

Level Crossing case study - SHARCS development

1 Overview

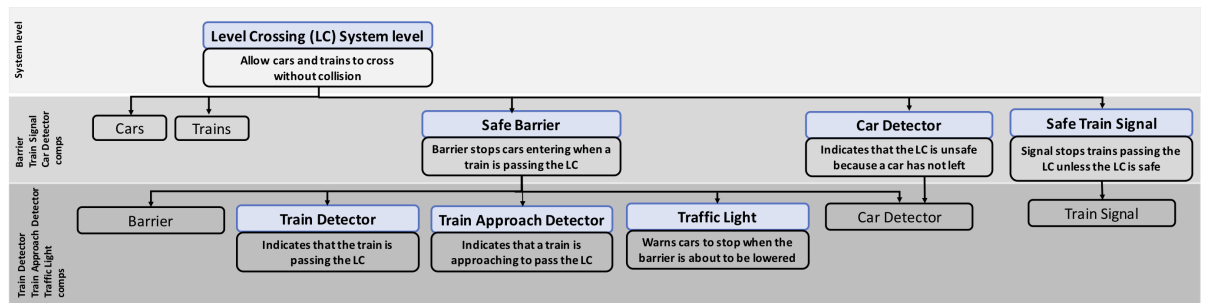


Figure 1: Level crossing: hierarchical component design, flow down requirements

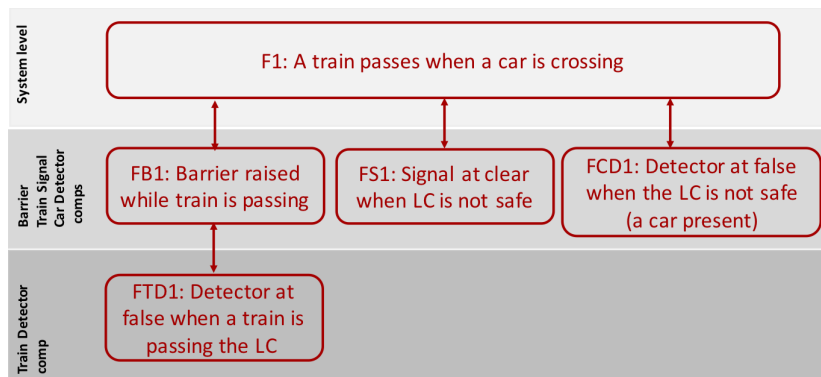


Figure 2: Level crossing: hierarchical failures

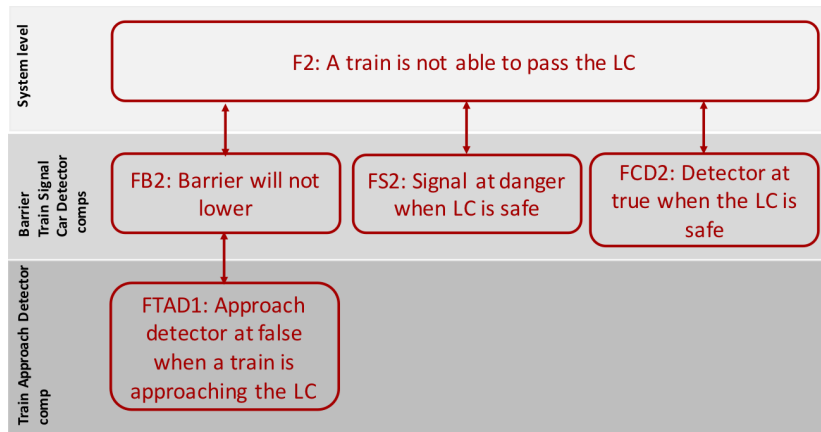


Figure 3: Level crossing: hierarchical failures

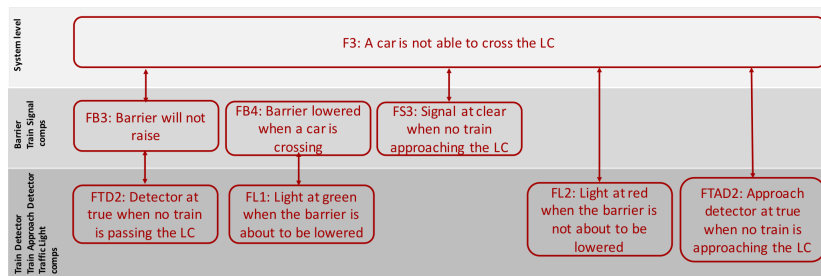


Figure 4: Level crossing: hierarchical failures

2 System Level

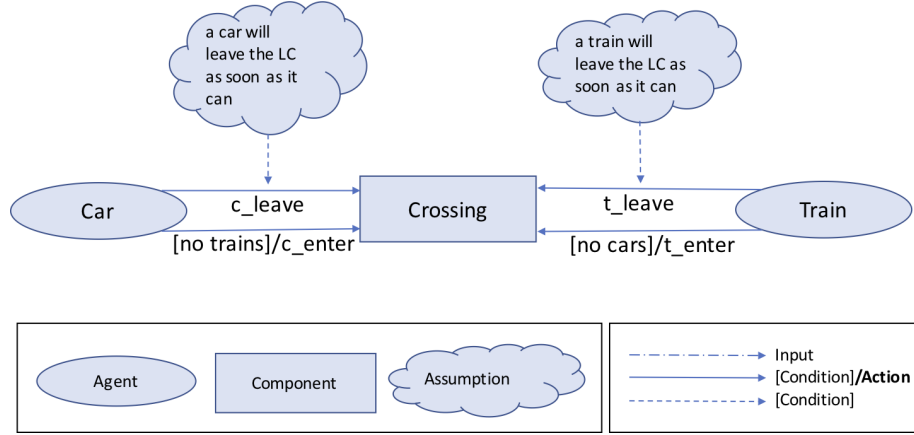


Figure 5: System level, abstraction control diagram

Level Crossing System level			
Purpose: Allow cars and trains to cross without collision.			
Actions: Trains can enter and leave the LC, Cars can enter and leave the LC.			
Failures: <ul style="list-style-type: none"> F1: A train passes when a car is crossing F2: A train is not able to pass the LC F3: A car is not able to cross the LC 			
System Action	Not Occurring Causes Failure	Occurring Causes Failure	Wrong Timing or Order Causes Failure
Train enters the LC	No failure	A12: A train enters the LC when a car is crossing (<i>F1</i>)	A13: A train enters the LC before a car finishes crossing (<i>F1</i>)
Train leaves the LC	A21: A train does not leave (<i>F3</i>)	No failure	A23: A train does not leave before a car crosses (<i>F1</i>)
Car enters the LC	No failure	A32: A car enters the LC when a train is passing (<i>F1</i>)	A33: A car enters the LC before a train finishes passing (<i>F1</i>)
Car leaves the LC	A41: A car does not leave the LC when a train passes (<i>F2</i>)	No failure	A43: A car does not leave the LC before a train passes (<i>F1</i>)
Mitigations: <ul style="list-style-type: none"> Safe Barrier component stops cars entering when a train is passing. It should stop cars from before a train starts passing until after it finishes passing (addressing <i>A23</i>, <i>A32</i>, <i>A33</i>). Safe Train Signal component stops the train when a car is passing. It should only allow the train to pass when the barriers are closed AND the crossing is clear (addressing <i>A12</i>, <i>A13</i>, <i>A43</i>). Car detector component (assists the Safe Train Signal) indicates that the LC is unsafe because a car has not left (addressing <i>A13</i>, <i>A43</i>). Assumption a train will leave the LC as soon as it can (addressing <i>A21</i>) Assumption a car will leave the LC as soon as it can (addressing <i>A41</i>) 			

