

1 **Active control of sound through full-sized open windows**

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**20 Abstract**

21 There is a pressing need to address urban sustainability challenges of increasing ambient  
22 temperatures and noise levels in densely-populated, high-rise cities. Solutions that utilise active  
23 noise control on open windows to reduce indoor noise levels seem promising, as natural  
24 ventilation is still maintained. Active noise control utilizes acoustic transducers arranged  
25 around the open window to generate a secondary incidence noise that destructively interferes  
26 with the real noise. The two most common techniques of transducer arrangement, distributed  
27 and boundary layouts, are investigated for the typical single-glazed sliding window. Finite  
28 element method is used to establish the control performance of the active noise control system  
29 and the passive attenuation provided by the sliding window. Based on the investigated  
30 fundamental limits of active control, the distributed layout has consistently yielded better  
31 performance than the boundary layout. The distributed-layout method can also reduce noise  
32 more effectively than a fully-glazed window. Moreover, sources distributed only in the partial  
33 opening of a simulated sliding window can attenuate noise as effectively as the fully-glazed  
34 window. The distributed-layout method is tested on a full-sized window, where the active  
35 control system has up to 16 channels and evenly distributed across the window opening. In the  
36 test with tonal sounds, the feasibility of the active control system is demonstrated. The  
37 experimental results have validated the simulation findings for normal incidence plane waves.

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39 **Keywords:** Active Noise Control, Finite Element Method, Noise Mitigation Through Open  
40 Windows, Building Acoustics

## 41 **1 Introduction**

42 Noise pollution is a pressing urban sustainability challenge for urban planners. Increasing  
43 urbanisation of the global population has driven common dwellings into high-rise buildings.  
44 This creates a dilemma between convenience and noise exposure as planners must decide the  
45 proximity of transport infrastructure (the noise source) to the housing estates. Noise barriers, a  
46 common noise mitigation measure in densely populated high-rise cities, only partially alleviate  
47 the noise problem as they inadvertently diffract noise to the upper floors of nearby high-rise  
48 buildings.

49 Therefore, there is an increasing need in controlling noise at the receiver end, such as noise that  
50 propagates through window openings. Furthermore, the importance of natural ventilation as a  
51 sustainable solution for rising ambient temperatures, has increased the demand for noise  
52 mitigation measures that retain maximum natural ventilation.

53 Passive noise control techniques have been proposed to increase the noise insulation  
54 performance of common single-glazed windows. Kang investigated the use of staggered panels  
55 with louvers (lined with micro-perforated absorbers) in between the panels. The performance  
56 of the staggered panels outperformed the closed single glazed windows, while allowing some  
57 natural ventilation, and without obstructing daylight [1]. Tong et al. also adopted the staggered  
58 panel “plenum” window approach and completed a full-scale field study yielding a maximum  
59 of 9.5 dB of insertion loss [2,3], albeit at a cost of reduced airflow. Huang et al. improved the  
60 noise reduction performance of the staggered panel system to 12 dB, by adopting a hybrid  
61 active and passive noise control system [4,5]. To combat noise pollution due to vehicle  
62 powertrain noise, Lee et al. proposed an experimental louver system based on the sonic crystal  
63 concept and reported a maximum insertion loss of 7.7 dB at 1100 Hz [6].

64 The passive and hybrid solutions, however, propose heavy modifications that changes the  
65 functionality of common single-glazed window systems. Furthermore, the natural ventilation  
66 airflow rates can be reduced by up to 2 – 4 times [4]. Hence, noise control strategies that retain  
67 maximum natural ventilation are key to meeting urban sustainability challenges. Moreover,  
68 noise mitigation strategies that augment onto existing windows can be easily removed when  
69 the noise has been mitigated at the source (e.g., better traffic management, completed  
70 construction projects, etc.).

71 To retain airflow rates of common single-glazed windows, several active noise control systems  
72 for open windows have been developed. Active noise control (ANC) systems are based on the  
73 principle of wave superposition, and thus require transducers (e.g., loudspeakers) that actively  
74 interfere (destructively) with the noise wave to achieve reduction. The ANC systems  
75 introduced will be grouped by their source arrangement strategies, namely, boundary and  
76 distributed layout methods.

77 Boundary layout ANC systems aim to minimise the physical obstructions in the opening of the  
78 window by distributing the control sources on the boundary, i.e., perimeter of the window. For  
79 instance, Kwon and Park, placed 8 control sources around the perimeter of a  $900 \text{ cm}^2$  ( $30 \times 30$   
80  $\text{cm}^2$ ) window in a scaled-down mock up, and achieved global control of up to 10 dB in the  
81 room interior [7]. The elaborate setup, however, warrants further investigation for scaling to  
82 full-sized windows. Although real-time adaptive systems mounted on tilt [8] and sliding  
83 windows [9] have been developed recently, control is only effective from 100 to 300 Hz with  
84 a  $2110 \text{ cm}^2$  ( $56 \times 142 \text{ cm}^2$ ,  $2^\circ$  tilt, 5 cm gap) and  $225 \text{ cm}^2$  ( $13 \times 75 \text{ cm}^2$ , sliding) opening,  
85 respectively. Recent advancements in boundary layout ANC systems on a partially opened  
86 regular tilt window ( $910 \times 910 \text{ cm}^2$ ) yielded up to 13 dB of control between 100 to 800 Hz,  
87 albeit with large transducers ( $\varnothing 8 \text{ cm}$ ) [10].

88 In comparison, distributed layout ANC systems are designed to achieve global noise  
89 attenuation in the room by arranging control sources within the aperture. Murao and Nishimura  
90 demonstrated a real-time ANC system with 4-channels on a  $625 \text{ cm}^2$  ( $25 \times 25 \text{ cm}^2$ ) square  
91 opening, achieving broadband attenuation of 10 dB from 0.5 to 1.5 kHz [11,12]. A virtual  
92 sound barrier (VSB) developed for a baffled rectangular opening also utilises the distributed  
93 control strategy [13,14]. The VSB system consists of 6 control sources distributed uniformly  
94 over the  $2881 \text{ cm}^2$  ( $43 \times 67 \text{ cm}^2$ ) aperture. Although the VSB was intended for frequencies  
95 below 500 Hz, broadband attenuation of up to 20 dB was achieved for a relatively large  
96 opening. The prior work mentioned thus far is summarised in Table 1.

97 Through recent developments, the apparent advantage of distributed over boundary layout  
98 ANC systems lie in their scalability. With the same number of sources, the upper frequency  
99 limit after which performance is poor, is lower in boundary layout than the distributed layout  
100 [15]. Since the control of diffraction around the edges of the aperture become less important as  
101 the wavelength decreases relative to the size of the aperture, the attenuation performance of the  
102 boundary layout will degrade as the aperture increases [16].

103 Since existing distributed control ANC studies have focused on the control of noise through  
104 unobstructed apertures of limited size, this paper will focus on typical full-sized single-glaze  
105 sliding windows as they are prevalent throughout the world. Firstly, as a benchmark for active  
106 control performance, the passive attenuation of the single-glaze sliding window is determined  
107 for increasing aperture sizes to mimic the mechanism of regular sliding windows. Secondly,  
108 using a single channel system, the physical limits of active control are compared numerically  
109 under different degrees of window glazing between the distributed and boundary layout. The  
110 comparison aims to investigate the limits of a proposed boundary layout [9,17] against the  
111 suggested positioning of active control sources away from the wall edges [18]. Thirdly, to  
112 quantify the physical limitations of a multichannel distributed layout active control system

**Table 1: Summary of prior work in the active control of sound through apertures**

Author	Layout	Type	Window Dimensions (W×H cm <sup>2</sup> )	Opening Size (cm <sup>2</sup> )	No. of Control Sources	Type of Noise	Reduction (Global/Local)
Window							
Murao 2012 [11]	Distributed	Open Aperture	25 × 25	25 × 25	4	BLWN (0.5 to 2kHz)	10-15 dB (Global)
Kwon 2013 [7]	Boundary	Open Aperture	30 × 30	30 × 30	8	BLWN (0.4 to 1 kHz)	Up to 10 dB (Global)
Paines 2014 [8]	Boundary	Tilt Window (Hopper)	56 × 142	5cm Gap 2° Tilt	Not stated	Real aircraft pass-by (0.2 to 0.16 kHz)	3 dB (Global)
Carne 2016 [9]	Boundary	Sliding Window	75 × 75	13 × 75	5	Traffic Noise (<300 Hz)	15.5 dB (Not Stated)
Hanselka 2016 [10]	Boundary	Tilt Window (Hopper)	91 × 91	Not stated	8	BLWN (0.1 to 1 kHz)	13 dB (Local)
Opening of baffled rectangular cavity							
Wang 2015, 2016 [13,14]	Distributed	Open Aperture	-	43 × 67	6	BLWN (<0.5 kHz)	~15 dB (Global)
Wang 2017 [19]	Boundary	Open Aperture	-	43 × 67	8	BLWN (<1 kHz)	10 dB (Local, 0.2 m around error points)
Wang 2017 [19]	Boundary	Open Aperture	-	43 × 67	32	Tonal (<1 kHz)	~20dB (Global)
Wang 2017 [19]	Distributed	Open Aperture	-	43 × 67	32	Tonal (<1 kHz)	~20dB (Global)

113 implemented on the sliding window, the control performance is investigated numerically for  
 114 the full-range of noise incidence angles. Lastly, the feasibility of a real-time distributed-layout  
 115 ANC system is investigated on a full-sized two-panel sliding window. The size of the  
 116 simulation model closely models the experimental setup for direct comparisons.

