

# 1 Impact of Local Terrain Features on Urban Airflow

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6 **Abstract** Past work has shown that coupling can exist between atmospheric  
7 air flows at street scale ( $O(0.1 \text{ km})$ ) and city scale ( $O(10 \text{ km})$ ). It is generally  
8 impractical at present to develop high-fidelity urban simulations capable of  
9 capturing such effects. This limitation imposes a need to develop better pa-  
10 rameterisations for meso-scale models but an information gap exists in that  
11 past work has generally focused on simplified urban geometries and assumed  
12 the buildings to be on flat ground. This study aimed to begin to address this  
13 gap in a systematic way by using the large eddy simulation method with syn-  
14 thetic turbulence inflow boundary conditions to simulate atmospheric air flows  
15 over the University of Southampton campus. Both flat and realistic terrains  
16 were simulated, including significant local terrain features, such as two valleys  
17 with a width about 50 m and a depth about average building height, and a  
18 step change of urban roughness height. The numerical data were processed to  
19 obtain averaged vertical profiles of time-averaged velocities and second order  
20 turbulence statistics. The flat terrain simulation was validated against high  
21 resolution particle image velocimetry data, and the impact of uncertainty in  
22 defining the turbulence intensity in the synthetic inflow method was assessed.  
23 The ratio between realistic and flat terrains of time-mean streamwise velocity

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at the same ground level height over a terrain crest location can be greater than 2, while over a valley trough it can be less than 0.5. Further data analysis conclusively showed that the realistic terrain can have a considerable effect on global quantities, such as the depth of the spanwise-averaged internal boundary layer and spatially-averaged turbulent kinetic energy ( $TKE$ ). These highlight the potential impact that local terrain features ( $O(0.1 \text{ km})$ ) may have on near-field dispersion and the urban micro-climate.

**Keywords** Above-Ground-Level Height · Downslope · Street-scale Terrain · Water Tunnel Experiment · Velocity Modulation

## 1 Introduction

At present operational meso-scale models are unable to predict the details of urban flows at street and neighbourhood scale (i.e  $O(1 \text{ km})$ ). Although finely resolved urban simulations can be generated by engineering computational fluid dynamics (CFD) codes (e.g. Xie and Castro, 2009; Han et al., 2017; Antoniou et al., 2017; Inagaki et al., 2017; Tolia et al., 2018; Gronemeier et al., 2020) over scales from 1 m to neighbourhood scale, larger city-scale simulations (i.e  $O(10 \text{ km})$ ) are generally impractical. This presents a significant limitation, as past work has shown that two-way coupling can exist between the urban boundary layer properties measured at street scale ( $O(0.1 \text{ km})$ ), neighborhood ( $O(1 \text{ km})$ ), and city scales ( $O(10 \text{ km})$ ) (Fernando, 2010; Barlow et al., 2017). Such coupling can be particularly pronounced when the urban area includes features such as a single or cluster of tall buildings (Han et al., 2017; Fuka et al., 2018; Hertwig et al., 2019), or a sharp change in topography (Conan et al., 2016; Blocken et al., 2015; Limbrey et al., 2016).

The development of simulations which accurately capture the coupling between street and city scales challenges both numerical and experimental approaches in many respects. This study uses numerical simulations to examine a selected heterogeneous area containing urban geometry and small sharp changes in topography ( $O(0.1 \text{ km})$ ) in a systematic way which is difficult to achieve through wind and water tunnel experiments, or field observations.

Xie and Castro (2009) shows that to resolve the flow at street scale a grid resolution of a metre or less is necessary, but using such a resolution for city scale simulations challenges both current computational tools and resources. This imposes challenges because of the limited computational resources, and consequently the limited resolution. The complex geometries of real buildings must be simplified without losing any features which have a critical effect on the flow. Small topographic features ( $O(0.1 \text{ km})$ ) impose similar challenges, which are typically smoothed and simplified in numerical and physical models. The first question is what are the critical - but perhaps small - features of buildings and terrain that must be resolved. The second question is whether special treatments are required.

Atmospheric flows around arrays of buildings with complex geometries have been investigated in a number of studies published since 2000, for example

67 Arnold et al. (2004); Xie and Castro (2009); Hertwig et al. (2012); Han et al.  
68 (2017); Antoniou et al. (2017); Inagaki et al. (2017); Tolia et al. (2018); Her-  
69 twig et al. (2019); Gronemeier et al. (2020); Sessa et al. (2020); Goulart et al.  
70 (2019); Ricci et al. (2020); Liu et al. (2023). These studies have principally ad-  
71 dressed the challenges arising from heterogeneity and anthropogenic drivers as  
72 identified in Barlow et al. (2017), such as may be associated with step-changes  
73 in urban roughness height and development of internal urban boundary layer,  
74 a cluster of tall buildings and local thermal stratification. As such, they have  
75 generally assumed the buildings to be on flat ground and neglected the effect  
76 of terrain.

77 A few studies that have considered the effects of urban terrain have focused  
78 on city-scale ( $O(10 \text{ km})$ ) topographic changes (e.g. Fernando, 2010). This may  
79 be because they have aimed to support meso-scale model developers striving  
80 to increase their spatial resolution (e.g. to  $O(1 \text{ km})$ ) and capture the average  
81 effects of small topographic features without resolving them. A small number  
82 of papers (Apsley and Castro, 1997; Blocken et al., 2015; Conan et al., 2016)  
83 have studied the airflow over small scale terrain without any buildings, and  
84 emphasized the crucial role of small terrain features. An exception is the work  
85 of Fossum and Helgeland (2020) which included ambitious large-eddy simula-  
86 tions (LES) for the hilly city of Oslo using a domain of  $150 \text{ km}^2$  at a spatial  
87 resolution of 2 m. The work aimed to demonstrate the capability of LES to  
88 provide detailed data for developing parameterisations for a fast-response tool.  
89 They emphasized the importance of the wall boundary conditions in particu-  
90 lar, which is linked to the importance of small-scale topographic features.

91 At present there is uncertainty in the role of small-scale topography on the  
92 street and neighbourhood scale which, through coupling, can result in uncer-  
93 tainty on the city scale. This highlights a need for new studies to investigate  
94 and understand the effects of small-scale topographic features on street ( $O(0.1$   
95  $\text{ km})$ ) to neighborhood ( $O(1 \text{ km})$ ) scales, before considering the coupling be-  
96 tween neighborhood and city scales.

## 97 **2 The Case Study of Southampton University Highfield Campus**

98 The city of Southampton lies at the confluence of the Test and Itchen rivers and  
99 the urban area contains numerous small valleys. Two such valleys are shown  
100 by the dark areas in Fig. 1 and the dark blue in Fig. 2, cross the University  
101 of Southampton Highfield campus. In Fig. 2 the positive  $x$  and  $y$  coordinates  
102 are west-east and south-north respectively. To the west of the campus is a  
103 1 km (west-east) by 2 km (south-north) public park, in which the terrain is  
104 flat with a small downslope of approximately 1:50 from north to south. With  
105 these features in westerly wind, the campus is an excellent site for conducting  
106 a study to examine the importance of small ( $O(0.1 \text{ km})$ ) and sharp changes in  
107 terrain elevation within a real urban area. Due to the complications involved in  
108 taking account of tree effects into the LES, trees in the park and in the campus

109 were ignored entirely. The current case study is a considerably simplified one  
 110 for terrain effect.

111 The approach adopted for assessing the significance of small scale topog-  
 112 raphy was to compare the simulations of atmospheric air flows around the  
 113 buildings in the campus for cases in which the buildings were on flat and on  
 114 real terrain (including the small-scale topography). To validate the numerical  
 115 modelling method for neutral atmospheric conditions, advantage was taken of  
 116 the availability of high resolution PIV data from a water tunnel experiment.

117 The domain chosen for the study was sized to include sufficient surround-  
 118 ing area to capture the flow development over the buildings upstream of the  
 119 campus and the downstream evolution of the wakes created by the campus  
 120 buildings. This led to a final domain which comprised the Highfield campus  
 121 plus the surrounding area out to 80 m, which was equivalent to  $5h$ , where  $h$   
 122 was the average building height of 16 m within the study domain. The packing  
 123 density was 29%. In Fig. 2a and b the solid black line at  $y=104$  m indicates the  
 124 streamwise-vertical ( $x-z$ ) plane in which the PIV data were taken, while the  
 125 solid black line at  $y = -210$  m indicates an example  $x-z$  plane for further  
 126 data analysis (e.g. see Fig. 4d).

127 Figure 2a shows the domain for the flat terrain case which has dimensions  
 128  $900$  m ( $L_x^F$ )  $\times$   $800$  m ( $L_y^F$ ). Figure 2b shows the domain of the real terrain  
 129 case, with dimensions  $1050$  m ( $L_x^T$ )  $\times$   $800$  m ( $L_y^F$ ). The domain for the real  
 130 terrain case includes a  $150$  m extension upstream of  $x = 0$ , to allow the  
 131 spanwise variation in terrain elevation at the location  $(x = 0, y)$  to be linearly  
 132 interpolated to zero terrain elevation at the corresponding inlet location  $(x =$   
 133  $-150$  m,  $y)$ , creating a rectangular shape inlet plane required by the synthetic  
 134 turbulence inflow (STI) conditions. This treatment is similar as that for wind  
 135 tunnel experiments. The first valley which has a width of about  $50$  m and  
 136 a depth of about  $10$  m is between  $x = 200$  m  $-$   $400$  m (Fig. 2b). The second  
 137 deeper and narrower valley between  $x = 800$  m  $-$   $900$  m is near the outlet of  
 138 the CFD domain and was not the focus of this study.

