

# Light $Z'$ Signatures at the LHC

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(Dated: Tuesday 20<sup>th</sup> September, 2022)

We propose a theoretical framework embedding a spontaneously broken  $U(1)'$  symmetry in addition to the Standard Model (SM) gauge group, from which a very light  $Z'$  state emerges, with both vector and axial (non-universal) couplings to fermions, able to explain the so-called Atomki anomaly, compliant with current measurements of the Anomalous Magnetic Moments (AMMs) of electron and muon as well as beam dump experiments while providing a distinctive  $pp \rightarrow \text{Higgs} \rightarrow Z'Z' \rightarrow 4l$  ( $l = e, \mu$ ) signal at the Large Hadron Collider (LHC), where the ‘Higgs’ label refers to the SM-like Higgs state discovered in 2012 or a lighter one. We finally show that the cross section for this process should be sufficiently large to afford one with significant sensitivity during Run 3 of the LHC.

A light neutral  $Z'$  boson (often dubbed a ‘dark photon’), with mass of order 17 MeV, provides a natural explanation for the clear anomaly observed by the Atomki collaboration [1] in the decay of excited states of Beryllium [2–7]. Furthermore, several studies have been conducted to investigate the effects of such light  $Z'$  on the AMM of the electron ( $a_e$ ) and muon ( $a_\mu$ ) as well as  $B$  anomalies such as  $R_{K^{(*)}}$  [8–15].

In this letter we analyse some LHC signatures of a light  $Z'$  associated with a non-universal  $U(1)'$  extension of the Standard Model (SM). This type of scenario has been shown to account for both the Atomki anomaly and  $a_{e,\mu}$  results [16]. In addition, we revisit the contributions of such light  $Z'$  to these observables to see how the most recent experimental results constrain the associated couplings.

We focus on a non-universal  $U(1)'$  extension of the SM in which the kinetic term in the Lagrangian is given by

$$\mathcal{L}_{\text{kin}} = -\frac{1}{4}\hat{F}_{\mu\nu}\hat{F}^{\mu\nu} - \frac{1}{4}\hat{F}'_{\mu\nu}\hat{F}'^{\mu\nu} - \frac{\eta}{2}\hat{F}'_{\mu\nu}\hat{F}^{\mu\nu}, \quad (1)$$

where  $\eta$  quantifies the mixing between the SM  $U(1)_Y$  and extra  $U(1)'$ . After the diagonalization of Eq. (1), the covariant derivative can be written as

$$\mathcal{D}_\mu = \partial_\mu + \dots + ig_1 Y B_\mu + i(\tilde{g}Y + g'z)B'_\mu, \quad (2)$$

where  $Y$  and  $g_1$  are the hypercharge and its gauge coupling while  $z$  and  $g'$  are the  $U(1)'$  charge and its gauge coupling. Further,  $\tilde{g}$  is the mixed gauge coupling between the two groups. The  $U(1)'$  symmetry is broken by a new SM singlet scalar,  $\chi$ , with  $U(1)'$  charge  $z_\chi$  and Vacuum Expectation Value (VEV)  $v'$ . The scalar potential for the Higgs fields can be written as

$$V(H, \chi) = -\mu^2|H|^2 + \lambda|H|^4 - \mu_\chi^2|\chi|^2 + \lambda_\chi|\chi|^4 + \kappa|\chi|^2|H|^2. \quad (3)$$

Here,  $H$  is the SM Higgs doublet while  $\kappa$  is the mixing parameter which connects that SM and  $\chi$  Higgs fields. After Electro-Weak Symmetry Breaking (EWSB), for