## 117 2 Acoustic considerations

118 The global effectiveness of ANC for windows treats the open aperture as the noise source to  
 119 be controlled. At frequencies where the wavelengths are much smaller than the size of the  
 120 aperture, the control problem approximates the free-field condition [20] and thus, the  
 121 distributed control strategy should be used over the boundary technique. Intuitively, this

122 implies that when the wavelengths are large compared to the aperture size, relatively few  
123 sources are required, suggesting that the boundary layout can provide effective control. On the  
124 contrary, the influence of diffraction becomes important at large wavelengths and has been  
125 shown to substantially limit the performance of configurations with few sources distributed  
126 across the aperture as well as along the boundary [16,18,20].

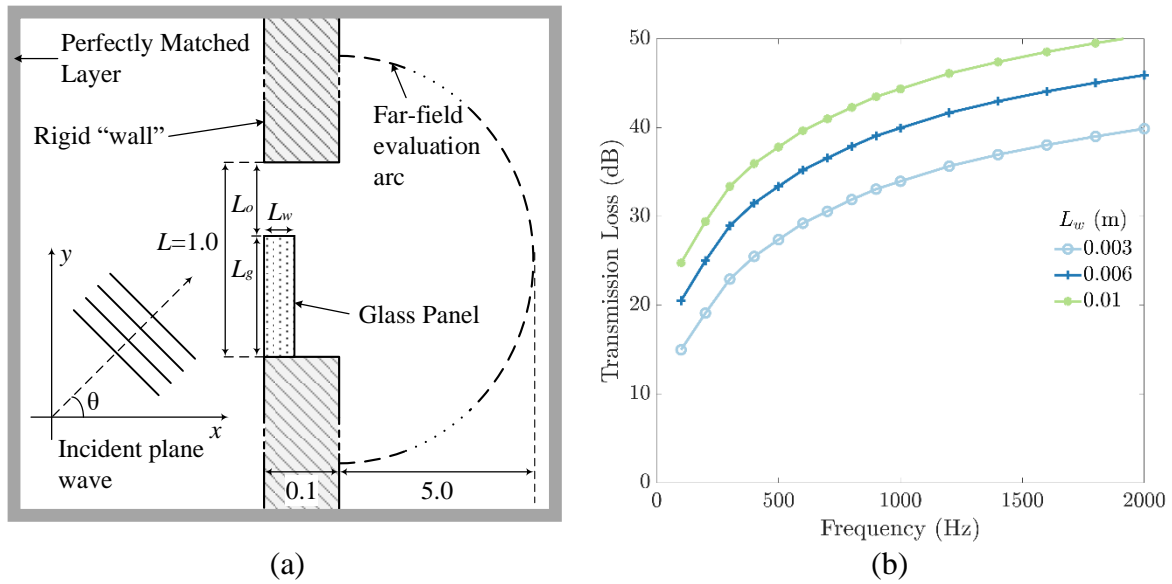
127 Moreover, as the noise incidence angle increases, the number of control sources must increase  
128 to maintain the same attenuation performance. This relation arises from the inverse relationship  
129 of the minimal separation distance between the sources, and  $1 + \sin \theta$ , where  $\theta$  is the angle  
130 of noise incidence [16,18,20].

131 Although the analytical solution indirectly suggests that the attenuation performance of the  
132 boundary control strategy will degrade in proportion to an increase in aperture size; the  
133 influence of diffraction through the aperture in a rigid wall, and the practicality of the boundary  
134 control strategy warrants further investigation.

### 135 **3 Numerical Study**

#### 136 **3.1 Passive insulation of single-glazed windows**

137 Sound insulation provided by a tightly-sealed, 6 mm thick, single-glazed window is a  
138 reasonable benchmark to grade the attenuation performance of open window active control  
139 systems. The 2D finite element method (FEM) simulation is set up to determine the  
140 transmission loss of a fully glazed window, as shown in Figure 1(a). The noise source is  
141 initiated as a background plane wave that is travelling in the x-axis direction when incidence  
142 angle  $\theta$  is  $0^\circ$ . For consistency and accuracy, the minimum element size is fixed at one-sixth  
143 the wavelength of 4000 Hz. A far-field arc with 1100 evenly distributed discrete points  
144 encompasses the entire window opening to monitor the attenuation performance of the active  
145 control system.



**Figure 1: (a) FEM simulation model to determine transmission loss. With all units in m.**  
**(b) Transmission loss  $TL_{GR=1}$  of a fully-glazed glass panel with different thickness,  $L_w$  m, at  $0^\circ$  noise incidence.**

146 The transmission loss (TL) is calculated by evaluating the sum-of-the-squared pressures on a  
 147 far-field arc, written as

$$148 \quad TL_{GR} = 10 \log_{10} \frac{\mathbf{p}_{L_g}^H \mathbf{p}_{L_g}}{\mathbf{d}^H \mathbf{d}}, \quad (1)$$

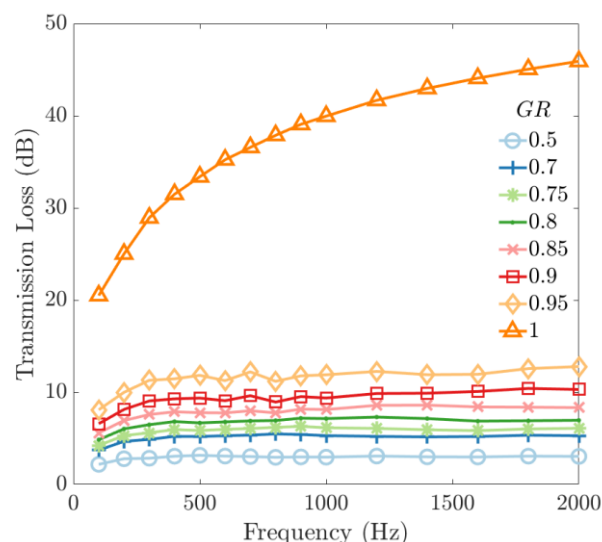
149 where  $\mathbf{d}$  is vector of complex pressure values at the arc without the glass panel,  $\mathbf{p}_{L_g}$  is the  
 150 vector of complex pressure values at the arc when the glass is  $L_g$  m, superscript  $^H$  is the  
 151 Hermitian operator, and  $GR = L_g/L$  is the glazing ratio.

152 Transmission loss due to passive insulation of a sealed window is emulated with a glass panel  
 153 spanning the entire aperture and a thickness of  $L_w$  m, as shown in Figure 1(b). From the  
 154 simulation with a plane wave at  $0^\circ$  incidence, the full glazing performance  $TL_{GR=1}$  increases

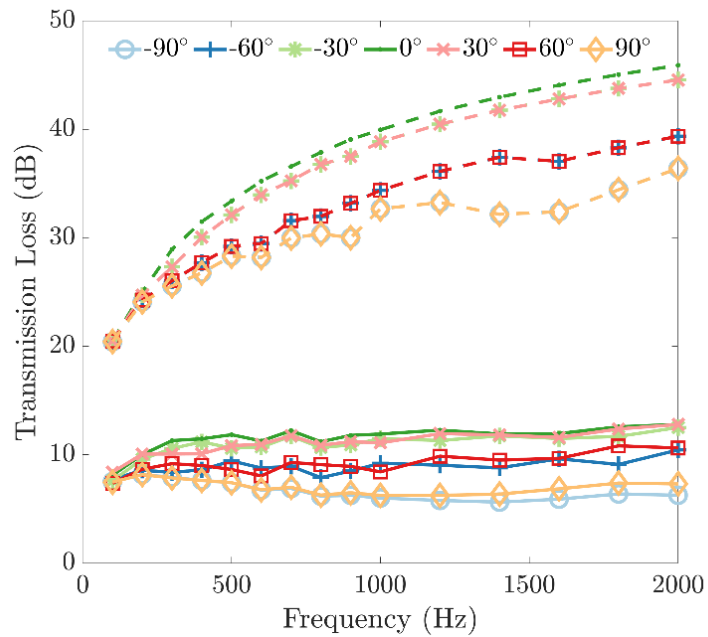


155 uniformly across all frequencies as thickness  $L_w$  increases. Performance decreases rapidly  
 156 with increasing wavelength, when the wavelength is larger than the size of the aperture,  $L$  m.  
 157 Results from the FEM simulation for  $L_w = 0.003$  m agrees with the measured data from past  
 158 experiments using the reverberation chamber method as described in ISO 10140 [21–24]. To  
 159 form a basis of comparison to the full-scale model, the size of the aperture is fixed at  $L = 1.0$   
 160 m for all FEM simulations in this study. The thickness  $L_w$  is fixed at 6 mm from this point  
 161 forth, as the thickness of 6 mm is commonly used in single panel windows in Singapore and  
 162 Hong Kong [3].

