RIS}}} \right]$ . (8f)

$$\mathbf{\Phi} = \operatorname{diag}\left[e^{j\phi_1}, e^{j\phi_2}, \cdots, e^{j\phi_{N_{\text{RIS}}}}\right]. \tag{8f}$$

We observe that problem (8) is a non-convex optimization problem due to the constant-modulus constraints (8c) and (8f). Moreover, the hybrid beamforming matrix  $\mathbf{F}_{\mathrm{RF}}\mathbf{F}_{\mathrm{BB}}$  and passive beamforming matrix  $\Phi$  are highly coupled with each other, which makes this problem quite challenging to solve. Hence we will propose a SIC-based joint design method for solving this problem.

#### C. Sub-Problem Formulation

Inspired by the SIC scheme of [43], we first derive the subproblem for each sub-array. Specifically, the objective function (OF) of (8a) is rewritten as

$$R = \log_2 \left( \left| \mathbf{I}_{N_r} + \frac{P_t}{\sigma^2 N_s} \mathbf{H}_{\text{eff}} \mathbf{F}_{\text{RF}} \mathbf{F}_{\text{BB}} \mathbf{F}_{\text{BB}}^{\text{H}} \mathbf{F}_{\text{RF}}^{\text{H}} \mathbf{H}_{\text{eff}}^{\text{H}} \right| \right),$$
(9)

where  $\mathbf{H}_{\mathrm{eff}} = \mathbf{G} \mathbf{\Phi} \mathbf{M}$  denotes the effective channel matrix. Then we calculate the digital precoding matrix  $\mathbf{F}_{\mathrm{BB}}=$  $\delta\left(\mathbf{F}_{\mathrm{RF}}^{\mathrm{H}}\mathbf{F}_{\mathrm{RF}}\right)^{-\frac{1}{2}}\mathbf{V}_{\mathrm{eff}}$ , where  $\mathbf{V}_{\mathrm{eff}}$  represents the first  $N_{\mathrm{RF}}$  right singular vectors of  $\mathbf{H}_{\mathrm{eff}}\mathbf{F}_{\mathrm{RF}}$ , and  $\delta=\sqrt{\frac{N_s}{\|\mathbf{F}_{\mathrm{RF}}\mathbf{F}_{\mathrm{BB}}\|_{\mathrm{F}}^2}}$ is a coefficient used for satisfying the total transmit power constraint [70]. Substituting  $\mathbf{F}_{BB}$  into  $\delta$ , we have  $\delta = 1$ . Then, we rewrite the analog beamforming matrix as

$$\mathbf{F}_{\mathrm{RF}} = \begin{bmatrix} \mathbf{F}_{\mathrm{RF},1} & \mathbf{F}_{\mathrm{RF},2} & \cdots & \mathbf{F}_{\mathrm{RF},N_{\mathrm{RF}}} \end{bmatrix}$$

$$= \begin{bmatrix} \mathbf{f}_{\mathrm{RF},1} & \mathbf{0} & \cdots & \mathbf{0} \\ \mathbf{0} & \mathbf{f}_{\mathrm{RF},2} & \cdots & \mathbf{0} \\ \mathbf{0} & \mathbf{0} & \cdots & \mathbf{f}_{\mathrm{RF},N_{\mathrm{RF}}} \end{bmatrix}. \tag{10}$$

After some mathematical transformations, we can equivalently rewrite (9) as [43]

$$R = \sum_{j=1}^{N_{\text{RF}}} \log_2 \left( \left| 1 + \frac{P_t}{\sigma^2 N_s} \mathbf{F}_{\text{RF},j}^{\text{H}} \mathbf{H}_{\text{eff}}^{\text{H}} \mathbf{T}_j^{-1} \mathbf{H}_{\text{eff}} \mathbf{F}_{\text{RF},j} \right| \right),$$
(11)

where  $\mathbf{T}_1 = \mathbf{I}_{N_r}$ ,  $\mathbf{T}_j = \mathbf{I}_{N_r} + \frac{P_t}{\sigma^2 N_s} \mathbf{H}_{\mathrm{eff}} \overline{\mathbf{F}}_{\mathrm{RF},j-1} \overline{\mathbf{F}}_{\mathrm{RF},j-1}^{\mathrm{H}} \mathbf{H}_{\mathrm{eff}}^{\mathrm{H}}$  for  $j \geq 2$ , and  $\overline{\mathbf{F}}_{\mathrm{RF},j-1} \in \mathbb{C}^{N_t \times (j-1)}$  is composed of the first j-1 columns of  $\mathbf{F}_{RF}$  [43].

In this paper, we propose to update the passive beamforming matrix  $\Phi$  after the design of each sub-array. Thus, we define the matrix  $\Phi$  obtained by the CCM-based method after the design of the j-th sub-array as  $\Phi_j$ . We can arrive at the final  $\mathbf{\Phi} = \mathbf{\Phi}_{N_{\mathrm{RF}}}$  after the design of the last sub-array, which is shared by all RF chains. Hence the effective channel in each sub-problem is  $\mathbf{H}_{\mathrm{eff},j} = \mathbf{G}\mathbf{\Phi}_{j-1}\mathbf{M}$  with  $\mathbf{\Phi}_{j-1}$  denoting the passive beamforming matrix obtained according to the design of the previous sub-arrays. Furthermore, we can divide problem (8) into  $N_{RF}$  sub-problems, where the j-th subproblem  $(j = 1, 2, \dots, N_{RF})$  is formulated as

$$\max_{\mathbf{f}_{\mathrm{RF},j},\mathbf{\Phi}_{j}} \log_{2} \left( \left| 1 + \frac{P_{t}}{\sigma^{2} N_{s}} \mathbf{f}_{\mathrm{RF},j}^{\mathrm{H}} \mathbf{B}_{j} \mathbf{f}_{\mathrm{RF},j} \right| \right)$$
(12a)

s.t. 
$$|\mathbf{f}_{\text{RF},j}(i)| = \frac{1}{\sqrt{M}}, \forall i = 1, 2, \dots, M$$
 (12b)

$$\theta_{i,j} \in \mathcal{Q}_{H} \text{ or } \mathcal{Q}_{L}, \forall i = 1, 2, \cdots, M$$
 (12c)

$$N_{\rm H} = N_{\rm L} = \frac{M}{2} \tag{12d}$$

$$\mathbf{\Phi}_{j} = \operatorname{diag}\left[e^{j\phi_{1}}, e^{j\phi_{2}}, \cdots, e^{j\phi_{N_{\mathrm{RIS}}}}\right], \quad (12e)$$

where  $\mathbf{B}_i \in \mathbb{C}^{M \times M}$  is composed of the rows and columns of  $\mathbf{H}_{\mathrm{eff},j}^{\mathrm{H}}\overline{\mathbf{T}}_{j}^{-1}\mathbf{H}_{\mathrm{eff},j}$  from the (M(j-1)+1)-st one to the (Mj)-th one,  $\overline{\mathbf{T}}_{1}=\mathbf{I}_{N_{r}}, \overline{\mathbf{T}}_{j}=\mathbf{I}_{N_{r}}+\frac{P_{t}}{\sigma^{2}N_{s}}\mathbf{H}_{\mathrm{eff},j}\overline{\mathbf{F}}_{\mathrm{RF},j-1}\overline{\mathbf{F}}_{\mathrm{RF},j-1}^{\mathrm{H}}\mathbf{H}_{\mathrm{eff},j}^{\mathrm{H}}$  for  $j\geq 2$ .

