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Challenges and perspectives for integral bridges in the UK: from design practice to fieldwork through small-scale laboratory experiments

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Challenges and perspectives for integral bridges in the UK: from design practice to fieldwork through small-scale laboratory experiments

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ABSTRACT

This study focuses on the investigation of the factors that have limited, so far, the development of a consistent design and assessment approach for integral bridges (IBs). This paper presents a review of previous research and current design practices for IBs, followed by a review of monitoring studies in the laboratory and in the field. As part of the UKCRIC PLEXUS experimental campaign, a small-scale 1g physical experiment is described. The test aimed to simulate the soil-structure interaction arising from seasonal expansion and contraction of the bridge deck and assess the performance of different monitoring techniques. Pressure cells were used to measure the lateral stresses behind the abutment wall, Particle Image Velocimetry was employed to monitor the soil behaviour behind the abutment and Linear Variable Differential Transformers were used to monitor the backfill surface movements. By combining the data from these instruments, a preliminary assessment of the soil-structure interaction behaviour of the idealised integral abutment under seasonal thermal loading has been obtained. These monitoring methods and the associated understanding of IBs' behaviour gained from the tests provide definitive evidence for the development of monitoring systems for larger-scale physical tests and field monitoring systems for IBs.

Keywords

Bridges; thermal effects; laboratory tests; earth pressure; settlement; monitoring; soil/structure interaction

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List of notation

K	lateral earth pressure coefficient
K_0	horizontal earth compression coefficient, at rest
K_a	horizontal earth compression coefficient, active
K_p	horizontal earth compression coefficient, passive
d	displacement at the top of the bridge abutment due to thermal loading
α	coefficient of thermal expansion of the deck (of the order of 10^{-5} for concrete decks)
L_x	expansion length measured from the end of the bridge to the position on the deck that remains stationary when the bridge expands
$T_{e,max}$	characteristic maximum uniform temperature for a 50-year return period in the UK
$T_{e,min}$	characteristic minimum uniform temperature for a 50-year return period in the UK
\emptyset	slope of the earth pressure
H	height of the abutment
d'_d	wall deflection at depth $H/2$ below ground level
K_d^*	design value of the earth pressure coefficient for expansion
C	dimensionless coefficient used in the calculation of K_d^*
$K_{p,t}$	coefficient of passive earth pressure used in the calculation of K_d^*
ϕ'	effective friction angle
c'_{peak}	peak effective cohesion
φ'_{peak}	peak effective friction angle
e_{min}	minimum void ratio
e_{max}	maximum void ratio
ε	soil volumetric strain

1 **1. Introduction**

2 A large investment is continually made in infrastructure globally. For example, the UK infrastructure pipeline
3 has committed £12.6bn for roads and £46.2bn for rail ([National Infrastructure Delivery Plan 2016-2021](#)).
4 Internationally, the global pipeline is estimated to be as high as US\$97 trillion ([Global Infrastructure Hub,](#)
5 [2020](#)). In transportation networks, bridges represent a particularly vulnerable element to which the largest
6 investment is linked (e.g., [Rasulo et al. 2004](#); [Nuti et al. 2009](#); [Thoft-Christensen 2012](#); [NIST 2015](#)). In
7 traditional bridges, joints and bearings have emerged as the main source of bridge maintenance problems
8 and costs ([Wolde-Tinsae and Greimann, 1988](#); [Greimann and Wolde-Tinsae, 1986](#)) due to the cyclic
9 displacements caused by thermal gradients, traffic and dynamic loads, while both corrosion of and access
10 to bearings provide particular maintenance challenges. Thus, integral bridges (IBs) are becoming
11 increasingly attractive because of reduced maintenance issues at the bridge deck–abutment interface
12 compared with traditional bridge construction.

13 Integral bridges have received increasing attention by designers in the last few decades and are widely
14 used in many countries for small-to-medium span highway bridges and overcrossings ([Burke, 2009](#)). They
15 now constitute a significant part of the transportation infrastructure stock, with an estimated number in
16 service of over 9,000 in the US alone ([Paraschos and Amde 2011](#); [White et al. 2010](#); [Fiorentino et al 2021](#)).
17 Integral bridges are likewise becoming more widely used in the United Kingdom, Europe and Asia
18 ([Bloodworth, 2011](#)), while their design varies according to practices and requirements outlined by regional
19 transportation authorities. In the United States, each state highway department has its integral abutment
20 programme and has established guidelines concerning their design and construction. The specification of
21 the American Association of State Highway and Transportation Officials (AASHTO LRFD; [AASHTO, 2012](#))
22 is the most widely accepted integral bridge design guideline in the United States, providing performance
23 criteria for IB design. Parallel design guidance is provided in the Canadian Foundation Engineering Manual
24 ([Canadian Geotechnical Society, 1978](#)).

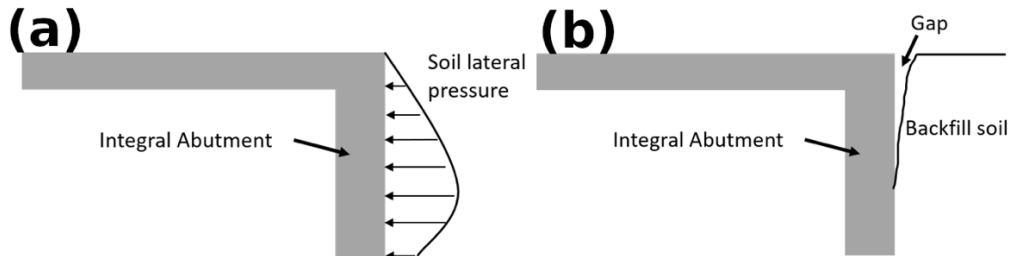
25 In the UK, PD 6694 ([PD 6694-1: 2011](#)) and the Highways Agency Design Manual for Roads and Bridges
26 ([BA42/96 2003](#)) are currently the reference guides, with these documents referring to European standards
27 ([EN 1997-1, Eurocode 7](#)) and CIRIA Report 760 on embedded retaining walls ([Gaba et al., 2017](#)) for
28 relevant design parameters. Currently, span lengths of integral bridges are limited due to the lack of an

29 adequate evidence base on which to predict their performance. There is consequent conservatism in design
30 guidance (Dicleli et al. 2003; Baptiste et al. 2011, Zordan 2011a; Zordan 2011b; Mitoulis et al. 2016), which,
31 in turn, reflects imperfect understanding of the behaviour of these structures under the imposed loads. In
32 the UK, spans are limited to 60 m length and 30 degrees skew (BA42/96 2003, PD 6694 2011). Although
33 design codes offer provision for the static design of integral bridges (BMVBS 2013; Gaba et al. 2017), the
34 use of IBs is limited mainly by the lack of explicit design guidelines coherent across different countries.
35 The rationale for the limitations in design codes lies mainly in the uncertainty related to the soil-structure
36 interaction between the backfill and the abutment walls when integral bridge decks expand due to seasonal
37 thermal loads under ambient conditions (Gorini and Callisto, 2017; 2019; Huffman et al., 2015). When the
38 bridge expands, substantial force is exerted on the abutment by the soil reaction, and this can significantly
39 impact the integrity of the structure. Such inherently nonlinear soil action is dependent on the magnitude
40 and distribution (with height) of the wall displacement, which encompasses both translational and rotational
41 displacements depending on the boundary conditions. In the longer term, as seasons of cyclic expansion
42 and contraction of the bridge decks occur, there can be a build-up of significant lateral earth pressure behind
43 the abutments (Figure 1a). This asymmetric cyclic stress-strain behaviour is known as *ratcheting* (Horvath,
44 2004; Cui and Mitoulis, 2015; England et al. 2000). However, soil conditions can vary from relatively loose
45 to dense states with different compaction levels; consequently, the pressure that builds-up behind the
46 abutment could significantly increase with time – by a factor of four or more. Accordingly, axial forces on
47 the bridge deck may increase as well, by a factor of around two (part of the pressure being absorbed by
48 the abutment foundation), while bending moments in the composite deck may increase by somewhat less
49 than the axial forces, depending on soil stiffness and boundary conditions (Fennema et al., 2005;
50 Shamsabadi et al., 2007; Clayton et al., 2006; Mahjoubi and Maleki, 2018). The thermal loading also causes
51 ground settlement adjacent to abutments (which may be under approach slabs, if present), with gaps often
52 observed at the surface between the abutment and backfill (Figure 1b). Moreover, subsidence behind the
53 abutment wall can cause structural problems in approach slabs if the bending loads due to traffic are
54 significant (Muttoni et al., 2013).

55 A number of mitigation measures are available to reduce the excessive lateral pressures on the abutment
56 walls. These include limiting bridge length, skew and the vertical penetration of abutments into

57 embankments; using selected granular backfill (Al-Ani et al., 2018); providing approach slabs to prevent
58 vehicular compaction of the backfill (Muttoni et al., 2013); using embankment benches to shorten wing
59 walls; and using suspended turn back wing walls (Paraschos, 2016).