Figure 6: System level, action analysis table

2.1 Event-B System Model

```
context c0
sets
  CAR // The set of cars
  TRAIN // The set of trains
end
```

```
machine m0
sees c0
variables
  cars // The set of cars in the level crossing
  trains // The set of trains in the level crossing
invariants
  theorem @typeof-cars: cars  $\subseteq$  CAR
  theorem @typeof-trains: trains  $\subseteq$  TRAIN

  // There should be no collision
  @safety: trains =  $\emptyset \vee$  cars =  $\emptyset$ 
events
  event INITIALISATION
  begin
    @init-cars: cars :=  $\emptyset$ 
    @init-trains: trains :=  $\emptyset$ 
  end

  /**
   * A car @c enters the level crossing.
   * Guards:
   * - @c is not yet in the level crossing
   * - There are no trains in the level crossing
   * Actions:
   * - @c is added to the set of cars in the level crossing.
   */
  event car_enters_LC
  any c where
    @grd1: c  $\notin$  cars
    @grd2: trains =  $\emptyset$ 
  then
    @act1: cars := cars  $\cup$  {c}
  end
```

```

/**
 * A car @c leaves the level crossing.
 * Guards:
 * - @c is in the level crossing
 * Actions:
 * - @c is removed from the set of cars in the level crossing.
 */
event car_leaves_LC
any c where
  @grd1: c ∈ cars
then
  @act1: cars := cars \ {c}
end

/**
 * A train @t enters the level crossing.
 * Guards:
 * - There are no trains in the level crossing
 * - There are no cars in the level crossing
 * Actions:
 * - @t is added to the set of trains in the level crossing.
 */
event train_enters_LC
any t where
  @grd1: t ∈ TRAIN
  @grd2: cars = ∅
then
  @act1: trains := trains ∪ {t}
end

/**
 * A train @t leaves the level crossing.
 * Guards:
 * - @t is in the level crossing
 * Actions:
 * - @t is removed from the set of trains in the level crossing.
 */
event train_leaves_LC
any t where
  @grd1: t ∈ trains
then
  @act1: trains := trains \ {t}
end

