

Stochastic Geometry Based Modeling and Analysis of Uplink Cooperative Satellite-Aerial-Terrestrial Networks for Nomadic Communications With Weak Satellite Coverage

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Abstract—Cooperative satellite-aerial-terrestrial networks (CSATNs), where unmanned aerial vehicles (UAVs) are utilized as nomadic aerial relays (A), are highly valuable for many important applications, such as post-disaster urban reconstruction. In this scenario, direct communication between terrestrial terminals (T) and satellites (S) is often unavailable due to poor propagation conditions for satellite signals, and users tend to congregate in regions of finite size. There is a current dearth in the open literature regarding the uplink performance analysis of CSATN operating under the above constraints, and the few contributions on the uplink model terrestrial terminals by a Poisson point process (PPP) relying on the unrealistic assumption of an infinite area. This paper aims to fill the above research gap. First, we propose a stochastic geometry based innovative model to characterize the impact of the finite-size distribution region of terrestrial terminals in the CSATN by jointly using a binomial point process (BPP) and a type-II Matérn hard-core point process (MHCPP). Then, we analyze the relationship between the spatial distribution of the coverage areas of aerial nodes and the finite-size distribution region of terrestrial terminals, thereby deriving the distance distribution of the T-A links. Furthermore, we consider the stochastic nature of the spatial distributions of terrestrial terminals and UAVs, and conduct a thorough analysis of the coverage probability and average ergodic rate of the T-A links under Nakagami fading and the A-S links under shadowed-Rician fading. Finally, the accuracy of our theoretical derivations are confirmed by

Monte Carlo simulations. Our research offers fundamental insights into the system-level performance optimization for the realistic CSATNs involving nomadic aerial relays and terrestrial terminals confined in a finite-size region.

Index Terms—Cooperative satellite-aerial-terrestrial networks, stochastic geometry, nomadic communications, coverage probability, Nakagami fading, shadowed-Rician fading.

I. INTRODUCTION

THE sixth generation (6G) mobile communications are aiming at providing ubiquitous connectivity for human society. However, extending the current terrestrial communication infrastructure to cover the vast rural and remote areas is encountering numerous problems, particularly in poor countries [1]. In order to realize ubiquitous connectivity, satellite communication has been considered as an alternative solution due to its convenient deployment, significant adaptability, and extensive coverage [2], [3], [4]. Nevertheless, despite the advantages of employing satellites as a supplementary means of communication alongside ground-based systems, practical implementation is impeded by the considerable challenges associated with ultra-long distance transmission from satellites to the earth's surface as well as the obstructive effects of buildings and mountains that result in deep shadowing, thereby hindering direct space-to-ground communication at the data rates expected by ground users.

In order to alleviate the aforementioned challenges, satellite networks have been integrated with terrestrial networks as a viable strategy, commonly known as cooperative satellite-terrestrial networks (CSTNs) [5], [6], [7]. In CSTNs, terrestrial stations traditionally act as relays, facilitating communication between satellites and terrestrial terminals. This not only extends the coverage of satellite signals but also reduces their pathloss, thereby enhancing the quality of reception at terrestrial terminals. Nevertheless, terrestrial stations also face challenges in fulfilling space-to-ground communication requirements due to various reasons, e.g., terrain conditions. In this context, the utilization of unmanned aerial vehicles (UAVs) as aerial relays is gaining popularity due to its cost-effectiveness and adaptability. For example, in disaster-stricken areas, UAVs can quickly serve as substitutes for

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impaired terrestrial stations. Moreover, UAVs possess the capability of intelligently adapting their locations to effectively respond to unforeseen traffic requirements in the terrestrial network [8], thus achieving nomadic communication. Hence, the integration of UAVs into CSTNs, leading to the establishment of cooperative satellite-aerial-terrestrial networks (CSATNs), holds significant importance.

A. Related Works

Thus far, numerous studies have been conducted on the design and analysis of satellite networks. These studies encompass a wide range of topics including system architecture, resource management, security, and performance evaluation, all aimed at enhancing the efficiency, reliability, and/or overall performance of satellite networks. Among the existing studies, some considered the uplink performance analysis of a simpler satellite-terrestrial network, by deriving the outage probability (OP) [11], [12], [13], [14], while the others considered the downlink ergodic sum rate (ESR) [9], [10] and OP [15], [16], [17], [18] for the more complex CSATNs.

