

Near-Instantaneously Adaptive Learning-Assisted and Compressed Sensing-Aided Joint Multi-Dimensional Index Modulation

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Abstract—Index Modulation (IM) is capable of striking an attractive performance, throughput and complexity trade-off. The concept of Multi-dimensional IM (MIM) combines the benefits of IM in multiple dimensions, including the space and frequency dimensions. On the other hand, IM has also been combined with compressed sensing (CS) for attaining an improved throughput. In this paper, we propose Joint MIM (JMIM) that can utilize the time-, space- and frequency-dimensions in order to increase the IM mapping design flexibility. Explicitly, this is the first paper developing a jointly designed MIM architecture combined with CS. Three different JMIM mapping methods are proposed for a space- and frequency-domain aided JMIM system, which can attain different throughput and diversity gains. Then, we extend the proposed JMIM design to three dimensions by combining it with the time domain. Additionally, to circumvent the high detection complexity of the proposed CS-aided JMIM design, we propose Deep Learning (DL) based detection. Both Hard-Decision (HD) as well as Soft-Decision (SD) detection are conceived. Additionally, we investigate the adaptive design of the proposed CS-aided JMIM system, where a learning-based adaptive modulation configuration method is applied. Our simulation results demonstrate that the proposed CS-aided JMIM (CS-JMIM) is capable of outperforming its CS-aided separate-domain MIM counterpart. Furthermore, the learning-aided adaptive scheme is capable of increasing the throughput while maintaining the required error probability target.

Index Terms—Index Modulation (IM), Compressed Sensing-aided Multi-Dimensional Index Modulation (CS-MIM), Soft-Decision Detection, Machine Learning, Neural Network.

I. INTRODUCTION

INDEX Modulation (IM) [1] can be considered as an energy-efficient candidate for next-generation wireless systems as a benefit of its flexible resource activation [2]. The concept of IM has been derived from that of Spatial Modulation (SM), which is a low-complexity Multiple-In and Multiple-Out (MIMO) scheme capable of striking a flexible performance *vs.* complexity trade-off using a single Radio Frequency (RF) chain [2]–[4]. Then, the concept of SM has also been extended to the frequency and time dimensions, where the philosophy of IM has been proposed [5], [6]. In the Frequency Domain (FD), the IM combined with Orthogonal

Frequency Division Multiplexing (OFDM) is referred to as Subcarrier-IM (SIM), where only a fraction of the subcarriers is activated for signal transmission and the index of active subcarriers conveys extra information bits [7]. The effective signal power of the subcarriers activated in the FD is amplified, without increasing the time domain signal power after Inverse Fast Fourier Transform (IFFT). This results in a higher Signal-to-Noise Ratio (SNR) for the modulated symbols without requiring extra radiated power. Then, Tsonev *et al.* [8] proposed an enhanced SIM and Basar *et al.* [9] conceived a novel IM-aided OFDM (OFDM-IM) scheme for increasing the spectral efficiency. However, subcarrier-index modulated OFDM suffers from significant throughput reduction compared to the classic OFDM due to the deactivation of a number of subcarriers. Hence, Zhang *et al.* [10] proposed an improved SIM concept relying on Compressed Sensing (CS) [11], which benefits from the sparsity of symbols in the FD by compressing the sparse transmit vector [12].

To further increase the overall performance, Datta *et al.* proposed the concept of Generalized SIM (GSIM) and proved that Generalized Space-and-Frequency IM (GSFIM) achieves better performance than MIMO-OFDM. Their solution conveyed extra information in the SM part compared to GSIM [13]. However, the detection complexity of GSFIM escalates. Hence, Chakrapani *et al.* [14] proposed a message passing based low-complexity detection method for reducing the complexity of GSFIM detection. Furthermore, inspired by the SM and Quadrature SM (QSM) concepts [15], Quadrature Space-Frequency IM (QSF-IM) was proposed in [16], which applies a twin-antenna constellation for the in-phase and quadrature-phase transmission, in order to increase the throughput without extra energy consumption. Hence this solution struck a compelling Spectral Efficiency (SE), Energy Efficiency (EE) and Cost Efficiency (CE) trade-off.

Furthermore, several researchers considered the design of Multi-Dimensional Index Modulation (MIM) relying on both the Spatial Domain (SpD) and FD. For example, Space-Frequency Shift Keying (SFSK) [17] relies on an SFSK Dispersion Matrix (DM), which achieves beneficial transmit diversity in rapidly time-varying channels. Space-Time Shift Keying (STSK) constitutes another multi-functional MIMO technique in the family of MIM. It combines the Time Domain (TD) and the SpD and it is capable of striking a beneficial diversity versus multiplexing trade-off [18]. More specifically, in STSK, Q DMs are designed for spreading the signal over

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L. Hanzo would like to acknowledge the financial support of the Engineering and Physical Sciences Research Council projects EP/W016605/1 and EP/X01228X/1 as well as of the European Research Council's Advanced Fellow Grant QuantCom (Grant No. 789028)

TABLE I: Contrasting our contributions to the literature

Contribution	proposed*	[10]	[24]	[22]	[25]	[26]	[27]	[28]	[29]	[30]
Index modulation	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓
CS at transmitter	✓	✓		✓						
Learning aided detector	✓		✓		✓			✓	✓	✓
Soft decision detector	✓		✓				✓		✓	
Adaptive design for index modulation	✓									✓
Multi-dimensional index modulation	✓			✓					✓	
Joint index mapping design	✓			✓					✓	
3-Dimensional joint index modulation	✓									

87 T Time Slots (TSs) and M Transmit Antennas (TA) in the
 88 TD and the SpD, respectively. Furthermore, the IM design
 89 activates one out of the Q DMs for transmission, hence $\log_2 Q$
 90 extra IM bits may be conveyed. By appropriately adjusting
 91 these parameters, improved Bit Error Ratio (BER), throughput
 92 and complexity trade-offs may be struck [19].

93 Additionally, the concept of MIM was proposed in [20],
 94 which is capable of improving the degrees of freedom, hence
 95 achieving all the benefits of the IM concept in several domains
 96 without introducing extra deployment costs, such as extra RF
 97 chains or transmission power. Furthermore, Lu *et al.* [21]
 98 proposed Compressed-Sensing-Aided Space-Time Frequency
 99 Index Modulation (CS-STFIM) to combine CS techniques
 100 with STSK and OFDM-IM, which is an MIM system concept
 101 that inherits the benefits of both STSK and OFDM-IM. As a
 102 further advance, SM was also integrated into this MIM scheme
 103 for TA selection in [22]. In [6], the concept of multi-functional
 104 layered SM was proposed, which offers flexible trade-offs in
 105 terms of performance, hardware cost and power dissipation.

106 However, in previous MIM schemes, the index selection
 107 was performed separately in each dimension. By contrast, in
 108 this paper, we extend this concept to a Joint MIM system,
 109 where we jointly designs the IM in several dimensions. More
 110 specifically, the degrees of freedom of the IM mapping design
 111 is increased by harnessing multiple dimensions, which leads
 112 to a more flexible trade-off between the throughput, power
 113 efficiency, and cost. In this case, both SFSK and STSK can be
 114 considered as special cases of the proposed joint MIM (JMIM)
 115 family. JMIM may also be combined with CS techniques for
 116 increasing the spectral efficiency.

117 However, the joint detection of multiple dimensions leads
 118 to massive computational complexity at the receiver side.
 119 More specifically, conventional Maximum Likelihood (ML)
 120 detection, suffers from a rapidly escalating complexity upon
 121 increasing in the number of dimensions [31]. Coherent detec-
 122 tion also requires the accurate knowledge of Channel State
 123 Information (CSI) at the receiver side, which leads to a
 124 substantial pilot overhead [32] as well as to a high Channel
 125 Estimation (CE) complexity [33], [34]. In [22], CS-aided MIM
 126 (CS-MIM) was presented, where multiple detection stages
 127 were required for recovering the data from the constituent
 128 CS, STSK, OFDM-IM and SM schemes. As a result, near-
 129 capacity operation can only be achieved, when Soft-Decision
 130 (SD) detection is used [35], but again, the complexity of MIM
 131 detection escalates with the number of IM dimensions.

132 Recently, learning-based detection has been used as an effi-
 133 cient tool for reducing the complexity of detection, while dis-

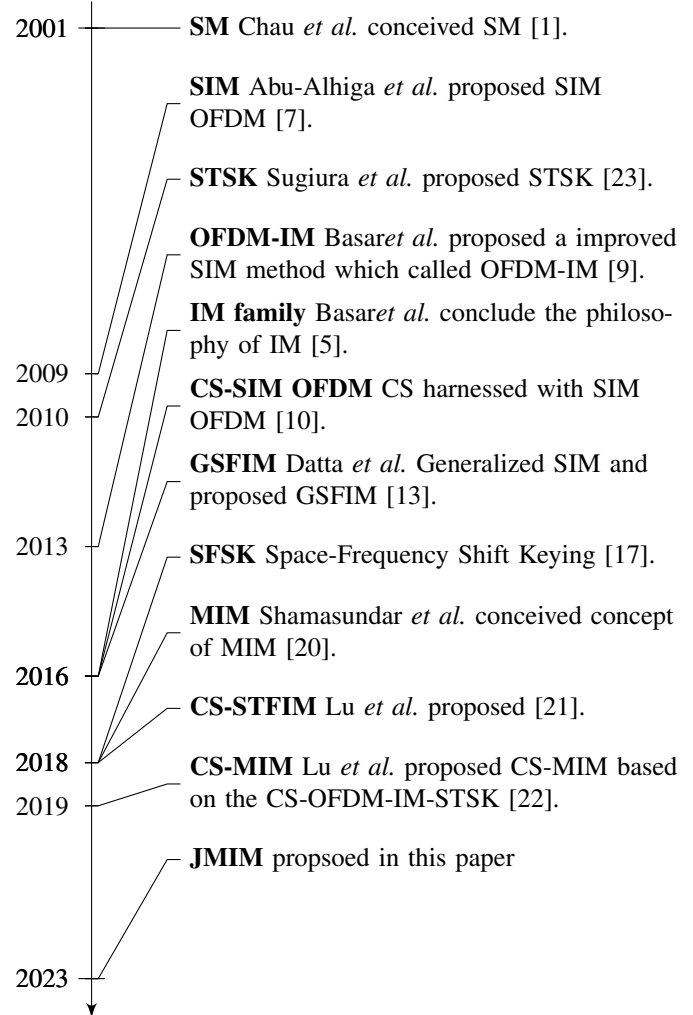


Fig. 1: Milestones of the index modulation family from single dimensional index modulation to MIM.

134 pensing with the requirement of explicit CSI estimation [36].
 135 In [37], a Deep Neural Network (DNN) based model is
 136 proposed for detecting the OFDM-IM signal, while the authors
 137 of [38] and [39] harnessed convolutional neural networks
 138 for IM detection, when the CSI is available at the input of
 139 the detector. By contrast, blind learning based detection was
 140 designed for Millimeter Wave (mmWave) IM in [28] and for
 141 multi-set STSK in [29]. However, the authors of [29] only
 142 investigated the combination of basic SD and Deep Learning
 143 (DL). In [36], both DNN-based Hard-Decision (HD) and
 144 iterative SD assisted blind detection have been proposed for

CS-MIM.

Additionally, given the flexibility of our CS-aided JMIM (CS-JMIM) design, we can adapt the JMIM mapping to hostile time-varying channel environments to improve the attainable performance. Hence, the concept of adaptive modulation can be intrinsically amalgamated with CS-JMIM to improve the attainable throughput, while maintaining a specific target BER. Yang *et al.* proposed machine learning aided adaptive SM [40], while Liu *et al.* [41] conceived learning-assisted IM for mmWave communications. In their follow-on research, they further developed the work by considering CE employing sparse Bayesian learning for accurate CSI estimation [42].

Table I boldly contrasts the novelty of this paper to the literature. More explicitly, the contributions of this paper can be further detailed as follows:

- 1) We propose the CS-JMIM system concept and present several JMIM mapping matrix designs. Then, we demonstrate that the proposed JMIM mapping design is capable of striking an attractive trade-off between diversity and throughput.
- 2) We propose a DL-based HD detection aided CS-JMIM system that can achieve near-ML performance, while imposing significantly reduced complexity. Furthermore, we propose a DNN-aided SD detector for the proposed CS-JMIM that is capable of achieving near-capacity performance.
- 3) Both a K -nearest neighbour (KNN) algorithm based and a DL-assisted adaptive modulation scheme is proposed for CS-JMIM. We demonstrate that the learning-assisted adaptive CS-JMIM scheme is capable of selecting more appropriate CS-JMIM mapping design for transmission than its conventional threshold-based adaptive counterparts. Hence it can obtain a significant throughput gain over the conventional threshold-based adaptive method.
- 4) Our simulation results demonstrate that the proposed learning-based detector is capable of approaching the performance of the conventional coherent detection techniques at a reduced detection complexity. We also provide the associated capacity and throughput analysis, for characterising the trade-off between each mapping matrix and the benefits of the learning-assisted adaptive method.

The rest of the paper is organized as follows. In Section II, the system model of CS-JMIM is presented. In Section III, we characterize both HD and SD based learning-aided detectors. Then, in Section IV we present our proposed adaptive system design. In Section V, we present our simulation results, while our conclusions are offered in Section VI.