$\mu^2 = \lambda v^2 + \frac{1}{2}\kappa v'^2$  and  $\mu_\chi^2 = \lambda_\chi v'^2 + \frac{1}{2}\kappa v'^2$ , the Higgs mass matrix in the  $(h_2, h_1)$  basis can be written as

$$m_{h_2 h_1}^2 = \begin{pmatrix} 2\lambda v^2 & \kappa v v' \\ \kappa v v' & 2\lambda_\chi v'^2 \end{pmatrix}, \quad (4)$$

where  $h_2$  is dominantly the SM-like Higgs boson while the exotic state  $h_1$  is dominantly the singlet Higgs ( $\chi$ -like). In this work, we consider  $m_{h_1} < m_{h_2}$  and the  $h_1 \rightarrow Z'Z'$  decay rate  $\geq 0.95$ , which are compatible with experimental results. The SM-like Higgs boson  $h_2$  can decay to  $Z'$  pairs too, proportionally to  $\kappa$ . Moreover, the spontaneous breaking of the  $U(1)'$  symmetry implies the existence of a mass term  $m_{Z'} = g'z_\chi v'$ . Thus, if  $g' \sim \mathcal{O}(10^{-4} - 10^{-5})$ ,  $M'_{Z'}$  would be of order  $\mathcal{O}(10)$  MeV. It is worth noting that we adopt non-universal charge assignments of the SM particles under  $U(1)'$ , as discussed in Ref. [16]. These assignments satisfy anomaly cancellation conditions, enforcing a gauge invariant Yukawa sector of the third fermionic generation and family universality in the first two while not allowing coupling between  $Z'$  and light neutrinos.

The Neutral Current (NC) interactions of this additional vector boson with the SM fermions are given as

$$\mathcal{L}_{\text{NC}}^{Z'} = -\sum_f \bar{\psi}_f \gamma^\mu (C_{f,L} P_L + C_{f,R} P_R) \psi_f Z'_\mu, \quad (5)$$

where Left (L) and Right (R) handed coefficients are written as

$$C_{f,L} = -g_Z \sin \theta' (T_f^3 - \sin^2 \theta_W Q_f) + (\tilde{g} Y_{f,L} + g' z_{f,L}) \cos \theta', \quad (6)$$

$$C_{f,R} = g_Z \sin^2(\theta_W) \sin(\theta') Q_f + (\tilde{g} Y_{f,R} + g' z_{f,R}) \cos(\theta'). \quad (7)$$

The parameters given in these expressions can be found in Ref. [16].

The contribution of this  $Z'$  gauge boson to the AMMs

of the charged leptons  $a_f$ , for  $f = e, \mu, \tau$  is given by [17]

$$\Delta a_f = \frac{m_f^2}{4\pi^2 m_{Z'}^2} \left( C_{f,V}^2 \int_0^1 \frac{x^2(1-x)}{1-x+x^2 m_\alpha^2/m_{Z'}^2} dx - C_{f,A}^2 \int_0^1 \frac{x(1-x)(4-x)+2x^3 m_f^2/m_{Z'}^2}{1-x+x^2 m_f^2/m_{Z'}^2} dx \right), \quad (8)$$

where  $C_{f,V} = \frac{C_{f,R}+C_{f,L}}{2}$  and  $C_{f,A} = \frac{C_{f,R}-C_{f,L}}{2}$ .

It is important to note that the contribution of the  $Z'$  to the AMMs of leptons is primarily determined by their vector and axial couplings as well as the mass of the  $Z'$  boson. Furthermore, the vector and axial couplings of the quarks are important in explaining the Atomki anomaly via the transition  ${}^8\text{Be}^* \rightarrow {}^8\text{Be} Z'$  [18]. In particular, the contribution of the quark axial couplings  $C_{q,A}$  in this transition is greater than that of the vector couplings  $C_{q,V}$  because the  $C_{q,A}$  and  $C_{q,V}$  terms are proportional to  $k/M_{Z'}$  and  $k^3/M_{Z'}^3$  (where  $k$  is the small momentum of the  $Z'$ ), respectively [19].

Parameter	Scanned range	Parameter	Scanned range
$g'$	$[10^{-5}, 5 \times 10^{-5}]$	$\lambda$	$[-0.132, -0.125]$
$\tilde{g}$	$[-10^{-3}, 10^{-3}]$	$\lambda_\chi$	$[-10^{-5}, -10^{-3}]$
$v_S$	$[0.1, 1] \text{ TeV}$	$\kappa$	$[10^{-6}, 10^{-3}]$