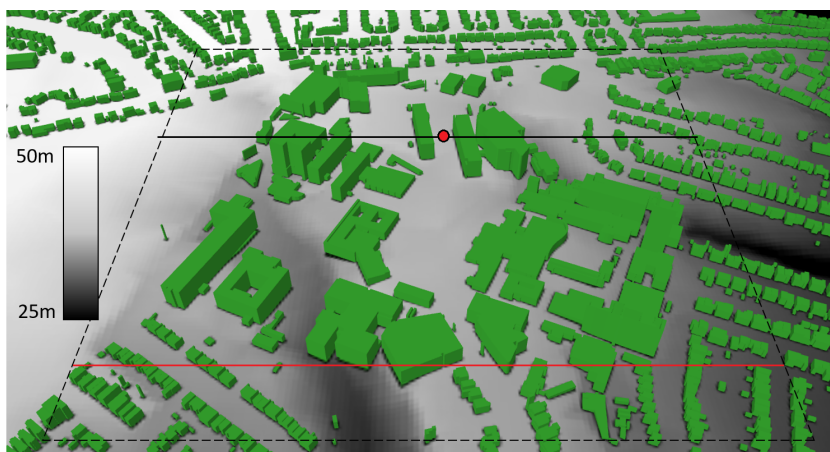


Fig. 1: Three-dimensional geometry and terrain contours (above sea-level) of the University of Southampton Highfield campus. The dashed frame shows the extent of computational domain. The red dot marks Location 7 (Fig. 5). The black solid line indicates the streamwise-vertical ( $x - z$ ) plane in which the PIV data were taken, while the red solid line indicates the streamwise-vertical ( $x - z$ ) plane shown in Fig. 4d

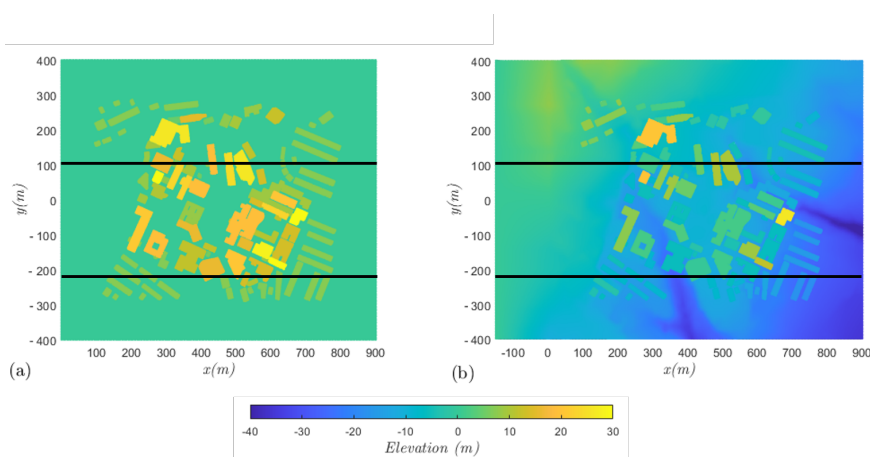


Fig. 2: Contours of the terrain and building elevation for a) the flat terrain cases (SF8, FF8, SF12) with the ground placed at elevation  $z = 0$ , and b) real terrain case (ST8 ext.) with the inlet ground located at elevation  $z = 0$ . The black solid line at  $y = 104$  m indicates the streamwise-vertical ( $x - z$ ) plane in which the PIV data were taken, while the black solid line at  $y = -210$  m indicates an example  $x - z$  plane for further analysis (i.e. Fig. 4d)

## 139 2.1 Setting Details of Study Cases

140 The LES case geometries for the study were developed using building footprint  
141 and height data from the OS MasterMap data set and Ordnance Survey (OS)  
142 5 m resolution terrain data. The simulation cases created are summarised in  
143 Table 1. For consistency with the physical model placed on the flat floor in  
144 the water-tunnel (flume) experiment, all the buildings were modelled as having  
145 flat roofs. The errors resulting from this simplification should be small as the  
146 university campus buildings generally have flat roofs, and the replacing the  
147 pitched roofs with flat ones on the small number of residential houses in the  
148 surrounding area should not produce large errors. The building heights of the  
149 water tunnel model and the cases SF8, SF12, FF8 were defined based on the  
150 longest vertical edges of the flat-roof buildings from the OS MasterMap data  
151 set, which avoids any ambiguity due to the terrain, and the average building  
152 height was denoted  $h$ .

153 The mesh generator SnappyHexMesh in OpenFoam v2.1.1 was used to cre-  
154 ate conformal (body-fitted) meshes (Coburn et al., 2022). The flat terrain case  
155 in which the real terrain was replaced with flat terrain and a grid developed  
156 with a resolution of 2m ( $h/8$ ) was denoted SF8 (Table 1). The ratio of the  
157 domain height and the average building height  $h$  of SF8 was 12, which was  
158 close to the ratio of the water tunnel boundary layer thickness and the aver-  
159 age building height  $h$ . To verify that the grid was sufficient, a case denotes  
160 SF12 with a finer resolution of  $h/12$  was also simulated. The case FF8 had the  
161 same other settings as SF8, except for its inflow mean velocity and Reynolds  
162 stresses obtained from the naturally grown turbulent boundary layer in the  
163 water-tunnel experiments (Fig. 3c and d), for the purpose of a direct compar-  
164 ison with the PIV data (see Table 1). The physical model had a Reynolds  
165 number  $Re_h \approx 3,080$  (Sect. 3.2), based on the average building height and  
166 the freestream velocity. The Reynolds number based on the average building  
167 height and freestream velocity for cases SF8, SF12 and FF8 was 16,000, while  
168 it was 13,600 for SF8 ext. and ST8 ext. Early studies (e.g. Stoesser et al., 2003;  
169 Cheng and Castro, 2002; Xie and Castro, 2006; Xie et al., 2008) suggested that  
170 Reynolds number dependency (if it does exist) was very weak for such flows.  
171 For example, the Reynolds number based on the bulk velocity and the cube  
172 height in a study of flow over an array of cubes mounted on a channel wall was  
173 3,823 (Stoesser et al., 2003), while it was 4,790 based on the average height  
174 and freestream velocity in a study of an array of random height blocks (Xie  
175 et al., 2008).

176 To avoid any blockage issue for the simulations of real terrain, the domain  
177 height was increased to  $15h$  (denoted ST8 ext. in Table 1). More interestingly,  
178 if building height is defined as the height difference between the roof and the  
179 average ground level around the perimeter of the building, adding the real  
180 terrain leads to 15% reduction in average building height compared to the  
181 water tunnel model. To have a closer comparison between flat terrain and real  
182 terrain, a new flat terrain case SF8 ext. (Table 1) was built with a domain  
183 height  $15h$  and an average building height 13.6m in full scale, equivalent to

184 15% reduction in average building height, compared to the water tunnel model  
185 and the cases SF8, FF8.

186 Given that the primary aim of the study was to examine the flow in a real  
187 urban area, synthetic turbulence inflow boundary (STI) conditions (e.g. Xie  
188 and Castro, 2008) were used throughout as it can replicate turbulent inflow  
189 conditions better than using periodic boundary conditions. However, as the  
190 inflow turbulence quantities may be subject to considerable uncertainty as  
191 they are difficult to obtain from observations, theoretical estimation, or down-  
192 scaling from meso-scale models, a sensitivity test was carried out with respect  
193 to the inflow turbulence levels.

194 The inflow conditions applied to cases SF8 and SF12 were taken from (Xie  
195 and Castro, 2009) and are shown in Fig. 3a and b. The conditions used were  
196 originally derived from wind tunnel experiments conducted in the EnFlo wind  
197 tunnel at the University of Surrey as part of the DAPPLE project, in which  
198 a thick turbulent boundary layer was generated using the so-called “simu-  
199 lated atmospheric boundary layer” approach (Counihan, 1969). This involved  
200 placing several large vortex generators at the wind tunnel inlet, and evenly  
201 distributed numerous small roughness elements on the floor between the inlet  
202 and the array of buildings. The roughness length  $z_0 = 0.0018m$  was equiva-  
203 lent to 0.0018 boundary thickness in Xie and Castro (2009), and equivalent  
204 to  $0.02h$  in Fig. 3a. For this study the STI vertical Reynolds stress profiles  
205 were scaled so that the peak Reynolds stress occurred approximately at the  
206 average building height. Below the peak height the Reynolds stress data were  
207 estimated through linear interpolation. “DAPPLE” in the “STI Input” column  
208 in Table 1 denotes the EnFlo wind tunnel data, while “FLUME” denotes the  
209 water tunnel data described in Sect. 3.2. The inflow mean streamwise velocity  
210 and Reynolds stresses at  $0 \leq z/h \leq 12$  for cases SF8 ext. and ST8 ext. were  
211 respectively the same as in Figs. 3 a and b, while the data at  $12 < z/h \leq 15$   
212 were constants respectively equal to those at  $z/h = 12$ .

213 Symmetry boundary condition was applied for the top and the two lateral  
214 boundaries, constant pressure was applied for the outlet, no-slip wall boundary  
215 condition was applied for ground and building surfaces. It usually took about  
216 60 wall-clock hours on 200 cores to complete one simulation case with the  
217 initialisation period  $80T_p$ , and the averaging period  $130T_p$ , where  $T_p$  was the  
218 characteristic time based on the average building height and the free stream  
219 velocity.

Cases	Resolu.	Domain size/h (x,y,z)	STI Input
Flat terrain (SF8)	$h/8$	56.25, 50, 12	DAPPLE
Flat terrain(SF12)	$h/12$	56.25, 50, 12	DAPPLE
Flume flat terrain(FF8)	$h/8$	56.25, 50, 12	FLUME
Flat terrain & Taller domain(SF8 ext.)*	$h/8$	56.25, 50, 15	DAPPLE
Real terrain & taller domain(ST8 ext.)*	$h/8$	65.625, 50, 15	DAPPLE

Table 1: Summary of the Highfield Campus simulation cases. The resolution is that within the canopy. \*Cases SF8 ext. and ST8 ext. have an average building height  $0.85h$ .

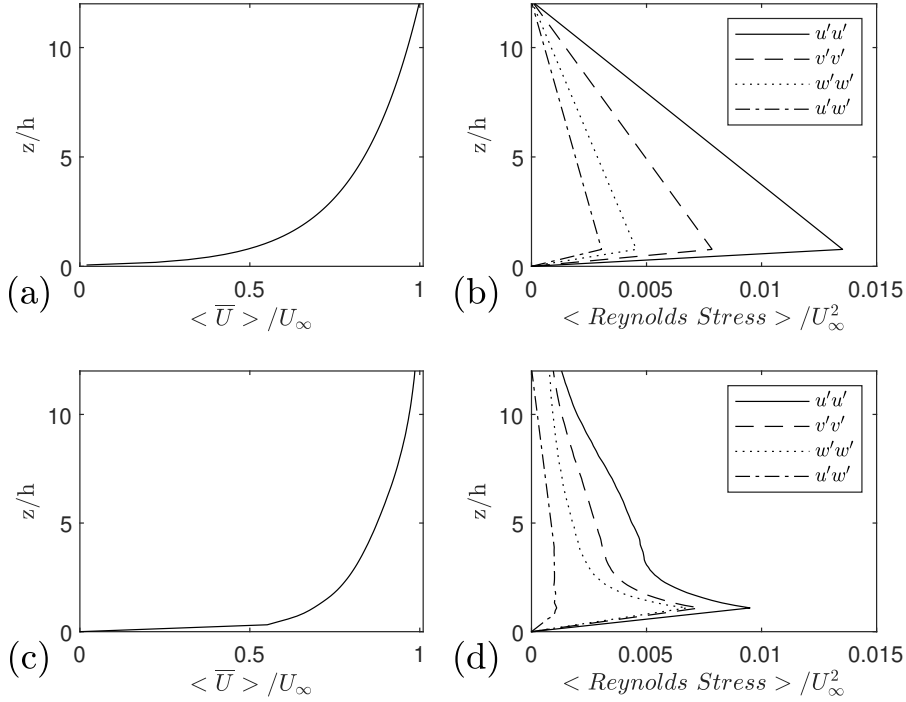


Fig. 3: Flow conditions of the experiments just upstream of the building cluster. a) mean streamwise velocity and b) Reynolds stresses from the EnFlo wind tunnel data (Xie and Castro, 2009). c) mean streamwise velocity and d) Reynolds stress from the flume experiments (see Sect. 3.2)

## 220 2.2 Terrain Elevation Analysis

221 Figure 2 plots the contours of terrain and building elevation with the inlet  
 222 ground located at  $z = 0$  for the flat terrain cases SF8, SF12 and FF8 (Fig.