II. SYSTEM MODEL

In this section, we introduce the transceiver model of the proposed CS-JMIM system employing N_t TAs and N_r Receive Antennas (RAs). Fig. 2 shows the block diagram of the CS-JMIM system considered, where b bits are equally divided into G groups. We consider OFDM having N_c subcarriers, which are then split into G groups and each group has

$N_f = N_c/G$ subcarriers in the FD¹, while N_{vt} TAs and N_v subcarriers of each group are applied for the CS-JMIM system in the Virtual Domain (VD)². To be more specific, in each subcarrier group, there are N_v available subcarrier indices within the VD, where the dimension N_v of the VD is larger than the dimension N_f of the FD. Similarly, N_{vt} antennas in the VD are larger than the N_t antennas of the SpD. For each group of b bits as $b_g (g = 1, 2, \dots, G)$, b_g^1 bits are used for generating K Phase Shift Keying/Quadrature Amplitude Modulation PSK/QAM symbols, while the remaining b_g^2 bits are mapped to the JMIM mapping matrix selector, which chooses a specific mapping matrix out of Q JMIM matrices. Then, these K PSK/QAM codewords and the selected JMIM mapping DM are combined to generate a Space-Time (ST) block S . Afterwards, the block creator of Fig. 2 collects all codewords from the G groups for forming a frame, which is mapped to multiple index domains by the carrier index mapper, followed by the CS method and OFDM modulation, as shown in Fig. 2. Then, after transmission over the wireless channel, the receiver estimates the channel and detects the signal. At the receiver side, the signal is transformed back to the subcarrier symbols and each JMIM group signal is detected separately.

In the following, we present the details of the processing stages at the transmitter and the receiver. In this case, we only focus our attention on a single group instead of G groups, since the same procedure is applied to all groups, as shown in Fig.2. The transmitter model is introduced in Section II-A, followed by the receiver model in Section II-B.

A. Transmitter

As shown in Fig. 2, b bits are split into G groups, where the b_g bits, ($g = 1, 2, 3 \dots G$) of each group are split into two parts by the block splitter: b_g^1 bits are used for JMIM mapping matrix selection and b_g^2 bits for the classic PSK/QAM. In the following we explain in detail the Joint Index Mapping (JIM) part of the CS-JMIM transmitter of Fig. 2.

1) *Joint Index Mapping*: As shown in Fig.2, the N_c subcarriers of the OFDM symbol are divided into G groups of size N_f , with $N_f = N_c/G$. For each b_g group of bits, the first part b_g^1 is used for selecting the active DM from the Q candidates $D_1, D_2, \dots, D_q, \dots, D_Q$ with $D_q \in \mathbb{C}^{N_v \times N_{vt}}$, $q = 1, 2, \dots, Q$. The second part is used for determining the constellation symbol, which is employed for modulating the active DM. The classic constellation symbol is then selected from a M -ary PSK or QAM constellation χ .

Let us denote the selected DM and the selected constellation symbol, respectively, by $D_i, i \in \{1, \dots, Q\}$ and $x, x \in \chi$. Then the combined signal in group g can be expressed by

$$S_g = xD_i, g = 1, \dots, G. \quad (1)$$

In the following, we introduce three designs of the DMs. Firstly, to leverage the multi-dimensionality of MIM systems, the design of IM encompasses all dimensions. Then, the activation of the corresponding indices is guided by the

¹FD is the OFDM symbol domain after CS processing, as shown in Fig. 2.

²VD is the actual domain. This concept was firstly introduced in [10] to illustrate the CS techniques in IM systems to improve the spectral efficiency.

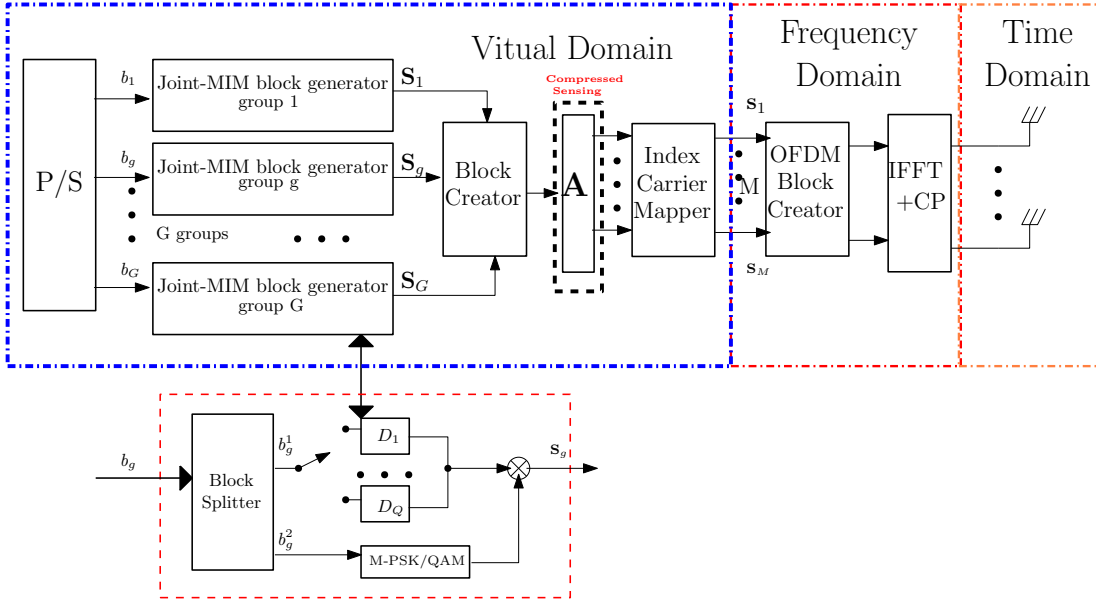


Fig. 2: CS-JMIM system transmitter block diagram.

251 coordinates of these joint dimensions, which is detailed in the
 252 following section in the context of a DM design referred to
 253 as General JIM. Secondly, to strike a design trade-off between
 254 the throughput and diversity gain attained, we can further split
 255 the joint multi-dimensional matrix into sub-group matrices,
 256 where different general JIM DMs can be selected for each
 257 sub-group matrix. We refer to this mapping design as Grouped
 258 JIM, which is further detailed in the following sections.
 259 Additionally, we introduce a coded DM design for achieving
 260 a high diversity gain, which is detailed in the following
 261 sections. Furthermore, we start a discussion considering the
 262 Space-Frequency (SF) dimensions and then we present a 3-
 263 dimensional mapping design for the Time-Space-Frequency
 264 (TSF) dimensions of JMIM.

265 *a) General Joint Index Mapping:* As JIM, first we con-
 266 sider joint SF DM design. The index is selected based on
 267 both dimensions' coordinates. We assign N_{vt} TAs and N_v
 268 subcarriers to a specific group, which results in $N_{vt}N_v$ possi-
 269 ble active positions and to a total of $C(N_tN_{vt}, K)$ legitimate
 270 realizations. As an example, let us consider having $K = 2$
 271 active subcarriers and $N_{vt} = 2, N_v = 2$ for each group. Then,
 272 we have $b_g^1 = \lceil \log_2 C(N_{vt}N_v, K) \rceil = \lceil \log_2 C(4, 2) \rceil = 2$ bits
 273 for selecting $K = 2$ active subcarriers out of 4 available
 274 subcarriers in each group, since we have $2^2 = 4$ legitimate
 275 combinations which equivalent to $Q = 4$ DMs, as shown in
 276 Table II. Fig.3 shows a block diagram of the general JIM
 277 example presented in Table II, where the activated index is
 278 then combined with the QAM symbol by the multiplier to
 279 form the combined symbol S . Furthermore, when compared
 280 to the CS-aided separate MIM system, CS-JMIM can attain
 281 comparable throughput as CS-MIM with significant sparsity.

282 *b) Grouped Joint Index Mapping:* Given a substantial
 283 number of TAs, subcarriers, and a limited quantity of active
 284 index elements K in each group, most elements in the DM
 285 remain inactive, leading to diminished SE. To address this,
 286 we propose grouped JIM, which divides the DM matrix into

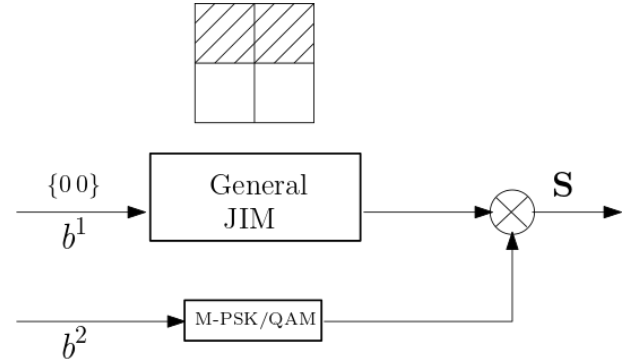


Fig. 3: Block diagram of the general JIM example in Table II with $b_1=[0 0]$.

TABLE II: An example selection procedure of joint SF index selection in a CS-JMIM system having $K = 2, N_v = N_{vt} = 2$

b_2	matrix No.	Indices	Allocation
[00]	D_1	(1, 2)	$\begin{bmatrix} 1 & 1 \\ 0 & 0 \end{bmatrix}$
[01]	D_2	(1, 3)	$\begin{bmatrix} 1 & 0 \\ 1 & 0 \end{bmatrix}$
[10]	D_3	(1, 4)	$\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$
[11]	D_4	(2, 3)	$\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$

287 smaller sub-group matrices, each adopting a general JIM. Fur-
 288 thermore, striking a trade-off between throughput and diversity
 289 involves choosing either the same or different DMs across
 290 groups. To elaborate further, applying the same DM across
 291 all groups results in multiple copies of the information bits,
 292 which produces a diversity gain. On the other hand, employing
 293 different DMs for each group improve the throughput.

294 For example upon assuming $N_{vt} = 4, N_v = 4$ and $K = 2$
 295 for each groups DM results in $D_q \in \mathbb{C}^{N_{vt} \times N_v}$. Then, we

296 further split D_q into four equal sub-matrices expressed as

$$D_q = \begin{bmatrix} D_q^{1,1} & D_q^{2,1} \\ D_q^{1,2} & D_q^{2,2} \end{bmatrix}, \quad (2)$$

297 where we have $D_q^i \in \mathbb{C}^{N_{vt}/2 \times N_v/2}$, $i = 1, 2, 3, 4$. For each
 298 sub-matrix $D_q^{i,j}$, ($i = 1, 2, 3 \dots gsx$), ($j = 1, 2, 3 \dots gsy$) general
 299 JIM can be applied. Here, gsx and gsy represent the number
 300 of sub-group's in the FD and SpD, respectively. In the above
 301 example, we can have a total of $gs = gsx \times gsy = 4$
 302 sub-groups and $b_g^1 = \lfloor \log_2 C(4, 2) \rfloor = 2$ bits for each sub-
 303 groups matrix. To maximize the throughput, four different
 304 sub-matrices can be aggregated to one DM D_q to obtain 8
 305 bits in total. Fig.4 shows the block diagram of the grouped
 306 JIM, where we have four sub-groups of smaller general JMIM
 307 matrix. For a small general JMIM matrix we can apply $Q = 4$
 308 DMs in total, where we can assign 4×2 bits for all sub-groups.
 309 On the other hand, if four repeated sub-matrices are used, we
 310 can achieve similar structure of coded JMIM which will be
 311 discussed below.

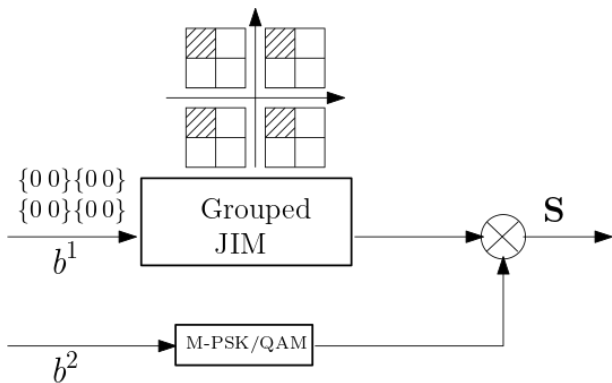


Fig. 4: Block diagram of a grouped JIM example with $b_1=[0\ 0\ 0\ 0\ 0\ 0\ 0\ 0]$

312 *Subsequently, the grouped JIM optimally utilizes the avail-*
 313 *able space of the VD matrix, albeit at the expense of sparsity.*
 314 *By adjusting the index mapping of each sub-group, it offers*
 315 *significant throughput or diversity gains. However, this leads*
 316 *to a substantial increase in detection complexity for conven-*
 317 *tional methods, such as the ML detector.*

318 *c) Coded Joint Index Mapping:* Another way of further
 319 increasing the transmit diversity is to employ coded index
 320 mapping, where we use a circular shift based design of the
 321 DMs, which was proposed for SFSK in [17]. In this method,
 322 the number of active subcarriers in each column is n_q , with
 323 $N_q - n_q$ inactive subcarriers, where N_q is the column length
 324 of D_q . Then, the second column is the circular down shift of
 325 the first column by one position. Similarly, other columns can
 326 be obtained based on the previous column distribution.