According to Problem (12), we observe that the bandwidth efficiency maximization problem can be transformed into a series of sub-rate maximization problems, each of which is for a specific sub-array. Then we optimize the sub-problems one by one [43]. Note that the specific order of the design has no influence on the bandwidth efficiency, which is determined by the sum of the sub-rates of all sub-arrays. By relying on an SIC scheme, we maximize the sub-rate of the first sub-array by jointly designing the twin-resolution phase shifters and the RIS elements. Then we obtain  $\mathbf{f}_{\mathrm{RF},1}$  and  $\mathbf{\Phi}_1$  for updating the matrix  $B_2$ , followed by similar procedures for the subsequent design steps, optimizing the sub-rate of the remaining subarrays one by one, until the last sub-array is considered.

# IV. PROPOSED JOINT HYBRID AND PASSIVE BEAMFORMING DESIGN

In this section, we will propose solutions to problem (12) obtained by a SIC-based joint design method.

# A. Greedy Method Proposed for Hybrid Beamforming Design

Relying on SIC, we design the analog beamformer  $\mathbf{F}_{\mathrm{RF}}$ column-by-column. For designing the j-th column  $\mathbf{F}_{\mathrm{RF},i}$  of  $\mathbf{F}_{\mathrm{RF}}$ , we assume a fixed passive beamforming matrix  $\mathbf{\Phi}_{j-1}$ . Problem (12) can be reformulated as

$$\max_{\mathbf{f}_{\mathrm{RF},j}} \log_2 \left( \left| 1 + \frac{P_t}{\sigma^2 N_s} \mathbf{f}_{\mathrm{RF},j}^{\mathrm{H}} \mathbf{B}_j \mathbf{f}_{\mathrm{RF},j} \right| \right)$$
(13a)

$$s.t.$$
  $|\mathbf{f}_{RF,j}(i)| = \frac{1}{\sqrt{M}}, \forall i = 1, 2, \cdots, M$  (13b)

$$\theta_{i,j} \in \mathcal{Q}_{H} \text{ or } \mathcal{Q}_{L}, \forall i = 1, 2, \cdots, M$$
 (13c)

$$N_{\rm H} = N_{\rm L} = \frac{M}{2}.\tag{13d}$$

Note that the conventional phase shifter design in the subconnected structure of [43] and in the twin-resolution fullyconnected structure of [42] are not suitable for the proposed twin-resolution dynamically sub-connected solution. Therefore, we propose a greedy method for determining the connections between the twin-resolution phase shifters and TAs in each sub-array. The initialization of  $\mathbf{f}_{\mathrm{RF},j}$  is set to  $\mathbf{f}_{RF,j} = \frac{1}{\sqrt{M}} e^{j \operatorname{angle}(\mathbf{v}_j)}$  [43], where  $\mathbf{v}_j$  is the first right singular vector of  $\mathbf{B}_{j}$ . We also initialize two counters  $c_{\rm H} = c_{\rm L} = 0$  for counting the number of twin-resolution phase shifters that have been connected to TAs. We define the set of discrete phases for the high-resolution and low-resolution phase shifters as  $Q_H$  and  $Q_L$ , respectively. Then we calculate  $q_{\mathrm{L}}\left(i\right) = \min_{q \in Q_{\mathrm{L}}}\left|\theta_{i,j} - Q_{\mathrm{L}}\left\{q\right\}\right|$  and  $q_{\rm H}\left(i\right) = \min_{q \in Q_{\rm H}} |\theta_{i,j} - Q_{\rm H}\left\{q\right\}| \text{ for } \forall i \in \mathcal{S}_{j}, \text{ where}$  $S_i = \{1, 2, \cdots, M\}$  is defined as the index set of TAs in the j-th sub-array. This step is used for obtaining the quantization errors for all elements in  $f_{RF,j}$ . Subsequently, we denote the indices of the element in  $\mathbf{f}_{\mathrm{RF},j}$  having the minimal quantization error for the high-resolution and lowresolution phase shifters as  $i_{L} = \min_{i \in S_{i}} |\theta_{i,j} - Q_{L} \{q_{L}(i)\}|$ and  $i_{H} = \min_{i \in \mathcal{S}_{j}} |\theta_{i,j} - Q_{H} \{q_{H}(i)\}|$  for  $\forall i \in \mathcal{S}_{j}$ . We check the relationship between  $|\theta_{i_{\rm L},j} - Q_{\rm L} \{q_{\rm L}(i_{\rm L})\}|$  and  $|\theta_{i_{\rm H},j} - Q_{\rm H} \{q_{\rm H}(i_{\rm H})\}|$  and determine the connection between a specific TA and a phase shifter as follows.

Case 1: If  $|\theta_{i_{\rm L},j}-Q_{\rm L}\left\{q_{\rm L}\left(i_{\rm L}\right)\right\}|<|\theta_{i_{\rm H},j}-Q_{\rm H}\left\{q_{\rm H}\left(i_{\rm H}\right)\right\}|$  and  $c_{\rm L}<\frac{M}{2}$ , we connect the  $i_{\rm L}$ -th TA in the j-th sub-array to a low-resolution phase shifter and set  $\mathbf{f}_{{\rm RF},j}\left(i_{\rm L}\right)=\frac{1}{\sqrt{M}}e^{jQ_{\rm L}\left\{q_{\rm L}\left(i_{\rm L}\right)\right\}}.$  We update  $c_{\rm L}=c_{\rm L}+1$  and  $\mathcal{S}_{j}=\mathcal{S}_{j}\setminus\{i_{\rm L}\}.$  When  $c_{\rm L}=\frac{M}{2},$  we connect the  $i_{\rm H}$ -th TA in the j-th sub-array to a high-resolution phase shifter and set  $\mathbf{f}_{{\rm RF},j}\left(i_{\rm H}\right)=\frac{1}{\sqrt{M}}e^{jQ_{\rm H}\left\{q_{\rm H}\left(i_{\rm H}\right)\right\}}.$  Similarly, we update  $c_{\rm H}=c_{\rm H}+1$  and  $\mathcal{S}_{j}=\mathcal{S}_{j}\setminus\{i_{\rm H}\}.$ 

Case 2: If  $|\theta_{i_{\rm L},j} - Q_{\rm L}\{q_{\rm L}(i_{\rm L})\}| \geq |\theta_{i_{\rm H},j} - Q_{\rm H}\{q_{\rm H}(i_{\rm H})\}|$  and  $c_{\rm H} < \frac{M}{2}$ , the  $i_{\rm H}$ -th TA in the j-th subarray is connected to a high-resolution phase shifter and set  ${\bf f}_{{\rm RF},j}(i_{\rm H}) = \frac{1}{\sqrt{M}}e^{jQ_{\rm H}\{q_{\rm H}(i_{\rm H})\}}$ . We update  $c_{\rm H} = c_{\rm H} + 1$  and  $\mathcal{S}_j = \mathcal{S}_j \setminus \{i_{\rm H}\}$ . When  $c_{\rm H} = \frac{M}{2}$ , the  $i_{\rm L}$ -th TA in the j-th sub-array is connected to a low-resolution phase shifter and  ${\bf f}_{{\rm RF},j}(i_{\rm L})$  is set to  ${\bf f}_{{\rm RF},j}(i_{\rm L}) = \frac{1}{\sqrt{M}}e^{jQ_{\rm L}\{q_{\rm L}(i_{\rm L})\}}$ . We update  $c_{\rm L} = c_{\rm L} + 1$  and  $\mathcal{S}_j = \mathcal{S}_j \setminus \{i_{\rm L}\}$ .