223 2a) and the real terrain case ST8 ext. (Fig. 2b). Case ST8 ext. has a gentle  
224 downward slope across the streamwise extent (west-east) of the domain, and  
225 a gentle downward slope across the north-south extent of the domain. An  
226 estimation of the “average slope” in west-east direction would be helpful to  
227 understand flow field in the western wind.

228 The ground elevation was defined as  $E(x, y)$ . The building elevation was  
229 ignored, while a linear interpolation was applied between the upstream and  
230 downstream building edges to fill in the gaps left by removing the building.  
231 The average ground elevation  $AE(y)$  over the entire streamwise extent at  $y$  was  
232 calculated by averaging  $E(x, y)$  over the  $x$  range. The average gradient of the  
233 slice at  $y$  was defined as the ratio of  $AE(y)$  to the half length of the domain in  
234 the streamwise direction. Figure 4 shows  $x - z$  slices at the spanwise locations  
235  $y = -28$  m,  $-102$  m,  $-181$  m and  $-210$  m, respectively. The vertical line in  
236 each sub-figure marks the location where the valley crosses the  $x - z$  plane.  
237 The spanwise-averaged slope gradient of the terrain elevation is approximately  
238  $-2.3^\circ$ .

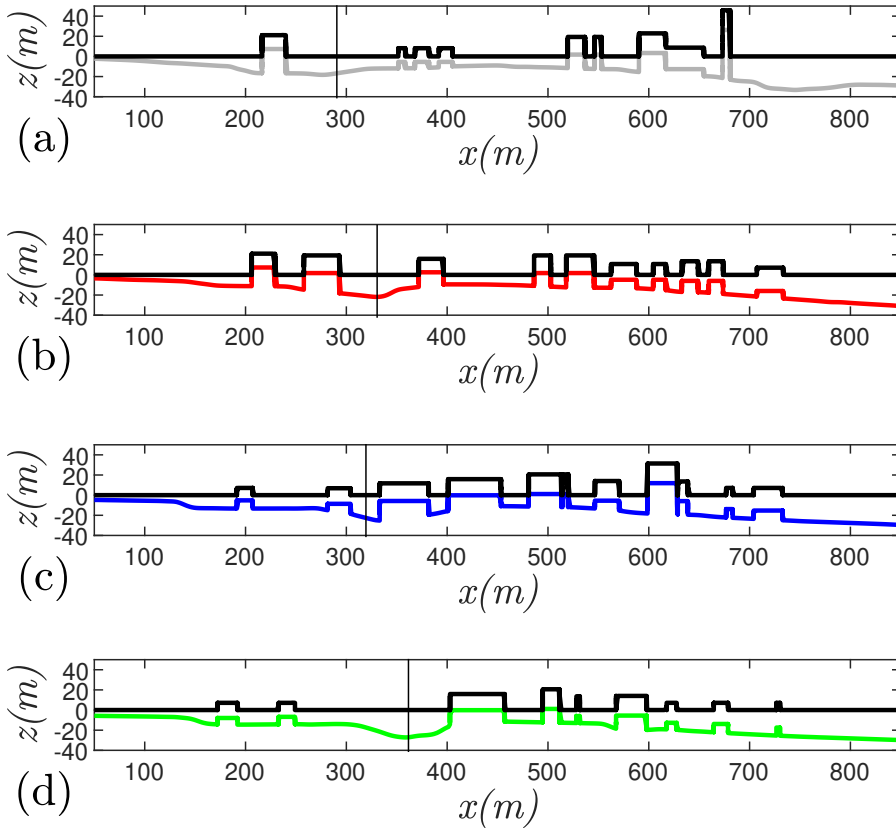


Fig. 4: Streamwise terrain and building profiles at four different spanwise locations, a)  $y = -28$  m, b)  $y = -102$  m, c)  $y = -181$  m and d)  $y = -210$  m (see Fig. 2 for the  $y$  coordinate). Thick black lines denote the flat terrain and buildings. Thick coloured lines denote the real terrain and buildings. Vertical black line in a) denotes Station 1 at  $(x, y) = (292 \text{ m}, -28 \text{ m})$ . Vertical black line in b) denotes Station 2 at  $(x, y) = (336 \text{ m}, -102 \text{ m})$ . Vertical black line in c) denotes Station 3 at  $(x, y) = (332 \text{ m}, -152 \text{ m})$ . Vertical black line in d) denotes Station 4 at  $(x, y) = (376 \text{ m}, -210 \text{ m})$

239 For statistics of the distribution of terrain and building elevation for each  
 240  $x - z$  slice shown in Fig. 4, the average linear slope for the slice was subtracted  
 241 from the elevation. The statistical data, i.e. mean, r.m.s., skewness and kurtosis,  
 242 are given in Table 2. The elevation data for the flat terrain case SF8 ext. in  
 243 Table 2 are consistently more skewed than those for the real terrain case ST8  
 244 ext. This is because the flat terrain contributes many zero elevation points to  
 245 the data-set. The addition of real terrain (ST8 ext.) leads to more Gaussian  
 246 distributions in elevation.

Case	Slice Location $y$ (m)	Mean Height (m)	r.m.s.	Skewness	Kurtosis
SF8 ext.	-28	5.009	8.4107	1.705	5.890
ST8 ext.	-28	7.128	11.196	1.689	6.571
SF8 ext.	-102	4.480	6.045	0.824	2.054
ST8 ext.	-102	8.276	8.284	0.243	2.000
SF8 ext.	-180	5.039	6.812	1.166	3.634
ST8 ext.	-180	9.505	9.607	0.937	3.949
SF8 ext.	-210	2.866	4.732	1.309	3.551
ST8 ext.	-210	7.008	8.035	0.306	2.483
SF8 ext.	Domain Av.	3.478	5.200	1.000	3.026
ST8 ext.	Domain Av.	6.384	7.424	0.635	3.001

Table 2: Terrain and building elevation statistics in four  $x - z$  planes ( $y = -28$  m,  $-102$  m,  $-180$  m and  $-210$  m) for cases SF8 ext. and ST8 ext.

### 247 3 Numerical Method and PIV data

#### 248 3.1 Large Eddy Simulation Method

249 The study was based on using the LES method to capture the inherent un-  
 250 steadiness of the atmospheric air flows which develop in urban areas (e.g.  
 251 Kanda et al., 2004; Xie and Castro, 2006; Castro et al., 2017; Wingstedt et al.,  
 252 2017). Equations 1 and 2 show the grid-size averaged (filtered) continuity and  
 253 Navier-Stokes equations respectively,

$$\frac{\partial u_i}{\partial x_i} = 0, \quad (1)$$

$$\frac{\partial u_i}{\partial t} + \frac{\partial u_i u_j}{\partial x_j} = -\frac{1}{\rho} \frac{\partial p}{\partial x_i} + \nu \frac{\partial^2 u_i}{\partial x_j \partial x_j} - \frac{\partial \tau_{ij}}{\rho \partial x_j}, \quad (2)$$

254 where  $u_i$  and  $p$  are the resolved or filtered velocity and pressure respectively,  $\tau_{ij}$   
 255 is the Subgrid-scale Reynolds stress,  $\rho$  is the air density, and  $\nu$  is the kinematic  
 256 viscosity,  $x_i$  denotes the coordinates, and  $t$  denotes time. The mixed time scale  
 257 sub-grid scale (SGS) model (Inagaki et al., 2005) was used to avoid using the  
 258 near wall damping functions required in the Smagorinsky SGS model. However,  
 259 reports in the literature (e.g. Xie and Castro, 2009) suggest that because the  
 260 flow is largely building block-scale dependent the airflow should be relatively  
 261 insensitive to the precise nature of the SGS model, as long as the grid resolves  
 262 the inertial range of the turbulence spectra. The LES model embedded in the  
 263 open-source package OpenFOAM v2.1.1 was used. A second-order backward  
 264 implicit scheme in time and second-order central difference scheme in space  
 265 were applied for the discretization in the finite volume method approach. More  
 266 details of methodology can be found in Sessa et al. (2020); Coburn et al. (2022).

### 3.2 Particle Image Velocimetry Data

An important part of the study was to validate a simulation of the atmospheric airflow around the Highfield Campus buildings on flat terrain with experimental data. The data used was high resolution particle image velocimetry (PIV) data obtained from experiments conducted in the University of Southampton's 6.75 m long re-circulating water tunnel (see more details in Lim et al. (2022)) using a 1:2400 scale 3D printed model. It should be noted that the water tunnel model was a simplification in that all the building roofs were made flat, whether they actually were or not. The freestream velocity of the water tunnel experiments was  $U_\infty = 0.46 \text{ ms}^{-1}$ . The average building height was  $h = 6.7 \text{ mm}$  at model scale. This leads to a Reynolds number of  $Re_h \approx 3080$  based on the average building height and the freestream velocity. The model was exposed to a naturally developed boundary layer (Fig. 3c and d). The boundary layer thickness was 83 mm, resulting in a boundary layer thickness to average building height ratio of approximately 12.

The particle image velocimetry (PIV) measurements of the velocity fields were obtained using two 4 mega pixel CMOS cameras and a 100mJ Nd:YAG double pulsed laser. A total of 2000 image pairs were captured at a separation time of 1200  $\mu\text{s}$  and sampling rate of 2 Hz. LaVision's DaVis 8.4.0 software was used for post-processing of the particle images to produce vector maps. The uncertainty in the velocity was estimated to be 2%, mostly due to image distortion and refraction affecting the magnification factor at the edges of the images.

The PIV data used in the study was taken in the streamwise vertical plane equivalent to  $y = 104 \text{ m}$  (full scale) in the computational domain (see Figure 2). Vertical profiles were extracted at 14 locations given IDs 1–14 counting from upstream to downstream, starting from a position equivalent to  $x = 220 \text{ m}$  ( $13.3h$ ) and then at 40 m intervals ( $\Delta x = 2.5h$ ).