To elaborate a little further, using a 'toy' example, for $N_q = N_{vt} = 4$, $n_q = 2$, we can have $Q = C(N_q, n_q) = 6$ possible combinations, yielding $b_g^1 = \lfloor \log_2 C(N_q, n_q) \rfloor = 2$ bits. The

following is an example of a circular shifting based DM:

$$D_1 = \begin{bmatrix} 1 & 0 & 0 & 1 \\ 1 & 1 & 0 & 0 \\ 0 & 1 & 1 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}, D_2 = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \\ 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix},$$

$$D_3 = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 1 & 1 & 0 \\ 0 & 0 & 1 & 1 \\ 1 & 0 & 0 & 1 \end{bmatrix}, D_4 = \begin{bmatrix} 0 & 0 & 1 & 1 \\ 1 & 0 & 0 & 1 \\ 1 & 1 & 0 & 0 \\ 0 & 1 & 1 & 0 \end{bmatrix},$$

$$D_5 = \begin{bmatrix} 0 & 1 & 0 & 1 \\ 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \\ 1 & 0 & 1 & 0 \end{bmatrix}, D_6 = \begin{bmatrix} 0 & 1 & 1 & 0 \\ 0 & 0 & 1 & 1 \\ 1 & 0 & 0 & 1 \\ 1 & 1 & 0 & 0 \end{bmatrix}.$$

Given $b_g^1 = 2$ bits, then $2^2 = 4$ DMs are selected for the CS-JMIM system.

Fig.5 shows a block diagram of the coded JIM, where we can apply the first JIM DM for $b_1=[0\ 0]$ based on the code book used. *In this scenario, coded JIM offers the maximum diversity in the design of coded DMs, enabling reliable detection even in highly noisy environments.*

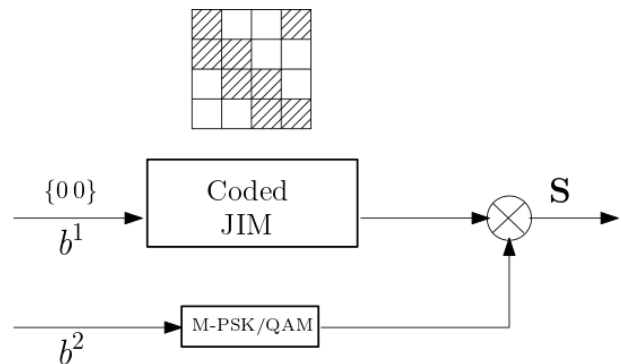


Fig. 5: Block diagram of a coded JIM example with $b_1=[0\ 0]$

334 *d) 3-Dimensional Dispersion Matrix Design:* In this design,
 335 the TD is introduced as an extra dimension for the JIM.
 336 We assume that T_v TSSs are applied in the VD and T TSSs are
 337 used in the TD, while we have $T_v > T$. Then, we can assign
 338 three-dimensional DMs $D_q \in \mathbb{C}^{N_v \times N_{vt} \times T_v}$. In this case, the
 339 above-mentioned three mapping techniques can be applied.

340 Specifically, for the general JIM we may consider the
 341 following example for further illustration. Let $K = 1$ and
 342 $N_{vt} = N_v = T_v = 2$ as shown in Fig. 6(a) and $b_g^1 = [001]$.
 343 More specifically, the three-dimensional matrix can be expressed
 344 in the coordinate form of (n_v, n_{vt}, t_v) . In this case,
 345 given the IM bits $b_g^1 = [010]$, we activate the fourth element in
 346 a set of 8 elements in this three-dimensional matrix with the
 347 coordinates $(2, 2, 1)$ as shown in Fig. 6(a). Then, the number
 348 of bits of this JMIM applied for the DM selection becomes
 349 $b_g^1 = \lfloor \log_2 C(N_{vt} N_v T_v, K) \rfloor = \lfloor \log_2 C(8, 1) \rfloor = 3$ bits.

350 Fig. 6(b) shows the structure of the grouped JIM applied in
 351 three dimensions. Similar to the SF matrix, the TSF matrix can
 352 be split into several equal sub-groups. As shown in Fig. 6(b),
 353 we assume $N_{vt} = N_v = T_v = 4$ and $K = 1$ for each group's
 354 DM, which results in $D_q \in \mathbb{C}^{N_v \times N_{vt} \times T_v}$. Then, we further
 355 split D_q into 8 equal sub-matrices. Each sub-group DM can

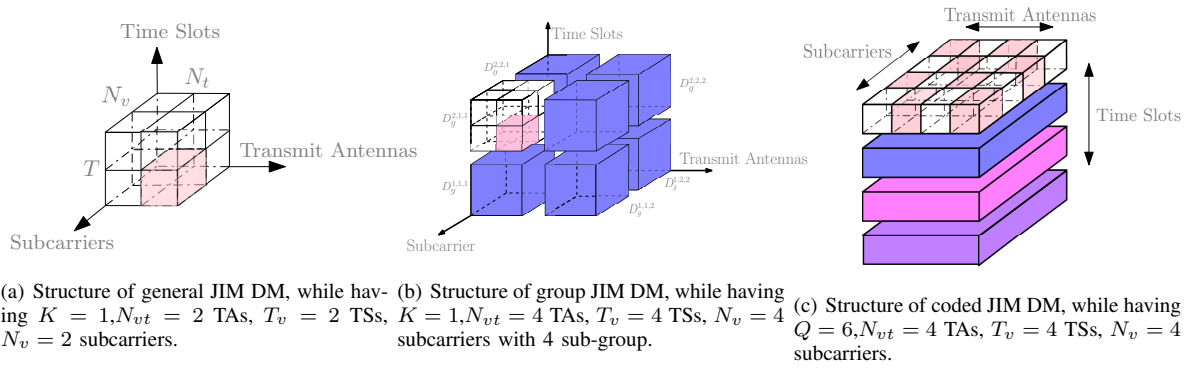


Fig. 6: Illustration of the structure for JIM DM in time-space-frequency domain

356 be expressed in the form of $D_g^{gsx,gsy,gsz}$, where gsx,gsy,gsz
 357 represents the split size in the FD, the SpD, and the TD,
 358 respectively. For each sub-matrix $D_g^{gsx,gsy,gsz}$, general JIM
 359 can be applied within a set of $gs = gsx \times gsy \times gsz = 8$ sub-
 360 group matrices. Then, we can have $\lfloor \log_2 C(8, 1) \rfloor = 3$ bits
 361 for each sub-matrix. To maximize the throughput, we can also
 362 assign different information to each sub-group and then the 8
 363 sub-matrices can be aggregated to form a single DM D_q
 364 to obtain $b_g^1 = gs \lfloor \log_2 C((N_v/gsx)(N_t/gsy)(T/gsz), K) \rfloor =$
 365 $8 \lfloor \log_2 C(8, 1) \rfloor = 24$ bits for the JMIM design. Compared
 366 to the same DM size used in the general JIM, which has
 367 $b_g^1 = \lfloor \log_2 C(64, 1) \rfloor = 6$ bits, the grouped JIM can provide a
 368 significant gain in the spectral efficiency. On the other hand,
 369 in order to attain a diversity gain, the sub-matrices can achieve
 370 maximum diversity gain, when all 8 sub-groups have the same
 371 active index.

372 Furthermore, for the coded JIM matrix design in three
 373 dimensions, the same method is applied for the first TS of
 374 the space-frequency matrix. Then, circular shifting is applied
 375 to the entire SF matrix to generate the next TS matrix
 376 with shifting by one position. As shown in Fig. 6(c), upon
 377 assuming $N_{vt} = N_v = T_v = 4$ for the DM size, as well as
 378 $N_q = n_q = 2$ for the activated subcarriers and $b^1 = [01]$, then
 379 the corresponding circular shifting based DM D_2 presented in
 380 the previous section is applied to the first TS of the 3D matrix.
 381 Then, we can generate each TS index mapping with the aid
 382 of a single position shifting, which can be represented as:

$$D_{t1} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \\ 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}, D_{t2} = \begin{bmatrix} 0 & 1 & 0 & 1 \\ 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \\ 1 & 0 & 1 & 0 \end{bmatrix},$$

$$D_{t3} = \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \\ 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}, D_{t4} = \begin{bmatrix} 0 & 1 & 0 & 1 \\ 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \\ 1 & 0 & 1 & 0 \end{bmatrix}.$$

383 2) *Compressed Sensing and Block Assembly*: In order to
 384 exploit the sparsity of the JIM DM, CS is applied to all
 385 the dimensions of the joint multi-dimensional matrix symbol
 386 created by the block assembled to increase the throughput. As
 387 shown in Fig. 7, a matrix S_g associated with $N_{vt} = N_v = 4$

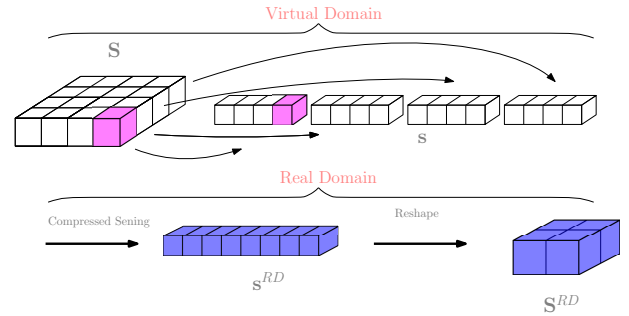


Fig. 7: Illustration of the process for compressing the JMIM DM in the SF domain with $N_{vt} = N_v = 4, K = 1$. Note that this example applies the general JIM with $b_g^1 = [0100]$.

388 will be transformed from the matrix $S, S \in \mathbb{C}^{N_{vt} \times N_v}$ into the
 389 vector $s, s \in \mathbb{C}^{N_{vt} N_v \times 1}$.

390 The symbol vector s is then compressed by a CS measure-
 391 ment matrix $A \in \mathbb{C}^{N_f N_t \times N_v N_{vt}}$ from the $N_v N_{vt}$ -dimensional
 392 s in the VD into the $N_f N_t$ -dimensional form in the Real
 393 Domain (RD)³ denoted as $s^{(RD)}$, which can be written
 394 as: $s^{RD} = As$. The RD vector s^{RD} after CS is then
 395 transferred into a compressed joint multidimensional symbol
 396 matrix $S^{(RD)}$, where $S^{(RD)} \in \mathbb{C}^{N_t \times N_f}$. Then, the index
 397 carrier mapper maps the corresponding joint multidimensional
 398 symbol elements to the OFDM subcarriers and the TAs to form
 399 the SF symbols. Afterwards, G groups of SF symbols S are
 400 assembled by the OFDM creator to a long SF symbol frame, as
 401 shown in Fig. 2. The RD SF symbol can be separated into N_t
 402 FD symbols, which means that N_t FD symbols are transmitted
 403 by N_t TAs. Similar to conventional OFDM, the FD symbol
 404 will be transformed into TD symbols to be transmitted by
 405 their corresponding TAs and then a Cyclic Prefix (CP) will
 406 be added. The G groups of SF symbols S are assembled
 407 by the block creator of Fig. 2 to form a long ST frame,
 408 which is processed by the ST mapper to output a symbol for
 409 transmission over multiple TAs and TSs, Equivalently, the ST
 410 symbols S of each subcarrier group are mapped to N_t TAs
 411 during T TSs, which have N_t symbol sequences $\{s_1, \dots, s_{N_t}\}$
 412 for transmission from the N_t TAs during each TS.

³RD is the joint dimension of DM after the CS process. For instance, the SF-based JMIM signal conveys more bits in the VD than in the RD.

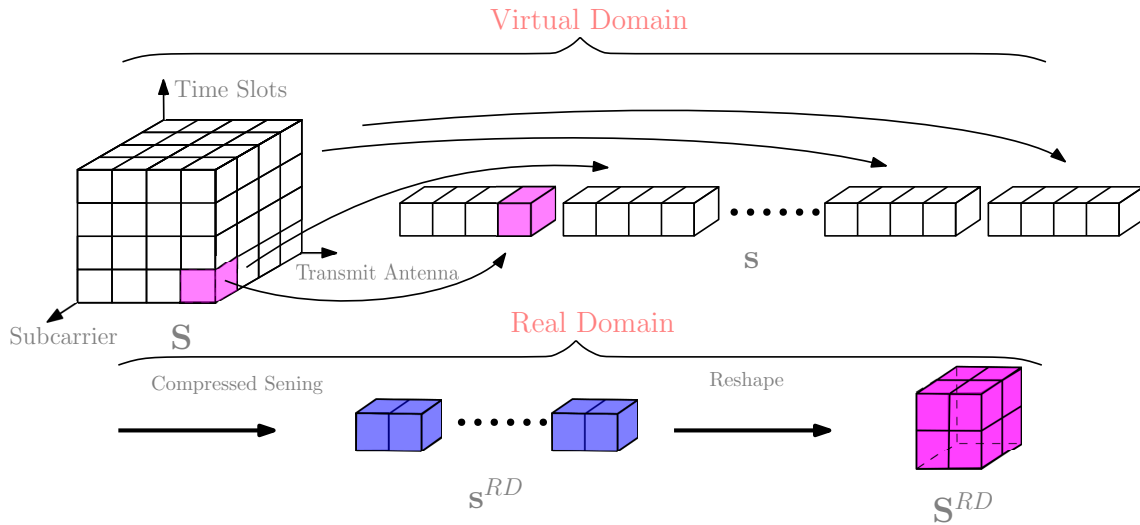


Fig. 8: Illustration of the process for compressing the JMIM DM in the TSF domain with $T = N_t = N_v = 4K = 1$. Additionally, the example presented applies the general JIM for $b_g^1 = [000100]$.