From the information theoretic perspective, ESR and OP are two main metrics for measuring network performance. Specifically, ESR assesses the network's total throughput, which corresponds to the network-level transmission efficiency, while OP assesses the network's capability to operate properly under noise and/or interference, which corresponds to the network-level transmission reliability. Therefore, it is essential to investigate the ESR and OP of CSATN systems. It should be noted that there exist other performance metrics for a network, such as end-to-end latency, network jitter, network lifetime, and so forth. However, these metrics are typically studied on the network layer, rather than on the fundamental physical layer of our interest. In [9], a switch-based hybrid FSO/millimeter wave scheme with a robust beamforming (BF) algorithm was proposed for the uplink non-orthogonal multiple access scenario, while a hybrid multiple access scheme was suggested in [10] to offer dependable connectivity for heterogeneous users in a CSATN. Yastrebova et al. [11] investigated the impact of terrestrial interference on the uplink of an LEO satellite constellation in high frequency bands of International Mobile Telecommunications (IMT), and the uplink coverage probability in hybrid satellite-terrestrial networks was analyzed in [12]. Manzoor et al. [13] modeled the data frame repetition behaviour based on the probability of a single transmission taking place on line-of-sight (LoS) links, and analyzed the coverage performance based on the frame success rate. Furthermore, Chan et al. [14] analyzed the uplink coverage probability and uplink throughput performance in massive IoT-over-satellite networks. The downlink OP of a CSATN was investigated in [15], where an optimization problem in terms of the transmit power and the transmission time over the satellite-aerial and aerial-terrestrial links is formulated and solved, to obtain the optimal end-to-end energy efficiency for the CSATN system considered. Song et al. [16] derived a closed-form expression for the OP of several types of communication links, including the uplink from the aerial source to the satellite or aerial relay, the downlink from

the satellite or aerial relay to the terrestrial destination, and the links between aerial relays. Zhang et al. [17] conducted a study on the OP of the downlink in a CSATN system that utilizes the decode-and-forward (DF) relay mechanism. Vasudha et al. [18] considered the relative velocity and the random position of receivers, and analyzed the aerial-terrestrial downlink performance by evaluating the instantaneous signal-to-noise ratio in the presence of erroneous estimation of both channel gain and noise.

We emphasize that among the above contributions, [11], [12], [13], [14] focused on analyzing the uplink performance; however, their system models only involved ground devices and satellites, without including aerial devices. Additionally, most existing studies on the performance of CSATNs focus on the downlink [15], [16], [17], [18], while the analysis of the uplink of CSATNs is lacking. In this paper we aim to fill this gap by providing a comprehensive analysis of the uplink performance of a CSATN that utilizes UAVs as relays.

In various real world scenarios, such as post-disaster urban reconstruction, it is commonly seen that users tend to congregate in finite-size areas. Understanding this fundamental property is critical for more effective network restoration or achieving more efficient network operation. However, evidently a significant gap exists in the current research landscape regarding the uplink performance analysis of CSATN systems, where the terrestrial terminals are located in finite-size areas. Existing studies often model terrestrial terminals by a Poisson point process (PPP) that relies on the assumption of an infinite distribution region [11], [12], [13], [14], which is not suitable for finite-size areas due to its boundary effects. As both the binomial point process (BPP) [19] and type-II Matérn hard-core point process (MHCPP) [20] are mathematically defined within finite regions, they are well suited for areas with spatial boundaries. This makes them particularly effective for explaining the network configuration attributes of finite-size areas. Although many studies using stochastic geometry explore finite distribution regions, they predominantly focus on terrestrial device-to-device networks [21], [22], [23], while neglecting the unique challenges posed by CSATNs. The main motivation of our work is to address this void in the research concerning CSATNs.

In addition to the aforementioned scenario modeling, the channel model also constitutes a pivotal aspect of CSATNs. The shadowed-Rician (SR) fading, distinguished from Rayleigh and Nakagami fading, has proven to be a more fitting choice for statistically characterizing satellite channels, as demonstrated in various frequency bands, e.g., S-, L-, Ku-, and Ka-band [24]. This versatility positions SR fading as a well-suited option for modeling satellite communication channels. In the existing works that focused on satellite communication using the SR fading model [25], [26], [27], [28], [29], [30], however, either the presence of interference is neglected or the channel model for interference links is studied using the Nakagami fading model. Therefore, it is evident that a comprehensive investigation into interference using the SR model is lacking. Addressing this issue is another motivation of our work.

