

All-Optical Switching of Liquid Crystals at Terahertz Frequencies Enabled by Metamaterials

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Abstract:

Nematic liquid crystals integrated with metallic resonators (metamaterials) are intriguing hybrid systems, which not only offer added optical functionalities, but also promote strong light-matter interactions. In this report, we show with a simple analytical model that the electric field generated by a conventional oscillator-based terahertz time domain spectrometer is strong enough to induce partial, all-optical switching of nematic liquid crystals in such hybrid systems. Our analysis provides a robust theoretical footing for the mechanism of optical nonlinearity of liquid crystals, which was recently proposed to explain anomalous resonance frequency shift in liquid crystal-loaded terahertz metamaterials [1]. This method offers a systematic approach to explore nonlinearity within hybrid liquid crystal cells; paves the way towards increased efficiency of existing devices; and broadens the range of applications of liquid crystals in the terahertz frequency range. This method offers a combinatorial way to study molecular liquid crystal interactions in the bulk and explore the related optical nonlinearity through interfacing with resonant structures.

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1. Introduction

Terahertz (THz) technologies have shown significant potential in several important application areas including: non-disruptive drugs sensing [2,3], security [4–6], medicine and life sciences [7] and next-generation short-range wireless systems operating at higher data transfer rates than currently available [8]. Yet, research in this field is still primarily focused on finding ways to both control and manipulate THz radiation effectively [9–12]. A particular focus is on the development of tuneable, compact and cheap devices such as modulators [13, 14] and phase shifters [15]. Liquid crystals (LCs) could offer a viable solution being already at the core of many technologies across most of the electromagnetic spectrum, such as: smart displays [16, 17], smart windows [18, 19], flat optics [20–23], and flexible electronics [24–26]. However, to operate efficiently in the THz spectral domain, LC-based optical components must be several hundred microns (or more) thick. This is due to the relatively low birefringence of available LC materials and the long wavelength of THz radiation. Furthermore, LC-based devices are typically controlled by externally applied electric fields, which necessitates the use of transparent electrodes [27, 28] not readily available in all regions of the spectrum, especially in THz [29]. The efficiency of LC-based devices in the THz regime can be substantially improved by the inclusion of metallic planar metamaterials (MMs). Such MMs are thin, metal films patterned on a sub-wavelength scale, enabling dramatic enhancement of diffraction-free light-matter interactions,

while maintaining a small device footprint (see e.g. [14, 30] and references therein). While thin layers of LCs integrated with MMs have been shown to be capable of effective modulation of THz radiation, their operation so far has been driven by externally applied electric fields and temperature [14, 30–38]. In our recent work we reported experimentally that such hybrid systems can also be controlled optically using the low-power THz radiation of a conventional THz-time domain spectrometer (TDS) [1]. The observed all-optical switching was attributed to a local in-plane reorientation of LC molecules induced by incident THz fields, which underwent resonant amplification and sub-wavelength concentration facilitated by the fabric of MMs. Here, we provide a comprehensive theoretical analysis of the proposed mechanism based on an analytical model of in-plane LC switching. We then confirm that engaging orientational optical nonlinearity of LCs at typical THz-TDS intensities is achievable with metallic MMs.

2. Experimental demonstration of optical switching

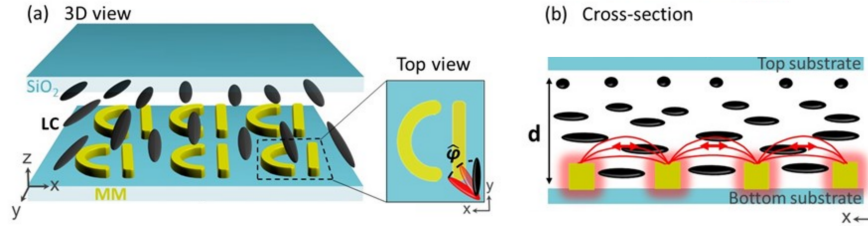


Fig. 1. (a) An artistic impression of a homogeneously aligned planar LC cell integrated with an array of D-shaped metallic resonators red(metamaterial). Inset shows schematically changes in the orientation of an LC molecule near a D-shaped resonator (and the associated twist angle, ϕ), driven by the near field. (b) Schematic representation of in-plane LC switching near the metamaterial induced by its resonantly enhanced near field (red arrows) in a homogeneously aligned hybrid LC cell.