163 The transmission loss of the fully-glazed aperture  $TR_{GR=1}$  increases with increasing  
 164 frequency, as shown in Figure 2.  $TL_{GR}$  degrades drastically as a function of frequency once  
 165 the glazing ratio is less than 100%. As  $GR$  decreases, the attenuation performance degrades  
 166 uniformly across all frequencies, as shown in Figure 2. It is worth noting that passive  
 167 attenuation is still notable (more than 5 dB) and uniform across all frequencies for glazing ratio



**Figure 2: Transmission loss  $TL_{GR}$  for different  $GR$ , with glass thickness of  $L_w = 0.006$  m, at  $0^\circ$  noise incidence.**



**Figure 3: Transmission loss at full-glazing  $TL_{GR=1}$  (dashed line), and 95% glazing,  $TL_{GR=0.95}$  (solid line), at different noise incidence angles.**

168 between 75% and 95%. The reduced attenuation of the window panel at frequencies 300 Hz  
 169 and below also presents a complementary role for an ANC system to provide increased  
 170 attenuation, as demonstrated by Carme et al [17].

171 When the plane wave incidence angle is varied from  $-90^\circ$  to  $90^\circ$ , the attenuation  
 172 performance for all  $GR$  degrades with increasing angle of incidence as a function of  
 173 frequency, as shown in Figure 3. There is no notable difference in performance between the  
 174 positive and corresponding negative noise incidence angles, as shown in Figure 3.

### 175 3.2 Active control formulation

176 The active control system is evaluated using the simulation setup shown in Figure 1(a). For a  
 177 global control formulation, the sound power transmitted through the aperture is controlled by  
 178 minimising the sum-of-the-squared pressures at the same 1100 discrete points on the far-field  
 179 arc depicted in Figure 1(a). Hence, the optimal solution of the control problem is obtained by

180 minimising a cost function [25], which is the sum of modulus squared error signals, denoted  
 181 here as a vector  $\mathbf{e}$  containing 1100 elements, and is given by

$$182 \quad \mathbf{e} = \mathbf{d} + \mathbf{G}\mathbf{u}, \quad (2)$$

183 where  $\mathbf{d}$  and  $\mathbf{G}\mathbf{u}$  are vectors of complex pressures due to the disturbance noise only, and from  
 184 contributions of all the  $N$  control sources, respectively.  $\mathbf{G}$  is the matrix of complex plant  
 185 responses and  $\mathbf{u}$  is the vector of control source strengths, at all the evaluation points on the  
 186 evaluation arc. The cost function to be minimised is therefore given by

$$187 \quad J = \mathbf{e}^H \mathbf{e} = \mathbf{q}_s^H \mathbf{A} \mathbf{q}_s + \mathbf{q}_s^H \mathbf{b} + \mathbf{b}^H \mathbf{q}_s + \mathbf{d}^H \mathbf{d}, \quad (3)$$

188 where  $\mathbf{A} = \mathbf{G}^H \mathbf{G}$  and  $\mathbf{b} = \mathbf{G}^H \mathbf{d}$ ,  $\mathbf{q}_s$  is the vector of control sources. The vector of optimal  
 189 secondary source strengths is derived from equating the derivative of (3) to zero yielding

$$190 \quad \mathbf{q}_s = -(\mathbf{G}^H \mathbf{G} + \beta \mathbf{I})^{-1} \mathbf{G}^H \mathbf{d}, \quad (4)$$

191 where  $\beta$  is the regularisation or weighting parameter that limits the control effort to minimise  
 192 overdriven control sources without increasing the residual mean-square error [25].

193 Similar to the transmission loss defined in Eq. (1), the transmission loss of the active control  
 194 system can be written as

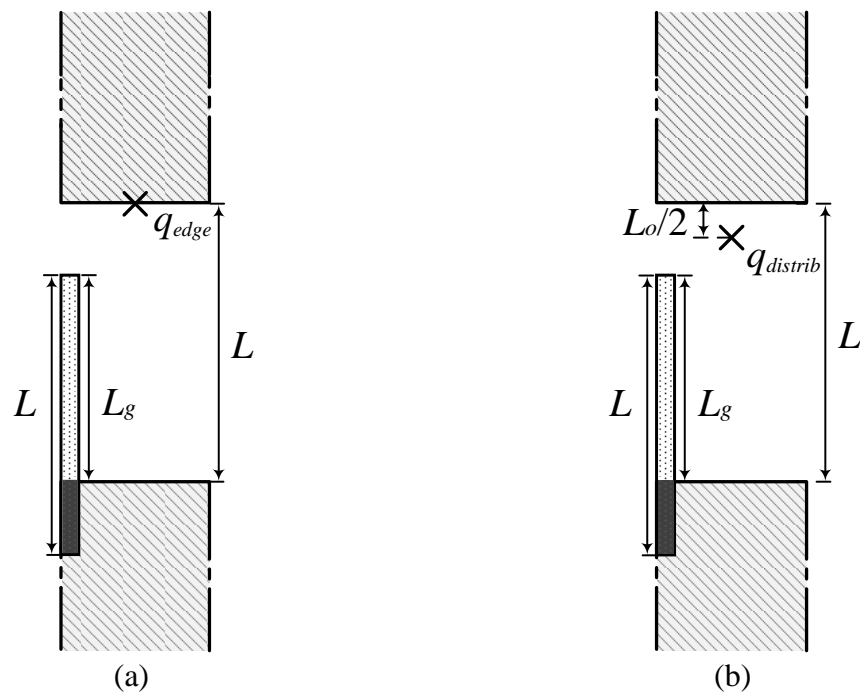
$$195 \quad TL_{GR,ANC} = -10 \log_{10} \frac{\mathbf{e}^H \mathbf{e}}{\mathbf{d}^H \mathbf{d}}, \quad (5)$$

196 where  $GR$  is the glazing ratio,  $\mathbf{e}$  is the vector of complex pressure values after active control  
 197 as defined by Eq. (2), and  $\mathbf{d}$  is the vector of complex pressure values of the fully open aperture  
 198 ( $L_g = 0$  m) as defined in Eq. (1).

### 199 3.3 Performance of the single source ANC system

200 In the 2D FEM model used, the simulated point source (denoted by cross mark), is essentially  
 201 an incoherent line source that radiates cylindrical waves [26]. Hence, a single point source on  
 202 the 2D model is a cross-sectional view of a line source. For simplicity, the acoustic line source  
 203 represented with a cross mark will henceforth be referred to as an individual ‘point’ source.

204 Due to the unique setup of the common sliding window in France, an active control system  
 205 was developed to mitigate urban noise transmission through an open window with minimal  
 206 modifications to existing windows [9,17]. The control sources were placed along the edge of  
 207 one wall, with the speakers facing perpendicular to the aperture, understandably for aesthetical

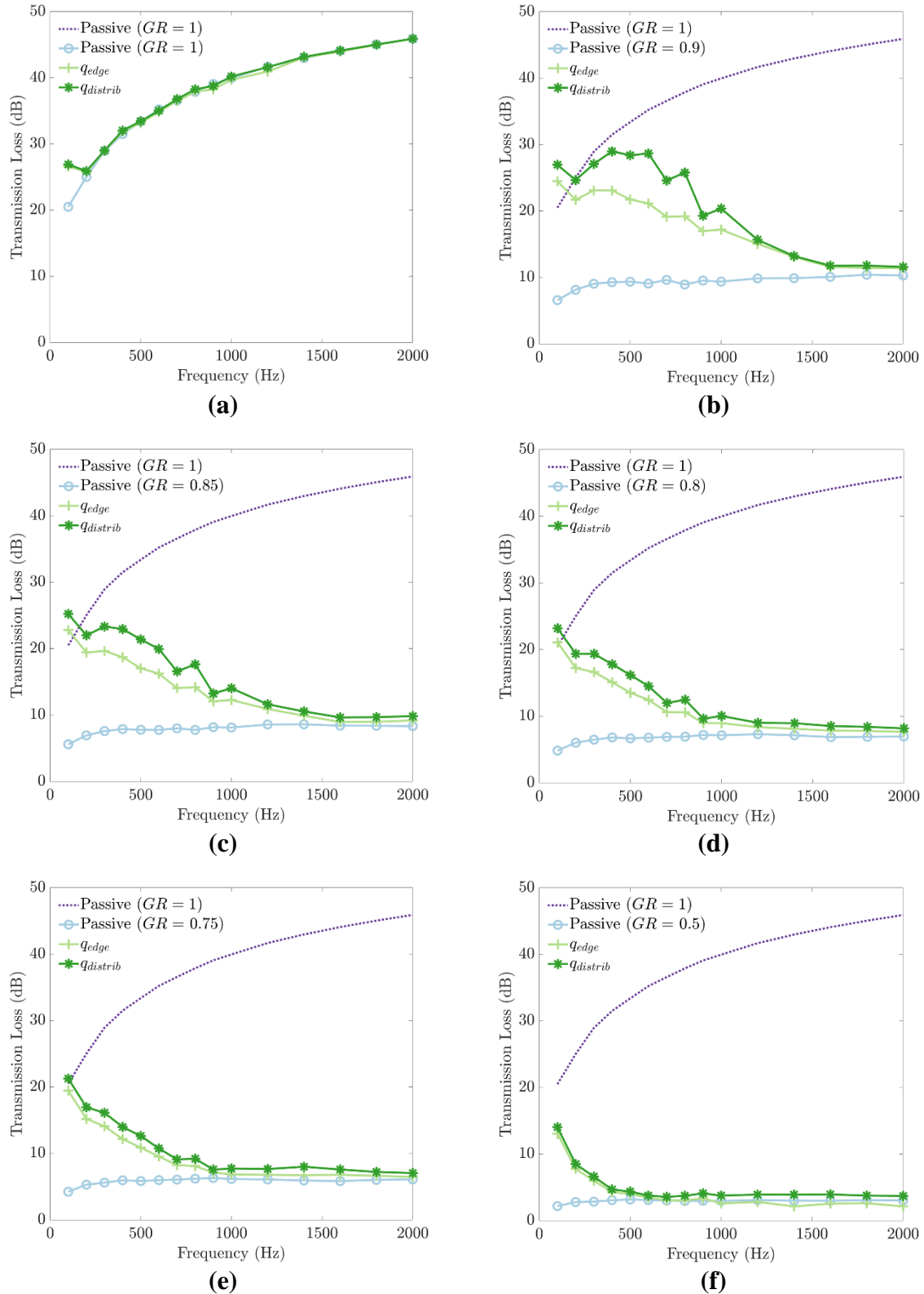


**Figure 4: A close-up view of the aperture showing positions of a single source for (a) the single-sided boundary layout denoted by a cross-mark along the edge of the wall width,  $q_{edge}$ , and (b) for the proposed distributed layout located  $0.125/2 = 0.0625$  m away from the edge denoted by  $q_{distrib}$ . Both line sources are placed in the middle of the wall width, and the shaded area indicates part of the glass panel that has been occluded and is included for illustrative purposes.**