For the subsequent design of the j-th sub-array in the twin-resolution dynamic sub-connected analog beamformer, we embark on further derivation of the OF (12a). An element-

wise decomposition is given by

$$\log_{2}\left(\left|1+\frac{P_{t}}{\sigma^{2}N_{s}}\mathbf{f}_{RF,j}^{H}\mathbf{B}_{j}\mathbf{f}_{RF,j}\right|\right)$$

$$=\log_{2}\left(\left|1+\mathbf{f}_{RF,j}^{H}\overline{\mathbf{B}}_{j}\mathbf{f}_{RF,j}\right|\right)$$

$$=\log_{2}\left(\left|1+\mathbf{f}_{RF,j}^{*}\left(i\right)\sum_{m\neq i}^{M}\mathbf{f}_{RF,j}\left(m\right)\overline{\mathbf{B}}_{j}\left(i,m\right)\right.\right.$$

$$+\mathbf{f}_{RF,j}\left(i\right)\sum_{n\neq i}^{M}\mathbf{f}_{RF,j}^{*}\left(n\right)\overline{\mathbf{B}}_{j}\left(n,i\right)$$

$$+\sum_{n\neq i}^{M}\mathbf{f}_{RF,j}^{*}\left(n\right)\sum_{m\neq i}^{M}\mathbf{f}_{RF,j}\left(m\right)\overline{\mathbf{B}}_{j}\left(n,m\right)+\frac{1}{M}\overline{\mathbf{B}}_{j}\left(i,i\right)\right|\right)$$

$$=\log_{2}\left(\left|1+\Re\left\{e^{-j\theta_{i,j}}\sum_{m\neq i}^{M}e^{j\theta_{m,j}}\overline{\mathbf{B}}_{j}\left(i,m\right)\right\}\right.$$

$$+\sum_{n\neq i}^{M}e^{-j\theta_{n,j}}\sum_{m\neq i}^{M}e^{j\theta_{m,j}}\overline{\mathbf{B}}_{j}\left(n,m\right)+\frac{1}{M}\overline{\mathbf{B}}_{j}\left(i,i\right)\right|\right),$$
(14)

where  $\overline{\mathbf{B}}_{j} = \frac{P_{t}}{\sigma^{2}N_{s}}\mathbf{B}_{j}$ . Therefore, for maximizing (14), we update  $\mathbf{f}_{\mathrm{RF},j}\left(i\right)$  for  $\forall i\in\mathcal{S}_{j}$  as

$$\mathbf{f}_{\mathrm{RF},j}\left(i\right) = \frac{1}{\sqrt{M}} \frac{\sum_{m \neq i}^{M} e^{j\theta_{m,j}} \overline{\mathbf{B}}_{j}\left(i,m\right)}{\left|\sum_{m \neq i}^{M} e^{j\theta_{m,j}} \overline{\mathbf{B}}_{j}\left(i,m\right)\right|}.$$
 (15)

Afterwards, we repeat the aforementioned joint connection and phase design method for determining the next element in  $\mathbf{f}_{\mathrm{RF},j}$ . By repeating the update of  $\mathbf{f}_{\mathrm{RF},j}$  (i) for  $\forall i \in \mathcal{S}_j$  via (15) and the corresponding connection design, we are able to accomplish the design for all elements in  $\mathbf{f}_{\mathrm{RF},j}$ . When  $c_{\mathrm{H}} = c_{\mathrm{L}} = \frac{M}{2}$ , the design of the j-th sub-array in the twin-resolution dynamic sub-connected analog beamformer is deemed to be accomplished. Then we have  $\overline{\mathbf{F}}_{\mathrm{RF},j} = [\overline{\mathbf{F}}_{\mathrm{RF},j-1} \ \mathbf{F}_{\mathrm{RF},j}]$ . Note that the proposed greedy method can also be invoked for deriving either an entirely high-resolution or low-resolution sub-connected analog beamformer by setting  $N_{\mathrm{L}} = 0$  or  $N_{\mathrm{H}} = 0$ . The greedy method is summarized at a glance in Algorithm 1.

# B. CCM-based Method Proposed for Passive Beamforming Design

Following the design of the first j sub-arrays, we proceed with the design of the passive beamforming matrix  $\Phi_j$  and update the effective channel  $\mathbf{H}_{\mathrm{eff},j+1}$  for designing the remaining sub-arrays. We regard  $\mathbf{G}\Phi_j\mathbf{M}\overline{\mathbf{F}}_{\mathrm{RF},j}$  as the equivalent channel matrix [71] and formulate the passive beamforming optimization problem by

$$\max_{\mathbf{\Phi}_{j}} \quad \log_{2} \left( \left| \mathbf{I}_{N_{r}} + \frac{P_{t}}{\sigma^{2} j} \mathbf{G} \mathbf{\Phi}_{j} \mathbf{M} \overline{\mathbf{F}}_{\mathrm{RF}, j} \overline{\mathbf{F}}_{\mathrm{RF}, j}^{\mathrm{H}} \mathbf{M}^{\mathrm{H}} \mathbf{\Phi}_{j}^{\mathrm{H}} \mathbf{G}^{\mathrm{H}} \right| \right)$$
(16a)

s.t. 
$$\Phi_j = \operatorname{diag}\left[e^{j\phi_1}, e^{j\phi_2}, \cdots, e^{j\phi_{N_{\text{RIS}}}}\right],$$
 (16b)

$$\begin{aligned} & \left\| \mathbf{G} \mathbf{\Phi}_{j} \mathbf{M} \overline{\mathbf{F}}_{\mathrm{RF},j} \right\|_{\mathrm{F}}^{2} \\ &= \mathrm{Tr} \left( \mathbf{G} \mathbf{\Phi}_{j} \mathbf{M} \overline{\mathbf{F}}_{\mathrm{RF},j} \overline{\mathbf{F}}_{\mathrm{RF},j}^{\mathrm{H}} \mathbf{M}^{\mathrm{H}} \mathbf{\Phi}_{j}^{\mathrm{H}} \mathbf{G}^{\mathrm{H}} \right) \\ &= \mathrm{Tr} \left( \begin{bmatrix} \boldsymbol{\phi}_{j}^{\mathrm{H}} & \mathbf{0} & \cdots & \mathbf{0} \\ \mathbf{0} & \boldsymbol{\phi}_{j}^{\mathrm{H}} & \cdots & \mathbf{0} \\ \mathbf{0} & \mathbf{0} & \cdots & \boldsymbol{\phi}_{j}^{\mathrm{H}} \end{bmatrix} \begin{bmatrix} \overline{\mathbf{M}}_{1}^{\mathrm{H}} \mathbf{G}^{\mathrm{H}} \\ \overline{\mathbf{M}}_{2}^{\mathrm{H}} \mathbf{G}^{\mathrm{H}} \\ \vdots \\ \overline{\mathbf{M}}_{j}^{\mathrm{H}} \mathbf{G}^{\mathrm{H}} \end{bmatrix} \left[ \mathbf{G} \overline{\mathbf{M}}_{1} & \mathbf{G} \overline{\mathbf{M}}_{2} & \cdots & \mathbf{G} \overline{\mathbf{M}}_{j} \end{bmatrix} \begin{bmatrix} \boldsymbol{\phi}_{j} & \mathbf{0} & \cdots & \mathbf{0} \\ \mathbf{0} & \boldsymbol{\phi}_{j} & \cdots & \mathbf{0} \\ \mathbf{0} & \mathbf{0} & \cdots & \boldsymbol{\phi}_{j} \end{bmatrix} \right) \\ &= \mathrm{Tr} \left( \begin{bmatrix} \boldsymbol{\phi}_{j}^{\mathrm{H}} \overline{\mathbf{M}}_{1}^{\mathrm{H}} \mathbf{G}^{\mathrm{H}} \mathbf{G} \overline{\mathbf{M}}_{1} \boldsymbol{\phi}_{j} & \boldsymbol{\phi}_{j}^{\mathrm{H}} \overline{\mathbf{M}}_{1}^{\mathrm{H}} \mathbf{G}^{\mathrm{H}} \mathbf{G} \overline{\mathbf{M}}_{2} \boldsymbol{\phi}_{j} & \cdots & \boldsymbol{\phi}_{j}^{\mathrm{H}} \overline{\mathbf{M}}_{1}^{\mathrm{H}} \mathbf{G}^{\mathrm{H}} \mathbf{G} \overline{\mathbf{M}}_{j} \boldsymbol{\phi}_{j} \\ \boldsymbol{\phi}_{j}^{\mathrm{H}} \overline{\mathbf{M}}_{2}^{\mathrm{H}} \mathbf{G}^{\mathrm{H}} \mathbf{G} \overline{\mathbf{M}}_{2} \boldsymbol{\phi}_{j} & \cdots & \boldsymbol{\phi}_{j}^{\mathrm{H}} \overline{\mathbf{M}}_{1}^{\mathrm{H}} \mathbf{G}^{\mathrm{H}} \mathbf{G} \overline{\mathbf{M}}_{j} \boldsymbol{\phi}_{j} \\ \vdots & \vdots & \ddots & \vdots \\ \boldsymbol{\phi}_{j}^{\mathrm{H}} \overline{\mathbf{M}}_{j}^{\mathrm{H}} \mathbf{G}^{\mathrm{H}} \mathbf{G} \overline{\mathbf{M}}_{1} \boldsymbol{\phi}_{j} & \boldsymbol{\phi}_{j}^{\mathrm{H}} \overline{\mathbf{M}}_{j}^{\mathrm{H}} \mathbf{G}^{\mathrm{H}} \mathbf{G} \overline{\mathbf{M}}_{2} \boldsymbol{\phi}_{j} & \cdots & \boldsymbol{\phi}_{j}^{\mathrm{H}} \overline{\mathbf{M}}_{j}^{\mathrm{H}} \mathbf{G}^{\mathrm{H}} \mathbf{G} \overline{\mathbf{M}}_{j} \boldsymbol{\phi}_{j} \end{bmatrix} \right) \\ = \boldsymbol{\phi}_{j}^{\mathrm{H}} \sum_{i=1}^{J} \overline{\mathbf{M}}_{i}^{\mathrm{H}} \mathbf{G}^{\mathrm{H}} \mathbf{G} \overline{\mathbf{M}}_{i} \boldsymbol{\phi}_{j}. \end{aligned} \tag{21}$$