For the sake of completeness and convenience to the reader, in this section we provide a brief account of our recent experimental study into LC optical switching using THz fields [1]. This study involved the characterisation of the transmission spectra of a 20 μ m thick LC optical cell hybridised with a metallic MM, using a conventional oscillator based THz-TDS setup in the 0.1-1.4 THz range of frequencies. The hybrid cell was filled with LC1825 and featured planar alignment set parallel to the straight sections of D-shaped MM resonators (metamolecules), as illustrated in Fig. 1(a). The measured spectrum shown with a black dashed line in Fig. 2(a) appeared blue-shifted with respect to the spectrum simulated for planar LC configuration (blue solid line) and displayed a smaller variation of transmission at the resonance. This surprising discrepancy was attributed to optically-induced local distortions of the initially planar alignment of the LC near the corners of the metamolecules ('hotspots'), where the re-orientation of LC molecules was driven by the resonantly amplified near field of the MMs (see Fig. 2(b)). To this end, the numerical model was modified to include the change in the refractive index of LC near the corners and in the gaps of D-shaped metallic resonators that would result from the re-orientation of LC molecules along the field lines. However, this would only occur when the direction of the local field deviated from the initial LC alignment by no more than $\pi/4$ (see inset to Fig. 2(a)). For other directions, (i.e., from $\pi/4$ to $\pi/2$) the local field was deemed too weak to ensure the complete re-orientation of LC molecules along its field lines. The transmission spectrum of the MM calculated using the modified numerical model is plotted in Fig. 2(a) with a red solid line and shows a good spectral overlap with the experimental data, thus, rendering

78 plausible our assumption that the deformation of planar LC alignment, ϕ , of up to $\pi/4$ was
 79 induced optically within the 'hotspots'. From the numerical model we also found that the overall
 80 local-field enhancement attainable with the MM was likely to exceed 200 [1], which suggested
 81 that in our case the orientational optical nonlinearity of LC might be engaged even with a
 82 low-power THz-TDS. In this work, we validate the above hypothesis using a simple analytical
 83 model of LC in-plane switching.

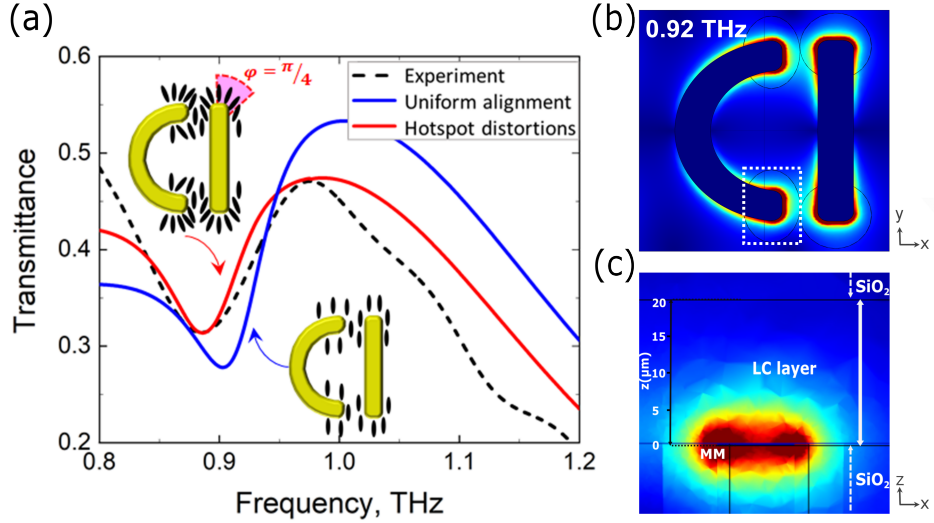


Fig. 2. (a) Transmission spectra of LC-loaded MM measured experimentally (black dash line) and modelled numerically in the cases when LC alignment is planar and uniform everywhere (blue solid curve) and distorted locally within 'hotspots' (red solid curve). Insets illustrate schematically the local alignment of LC molecules assumed in the two cases. Angle ϕ describes the twist deformation of LC in the 'hotspots' and has the maximum value of $\frac{\pi}{4}$. (b) Field map shows the variation of electric field induced in the plane of a metamolecule (xy -plane) at the resonance frequency of 0.92 THz. Electric field is strongest near the corners and in the gaps of the metamolecule. (c) Field map show the variation of the in-plane component of electric field induced in xz -plane near the corner of the metamolecule (marked by white rectangle in panel (b)).