208 reasons. This single-sided source layout can be classified as a form of boundary control  
209 strategy. However, it was previously found that placing sources on the edge significantly limits  
210 the performance of an active control system in the open aperture scenario albeit for a relatively  
211 large number of sources [18].

212 As there is a lack of analysis on the physical limits of the discussed single-sided boundary  
213 control in [9,17], it is numerically investigated here with comparisons to a proposed distributed  
214 strategy. The single-sided boundary control strategy, and a proposed single source ‘distributed’  
215 system is evaluated in 2D FEM as depicted in Figure 4(a) and (b), respectively. Since the glass  
216 panel is based on the same model shown in Figure 1(a) as sliding downwards in the depicted  
217 cross-sectional top view, the single sources are positioned near the top wall, where the opening  
218 caused by the downwards sliding glass panel will start (i.e.,  $L_g$  decreases). Hence, the single-  
219 sided boundary control is represented by a source located on the wall edge, denoted by  $q_{edge}$   
220 in Figure 4(a). The distributed layout is represented by a single source located  
221  $0.125/2 = 0.0625$  m away from the edge of the wall, denoted by  $q_{distrib}$  in Figure 4(b). Both  
222 the single line sources are located in the middle of the wall width, based on recommendations  
223 from a previous study about the physical limits of active control of noise through an aperture  
224 [18].

225 The parameter  $L_o$ , is the aperture size of the acoustic window system described in [17], which  
226 is based on the maximum window gap for infant safety in France. For the convenience of  
227 experimentation and execution of the simulations,  $L_o$  is reduced to 12.5 cm instead of 13 cm.  
228 Hence, the line source placed at  $L_o/2 = 0.0625$  m, which is the centre of the intended  
229 opening in [17].



**Figure 5: Transmission loss  $TL_{GR,ANC}$  of the single line source systems  $q_{edge}$  and  $q_{distrib}$ , with  $GR$  equals (a) 1, (b) 0.9, (c) 0.85, (d) 0.8, (e) 0.75, (f) and 0.5. Passive  $TL_{GR}$  and  $TL_{GR=1}$  included for comparison.**

### 230 3.3.1 Performance of single source ANC system at normal incidence

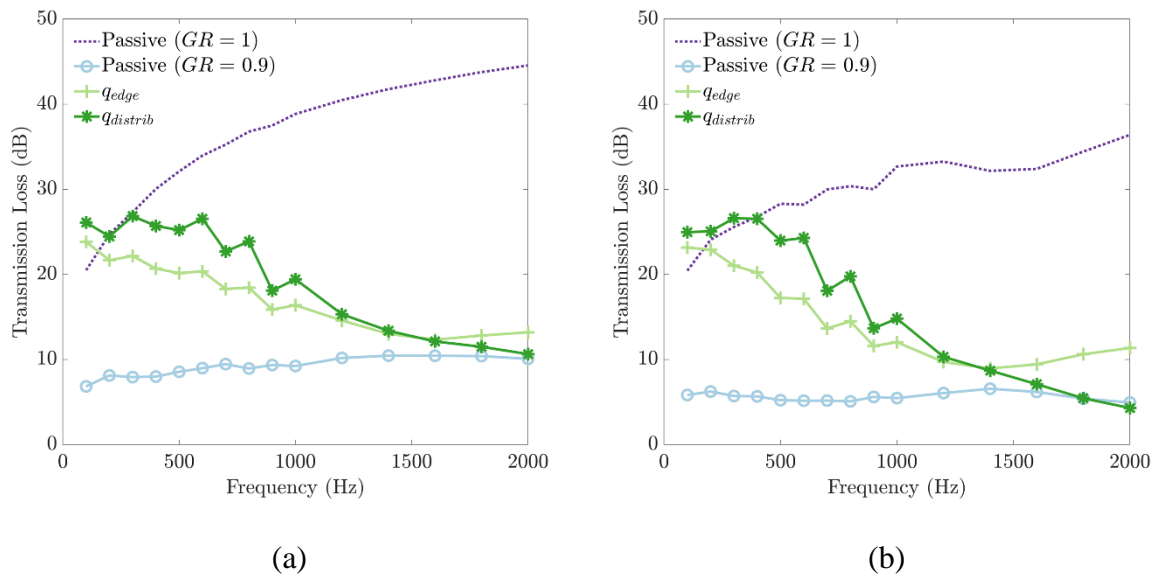
231 Besides investigating the difference in performance between the two strategies with the  
 232 intended window gap size of  $L_o$  ( $GR = 0.875$ ), it is also worthwhile to explore the changes  
 233 in performance with decreasing  $GR$  (i.e., increasing gap size). By varying  $GR$  between 1  
 234 (full-glazing) and 0.5 (fully-open two-panel sliding window), the physical limits of the single  
 235 line source system will be defined in the context of the regular operating conditions of a two-  
 236 panel sliding window. The performance limits of  $q_{edge}$  and  $q_{distrib}$  are firstly determined for  
 237 noise impinging at normal incidence, with decreasing  $L_g$ .

238 At full-glazing ( $GR = 1$ ), the single source in both configurations are not contributing to the  
 239 transmission loss of the window system except at 100 Hz, as illustrated in Figure 5(a). When  
 240 the glazing ratio is close to the limit of the proposed system in [17], the arrangement where the  
 241 single source is located slightly away from the wall ( $q_{distrib}$ ) outperforms the boundary layout  
 242 ( $q_{edge}$ ) by as much as 8 dB, as shown in Figure 5(b) and (c). Even at  $GR$  beyond the effective  
 243 range of a single source system, the benefit of placing the sources (which even becomes  
 244 arbitrary when  $(L - L_g) \neq L_o$ ) away from the edge of the wall (i.e.,  $q_{distrib}$ ) is apparent, as  
 245 illustrated in Figure 5(d) and (e).

246 If the goal of active control is to attain the passive attenuation level of the fully-glazed aperture,  
 247 whilst still allowing natural ventilation ( $GR < 1$ ), the results presented in this subsection also  
 248 illustrates that a single source (or line of sources as depicted in [17]) is insufficient.

### 249 3.3.2 Performance of single source ANC system at oblique incidences

250 It may seem intuitive that placing the source on the edge (i.e.,  $q_{edge}$ ) might be beneficial for  
 251 noise impinging from oblique angles, especially for controlling the diffracted waves near the



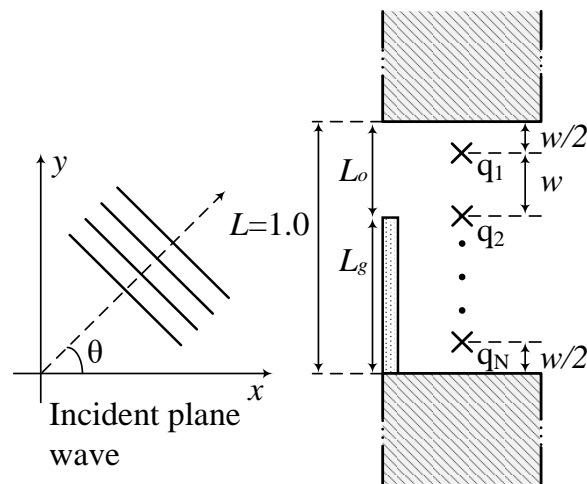
**Figure 6: Transmission loss of the single source ANC system,  $TL_{0.9,ANC}$ , as a function of frequency for source positions at  $q_{edge}$  and  $q_{distrib}$ , when noise incidence angles are (a)  $30^\circ$ , and (b)  $90^\circ$ . Transmission loss of the fully glazed window,  $TL_1$ , and with 90% glazing,  $TL_{0.9}$ , without ANC is included for comparison.**

252 edges. However, it has been also been shown to be otherwise in a multichannel layout, where  
 253 placing active control sources away from the edge provided better attenuation performance at  
 254 oblique incidences as described in section 3.3.1 [18].