```

end

3 Safe Barrier Component

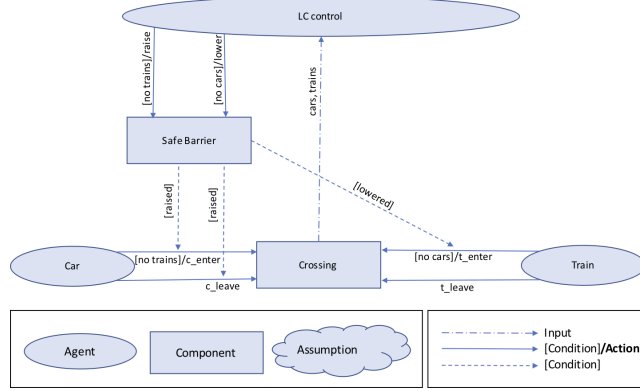


Figure 7: Safe Barrier component, abstraction control diagram

Safe Barrier			
Purpose: Barrier stops cars entering when a train is passing the LC.			
Actions: Barrier can raise and lower.			
Failures: <ul style="list-style-type: none"> • FB1: Barrier raised while train is passing (causes <i>F1</i>) • FB2: Barrier will not lower (<i>F2</i>) • FB3: Barrier will not raise (<i>F3</i>) • FB4: Barrier lowered when a car is crossing (new) 			
System Action	Not Occurring Causes Failure	Occurring Causes Failure	Wrong Timing or Order Causes Failure
Barrier raises	AB11: Barrier will not raise, when no train approaching or passing, preventing cars from crossing (<i>FB3</i>)	AB12: Barrier raises while train is passing (<i>FB1</i>)	AB13: Barrier raises before train leaves the LC (<i>FB1</i>)
Barrier lowers	AB21: Barrier will not lower, when a train approaching and no car crossing, preventing trains from passing (<i>FB2</i>)	AB22: Barrier lowers when a car is entering or leaving the LC (<i>FB4</i>)	AB23: Barrier does not lower before train enters the LC (<i>FB1</i>)
Mitigations: <ul style="list-style-type: none"> • Train detector component indicates that the train is passing the LC (<i>AB12</i>, <i>AB13</i>, <i>AB11</i>) • Train approach detector component indicates that a train is approaching to pass the LC (<i>AB21</i>, <i>AB23</i>) • Car detector component indicates that no car is crossing (addressing <i>AB21</i>). • Traffic light component warns cars to stop when the barrier is about to be lowered (<i>AB22</i>) 			

Figure 8: Barrier component, action analysis table

3.1 Event-B Safe Barrier Model

```
context c1
sets
  BARRIER
constants
  Lowered
  Raised
axioms
  @def-BARRIER: partition(BARRIER, {Lowered}, {Raised})
end
```

```
machine m1
refines m0
sees c0 c1
variables
  cars // The set of cars in the level crossing
  trains // The set of trains in the level crossing
  barriers // The status of the barriers: Lowered, Raised
invariants
  @safety-barriers_cars: barriers = Lowered  $\Rightarrow$  cars =  $\emptyset$ 
  @safety-barriers_trains: barriers = Raised  $\Rightarrow$  trains =  $\emptyset$ 
events
  event INITIALISATION extends INITIALISATION
  begin
    @init-barriers: barriers := Raised
  end

  /**
   * A car only can enter if the barriers are not Lowered
   */
  event car_enters_LC refines car_enters_LC
  any c where
    @grd1: c  $\notin$  cars
    @grd2: barriers = Raised
  then
    @act1: cars := cars  $\cup$  {c}
  end

  /**
   * A car only can leave if the barriers are not Lowered
   */
  event car_leaves_LC extends car_leaves_LC
```

```

when
  @grd2: barriers = Raised
end

/**
 * A train only can safely enters the level crossing if the barriers are
   Lowered
 */
event train_enters_LC refines train_enters_LC
any t where
  @grd1: t ∈ TRAIN
  @grd2: barriers = Lowered
then
  @act1: trains := trains ∪ {t}
end

event train_leaves_LC extends train_leaves_LC
end

/**
 * Lowering the barrier from "raised" status
 * Guards:
 * – The barriers are raised
 * Actions:
 * – The barriers are lowered
 */
event barriers_lowers
when
  @grd1: barriers = Raised
  @grd2: cars = ∅
then
  @act1: barriers := Lowered
end

/**
 * Raising the barrier from "lowered" status
 * Guards:
 * – The barriers are lowering
 * – There are no trains
 * Actions:
 * – The barriers are raised
 */
event barriers_raises