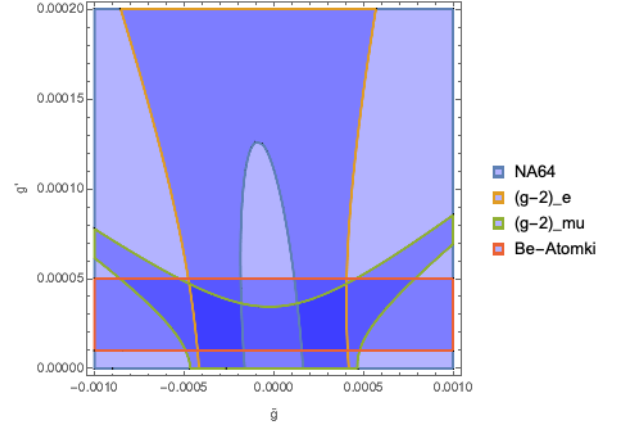
**TABLE I:** Scanned parameter space of our model.

In our numerical analysis, we have employed SPHENO 4.0.4 [20–22] generated with SARAH 4.14.3 [23, 24]. In Fig. 1, we show the portion of  $(g_p, \tilde{g})$  parameter space that satisfies the current experimental bounds from  $(g-2)_{e,\mu}$ , the  ${}^8\text{Be}^*$  anomaly and NA64 (as well as electron beam dump experiments) [25? – 27]. Here, the darkest shaded blue regions comply with all such constraints. During the scanning of the  $U(1)'$  parameter space, within the ranges specified in Tab. I, the Metropolis-Hastings algorithm has been used. After data collection, we implement Higgs boson mass bounds [29, 30] as well as constraints from Branching Ratios (BRs) of  $B$  decays such as  $\text{BR}(B \rightarrow X_s \gamma)$  [31],  $\text{BR}(B_s \rightarrow \mu^+ \mu^-)$  [32] and  $\text{BR}(B_u \rightarrow \tau \nu_\tau)$  [33]. We have also bounded the  $Z/Z'$  mixing to be less than a few times  $10^{-3}$  as a result of EW Precision Tests (EWPTs) [34].

The experimental constraints can be summarized as follows:

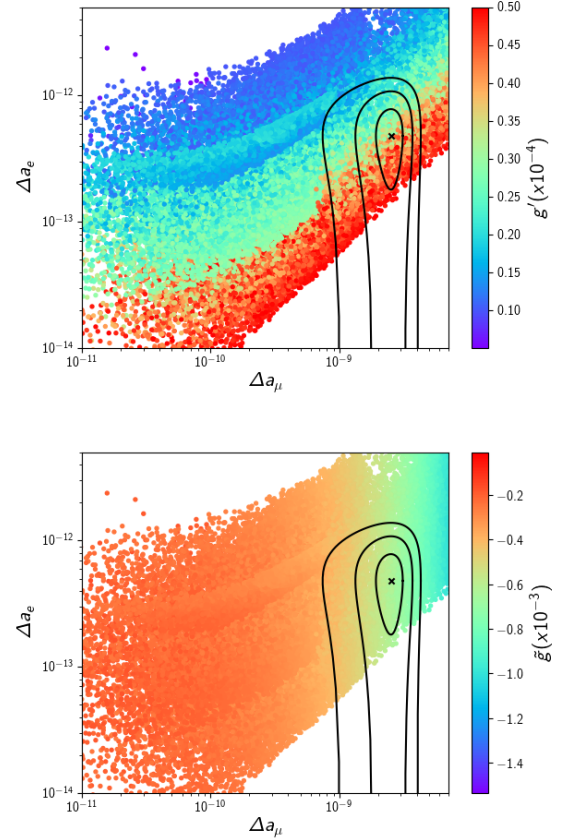
$$\begin{aligned} m_h &= 122 - 128 \text{ GeV (as our masses are lowest order),} \\ 2.99 \times 10^{-4} &\leq \text{BR}(B \rightarrow X_s \gamma) \leq 3.87 \times 10^{-4} \text{ (} 2\sigma \text{ tolerance),} \\ 0.15 &\leq \frac{\text{BR}(B_u \rightarrow \tau \nu_\tau)}{\text{BR}(B_u \rightarrow \tau \nu_\tau)_{\text{SM}}} \leq 2.41 \text{ (} 3\sigma \text{ tolerance),} \\ \Delta a_e &= (4.8 \pm 9.0) \times 10^{-13} \text{ (} 3\sigma \text{ tolerance),} \\ \Delta a_\mu &= (2.51 \pm 1.77) \times 10^{-9} \text{ (} 3\sigma \text{ tolerance).} \end{aligned} \quad (9)$$

Additionally, the cross section values for the given



**FIG. 1:** Allowed parameter space mapped on the  $(g', \tilde{g})$  plane for  $Z'$  mass of 17 MeV against four different experimental constraints.