255 Hence, the same single channel setup from section 3.3.1 is used to investigate the performance  
 256 of the single source system by varying the angle of noise incidence from  $-90^\circ$  to  $90^\circ$  in steps of  
 257  $30^\circ$ . In all the cases simulated,  $q_{distrib}$  always outperforms  $q_{edge}$  for frequencies less than 1000  
 258 Hz. The scenario when  $GR = 0.9$ , with noise impinging from  $30^\circ$  and  $90^\circ$  is shown in Figure  
 259 6 (a) and (b) respectively.

260 From the comparison between the attenuation performance of  $q_{edge}$  and  $q_{distrib}$ , it is now clear  
 261 that even for a single source, it should not be positioned on the edge of the wall. However, at





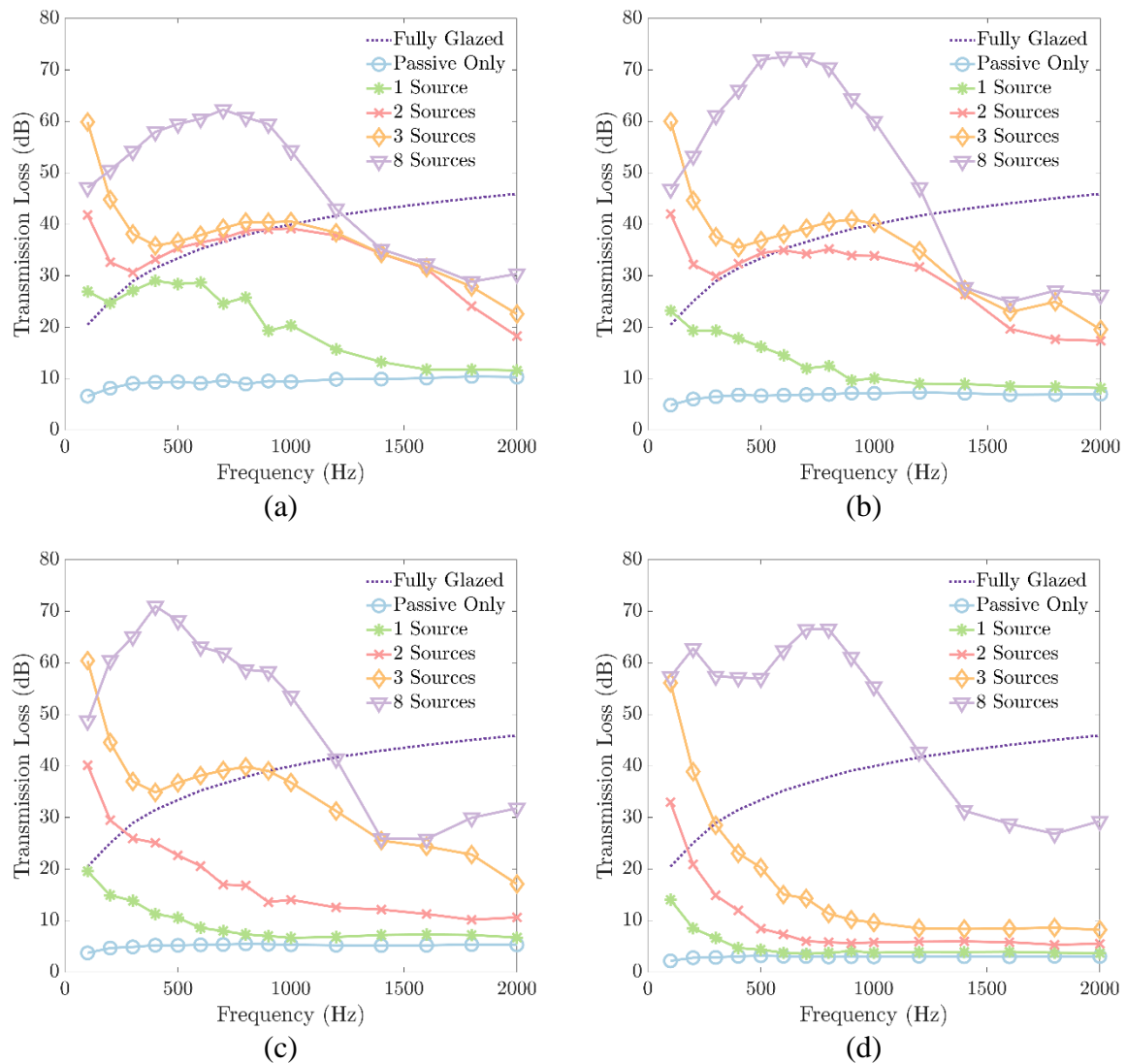
**Figure 7: Arrangement of secondary sources within the aperture, relative to the position of the glass panel.**

262 present, the physical basis for this phenomenon is still unclear, owing to known complexities  
 263 of the diffracted sound field in the aperture [27].

264 In gist, the numerical analysis into the physical limits of an acoustic window system using a  
 265 single-sided boundary layout [9] has revealed that a single source is unable to attain sufficient  
 266 attenuation regardless of  $GR$  and  $\theta$ . Furthermore, one should avoid positioning sources on the  
 267 edge when scaling the number of sources used, as shown in this section and in a previous study  
 268 [18].

### 269 3.4 Performance of a distributed-layout multichannel ANC system

270 In the distributed control system, the control sources are symmetrically distributed across the  
 271 entire opening, where sources are spaced  $w = L / N$  m apart with peripheral sources  
 272  $w / 2$  m away from the wall, as depicted in Figure 7. The minimum number of sources  
 273 required in the aperture can be guided by the spatial aliasing formula in microphone array  
 274 processing, given by  $kw < 2\pi / (\sin \theta + 1)$ , where  $k$  is the wavenumber, from a previous  
 275 study [18,28] and from a free-field analysis [16,20].



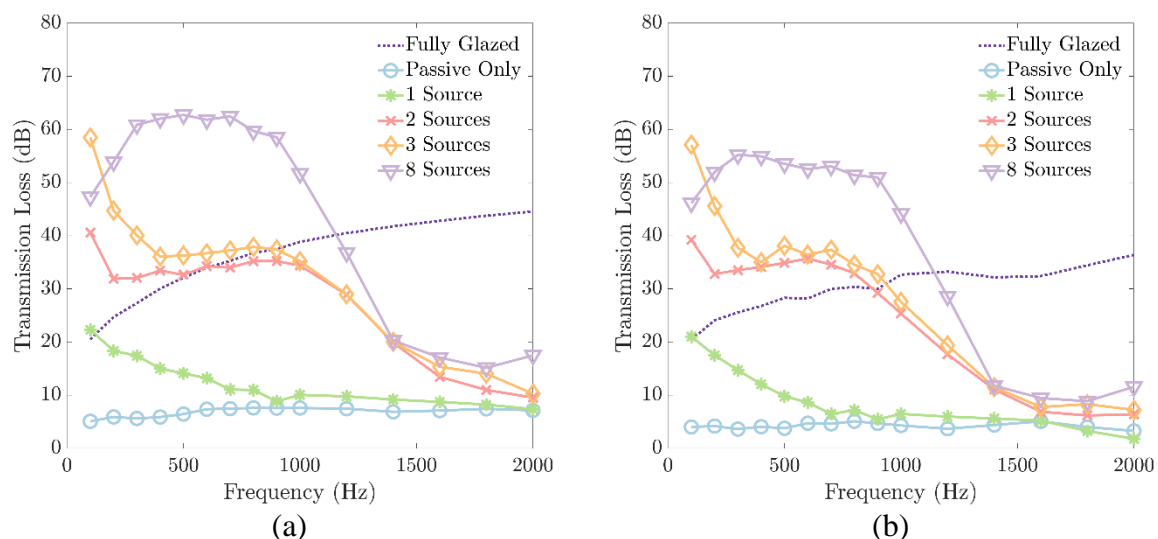
**Figure 8:** *TL* of the multiple line source configurations with glazing ratios of (a) 90%, (b) 80%, (c) 70%, and (d) 50%, at  $0^\circ$  noise incidence angle.

276 By investigating the physical limits of different distributed-layout configurations, the minimum  
 277 source configuration can be determined for a specific glazing ratio and vice versa. The  
 278 attenuation performance of different configurations with noise at  $\theta = 0^\circ$  incidence, is  
 279 illustrated in Figure 8 for glazing ratio of (a) 90%, (b) 80%, (c) 70%, and (d) 50%. For the  
 280 numerical simulations of the distributed layout, the position of the  $N$  incoherent line sources  
 281 correspond to the subscript numbering of sources  $q_N$  as shown in Figure 7. For instance, one

282 source corresponds to  $q_1$ , and three sources are located at positions  $q_1$ ,  $q_2$ , and  $q_3$ . The results  
 283 when  $N$  is 1, 2, 3, or 8 are highlighted and compared to the transmission loss of a fully glazed  
 284 window, and the contributions due to partial glazing without control, as shown in Figure 8.

285 When there are control sources symmetrically distributed across the entire aperture (i.e.,  
 286  $N = 8$ ), the transmission loss of the ANC system  $TL_{GR,ANC}$  exceeds that of a fully glazed  
 287 aperture without control  $TL_1$  (purple dashed line), up till 1200 Hz for  $GR$  greater than 50%.  
 288 Although active control with sufficient sources across the entire aperture could ideally yield  
 289 greater attenuation performance than a fully glazed aperture, it is still worthwhile to determine  
 290 the minimum configuration that can yield sufficient attenuation for sustainability and  
 291 practicality.