B. Contributions and Organization of the Paper

Inspired by the insights gained from prior discoveries, this study directs its focus towards the uplink performance of CSATNs, whose terrestrial terminals are constrained in finite-size regions. Specifically, we introduce an innovative CSATN system tailored to a finite-size region and derive an expression to characterize the communication coverage of users within this finite-size area, where terrestrial terminals establish connections with satellites through the assistance of multiple aerial relays. In our exploration, we partition the uplink system into two main segments: the terrestrial terminals to aerial relays (T-A) link and the aerial relays to the satellite (A-S) link. Subsequently, we conduct an accurate analysis of each segment's performance by using Nakagami and SR fading models, respectively. This approach allows us to gain profound insights into the network's behavior, shedding light on the unique challenges and opportunities presented by the interplay of terrestrial, aerial, and satellite components in a finite-size geographical region. Our novel contributions are summarized as follows.

- We introduce a stochastic geometry based innovative model to characterize the impact of the finite-size distribution region of terrestrial terminals in the CSATN by jointly using a BPP and a type-II MHCPP. There is a current dearth in the open literature regarding the uplink performance analysis of CSATN. The limited research of using stochastic geometry in satellite communications mainly focuses on the downlink of CSTNs and uses the classical PPP to model the distribution of terrestrial nodes. However, PPP relies on the unrealistic assumption that terrestrial nodes are distributed in an infinite area. In this work, the CSATN considered comprises a satellite, multiple aerial nodes, and a set of terrestrial terminals that are located in a finite-size area. In our proposed model, terrestrial terminals are governed by a BPP, while aerial nodes adhere to a type-II MHCPP.
- We analyze the sophisticated relationship between the spatial distribution of the coverage areas of aerial nodes and the finite-size distribution region of terrestrial terminals, thereby deriving the T-A links' distance distribution, which must be obtained for further analyzing the coverage probability and the average ergodic rate. Our system model incorporates a representation of the coverage area of each aerial node, in the form of a circle that results from a 2-D projection of a cone. Although there exist studies that use stochastic geometry to analyze network performance subject to the constraint of finite node distribution region, they predominantly focus on terrestrial networks, where the unique challenges posed by CSATNs are of course not involved. Furthermore, we delineate the operational range of the aerial nodes by assessing their communication links with the terrestrial terminals.
- We consider the stochastic nature of the spatial distributions of terrestrial terminals and UAVs, and conduct a thorough analysis of both the coverage probability and the average ergodic rate of the T-A links under Nakagami fading and the A-S links under SR fading. Since there is

still a lack of interference analysis for the SR model at present, we propose a novel method for analyzing the coverage probability and the average ergodic rate of A-S links while assuming the interference imposed on the target aerial node by other aerial nodes experiences the SR fading. Specifically, we delineate the statistical properties of the received signal-to-interference-plus-noise ratio (SINR) for the T-A and A-S links based on the distance distribution function obtained. Moreover, we analyze the communication quality of the A-S links in terms of coverage probability when using the directional BF, and the benefits of this strategy are validated by subsequent simulations.

We garner a substantial volume of results to assess the performance of the CSATN considered via extensive Monte Carlo simulations, which demonstrate the correctness of our theoretical analysis. Specifically, we conduct comprehensive numerical simulations and discussions for both the T-A and A-S links. Additionally, we conduct a comparative study of the impact of key system parameters, including the coverage area of aerial nodes, the flying altitude of aerial nodes, as well as the terrestrial and aerial nodes' densities, transmission distance, and antenna gain, on the achievable system performance.

Table I summarizes the distinctions between our work and the state-of-the-art studies, which highlights the novelty of our contributions.

The remainder of this paper is organized as follows. Section II presents the network deployment, propagation models and association policy for the CSATN system. The distribution of distances within a finite-size region is provided in Section III, where we discuss the positioning relationship between the finite-size area and the coverage range of aerial nodes. Section IV presents our main performance analysis results, including the derivation of the analytical coverage probability for the T-A link and A-S link in the uplink. Section V provides the derivations of the analytical average ergodic rate for the T-A link and the A-S link, respectively. In Section VI, we provide numerical results to verify our theoretical derivations and to study the effect of key system parameters, such as network scale, array gain and transmission power, on the network performance. Our conclusions are drawn in Section VII.