84 3. Analytical model of LC optical switching

85 To estimate the strength of the THz field required to switch LCs in such hybrid cells we used a
 86 mathematical model previously developed for the analysis of the in-plane switching (IPS) of a
 87 nematic LCs [39]. Briefly, in the IPS model the electric field that re-orientes LC molecules is
 88 produced by interdigital electrodes, which have an infinite length and are all arranged on the same
 89 plane (e.g., the surface of a substrate), forming two interlocking combs. It is assumed that every
 90 pair of neighbouring electrodes acts like a capacitor so that the electric field is homogeneous
 91 and aligned parallel to the substrate. In the OFF state, the LC molecules are oriented along the
 92 electrodes (see Fig. 3(a)). In the ON state, the electric field of the electrodes forces the LC
 93 molecules to orient along the field lines, i.e., orthogonal to the electrodes. Thus, IPS corresponds
 94 to $\pi/2$ 'in-plane' twist deformation of the LC (see Fig. 3(a)) [40,41]. Similarly, we assume that
 95 in our case the electric field induced at the corners of metamolecules, upon their illumination
 96 with a THz beam (ON state), drives the re-orientation of LC molecules within the 'hotspots'.
 97 This occurs in the plane of the MM, towards the direction of the field lines (see Fig. 1(b)). What

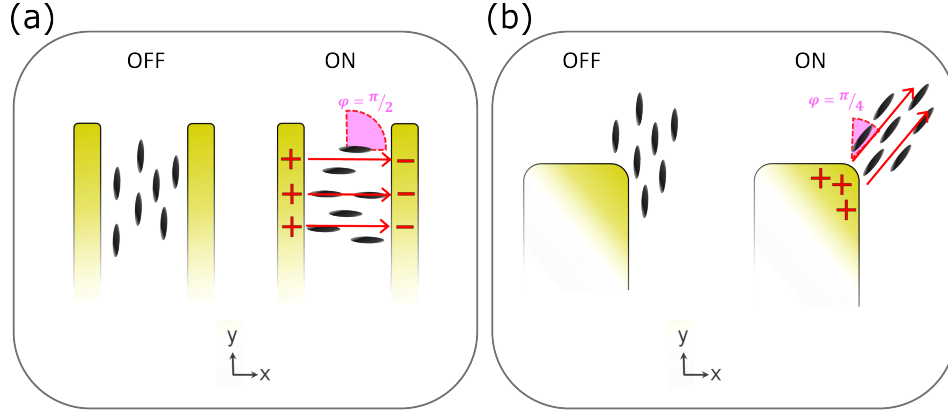


Fig. 3. (a) Schematically shown conventional in-plane switching mode of an LC cell
 (b) Schematically shown in-plane switching driven by the near field of a metamolecule,
 which models the re-alignment of LC in the area of the 'hotspot' where the initial
 misalignment between LC director and local field reaches $\pi/4$.

98 makes our case principally different from the conventional IPS model is that the electric field
 99 acting on the LC does not extend all the way across the cell, but is rather confined to a distance
 100 of few microns above the MM. More specifically, given that the local field decays exponentially
 101 within the hotspots, which is supported by the result of our simulation (see Fig. 2(c)), the spatial
 102 extent of the electric field is capped by $z_c = 2.9\mu\text{m}$, as given by e^{-1} falloff of the electric field
 103 strength. Thus, we use the IPS model approach locally, in close vicinity to the metamolecules,
 104 where the electric field is further assumed to be uniform and aligned parallel to the substrate.
 105 Another principle difference with the conventional IPS is that the twist deformation of LC, ϕ , in
 106 the areas featuring complete in-plane switching does not exceed $\pi/4$, as illustrated in Fig. 3(b).
 107 This fact was established earlier in [1] and, as we will show below, it lifts the restriction on the
 108 minimal strength of the electric field (i.e., voltage threshold) that can drive in-plane re-orientation
 109 of LC molecules and the resulting orientational optical nonlinearity of LC in the THz regime.