# Algorithm 1 Greedy Method Proposed for the *j*-th Sub-Array

# **Input:**

$$\overline{\mathbf{F}}_{\mathrm{RF},j-1}, \ \mathbf{H}_{\mathrm{eff},j}, \ \mathcal{Q}_{\mathrm{H}}, \ \mathcal{Q}_{\mathrm{L}}, \ \mathcal{S}_{j} = \{1,2,\cdots,M\}, \ c_{\mathrm{L}} = c_{\mathrm{H}} = 0;$$

# Algorithm design:

- 1: Initialize  $\mathbf{f}_{\mathrm{RF},1}$  as  $\mathbf{f}_{\mathrm{RF},1} = \frac{1}{\sqrt{M}} e^{j\mathrm{angle}(\mathbf{v}_1)};$
- 2: **for** i = 1 : M **do**
- 3: Design the connection between the  $i_{\rm L}$ -th or the  $i_{\rm H}$ -th TA and the corresponding phase shifter and set  ${\bf f}_{\rm RF,j}$  ( $i_{\rm L}$ ) =  $\frac{1}{\sqrt{M}}e^{jQ_{\rm L}\{q_{\rm L}(i_{\rm L})\}}$  or  ${\bf f}_{\rm RF,j}$  ( $i_{\rm H}$ ) =  $\frac{1}{\sqrt{M}}e^{jQ_{\rm H}\{q_{\rm H}(i_{\rm H})\}}$  according to the greedy method proposed in Section III-C;
- 4: Update  $S_i = S_i \setminus \{i_L\}$  or  $S_i = S_i \setminus \{i_H\}$ ;
- 5: Update  $c_L = c_L + 1$  or  $c_H = c_H + 1$ ;
- 6: Update residual elements in  $\mathbf{f}_{RF,j}$  according to (14)-(15);
- 7: end for

We further derive the upper bound of the OF (16a) as

$$\log_{2}\left(\left|\mathbf{I}_{N_{r}} + \frac{P_{t}}{\sigma^{2}j}\mathbf{G}\mathbf{\Phi}_{j}\mathbf{M}\overline{\mathbf{F}}_{\mathrm{RF},j}\overline{\mathbf{F}}_{\mathrm{RF},j}^{\mathrm{H}}\mathbf{M}^{\mathrm{H}}\mathbf{\Phi}_{j}^{\mathrm{H}}\mathbf{G}^{\mathrm{H}}\right|\right)$$

$$\stackrel{(a)}{\approx} \sum_{i=1}^{j}\log_{2}\left(\left|1 + \frac{P_{t}}{\sigma^{2}j}\boldsymbol{\Sigma}_{\mathrm{eff},j}^{2}\left(i,i\right)\right|\right)$$

$$\stackrel{(b)}{\leq} j\log_{2}\left(\left|1 + \frac{P_{t}}{\sigma^{2}j^{2}}\sum_{i=1}^{j}\boldsymbol{\Sigma}_{\mathrm{eff},j}^{2}\left(i,i\right)\right|\right)$$

$$= j\log_{2}\left(\left|1 + \frac{P_{t}}{\sigma^{2}j^{2}}\left\|\mathbf{G}\mathbf{\Phi}_{j}\mathbf{M}\overline{\mathbf{F}}_{\mathrm{RF},j}\right\|_{\mathrm{F}}^{2}\right|\right), \tag{17}$$

where  $\Sigma_{\text{eff},j}$  is a diagonal matrix with the diagonal elements being the singular values of  $\mathbf{G}\mathbf{\Phi}_{j}\mathbf{M}\mathbf{\overline{F}}_{\text{RF},j}$ , and (a) holds for the approximation in [12] by relying on the truncated SVD of the equivalent channel matrix  $\mathbf{G}\mathbf{\Phi}_{j}\mathbf{M}\mathbf{\overline{F}}_{\text{RF},j}$ , (b) is obtained by adopting Jensen's inequality. We then maximize the upper bound of the bandwidth efficiency and transform the problem

as

$$\max_{\mathbf{\Phi}_{j}} \quad j \log_{2} \left( \left| 1 + \frac{P_{t}}{\sigma^{2} j^{2}} \left\| \mathbf{G} \mathbf{\Phi}_{j} \mathbf{M} \overline{\mathbf{F}}_{RF, j} \right\|_{F}^{2} \right| \right)$$
 (17a)

s.t. 
$$\Phi_j = \operatorname{diag}\left[e^{j\phi_1}, e^{j\phi_2}, \cdots, e^{j\phi_{N_{\text{RIS}}}}\right]$$
. (17b)