292 To achieve similar attenuation as the fully glazed aperture, a minimum of 2 sources are required  
 293 when the glazing ratio is 90% or less, for frequencies less than 1000 Hz, as shown in Figure  
 294 8(a). If the benchmark is lowered to 20 dB, a minimum of 2 sources is required for 70% glazing.



**Figure 9:**  $TL_{GR,ANC}$  of  $N = 1, 2, 3,$  and  $8$  source configurations at 80% glazing for noise incidence angles at (a)  $30^\circ$ , and (b)  $90^\circ$ .

295 The minimum number of sources with respect to the opening size  $L_o$ , can be further generalised  
296 to  $N_{\min} = L_o/w$ , where  $w$  is predetermined based on the general rule [18]. At a separation  
297 of  $w = 0.125$  m, the ANC system would be effective up to 2500 Hz at  $0^\circ$  incidence and up  
298 to half that frequency at  $90^\circ$ , which would be sufficient to tackle traffic noise [29].

### 299 **3.4.1 Performance at different angles of incidence**

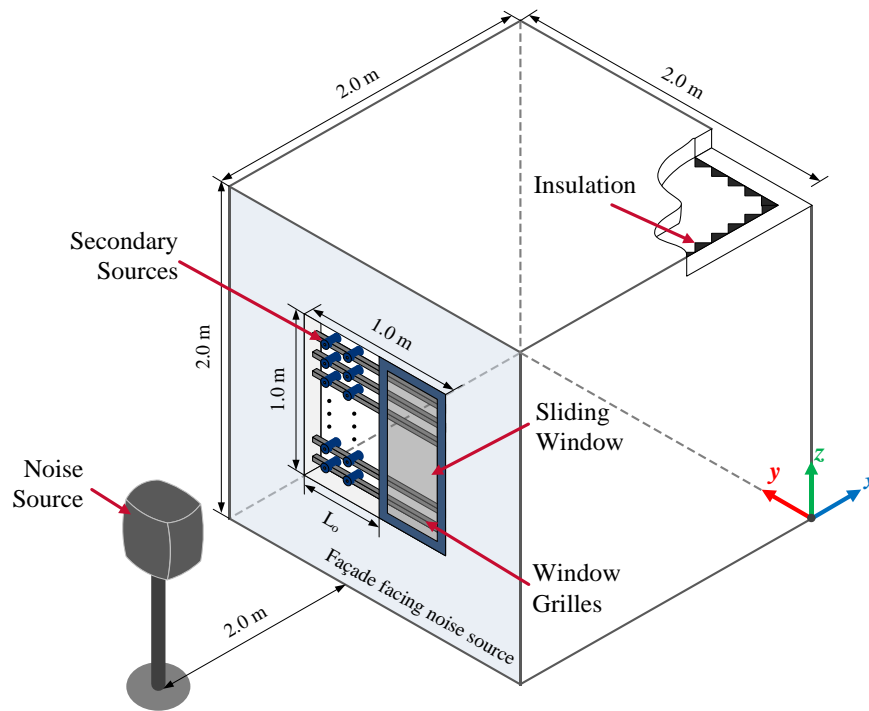
300 In the 2D simulation model shown in Figure 9, the angle of incidence refers to the azimuthal  
301 angles, for instance, from a moving noise source in the horizontal plane. This is analogous to  
302 a top-view cross-section of a domestic sliding window. Since the glass panel in the aperture is  
303 asymmetric, the angles of incidence are simulated from  $\theta = -90^\circ$  to  $90^\circ$ .

304 When the noise is normally incident, the performance of both two and three source  
305 configurations at glazing ratio of 80%, sufficiently satisfy the benchmark of the fully glazed  
306 system, as shown in Figure 8. At glazing ratio of 80% the  $TL_{0.8.ANC}$  of the two and three source  
307 configurations also satisfy the benchmark as shown in Figure 9 for incidence angles of (a)  $30^\circ$   
308 , (b)  $90^\circ$ . The attenuation performance of the corresponding negative noise incidence angles  
309 are similar to the positive ones. Since the performance of the two-source system closely  
310 matches that of the three sources, it suggests that two sources at 80% glazing can sufficiently  
311 attenuate noise at least as well as full glazing at all incidences  $\theta$ .

## 312 **4 Experiments**

### 313 **4.1 Test chamber**

314 A  $2 \times 2 \times 2$  m<sup>3</sup> wooden chamber was constructed and placed in a recording studio, as depicted  
315 in Figure 10. The wooden chamber consists of five 30 mm and one 36 mm thick plywood  
316 panels, with the thickest panel housing the window structure and facing the noise source.



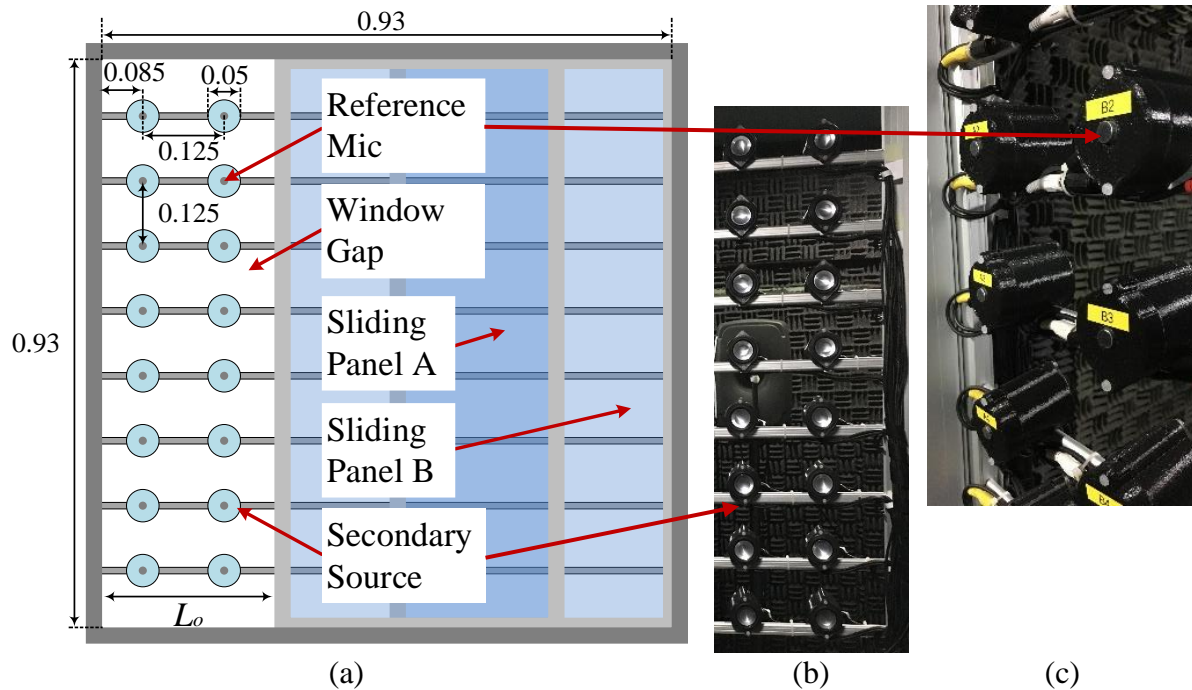
**Figure 10: A sketch of the experimental setup with dimensions in m.**

317 A  $1 \times 1$  m<sup>2</sup> sliding window is installed in the aperture, accompanied by a security grille. The  
 318 window and grille conform to the standards for domestic windows set by the Singapore  
 319 standards body, SPRING Singapore [30]. After discounting the frames of the window and  
 320 grilles, the effective open area of the two-panel sliding window is  $(0.93 / 2) \times 0.93$  m<sup>2</sup>, where  
 321 the shorter edge represents the width and the latter representing the height.

322 To minimise the interference due to reverberation, the inside surface of the entire chamber has  
 323 been lined with acoustic foam. The opening size is depicted by  $L_o$  and the noise source is  
 324 located 2 m away from the middle of the opening.