```

```
when
  @grd1: barriers = Lowered
  @grd2: trains =  $\emptyset$ 
then
  @act1: barriers := Raised
end
end
```

4 Safe Train Signal Component

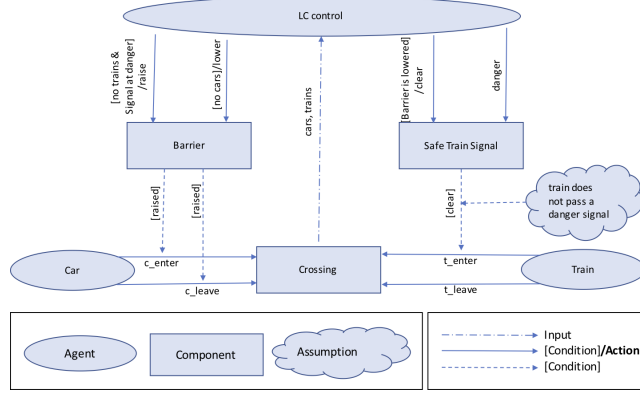


Figure 9: Safe Train Signal component, abstraction control diagram

Safe Train Signal			
Purpose: Signal stops trains passing the LC unless the LC is safe (barrier lowered).			
Actions: Signal changes to clear or to danger			
Failures: <ul style="list-style-type: none"> • FS1: Signal at clear when LC is not safe (causes F1) • FS2: Signal at danger when the LC is safe (causes F2) • FS3: Signal at clear when no train approaching the LC (causes F3) 			
System Action	Not Occurring Causes Failure	Occurring Causes Failure	Wrong Timing or Order Causes Failure
Signal changes to danger	AS11: Signal does not change to danger when LC is unsafe (FS1)	AS12: Signal changes to danger when the LC is safe (FS2)	AS13: Signal does not change to danger when no train approaching (FS3)
Signal changes to clear	AS21: Signal does not change to clear when the LC is safe (FS2)	AS22: Signal changes to clear when LC is unsafe (FS1)	AS23: Signal changes to clear when no train approaching (FS3)
Mitigations: <ul style="list-style-type: none"> • Train approach detector component indicates that a train is approaching to pass the LC (AS13, AS23) • Train signal component is verified to ensure that the signal changes to, and remains at, danger when no train is approaching or the LC is unsafe (AS13, AS23, AS11, AS22) • Train signal component is verified to ensure that the signal changes to clear when a train is approaching and the LC is safe (AS12, AS21) 			

Figure 10: Train Signal component, action analysis table

4.1 Event-B Safe Train Signal Model

```
context c2
sets
  TRAIN_SIGNAL
constants
  SIGNAL_CLEAR
  SIGNAL_DANGER
axioms
  @def- TRAIN_SIGNAL : partition (TRAIN_SIGNAL, {SIGNAL_CLEAR}, {
    SIGNAL_DANGER})
end
```

```
machine m2
refines m1
sees c0 c1 c2
variables
  cars // The set of cars in the level crossing
  trains // The set of trains in the level crossing
  barriers // The status of the barriers: Lowered, Raised
  train_signal // The train signal
invariants
  @safe_train_signal : train_signal = SIGNAL_CLEAR  $\Rightarrow$  barriers = Lowered
events
  event INITIALISATION extends INITIALISATION
  begin
    @init- train_signal : train_signal := SIGNAL_DANGER
  end

  event car_enters_LC extends car_enters_LC
  end

  event car_leaves_LC extends car_leaves_LC
  end

  /**
   * A train @t enters the level crossing.
   * Guards:
   * - There are no trains in the level crossing
   * - The train signal is "Clear"
   * Actions:
   * - @t is added to the set of trains in the level crossing.
```

```

*/
event train_enters_LC refines train_enters_LC
any t where
  @grd1: t ∈ TRAIN
  @grd2: train_signal = SIGNAL_CLEAR
then
  @act1: trains := trains ∪ {t}
end

event train_leaves_LC extends train_leaves_LC
end

event barriers_lowers extends barriers_lowers
end

/**
 * The barriers are raising only when the train signal is "Danger"
 */
event barriers_raises extends barriers_raises
when
  @grd3: train_signal = SIGNAL_DANGER
end

/**
 * Train signal set to "Clear"
 * Guards:
 * – Train signal is current "Danger"
 * – There are no cars detected
 * – The barriers are Lowered
 * Actions:
 * – Train signal is set to "Clear"
 */
event train_signal_to_clear
when
  @grd1: train_signal = SIGNAL_DANGER
  @grd2: barriers = Lowered
then
  @act1: train_signal := SIGNAL_CLEAR
end

/**
 * Train signal set to "Danger"
 * Guards:

```

```
* – Train signal is current "Clear"
* Actions:
* – Train signal is set to "Danger"
*/
event train_signal_to_danger
when
  @grd1: train_signal = SIGNAL_CLEAR
then
  @act1: train_signal := SIGNAL_DANGER
end

end
```

5 Car Detection Component

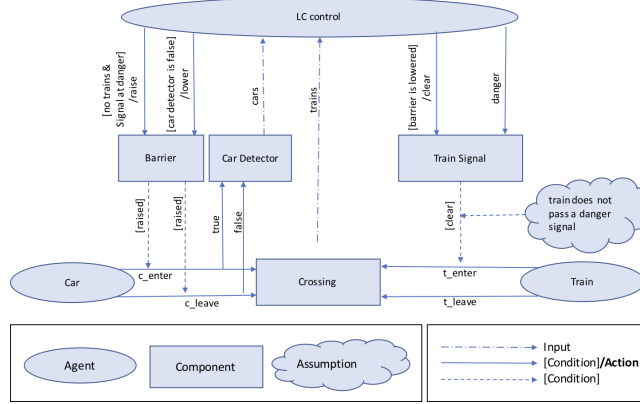


Figure 11: Car detector component, abstraction control diagram

Car Detector			
Purpose: (assists the Safe Train Signal) Indicates that the LC is unsafe because a car has not left.			
Actions: Detector changes to true or false.			
Failures:			
<ul style="list-style-type: none"> FCD1: Detector at false when the LC is not safe (a car present) (causes <i>F1</i>) FCD2: Detector at true when the LC is safe (no car present) (causes <i>F2</i>) 			
System Action	Not Occurring Causes Failure	Occurring Causes Failure	Wrong Timing or Order Causes Failure
Detector changes to true	ACD11: Detector does not change to true when LC is unsafe (<i>FCD1</i>)	ACD12: Detector changes to true when LC is safe (<i>FCD2</i>)	No failure
Detector changes to false	ACD21: Detector does not change to false when the LC is safe (<i>FCD2</i>)	ACD22: Detector changes to false pass when LC is unsafe (<i>FCD1</i>)	No failure
Mitigations:			
<ul style="list-style-type: none"> Car detector component is verified to ensure that it changes to true when the LC is not safe (a car present) (<i>ACD11</i>, <i>ACD22</i>) Car detector component is verified to ensure that it changes to false when the LC is safe (no car present) (<i>ACD12</i>, <i>ACD21</i>) 			

Figure 12: Car detector component, action analysis table

5.1 Event-B Car Detector Model

```
machine m3
refines m2
sees c0 c1 c2
variables
  cars // The set of cars in the level crossing
  trains // The set of trains in the level crossing – at most one
  barriers // The status of the barriers: Lowered, Lowering, Raising, Raised
  train_signal // The train signal
  car_detector // car detector mechanism
invariants
  // The car detector mechanism indicating whether or not there are cars
  in the level crossing
  @car_detector: car_detector = TRUE  $\Leftrightarrow$  cars  $\neq \emptyset$ 
events
  event INITIALISATION extends INITIALISATION
  begin
    @init: car_detector := FALSE
  end

  /**
   * Activate the car detector when a car enter the level crossing.
   */
  event car_enters_LC extends car_enters_LC
  begin
    @act2: car_detector := TRUE
  end

  /**
   * Set the car detector accordingly to whether or not @c is the only car in
   the level crossing
   */
  event car_leaves_LC extends car_leaves_LC
  begin
    @act2: car_detector := bool(cars  $\neq$  {c})
  end

  event train_enters_LC extends train_enters_LC
  end

  event train_leaves_LC extends train_leaves_LC
  end
```

```

/**
 * Lowering the barrier from "raised" status
 * Guards:
 * - The barriers are raised
 * - The car detector is FALSE
 * Actions:
 * - The barriers are lowered
 */
event barriers_lowers refines barriers_lowers
when
  @grd1: barriers = Raised
  @grd2: car_detector = FALSE
then
  @act1: barriers := Lowered
end

event barriers_raises extends barriers_raises
end

event train_signal_to_clear extends train_signal_to_clear
end

event train_signal_to_danger extends train_signal_to_danger
end

end