However, the OF (17a) is still not in a tractable form. Thus, we substitute the block diagonal hybrid beamforming matrix (10) into (17a). The item in  $\|\cdot\|_{\mathrm{F}}^2$  can be equivalently transformed as

$$\mathbf{G}\mathbf{\Phi}_{j}\mathbf{M}\mathbf{F}_{\mathrm{RF},j}$$

$$=\mathbf{G}\mathbf{\Phi}_{j}\begin{bmatrix}\mathbf{M}_{1} & \mathbf{M}_{2} & \cdots & \mathbf{M}_{N_{\mathrm{RF}}}\end{bmatrix} \cdot$$

$$\begin{bmatrix}\mathbf{f}_{\mathrm{RF},1} & \mathbf{0}_{M} & \cdots & \mathbf{0}_{M} \\ \mathbf{0}_{M} & \mathbf{f}_{\mathrm{RF},2} & \cdots & \mathbf{0}_{M} \\ \vdots & \vdots & \ddots & \vdots \\ \mathbf{0}_{M} & \mathbf{0}_{M} & \cdots & \mathbf{f}_{\mathrm{RF},j} \\ \mathbf{0}_{N_{\mathrm{RF}}-jM} & \mathbf{0}_{N_{\mathrm{RF}}-jM} & \cdots & \mathbf{0}_{N_{\mathrm{RF}}-jM} \end{bmatrix}$$

$$=\mathbf{G}\mathbf{\Phi}_{j}\begin{bmatrix}\mathbf{M}_{1}\mathbf{f}_{\mathrm{RF},1} & \mathbf{M}_{2}\mathbf{f}_{\mathrm{RF},2} & \cdots & \mathbf{M}_{j}\mathbf{f}_{\mathrm{RF},j}\end{bmatrix}, (18)$$

where  $\mathbf{M}_i$  contains the columns of  $\mathbf{M}$  from the M(i-1)+1-st one to the Mi-th one,  $\mathbf{0}_a$  denotes the all zero vector with the dimension of a. Then we have

$$\mathbf{G}\mathbf{\Phi}_{j}\mathbf{M}\mathbf{\overline{F}}_{RF,j}$$

$$=\mathbf{G}\mathbf{\Phi}_{j}\begin{bmatrix}\mathbf{M}_{1}\mathbf{f}_{RF,1} & \mathbf{M}_{2}\mathbf{f}_{RF,2} & \cdots & \mathbf{M}_{j}\mathbf{f}_{RF,j}\end{bmatrix}$$

$$=\begin{bmatrix}\mathbf{G}\overline{\mathbf{M}}_{1}\boldsymbol{\phi}_{j} & \mathbf{G}\overline{\mathbf{M}}_{2}\boldsymbol{\phi}_{j} & \cdots & \mathbf{G}\overline{\mathbf{M}}_{j}\boldsymbol{\phi}_{j}\end{bmatrix}$$

$$=\begin{bmatrix}\mathbf{G}\overline{\mathbf{M}}_{1} & \mathbf{G}\overline{\mathbf{M}}_{2} & \cdots & \mathbf{G}\overline{\mathbf{M}}_{j}\end{bmatrix}\begin{bmatrix}\boldsymbol{\phi}_{j} & \mathbf{0} & \cdots & \mathbf{0}\\ \mathbf{0} & \boldsymbol{\phi}_{j} & \cdots & \mathbf{0}\\ \mathbf{0} & \mathbf{0} & \cdots & \boldsymbol{\phi}_{j}\end{bmatrix}, (19)$$

where  $\phi_j = \begin{bmatrix} e^{j\phi_1} & e^{j\phi_2} & \cdots & e^{j\phi_{N_{\rm RIS}}} \end{bmatrix}^{\rm T}$ ,  $\overline{\mathbf{M}}_i$  is a diagonal matrix with the (k,k)-th element being the k-th element of  $\mathbf{M}_i\mathbf{f}_{{\rm RF},i}$ . Then we can reformulate  $\|\mathbf{G}\mathbf{\Phi}\mathbf{M}\overline{\mathbf{F}}_{{\rm RF},j}\|_{\rm F}^2$  as (21) shown on the top of this page. Therefore, the problem (17)

can be rewritten into a tractable form as

$$\max_{\boldsymbol{\phi}_{j}} \quad j \log_{2} \left( \left| 1 + \frac{P_{t}}{\sigma^{2} j^{2}} \boldsymbol{\phi}_{j}^{H} \mathbf{R} \boldsymbol{\phi}_{j} \right| \right)$$
 (22a)

s.t. 
$$\boldsymbol{\phi}_{i} = \begin{bmatrix} e^{j\phi_{1}} & e^{j\phi_{2}} & \cdots & e^{j\phi_{N_{\text{RIS}}}} \end{bmatrix}^{\text{T}},$$
 (22b)

where  $\mathbf{R} = \sum_{i=1}^{j} \overline{\mathbf{M}}_{i}^{\mathrm{H}} \mathbf{G}^{\mathrm{H}} \mathbf{G} \overline{\mathbf{M}}_{i}$ . Note that the problem (22) has a classical form, hence we adopt the low-complexity CCM-based method for solving it [12], [39], [40]. Specifically, the search space of the problem (22) can be regarded as the product of  $N_{\mathrm{RIS}}$  complex circles, each of which is  $\mathcal{C} \stackrel{\Delta}{=} \left\{ u \in \mathbb{C} : u^{\mathrm{H}}u = 1 \right\}$ . The product of such  $N_{\mathrm{RIS}}$  complex circles is a sub-manifold of  $\mathbb{C}^{N_{\mathrm{RIS}}}$ , which is regarded as CCM and defined by

$$\mathcal{M} = \mathcal{C}^{N_{\text{RIS}}} \stackrel{\Delta}{=} \left\{ \mathbf{u} \in \mathbb{C}^{N_{\text{RIS}}} : |u_i| = 1, i = 1, 2, \cdots, M \right\},$$
(23)

where  $u_i$  denotes the *i*-th element of **u**. The main steps of the CCM-based method consist of three steps during the *t*-th iteration:

#### 1) Riemannian gradients:

The Riemannian gradient has the closed-form expression of [72]

$$\mathcal{T}_{\phi_{j}^{t}}\mathcal{M} = \left\{ \mathbf{z} \in \mathbb{C}^{N_{\mathrm{RIS}}} : \mathfrak{R} \left\{ \mathbf{z} \circ \left(\phi_{j}^{t}\right)^{*} \right\} = \mathbf{0} \right\}.$$
 (24)

The Riemannian gradient of the OF  $f(\phi_j) = j\log_2\left(\left|1+\frac{P_t}{\sigma^2j^2}\phi_j^{\rm H}\mathbf{R}\phi_j\right|\right)$  at the point  $\phi_j^t$  is a tangent vector  $\nabla_{\mathcal{M}}f\left(\phi_j^t\right)$  given by [72]

$$\nabla_{\mathcal{M}} f\left(\boldsymbol{\phi}_{j}^{t}\right) = \operatorname{Proj}_{\boldsymbol{\mathcal{T}}_{\boldsymbol{\phi}_{j}^{t}}, \mathcal{M}} \left(\nabla f\left(\boldsymbol{\phi}_{j}^{t}\right)\right)$$

$$= \nabla f\left(\boldsymbol{\phi}_{j}^{t}\right) - \Re\left\{\nabla f\left(\boldsymbol{\phi}_{j}^{t}\right) \circ \left(\boldsymbol{\phi}_{j}^{t}\right)^{*}\right\} \circ \boldsymbol{\phi}_{j}^{t},$$
(25)

where  $\operatorname{Proj}_{\mathcal{T}_{\phi_j^t}\mathcal{M}}(\cdot)$  is the orthogonal projection operator in the tangent space, while the Euclidean gradient  $\nabla f\left(\phi_j^t\right)$  is in the direction opposite to the gradient of  $f\left(\phi_j^t\right)$  given by

$$\nabla f\left(\boldsymbol{\phi}_{j}^{t}\right) = -\frac{1}{\ln 2} \frac{\frac{2P_{t}}{\sigma^{2}j} \mathbf{R} \boldsymbol{\phi}_{j}^{t}}{1 + \frac{P_{t}}{\sigma^{2}j^{2}} \left(\boldsymbol{\phi}_{i}^{t}\right)^{H} \mathbf{R} \boldsymbol{\phi}_{i}^{t}}.$$
 (26)

# 2) Update over the tangent space:

We update  $\phi_j^t$  on the tangent space with a Armijo step size  $\omega^t$  of [72]

$$\overline{\boldsymbol{\phi}_{j}}^{t} = \boldsymbol{\phi}_{j}^{t} - \omega^{t} \nabla_{\mathcal{M}} f\left(\boldsymbol{\phi}_{j}^{t}\right). \tag{27}$$

# 3) Retraction operator:

In order to map  $\overline{\phi_j}^t$  into the CCM  $\mathcal{M}$ , we use the retraction operator, which is given by [72]

$$\overline{\phi_j}^{t+1} = \overline{\phi_j}^t \circ \frac{1}{\overline{\phi_j}_{abs}^t}, \tag{28}$$

where the *i*-th element in  $\overline{\phi_j}_{abs}^t$  is the absolute of the *i*-th element in  $\overline{\phi_j}^t$ .