110 Following [39], we start with the free energy functional $F(\phi)$ of the twist deformation for the
 111 layer of LC subjected to the local electric field ($0 \leq z \leq z_c$), which has the form

$$F(\phi) = \frac{1}{2} \int_0^{z_c} \left(K_2 \left(\frac{d\phi}{dz} \right)^2 - \epsilon_0 |\Delta\epsilon| E^2 \sin^2 \phi \right) dz \quad (1)$$

112 where K_2 is the elastic constant of the twist deformation, ϕ is the twist angle in the xy-plane,
 113 $\Delta\epsilon$ denotes the dielectric anisotropy of LC, and E is the strength of the in-plane component of
 114 the local electric field. To further simplify the analysis, E is taken to be constant with the value
 115 given by the strength of the local field averaged across $0 \leq z \leq z_c$. To minimize the functional
 116 Eq. (1), ϕ must satisfy the following Euler-Lagrange equation.

$$K_2 \frac{d^2\phi}{dz^2} + \epsilon_0 |\Delta\epsilon| E^2 \sin \phi \cos \phi = 0 \quad (2)$$

117 In the IPS model ϕ is defined as the angle between LC director and the direction orthogonal
 118 to the electric field lines and, hence, due to the initially planar alignment, LCs in the hotspots
 119 appear twisted with respect to the local field lines with ϕ being equal to or exceeding $\pi/4$ [1].
 120 Thus, for those sectors of the hotspots that permit the largest optically-induced twist deformation
 121 the following substitution can be made: $\phi = \phi + \pi/4$, where ϕ now describes the deformation
 122 relative to the initial twist. As a result, Eq. (2) transforms into

$$K_2 \frac{d^2 \phi}{dz^2} + \frac{\epsilon_0 |\Delta \epsilon| E^2}{2} \cos 2\phi = 0 \quad (3)$$

We proceed by solving Eq. (3) first under the assumption that the relative twist deformation is small, i.e., $\phi \rightarrow 0$. To find the solution we apply the following boundary conditions: $\phi = 0$ at $z = 0$ (corresponds to strong LC anchoring imposed on the MM side of the cell by rubbed polyimide) and $\frac{d\phi(z)}{dz} = 0$ at $z = z_c$, which stems from the transversality condition and effectively defines z_c as a ‘free’ boundary. In this case we arrive at the following solution

$$\phi(z) = \frac{\epsilon_0 |\Delta \epsilon| E^2}{4K_2} (2z_c - z)z \quad (4)$$

Evidently, Eq. (4) yields a non-zero ϕ for any $E \geq 0$, which indicates that in-plane re-orientation of LC molecules within the hotspots starts with no threshold on the strength of the local electric field. This is in stark contrast to the conventional IPS mode, which manifests itself as a Fréedericksz transition and typically cannot be engaged with electric fields weaker than $1.05V/cm$ [39].

Next, we aim to find an analytical solution of Eq. (3), which will be valid in the limit of large relative twist angles, i.e., $\phi \rightarrow \pi/4$. To this end we linearise Eq. (3) by replacing $\cos 2\phi$ in the second term with its linear approximation at $\phi = \pi/4$. Here we have chosen the linear function that is tangential to $\cos 2\phi$ at $\phi = \pi/4$ (black dashed line Fig. 4(a)).

To this end, we use the approximation

$$\cos 2\phi \approx \pi/2 - 2\phi \quad (5)$$

which turns the initially nonlinear differential Eq. (3) into

$$K_2 \frac{d^2 \phi}{dz^2} - \epsilon_0 |\Delta \epsilon| E^2 \phi + \epsilon_0 |\Delta \epsilon| E^2 \frac{\pi}{4} = 0 \quad (6)$$

Eq. (6) can now be solved analytically and its solution is given by

$$\phi(z, E) = \frac{\pi}{4} + k_1 \exp\left(-\sqrt{\frac{\epsilon_0 |\Delta \epsilon|}{K_2}} E z\right) + k_2 \exp\left(\sqrt{\frac{\epsilon_0 |\Delta \epsilon|}{K_2}} E z\right) \quad (7)$$

To determine k_1 and k_2 , we use the same boundary conditions as above, namely $\phi(0) = \frac{d\phi(z_c)}{dz} = 0$. The derived expressions for k_1 and k_2 are

$$k_1 = -\left(\frac{\pi}{4} + k_2\right) \quad (8)$$

$$k_2 = -\frac{\pi \exp\left(-\sqrt{\frac{\epsilon_0 |\Delta \epsilon|}{K_2}} E z_c\right)}{8 \left(\cosh\left(\sqrt{\frac{\epsilon_0 |\Delta \epsilon|}{K_2}} E z_c\right)\right)} \quad (9)$$

The constants in Eq. (7), (8) and (9) for LC1825 are taken from [42] (see table 1).