#### 325 4.2 Real-time Active Noise Control System

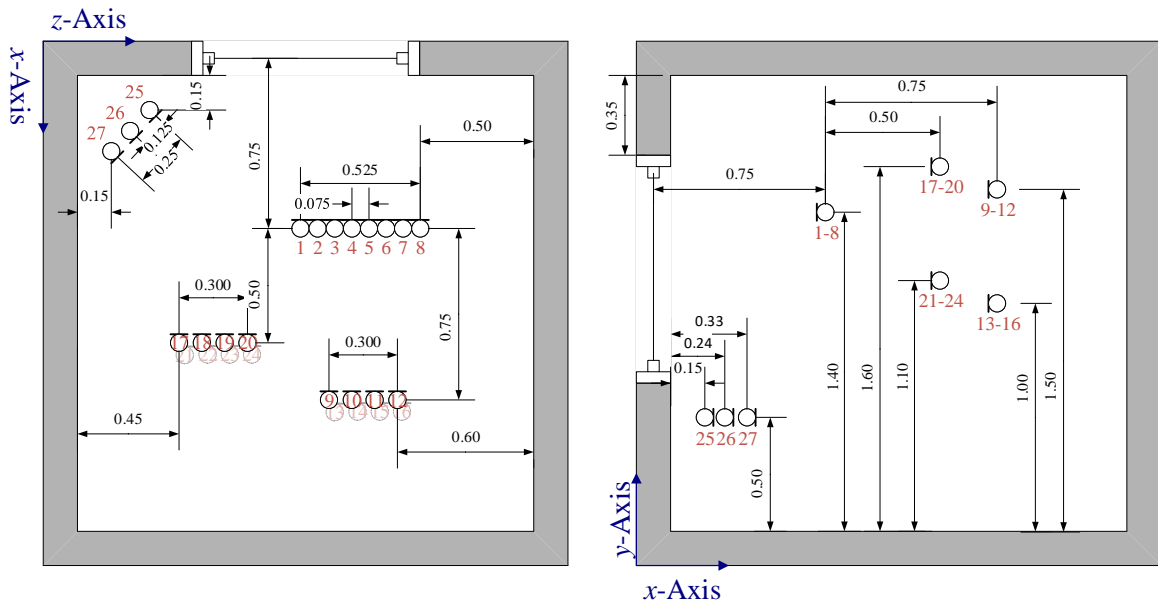
326 The primary source is a large loudspeaker (Genelec 8341A) with flat frequency response and  
 327 large wave fronts. Sixteen secondary sources were installed on the window grille in two  
 328 columns of 8 sources facing into the chamber, as shown in Figure 11. Taking reference from



**Figure 11: (a) View of the ANC system from outside the chamber with dimensions in m. The secondary source is fixed on the window grille, and  $L_o$  is varied by moving sliding panel A only. View of the (b) secondary sources from inside the chamber, and (c) reference microphones from outside.**

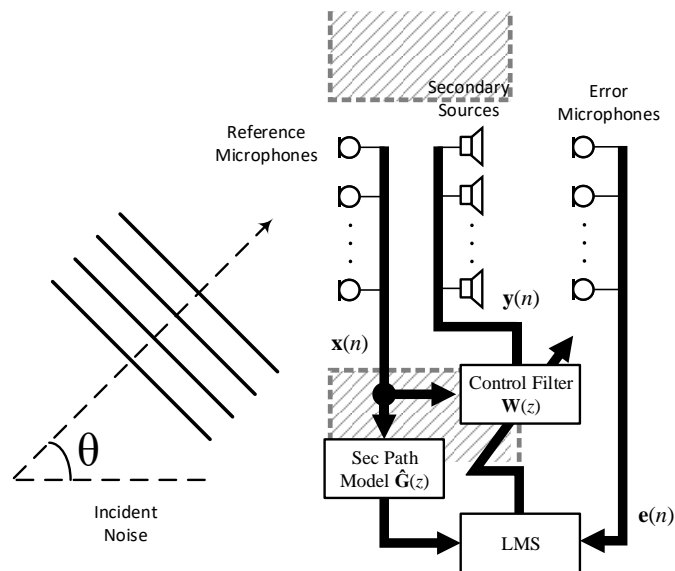
329 the Active Acoustic Shielding (AAS) cell proposed by Murao and Nishimura [11], one  
 330 reference microphone is paired with a secondary speaker to form a single compact unit, as  
 331 shown in Figure 11(b).

332 Eight error sensors are placed 0.5 m away from the secondary source to avoid the near-field  
 333 effects of the secondary sources. There are 27 observation microphones (G.R.A.S. 40PH)  
 334 distributed inside the chamber, as shown in Figure 12 in both the  $xz$ -plane (left) and  $xy$ -plane  
 335 (right). The observation microphone output from the National Instruments 9234 data  
 336 acquisition device was analysed with the LabVIEW software.



**Figure 12. Layout of the 27 observation microphones in the chamber in the  $xz$ -plane (left) and  $xy$ -plane (right).**

337



**Figure 13: Active control system block diagram showing the cross-section of the physical layout and path of the reference  $x(n)$ , control  $y(n)$ , and error  $e(n)$  signals. The control filter is updated by the FXLMS algorithm.**

338 A collocated implementation of the FXLMS algorithm [11], was programmed into a modular  
 339 real-time embedded platform (National Instruments PXIe-8135). The sampling rate was 16  
 340 kHz, and the filter lengths of the secondary path model and adaptive filter was set to 100 and  
 341 200 taps, respectively. The block diagram of the multichannel ANC system is depicted in  
 342 Figure 13.

### 343 4.3 Evaluation Criteria

344 The time-averaged SPL readings from all  $n$  observation microphones,  $SPL_{TA,n}$ , are used to  
 345 determine  $SPL_{EA}$  the energy-average sound pressure level in the chamber, given by

$$346 \quad SPL_{EA} = 10 \lg \left( \frac{1}{n} \sum_{i=1}^n 10^{SPL_{TA,i}/10} \right). \quad (6)$$

347 The energy-average SPL,  $SPL_{EA}$ , represents the space and time average of the SPL in the  
 348 chamber as defined in ISO 16283-3.

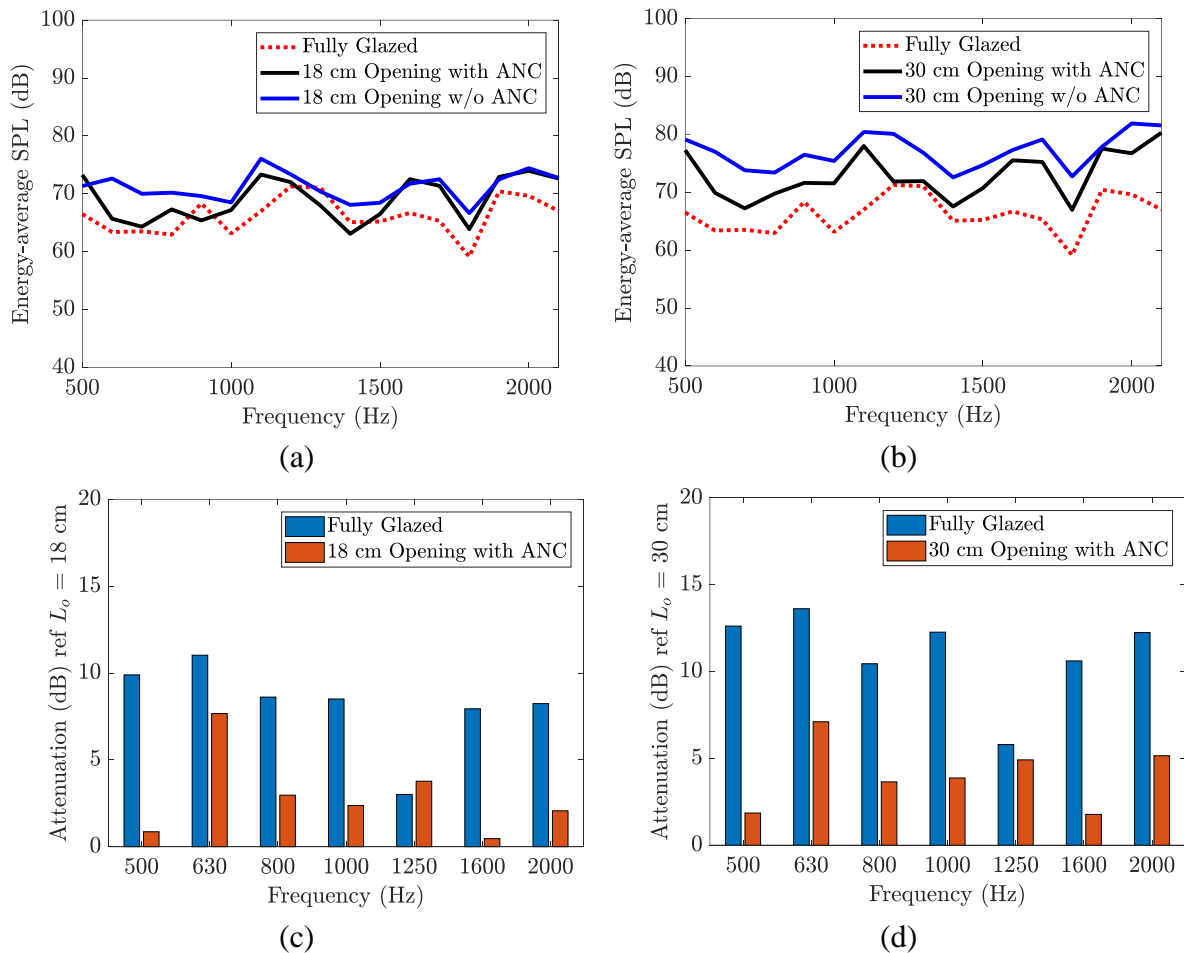
349 The attenuation of the fully-glazed (FG) window as compared to the case where the window  
 350 gap is  $L_o$  m, is thus given by,

$$351 \quad ATT_{L_o,FG} = SPL_{EA,L_o} - SPL_{EA,FG}, \quad (7)$$

352 where  $SPL_{EA,L_o}$  is the energy-average SPL when the window gap is  $L_o$  m, and  $SPL_{EA,FG}$  is  
 353 the energy-average SPL of the fully-glazed system under the same test signal. The attenuation  
 354 performance of the ANC system is evaluated by

$$355 \quad ATT_{L_o,ANC} = SPL_{EA,L_o} - SPL_{EA,L_o,ANC}, \quad (8)$$





**Figure 14. Energy-average sound pressure levels of 27 microphones at (a)  $L_o = 0.18$  m and (b)  $L_o = 0.30$  m, when (1) fully glazed (red dashed line), (2) without ANC (solid blue line), and (3) with ANC activated (solid black line). Attenuation performance in 1/3 octave bands of the fully-glazed window and an (c) 8-channel and (d) 16-channel ANC system, normalised by the energy-average SPL.**

356 where  $SPL_{EA,L_o,ANC}$  is the energy-average SPL when the window gap is  $L_o$  m with ANC

357 activated.