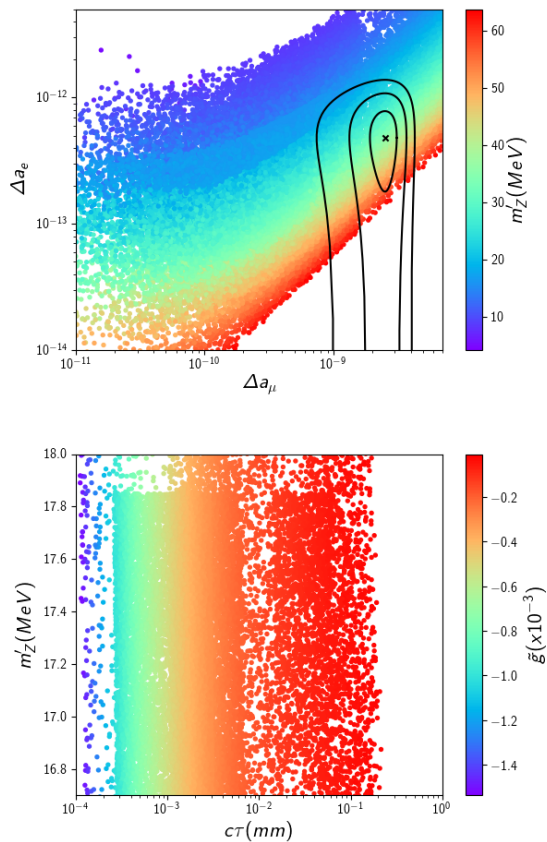
processes at the LHC have been calculated by using CalcHEP [35].



**FIG. 2:** Results for  $g'$  (top) and  $\tilde{g}$  (bottom) in terms of  $(g-2)_e$  vs  $(g-2)_\mu$ . Each solid line from inner to outer represents  $1\sigma$ ,  $2\sigma$  and  $3\sigma$  bounds from the experimental central values in Eq. (9).

## I. RESULTS

In this section, we will first present the dependence of  $\Delta a_\mu$  and  $\Delta a_e$  to the fundamental parameters  $g'$  and  $\tilde{g}$ . Fig. 2 depicts  $\Delta a_\mu$  vs  $\Delta a_e$ , where the color bars show  $g'$  (top panel) and  $\tilde{g}$  (bottom panel) parameters. Herein, one can learn about the favoured ranges of these parameters in order to obtain AMMs within their  $1\sigma$ ,  $2\sigma$  and  $3\sigma$  value. As seen from the plots, the experimental bounds of  $\Delta a_\mu$  and  $\Delta a_e$  within  $3\sigma$  allow for a narrow range in  $\tilde{g}$ , namely,  $-0.6 \times 10^{-3} \lesssim \tilde{g} \lesssim -0.4 \times 10^{-3}$  while  $g'$  lies in the range of  $0.2 \times 10^{-4} \lesssim g' \lesssim 0.5 \times 10^{-4}$ .



**FIG. 3:** Results for  $m_{Z'}$  in terms of  $(g-2)_e$  vs  $(g-2)_\mu$  (top) and for  $\tilde{g}$  in terms of  $m_{Z'}$  vs the proper lifetime of the  $Z'$  (for  $m_{Z'} \approx 17$  EV).