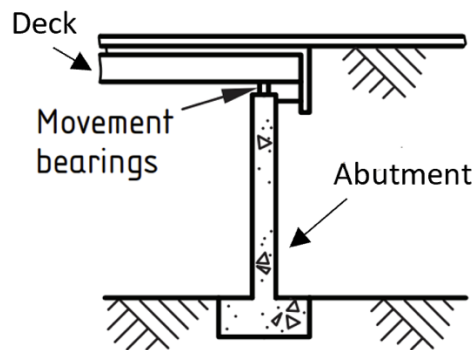
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61

62 *Figure 1. (a) build-up of lateral earth pressures behind the abutment under thermal loading, (b) gapping*
63 *between abutment wall and backfill under cyclic thermal loading.*

64 In addition, semi-integral abutment designs (Figure 2) are used to remove passive pressures under bridge
65 seats. In such designs, the end screen wall and deck beams are integral with each other, but the end screen
66 wall does not provide support to the deck beams. Instead, a structure with bearings, which can
67 accommodate horizontal displacement, is provided as support to the deck beams.



68

69 *Figure 2. Semi-integral abutment design (from PD6694, 2011)*

70 Compressible inclusions between the abutments and the backfill, such as EPS Geofoam, have also been
71 proposed to mitigate the build-up of earth pressures and uncouple the response of the bridge from that of
72 the backfill (Horvath 2000, 2005, Mylonakis et al. 2007a, Mitoulis et al. 2016, Fiorentino et al. 2021).
73 However, extra design and construction work should be allowed for at the design stage. Compressible
74 inclusions between the abutment and the backfill allow dissipation of the lateral earth pressures and the

75 control of displacements in the backfill in performance-based design ([Karpurapu and Bathurst 1992](#), [Abdel](#)
76 [Salam and Azzam 2016](#)).

77 It has also been observed that even if the superstructure responds linearly elastically under thermal loads
78 (which is anticipated in IBs), local nonlinear material behaviour of the backfill could result in triggering a
79 nonlinear response in the entire soil-bridge system ([McCallen et al. 1994](#)). Recurrent cyclic traffic loads
80 during integral bridge operation (assuming there is no bridging slab) further compacts the backfill, and may
81 also contribute to increases in lateral earth pressures. These effects can be replicated through mechanistic
82 models that have been proposed for the numerical modelling of soil-structure interaction effects on integral
83 bridge abutments ([Zhang and Makris 2002](#), [Kotsoglou and Pantazopoulou 2007, 2009](#); [Kappos and Sextos](#)
84 [2009](#)).

85 A field study of an integral bridge equipped with an elastic inclusion (i.e., a layer of elastic material between
86 the abutment and the retained soil) showed significantly reduced lateral earth pressures and tolerable
87 settlements of the approach fill ([Hoppe, 2005](#)). This isolated system exhibited a mirrored behaviour, with
88 increasing pressure effects occurring at each consecutive thermal cycle, while the backfill soil
89 displacements showed a settling effect with a decreasing magnitude with increasing number of cycles. An
90 important finding was that both the developed pressures and the associated displacements were smaller
91 than those in the conventional system: the peak pressures were seven times smaller and the settlement
92 around four times smaller. Due to the lower absolute pressures and an approximately linear pressure
93 distribution behind the abutment, the overall bending moments induced on the abutment walls were also
94 greatly reduced. This approach may, therefore, lead a more sustainable solution to span longer distances
95 ([Caristo et al., 2018](#)). However, without explicit adoption in codes, elastic inclusions are unlikely to achieve
96 widespread use and there remain maintenance implications that can make this solution less appealing.

97 Reducing or removing uncertainties/barriers and improving the functionality of IBs, throughout their design,
98 construction, operation and maintenance phases, provide a means of reducing infrastructure costs and
99 increasing their value. This can be achieved by better diagnosis (i.e., developing knowhow on the problem
100 to reduce epistemic uncertainty) and feeding research findings from laboratory experiments, modelling and
101 field-monitoring campaigns into national and international design code development ([Dhar and Dasgupta](#)
102 [2019](#)). In support of this and similar goals, the UK Collaboratorium for Research on Infrastructure and Cities

103 (UKCRIC; www.ukcric.com), has recently created a suite of world-leading laboratory facilities combining
104 multi-disciplinary research teams with systems thinking and practice approaches to enhance the value of,
105 and de-risk investments in, infrastructure and urban systems interventions.

106 The UKCRIC–PLEXUS (Priming Laboratory EXperiments on infrastructure and Urban Systems)
107 programme included a project that combined three of the new national facilities and a variety of research
108 approaches to establish a comprehensive picture of the soil-structure interaction behaviour of IB abutments
109 under lateral loading. This included a small-scale experimental campaign to complement the evidence base
110 available in the literature, which is reported herein following a brief review of current international design
111 practices (Section 2), an introduction to previous field monitoring techniques (Section 3) and a review of
112 previous research on IBs (Section 4). The results from the experimental campaign (Section 5) are then
113 presented and discussed in relation Sections 1-4, along with conclusions and plans for large-scale
114 experimental tests (Section 6).

115 **2. Current design practice**

116 The design of IBs varies according to practices and requirements stipulated by local transportation
117 agencies, a brief summary is presented in [Table 1](#). The US ([AASHTO, 2012](#)), Canadian ([Canadian
118 Geotechnical Society, 1978](#)) and UK ([PD 6694-1: 2011](#); [BA42/96 2003](#)) guidance are perhaps the most
119 authoritative.

120 For abutment design, the earth pressure distribution behind the abutment is determined using a depth-
121 dependent lateral earth pressure coefficient, K ([Mei et al., 2017](#); [Vahedifard, 2015](#)), defined as the ratio of
122 effective lateral (horizontal) effective stress to the effective vertical stress at a specific depth. The value of
123 K depends on many parameters, notably the nature of soil (coarse grained vs fine grained), its density and
124 its loading history (over-consolidation ratio). There are three categories of horizontal earth pressure
125 coefficient: at rest (K_0) corresponding to zero horizontal wall movement and zero normal horizontal soil
126 strain, active (K_a) representing a theoretical minimum value requiring sufficient outward wall displacement
127 (i.e., away from the backfill), and passive (K_p) representing a theoretical maximum value requiring sufficient
128 inward wall displacement (towards the backfill). There are several, theoretical and empirical, theories for
129 establishing the lateral earth pressure coefficient. Coulomb ([1773](#)) first proposed a heuristic limit analysis

130 framework (known today as the Limit Equilibrium method) associated with shear failure of a soil wedge
131 within the backfill, using an optimisation procedure to identify stationary values among an infinite set of
132 candidate lateral thrusts. Mayniel in 1808 extended Coulomb's equations to include wall friction, and Muller-
133 Breslau in 1906 further generalised Mayniel's equations to incorporate an inclined backfill and wall.
134 Coulomb's solution provides the most useful tool for establishing earth thrusts by hand calculations, yet the
135 method works solely with forces (not stresses) and thus cannot establish the point of application (elevation)
136 of the overall soil thrust. Subsequently, Rankine's (1857) theory, based on limit stresses to predict active
137 and passive pressure coefficients, produced exact stresses (hence predicting the point of application of soil
138 thrust). However, its applicability is limited – notably to vertical walls having roughness equal to the
139 inclination of the backfill under plane strain conditions – while the kinematics of the problem (i.e., soil and
140 wall displacements) and the compatibility of deformations are essentially ignored. More advanced stress
141 solutions encompassing inclined backfill and wall are available in Mylonakis et al. (2007b).

142 Importantly, the use of full passive pressures without regard to displacements and compatibility of
143 deformations is not conservative as it invariably suppresses the flexural effects of dead and live loads on
144 the bridge girders. Modified coefficients based on Rankine's solution have been proposed (Kloukinas et al
145 2015; Hanna and Diab, 2016; Pain et al., 2017; Rajesh and Choudhury, 2017). For relatively short single-
146 span IBs, the passive earth pressure coefficients were reduced by multiplying the relevant Rankine
147 coefficients with modification factors. The displacement at the top of the bridge abutment due to thermal
148 loading, d , is calculated using Equation 1 (PD6694, 2011):

149
$$d = \alpha L_X (T_{e,max} - T_{e,min}) \quad (1)$$

150 where:

151 α is coefficient of thermal expansion of the deck (of the order of 10^{-5} for concrete decks);

152 L_X is expansion length measured from the end of the bridge to the position on the deck that remains
153 stationary when the bridge expands;

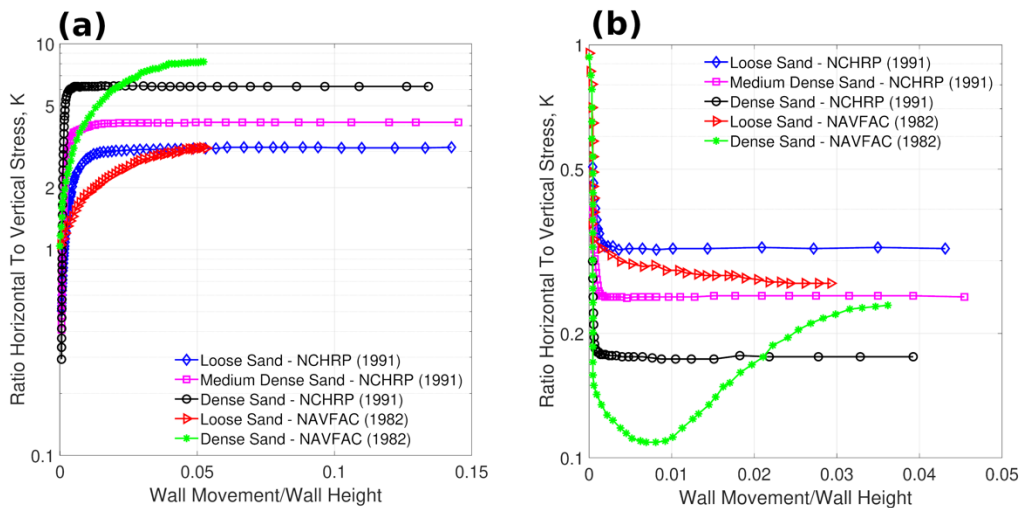
154 $T_{e,max}$ and $T_{e,min}$ are the characteristic maximum and minimum uniform bridge temperature components for
155 a 50-year return period in the UK (National Annex to BS EN 1991-1-5, 2003), respectively.