358

#### 359 4.4 Test of tonal noise

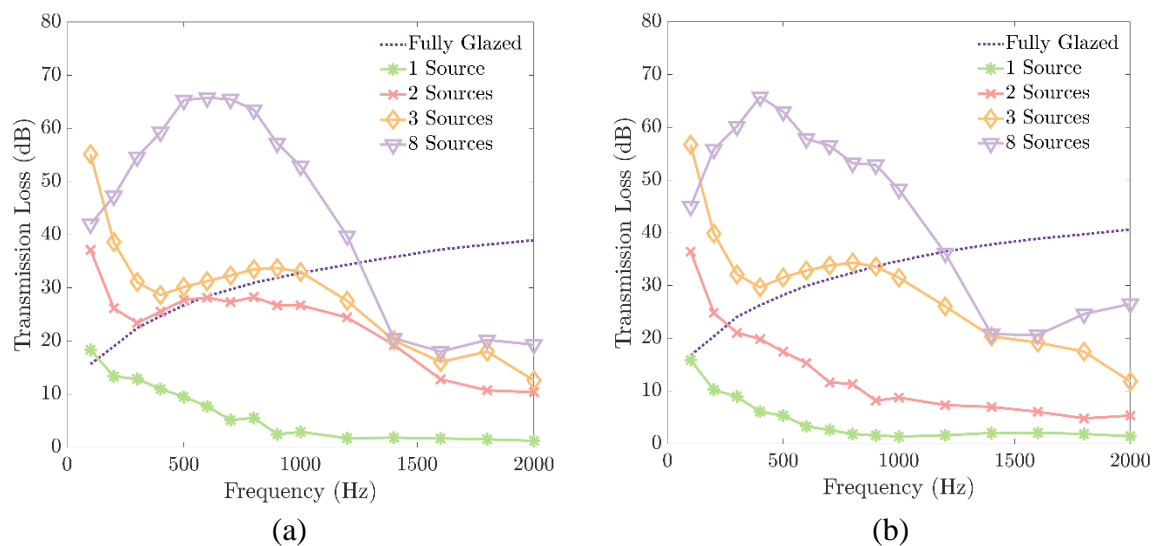
360 In the single tone tests, the primary source is excited with frequencies of 500 Hz to 2100 Hz  
 361 under three scenarios, namely: (1) fully-glazed window, (2) window with glazing ratio  $GR$   
 362 without active control, and (3) window with glazing ratio  $GR$  and active control activated.

363 When the window is 0.18 m ajar ( $L_o = 0.18$  m,  $GR \approx 80\%$ ) the energy-average sound  
 364 pressure level,  $SPL_{EA,L_o=0.18}$  is nearly constant ( $71$  dB  $\pm$  2 dB) as reflected by the blue line in

365 Figure 14 **Error! Reference source not found.**(a). Shutting the window clearly yields  
 366 noticeable attenuation as shown by the red dashed line. The layout of the 8-channel system  
 367 used when  $L_o = 0.18$  m is depicted by the left most column of sources in Figure 11(a).

368 Notable attenuation between the 630 to 1250 Hz 1/3 octave bands is achieved with the 8-  
 369 channel ANC system as indicated by the red bars in **Error! Reference source not found.**

370 Figure 14(c).



**Figure 15.**  $TL$  of the fully-glazed window without ANC, and  $TL$  of the different source configurations at  $GR$  of (a) 80%, and (b) 70%, normalised by the sum-of-the-square pressures at the evaluation arc without ANC for  $GR$  of (a) 80%, and (b) 70%.

371 The attenuation performance of the fully-glazed window ( $ATT_{L_o,FG}$ ) and the 8-channel ANC  
 372 system ( $ATT_{L_o,ANC}$ ) when  $L_o = 0.18$  m represented by the blue bars in Figure 14**Error!**  
 373 **Reference source not found.**(c). It is expected that the performance of the ANC system would  
 374 be less effective than the fully-glazed window as discovered in the numerical simulations for  
 375 the normalised single source performance in Figure 15(a). However, the perceivable reduction  
 376 is at most 5 dB lower than the fully-glazed window in most frequencies below 1500 Hz, instead  
 377 of more than 15 dB difference in the FEM simulations in Figure 15(a). This discrepancy arises  
 378 from both the active control system and the window structure. Despite the inclusion of sealing  
 379 foam, the passive attenuation of a closed two-panel sliding window is still hampered by the  
 380 gaps between the panels and the sliding tracks. After optimisation of the secondary source  
 381 locations, the active control performance is still dependent on the cost function choice, error  
 382 sensor arrangement, and controller and hardware choices [31].

383 When the opening  $L_o$  is increased to 0.3 m ( $GR \approx 70\%$ ), a 16-channel ANC system is  
 384 activated. A diagram of the source placement and the actual image, as shown from the inside  
 385 of the chamber, are depicted in Figure 11. The energy-average SPL in the chamber is  
 386 significantly increased when the opening is two-thirds wider as shown by the solid blue line in  
 387 the bottom-left plot in Figure 14**Error! Reference source not found.**(b). Considerable passive  
 388 noise reduction (<10 dB) is achieved when the window is fully glazed (dashed red line).  
 389 Between 630 to 1250 Hz 1/3 octave bands, the attenuation performance of the 16-channel ANC  
 390 system is better than the performance of the 8-channel system when  $L_o = 18$  cm, as shown in  
 391 Figure 14**Error! Reference source not found.**(d).

## 392 5 Discussion

393 It is expected from the simulations that the performance of the active control system will be  
 394 worse than the passive attenuation of a fully-glazed system. However, the difference between

395 both ANC configurations and the fully-glazed system is only between 5 to 10 dB (energy-  
396 average SPL) in most frequencies below 1500 Hz, in contrast to the sound power difference of  
397 greater than 15 dB in the finite element simulations.

398 Even though the (demonstrated) system has a large opening similar to actual in-situ usage, and  
399 larger than that demonstrated by Murao and Nishimura, Carme et al., and Kwon and Park, the  
400 performance trade-offs have to be addressed.

401 In the proposed system, the size of the speaker diaphragm was reduced (0.045 m) in favour of  
402 reduced visual obstruction. Hence, the low frequency performance (<500 Hz) was drastically  
403 affected. Depending on the target noise, however, there may not be a need to address this  
404 shortcoming as the dominant energy is usually not less than 500 Hz (i.e., traffic noise) and  
405 human hearing is less sensitive to low frequencies.

406 To realise the active control system for practical applications, the high computational  
407 complexity associated with the implementation of the multi-channel system needs to be  
408 addressed [32–34]. Moreover, development of a computationally efficient method, as opposed  
409 to regular leaky FXLMS, is required to prevent overdriving the control sources in the presence  
410 of high SPL noise especially for small speakers [35]. Further investigation into the robustness  
411 of the fixed coefficient implementation allows for the omission of error microphones in the  
412 interior of the room [36–38], a major boon for practical implementation.

## 413 **6 Conclusion**

414 To establish a performance benchmark for the active control of noise through open windows,  
415 the transmission loss of a single-glazed aperture was investigated through FEM simulations.  
416 The simulations represent an ideal glazing scenario, where the glass panel is perfectly sealed  
417 to the rigid walls.

418 The physical limits of two types of control source arrangements and their interactions with  
419 varying glazing ratios were examined. In the ideal control scenario, the distributed control  
420 source method consistently outperforms the boundary control method for different glazing  
421 ratios and angles of plane noise incidence.

422 A guideline is formulated for realising a practical ANC system on standard windows in  
423 Singapore through investigation of the physical limits of control, for an increasing number of  
424 control sources in the distributed configuration at different glazing ratios and angles of  
425 incidences. The recommended window gap should be guided by the minimum source  
426 separation distance determined for sufficient control of traffic noise, where  $N_{min} = L_o / w$   
427 and  $w = 0.125$  m.

428 A full-scale model with an actual domestic sliding window and security grille was constructed  
429 to test the performance of the distributed control system. Although it was determined that at  
430 80% glazing, two sources (line) would sufficiently attain the attenuation performance of a  
431 fully-glazed window, it is not realisable in practical conditions due to the partial obstruction of  
432 reference microphones on the proposed control cell. After accounting for the physical  
433 constraints of the real window, two distributed configurations were tested, (1) 8 sources  
434 arranged uniformly in a vertical column in a  $0.1674 \text{ m}^2$  opening (  $0.18 \times 0.93 \text{ m}^2$ ,  
435  $GR = 0.8$  ), and (2) 16 sources arranged uniformly in two vertical columns in a  $0.279 \text{ m}^2$   
436 opening ( $0.3 \times 0.93 \text{ m}^2$ ,  $GR = 0.7$ ).

437 Through tonal experiments, notable attenuation ( $> 5$  dB energy-average SPL) was achieved  
438 by means of a 16-channel ANC system installed in real window at 70% ( $0.3 / (0.93 \times 0.465)$   
439  $\text{m}^2$ ) of its maximum allowable opening size.

440

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444 2013-7

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