413 For the three-dimensional JMIM, utilizing the TSF dimensions, the TD is also compressed by CS for improving the
 414 throughput, where T_v TSs are introduced in the VD for IM, complemented by T TSs in the TD. Specifically, for the
 415 general JMIM scheme, the TD is introduced for increasing the sparsity and for incorporating extra embedded information
 416 bits. As shown in Fig. 8, we apply CS to the TSF JMIM, where all the three dimensions are compressed for increasing
 417 the throughput. Specifically, a $(4 \times 4 \times 4)$ -sized DM in the VD will be compressed to a $(2 \times 2 \times 2)$ -sized DM of the RD. For
 418 example, when we have $T_v = N_{vt} = N_v = 4$, $b_g^1 = [000100]$ and $K = 1$, the element at the fourth subcarrier, fourth TA
 419 and first TS is activated, corresponding to the coordinate of $(4, 4, 1)$.
 420

421 As for the coded JMIM scheme, additionally the TD is harnessed for further increasing the diversity gain, where CS
 422 is not considered for the TD. We assign either the same or different symbols in a sub-group matrix of the grouped JMIM
 423 scheme, which leads to a different CS approach. Given the different sub-group matrix symbols, the TD is exclusively
 424 harnessed for carrying extra copies of the symbol without CS. The design objective of this scheme is to increase the diversity
 425 gain.
 426

436 B. Receiver Processing

437 As shown in Fig. 9, a receiver having N_r antennas is employed, where we assume that the transmitted signals are
 438 conveyed over a frequency-selective Rayleigh fading channel and the CSI is perfectly acquired at the receiver side. The G
 439 groups of signal are received by the receiver over N_r antennas and then the CP part of the received signals is removed.
 440 Finally, the processed signal is transformed into the FD by using the Fast Fourier Transform (FFT), as shown in Fig. 9.
 441

442 The channel model can be expressed as $\mathbf{h}_\alpha \in \mathbb{C}^{N_r \times N_t}$, which represents the TD CSI between the N_t TAs and the
 443 N_r RAs. Then, the FD channel matrix can be expressed as $\mathbf{H}_\alpha \in \mathbb{C}^{N_r \times N_t}$ for $\alpha = 1, \dots, M$, which are then

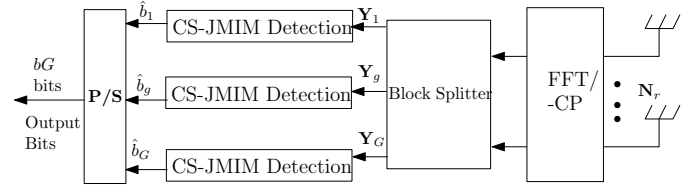


Fig. 9: CS-JMIM system receiver block diagram

444 split into G groups by the Block Splitter of Fig. 9. The symbols received by each subcarrier group are represented as
 445 $\mathbf{Y} = \{\mathbf{Y}[1], \dots, \mathbf{Y}[\alpha], \dots, \mathbf{Y}[N_f]\}$, with $\mathbf{Y} \in \mathbb{C}^{N_r \times N_f}$ and $\alpha = 1, 2, \dots, N_f$.
 446

447 As for the three-dimensional signal, the transmitted signal is mapped ST symbols, which are also collected by the receiver
 448 and split into G groups by the Block Splitter of Fig. 9. Afterwards, the symbols received in the three dimensions by
 449 each subcarrier group $\mathbf{Y} \in \mathbb{C}^{N_r \times M \times T}$ may be expressed as
 450

$$451 \mathbf{Y} = \left\{ \begin{bmatrix} \mathbf{Y}_{1,1}^1 & \dots & \mathbf{Y}_{1,N_f}^1 \\ \dots & \dots & \dots \\ \mathbf{Y}_{1,1}^{N_r} & \dots & \mathbf{Y}_{1,N_f}^{N_r} \end{bmatrix}_1, \dots, \begin{bmatrix} \mathbf{Y}_{T,1}^1 & \dots & \mathbf{Y}_{T,N_f}^1 \\ \dots & \dots & \dots \\ \mathbf{Y}_{T,1}^{N_r} & \dots & \mathbf{Y}_{T,N_f}^{N_r} \end{bmatrix}_T \right\}. \quad (3)$$

452 The received symbol of the t -th TS can be represented as $\mathbf{Y}_t = \{\mathbf{Y}_t[1], \dots, \mathbf{Y}_t[\alpha], \dots, \mathbf{Y}_t[N_f]\}$, with $\mathbf{Y}_t \in \mathbb{C}^{N_r \times T}$
 453 and $\alpha = 1, 2, \dots, N_f, t = 1, 2, \dots, T$ characterizing the ST structure per group and the ST symbol received at the α -th
 454 subcarrier of each subcarrier group, respectively. Since the index is jointly decided in the multi-dimensional space, we can
 455 transform the ST symbol into a vectorial form \mathbf{y} associated with $\mathbf{y} \in \mathbb{C}^{N_r N_f T \times 1}$.
 456

457 Let the FD channel be $\mathbf{H}_\alpha \in \mathbb{C}^{N_r \times T}$ for $\alpha = 1, \dots, N_f$. Then the signal $\mathbf{Y}_t[\alpha] \in \mathbb{C}^{N_r \times T}$ ($\alpha = 1, \dots, N_f$) received
 458 during the T TSs for each subcarrier group can be expressed as [22]
 459

$$460 \mathbf{Y}[\alpha] = \mathbf{H}_\alpha \mathbf{S}^{(RD)}[\alpha] + \mathbf{W}[\alpha], \quad (4)$$

where $\mathbf{S}^{RD}[\alpha] \in \mathbb{C}^{N_r \times T}$ denotes the ST symbols at the sub-carrier α transmitted from the N_t TAs in the RD. Furthermore, $\mathbf{W}[\alpha] \in \mathbb{C}^{N_r \times T}$ represents the Additive White Gaussian noise (AWGN) obeying the distribution of $\mathcal{CN}(0, \sigma_N^2)$, and σ_N^2 is the noise variance.

III. CS-JMIM SIGNAL DETECTION

Given the received signal model \mathbf{Y} in (4), the receiver detects the information bits of the JMIM mapping matrix, which jointly conveys the index of the active subcarrier, the active TA and TS in the VD. Firstly, we reshape the received signal into a vectorial form \mathbf{y} associated with $\mathbf{y} \in \mathbb{C}^{N_r N_f T \times 1}$.

The received signal \mathbf{y} contains N_f ST symbols at N_f subcarriers in the FD of each subcarrier group. Then, we can rewrite \mathbf{y} with the aid of (4) in the following form:

$$\mathbf{y} = \mathbf{H} \bar{\mathbf{A}} \bar{\mathbf{s}} + \mathbf{w}, \quad (5)$$

where $\bar{\mathbf{A}}$ is the equivalent measurement matrix \mathbf{A} used for compressing the s VD vectors. In our three-dimensional CS-JMIM system, $\bar{\mathbf{A}}$ also compresses the TD, where we have $\bar{\mathbf{A}} \in \mathbb{C}^{N_v t N_v \times N_t N_f}$. Furthermore, $\bar{\mathbf{s}} \in \mathbb{C}^{N_v N_v t T_v \times 1}$ denotes the vector of DM combined with the PSK/QAM symbol. In this case, we could rewrite $\bar{\mathbf{s}}$ in a matrix $\bar{\mathbf{S}}$ associated with $\bar{\mathbf{S}} = \mathbf{x} \bar{\mathbf{D}}$, where $\bar{\mathbf{D}} \in \mathbb{C}^{N_v \times N_v t \times T_v}$ denotes the realization of the JMIM DM in each subcarrier group.

Conventional exhaustive search based maximum likelihood (ML) detection can be applied at the receiver, albeit this may lead to excessive complexity [5]. Furthermore, in the soft detection scenario, the received signal is converted into probability values, which are referred to as Log Likelihood Ratios (LLR) that are fed into the channel decoder for obtaining a near-capacity performance [43].

In the following section we present the conventional ML-based HD detector, followed by our proposed DNN aided HD detector, where the neural network replaces the exhaustive search by a learning-based classification model in order to significantly reduce the complexity. Afterwards, we discuss the SD detector, where we first present the conventional SD detectors followed by our learning-aided SD receiver.

A. Hard Decision Decoding

Again, we commence with the conventional ML-based detection of the CS-JMIM system, followed by the DNN-based detector.

1) *Maximum Likelihood Detection:* As shown in Fig. 9, we detect each group's signal separately. In the CS-JMIM detector, according to the receiver model of (5), we have the modified joint JMIM and PSK/QAM symbol, which can be expressed as $\bar{\mathbf{S}} = \mathbf{x} \bar{\mathbf{D}}$. Here $\bar{\mathbf{D}}$ represents a specific realization of the selected JMIM DM and \mathbf{x} represents K STSK PSK/QAM symbols. To detect the specific realization, we use $\bar{\mathcal{D}}(\beta)$ ($\beta = 1, 2, \dots, N_{JMIM}$) to denote all the possible realizations of the JMIM DM. Furthermore, as there are $N_x = (X)^K$ realizations of \mathbf{x} , $\bar{\mathcal{X}}(\gamma)$ ($\gamma = 1, 2, \dots, N_x$) denotes all the possible realizations of the selected PSK/QAM symbol.

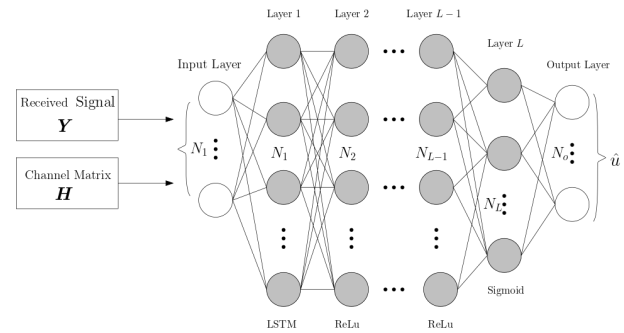


Fig. 10: Fully-connected DNN model for CS-JMIM HD detection.

The ML detector makes a joint decision concerning the JMIM DM and PSK/QAM with the aid of exhaustive search, which can be modelled as

$$\langle \hat{\gamma}, \hat{\beta} \rangle = \arg \min_{\gamma, \beta} \|\mathbf{Y} - \mathbf{H} \bar{\mathbf{A}} \bar{\mathcal{X}}(\gamma) \bar{\mathcal{D}}(\beta)\|^2, \quad (6)$$

where $\hat{\gamma}$ and $\hat{\beta}$ represent the estimates of the selected DM and the corresponding PSK/QAM constellation in each subcarrier group, respectively.

The excessively high search complexity of considering all possible candidates by the ML detector is given by $\mathcal{O}[N_{JMIM}(\mathcal{X})^K]$ per subcarrier group.

2) *DNN-based Detection:* To reduce the complexity of the ML detector, learning based detection is considered in this section, where a DNN based model is proposed for detecting the received CS-JMIM signal.

Detection may also be considered as a classification problem, where the corresponding bits of the harnessed CS-JMIM DM and PSK/QAM symbol constitute the DNN output. Under the assumption of perfect CSI at the receiver side, we use the received signal and the CSI as the input of the DNN model. The proposed DNN structure is shown in Fig. 10, where both the CSI \mathbf{H} at the receiver and the received symbols \mathbf{Y} constitute the inputs of the L -layer Fully-Connected (FC) network. Then, the output bits $\hat{\mathbf{u}}$ can be modelled as

$$\hat{\mathbf{u}} = f_{sigmoid}(\mathbf{W}_n \dots f_{Relu}\{\mathbf{W}_2(f_{Relu_1}[\mathbf{W}_1 f_{LSTM}(\mathbf{Y}) + \boldsymbol{\theta}_1]) + \boldsymbol{\theta}_2\} + \dots + \boldsymbol{\theta}_n), \quad (7)$$

where \mathbf{W}_n and $\boldsymbol{\theta}_n$, $n = 1, \dots, L$ represent the weights and biases, respectively. In (7), the Rectified linear unit (Relu) function of $f_{Relu}(s) = \max(0, s)$ is employed for activating the DNN during the training phase, while the sigmoid function of $f_{sigmoid}(s) = \frac{1}{1+e^{-s}}$ is used to obtain the detected bits $\hat{\mathbf{u}}$. The raw input data represented in the complex-valued matrix form obtained from the received signal \mathbf{Y} is vectorized first and then we rearrange the complex values by separately extracting the real as well as the imaginary parts and then merging them into a real-valued vector.