156 The specified dimensionless displacement (“drift”, which is the horizontal movement applied on the top of
 157 the abutment wall from span over the abutment wall height) for full passive pressure development is equal
 158 to approximately 4×10^{-2} for loose sand and equal to 1×10^{-2} for dense sand (Clough and Duncan, 1991).
 159 Widely used curves to determine the lateral soil pressure for loose, medium and dense granular materials
 160 (Figure 3) are presented in NCHRP Report 343 (NCHRP, 1991) and NAVFAC (1982), while design curves
 161 are provided in the Canadian Foundation Engineering Manual (Canadian Geotechnical Society, 1978) and
 162 by the US Section of the Navy (Cole and Rollins, 2006).

163 NCHRP (1991) and NAVFAC (1982) recommend applying limit equilibrium solutions based on log spiral
 164 failure mechanisms for standard backfill configurations, since Coulomb’s failure wedge methodology is
 165 notoriously non-conservative for determining passive pressures (Xu et al., 2018; Keykhosropour, and
 166 Lemnitzer, 2019). AASHTO (2012) determines horizontal soil pressures on bridge abutments according to
 167 Rankine’s active soil pressures, based on variations in the earth pressure coefficient as a function of
 168 structural displacement from experimental data and finite element analyses, leading to a practically linear
 169 relationship as shown in Equation 2 (Bal et al., 2018; Capilleri et al., 2019):

$$K = K_0 + \phi d \leq K_p \quad (2)$$

171 where d is the displacement of the IB towards the backfill, and ϕ is the slope of the earth pressure variation
 172 with horizontal displacement (which varies with the backfill type).



173

174 *Figure 3. Relationship between wall displacement and earth pressure in sand (a) wall moving towards the*
175 *backfill (passive like) (b) wall moving away from the backfill (active like) according to NCHRP (1991) and*
176 *NAVFAC (1982).*

177 There is reasonable agreement between the predicted average passive earth pressure of standard
178 compacted gravel backfill with the results from full-scale wall tests performed at the University of
179 Massachusetts (Bonczar et al., 2005). According to the tests, the pressure coefficient K (Massachusetts
180 Bridge Manual, 1999) can be estimated using the following empirical equation:

$$181 \quad K = 0.43 + 5.7 \left[1 - e^{-190\left(\frac{d}{H}\right)} \right] \quad (3)$$

182 where d is the displacement of the IB towards the backfill soil, and H is the height of the abutment. The first
183 term in Equation 3 (0.43) can be interpreted as a K_0 coefficient, while the multiplier on the second term (5.7)
184 can be interpreted as the difference between passive and at rest pressures ($K_p - K_0$), being zero for zero
185 displacement and maximum (5.7) for infinite displacement. To achieve a pressure equal to 99% of active
186 requires a dimensionless displacement (“drift”) of approximately 2.4%. These values correspond to the case
187 of a rough wall and a medium-dense granular backfill.

188 From experiments investigating the cyclic stresses in backfill soil on a concrete wall with a pinned
189 connection to a strip footing (Firoozi et al., 2016; Yazdandoust et al., 2019), and according to PD 6694
190 (2011) for full height abutments on spread footings, which accommodate thermal movements by rotation or
191 flexure, the earth pressure on the retained face for an integral abutment wall is dependent on: (1) the
192 thermal movement range (based on a 50-year return period), (2) the direction of movement (expansion or
193 contraction), and (3) the magnitude of expansion or contraction for the combination of actions for the design
194 situation under consideration (Figure 4). The design value of the earth pressure coefficient for expansion K_d^*
195 can be estimated from Equation 4, but should not be taken as greater than $K_{p,t}$:

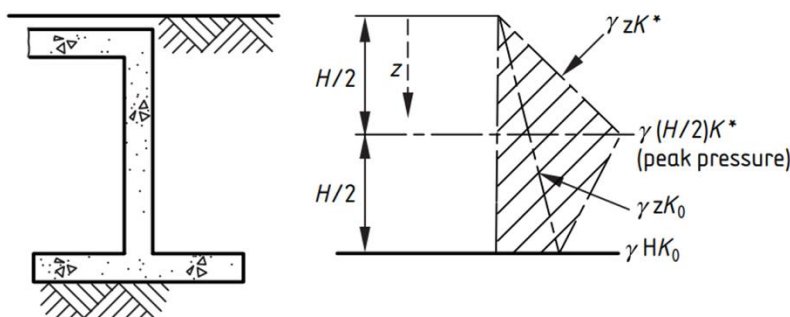
$$196 \quad K_d^* = K_0 + \left(\frac{Cd'_d}{H}\right)K_{p,t} \quad (4)$$

197 where K_0 is the coefficient of earth pressure at rest; H is the vertical distance from ground level to the level
198 at which the abutment is assumed to rotate; d'_d is the wall deflection at depth $H/2$ below ground level; C is

199 a dimensionless coefficient equal to 20 for foundations on loose soils with Young's modulus $E \leq 100$ MPa,
 200 and 66 for foundations on rock or soils with $E \geq 1000$ MPa, and which may be determined by linear
 201 interpolation for values of between 100 MPa and 1000 MPa; $K_{p;t}$ is the coefficient of passive earth pressure
 202 used in the calculation of K_d^* .

203 Design guidance for IBs is developing worldwide with a particular focus on the effect of thermal loading.
 204 However, there are still unanswered questions related to longer-term effects due to cyclic loading, notably
 205 does the earth pressure distribution change after many years of thermal cycling loading, and should the
 206 cycling loading history be considered in the estimation of the lateral pressure distribution behind the
 207 abutment?

208 It is evident, therefore, that the design methods provided in guidelines are characterised by significant
 209 uncertainty on the degree of conservatism embedded in the methods and lack consistency between
 210 countries. This emphasises the need for further investigation both under controlled condition in laboratories
 211 and via monitoring of IBs in the field, notably focussing on the abutment and associated backfill behaviour
 212 during a large number of repetitive cycles of displacement.



213
 214 *Figure 4. Earth pressure distributions for abutments that can accommodate thermal expansion by rotation*
 215 *and/or flexure (from PD6694, 2011), where K_0 is the coefficient of earth pressure at rest; H is the vertical*
 216 *distance from ground level to the level at which the abutment is assumed to rotate; γ is united soil weight;*
 217 *z is the soil depth; K^* is the design value of the earth pressure coefficient for expansion.*

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Table 1. Summary information of design guidance. (Note that limit equilibrium methods cannot predict distributions of passive pressures with depth. Accordingly, additional assumptions are needed to predict shear forces and bending moments at the two end of the wall).

Design guidance	Region	Estimation of earth pressures	Limiting Design Criteria
AASHTO LRFD, 2012	USA	The earth pressure coefficient variations are a function of structural displacement from experimental data and finite-element analyses, leading to a quasi-linear relationship	The limiting design criteria varies in different states. In 1980, American Federal Highway Association (FHWA) recommended: steel bridge - 90m; cast-in-place concrete bridge - 150m; post-tensioned bridges - 183m.
NCHRP, 1991		Limit equilibrium solutions based on log spiral failure mechanisms for standard backfill configurations (loose, medium and dense sand)	
NAVFAC, 1982		Limit equilibrium solutions based on log spiral failure mechanisms for standard backfill configurations (loose and dense sand)	
U.S. Department of Navy, 1982		Terzaghi's log spiral wedge theory to determine passive soil pressure coefficient	
Massachusetts Bridge Manual, 1999		Provided the equations (according to full-scale wall tests) to calculate the design earth pressure distribution behind the abutment of IABs	
Canadian Geotechnical Society, 1978	Canada	The soil pressure coefficients are based on the thermal movement of the model, vary with abutment rotation.	Different provinces have their own design guidance. For example, Alberta limited the span of IABs to 100m, with skew angle less than 20 degrees. Ontario limited the height of the abutment to 7m and length of wingwall to 6m.
PD6694,2011	UK	Limit equilibrium approach and SSI analysis	Span length - 60m; skew - 30 degree; the characteristic thermal movement of the end of the deck is less than or equal to 40 mm.

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226

227

228 3. Field monitoring of IBs

229 Field monitoring data from in-service IBs is significant both to inform and improve future design guidance,
230 and to refine experimental and numerical research. Many IBs globally are currently being monitored, see
231 [Table 2](#) for a general overview of significant monitoring studies. One of the monitored IABs is the
232 Manchester Road Overbridge between Denton and Middleton: two side-by-side 40m span IBs with no skew
233 and 7m high abutments carrying the A62. The strain in, and the earth pressure acting on, the abutments
234 were monitored during construction and throughout the first two years of service. The first bridge was a
235 conventional portal frame structure retaining granular backfill, while the second was constructed with
236 contiguous bored pile abutments founded on glacial till. As the bridge deck expanded, lateral stresses
237 increased, demonstrating a strong correlation between lateral stresses and bridge temperature ([Barker and](#)
238 [Carder, 2000](#)).