## 4 Urban Airflow Over the flat Terrain

### 4.1 Validation against PIV measurements

Figures 5 and 6 show comparisons between the PIV data obtained in the naturally grown turbulent boundary layer and data from the LES case FF8. In both figures the squares are the PIV data showing every fifth data point, while the solid line is the LES data. Vertical profiles of mean streamwise and vertical velocities (Fig. 5), and  $u_{rms}$ ,  $w_{rms}$  and  $\overline{u'w'}$  (Fig. 6) at the 14 stations defined in Section 3.2 starting at  $x = 13.3h$  with an interval  $\Delta x = 2.5h$  are shown. Figure 5 shows slight under-predictions in the LES data at some locations. The discrepancy in the mean axial velocity is within 5% of the experimental data. The vertical velocity differs slightly more, but agreement between the mean velocity profiles in Fig. 5 appears as good as might be expected when comparing to PIV data from a small scale model.

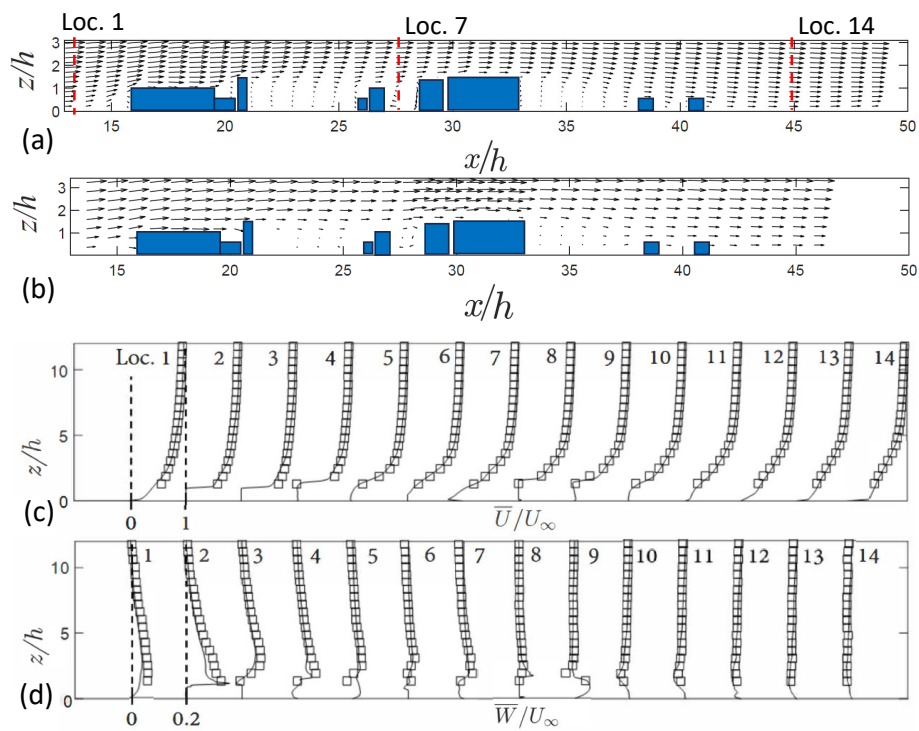


Fig. 5: a) LES case FF8 and b) PIV velocity vectors in vertical plane at  $y = 104$  m. c) mean normalised streamwise velocity. d) mean normalised vertical velocity. lines, LES data; squares, PIV data

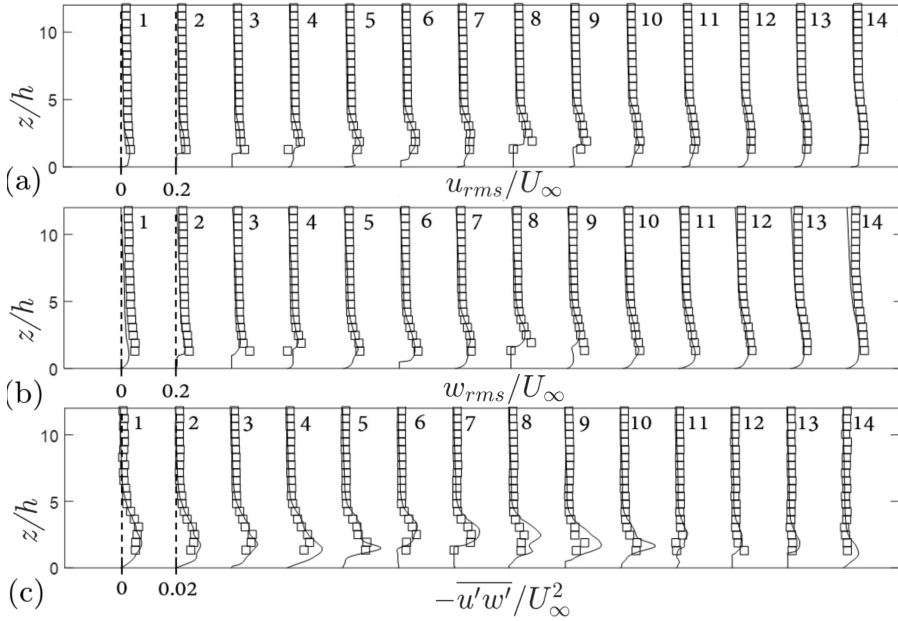


Fig. 6: a) Normalised r.m.s. streamwise velocity fluctuations b) normalised r.m.s. vertical velocity fluctuations, and c) normalised mean Reynolds shear stress. lines, LES data; squares, PIV data

308 Figure 6 shows profiles of the r.m.s. streamwise and vertical velocity fluctu-  
 309 tuations and the mean Reynolds shear stress. There is a small under-prediction  
 310 of the peak values which occur close to the ground and building surfaces, for  
 311 example in the fourth profile in Fig. 6, but also an over-prediction of the mean  
 312 Reynolds shear stress at locations 8-10, again close to building surfaces. Dis-  
 313 crepancies of this type were expected in the near-wall region, as the quality of  
 314 the PIV data was affected by high intensity reflections from the model surface.  
 315 The agreement is very good in the regions devoid of reflections from the laser  
 316 sheet and dominated by the free shear layers which develop downstream of the  
 317 roughness elements. Overall, the level of agreement between the PIV data and  
 318 the case FF8 with the inflow conditions based on the water tunnel turbulence  
 319 quantities is very promising.

#### 320 4.2 Effects of Inflow Turbulence Quantities

321 Two sets of turbulent inflow quantities were used (see Fig. 3). The integral  
 322 length scales used for all cases in this study were the same as those as in Xie  
 323 and Castro (2009), which were  $4h$  in the streamwise direction, and  $1h$  in the  
 324 vertical and lateral (spanwise) directions. The effect of different inflow turbu-

325 lence quantities was evaluated by looking at Location 7 (Fig. 5) which was  
 326 approximately  $15h$  downstream of the leading edge of building array, placed  
 327 in a narrow canyon between two highest ( $1.5h$ ) buildings in the  $y = 104$  m  
 328 plane (Fig. 2). Figures 7 and 8 show comparisons of mean velocities and tur-  
 329 bulance statistics at Location 7 for two sets of inflow conditions and two grid  
 330 resolutions.

331 Figure 7 generally shows only very small differences in the mean veloci-  
 332 ties predicted in cases FF8 and SF8, suggesting that the effect of the inflow  
 333 turbulence quantities on mean flow is small. This confirmed the findings in  
 334 other published studies (e.g. Macdonald et al., 2000; Hanna et al., 2002; Xie  
 335 and Castro, 2008; Sessa et al., 2020; Fossum and Helgeland, 2020). Macdon-  
 336 ald et al. (2000); Hanna et al. (2002) which reported that the mean flow and  
 337 the turbulence fields typically approached equilibrium values after three rows  
 338 of obstacles, which occurred at about  $8h$  downstream, while Xie and Castro  
 339 (2008); Sessa et al. (2020) reported that after more than 6 rows (approx-  
 340 imately  $12h$  downstream) the flow and turbulence fields can be considered  
 341 being in equilibrium state, and Location 7 was at  $15h$ .

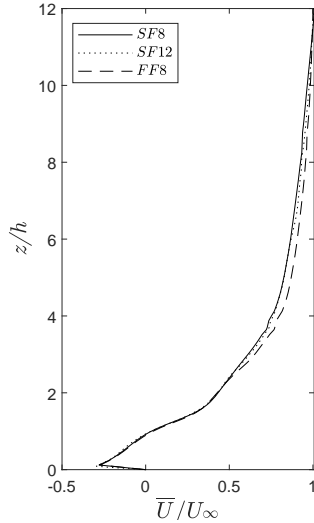


Fig. 7: Vertical profiles of mean normalised streamwise velocity at Location 7 (Fig. 5)

342 Figure 8 shows that the differences in the second order moments of turbu-  
 343 lence statistics between cases SF8 and FF8 are small within and immediately  
 344 above the canopy (e.g. below  $z = 1.5h$ ), but increase above  $z = 1.5h$ , which  
 345 is the height of the building upstream of Location 7. The differences increase  
 346 substantially at heights above  $z = 4h$  where the effect of the urban canopy  
 347 diminishes and the large difference in turbulence level between the two in-

348 flow conditions becomes apparent (Fig. 3). This is because the inlet Reynolds  
 349 stresses for the case FF8 are substantially less than for the other two cases.  
 350 The smaller differences below  $z = 1.5h$  are consistent with the findings in  
 351 Xie and Castro (2008) that the turbulence statistics predicted by LES within  
 352 and immediately above canopy relatively insensitive to the inflow turbulence  
 353 quantities, so long as they are not too unrealistic, and the distance between  
 354 the inlet and the sampling location is large enough (e.g. greater than  $14h$ ).

355 Considering the sensitivity to grid resolution, Figures 7 and 8 show smaller  
 356 differences in the data from cases SF8 and SF12, than between cases SF8 and  
 357 FF8. Overall, it was concluded that the resolution and inflow conditions used  
 358 in case ST8 ext. provided reliable data, and that data from SF8 could be used  
 359 for the assessing the effect of terrain.