Constants	Values
ϵ_0	$8.85 \times 10^{-12} [N/V^2]$
$\Delta\epsilon$	17
K_2	$7.4 \times 10^{-12} [N]$

Table 1. Specifications of LC1825 [42]

4. Discussion

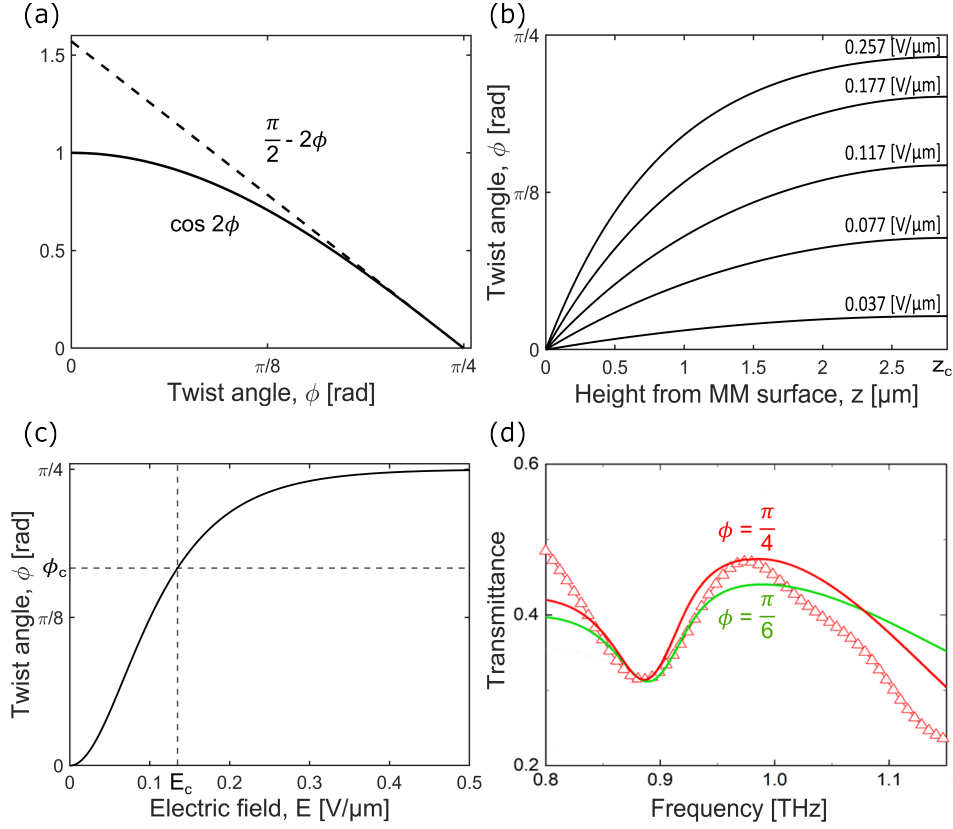


Fig. 4. (a) The linear approximation of $\cos 2\phi$ (solid line) approximated using $\frac{\pi}{2} - 2\phi$ (dashed line). (b) The change of twist angle, ϕ , within LC layer ($0 \geq z \geq z_c$), for different E-field values using the $\frac{\pi}{2} - 2\phi$ approximation. (c) The maximal twist angle, ϕ , achieved at $z = z_c$ as a function of the local electric-field strength, E . (d) Simulated results of the transmission spectra for hybrid LC cells at different angular limits of reorientation around MM 'hotspots' (solid lines), with experimental results (open triangles).