```

6 Train Detector Component

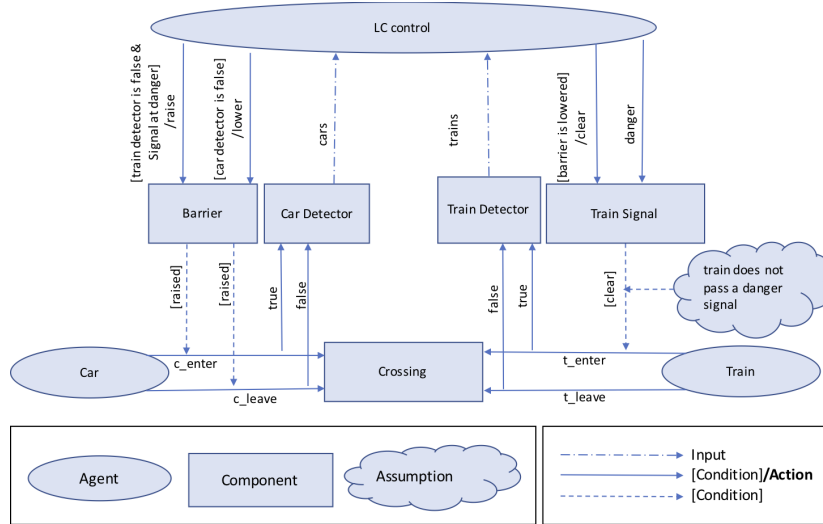


Figure 13: Train detector component, abstraction control diagram

Train Detector			
Purpose: Indicates that the train is passing the LC.			
Actions: Detector changes to true or false.			
Failures:			
<ul style="list-style-type: none"> FTD1: Detector at false when a train is passing the LC (causes <i>FB1</i>) FTD2: Detector at true when no train is passing the LC (causes <i>FB3</i>) 			
System Action	Not Occurring Causes Failure	Occurring Causes Failure	Wrong Timing or Order Causes Failure
Train detector changes to true	ATD11: Train detector does not change to true when a train is passing (<i>FTD1</i>)	ATD12: Train detector changes to true when a train is not passing (<i>FTD2</i>)	No failure
Train detector changes to false	ATD21: Train detector does not change to false when a train is not passing the LC (<i>FTD2</i>)	ATD22: Train detector changes to false when a train is passing (<i>FTD1</i>)	No failure
Mitigations:			
<ul style="list-style-type: none"> Train detector component is verified to ensure that it changes to true when a train is passing (<i>ATD11</i>, <i>ATD22</i>) Train detector component is verified to ensure that it changes to false when no train is passing (<i>ATD12</i>, <i>ATD21</i>) 			

Figure 14: Train detector component, action analysis table

6.1 Event-B Train Detector Model

```
machine m4
refines m3
sees c0 c1 c2
variables
  cars // The set of cars in the level crossing
  trains // The set of trains in the level crossing – at most one
  barriers // The status of the barriers: Lowered, Lowering, Raising, Raised
  train_signal // The train signal
  car_detector // car detector mechanism
  train_detector // train detector mechanism
invariants
  // The train detector mechanism indicating whether or not there are
  // trains in the level crossing
  @train_detector: train_detector = TRUE  $\Leftrightarrow$  trains  $\neq \emptyset$ 

events
  event INITIALISATION extends INITIALISATION
  begin
    @init: train_detector := FALSE
  end

  event car_enters_LC extends car_enters_LC
  end

  event car_leaves_LC extends car_leaves_LC
  end

  event train_enters_LC extends train_enters_LC
  begin
    @act2: train_detector := TRUE
  end

  event train_leaves_LC extends train_leaves_LC
  begin
    @act2: train_detector := bool(trains  $\neq$  {t})
  end

  event barriers_lowers extends barriers_lowers
  end

/**
 * Raising the barrier from "lowered" status
```

```

* Guards:
* - The barriers are lowered
* - The train detector is FALSE
* - The train signal is Danger
* Actions:
* - The barriers are raised
*/
event barriers_raises refines barriers_raises
when
  @grd1: barriers = Lowered
  @grd2: train_detector = FALSE
  @grd3: train_signal = SIGNAL_DANGER
then
  @act1: barriers := Raised
end

event train_signal_to_clear extends train_signal_to_clear
end

event train_signal_to_danger extends train_signal_to_danger
end

end