In the training phase, we employ randomly generated received signals, which are transmitted over a frequency selective Rayleigh fading channel for CS-JMIM. Afterwards, both the CSI and the received symbols are employed as the input data of the DNN. The number of training samples required is

558 selected based on experimentation by gradually increasing the
 559 training size until acceptable mean square error (MSE) values
 560 are achieved. In this case, the MSE loss function of the DNN
 561 used for the training is

$$\mathcal{L}(\mathbf{u}, \hat{\mathbf{u}}; \mathbf{W}_n, \boldsymbol{\theta}_n) = \frac{1}{B} \sum_{i=1}^B \|\mathbf{u} - \hat{\mathbf{u}}\|^2, \quad (8)$$

where B is the sample size of the current iteration. A stopping criterion can be defined either by the number of iterations or by an MSE threshold. Then, the parameter sets $\{\mathbf{W}_n, \boldsymbol{\theta}_n\}$ can be updated in each training iteration based on our learning algorithm using gradient descent, which is formulated as

$$\{\mathbf{W}_n, \boldsymbol{\theta}_n\} \leftarrow \{\mathbf{W}_n, \boldsymbol{\theta}_n\} - \alpha \nabla \mathcal{L}(\{\mathbf{W}_n, \boldsymbol{\theta}_n\}),$$

562 where $\alpha > 0$ is the learning rate and $\nabla \mathcal{L}(\{\mathbf{W}_n, \boldsymbol{\theta}_n\})$
 563 represents the gradient of $\mathcal{L}(\{\mathbf{W}_n, \boldsymbol{\theta}_n\})$. In our proposed
 564 network aided detection, we use $\alpha = 0.001$.

565 By the end of the training phase, the DNN has learnt the
 566 mapping from the received signal and stores both the weight as
 567 well as the bias information, which will be used for producing
 568 the desired outputs based on the input data in the testing
 569 phase. The statistical properties of the input/output data have
 570 to remain the same as those used during training.

571 The detection complexity of the learning algorithm is domi-
 572 nated by the calculation of the layer weights and biases, which
 573 may be considered to be of the order of $\mathcal{O}(n_i n_h) + \mathcal{O}(n_h^2) +$
 574 $\mathcal{O}(n_h n_o)$ [29], with n representing the number of neurons in
 575 each layer. Hence, the DNN complexity order is significantly
 576 lower than that of the ML detector.

577 B. Soft Decision Decoding

578 SD detection is employed for attaining near-capacity perfor-
 579 mance, when combined with channel coding. As the computa-
 580 tional complexity of the maximum *a posteriori* probability in
 581 SD detector rapidly increases upon increasing the modulation
 582 order and the number of dimensions [44], the complexity
 583 of CS-JMIM rapidly becomes prohibitive, owing to the joint
 584 detection of JMIM signal in multiple dimensions. In the
 585 following, we present the conventional SD detector of CS-
 586 JMIM, followed by the correspond learning aided SD detector.

587 1) *Conventional Soft Decision Detection*: A channel coded
 588 CS-JMIM scheme is shown in Fig. 11, which was derived from
 589 the CS-MIM model of [22], [36] for achieving near-capacity
 590 performance. A Recursive Systematic Convolutional (RSC)
 591 encoder encodes the information bit sequence \mathbf{b} followed by
 592 an interleaver, where the coded bit sequence \mathbf{c} is interleaved
 593 to generate the stream \mathbf{u} of Fig. 11. Then, the stream \mathbf{u} is
 594 modulated in the CS-JMIM modulator of Fig. 2.

595 At the receiver side of Fig. 11, the received signal \mathbf{Y} and
 596 CSI $\bar{\mathbf{H}}$ are input to the soft CS-JMIM that outputs LLRs.
 597 The LLRs output from the demodulator are then passed to the
 598 de-interleaver and the RSC decoder performs soft decoding. In
 599 Fig. 11, $L(\cdot)$ represents the LLRs of the bit sequences, where
 600 $L_e(u)$ is the output extrinsic LLR after soft demodulation and
 601 $L_a(c)$ is the de-interleaved LLR sequence of $L_e(u)$.

602 The LLR of a bit is defined as the ratio of probabilities
 603 associated with the logical bits '1' and '0', which can be

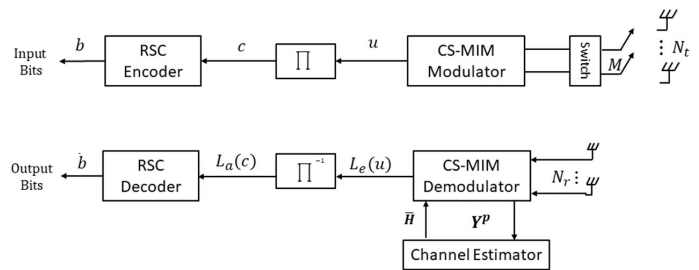


Fig. 11: The transceiver architecture of channel-coded CS-MIM.

written as $L(b) = \log \frac{p(b=1)}{p(b=0)}$. The conditional probability
 604 $p(\mathbf{Y}|\mathcal{X}_{\beta,\gamma})$ of receiving the group signal \mathbf{Y} is given by [45]
 605

$$p(\mathbf{Y}|\mathcal{X}_{\gamma,\beta}) = \frac{1}{(\pi N_0)^{NT}} \exp\left(-\frac{\|\mathbf{Y} - \mathbf{H}\bar{\mathbf{A}}x(\gamma)\bar{\mathbf{D}}(\beta)\|^2}{N_0}\right), \quad (9)$$

566 where $\mathcal{X}_{\gamma,\beta}$ represents the PSK/QAM symbol at the β -th CS-
 567 JMIM DM. Furthermore, N_0 is the noise power, where we
 568 have $\sigma_n^2 = N_0/2$ with $N_0/2$ representing the double-sided
 569 noise power spectral density.

Hence, we can formulate the LLR of bit u_i as

$$L_e(u_i) = \ln \frac{p(\mathbf{y}|u_i = 1)}{p(\mathbf{y}|u_i = 0)} = \ln \frac{\sum_{\mathcal{X}_{\gamma,\beta} \in \mathcal{X}_1^i} p(\mathbf{Y}|\mathcal{X}_{\gamma,\beta})}{\sum_{\mathcal{X}_{\gamma,\beta} \in \mathcal{X}_0^i} p(\mathbf{Y}|\mathcal{X}_{\gamma,\beta})}, \quad (10)$$

571 where \mathcal{X}_1^i and \mathcal{X}_0^i represent a subset of the legitimate equiv-
 572 alent signal \mathcal{X} corresponding to bit u_i , when $u_i = 1$ and
 573 $u_i = 0$, respectively, yielding $\mathcal{X}_1^i \equiv \{\mathcal{X}_{\gamma,\beta} \in \mathcal{X} : u_i = 1\}$ and
 574 $\mathcal{X}_0^i \equiv \{\mathcal{X}_{\gamma,\beta} \in \mathcal{X} : u_i = 0\}$.

575 Upon using (9) and (10) we obtain the LLR $L(b_i)$ of the bit
 576 sequence conveyed by the received signal \mathbf{Y} . To simplify the
 577 calculation, the Approximate Log-MAP (Approx-Log-MAP)
 578 algorithm based on the Jacobian Maximum operation can be
 579 used, which is given by [46], [47]

$$L_e(u_i) = \text{jac}_{\mathcal{X}_{\gamma,\beta} \in \mathcal{X}_1^i}(\lambda_{\gamma,\beta}) - \text{jac}_{\mathcal{X}_{\gamma,\beta} \in \mathcal{X}_0^i}(\lambda_{\gamma,\beta}), \quad (11)$$

580 where $\text{jac}(\cdot)$ denotes the Jacobian maximum operation and the
 581 intrinsic metric of $\lambda_{\gamma,\beta}$ is

$$\lambda_{\gamma,\beta} = -\|\mathbf{Y} - \mathbf{H}\bar{\mathbf{A}}x(\gamma)\bar{\mathbf{D}}(\beta)\|^2/N_0. \quad (12)$$

622 At the receiver, the soft demodulator evaluates the prob-
 623 ability of each bit being logical '1' and '0'. Then it ap-
 624 plies the approx-log-MAP algorithm for obtaining the extrin-
 625 sic LLR of the coded bits, which has a complexity order
 626 $\mathcal{O}[2^{(c_g)}(N_{JMIM}(\mathcal{X})^K)]$, where c_g represents the number of
 627 coded bits after the RSC encoder and interleaver, and N_{JMIM}
 628 represents the number of possible realizations of JMIM.

629 2) *DNN-based SD Detection*: In this section, we propose a
 630 reduced-complexity SD detector using DNN, which considers
 631 a similar DNN architecture to that of [29]. Since the conven-
 632 tional SD detector obtains the LLRs of the received signal
 633 after the CS-MIM soft demodulator, we replace the detected

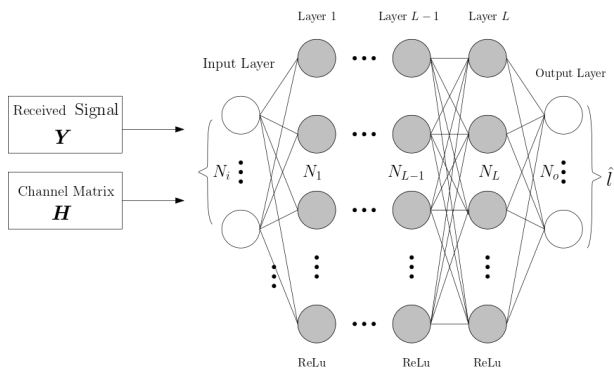


Fig. 12: Fully-connected DNN model for CS-JMIM SD detection.

bits \hat{u} output by the DNN in Fig. 10 with the extrinsic LLR L_e at the output of the DNN, as shown in Fig. 12. Then, the output of the SD DNN model can be expressed as

$$\hat{L}_e = \mathbf{W}_{N_2} \dots f_{Relu} \{ \mathbf{W}_2 (f_{Relu_1} [\mathbf{W}_1 (\mathbf{Y}_\tau) + \mathbf{b}_1]) + \mathbf{b}_2 + \dots + \mathbf{b}_{N_2} \}, \quad (13)$$

and the corresponding loss function is

$$\mathcal{L}(\theta,) = \frac{1}{BT} \sum_{i=1}^B \sum_{t=1}^T \|\hat{L}_e(\tau) - L_e(\tau)\|_2^2. \quad (14)$$

We can also define a stopping criterion, which can be either the number of iterations or meeting a maximum MSE threshold. Then, the parameter sets $\{\mathbf{W}_n, \theta_n\}$ can be updated in each training iteration based on the learning algorithm using gradient descent, which is formulated as

$$\{\mathbf{W}_n, \theta_n\} \leftarrow \{\mathbf{W}_n, \theta_n\} - \alpha \nabla L(\{\mathbf{W}_n, \theta_n\}),$$

where $\alpha > 0$ is the learning rate and $\nabla L(\{\mathbf{W}_n, \theta_n\})$ represents the gradient of $L(\{\mathbf{W}_n, \theta_n\})$.

In our proposed neural network aided detection, we use $\alpha = 0.001$. Similar to the HD DNN detector described above, the model learns the parameters in the training phase and then outputs the LLR information.

The detection complexity of the learning algorithm is dominated by the calculation of the layer weights and biases, which may be considered to be of the order $\mathcal{O}(n_i n_h) + \mathcal{O}(n_h^2) + \mathcal{O}(n_h n_o)$ [29], with n representing the number of neurons in each layer.

IV. ADAPTIVE DESIGN

Since the proposed CS-JMIM design provides flexibility in the design of the JMIM DM, we can design appropriate JMIM DMs for different channel conditions that can provide either an improved BER performance or an increased throughput. Furthermore, in our system, the transmitter can adapt both the JMIM DM \mathcal{D} and the modulation order Q of PSK/QAM. Then, the system throughput may be adapted by appropriately adjusting the above parameters, while maintaining a target BER performance.

In the following two subsections, we highlight the classic threshold-based adaptive modulation, followed by its learning-aided counterpart. More specifically, both the KNN and DNN based adaptive model are applied for the proposed system.

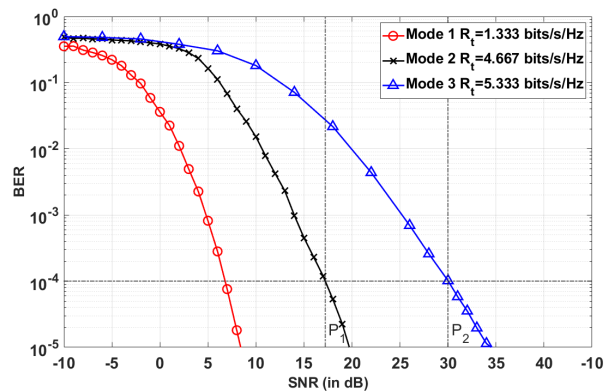


Fig. 13: BER vs. SNR performance of the CS-JMIM system for different mapping modes shown in Table III.

TABLE III: Configuration of the modes presented in Fig. 13

Mode	Mapping Type	Q	N_t	$N_v t$	N_f	N_v	K	R_t
1	Coded	4	4	8	4	8	2	1.333
2	General	4	4	8	4	8	3	4.666
3	Grouped	4	4	8	4	8	1	5.333

1) *Conventional Threshold-based Adaptive Design:* In our adaptive scheme, we can adapt both the configuration of JMIM DM and of the PSK/QAM mode. We can define the different configurations as *Mode1*, *Mode2*, *Mode3*, ..., which can attain different BER performance and throughput. Based on the different modes, the parameters N_v, N_t, T and A of JMIM DM can be selected according to the SNR calculated at the receiver, where the SNR threshold values are selected for the different modes to satisfy a specific target BER [41], [42]. In the following, we present the scenario, where the different adaptive modes P refer to different configurations of the JMIM DM for characterising its design flexibility⁴.