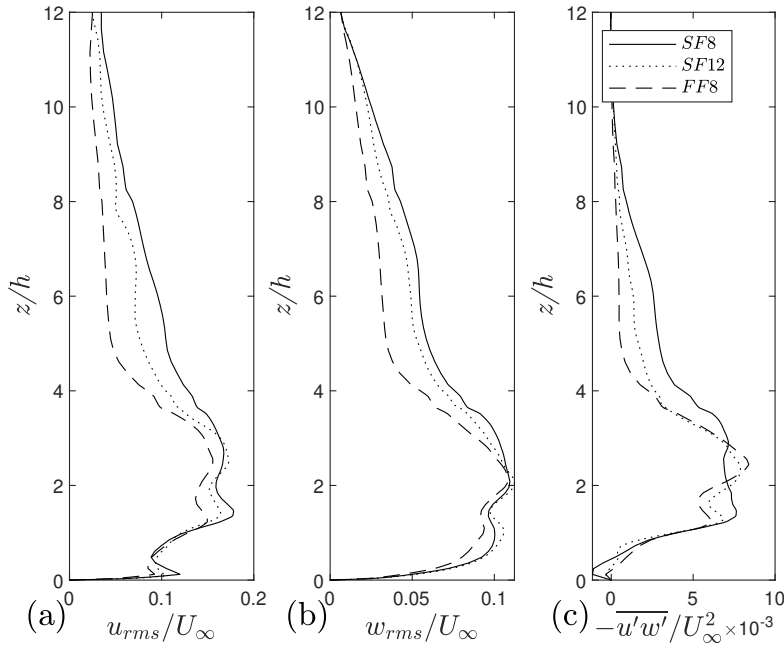


Fig. 8: Same as in Fig. 7, but for a) normalised streamwise velocity fluctuation r.m.s., b) normalised vertical velocity fluctuation r.m.s. and c) normalised vertical Reynolds shear stress



360 **5 Local Terrain Effects – a Comparison between Flat (SF8 ext.)**  
 361 **and Realistic (ST8 ext.) Terrains**

362 5.1 Spatially Averaged Quantities

363 Spatially averaging fluid quantities over a domain that captures real topologi-  
 364 cal features is not trivial. The method adopted in this study is to average data  
 365 at the same above ground level (AGL) height as defined in Equation 3:

$$\langle \phi \rangle_f(z_{AGL}) = \frac{1}{S_t} \int_{(S_f)} \phi(x, y, z_{AGL}) dx dy, \quad (3)$$

366 where  $\phi$  denotes the quantity to be spatially-averaged,  $\langle \cdot \rangle_f$  denotes the spatial  
 367 average over the area not covered by buildings, which is approximately 71%  
 368 of the ground surface within the study domain.  $S_f$  denotes the total area not  
 369 covered by buildings and is constant over the entire AGL height  $z_{AGL}$ . In  
 370 other words, it does not take into account the fluid region that is above a  
 371 building, and of which the coordinates  $(x, y)$  are within the ground perimeter  
 372 of the buildings. This ensures that inconsistencies are not introduced when  
 373 using Eq. 3.

374 To identify the impact of the variation of terrain elevation, hereafter only  
 375 data from cases SF8 ext. and ST8 ext. were the focus for comparison. All  
 376 quantities were normalised by the spatially-averaged mean streamwise velocity  
 377  $U_{6h}$  at  $z = 6h$ . The spatially-averaged mean velocities and turbulence statistics  
 378 are shown in Fig. 9. Albeit the large local differences in the ratio of mean  
 379 velocities (e.g. Fig.12 b and c), Figures 9a shows a negligible difference in the  
 380 spatially averaged dimensionless streamwise velocity between the flat (SF8  
 381 ext.) and real (ST8 ext.) terrain cases. By linearly extrapolating the Reynolds  
 382 shear stress (Fig. 9c) to estimate the effectively friction velocity  $u_*/U_{6h} =$   
 383  $0.096$ , a best fitting of the  $\langle U \rangle$  data above  $z_{AGL} = 4h$  to a logarithmic  
 384 profile gave  $z_0 = 0.08h$ , and displacement  $d = 0.5h$ , which were not dissimilar  
 385 to those in Castro et al. (2017).

386 Below  $z_{AGL} = 2h$ , the dimensionless Reynolds shear stress are essentially  
 387 the same for the two cases SF8 ext. and ST8 ext., while the dimensionless  
 388 turbulent kinetic energy for the case ST8 ext. is slightly less. Above  $z_{AGL} = 2h$ ,  
 389 the case ST8 ext. shows slightly greater turbulent kinetic energy and Reynolds  
 390 shear stress, which is likely due to the local terrain elevation variation. The  
 391 flat terrain case SF8 in Fig. 9 shows a visible difference in the streamwise  
 392 velocity, turbulent kinetic energy and Reynolds shear stress, compared to the  
 393 flat terrain case SF8 ext. This was due to the 15% greater average building  
 394 height, and the 25% less domain height in the case SF8. The overall difference  
 395 is not significant.

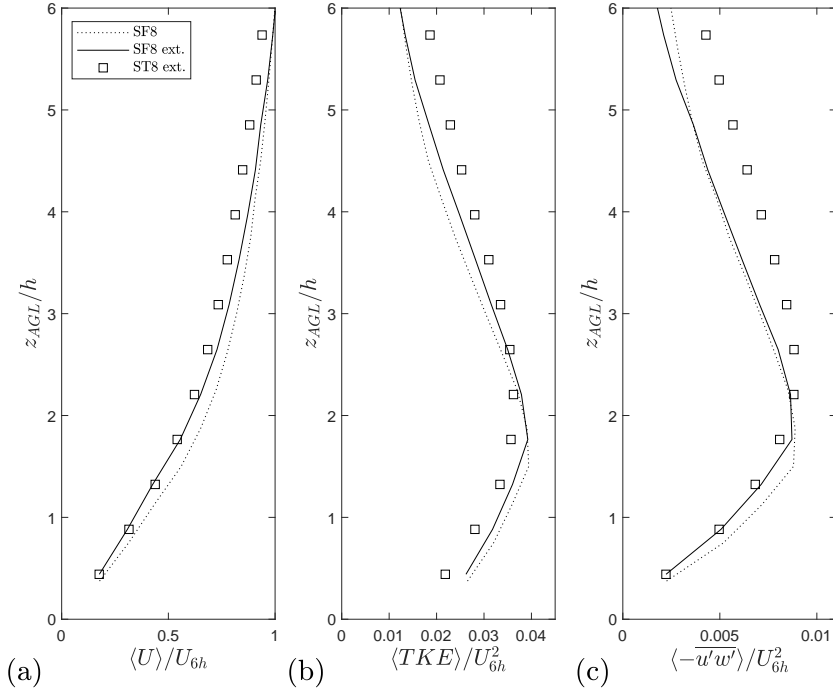


Fig. 9: Dimensionless spatially-averaged a) mean-streamwise velocity, b) turbulent kinetic energy and c) Reynolds shear stress, for cases SF8, SF8 ext. and ST8 ext.

## 396 5.2 Flow and Turbulence at Typical Locations

397 Figure 10 shows the mean streamwise velocity and Reynolds shear stress profiles at the same 14 locations in the plane  $y = 104$  m as in Fig. 5. The turbulence  
 398 statistics on the vertical profiles are set to zero below the ground and building  
 399 surfaces. Figure 10 reveals a visible difference in the mean streamwise velocity  
 400 from including terrain, but the effect on vertical Reynolds shear stress is  
 401 much greater. It was noted that at some locations the vertical mean velocity  
 402 was sensitive to where the data was sampled (not shown). This suggests that  
 403 given such sensitivities it might be extremely difficult to get close agreement  
 404 in vertical mean velocity when comparing numerical and small scale physical  
 405 simulations.  
 406

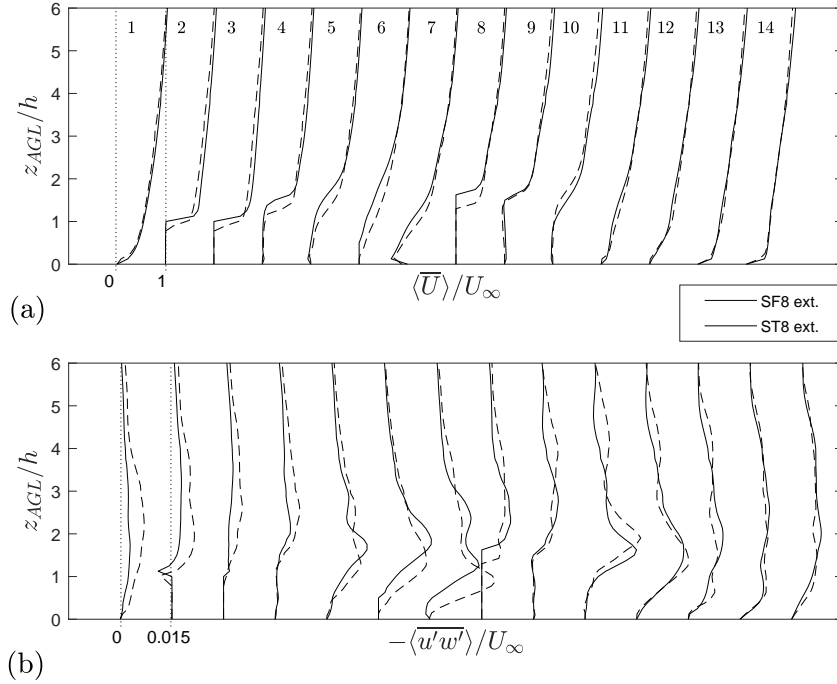


Fig. 10: Vertical profiles across an  $(x, z_{AGL})$  plane at  $y = 104$  m for a) mean streamwise velocity, and b) vertical Reynolds shear stress at the 14 stations shown in Fig.5.  $z_{AGL}$  is the local above ground height.  $U_{6h}$  is the spatially-averaged mean streamwise velocity at  $z_{AGL} = 6h$ . For building locations, see Fig.5a

407 Figure 11 shows a comparison of mean streamwise velocities in the  $(x, z)$   
 408 plane at  $y = -210$  m shown in Fig. 2, for the flat (SF8 ext.) and real (ST8 ext.)  
 409 terrain cases. Figure 11a shows that the boundary layer depth remains almost  
 410 constant throughout the flat terrain domain. This suggests that the inflow  
 411 boundary conditions were set appropriately to produce a fully developed flow  
 412 across the domain. Figure 11b, however, shows that the boundary layer depth  
 413 increases more evidently as it develops downstream, which is due to the terrain  
 414 variation.

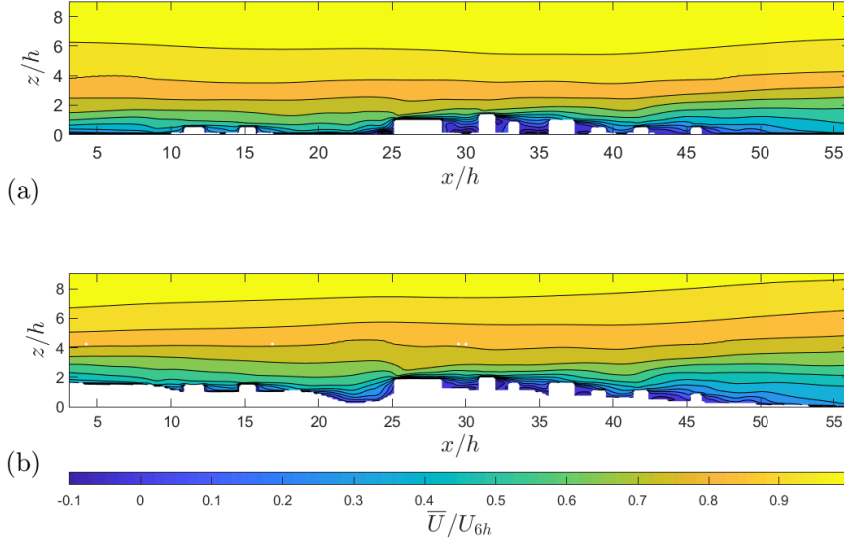


Fig. 11: Mean streamwise velocity in the  $(x, z)$  plane at  $y = -210$  m shown in Fig.2 for a) SF8 ext. and b) ST8 ext.