239 Similarly monitored was a two-span, skewed IB of 50 m total length consisting of pre-stressed concrete
240 beams and cast in-situ deck structurally connected to full height, 9m high abutments founded in magnesian
241 limestone over the M1-A1 Link Road at Bramham Crossroads, North Yorkshire. The field measurements
242 (displacements of the abutment and deck; strains in the abutment and deck; earth pressures on the
243 abutment) were recorded during construction and over the first three years of service. The measured lateral
244 earth pressures after backfilling were consistent with predictions using the coefficient of earth pressure at
245 rest (K_0), calculated based on the estimated friction angle (ϕ'), while they increased slightly for each of the
246 following summers ([Barker and Carder, 2001](#)).

247 The results from both monitoring campaigns were invaluable, yet they only cover a relatively short period
248 after construction whereas longer-term monitoring would be needed to determine the expected pattern of
249 significant earth pressure escalation after more seasonal cycles; this would also have provided a better
250 return on investment from the instruments installed ([Barker and Carder, 2000; 2001](#)).

251 A 15-degree skew, two-span IB of 90.9 m total length with 2.88 m high abutments in Trenton, New Jersey
252 (USA), was monitored for a year. Abutment strains and soil pressures behind the abutment were monitored
253 by the New Jersey Department of Transportation when revising the design specifications for integral bridges
254 ([Hassiotis et al., 2005](#)). A steady build-up of soil pressures behind the abutment was observed.

255
 256 A no-skew three-span IB of 82.3 m total length with 3.05 m high abutments spanning the Millers River
 257 between the towns of Orange and Wendell, USA, was monitored from 2002 to 2004, including longitudinal
 258 and transverse bridge displacements, backfill pressure distribution behind the abutment and abutment
 259 strains. The peak earth pressure at 2.5 m from the abutment top was observed to increase annually from
 260 245 kPa (2002) to 280 kPa (2003) and 315 kPa (2004); similar earth pressure increases were observed at
 261 other depths behind the abutment (Brena et al., 2007).

262 The Van Zylsprit River Bridge (a five-span IB of 90.45 m total length with no skew and 6.6 m high
 263 abutments, located on the N1 in South Africa) exhibited a maximum earth pressure significantly (~1.75
 264 times) higher than the at rest pressure (Skorpen et al., 2018).

265 *Table 2. Summary information of monitored IABs*

Reference	Location	Span length (m)	Skew degree	Hight of abutment (m)	Key monitoring findings
Barker and Carder, 2000	Manchester, UK	40	0	7	first two years of service, measured lateral stresses increased
Barker and Carder, 2001	North Yorkshire, UK	50	skewed	9	first three years of service, measured lateral earth pressures increased slightly for each of the following summers
Hassiotis et al., 2005	Trenton, New Jersey, USA	90.9	15	2.88	A steady build-up of soil pressures behind the abutment was observed
Brena et al., 2007	Millers River, USA	82.3	0	3.05	The peak earth pressure at 2.5 m from the abutment top was observed to increase annually.
Skorpen et al., 2018	Van Zylsprit River, South Africa	90.45	0	6.6	First of year of service, a maximum earth pressure significantly (~1.75 times) higher than the at rest pressure

266
 267 It is clear from the published literature that there is no more than ten years of reliable monitoring data
 268 available for IBs, whereas backfill stress measurements are required for a bridge that has been in service
 269 for more than a decade (Lock, 2002). It is currently unclear whether earth pressures would continue to

270 increase, or increase asymptotically, or level off to a steady value towards the end of the bridge's service-
271 life (implying a hypothetical need for a 120-year observation period; [Yap, 2011](#)). Longer-term monitoring
272 campaigns, notably focussing on the lateral soil pressure behind the abutment and incorporating
273 redundancy to allow for instrumentation failures, are therefore essential; linking the data feeds to digital
274 twins would further improve understanding of IB behaviour, improve designs and inform maintenance
275 strategies.

276 **4. Previous laboratory experimental research on IBs**

277 **4.1 Lateral earth pressure**

278 Increases in IB backfill pressure or lateral earth pressure, which is related to the soil stiffness and strength
279 and is dominated by the compaction of the granular backfill, have been confirmed by cyclic triaxial tests on
280 Leighton Buzzard Sand that simulated the stress path that a typical IB abutment might impose on its
281 retained soil ([Xu, 2005](#)). In a centrifuge model study of a spread-base integral bridge abutment assembled
282 in a (677 × 192 × 535 mm) strongbox, the measured lateral earth pressure increased with the amplitude of
283 the passive displacements and the number of cycles, but at a decreasing rate ([Ng et al., 1998](#)). This
284 progressive increase in lateral stresses was also observed when the active state was reached at the end
285 of each cycle in laboratory triaxial tests on specimens of Leighton Buzzard sand subjected to the stress
286 paths and levels of cyclic straining that typical IB abutments might impose on its retained soil ([Clayton et](#)
287 [al., 2006](#)). Tapper and Lehane ([2005](#)) describe a centrifuge experiment on a pinned base abutment in a
288 (510 × 200 × 245mm) strongbox characterised by increasing displacements (d/H 0.10%, 0.40% and 1.26%),
289 which showed that lateral stress did indeed increase until the passive limit was reached. In small-scale
290 (1140 × 570 × 300 mm) 1g testing, the lateral stress first increased significantly (around 25 cycles), then
291 the increase slowed (around 50 cycles), approaching asymptotically a steady-state condition ([England et](#)
292 [al., 2000](#)). This is anticipated, as the vertical effective stresses are approximately constant, so an
293 unbounded increase in lateral stresses is impossible, requiring an infinite magnitude of shear stress within
294 the backfill.

295 Centrifuge tests in a (677 × 192 × 535 mm) strongbox by [Springman et al. \(1996\)](#) used embedded and
296 spread-base abutments retaining Leighton Buzzard sand; they observed that the rate of stress increase on

297 the back of the abutment was much reduced after the first 20 cycles. The upper limits of the stress
298 escalation, however, are not well known (England et al., 2000). This earth pressure escalation was
299 attributed to two distinct mechanisms: the arching effect at small amplitudes and granular flow at large
300 amplitudes. The arching mechanism reduces the vertical stresses acting on the soil behind the lower half
301 of the wall, resulting in lower horizontal earth pressures at this point. A dominant arching mechanism relates
302 to small wall rotations while a dominant flow mechanism relates to large wall rotations (Tsang et al., 2002).
303 The flow mechanism allows a continuous deformation of the soil mass in one direction. The build-up of
304 lateral pressure was explained by the flow of granular materials during cyclic loading, known in the literature
305 as strain ratcheting (Hassiotis et al., 2005). The significant pressure build-up was attributed to sand particle
306 flow and densification due to cyclic loading, as well as the shearing of dense sand during bridge expansion
307 (Khodair and Hassiotis, 2005).

308 There seems to be agreement based on the published evidence that the lateral pressure behind an IB
309 abutment increases with sufficient displacement of the abutment under thermal loading. However, it
310 remains unclear whether the lateral pressure behind the abutment will continue building up at a specific
311 rate eventually stabilising. Furthermore, the different soil types and construction conditions make this
312 situation more complex. Therefore, monitoring of lateral soil pressure behind abutments is needed to obtain
313 a full understanding of IB behaviour under thermal loading. An overview of the main features of
314 experimental studies on earth pressures in IABs is provided in Table 3.

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Table 3. Dimensions of available model tests

Model	h [mm]	test type	aspect ratio				abutment material	backfill material	constraint abutment
			w/h	t/h	h/H	L/h			
England et al. 2000	570	1g pseudo-static	0.53	0.035*	1	2	metal	Leighton Buzzard	Fixed-hinged
Springman et al. 1996	110/115.9	60g centrifuge	1.88/162	0.099/0.085	0.45/0.53	2.9/2.5	dural/steel	Dry sand	Embedded/spread-base
Cosgrave and Lehane 2003	1000	1g pseudo-static	0.3	0.025	1	2.61	mild steel plate	Dry siliceous sand	hinge
Lehane 2011	160/200	(20; 25; 37.5; 40) g centrifuge	0.8/1	0.1/0.08	0.65/1	3.19/2.55	aluminium	Fine sand/ Glass ballottini/ High-OCR kaolin	hinge

h: height, w: width, t: thickness of the abutment; H: height, L: length of the backfill

*Estimation from the diagram proposed in the paper

321

322

323 **4.2 Backfill settlement**

324 Soil settlement has been observed when IBs are subjected to cyclic loading in centrifuge models of a
325 spread-based abutment (Ng et al., 1998) and scale-model retaining walls (England et al., 2000), some
326 authors even observed a gap developing between the soil behind the abutment and the wall (David and
327 Forth, 2011). The significant settlement behind the abutment reported by Ng et al. (1998) was attributed to
328 soil densification, strain ratcheting, horizontal sliding and the rocking motion of the abutment, while
329 Springman et al. (1996) warned against using loose backfill behind an IB abutment to prevent excessive
330 soil settlements. Lock (2002) noted that settlement due to thermal displacement of the IB deck is often
331 addressed by incorporating an approach slab, whereas Hoppe (1999) suggested this to be unnecessary if
332 the backfill is properly compacted.