```

7 Train Approach Detector Component

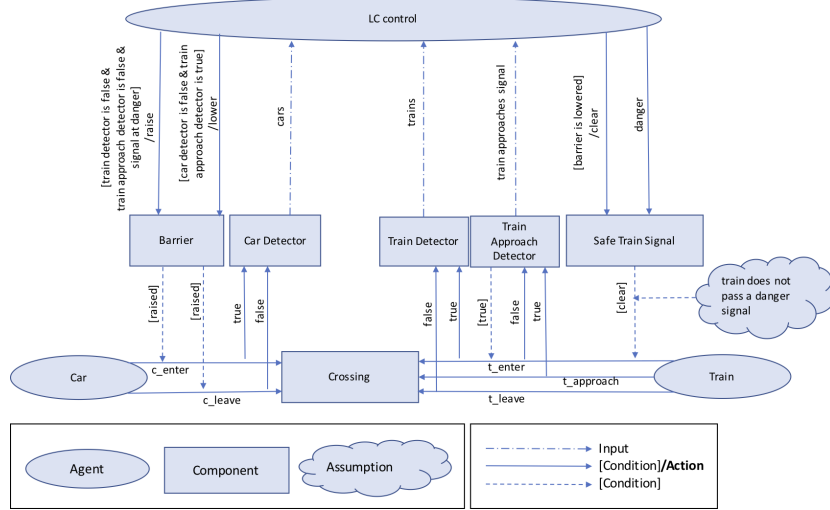


Figure 15: Train approach detector component, abstraction control diagram

Train Approach Detector			
Purpose: Indicates that a train is approaching to pass the LC.			
Actions: Approach detector changes to true or false.			
Failures: <ul style="list-style-type: none"> FTAD1: Approach detector at false when a train is approaching the LC (causes FB2) FTAD2: Approach detector at true when no train is approaching the LC (causes FS3) 			
System Action	Not Occurring Causes Failure	Occurring Causes Failure	Wrong Timing or Order Causes Failure
Train approach detector changes to true	ATAD11: Train detector does not change to true when a train is approaching (FTAD1)	ATAD12: Train detector changes to true when a train is not approaching (FTAD2)	No failure
Train approach detector changes to false	ATAD21: Train detector does not change to false when a train is not approaching the LC (FTAD2)	ATAD22: Train detector changes to false when a train is approaching (FTAD1)	No failure
Mitigations: <ul style="list-style-type: none"> Train approach detector component is verified to ensure that it changes to true when a train is approaching (ATAD11, ATAD22) Train approach detector component is verified to ensure that it changes to false when no train is approaching (ATAD12, ATAD21) 			

Figure 16: Train approach detector component, action analysis table

7.1 Event-B Train Approach Detector Model

```
machine m5
refines m4
sees c0 c1 c2
variables
  cars // The set of cars in the level crossing
  trains // The set of trains in the level crossing – at most one
  barriers // The status of the barriers: Lowered, Lowering, Raising, Raised
  train_signal // The train signal
  car_detector // car detector mechanism
  train_detector // train detector mechanism
  train_approach_detector // train approach detector mechanism
invariants
  theorem @typeof-train_approach_detector: train_approach_detector ∈
    BOOL
events
  event INITIALISATION extends INITIALISATION
  begin
    @init-train_approach_detector: train_approach_detector := FALSE
  end

  event car_enters_LC extends car_enters_LC
  end

  event car_leaves_LC extends car_leaves_LC
  end

  event train_enters_LC extends train_enters_LC
  when
    @grd3: train_approach_detector = TRUE
  then
    @act3: train_approach_detector := FALSE
  end

  event train_leaves_LC extends train_leaves_LC
  end

  event barriers_lowers extends barriers_lowers
  when
    @grd3: train_approach_detector = TRUE
  end

  event barriers_raises extends barriers_raises
```

```
when
  @grd4: train_approach_detector = FALSE
end

event train_signal_to_clear extends train_signal_to_clear
end

event train_signal_to_danger extends train_signal_to_danger
when
  @grd2: train_approach_detector = FALSE
end

event train_approaches_LC
begin
  @act1: train_approach_detector := TRUE
end

end
```