Figure 4(b) shows how the twist angle varies within a $2.9 \mu\text{m}$ thick layer of LC above the MM, as calculated using Eq. (7) for different values of the local electric-field strength. Evidently, the twist deformation increases monotonously away from the MM and saturates on approaching z_c . Note that while in-plane switching in our case features no voltage threshold, it formally remains incomplete since the analytical solution approaches $\pi/4$ asymptotically. This is best illustrated

by Fig. 4(c), where we plot the maximal twist angle (achieved at $z = z_c$) as a function of the local electric-field strength. Such behavior is underpinned by the dependence of the electrically induced LC torque on the twist angle. The torque in our case is proportional to $\cos 2\phi$ and, therefore, decreases with increasing ϕ , vanishing completely for LC molecules aligned parallel to the electric field (i.e., when $\phi = \pi/4$). In practice, however, the switching of LC within the hotspots does not have to be complete, as the dielectric permittivity of LC ‘sensed’ there by the local electric field is proportional to $\cos \Delta\phi$, where $\Delta\phi = \pi/4 - \phi$. If $\Delta\phi \ll 1$ the deviation of dielectric permittivity from the maximum value will be proportional to $\Delta\phi^2$ and, hence, appear insignificant.

Since the solution Eq. (7) is valid for $\phi \rightarrow \pi/4$, where the dependence on the local-field strength resembles a saturating exponential function (Fig. 4(c)), we take $\Delta\phi = \pi/4e$. It corresponds to a twist angle of $\pi/6$, which we regard as the ‘characteristic’ twist angle, ϕ_c . It defines $[0, \pi/6]$ as the range of LC twist deformations beyond which a significant change in the optical response of LC-loaded MM no longer occur, as also confirmed by our rigorous numerical modeling (see Fig. 4(d)). Hence, the characteristic twist angle can be used to determine the strength of local electric field, E_c , which would yield the level of optical switching comparable to that observed in the experiment [1]. Applying ϕ_c to the dependence plotted in Fig. 4(c) gives $E_c \approx 0.13V/\mu m$.

In the final part of our analysis we compare the typical strength of electric fields generated by a THz-TDS system with the strength of incident electric field required to seed the observed nonlinearity. To estimate the latter, we recall that local electric field decays exponentially away from the surface of the MM with e^{-1} falloff at $2.9 \mu m$, while E_c in our analysis corresponds to the average value of the local-field strength. Hence, the electric field produced in the plane of the MM is a factor of 3 stronger than E_c . Since the field-enhancement factor characteristic of D-shaped metamolecules exceeds 200 [1], the required strength of electric field in an incident terahertz beam can be less than $3E_c/200 \approx 20V/cm$. Given that in conventional THz-TDS setups the electric field probed by THz detectors has the strength in the range from 10 to 100 V/cm [43], we conclude that the orientational optical nonlinearity of LCs can be readily engaged at THz frequencies with the help of purposely designed metallic MMs (at least, at the modest level observed in [1]). Also, we envisage that further optimisation of MM designs and the use of stronger sources of THz radiation will allow one to maximise the extent of LC all-optical switching in hybrid cells by enabling complete re-orientation of LC molecules even in those areas of the hotspots, where the initial misalignment between LC director and local field exceeds $\pi/4$. Among potential candidates for the THz sources that would be required, we have identified quantum cascade laser systems, which can achieve powers on the order of microwatts and up to milliwatts [44].

5. Conclusion

In this work, we analysed the nonlinear optical response of a liquid crystal cell hybridised with a metallic metamaterial and, in particular, a prominent shift of the metamaterial resonance frequency observed recently using a conventional oscillator-based terahertz time domain spectrometer [1]. We show that a local field enhancement exceeding a factor of 200 characteristic of the MM allows engaging nonlinear effects, despite the relatively low intensity radiation used. Indeed, a simple analytical model based on the in-plane switching mode of an liquid crystal cell confirms that the re-orientation of liquid crystal near the metamaterial is a thresholdless process and incident terahertz electric field of as low as $\approx 20V/cm$ is strong enough to ensure the level of all-optical liquid crystal switching observed in the experiment. Our study paves a way towards systematic investigation of nonlinear optical effects in metamaterial-enhanced liquid crystal devices using conventional THz-TDS systems, with prospects for the development of low-power terahertz all-optical switches, spatial light modulators and image processors.

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202 **9. Disclosures**

203 The authors declare no conflicts of interest.

204 **10. Data Availability Statement**

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206 **11. Supplemental document**

207 ??

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