As an example, Fig.13 shows the BER performance of three different CS-JMIM mapping modes. The corresponding parameters and data rates provided by these modes are shown in Table III. For a target BER of 10^{-3} , as shown in Fig. 13 the SNR values of mode transition points P_1 and P_2 can be selected as the thresholds for operating the appropriate modes. Specifically, *Mode1* is applied at low SNR values until the specific SNR reaches P_1 . Then, the mode is changed to *Mode2* to provide higher throughput, when the SNR range spans from P_1 to P_2 . Finally, *Mode3* is selected at SNRs higher than P_2 , which has the highest throughput among the three modes.

For adaptive modulation, the receiver has to confidently infer the choice of the most appropriate transmission mode by comparing the instantaneous SNR of the received symbol against the Mode-switching threshold values. Then, the decision is fed back to the transmitter and applied for the next frame to be transmitted. Generally, with more available operation modes as well as faster and more accurate SNR feed-

⁴Note that the modulation scheme such as PSK/QAM can also be adapted, but in this design example, we aim to show the flexibility of the proposed CS-JMIM design.

back to the transmitter, we can obtain an increased throughput compared to non-adaptive designs. However, threshold-based adaptive modulation design ignores many of the hardware imperfections when deciding upon the threshold values, which results in sub-optimal performance of the adaptive system [41], [42]. Hence, in the next subsection, we propose the learning-based adaptive modulation scheme for our CS-JMIM system to further improve the adaptive system's performance.

2) *Learning aided adaptive modulation*: The adaptive modulation can be modelled as a classification problem, which can be solved using learning-based methods. The SNR of the received signal, which is evaluated at the receiver side, can be fed back to the transmitter and then given the SNR information, which also corresponds to the current channel state information, the transmitter can select a specific mode from a range of candidates to achieve the highest throughput, which still maintain the target BER. Therefore, for a given channel condition, adaptive modulation selects the most suitable mode to achieve the highest throughput, under the constraint of achieving the target BER. In this paper, both the KNN and DNN techniques are investigated in the context of adaptive modulation.

Before the training phase, the input data should be pre-processed to improve the learning efficiency. First, we randomly generate the training data of each mode under different instantaneous SNR values at the receiver. Then, the corresponding switching SNRs that can maintain a BER lower than the target BER are stored. Given these training data, we can use learning models to find the mode switching thresholds in the training phase. After training, the trained model becomes capable of predicting the next mode, given the knowledge of the SNR. In the following, we first employ KNN for our adaptive modulation scheme and then we propose a DNN-based adaptive model for further improving the performance.

a) *KNN-based Adaptive Design*: KNN is a popular classification techniques relying on low-complexity implementation and yet providing a good performance [48]. Yang *et al.* [40] developed KNN-assisted adaptive modulation schemes for SM, while Liu *et al.* [41] further developed DNN aided adaptive modulation to millimeter wave communication. To elaborate briefly on the KNN process, we define the training sets as

$$\mathcal{T}^{(i)} = [\xi_1^{(i)}, \dots, \xi_n^{(i)}, \dots, \xi_{N_p}^{(i)}]^T, \quad (15)$$

where ξ represents the SNR value of a symbol with a BER lower than the target BER value, with $i = 1, 2, \dots, \mathcal{I}$ representing the adaptive mode index and N_p is the total number of instantaneous SNR values with BER under the target. Then, the total training set of each mode can be formulated as

$$\mathcal{T} = [\mathcal{T}^{(1)}, \dots, \mathcal{T}^{(i)}, \dots, \mathcal{T}^{(I)}]^T. \quad (16)$$

During runtime, for a given new data point, which corresponds to the instantaneous SNR ξ , the KNN model finds k nearest neighbours in the training set \mathcal{T} , using a distance metric $d(\cdot)$, which can be expressed as

$$d(\xi_n^{(i)}, \xi_{new}) = \|\xi_n^{(i)} - \xi_{new}\|^2. \quad (17)$$

Then, the mode is decided by the majority mode of the k nearest neighbours to the input test point. With the possibility

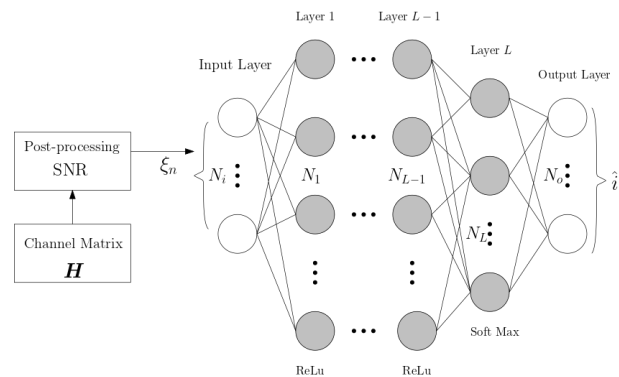


Fig. 14: Fully-connected DNN model for CS-MIM adaptive modulation selection.

of several modes having the same number in the k nearest neighbours, the mode with the highest throughput will be selected.

The performance of KNN significantly depends on its parameters and on the value of k , where the best value of k can be selected empirically. In this adaptive system, the best value of k is determined by considering the trade-off between the BER and throughput. Furthermore, KNN results in a high computational complexity for the nearest neighbour search in addition to requiring a large memory for storing the training. Hence, in the following we present a DNN based design alternative.

b) *DNN-aided Adaptive Design*: In this section, we present the DNN-based adaptive modulation regime of Fig. 14. Similarly to KNN, we randomly generate the training data and then store the mode index and SNR value pairs, which have BERs lower than the target value. Then, the training set \mathcal{T} constitutes the estimated SNR ξ of a symbol associated with a BER lower than the target BER. We use the DNN-based classification model, where the input corresponds to the instantaneous SNR and the output corresponds to the mode index of adaptive modulation.

The output mode index \hat{i} of the DNN can be expressed as

$$\hat{i} = f_{softmax}(\mathbf{W}_n \dots f_{Relu}\{\mathbf{W}_2(f_{Relu_1}[\mathbf{W}_1\xi + \boldsymbol{\theta}_1]) + \boldsymbol{\theta}_2\} + \dots + \boldsymbol{\theta}_n), \quad (18)$$

where \mathbf{W}_n and $\boldsymbol{\theta}_n$, $n = 1, \dots, L$ represent the weights and biases, respectively. Relu is also employed for activating the DNN during the training phase, and the softmax function is used to obtain the mode index \hat{i} , which is

$$f_{softmax}(s) = \frac{e^s}{\sum_{c=1}^C e^{s_c}}. \quad (19)$$

The number of training samples required is selected based on experimentation by gradually increasing the training size until acceptable MSE values are achieved. In this case, the MSE loss function of the DNN used for the training is

$$\mathcal{L}(\xi, \hat{\xi}; \mathbf{W}_n, \boldsymbol{\theta}_n) = \frac{1}{B} \sum_{i=1}^B \|\xi - \hat{\xi}\|^2, \quad (20)$$

where B is the sample size of the current iteration.

TABLE IV: CS-MIM system simulation parameters.

Parameters	Scheme 1	Scheme 2	Scheme 3	Scheme 4	Scheme 5	Scheme 6	Scheme 7	Scheme 8	Scheme 9
Scheme type	CS-GFIM-SM	CS-JMIM	CS-GFIM-SM	CS-JMIM	CS-MIM	CS-JMIM			
Detection type	HD						SD		
Multi-carrier System	OFDM								
Number of subcarriers, N_c	128								
Cyclic prefix	16								
Num of subcarrier group, G	64		32		1,2		64		
Num of active indices/gp, K	1,2		1,2,3		1,2		2		
Receiver antennas, N_r	2		4		8		2		
RSC code, (n, k, K)							(2,1,3)		
Real Domain									
Num of subcarrier/group, N_f	2		4		8		2		
Transmit antennas, N_t	2		4		8		2		
Activated antennas, N_{at}	1	-	1	-	2				
Time Slots, T							2		
Virtual Domain									
Num of available subcarrier/group, N_v	8	4	16	8	8			4	
Transmit antennas, N_{vt}	-	4	-	8	-			2	
Time Slots, T_v							4		
STSK codeword, (m, n, t, q, l)	-				(2,2,2,2,4)		-		

A stopping criterion can be defined either by the number of iterations or by the maximum tolerable MSE threshold. Then, the parameter sets $\{\mathbf{W}_n, \boldsymbol{\theta}_n\}$ can be updated in each training iteration based on our learning algorithm using gradient descent, which is formulated as

$$\{\mathbf{W}_n, \boldsymbol{\theta}_n\} \leftarrow \{\mathbf{W}_n, \boldsymbol{\theta}_n\} - \alpha \nabla L(\{\mathbf{W}_n, \boldsymbol{\theta}_n\}),$$

where $\alpha > 0$ is the learning rate and $\nabla L(\{\mathbf{W}_n, \boldsymbol{\theta}_n\})$ represents the gradient of $L(\{\mathbf{W}_n, \boldsymbol{\theta}_n\})$. In our proposed DNN-aided detection, we use $\alpha = 0.001$.

V. SIMULATION RESULTS AND ANALYSIS

In this section, we characterize the performance of the proposed CS-JMIM system, where conventional detection will be used for benchmarking the proposed learning aided detection methods. Furthermore, we consider the system employing SF CS-JMIM and TSF CS-JMIM. The BER performance is evaluated by Monte-Carlo simulations, where we use the simulation parameters summarized in Table IV. The parameters used by the learning models are presented in Table VI. In our simulations, we assume that the receiver has perfect channel knowledge, while in practice this is estimated using channel estimation techniques.

In the following, we present the different schemes considered in our simulations for comparison purposes. Firstly, we compared CS-aided separate multi-dimensional IM with CS-JMIM. More specifically, for our SF domain system, we compared CS-aided Generalized Subcarrier Index Modulation with SM (CS-GFIM-SM). These are termed as **Scheme 1, 3**, with CS-JMIM as **Scheme 2, 4**. Then, for the TSF domain, the CS-JMIM of **Scheme 5** is compared to **Scheme 6**, which represents the CS-MIM [22] [36]. Secondly, we compared the performance of different parameters in the context of **Schemes 2, 4, 6**. Thirdly, we characterized the performance of DNN-aided CS-JMIM both in HD and SD in **Schemes 6-9**. We also quantified the complexity and compared it to conventional ML detection. Finally, we also exploited the adaptation of CS-JMIM between different JMIM methods in **Scheme 10**. To elaborate:

1) **Scheme 1**: applies ML HD detection for the CS-GFIM-SM, which activated one of 2 TAs, 2 RAs, and 2

subcarriers per group, while considering 8 subcarriers per group in the VD and $K = 1, 2$ activated subcarriers.

2) **Scheme 2**: applies maximum likelihood hard decision detection for the CS-JMIM system in the SF domain along with 2 TAs, 2 RAs, and 2 subcarriers per group in the RD, while considering 4 antennas and 4 subcarriers per group in the VD. In this scheme, we consider the following mappings:

- a) General JMIM with $K = 1, 2$.
- b) Grouped JMIM with $gs = 4$ subgroups, and each subgroup applies general JMIM in conjunction with $K = 1$ (In this case, we can consider that both the FD and SpD is split into two sub groups, which have $gsx = gsy = 2$).
- c) Coded JMIM with $n_q = 2$.

3) **Scheme 3**: applies ML HD detection for the CS-GFIM-SM, which activated one antenna out of 4 TAs, 4 RAs, and 4 subcarriers per group, while considering 16 subcarriers per group in the VD and $K = 1, 2, 3$ activated subcarriers.

4) **Scheme 4**: applies maximum likelihood hard decision detection for the CS-JMIM system in the SF domain along with 4 TAs, 4 RAs, and 4 subcarriers per group in this RD, with 8 antennas and 8 subcarriers per group in the VD. In this scheme, we consider the following mappings:

- a) General JMIM with $K = 1, 2, 3$.
- b) Grouped JMIM with $gs = 4, gsx = gsy = 2$ subgroups, with each subgroup applying the general JMIM along with $K = 1$.
- c) Coded JMIM with $n_q = 4$.

5) **Scheme 5**: applies ML HD detection for the CS-MIM system in the TSF domain with 8 TAs, 8 RAs, 2 subcarriers per group and 2 TSs, while having 8 subcarriers per group in the VD. For the Space-Time-Shift-Keying (STSK) codeword $STSK(M, N, T, Q, L)$ used in CS-MIM [22], STSK(2,2,2,2,4) is applied. In this case, we have 2 activated antennas out of 8 and $K = 1, 2$ activated subcarrier out of 8 subcarrier in the VD.

6) **Scheme 6**: applies maximum likelihood hard decision

TABLE V: Simulation results and complexity analysis of each Scheme.