Notation: $\mathbb{P}(\cdot)$ denotes the probability measure and $\mathbb{E}[\cdot]$ denotes the average measure. The Laplace transform of random variable X is defined as $\mathcal{L}_X(s) = \mathbb{E}[\exp(-sX)]$. The cumulative distribution function (CDF) and probability density function (PDF) of X are denoted by $F_X(x)$ and $f_X(x)$, respectively, while the conditional PDF of X conditioned on Y is denoted as $f_{X|Y}(x|y)$. $\Gamma(\cdot)$ is the Gamma function, and $(\cdot)_n$ is the Pochhammer symbol, which is defined as $(x)_n = \Gamma(x+n)/\Gamma(x)$. The lower incomplete Gamma function is defined as $\bar{\gamma}(a, x) = \int_0^x t^{a-1} \exp(-t) dt$. $\mathcal{B}(\mathbf{o}, R_A)$ denotes the circular plane with radius R_A centered at point \mathbf{o} . The 2-norm of $\mathbf{x} = [x_1, x_2, \dots, x_n]^T$ is defined as $\|\mathbf{x}\|_2 = \sqrt{x_1^2 + \dots + x_n^2}$. $\binom{n}{k}$ denotes the binomial coefficient. ${}_1F_1(\cdot; \cdot; \cdot)$ is the confluent hypergeometric function of the first kind.

TABLE I
COMPARISON OF EXISTING STATE-OF-THE-ARTS IN RELATED WORKS WITH OUR PROPOSED WORK

| Reference | Link types | Channel fading model of target signal | Channel fading model of interference signal | finite-size area | Beamforming | Point process |
|-------------------------------|-------------|---|---|------------------|-------------|---------------|
| Yastrebova <i>et al.</i> [11] | T-S | T-S: Rician | T-S: Rician | - | - | PPP |
| Homssi <i>et al.</i> [12] | T-BS-S | T-BS: Rayleigh BS-S: the empirical model | T-BS: Rayleigh BS-S: the empirical model | - | - | PPP |
| Manzoor <i>et al.</i> [13] | T-S | T-S: the empirical model | T-S: the empirical model | - | - | PPP |
| Chan <i>et al.</i> [14] | T-S | T-S: the empirical model | T-S: the empirical model | - | - | PPP |
| Pan <i>et al.</i> [15] | S-A-T | S-A: SR A-T: Rician | - | - | - | Single-Point |
| Song <i>et al.</i> [16] | A-S-GW | A-S: Nakagami S-GW: SR | Nakagami | - | - | MHCPP/PPP |
| Zhang <i>et al.</i> [17] | S-A-T | S-A: SR A-T: Rician | - | - | - | Single-Point |
| Vasudha <i>et al.</i> [18] | S-A-T | S-A: - A-T: Rayleigh | - | - | - | PPP |
| Kolawole <i>et al.</i> [25] | S-T BS-T | S-T: SR (Approximated as a Gamma function) | BS-T: Nakagami | - | ✓ | PPP |
| Talgat <i>et al.</i> [26] | S-GW-T | S-GW: SR GW-T: Rayleigh | - | - | - | BPP/PPP |
| Jung <i>et al.</i> [27] | S-T | SR | - | - | - | BPP |
| Our work | T-A-S | T-A: Nakagami A-S: SR | T-A: Nakagami A-S: SR | ✓ | ✓ | BPP/MHCPP |

S: satellite, A: aerial node, T: terrestrial terminal, GW: gateway, BS: base station, SR: shadowed-Rician fading. ✓: considered, -: not considered. MHCPP: Matérn hard-core point process, PPP: Poisson point process, BPP: binomial point process.

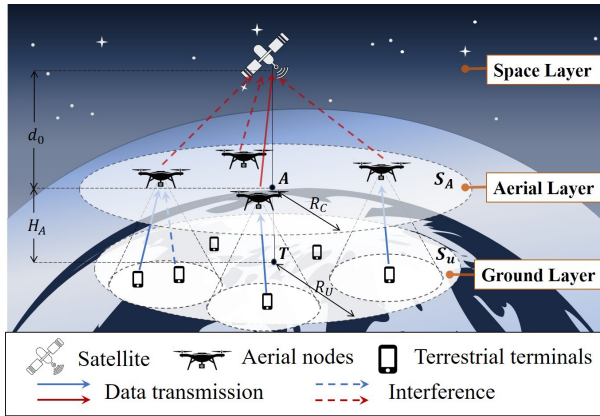


Fig. 1. Illustration of the CSATN system.