415 To quantify the effect of terrain on the local mean velocity, the ratio of  
 416 mean streamwise velocity is defined,

$$\bar{U}_{ST8}/\bar{U}_{SF8} = \frac{\|\bar{U}_T(x, y, z_{AGL})\|}{\|\bar{U}_F(x, y, z_{AGL})\|}, \quad (4)$$

417 where  $\|\bar{U}_T(x, y, z_{AGL})\|$  and  $\|\bar{U}_F(x, y, z_{AGL})\|$  are the absolute values of the  
 418 mean streamwise velocity for the real terrain case ST8 ext., and the flat terrain  
 419 case SF8 ext., respectively.

420 Figure 12a shows the elevation contours of the real terrain in the valley  
 421 region ( $0 \leq x/h \leq 40$ ,  $-15 \leq y/h \leq 0$ ). Fig. 12 b and c show the ratio  
 422  $\bar{U}_{ST8}/\bar{U}_{SF8}$  of the mean-streamwise velocities at  $z_{AGL}/h = 0.56$  and  $2.3$ , re-  
 423 spectively. **It is to be noted the fluid regions above buildings are not shown.**  
 424 The ratio  $\bar{U}_{ST8}/\bar{U}_{SF8}$  correlated positively well with the terrain elevation. In  
 425 general, a high elevation location was associated with a high ratio  $\bar{U}_{ST8}/\bar{U}_{SF8}$ ,  
 426 and vice versa. At an AGL height of more than twice average building height  
 427 (i.e.  $2.3h$ ), within and immediate downwind of the valley that was approxi-  
 428 mately  $5h$  in width and  $h$  in depth, the ratio  $\bar{U}_{ST8}/\bar{U}_{SF8}$  showed a minimum  
 429 less than 70% above the valley, and a maximum 120% immediately downwind  
 430 of the valley. Within the urban canopy at an AGL height of  $0.56h$ , the correla-  
 431 tion between the mean streamwise velocity ratio and the terrain elevation was  
 432 even more evident, albeit the disturbance due to the buildings. Th correlation

433 between the terrain elevation and streamwise velocity was because the bound-  
434 ary layer flow could not immediately adjust to “body-fit” the local terrain, in  
435 particular at the valley trough and the crest. The enhanced streamwise ve-  
436 locity at the valley crest could also be due to the so-called “Bernoulli effect”.  
437 The visual strength of the correlation between elevation and mean streamwise  
438 velocity ratio suggests that it might be used to account for local terrain effects  
439 when flat terrain has to be used in experiments or numerical simulations.

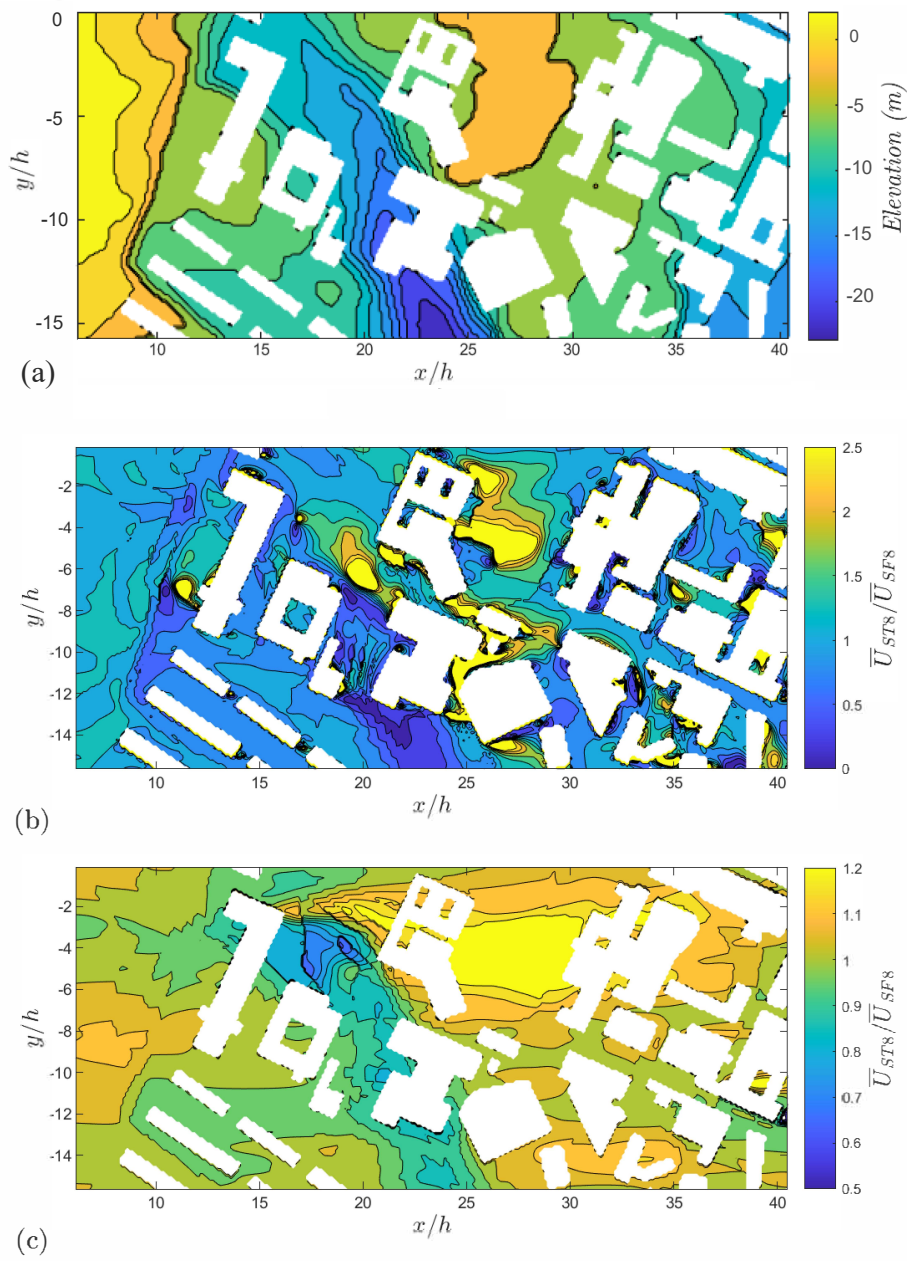


Fig. 12: a) Elevation contours of the real terrain in ST8 ext. with the inlet ground placed at elevation  $z = 0$  as in Fig. 2, b) the ratio  $\bar{U}_{ST8}/\bar{U}_{SF8}$  of the mean-streamwise velocity for ST8 ext. and SF8 ext. at  $z_{AGL}/h = 0.56$ , and c) at  $z_{AGL}/h = 2.3$ . The fluid regions above the buildings are not shown but left blank

440 Figure 13 shows contour plots of the dimensionless turbulent kinetic energy  
441 at  $z_{AGL}/h = 0.56$  for cases SF8 ext. and ST8 ext. For most of the area, the  
442  $TKE$  within the canopy for the real terrain case was lower than that in the flat  
443 terrain one (see Fig. 9). Figure 13a shows high  $TKE$  in front and behind large  
444 buildings. This was because 1) higher  $TKE$  at the average building height (see  
445 Fig. 3) was entrained into this altitude, and 2) the large buildings produced  
446 more turbulence into the wake region. Compared to the flat terrain case, Figure  
447 13b shows less evident increase in  $TKE$  in front and behind large buildings,  
448 in particular over the valley region. Low  $TKE$  was expected over the valley  
449 region at  $z_{AGL} = 0.56h$  as the deep valley preventing convection of high  $TKE$   
450 into low altitude. Another reason was perhaps due to the downslope, which  
451 effectively reduced the average altitude of buildings.

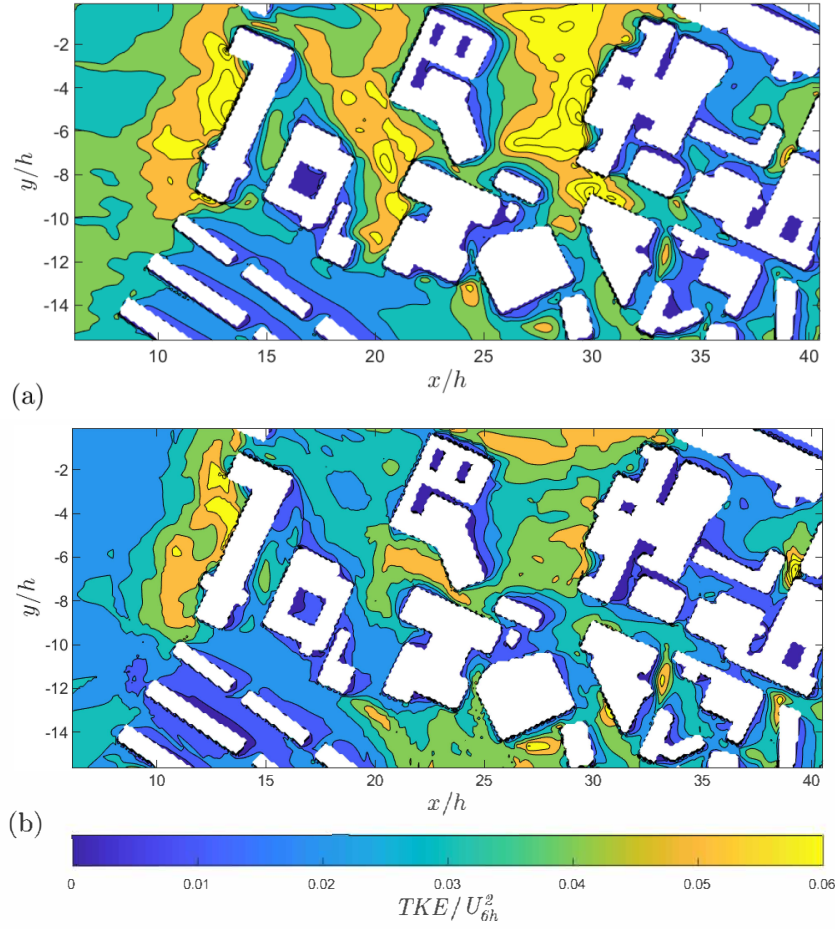


Fig. 13: Dimensionless turbulent kinetic energy at  $z_{AGL} = 9$  m ( $0.56h$ ) for a) SF8 ext., and b) ST8 ext.