333 The UK Design Manual for IBs (DMRB; BA42/96, 2003) does not mention the use of approach slabs,
334 although backfill compaction is recommended to limit the soil settlement due to thermal displacement of the
335 structure. Indeed, a survey of the UK's Highway Agency maintenance records of existing IBs revealed that,
336 aside from isolated cases, most bridges showed no settlement problems (Yap, 2011); other field studies
337 produced similar findings, with very few reporting soil settlement issues (Lock, 2002), emphasising the need
338 for, and effectiveness of, good control of compaction specifications.

339 **4.3 Effect of soil backfill**

340 In the UK, free-draining backfill is specified in DMRB (BA42/96, 2003) as well-graded granular material with
341 particle sizes up to 75 mm (gravel), which could include constituents such as natural gravel, natural sand,
342 crushed gravel, crushed rock, crushed concrete, slag or chalk. It further specifies representative values of
343 peak effective cohesion (c'_{peak}) and peak effective friction angle (φ'_{peak}) should be based on the compaction
344 to 95% of the maximum dry density in accordance with BS1377: part 4 (BSI 1990) using the vibrating
345 hammer method. The zone of granular backfill should extend from the bottom of the abutment wall to at
346 least a plane inclined at 45° to the wall. According to Al-Ani et al. (2018), the backfill behind the abutment
347 should be compacted over at least the height of abutment and vertically below the bottom of the abutment
348 for about 25% of the abutment height.

349 Shah et al. (2008) state that the magnitude and mode of deformation of the backfill, the overall soil response
350 and the overall structural response are all heavily influenced by the level of compaction in the granular fill
351 behind the abutment, along with the relative flexural stiffness of the bridge deck, the abutment wall and any
352 foundation piles, the lateral pressure of the soil behind the wall, and the confining stress level in the soil.
353 This complex set of interdependencies is further complicated by lateral earth pressure build-up in granular
354 being not solely be due to densification, but readjustment of the soil fabric due to particles reorienting under
355 cyclic loading or straining (Fleming and Rogers, 1995), and hence compaction processes should replicate
356 this action (i.e. using a vibrating roller rather than vertical compaction technology). Particle shape is
357 therefore an additional consideration since it influences this readjustment in soil fabric (Yap, 2011).

358 The boundaries of design are being pushed further with the use of innovative backfill materials (e.g. elastic
359 inclusions – a block of elastic material placed between the abutment wall and the retained soil) and
360 approach slabs – such as in a US IB of 300m total length that is performing well without cracking and
361 settlement of the pavement (Frosch, 2002). However, standard guidance on design and detailing of
362 approach slabs (e.g. the connection to the abutment backwall, and the interface between the approach slab
363 and approach fills) is lacking.

364 It is evident that a focus on backfill compaction (intensity, rotation of principal stresses, layer thickness and
365 confinement) could lead to decrease the build-up of pressure on the IB abutment and substantially avoid
366 backfill settlement. However, backfill compaction is not straightforward to control in IB construction
367 processes, therefore poorly-compacted backfill should be investigated alongside well-compacted granular
368 backfill taking cognisance of material types and gradings used in road foundations to limit permanent
369 deformation.

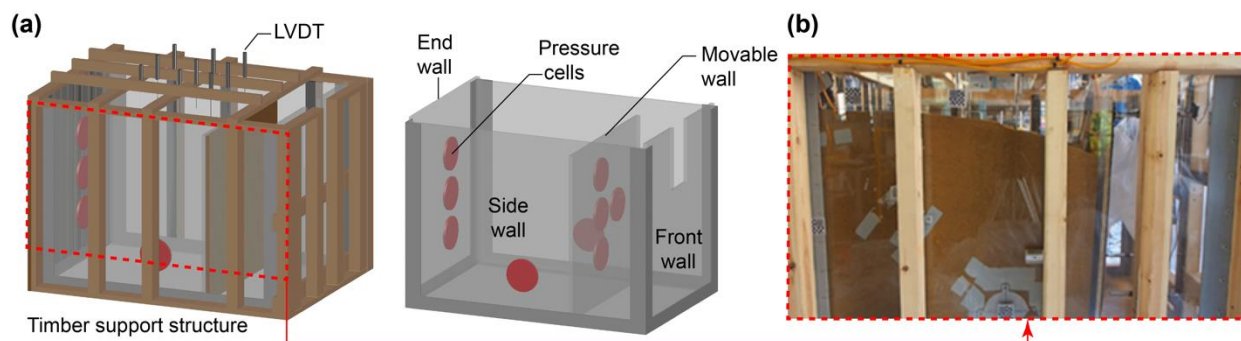
370 **5. PLEXUS pump-priming experimental campaign**

371 To investigate the soil-structure interaction uncertainties related to the backfill behaviour behind IBs and
372 establish the efficacy of different sensing technologies, a PLEXUS 1g small-scale soil box experimental
373 campaign was devised, thus also paving the way for experimentation at or near full-scale in the Soil-
374 Foundation-Structure Interaction Laboratory (SoFSI) at the University of Bristol.

375 The PLEXUS rig was designed to simulate the effect on the backfill from abutment displacements due to
376 seasonal expansion and contraction of the bridge deck. The monitoring regime included lateral stresses
377 behind the abutment wall (pressure cells), the backfill surface displacement (LVDTs) and backfill soil
378 deformation behind the abutment (Particle Image Velocimetry, PIV). Initial tests included the backfill
379 material being loaded by a moving abutment wall having two different relative stiffnesses (i.e., flexible and
380 rigid abutments), the displacements replicating horizontal thermal loading conditions associated with
381 increasing cyclic displacements and multiple-cycle constant-displacement histories.

382 **5.1 Experimental configuration**

383 The 1525 × 1050 × 1150 mm test box accommodated the loading system (actuator) and a 1000 × 1000 ×
384 1000 mm specimen of backfill. A 1000 mm high moveable wall was hinged at the bottom of the soil box to
385 simulate an IB abutment able to rotate about its base. The movable wall consisted of a 25 mm Perspex and
386 25 mm timber composite to simulate a flexible abutment wall, while the rigid movable wall consisted of a
387 25 mm Perspex, 25 mm timber composite, 50 mm aluminium frame and 25 mm timber composite producing
388 a sandwich configuration. Perspex was used for the box wall to enable PIV observations of backfill
389 displacements, while the remainder of the rig was designed without metal components to facilitate future
390 trialling of a ground penetration radar as a monitoring tool (see [Figure 5](#)). The abutment wall, end wall and
391 side wall were instrumented with pressure cells, while LVDTs were used to measure surface backfill
392 displacements. The backfill consisted of uniform Leighton Buzzard sand fraction B (see [Fiorentino et al.](#)
393 [2021](#)).



394
395 *Figure 5. (a) an annotated 3D diagram of the test box, (b) the test box filled with Leighton Buzzard (LB)*
396 *sand.*

397 **5.2 Thermal loading**

398 Thermal loading from temperature-induced cyclic expansion and contraction of the bridge deck was
 399 simulated by push-pull pseudo-static motion of the moveable wall, its displacement being controlled by the
 400 actuator mounted 870 mm above the wall base. In Test#1, the flexible abutment wall was subjected to 12
 401 loading cycles with a loading rate of 0.5 mm/s (to simulate static thermal loading, [Springman et al., 1996](#);
 402 [Lehane, 2011](#)), each cycle lasting at least 40 seconds. The cyclic displacements at the top of the movable
 403 wall started at ± 5 mm, with increments of ± 5 mm every two cycles, to reach ± 30 mm (drift $\sim 3.5 \times 10^{-2}$; see
 404 [Table 4](#)). In Test#2, the rigid abutment wall was subjected to 59 'loading' cycles with a loading rate of 1.0
 405 mm/s and cyclic displacements at the top of wall fixed at ± 30 mm for each cycle (1 mm/s was considered
 406 slow enough to simulate static thermal loading). The 30mm equals the seasonal deck movement (one end)
 407 of a IAB in London with a 131m length concrete deck or a 91m length of steel deck ([England et al. 2000](#)).

408 **5.3 Instrumentation layout**

409 The instrumentation employed consisted of TPC-4000 series Total Earth Pressure Cells (TEPCs) to
 410 measure lateral stresses, and Linear Voltage Differential Transducers (LVDTs) and a high-resolution
 411 camera on the side of the test-rig to measure displacements. The TEPCs are designed to measure total
 412 pressure (combined effective stress and pore water pressure) in soils and at soil-structure interfaces yet,
 413 as the Leighton Buzzard Sand was dry, they directly provided effective stress measurements. The locations
 414 of the three end wall TEPCs (1-3), four moveable wall TEPCs (6-9) and sidewall TEPCs (4 and 5) are
 415 shown in [Figure 6](#).