The CCM-base method can converge to a critical point of the problem (22) [72], when the error between the OF (22a) before and after the final iteration is less than a predefined criterion  $\epsilon$ .

# C. Extension to discrete RIS scenarios

When considering discrete phases for the RIS elements, we adopt the common method of addressing the non-convex constraint of discrete space relying on approximation projection [41]. Specifically, we define the phase set, where the phases of RIS elements are chosen from the set  $\mathcal{Q}_{\rm RIS}$  associated with  $B_{\rm RIS}$  bits. Following the proximity principle, we can project the resultant  $\Phi_j$  after designing the j-th sub-array to the elements in  $\mathcal{Q}_{\rm RIS}$  relying on approximation projection given by

$$\angle \mathbf{\Phi}_{j}^{\text{dis}}(i, i) = \arg \min_{\psi \in \mathcal{Q}_{\text{RIS}}} |\angle \mathbf{\Phi}_{j}(i, i) - \psi|,$$

$$i = 1, 2, \dots, N_{\text{RIS}}, \quad (29)$$

where  $\psi$  denotes the discrete phases in  $\mathcal{Q}_{RIS}$ . Afterwards, we substitute  $\Phi_j^{\mathrm{dis}}$  into Problem (13) for the subsequent design steps.

**Algorithm 2** Overall Algorithm for Joint Hybrid and Passive Beamforming Design

## **Input:**

G, M, random generalized  $\Phi$ ;

# Algorithm design:

- 1: Initialize  $\mathbf{F}_{\mathrm{RF}}$  as  $\mathbf{F}_{\mathrm{opt}}$ ;
- 2: **for**  $j = 1 : N_{RF}$  **do**
- 3: Update the analog beamforming matrix  $\mathbf{f}_{RF,j}$  according to Algorithm 1;
- 4: Calculate  $\mathbf{F}_{\mathrm{RF},j}$  according to (10);
- 5: Calculate  $\overline{\mathbf{F}}_{\mathrm{RF},j} = \begin{bmatrix} \overline{\mathbf{F}}_{\mathrm{RF},j-1} & \mathbf{F}_{\mathrm{RF},j} \end{bmatrix}$ ;
- 6: Update the passive beamforming matrix  $\Phi_j$  relying on the CCM-based method until meeting the convergence criterion  $\epsilon$ ;
- 7: end for
- 8: Calculate  $\mathbf{F}_{\mathrm{RF}} = \overline{\mathbf{F}}_{\mathrm{RF},N_{\mathrm{RF}}};$
- 9: Calculate  $\Phi = \Phi_{N_{\mathrm{RF}}}$ ;
- 10: Calculate  $\mathbf{F}_{\mathrm{BB}} = \left(\mathbf{F}_{\mathrm{RF}}^{\mathrm{H}} \mathbf{F}_{\mathrm{RF}}\right)^{-\frac{1}{2}} \mathbf{V}_{\mathrm{eff}};$

#### D. Overall Algorithm and Complexity Analysis

The overall SIC-based joint hybrid and passive beamforming design is summarized in Algorithm 2. We update one of the variables, while the others are fixed when designing each sub-array. Once all sub-arrays have been designed, our joint design is accomplished.

Remark 1: In our SIC-based joint design method, we use the analog and passive beamforming matrices previously obtained for designing the remaining columns, which is based on SIC. Furthermore, according to the greedy method, for designing the remaining elements in a sub-array, we update the elements according to (15) that have not yet been designed in the analog beamforming matrix. Therefore, the quantization error of all previously designed phases is taken into consideration when we design the remaining phases and update the RIS elements.

Remark 2: Given the approximation procedures used during the problem transformation, the SIC scheme and the specific properties of the proposed greedy method employed for

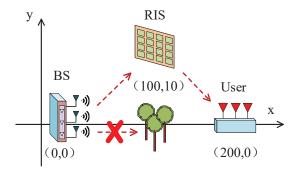


Fig. 3. Illustration of our simulation scenario.

configuring the twin-resolution phase shifters of each subarray, our proposed joint hybrid and passive beamforming design method delivers feasible solutions, rather than globally or locally optimal solutions. Nevertheless, they can achieve near-optimal spectral performance according to the simulation results of Section VI.

The computational complexity is analyzed as follows. For our hybrid beamforming design, the SVD of calculating  $v_i$ for  $j = 1, 2, \dots, N_{\rm RF}$  has the computational complexity order of  $\mathcal{O}(M^3N_{\rm RF})$ . The update of  $\mathbf{f}_{{\rm RF},j}(i)$  for i= $1, 2, \cdots, M, j = 1, 2, \cdots, N_{RF}$  in (15) has the computational complexity order of  $\mathcal{O}(M-1)$ , which has to be repeated  $\frac{M(M-1)}{2}N_{\rm RF}$  times for completing the analog beamforming matrix design. Thus, the computational complexity order of the greedy method is  $\mathcal{O}\left(M^3N_{\mathrm{RF}} + \frac{M(M-1)^2}{2}N_{\mathrm{RF}}\right)$ . For our passive beamforming design, much of the complexity is associated with calculating the Riemannian gradient, which can be accomplished by calculating  $\mathbf{R}\phi_{i}^{t}$  during the t-th iteration. The complexity order of the CCMbased passive beamforming design is  $\mathcal{O}(N_{RIS}N_{RF}I_1)$ , where  $I_1$  is the number of iterations required for convergence. Therefore, the complexity order of the overall algorithm is  $\mathcal{O}\left(M^3N_{\mathrm{RF}}+\frac{M(M-1)^2}{2}N_{\mathrm{RF}}+N_{\mathrm{RIS}}N_{\mathrm{RF}}I_1\right)$ .

#### V. NUMERICAL RESULTS

In this section, we provide simulation results for characterizing the proposed joint hybrid and passive beamforming design of RIS-assisted mmWave systems relying on twin-resolution dynamic sub-connected hybrid structures.