Now, let us focus on  $Z'$  properties, such as its mass  $m_{Z'}$  and proper lifetime  $c\tau$ . In the top panel of Fig. 3, we demonstrate how  $Z'$  mass solutions showed in the color bar correlate with  $\Delta a_\mu$  and  $\Delta a_e$ . As expected, the behavior of  $m_{Z'}$  is very similar to  $g'$  in the top panel of Fig. 2. Herein, our  $1\sigma$  solutions are excluded for  $m_{Z'} \approx 17$  MeV, the value satisfying the Atomki anomaly. Such  $Z'$  mass bound also puts an additional limit on  $g'$  and  $\tilde{g}$ , in addition to those already obtained from the AMMs in Fig. 2. We also examine the  $Z'$  lifetime since it is crucial to explore potentially displaced signatures at

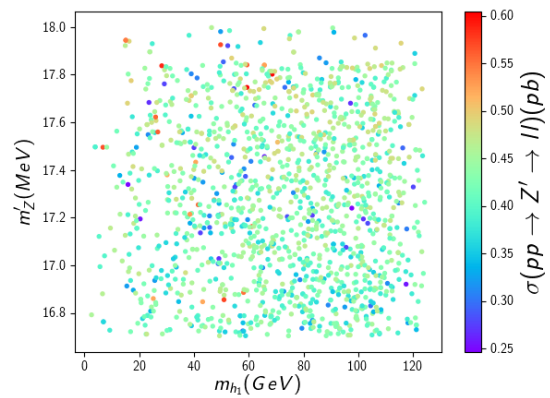
the LHC. The plot at the bottom of Fig. 3 showcases the proper lifetime of  $Z'$  in millimeters over the mass range  $16.7 \text{ MeV} \lesssim m_{Z'} \lesssim 18 \text{ MeV}$  while the color bar indicates  $\tilde{g}$ . As mentioned in Ref. [36], for small values of  $|\tilde{g}|$ , the  $Z'$  lifetime becomes longer. Considering the  $\tilde{g}$  solutions which fulfill all experimental conditions, the lifetime of the  $Z'$  should be  $\sim 10^{-3}$  mm, which is not sufficient to produce a displaced detector signal.

### A. $Z'$ production at the LHC

Now, we will study the collider signatures of our light  $Z'$  boson in three different channels at the LHC: Drell-Yan (DY) and  $Z'$  pair production through both SM-like Higgs  $h_2$  and exotic Higgs  $h_1$  mediation, wherein we consider both fully leptonic and semi-leptonic final states.

#### 1. Drell-Yan

At the LHC, the most favored process for a light  $Z'$  boson is the DY channel, where it can directly be generated via  $q\bar{q}$  fusion in  $s$ -channel. In Fig. 4, we present the dilepton production cross section via our light  $Z'$  resonance. Although the corresponding  $Z'$  production and decay rates are always large for  $m_{Z'} \approx 17$  MeV, the process is difficult to detect given the very light  $Z'$ , implying very soft decay products. Hence, our  $Z'$  is not really constrained by present LHC data, so that all points presented in this plot (at  $\sqrt{s} = 14$  TeV) are amenable to experimental investigation during Run 3. However, a more striking signature would be  $Z'$  pair production, to which we turn next.

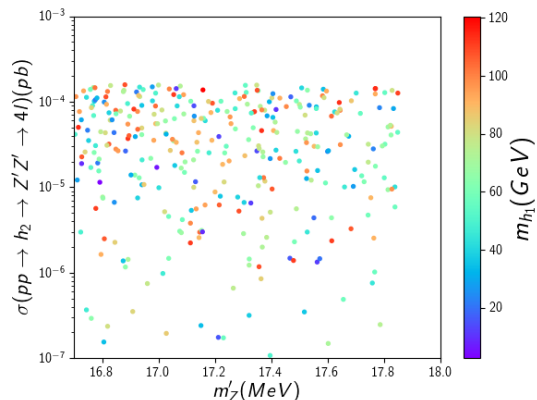


**FIG. 4:** Results for  $\sigma(pp \rightarrow Z' \rightarrow ll)$  ( $l = e, \mu$ ) in terms of  $m_{h_1}$  vs  $m_{Z'}$ , for  $\sqrt{s} = 14$  TeV.