416 *Table 4. Summary information for Tests #1 and #2.*

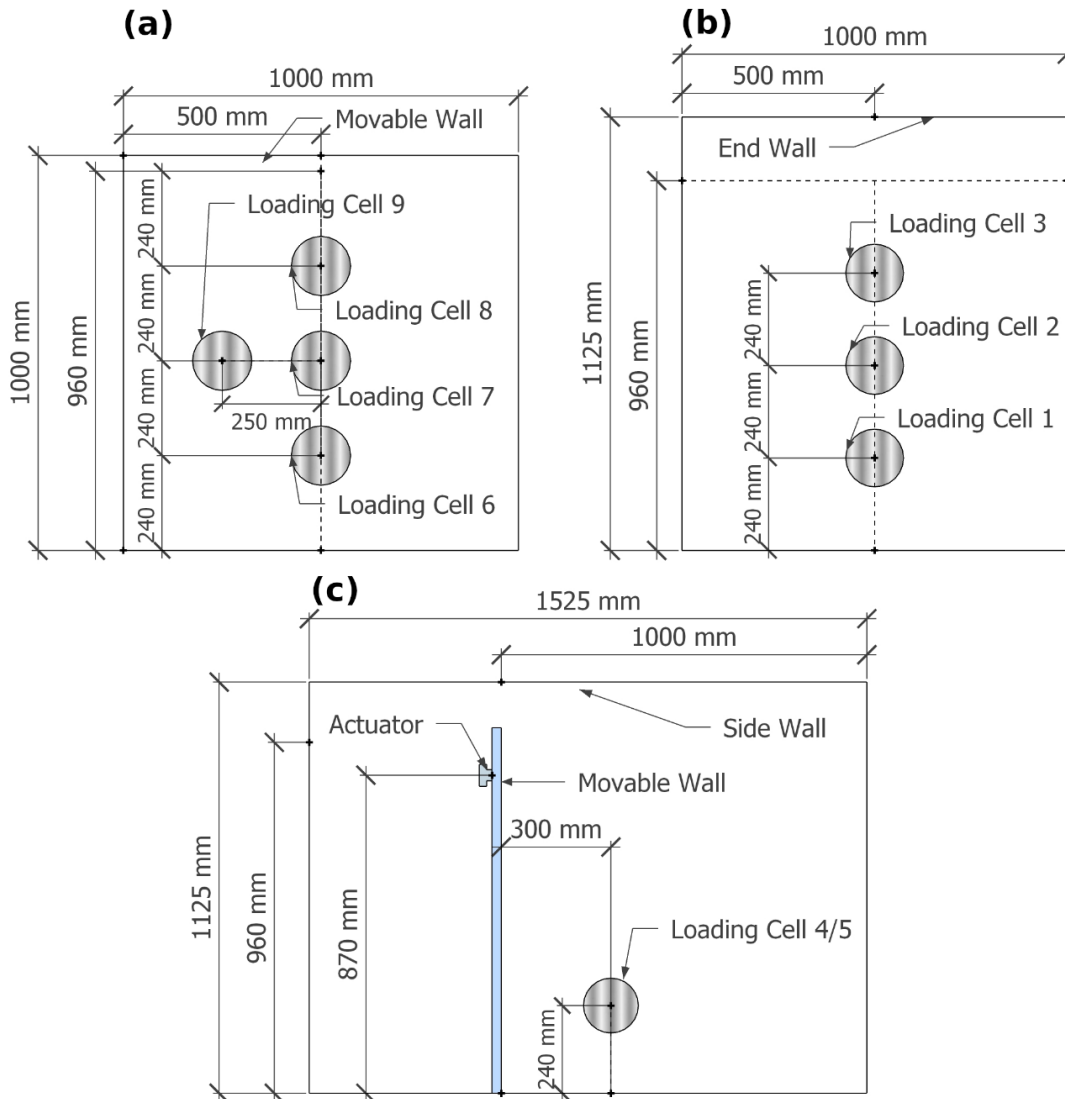
Test ID	Abutment Wall	Total Cycles	Loading Rate [mm/s]	Displacement history [mm] & Drifts
#1	Flexible Perspex + Timber ¹	12	0.5	$2 \cdot \{\pm 5\text{mm}; \pm 10\text{mm}; \pm 15\text{mm}; \pm 20\text{mm}; \pm 25\text{mm}; \pm 30\text{mm}\}$ $2 \cdot \{(\pm 5.7; \pm 11.5; \pm 17.2; \pm 23.0; \pm 28.7; \pm 34.5) \times 10^{-3}\}$
#2	Stiff Sandwich section ²	59	1.0	$59 \cdot \{\pm 30\text{ mm}\}$ $59 \cdot \{\pm 34.5 \times 10^{-3}\}$

¹ 25 mm Perspex + 25 mm Timber

² 25 mm Perspex + 25 mm Timber + 50 mm Aluminium frame + 25 mm Timber

417

418 **Figure 7** shows the positions of the nine LVDTs (1-9) placed in three rows on the backfill surface and four
 419 LVDTs (11-13) measuring the moveable (abutment) wall displacement. The high-resolution camera (Canon
 420 70D 5472*3648 pixels) focussed on the Perspex sidewall to record ‘full-field’ backfill deformation using the
 421 PIV method, regarded as slow “fluid motion” (Stanier et al., 2010).



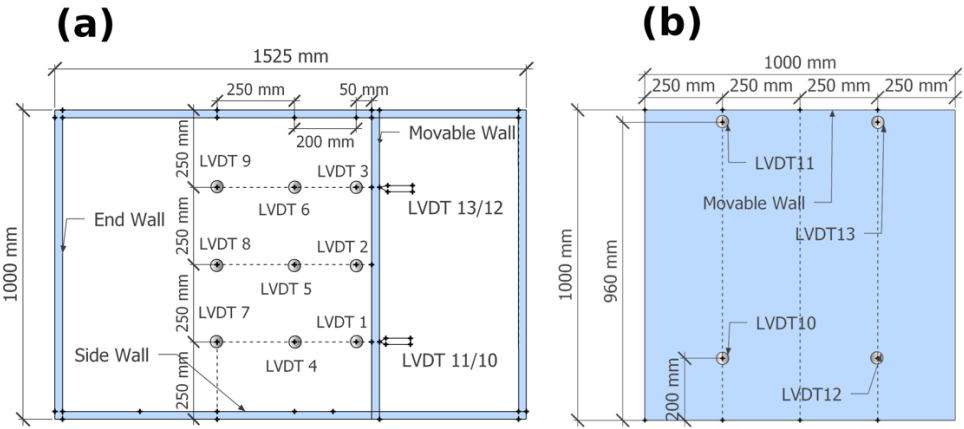
422

423 *Figure 6. The layout of the pressure cells in the test box: (a) movable wall, (b) end wall, (c) sidewall*
 424 *including exact position of actuator.*

425 **5.4 Backfill**

426 The backfill material selected was Leighton Buzzard Sand (LBS) fraction B (Lings and Dietz, 2004;
 427 Kloukinas et al., 2015; Fiorentino et al., 2021), having dry densities in Test #1 and Test #2 of 1.48 Mg/m³

428 and 1.44 Mg/m³, respectively. The minimum and maximum dry densities for the LBS were determined as
 429 1.48 Mg/m³ and 1.65 Mg/m³. The density value in Test #2 obtained is slightly lower than the minimum
 430 provided by [Fiorentino et al. \(2021\)](#) but this is likely due to the absence of compaction and no control of
 431 density at the different filling stage leading to an overall figure that is about right within the tolerance of the
 432 process implemented experimentally. The specific gravity of LBS grains was 2.65, while the minimum and
 433 maximum void ratios (e_{min} and e_{max}), were 0.35 and 0.83, respectively ([Fiorentino et al., 2021](#)). To achieve
 434 a uniform, relatively loose LBS specimen, the sand was pluviated into the soil box in three layers, with
 435 levelling (but no compaction) applied after each pour.



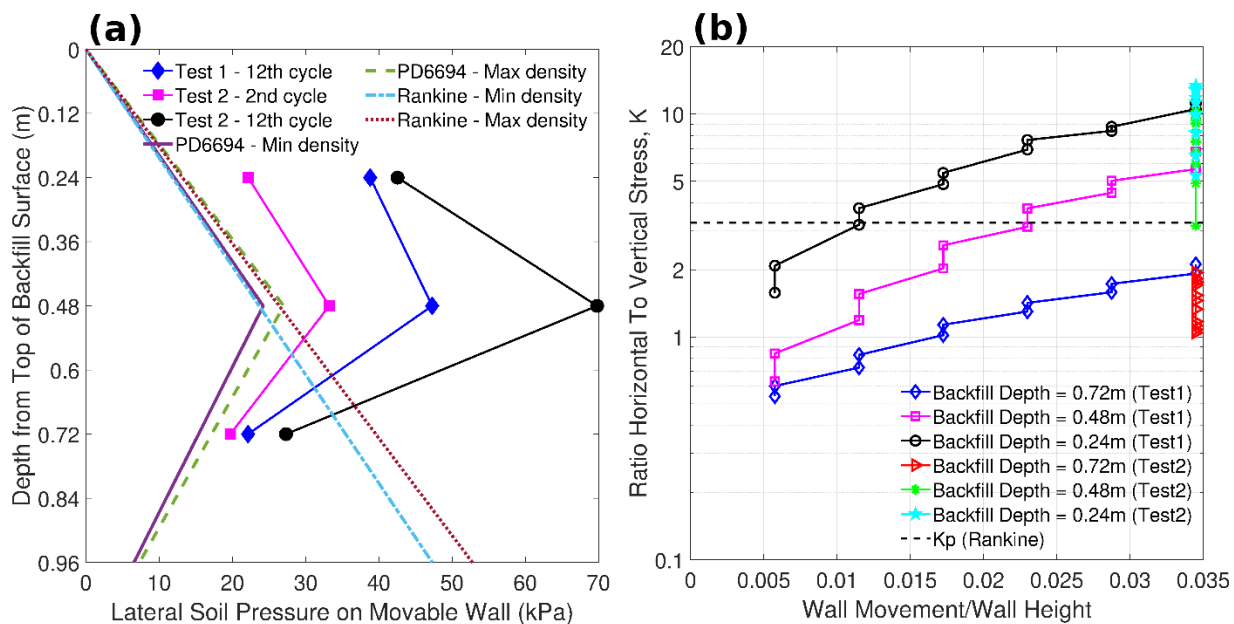
436
 437 *Figure 7. The layout of the LVDTs (a) plan view of the test box, (b) front view of the movable wall.*