452 Due to the difference in local packing density, the size of the buildings, the  
 453 spatial scale and the amplitude of the terrain elevation variation, the effect of  
 454 terrain on the local flow and turbulence quantities differed substantially from  
 455 place to place. In this study we focused on four typical stations located in  
 456 the valley (see Fig. 4). Figure 14a shows vertical profiles of mean streamwise  
 457 velocity at the four stations for the flat (SF8 ext.) and real (ST8 ext.) terrains.  
 458 At station 4 the valley was deep and wide and had a significant effect on mean  
 459 streamwise velocity. At station 3, the effect of the valley was also evident. At  
 460 stations 1 and 2, the effect of terrain on the mean streamwise velocity was  
 461 much less. This was because the valley was very shallow at stations 1 and 2,



462 and tall buildings were immediately upstream of them which played a more  
463 dominant role on the local wind.

464 Figure 14b-d show normal stresses  $\overline{u'u'}$ ,  $\overline{w'w'}$  and Reynolds shear stress  
465  $\overline{u'w'}$ , respectively. These second order turbulence statistics were highly de-  
466 pendent on the local terrain and upstream buildings. Approximately 60m up-  
467 stream of station 1, a tall and wide L shape building was located, from where  
468 a steep velocity gradient (Fig. 14a) and a strong shear layer with great tur-  
469 bulent kinetic energy and Reynolds shear stress at the building height (Fig.  
470 14b-d) were generated and convected downstream. A square shape building  
471 was placed 30m upstream of station 2, which had an above-ground level height  
472 approximately 20 m, produced an evident shear layer (Fig. 14a) and increased  
473 turbulent kinetic energy and Reynolds stress (Fig. 14b-d) at the building  
474 height at station 2. Overall, the tall buildings upstream of stations 1 and 2  
475 played a dominant role on the local wind field and turbulence, and the down-  
476 stream valley enhanced this effect.

477 Station 3 was located in a narrow spacing between buildings in the valley,  
478 where the vertical profiles of  $\overline{U}/U_{6h}$ ,  $\overline{u'u'}/U_{6h}$  and  $\overline{u'w'}/U_{6h}$  were respectively  
479 similar to those at station 2, but with a weaker shear layer at the local building  
480 height. The  $\overline{w'w'}/U_{6h}$  in the vicinity of the ground was very different between  
481 the flat and real terrains, which was because of the narrow spacing between  
482 buildings and the steep terrain gradient. There were no large and tall buildings  
483 immediately upstream of station 4. The vertical profiles of mean streamwise  
484 velocity, Reynolds normal and shear stresses for case SF8 ext. hardly showed  
485 an evident shear layer at the average building height  $h$ , whereas those for  
486 case ST8 ext. showed a weak local shear layer at  $0.5h$ , which was caused by  
487 the gentle slope approximately 70 m upstream. This means that it would be  
488 extremely challenging to develop a simple method to precisely account for  
489 the effect of terrain and so correct the turbulent stresses obtained from a flat  
490 terrain model.

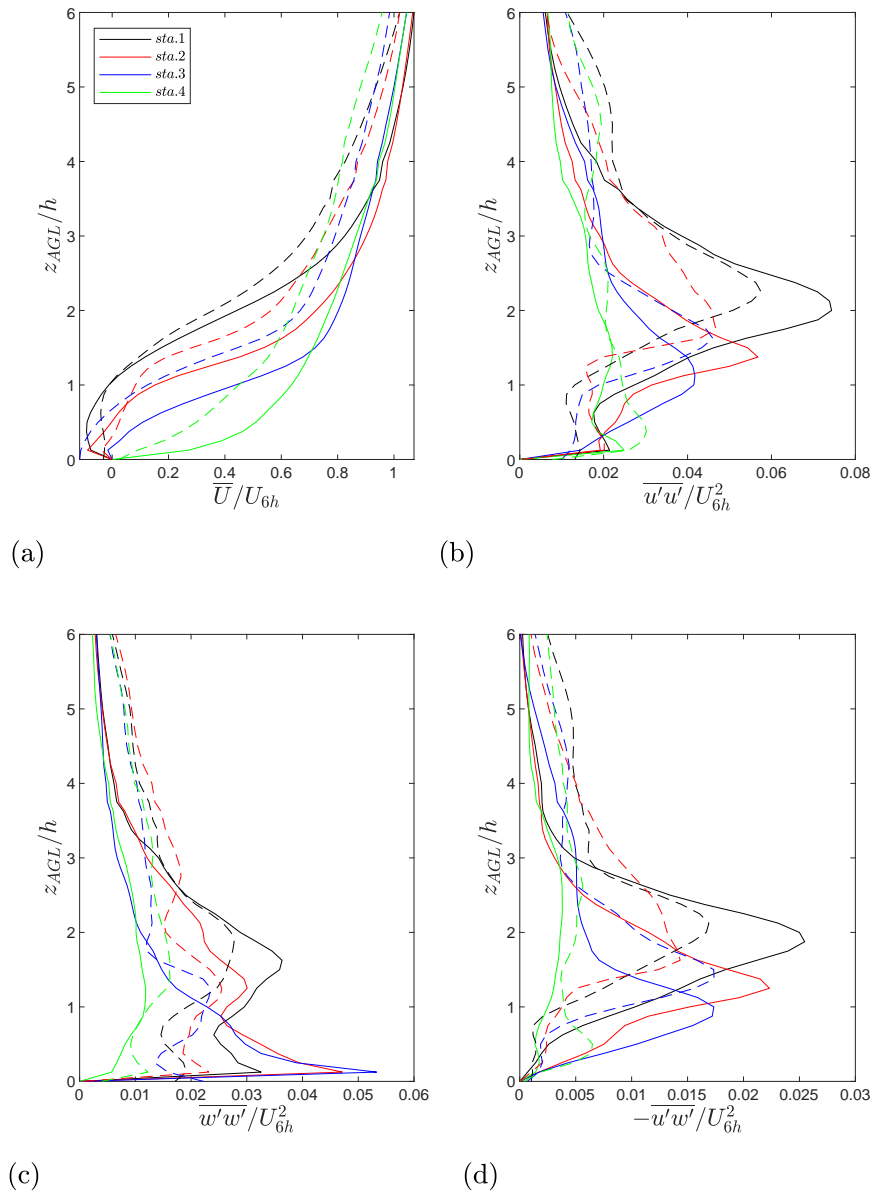


Fig. 14: Vertical profiles of a) streamwise mean velocity, b) streamwise normal stress, c) vertical normal stress and d) vertical Reynolds shear stress, at stations 1 – 4. Solid line, SF8 ext. Dashed line, ST8 ext. See the coordinates of the stations in Fig. 4

491 Figure 15 shows four mean streamwise velocity profiles at  $y = -28$  m,  
 492  $-102$  m,  $-152$  m, and  $-210$  m, at  $z_{AGL} = 48$  m ( $3h$ ) (see Fig. 4), of which the  
 493 spanwise coordinates ( $Y Loc.1$ ,  $Y Loc.2$ ,  $Y Loc.3$  and  $Y Loc.4$ ) are respectively  
 494 the same as the 4 stations ( $sta.1$ ,  $sta.2$ ,  $sta.3$ , and  $sta.4$ ) in Fig. 14. Overall,  
 495 the mean streamwise velocity profiles at the 4 spanwise locations over the flat  
 496 terrain were highly similar in shape and magnitude with the corresponding  
 497 ones over the real terrain, suggesting that the buildings played a dominant  
 498 role, while the local terrain played a role of modulation. This was because  
 499 the horizontal scale of the terrain elevation variation was much greater than  
 500 building scale (see Figs. 2,4), albeit the terrain elevation magnitude was similar  
 501 as the building height. For the  $Y Loc.1$  profile there is a peak negative velocity  
 502 at approximately  $x = 700$  m, which is close to the tallest building in the  
 503 campus. Within and immediate above the urban canopy, a positive correlation  
 504 between the flat terrain and real terrain data was more complicated (Fig. 12a),  
 505 but evident.

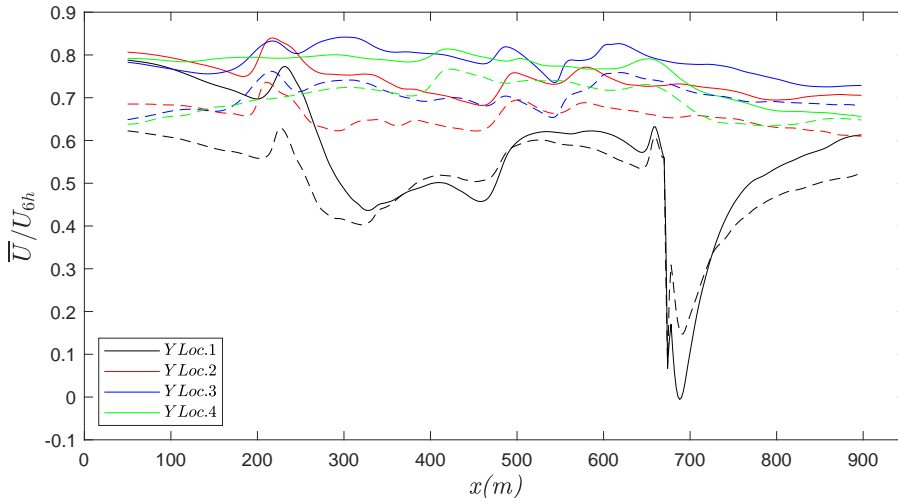


Fig. 15: Four streamwise mean velocity profiles along the streamwise direction, respectively at  $y = -28$  m ( $Y Loc.1$ ),  $-102$  m ( $Y Loc.2$ ),  $-152$  m ( $Y Loc.3$ ), and  $-210$  m ( $Y Loc.4$ ), and  $z_{AGL} = 48$  m ( $3h$ ) (Fig. 4). Solid line, SF8 ext. Dashed line, ST8 ext.

### 506 5.3 Internal Boundary Layers

507 The internal boundary layer (IBL) depth for both the flat (SF8 ext.) and  
 508 real terrain (ST8 ext.) cases was estimated using the methodology proposed  
 509 in Sessa et al. (2018) by determining the critical slope-change point of the  
 510 spatially averaged vertical normal stress profiles  $\overline{w'w'}$ . The spatial average  
 511 being calculated as defined below,

$$\langle \phi \rangle_s(x_m, z_{AGL}) = \frac{1}{2h \times Span} \int_{(x_m-h)}^{(x_m+h)} \left( \int_{(Span)} \phi(x, y, z_{AGL}) dy \right) dx, \quad (5)$$

512 where  $\langle \cdot \rangle_s$  denotes the spatial average over a slice ( $(x_m - h) \leq x \leq (x_m + h)$ ,  
 513  $-300 \text{ m} \leq y \leq 300 \text{ m}$ ), which accounts for the span of the campus ( $Span$ ).  $\phi$   
 514 denotes the quantity (e.g.  $\overline{w'w'}$ ) to be spatially-averaged. The comprehensive  
 515 spatial average method of Xie and Fuka (2018) was used. This meant that  
 516 where the average slice crossed a building all the solid regions at height  $z_{AGL}$   
 517 within the averaging region were included, but the value of the quantity was  
 518 set to zero within them.