Unless otherwise stated, the number of TAs in our simulations is set to  $N_t=8\times 8=64$ , the number of RF chains is  $N_{\rm RF}=4$ , the number of complex-gain propagation paths is L=P=4, while the number of data streams is set to  $N_s=4$ . The azimuth AoA  $\phi_\ell^{\rm r}$  and AoD  $\phi_\ell^{\rm t}$  are uniformly distributed in the interval  $\left[-\pi,\pi\right)$  and the elevation AoA  $\theta_\ell^{\rm r}$  and AoA  $\theta_\ell^{\rm t}$  are uniformly distributed in the interval  $\left[-\frac{\pi}{2},\frac{\pi}{2}\right]$  [73]. As illustrated in Fig. 3, the coordinates of the BS, the RIS and the user are  $(x_{\rm BS},y_{\rm BS})=(0,0)$ m,  $(x_{\rm RIS},y_{\rm RIS})=(100,10)$ m,  $(x_{\rm user},y_{\rm user})=(200,0)$ m, respectively. The distances between the BS and the RIS and that between the RIS and the user are denoted by  $d_{\rm BS-RIS}$  and  $d_{\rm RIS-user}$ , respectively. We

#### TABLE II KEY PARAMETERS

Parameter	Value
Number of paths, $L$ , $P$	4
Distances, $d_{BS-RIS}$ , $d_{RIS-user}$	100.4988m
Path Loss, $A_{\rm BR}$ , $A_{\rm RU}$	-74.0475dB
Carrier frequency	28GHz
Bandwidth, $B$	251.1886MHz [12]
Noise power, $\sigma^2$	-90dBm

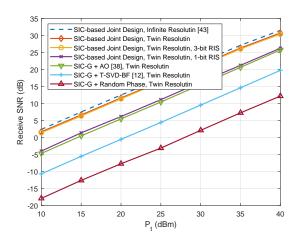


Fig. 4. Receive SNR vs. transmit power.

calculate the system's path loss according to the theoretical free-space distance-dependent path-loss model for investigating the bandwidth efficiency of our proposed structure and beamforming methods [15], [74]. The path-loss in the BS-RIS link and RIS-user link is then calculated by  $A_{\rm BR} = -30-22.0\log d_{\rm BS-RIS}$  and  $A_{\rm RU} = -30-22.0\log d_{\rm RIS-user}$ , respectively [15]. The carrier frequency is 28GHz and the bandwidth is B=251.1886MHz [12]. The noise power is calculated by  $\sigma^2=-174+10\log_{10}B=-90$ dBm. In our simulations, the higher resolution of the phase shifter is set to  $B_{\rm H}=4$ bits and the lower resolution is set to  $B_{\rm L}=1$ bit. We set the error threshold of passive beamforming to  $\epsilon=10^{-6}$ . The key parameters are listed in Table II.

# A. Receive SNR and bandwidth efficiency comparison

In Fig. 4, we show the relationship between the receive SNR defined by  $\frac{P_t \|\mathbf{G} \mathbf{\Phi} \mathbf{M} \mathbf{F}_{\mathrm{RF}} \mathbf{F}_{\mathrm{BB}}\|_{\mathrm{F}}^2}{\sigma^2 N_s}$  and the transmit power  $P_t$ . Since the hybrid beamforming matrix  $\mathbf{F}_{\mathrm{RF}}\mathbf{F}_{\mathrm{BB}}$  and RIS matrix  $\Phi$  are optimized for a given transmit power constraint  $P_t$ , the effective channel (including RIS reflection) and the receive SNR are different, when we adopt different hybrid/passive beamforming design methods. We consider 7 curves for comparison, including: 1) SIC-based Joint Design, Infinite Resolution [43]: we adopt the SIC-based joint design method for hybrid beamforming design, where the greedy method is replaced by the algorithm of [43] considering the infinite resolution of phase shifters; 2) SIC-based Joint Design, Twin Resolution: we adopt the method advocated for the proposed structure; 3) SIC-based Joint Design, Twin Resolution, 3-bit RIS: we adopt the method advocated and the resolution of the RIS elements is  $B_{RIS} = 3$ ; 4) SIC-based Joint Design,

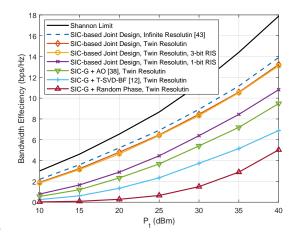


Fig. 5. Bandwidth Efficiency vs. transmit power.

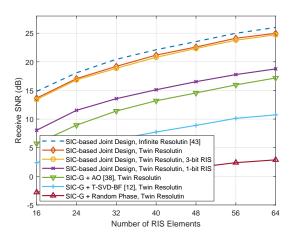


Fig. 6. Receive SNR vs. number of RIS elements.

Twin Resolution, 1-bit RIS: This method is the same as 3) except that  $B_{RIS} = 1$ ; 5) SIC-G + AO [38], Twin Resolution: we adopt the proposed SIC-based greedy beamforming method for the hybrid beamforming design and the AO-based method of [38] for passive beamforming design, where twin-resolution of phase shifters are considered; 6) SIC-G + T-SVD-BF [12], Twin Resolution: we adopt the proposed SIC-based greedy beamforming method for hybrid beamforming design and the truncated SVD beamforming (T-SVD-BF) method of [12] for passive beamforming design, where the phase shifters are of twin-resolution; 7) SIC-G + Random Phase, Twin Resolution: the phases of RIS elements are randomly set for comparison. Fig. 4 demonstrates that our structure conceived with our proposed SIC-based joint design achieves higher receive SNR than the other methods. Fig. 5 also illustrates that when the resolution of the RIS elements is  $B_{RIS} = 3$ bits, the proposed quantization method approaches the bandwidth efficiency of the infinite-resolution RIS scenarios. Moreover, there is a 20dB receive SNR gain, when the RIS elements are optimized. With the aid of the proposed joint hybrid and passive beamforming method, we can improve the receive SNR by 20dB.

In Fig. 5, we show the bandwidth efficiency vs. the trans-

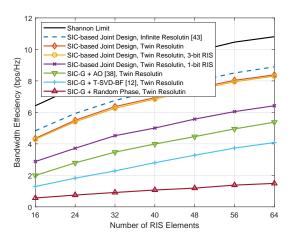


Fig. 7. Bandwidth efficiency vs. number of RIS elements.

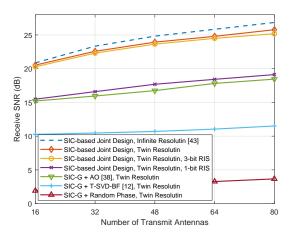


Fig. 8. Receive SNR vs. number of transmit antennas.

mit power  $P_t^{-1}$ . Observe that our solution outperforms the benchmarks, because it relies on a joint hybrid and passive beamforming design. We also add *Shannon Limit* to Fig. 5, which is obtained by the Shannon limit defined in [75] with the effective channel obtained by the proposed joint hybrid and passive beamforming matrix. Nevertheless, the hybrid beamforming structure, finite/low-resolution phase shifters and the approximations adopted during the problem transformation inevitably erode the system's performance. Therefore, our proposed method lags behind than the Shannon limit.

Fig. 6 illustrates the relationship between the receive SNR and the number  $N_{\rm RIS}$  of RIS elements. As shown in Fig. 6, the receive SNR increases as  $N_{\rm RIS}$  increases, which is due to the fact that having more RIS elements leads to higher beamforming gains. Furthermore, when  $N_{\rm RIS}$  is increased, the receive SNR tends to saturate, owing to the maximum SNR given by  $\frac{P_t}{\sigma^2}$ .

Fig. 7 shows the relationship between the bandwidth efficiency and the number  $N_{\rm RIS}$  of RIS elements. The relative relationship among the 6 curves is reminiscent of those in Fig.

<sup>1</sup>Using the transmit power is unconventional. This quantity is however beneficial for the problem considered, because the proposed method increases the receive SNR for given transmit power.

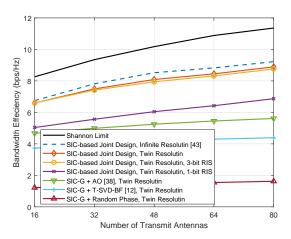


Fig. 9. Bandwidth efficiency vs. number of transmit antennas.

TABLE III
POWER CONSUMPTION OF DEVICES

Device	Power Consumption
Baseband processor, $P_{\rm BB}$	200 mW [76]
Each RF chain, $P_{RF}$	300 mW [76]
Each high-resolution phase shifter, $P_{\rm H}$ (4 bits)	52 mW [77]
Each low-resolution phase shifter, $P_{\rm L}$ (1 bit)	10 mW [77]
Each switch, $P_{SW}$	1mW [42]
Each RIS element, $P_{\rm RIS}$	1mW [46]

5. Moreover, we observe that as  $N_{\rm RIS}$  increases from 16 to 64, the system's bandwidth efficiency increases in line with the Shannon limit, because more RIS elements increase the beamforming gain of the effective channel  $\mathbf{G}\mathbf{\Phi}\mathbf{M}$ .