8 Traffic Light Component

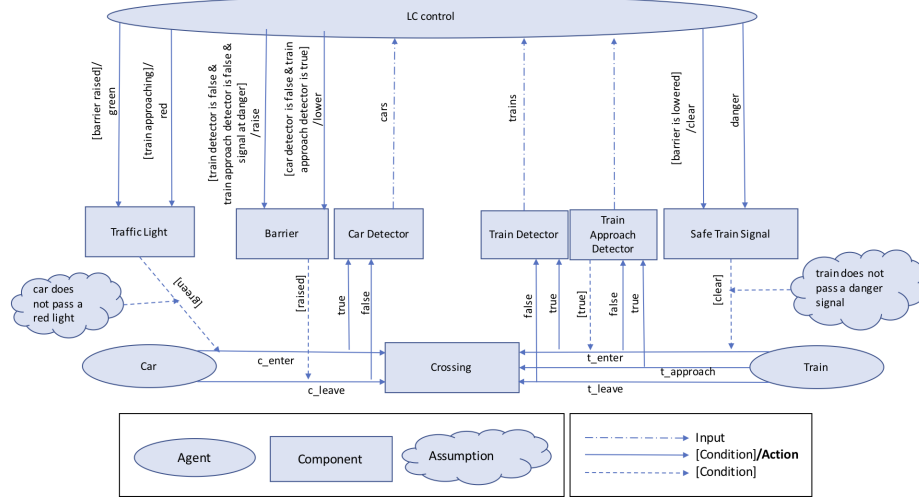


Figure 17: Traffic Light component, abstraction control diagram

Traffic Light			
Purpose: Warns cars to stop when the barrier is about to be lowered.			
Actions: Light changes to green and red.			
Failures: <ul style="list-style-type: none"> FL1: Light at green when the barrier is about to be lowered (causes FB4) FL2: Light at red when the barrier is not about to be lowered (causes F3) 			
System Action	Not Occurring Causes Failure	Occurring Causes Failure	Wrong Timing or Order Causes Failure
Light changes to Red	AS11: Light does not change to red when the barrier is about to be lowered (FL1)	AS12: Light changes to red when the barrier is not about to be lowered (FL2)	No failure
Light changes to Green	AS21: Light does not change to green when the barrier has been raised (FL2)	AS22: Light changes to green when the barrier is about to be lowered (FL1)	No failure
Mitigations: <ul style="list-style-type: none"> Traffic light component is verified to ensure that it changes to red when the barrier is about to be lowered (AS11, AS22) Traffic light component is verified to ensure that it changes to green when the barrier is raised (AS21, AS12) 			

Figure 18: Traffic Light component, action analysis table

8.1 Event-B Traffic Light Model

```
context c6
sets
  TRAFFIC_LIGHT
constants
  LIGHT_RED
  LIGHT_GREEN
axioms
  @def-TRAFFIC_LIGHT: partition(TRAFFIC_LIGHT, {LIGHT_RED}, {
    LIGHT_GREEN})
end
```

```
machine m6
refines m5
sees c0 c1 c2 c6
variables
  cars // The set of cars in the level crossing
  trains // The set of trains in the level crossing – at most one
  barriers // The status of the barriers: Lowered, Lowering, Raising, Raised
  train_signal // The train signal
  car_detector // car detector mechanism
  train_detector // train detector mechanism
  train_approach_detector // train approach detector mechanism
  traffic_light // The traffic light
invariants
  // If the traffic light is green then the barriers are not Lowered
  @safety-traffic_light_barriers: traffic_light = LIGHT_GREEN  $\Rightarrow$  barriers =
    Raised
events
  event INITIALISATION extends INITIALISATION
  begin
    @init-traffic_light: traffic_light := LIGHT_RED
  end

  event car_enters_LC refines car_enters_LC
  any c where
    @grd1:  $c \notin \text{cars}$ 
    @grd2: traffic_light = LIGHT_GREEN
  then
    @act1: cars := cars  $\cup$  {c}
    @act2: car_detector := TRUE
```

```

end

event car_leaves_LC extends car_leaves_LC
end

event train_enters_LC extends train_enters_LC
end

event train_leaves_LC extends train_leaves_LC
end

event barriers_lowers extends barriers_lowers
when
  @grd4: traffic_light = LIGHT_RED
end

event barriers_raises extends barriers_raises
end

event train_signal_to_clear extends train_signal_to_clear
end

event train_signal_to_danger extends train_signal_to_danger
end

event train_approaches_LC extends train_approaches_LC
end

event traffic_light_to_green
when
  @grd1: traffic_light = LIGHT_RED
  @grd2: barriers = Raised
then
  @act1: traffic_light := LIGHT_GREEN
end

event traffic_light_to_red
when
  @grd1: traffic_light = LIGHT_GREEN
  @grd2: train_approach_detector = TRUE
then
  @act1: traffic_light := LIGHT_RED
end
end

```