438 **5.5 Results**

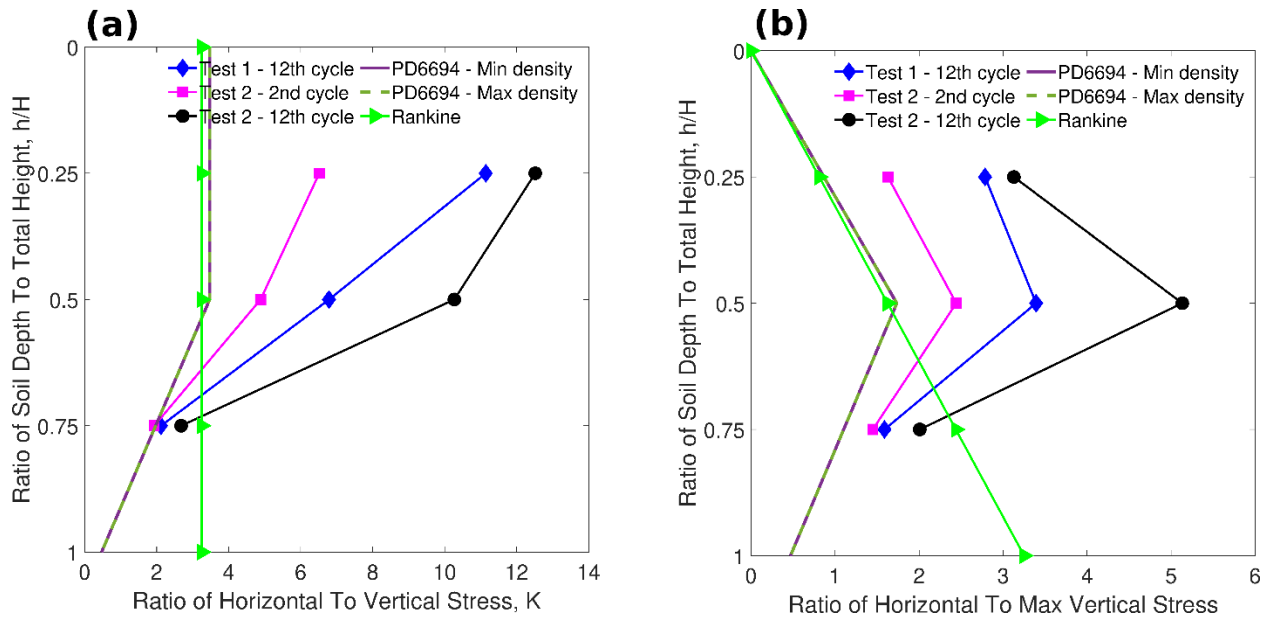
439 The two tests have multiple differences (i.e., wall stiffness, 'loading' rate, displacement history increasing
 440 or kept constant), making a systematic comparison difficult. Nevertheless, in [Figure 8a](#), a preliminary
 441 comparison is proposed between the earth pressure distributions obtained using Rankine theory and
 442 PD6694 (see [Figure 4](#) and [Equation 4](#)) and the passive-like pressure recorded at three instants: (a) at cycle
 443 12 of Test #1 (i.e. the second cycle at +30 mm after the increasing displacement history), (b) at cycle 2 of
 444 Test #2 (i.e. the second cycle at +30 mm), and (c) at cycle 12 of Test #2 (i.e. the twelfth cycle at +30 mm).
 445 The vertical distance from ground level to the assumed point of rotation of the abutment (H) is 0.96 m, while
 446 the wall deflection at depth $H/2$ below ground level (d'_a) was 0.7 times the horizontal movement of the end
 447 of the bridge deck. C is 20 assuming that the Young's modulus of the sand is less than 100 MPa. The critical
 448 friction angle was taken as $\phi_{cs} = 32^\circ$ and the elastic modulus as 20 MPa ([Ng et al., 1998](#)). The coefficient

449 of passive earth pressure ($K_{p;t}$) was obtained through linear interpolation for values of ϕ_{cs} between
 450 30° ($K_{p;t} = 4.29$) and 35° ($K_{p;t} = 5.88$) for a non-smooth vertical wall with $\delta/\phi' = 0.5$ retaining a horizontal
 451 backfill (see Table 8 in PD6694 2011).

452 The lateral soil pressures measured in both tests were larger than the pressures calculated according to
 453 Equation 4 from PD6694 (see Section 2) using the maximum and minimum LBS densities. This may be
 454 caused by the specific configuration of the experiments and the influence of the backwall (as the distance
 455 between the abutment and the backwall was 1 m when at least 1.7 m would be necessary to develop a
 456 complete passive failure wedge). However, the shape of the lateral pressure distribution on the abutments,
 457 resulting from the three experimental measurement points, mimics the shape of the envelope proposed by
 458 PD6694. The lateral pressure on the abutment after the 12th cycle in Test #2 was larger than that after the
 459 12th cycle in Test #1, attributed to the larger cyclic lateral displacement in Test #2 (an expected result)
 460 and/or the lower stiffness of the abutment wall in Test#1 (also an expected phenomenon).



461
 462 Figure 8. (a) Measured earth pressures and (b) ratio of horizontal to vertical stress when wall is moving
 463 into the backfill soil (passive).
 464



465

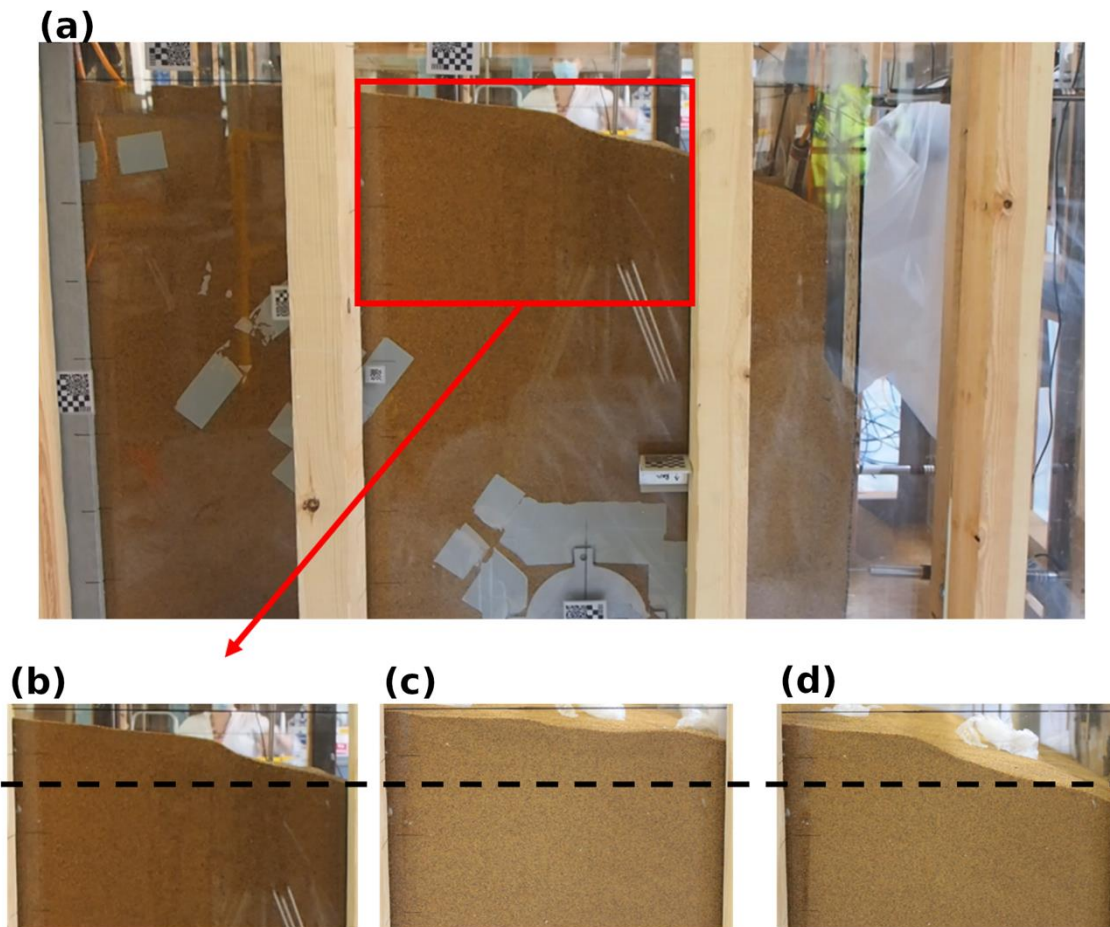
466 *Figure 9. Normalised distributions of earth pressures with depth: (a) x axis normalised by γz and (b) x*
 467 *axis normalised by γH represented against y axis normalised by total height of the soil ($H = 96$ cm).*

468 The lateral soil pressures on the movable wall in **Figure 8a** were normalised separately by the vertical
 469 stress, γz , where γ is unit weight, z is the soil depth (**Figure 9a**), and by the maximum vertical stress, γH ,
 470 where H is the total depth of the soil (**Figure 9b**), thereby making them scalable for general translation. The
 471 vertical axes of **Figure 9** are normalised by the total height of the backfill. The ratios of horizontal to vertical
 472 stress measured by the bottom pressure cell at cycle 12 in Test #1 and at cycle 2 in Test #2 were very close
 473 to that calculated from PD6694, while the pressure at cycle 12 in Test #2 is larger.