The relationship between the receive SNR and the number  $N_t$  of TAs is shown in Fig. 8. As  $N_t$  increases from 16 to 80, the number of antennas in each sub-array M increases from 4 to 20, which improves the beamforming gain. Similar to the above analysis, the receive SNR cannot be larger than  $\frac{P_t}{\sigma^2}$ .

We show the relationship between the bandwidth efficiency and  $N_t$  in Fig. 9. Since more TAs lead to higher beamforming gain for the effective channel  $\mathbf{G}\mathbf{\Phi}\mathbf{M}$ , both the Shannon limit and the bandwidth efficiency increase upon increasing  $N_t$ .

## B. Bandwidth efficiency vs. energy efficiency trade-off

Fig. 10 illustrates the bandwidth efficiency and energy efficiency vs. the transmit power  $P_t$ . Note that our proposed method can be used for designing the hybrid beamforming matrix entirely relying on high-resolution or low-resolution phase shifters by setting  $N_{\rm L}~=~0$  or  $N_{\rm H}~=~0$  in the proposed method. Three scenarios are considered, including 1) SIC-based Joint Design, High Resolution: we adopt the proposed method for jointly designing the hybrid and passive beamforming matrices. In each sub-array, only high-resolution phase shifters are used; 2) SIC-based Joint Design, Twin Resolution: we adopt the proposed method for the advocated structure; 3) SIC-based Joint Design, Low Resolution: this scenario is similar to 1) except that only low-resolution phase shifters are adopted in each sub-array. Although controlling all switches will lead to some energy loss [78], the main power dissipation of the dynamically configurable switching

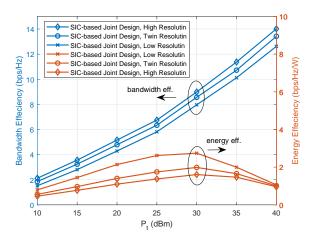


Fig. 10. Bandwidth efficiency & energy efficiency trade-off vs. transmit power.

network advocated is due to the total power of the switches enabled during the transmission [79], [80]. Hence the power consumption of the switches is given by  $N_t P_{SW}$ . The energy efficiency of the proposed RIS-assisted mmWave MIMO communication systems relying on twin-resolution dynamic subconnected hybrid structures is calculated by  $\mathrm{EE_{Twin}} = \frac{R}{P_{\mathrm{Twin}}}$ , where  $P_{\text{Twin}}$  is the total power consumption of the systems, which is calculated by  $P_{\mathrm{Twin}} = P_t + P_{\mathrm{BB}} + N_{\mathrm{RF}} P_{\mathrm{RF}} + N_{\mathrm{RIS}} P_{\mathrm{RIS}} + \frac{N_t}{2} P_{\mathrm{H}} + \frac{N_t}{2} P_{\mathrm{L}} + N_t P_{\mathrm{SW}}$ , and  $P_{\mathrm{BB}}$  is the power consumption of the baseband processor, and  $P_{RF}$  denotes the power consumption of each RF chain. The symbols  $P_{\rm H}$ and  $P_{\rm L}$  are the power consumption of a high-resolution and of a low-resolution phase shifter, respectively. The symbol  $P_{\rm SW}$  represents the power consumption of each switch in the systems, which is used for connecting the phase shifters to the TAs. The symbol  $P_{\rm RIS}$  stands for the power consumption of each RIS element. When considering the purely high- or solely low-resolution sub-connected analog beamformer, the energy calculation is slightly modified by  $EE_o = \frac{R}{P_o}$ , where  $o \in \{H, L\}$ , and  $P_o$  is the total power consumption defined by  $P_o = P_t + P_{BB} + N_{RF}P_{RF} + N_{RIS}P_{RIS} + N_tP_o$ . The power consumptions of the devices in the system are presented in Table III. We can draw the conclusion for Fig. 10 that the twin-resolution dynamic sub-connected hybrid beamforming structure strikes a bandwidth efficiency vs. energy efficiency trade-off. Specifically, the RIS-assisted MIMO systems using twin-resolution dynamic sub-connected analog beamformers have a higher bandwidth efficiency than that of the entirely low-resolution sub-connected analog beamformer, while its energy efficiency is lower. By contrast, although the RISassisted system relying on the proposed structure has a lower bandwidth efficiency than the entirely high-resolution subconnected hybrid structure, it is more energy-efficient. Observe in Fig. 10 that the energy efficiency increases first and then decreases. This is because the energy efficiency is calculated as a ratio, where the bandwidth efficiency in the numerator is a logarithmic function of  $P_t$ , while the power consumption in the denominator is a linear function of  $P_t$ . Therefore, the numerator increases more rapidly than the denominator first,

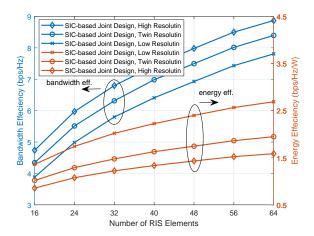


Fig. 11. Bandwidth efficiency & energy efficiency trade-off vs. number of RIS elements.

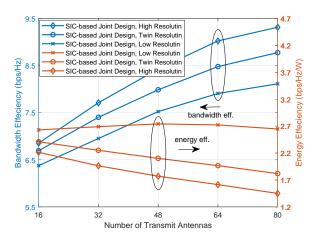


Fig. 12. Bandwidth efficiency & energy efficiency trade-off vs. number of transmit antennas.

but slower beyond the maximum. The optimal transmit power  $P_t$  for maximum EE is about 30dBm. Fig. 11 portrays both the bandwidth efficiency and energy efficiency versus the number of RIS elements. Similar to the trends in Fig. 10, our proposed structure strikes a trade-off between bandwidth efficiency and energy efficiency, when the number of RIS elements increases from 16 to 64. Furthermore, as the number of RIS elements increases, both the system's bandwidth efficiency and energy efficiency increases for all three cases, but gradually saturates.

A bandwidth efficiency vs. energy efficiency trade-off can also be observed from Fig. 12, as the number TAs increases from 16 to 80. We observe that the energy efficiency of the entirely low-resolution sub-connected hybrid structure based RIS-assisted MIMO systems is better than that of the twin-resolution dynamic sub-connected hybrid structure based ones and of the entirely high-resolution sub-connected hybrid structure based schemes.

# VI. CONCLUSION

In this paper, we proposed RIS-assisted millimeter-wave (mmWave) wireless communication systems relying on twin-

resolution dynamic sub-connected hybrid beamforming structures. More explicitly, we conceived an energy-efficient and low-complxity dynamic sub-connected analog beamformer relying on twin-resolution phase shifters, which combines the advantages of the high spatial gain brought about by high-resolution phase shifters and the cost efficiency of lowresolution phase shifters. The RIS enhances the performance of communication systems by beneficially reflecting the multipath signals. For jointly designing the hybrid beamforming and RIS elements, a SIC-based joint design method was proposed. Specifically, we decomposed the bandwidth efficiency maximization problem into a series of sub-rate maximization problems, where the sub-array of phase shifters and RIS elements were jointly optimized. For our hybrid beamforming design, we proposed a greedy method for beneficially configuring the connections between the TAs of each sub-array and the phase shifters. For our passive beamforming design, we developed a CCM-based method for updating the RIS elements. Our simulation results demonstrated the superiority of the proposed structure and the proposed method over its counterparts. In conclusion, the proposed structure combined with the proposed method strikes an attractive trade-off between the bandwidth efficiency and power consumption.

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