Scheme index		SNR at BER of 10^{-5}	Throughput(bits/s/Hz)	Complexity
HD Detection				
Scheme 1	K=1	20.8	2.667	1.4×10^5
	K=2	26.5	4	5.6×10^5
Scheme 2	a)	K=1	30.3	9.5×10^5
		K=2	30.2	3.8×10^6
	b)	34.9	7.111	5.1×10^8
	c)	22.4	1.778	1.8×10^5
Scheme 3	K=1	16.6	1.778	8.6×10^6
	K=2	23.4	2.667	3.4×10^7
	K=3	28.1	3.778	1.4×10^8
Scheme 4	a)	K=1	8.2	1.778
		K=2	13.4	3.111
		K=3	19.4	4.667
	b)	34.6	5.333	
	c)	8.3	1.333	
Scheme 5	K=1	9.6	3.556	1.2×10^7
	K=2	13.3	5.333	4.9×10^7
Scheme 6	a)	K=1	-0.4	4.1×10^7
		K=2	4.9	6.222
	b)	15.7	17.778	
	c)	1.5	1.778	
Scheme 7	a)	5.6	3.556	2.2×10^5
	b)	18.7	17.778	1.7×10^6
	c)	1.8	1.778	6.6×10^4
SD Detection				
Scheme 8	a)	1.1	1.778	2.2×10^{13}
	b)	6.2	8.889	3.2×10^{14}
	c)	0.1	0.889	3.4×10^{12}
Scheme 9	a)	4.3	1.778	1.3×10^6
	b)	8.9	8.889	8.3×10^6
	c)	4.1	0.889	1.2×10^5
Adaptive Modulation				
Scheme 10	a)	-	-	-
	b)	-	-	5.2×10^6
	c)	-	-	1.22×10^5

TABLE VI: Training configuration for learning-aided detection method of Scheme 7,9

Setting	Hard-decision	Soft-decision
Maximum training epoch	400	1000
Initial learning rate	0.001	
Target SNR for training	0dB-20dB	-10dB to 5dB
Mini batch size	1000	200 to 500
Optimizer	Adam	
Training data size	50000	
Validation data ratio	0.1	

TABLE VII: Training configuration for adaptive modulation of Scheme 10

Setting	value
Number of Channel realizations for training	100000
Number of Channel realizations for testing	20000
Target SNR for training	0dB-30dB
Number of neighbors in KNN searchin k	15
Number of FC layers in DNN	3
Number of neurons in each FC layer	(128,256,128)
Number of output layer size	3
Activation function for output layer	Soft Max

detection for the CS-JMIM system in the TSF domain with 2 TAs, 2 RAs, 2 subcarriers per group and 2 TSs in the RD, while using 4 antennas, 4 subcarriers per group and 4 TSs in the VD. In this scheme, we consider the following mappings:

- a) General JMIM with $K = 1, 2$.
- b) Grouped JMIM with $g_s = 8, g_{sx} = g_{sy} = g_{sz} = 2$ subgroups, where each subgroup applies general JMIM along with $K = 1$. (In this case, we further split the TD into two parts, which have $g_{sz} = 2$).
- c) Coded JMIM $n_q = 2$.

7) **Scheme 7**: applies DNN based HD detection for the CS-JMIM system. Here, we consider 2 TAs, 2 RAs, 2 subcarriers per group, and 2 TSs in the RD, while using 4 antennas, 4 subcarriers per group and 4 TSs in the VD. In this scheme we consider the following mappings:

- a) General JMIM with $K = 2$.
- b) Grouped JMIM with $g_s = 8, g_{sx} = g_{sy} = g_{sz} = 2$ subgroups, where each subgroup applies general JMIM with $K = 1$.
- c) Coded JMIM with $n_q = 2$.

8) **Scheme 8**: applies conventional SD detection for the CS-JMIM system in the TSF domain, while using RSC channel coding RSC(2,1,3). Here, we consider 2 TAs, 2 RAs, 2 subcarriers per group, and 2 TSs in the RD, while using 4 antennas, 4 subcarriers per group and 4 TSs in the VD. In this scheme, we consider the following mappings:

- a) General JMIM with $K = 2$.
- b) Grouped JMIM with $g_s = 8, g_{sx} = g_{sy} = g_{sz} =$

- 882 2 subgroups, each subgroup applied general JMIM
 883 with $K = 1$.
 884 c) Coded JMIM with $n_q = 2$.
 885 9) **Scheme 9**: applies DNN-based SD detection for the CS-
 886 JMIM system in the TSF domain, while using RSC
 887 channel coding RSC(2,1,3). Here, we consider 2 TAs,
 888 2 RAs, 2 subcarriers per group, and 2 TSs in the RD,
 889 while using 4 antennas, 4 subcarriers per group and 4
 890 TSs in the VD. In this scheme, we consider the following
 891 mappings:
 892 a) General JMIM with $K = 2$.
 893 b) Grouped JMIM with $gs = 8, gsx = gsy = gsz =$
 894 2 subgroups, each subgroup applied general JMIM
 895 with $K = 1$.
 896 c) Coded JMIM with $n_q = 2$.
 897 10) **Scheme 10**: Adaptive HD-CS-JMIM system based on
 898 the TSF domain with 2 TAs, 2 RAs, 2 subcarriers per
 899 group, 2 TSs in RD and 4 antennas, 4 subcarriers per
 900 group and 4 TSs in VD. The details of the DNN based
 901 adaptive system design are shown in Table VII. In this
 902 system, we consider the following adaptation schemes:
 903 a) Conventional adaptation.
 904 b) KNN-based adaptation.
 905 c) DNN-based adaptation.

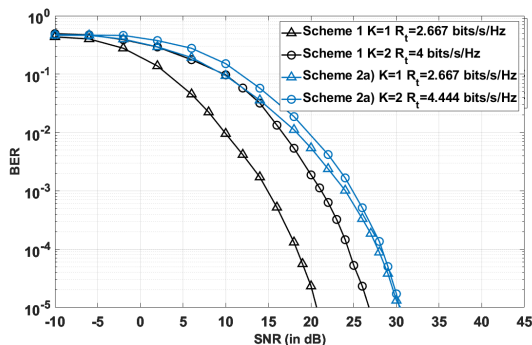


Fig. 15: BER performance comparison of Scheme 1 and Scheme 2a). Our simulation parameters are shown in Table IV.

906 As shown in Fig. 15, we compared the CS-aided separate
 907 MIM - namely the CS-GFIM-IM in this case - to CS-JMIM,

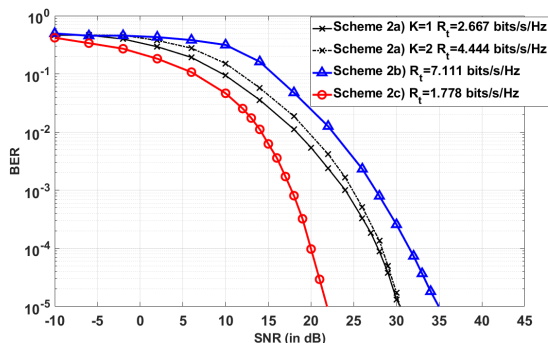


Fig. 16: BER performance comparison of CS-JMIM Scheme 2. Our simulation parameters are shown in Table IV.

908 which applied the general JMIM method of Section II-A1a).
 909 In this case, based on the transmission rate calculation formula
 910 $\frac{bG}{N_c + L_{CP}}$, we have the transmission rate of the CS-GFIM-
 911 IM associated with $K = 1$ in **Scheme 1** as $R_t^{k=1} = 2.667$
 912 bits/s/Hz. This is the same as the CS-JMIM associated with
 913 $K = 1$ in **Scheme 2a)** under identical hardware configuration.
 914 However, the performance of **Scheme 2a)** is almost 10 dB
 915 worse than that of **Scheme 1** at a BER of 10^{-5} . Hence CS-
 916 JMIM is unattractive in this situation. For more activated index
 917 entities of both CS-JMIM and CS-GFIM-IM, the throughput
 918 of **Scheme 1** is increased to $R_t^{1,k=2} = 4$ bits/s/Hz and **Scheme**
 919 **2a** has $R_t^{2,k=2} = 4.444$ bits/s/Hz. In this case, **Scheme 2a)** of
 920 $K = 2$ has a 3.6 dB better performance than **Scheme 1** of
 921 $K = 2$ at a BER of 10^{-5} .

922 Fig. 16 shows the performance of the proposed CS-JMIM
 923 **Scheme 2** for different JMIM methods. Observe that for a
 924 small index space of $N_t = N_f = 2$, the detector cannot
 925 beneficially exploit the sparsity. The transmission rate of
 926 **Scheme 2** is either $R_t^{k=1} = 2.667$ bits/s/Hz, or $R_t^{k=2} = 4.444$
 927 bits/s/Hz and we have $R_t^b = 7.111$ bits/s/Hz, $R_t^c = 1.778$
 928 bits/s/Hz. As shown in Fig. 16, **Scheme 2a)** associated with
 929 $K = 1, 2$ has a similar BER performance, while **Scheme 2a)**
 930 of $K = 2$ has a higher throughput. Additionally, **Scheme 2b)**
 931 has almost 4 times the transmission rate compared to **Scheme**
 932 **2c)**, but the latter has an increased diversity gain. Hence the
 933 BER performance of **Scheme 2c)** is 12dB better than that of
 934 **Scheme 2c)**.

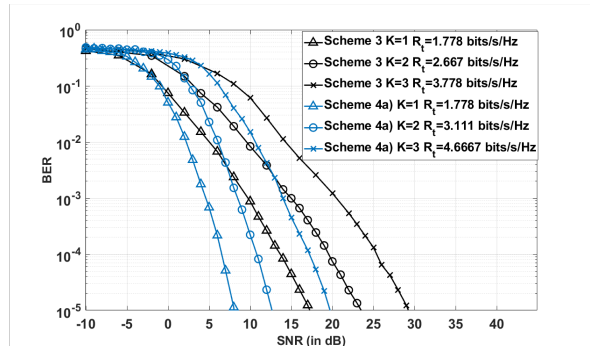


Fig. 17: BER performance comparison of Scheme 3 and Scheme 4a). Our simulation parameters are shown in Table IV.

935 To further exploit the sparsity of CS-JMIM, we also
 936 consider larger SF dimensions applied to the JMIM method, as
 937 shown in Fig. 17. We assume that both schemes have the
 938 same number of TAs and subcarriers per group along with an
 939 adjustable number of VD subcarriers. For $N_t = 4, N_f = 4$,
 940 the CS-JMIM of **Scheme 4a)** achieves better performance
 941 than the separate MIM in **Scheme 3** with the same K value.
 942 Specifically, both schemes have $R_t^{k=1} = 1.777$ bits/s/Hz and
 943 **Scheme 3** associated with $K = 1$ obtains 5 dB SNR gain over
 944 **Scheme 4a)** with $K = 1$ at BER of 10^{-5} . When relying on a
 945 higher K, CS-JMIM is capable of providing higher throughput
 946 as well as improved detection performance. With $K = 2, 3$,
 947 the throughput of **Scheme 3** is $R_t^{k=2} = 2.667$ bits/s/Hz and
 948 $R_t^{k=3} = 3.333$ bits/s/Hz, respectively, while **Scheme 4a)** could
 949 achieve $R_t^{k=2} = 3.111$ bits/s/Hz and $R_t^{k=3} = 4.667$ bits/s/Hz.

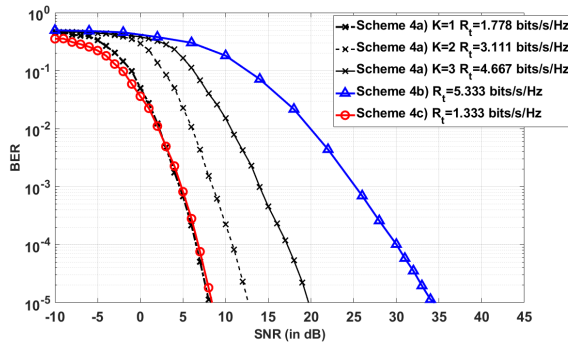


Fig. 18: BER performance comparison of CS-JMIM Scheme 4. Our simulation parameters are shown in Table IV.

950 Fig. 18 shows the BER performance of **Scheme 4**. A
 951 higher VD index mapping DM size allows for more flexible
 952 K value selection in **Scheme 4a)**. Observe that **Scheme 4a)**
 953 with $K = 1$ achieves a similar performance to **Scheme 4c)**,
 954 where **Scheme 4a)** with $K = 1$ has $R_t = 1.778$ bits/s/Hz and
 955 **Scheme 4c)** has $R_t = 1.333$ bits/s/Hz.

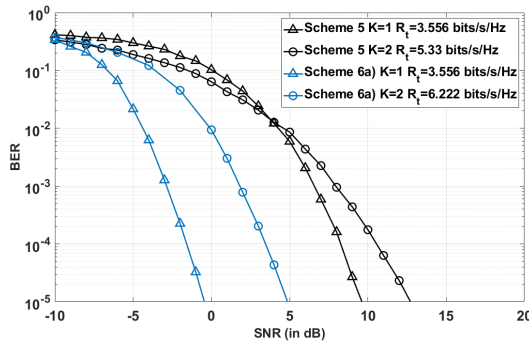


Fig. 19: BER performance comparison of Scheme 5 and Scheme 6a). Our simulation parameters are shown in Table IV.

956 For the TSF domain system of Fig.6(a), we consider a
 957 separate model termed as CS-MIM [22]. This model applied
 958 SIM and STSK in the FD and CS is applied for the FD. Then
 959 the symbol after IFFT is modulated using SM and transmitted
 960 by the activated antennas. The CS-MIM scheme is simulated
 961 using the parameters of Table IV for **Scheme 5**. In this case,
 962 to achieve the same throughput as **Scheme 5** and **Scheme 6a)**
 963 at $K = 1$, for **Scheme 5**, we deliver the signals over 8 TAs
 964 with the aid of 2 RF chains. Then both **Scheme 5** and **Scheme**
 965 **6a)** can have a throughput of $R_t^{K=1} = 3.556$ bits/s/Hz with
 966 $K = 1$. Then, we can observe in Fig.19 that **Scheme 6a)**
 967 achieves a BER of 10^{-5} at -0.1 dB while **Scheme 5** requires
 968 about 9.8 dB at the same BER. For $K = 2$, **Scheme 5** requires
 969 13.5 dB SNR at 10^{-5} BER for $R_t^{K=2} = 5.333$ bits/s/Hz and
 970 **Scheme 6a)** requires 7.5 dB lower SNR than **Scheme 5** for
 971 $R_t^{K=2} = 6.222$ bits/s/Hz.