474 In Test #2, the lateral pressure on the stiffer abutment after 12 cycles was larger than after 2 cycles (all
 475 cycles consisting of ± 30 mm displacement). **Figure 8b** shows the rapid increase in lateral soil pressure with
 476 increasing number of cycles and displacements (up to cycle 12) in Test #1, and with constant displacement
 477 and increasing cycles in Test #2, compared with the theoretical passive Rankine value and comparative
 478 values suggested by NCHRP (1991) and NAVFAC (1982) shown in **Figure 3a**.

479 Backfill surface settlement is significantly smaller for the stiffer abutment after 2 cycles than after 12 cycles
 480 (**Figure 10**). The settlements rapidly increased with the number of cycles. The settlement behind the stiff

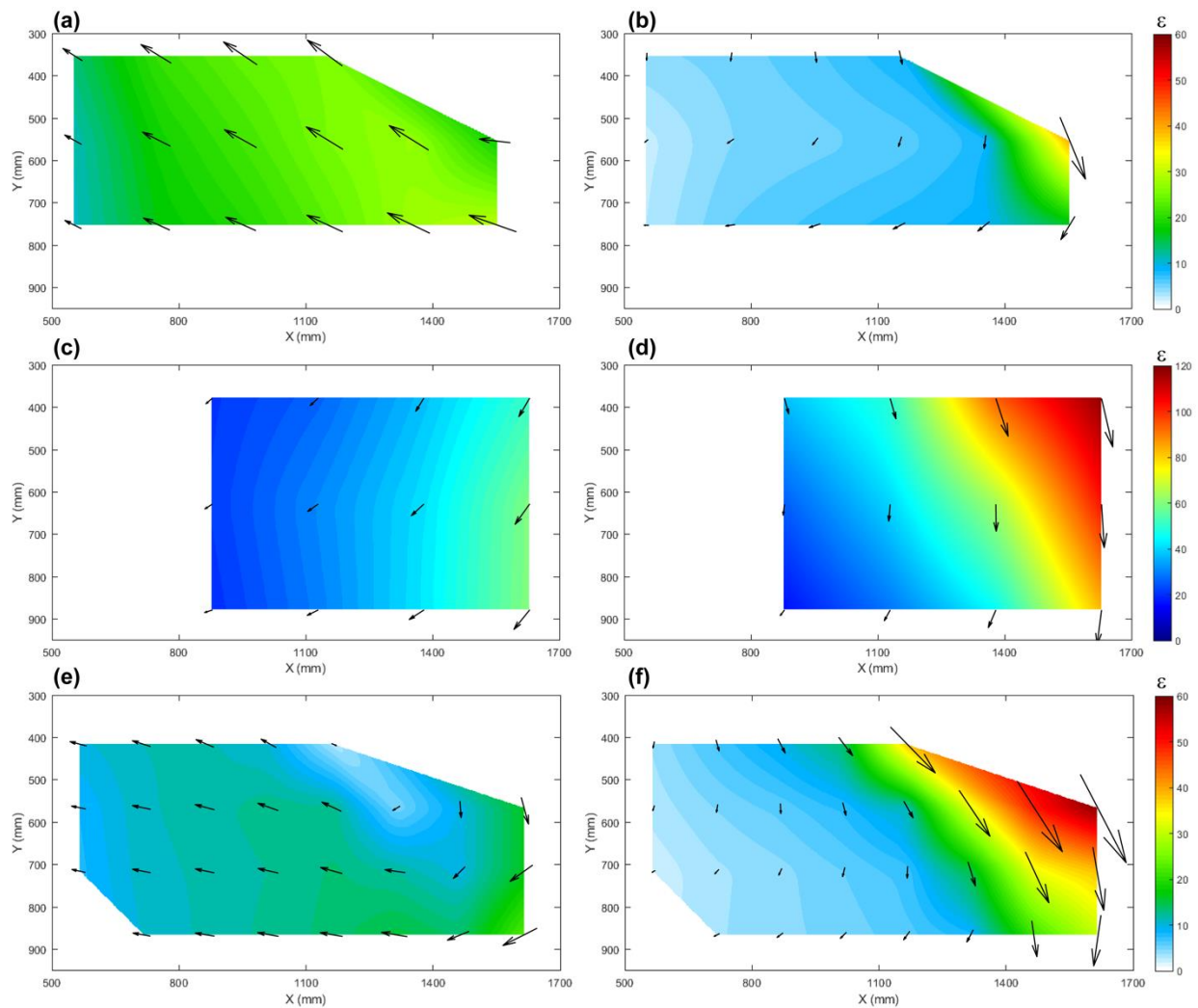
481 abutment after 12 cycles is slightly larger than for the 12th cycle behind the flexible abutment, attributed to
482 abutment stiffness and/or amplitude of cyclic loading.



483
484 *Figure 10. The settlement behaviour of the backfill, (a) Test #1 – 12th cycle, (b) Test #1 – 12th cycle*
485 *(zoomed-in), (c) Test #2 – 2nd cycle (zoomed-in), (d) Test #2 – 12th cycle (zoomed-in), the black dotted*
486 *line offers the same reference level for a better comparison.*

487 The densification of the backfill in the zoomed-in areas of **Figures 10b to 10d** was analysed using the
488 GeoRG PIV MATLAB analysis package ([Stainer et al. 2015](#)). As shown in **Figure 11** (where volumetric
489 strain value shown with the colour of contour and the black arrows only present the deformation direction
490 of the soil backfill), the deformation of the backfill after 12 cycles in Test #1 (**Figure 11a and 11b**) was larger
491 than that in Test #2 when the actuator was at maximum extension. In contrast, the opposite behaviour was
492 observed when the actuator was at its maximum contraction. The lower lateral soil pressure on the flexible

493 abutment than that on the stiff abutment was attributed to the backfill becoming denser in the stiff abutment
 494 test. The densification of the backfill after two cycles in the stiff abutment configuration (Figure 11c and 11d)
 495 is much larger than after 12 cycles (Figure 11e and 11f), thus indicating that the amplitude of the backfill
 496 densification decreases with increasing loading cycles in the same test.
 497 It is evident from these results that abutment stiffness, number of cycles, backfill material state and the
 498 magnitude of abutment horizontal displacement are key parameters in determining IB performance, and
 499 warrant further investigation in controlled experiments. Pressure cells and PIV measurements are
 500 particularly suitable to compare the performance of different test configurations.



501
 502 *Figure 11. Percentage volumetric strain (ϵ) and deformation direction (black arrows) of the soil backfill:*
 503 *Test #1 – 12th cycle (a) maximum extension position and (b) maximum contraction position; Test #2 – 2nd*

504 *cycle (c) maximum extension position and (d) maximum contraction position; Test #2 – 12th cycle (e)*
505 *maximum extension position and (f) maximum contraction position.*

506 **6. Conclusions**

507 This paper discussed the behaviour of integral bridges (IB's) under thermal loading by reviewing: (1) current
508 international design practices, and (2) lessons learnt from field monitoring cases and previous experimental
509 research. The soil pressure behind the abutment wall is a crucial factor for the design and performance of
510 integral bridges, while the backfill behind the abutments significantly influences performance. The PLEXUS
511 experimental campaign, described herein, demonstrated the efficacy of its monitoring processes in
512 establishing soil-structure interaction behaviour of integral bridge abutments under thermal loading and
513 identified key research needs. In particular, pressure cells and PIV provided useful data for performance
514 comparisons in laboratory environments, while settlements measurements proved less informative. The
515 research revealed a need for precise density monitoring of the backfill throughout the duration of the tests
516 and throughout the soil specimen. In the non-metallic PLEXUS test rig, this could be achieved by ground
517 penetration radar, x-ray tomography and/or similar techniques.

518 The small-scale tests have created results that are suitable for analytical and numerical validation, although
519 scaling effectiveness needs to be proven. Further, larger-scale physical model tests of integral bridge
520 abutments, using different types of backfill compacted to counter unwanted deformations due to ratcheting
521 (e.g. incorporating rotation of principal stresses) and to cover the variety of materials likely in practice, are
522 required to ensure improved sustainable and resilient designs of integral bridges.

523

524 **Data availability statement**

525 All data from the Plexus experimental campaign are available from the corresponding author by request

526

527 **Acknowledgements**

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531

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