519 Figure 16 presents contour plots of the normalised spanwise averaged vertical  
 520 normal stresses for cases SF8 ext. and ST8 ext, where the terrain surface  
 521 was the lowest terrain elevation across the span. Overall, the two plots showed  
 522 a similar developing internal boundary layer with an average thickness of about  
 523  $4h$ . At the centre of the domain ( $x/h \approx 29$ ), the large  $\overline{w'w'}$  value showed the  
 524 north-south University Road crossed the entire campus. There were also some  
 525 evident differences. At the west end of the campus, the internal boundary layer  
 526 thickness over the real terrain increased abruptly due to local downslope start-  
 527 ing from the west end of the campus up to the first valley. Immediately above  
 528 the valley bottom surface, there was a region in which the values of  $\overline{w'w'}$  were  
 529 very low. This was because of the valley effect and the use of the compre-  
 530 hensive spatial average method (Eq. 5). Downwind of the University Road, the real  
 531 terrain case ST8 ext. showed slower IBL spreading in the vertical direction,  
 532 compared to the flat terrain case.

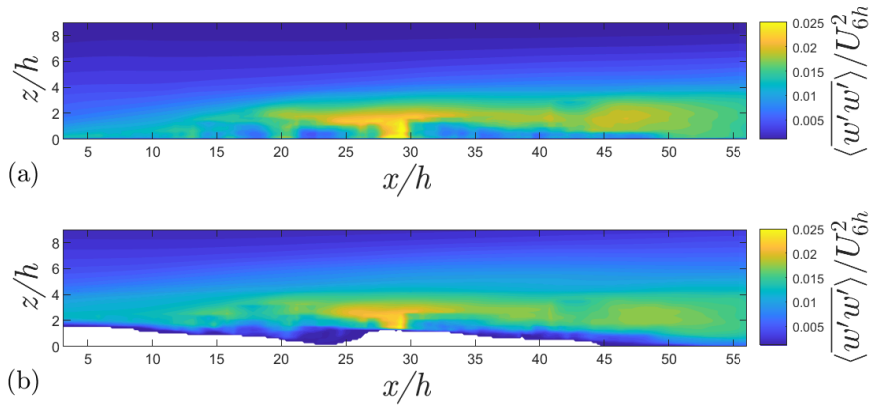


Fig. 16: Spanwise averaged normalised vertical normal stress for a) SF8 ext., and b) ST8 ext.

533 Figure 17a shows estimated IBL depths over the urban canopy for the  
 534 flat (SF8 ext.) and real terrain (ST8 ext.) cases. To show an example of the

535 estimation approach for the IBL depth, Figure 17b shows spanwise-averaged  
536 vertical normal stress  $\overline{w'w'}$  for the flat terrain case at  $(x - x_{LE})/h=2, 6, 10,$   
537  $14, 18, 22, 26$  and  $30$ , marked with the critical slope-change point (i.e. the  
538 intersection of the two straight lines). The critical slope-change in Fig. 17b  
539 was visible, but was not evident as that over a regular cuboid array in Sessa  
540 et al. (2018). This was because of the random nature of the array of buildings  
541 in the case SF8. ext, which generated a thicker but weaker shear layer above  
542 the canopy (e.g. Xie et al., 2008) than a uniform array. The average thickness  
543 above the ground level for SF8 ext. was about  $4h$ , whereas it was about  $3h$   
544 above ground level for a uniform array of cuboid blocks with a packing density  
545 33% in Sessa et al. (2020). The random distribution of the building height,  
546 building size and spacing in the case SF8 ext. were the main factors causing  
547 the fast growth of the IBL thickness.

548 The interface of the internal and external boundary layers over the real  
549 terrain was much more difficult to identify than that over the flat terrain.  
550 Considering the uncertainties due to the variation of terrain elevation in the  
551 near-inlet region, only the IBL thickness downstream of  $x = 10h + x_{LE}$  was  
552 estimated. The IBL thickness for case ST8 ext. measured from  $z = 0$  was close  
553 to that for case SF8 ext. while measured from the local ground level it was  
554 slightly less than that for case SF8 ext. Figure 17a shows that the IBL thickness  
555 curves for both cases oscillated while the IBL progressed downstream, differing  
556 from that over a uniform array of buildings (e.g. Sessa et al., 2018). The  
557 oscillations were caused by changes in the elevation of the underlying surface,  
558 i.e. buildings and terrain.

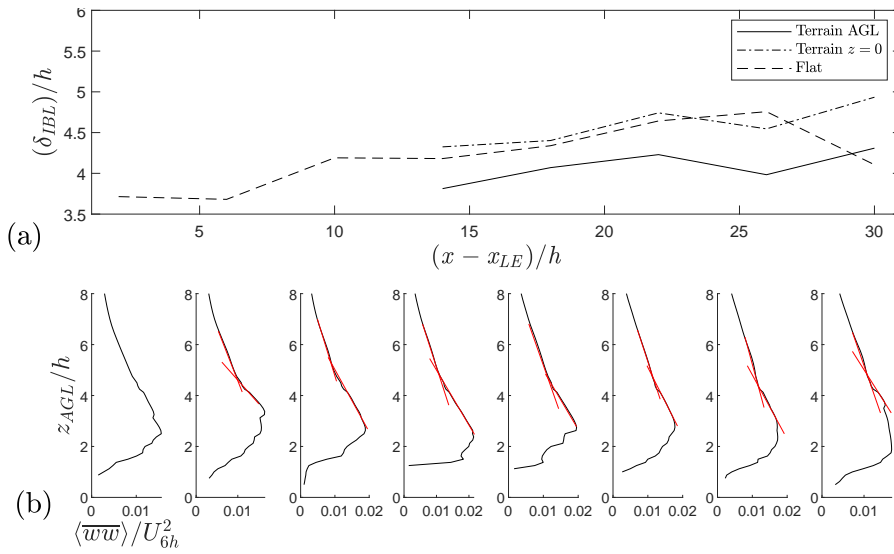


Fig. 17: a) Development of IBL (AGL) from the leading edge of the canopy, for flat (SF8 ext.) and real (ST8 ext.) terrain cases. The leading edge of the canopy occurs at  $x_{LE} = 14h$  in Fig. 17. b) Spanwise-averaged vertical normal stress  $\overline{w'w'}$  over the flat terrain (SF8 ext.), marked with the critical slope-change point (i.e. the intersection of the two straight lines)

## 559 6 Concluding Remarks and Discussion

560 LES simulations were carried out to simulate atmospheric airflows over the  
 561 University of Southampton Highfield Campus considering both flat and real  
 562 terrains, with the aim of quantifying and understanding the impact of street  
 563 scale ( $O(0.1 \text{ km})$ ) variations in urban terrain on urban aerodynamics and  
 564 turbulent boundary layer quantities. It is to be noted that the current case  
 565 study is a considerably simplified one for terrain effect. Further studies should  
 566 consider thermal stratification, tree effect and various wind directions.

567 To assess the sensitivity of the results to uncertainties in the inflow tur-  
 568 bulance quantities input to the synthetic turbulence inflow conditions, sim-  
 569 ulations were made with data from two experimental sources. The first was  
 570 “simulated atmospheric boundary layer” data generated from the University  
 571 of Surrey EnFlo wind tunnel, the second was naturally generated boundary  
 572 layer data from the water tunnel at the University of Southampton. The LES  
 573 data showed that turbulence statistics sampled at a sufficiently large distance  
 574 from the inlet (e.g. more than 10 average building heights), within and im-  
 575 mediately above the urban canopy, were relatively insensitive to the precise  
 576 inflow Reynolds stresses, given the same inflow integral length scale and mean  
 577 streamwise velocity. This does not undermine the idea that street and city

578 scales of airflow are coupled as there were substantial differences in the turbu-  
579 lence quantities above twice average building height.

580 A systematic comparison of LES predictions of atmospheric airflows over  
581 the flat and real terrains showed that capturing terrain effects was crucial,  
582 where the height variation of a street-scale ( $O(0.1 \text{ km})$ ) topographic feature  
583 was of the same order of magnitude as the neighbourhood buildings. This  
584 was perhaps what one would expected. The ratio between realistic and flat  
585 terrains of time-mean streamwise velocity at the same ground level height  
586 over a terrain crest location can be greater than 2, while over a valley trough  
587 it can be less than 0.5. The correlation between the mean streamwise velocity  
588 and the terrain elevation is evident within and immediately above the urban  
589 canopy, despite the disturbance due to the buildings. To enable corrections to  
590 be developed for experimental and numerical data acquired from flat terrain  
591 simulations, it is crucial to quantify and understand how street-scale terrain  
592 variations modulate the local mean velocity and turbulence statistics at a given  
593 above-ground level (AGL) height.

594 The global (average) gradient of the west-east downslope of the studied do-  
595 main is much smaller ( $\approx 2.3^\circ$ ) than the local terrain gradients, and contributes  
596 little to the evident modulations observed in the local mean velocity field. The  
597 small global gradient yields negligible discrepancy in the horizontally averaged  
598 mean streamwise velocity against the AGL height.

599 The significant impact from the local terrain features ( $O(0.1 \text{ km})$ ) on the  
600 local airflow and turbulence, and on the global quantities, such as the depth of  
601 the spanwise-averaged internal boundary layer and spatially-averaged turbu-  
602 lent kinetic energy ( $TK E$ ), highlights the crucial importance of taking it into  
603 account of the prognostic numerical models. In the micro-scale engineering  
604 type models, a fine mesh for resolving these small terrain feature, as well as  
605 the buildings, is an option for improving the prediction of near-field dispersion  
606 and the urban micro-climate. Such small terrain features in a grid of the future  
607 high-resolution meso-scale models of a mesh resolution ( $O(0.1 \text{ km})$ ) is consid-  
608 ered as a heterogeneous underlying surface, and an advanced parameterisation  
609 for an inclusion of the heterogeneity effect is required.

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**620 Declarations****621 Ethical Approval**

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**623 Competing interests**

624 No, I declare that the authors have no competing interests as defined by  
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**627 Authors' contributions**

628 Coburn: carried out simulations, experiments and analysis; prepared figures,  
629 wrote the main manuscript text. Vanderwel: supervised the experimental work;  
630 prepared the experimental facilities. Herring: supervised the design of the  
631 study, reviewed and edited the MS. Xie: Project administration; supervised  
632 simulations and analysis; wrote the main manuscript text. All authors re-  
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**637 Availability of data and materials**

638 The datasets generated during and/or analysed during the current study are  
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**640 Conflict of interest**

641 The authors declare that they have no conflict of interest.

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