972 In Fig. 20, the TSF domains are considered for the
 973 CS-JMIM using **Scheme 6**. As shown in Fig. 20, **Scheme**
 974 **6a)** with $K = 1$ attains the best performance among all
 975 types in **Scheme 6**. Quantitatively, at a BER of 10^{-5} ,
 976 it requires an SNR of -0.3 dB and has a throughput of

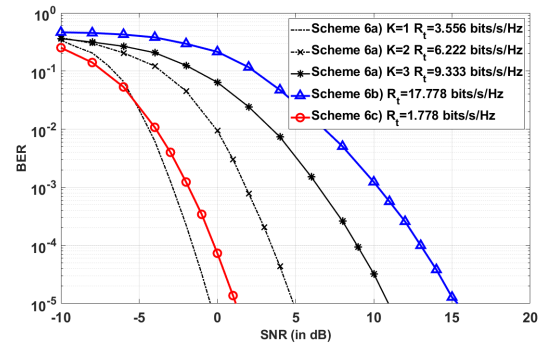


Fig. 20: BER performance comparison of CS-JMIM Scheme 6. Our simulation parameters are shown in Table IV.

$R_t = 3.556$ bits/s/Hz. **Scheme 6c)** achieves a BER of 10^{-5}
 at an SNR of 1.1 dB. When higher dimensions are introduced,
 both the general JMIM and grouped JMIM can provide a
 high throughput as well as a good BER performance, albeit
 at the cost of a huge detection complexity. In Fig. 20,
Scheme 6b) represents the grouped JMIM associated with
 8 sub-groups. When $K = 1$ and the general JMIM DM
 is applied, we have $R_t = 17.778$ bits/s/Hz. This scheme
 attains a BER of 10^{-5} at an SNR of 15.1 dB. **Scheme**
6a) with $K = 3$ has $R_t = 9.333$ bits/s/Hz and achieves
 a BER of 10^{-5} at an SNR of 11 dB. Hence, for higher
 dimensions, the grouped JMIM outperforms the other
 two JMIM methods. However, the complexity of grouped
 JMIM is exponentially increasing. Specifically, the detection
 complexity order of the grouped JMIM can be expressed as
 $\mathcal{O}[(N_{JMIM}(\mathcal{X}^K))^{N_{sub}}]$ for the TSF domain CS-JMIM system.
 This can be simplified to $\mathcal{O}[(N_v N_{vt} T_v / (g_s)) (M^K)^{N_{sub}}]$,
 where N_{sub} represents the number of sub-groups. On the
 other hand, the detection complexity order of the general
 JMIM is $\mathcal{O}[(N_v N_{vt} K T_v M^K)]$. Furthermore, the coded
 JMIM complexity order can be $\mathcal{O}[(N_q - n_q) n_q M]$. Then we
 can formulate the computational complexity order of ML
 for **Scheme 7a)** as $\mathcal{O}_{ML}[N_r N_f N_t T (N_r N_f N_t T N_{vt}^2 N_v^2 T_v^2 +$
 $N_{vt} N_v T_v M^2 N_f N_t T + MK)(N_{JMIM}(\mathcal{X}^K))]$. For
Scheme 7b), the sub-groups must be considered
 in each rounds, which have a complexity of
 $\mathcal{O}_{ML}[(N_{sub} N_r N_f N_t T / g_s) (N_r N_f N_t T N_{vt}^2 N_v^2 T_v^2 / (g_s^2) +$
 $N_{vt} N_v T_v M N_f N_t T M / g_s + MK)(N_{JMIM}(\mathcal{X}^K))^{N_{sub}}]$.
 For **Scheme 7c)**, we have a reduced complexity order of
 $\mathcal{O}_{ML}[N_r N_f N_t T N_{vt} N_v T_v M N_f N_t T M (N_q - n_q) n_q M]$
 due to having multiple bit copies. Then we can calculate the
 computational complexity based on Table IV, as shown in
 Table V.

Upon increasing the throughput excessive detection complex-
 ity is imposed by conventional ML detection. To reduce
 the detection complexity, we have to accept a performance vs.
 complexity trade-off. In this context, we compare our DNN-
 based detector of the TSF based CS-JMIM system to conven-
 tional maximum likelihood detection by comparing **Scheme 6**
 and **Scheme 7** in Fig 21. Observe that the DNN-assisted HD
 detector achieves a similar performance to the ML detector.
 Furthermore, the complexity of the NN is determined by that

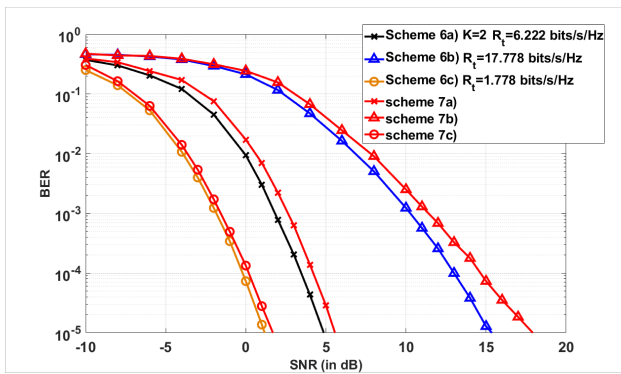


Fig. 21: BER performance comparison of CS-JMIM Scheme 6 and Scheme 7. Our simulation parameters are shown in Table IV.

1019 of the forward and backward propagation, where we have the
 1020 general DNN complexity order of $\mathcal{O}[n_i n_l n_{l+1} n_{h_L} n_o]$. Here n_i
 1021 and n_o denote the number of neurons in the input and output
 1022 layers, $n_l (l = 1, 2, \dots)$ is the number of neurons in the hidden
 1023 layer between the input and output. Then we can analyse each
 1024 DNN model in **Scheme 8**. For a classification neural network,
 1025 we have the LSTM layer as the activation layer of the input
 1026 layer, which has the complexity of $\mathcal{O}_{LSTM}[4n_l(n_d + 2 + n_l)]$,
 1027 where n_d is the number of neurons in the input layer and
 1028 the popular sigmoid function is used as the activation layer of
 1029 the output layer. The associated complexity is $\mathcal{O}[2n_L n_{L-1} -$
 1030 $n_{L-1} + 2n_{L-1}]$. The complexity of the FC layer with the
 1031 ReLu function is given by $\mathcal{O}[2n_l n_{l-1} - n_{l-1} +$
 1032 $\sum^L -1_l(2n_{l+1} n_l - n_l) + 2n_{L-1}]$. Now we can also summarize
 1033 the computational complexity of the DNN methods in Table
 1034 V.
 1035

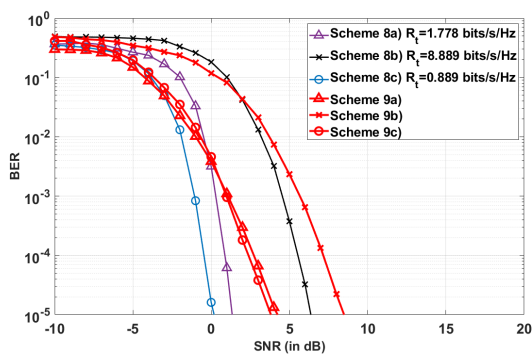


Fig. 22: BER performance comparison of CS-JMIM Scheme 8 and Scheme 9. Our simulation parameters are shown in Table IV.

1036 Furthermore, we extend the DNN-assisted detector to the
 1037 SD of the TSF domain CS-JMIM system in **Scheme 8** and
 1038 **Scheme 9**, while using the half-rate RSC encoder RSC(2,1,3),
 1039 having a memory of 3. As shown in Fig. 22, with the aid of
 1040 channel coding, the performance of CS-JMIM can be further
 1041 increased, as seen for **Scheme 8**. By comparing **Scheme 8** of

TABLE VIII: Configuration of mode used in conventional adaption with TSF domain CS-JMIM

No	Type	Scheme	R_t
1	Coded	Scheme 7a)	1.778
2	General	Scheme 7b)	6.222
3	Grouped	Scheme 7c)	17.778

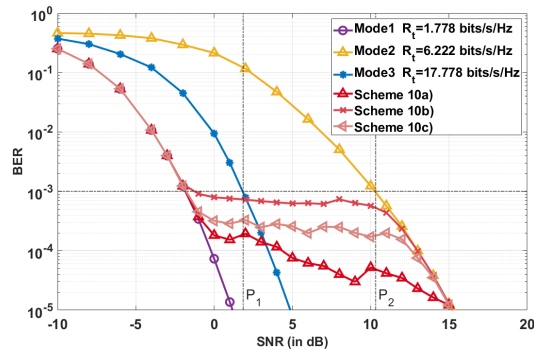


Fig. 23: Adaptive modulation performance comparison of CS-JMIM Scheme 7. Our simulation parameters are shown in Table IV.

Fig. 22 and **Scheme 6** of Fig. 21, the detection performance is 1dB better for **Scheme 8c**) than for **Scheme 6c**) at the BER of 10^{-5} . Furthermore, **Scheme 8a**) requires an SNR of 6.2 dB at BER= 10^{-5} , while **Scheme 6a**) necessitates SNR=1.6 dB. **Scheme 8b**) has the best performance, outperforming **Scheme 6b**) by about 8 dB at a BER of 10^{-5} . Fig.22 also shows the performance of DNN based detection for TSF CS-JMIM, where **Scheme 9a**) and **Scheme 9c**) exhibit similar performance. Quantitatively, they require about 4 and 3.2 dB at a BER of 10^{-5} . **Scheme 9b**) requires 3 dB higher SNR than the conventional SD detector, but it is still about 6 dB better than **Scheme 7b**). The proposed learning method has a complexity order of $\mathcal{O}[\mathcal{O}(n_i n_l) + \mathcal{O}(n_l^2) + \mathcal{O}(n_l n_o)]$ compared to $\mathcal{O}[2^{c_g} (T_v N_t N_{vt} (Q\mathcal{X})^K)]$ for the conventional scheme, where c_g denotes the RSC-coded number of bits in a transmitted symbol.

Finally, we present the performance of **Scheme 10** in

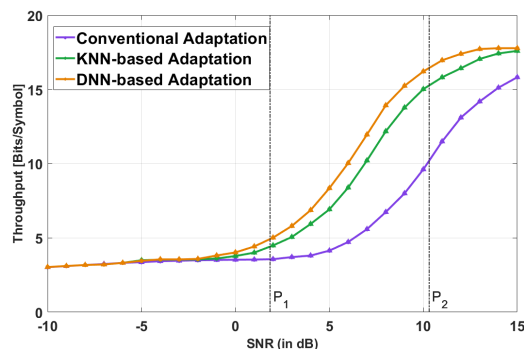


Fig. 24: Adaptive modulation performance comparison of CS-JMIM Scheme 7. Our simulation parameters are shown in Table IV.

Fig. 23. For the sake of a fair comparison, we use the data sets of the same size for both training and testing the KNN and DNN-based systems. Table VIII presents the configurations of the three modes of operation used in the adaptive system simulated. The switching thresholds for the conventional adaptive modulation are set as $P_1 = 1.85$ dB and $P_2 = 10.3$ dB, as shown in Fig. 23. Specifically, the conventional adaptive modulation scheme characterized in Fig. 23 uses $Mode_1$ when $SNR < P_1$, and $Mode_2$ for $P_2 > SNR$. After the instantaneous SNR becomes higher than P_2 , $Mode_3$ is selected. Again, our KNN-based and DNN-based mode-selection algorithms are used in Fig. 23. Observe that the DNN based adaptive system attains a BER closer to the target of 10^{-3} than the KNN based adaptive system. Then we can further analyse the throughput of each mode selection scheme in Fig. 24. Observe that the DNN-based adaptive modulation scheme achieves a higher throughput than the KNN-based one, because more accurate decisions can be made by the DNN classifier than by the KNN classifier. Clearly, the learning assisted adaptive schemes are capable of selecting the best possible mode, while the conventional adaptive modulation uses the predefined average SNR-based thresholds for mode selection.

VI. CONCLUSIONS

A CS-JMIM system was proposed and DL-aided detection using both HD and SD was conceived for reducing the detection complexity. We demonstrated that the proposed JMIM system is capable of outperforming its individual domain based counterpart, striking more flexible trade-offs between the BER performance and throughput. The learning method constructed is capable of approaching the performance of the maximum likelihood detector at a significantly reduced complexity. Furthermore, we showed that adaptive modulation can be applied for the selection of the JMIM DM design. We demonstrated that the CS-JMIM can flexibly adjust the transmission mode for accommodating time-variant channel conditions. We presented both KNN and DNN based adaptive schemes. Our simulation results showed that both the KNN and DNN-based approaches outperform the conventional threshold-based adaptive modulation. We also demonstrated that the DNN based adaptive design has a lower computational complexity and higher throughput than the KNN based approach.

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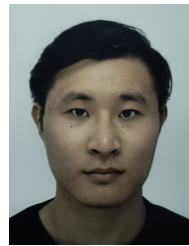
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