#### 2. $Z'$ Pair Production via SM-like Higgs Mediation

As  $m_{Z'} \ll m_{h_{1,2}}/2$ , our light  $Z'$  boson can be pair produced via both Higgs bosons  $h_1$  and  $h_2$ . Let us start

with SM-like Higgs mediation. In Fig.5, we present the cross section of the ensuing four-lepton final state at  $\sqrt{s} = 14$  TeV for the solutions satisfy all experimental bounds considered so far, with the additional requirement  $\text{BR}(h_2 \rightarrow Z'Z' \rightarrow 4l) < 5 \times 10^{-6}$ , following ATLAS [37] and CMS [38] results. The color bar shows the mass of the  $h_1$ . As can be seen, the rates for  $\sigma(pp \rightarrow h_2 \rightarrow Z'Z' \rightarrow 4l)$  can be rather large, up to  $\approx 0.1$  fb, over a wide range of  $m_{h_1}$ , including very small values of the latter, which in turn call for studying  $h_1$  mediation, our next section.



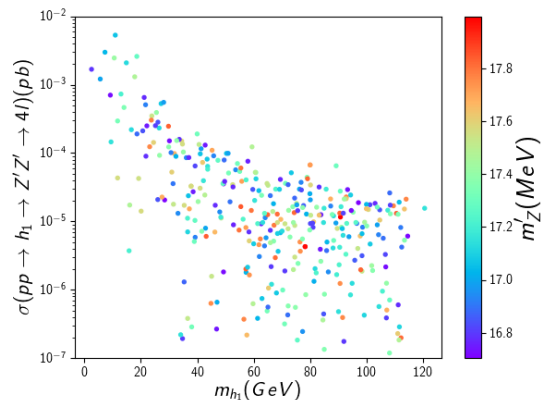
**FIG. 5:** Results for  $m_{h_1}$  in terms of  $m_{Z'}$  vs  $\sigma(pp \rightarrow h_2 \rightarrow Z'Z' \rightarrow 4l)$ , for  $\sqrt{s} = 14$  TeV.

### 3. $Z'$ Pair Production via Exotic Higgs Mediation

In this final part, we investigate  $Z'$  pair production via the new exotic Higgs,  $h_1$ . Fig. 6 shows  $\sigma(pp \rightarrow h_1 \rightarrow Z'Z' \rightarrow 4l)$  correlated to  $m_{h_1}$  as well as  $m_{Z'}$ , for the same parameter space considered in the previous plot (again,  $\sqrt{s} = 14$  TeV). In this case, the four-lepton rate can be larger than  $10 \times 10^{-3}$  pb for a light  $h_1$  while reaching  $2 \times 10^{-5}$  pb for  $m_{h_1}$  tending to  $m_{h_2}$ . Hence, the  $h_1$  mediated process, depending on the  $m_{h_1}$  values, producing a  $Z'$  pair decaying into four-lepton final states, can actually be the best way to access both the new Higgs and new gauge sectors of our scenario.

## II. CONCLUSION

In summary, a rather simple theoretical framework, assuming a non-universally coupled (to fermions)  $Z'$  boson, with a mass of  $O(10)$  MeV, emerging from a spontaneously broken  $U(1)'$  group additional to the SM gauge symmetries, is able to explain several data anomalies currently existing at low energies while predicting a clear signal at high energies. Namely, the latter is a very clean process, potentially extractable at the upcoming Run 3 of the LHC, i.e.,  $pp \rightarrow h_i \rightarrow Z'Z' \rightarrow 4l$  ( $l = e, \mu$ ), where  $h_1$  and  $h_2$  are the new Higgs state associated to the additional gauge group and the SM-like one already discovered, respectively. Hence, a new ‘golden channel’ involving again four leptons in the final state could soon give access to both a new neutral Higgs and gauge boson.



**FIG. 6:** Results for  $m_{Z'}$  in terms of  $m_{h_1}$  vs  $\sigma(pp \rightarrow h_1 \rightarrow Z'Z' \rightarrow 4l)$ , for  $\sqrt{s} = 14$  TeV.

## ACKNOWLEDGEMENTS

SK is partially supported by the Science, Technology and Innovation Funding Authority (STDF) under Grant No. 37272. SM is supported in part through the NExT Institute and the STFC Consolidated Grant No. ST/L000296/1. The work of YH is supported by The Scientific and Technological Research Council of Turkey (TUBITAK) in the framework of the 2219-International Postdoctoral Research Fellowship Programme and by Balikesir University Scientific Research Projects with Grant No. BAP-2022/083.

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