II. SYSTEM MODEL

The system model of our uplink CSATN is depicted in Fig. 1, which consists of an LEO satellite (S), a group of aerial nodes, e.g., UAVs (A_n , $n \in \{1, \dots, N_A\}$ and $N_A \geq 1$) and a number of terrestrial terminals, i.e., users, (T_l , $l \in \{1, \dots, N_0\}$ and $N_0 \geq 1$). The aerial-satellite links operate in frequency division duplex (FDD) mode to improve the communication efficiency, mitigate sophisticated interference, and simplify performance assessment.¹ In terms of the terrestrial-aerial links, since the transmission distance is much smaller than that of the aerial-satellite links, in principle both FDD and TDD can be used, depending on specific

¹In satellite communications, significant round-trip signal delay due to long signal propagation distance causes a large idle period between the pair of uplink and downlink time slots when using time division duplex (TDD), making TDD inefficient for most satellite communication systems. Currently almost all the existing satellite communication systems adopt FDD rather than TDD. In addition, time-slot overlap due to time synchronization errors may lead to sophisticated interference. By contrast, FDD can effectively mitigate these issues, though the individual bandwidths on the uplink and downlink are less abundant.

application requirements. Specifically, the signal from T_l is transmitted to S through A_n using two links, namely, the T-A link and the A-S link.

The aerial nodes serve as relays that can use any feasible relay protocol, such as amplify-and-forward (AF) and DF, while the satellite either processes the data as a space base station or as a space relay forwarding ground signals to remote ground gateways. In order to enhance spectrum utilization, the communications on the T-A links, and the communications on the A-S links, share their individual frequency bands, respectively. As a result, the received signals at A_n and S are subject to multi-user interference (MUI) caused by other terrestrial terminals and other aerial nodes, respectively. It is worth noting that the aerial nodes employ a dual-band, dual radio frequency (DRF) transmission and reception mechanism. Hence, the transmission of signals from terrestrial terminals will not cause any interference with the transmission of signals from aerial nodes to the satellite. Furthermore, it is assumed that aerial nodes in this system fly at the same height H_A above the earth surface while the satellite is located at a height of d_0 above the plane of aerial nodes.² For the sake of conciseness, we also use A or AN and T or TN to stand for aerial node and terrestrial node, respectively.

A. Topology Deployment

1) *Deployment of TNs:* We consider a realistic scenario where the majority of users are geographically concentrated within a specific finite region, such as a post-disaster gathering point. To represent this user concentration, we use a circular

²In practical applications, slight errors in the height of aerial nodes are inevitable, making it unrealistic for them to be perfectly aligned at the same altitude. However, in ultra-low altitude environments, the impact of small fluctuations in H_A on the theoretic results can be neglected. Therefore, for the sake of simplicity, we assume that the aerial nodes are positioned at the same height.

bounded area designated as \mathcal{S}_U , with radius R_U . Within this area, users are modeled as BPP denoted as Φ_1 , with density λ_T . Additionally, users located inside the coverage area of an AN are represented as Φ_U .

2) *Deployment of ANs*: We exploit type-II MHCPP to mimic the deployment of ANs. The aerial transmitters are randomly dispersed on the circular plane, denoted as \mathcal{S}_A , with radius R_C . The vertical distance from the ANs to the ground is H_A . Additionally, the coverage of each AN A on the ground can be modeled as a circular plane of radius R_A . That is, the coverage range of AN A on the ground is the circular region $\mathcal{S}'_A = \mathcal{B}(\mathbf{a}, R_A)$, which contains TNs capable of establishing connection with the AN, where \mathbf{a} is the ground projection position of A .

Next we delineate the construction of MHCPP, represented as Φ_A , utilizing a two-step approach.

Initially, candidate points are uniformly generated using a homogeneous PPP with density λ_1 within the circular space \mathcal{S}_A . With respect to the quantity of candidate points, denoted as N_c , the PDF of the Poisson distribution can be represented as $\mathbb{P}(N_c = k) = \frac{\lambda_1 \mathcal{S}_A}{k!} \exp(-\lambda_1 \mathcal{S}_A)$ where k is the number of candidate points and \mathcal{S}_A denotes the area of space \mathcal{S}_A .

Subsequently, each candidate point is assigned with an individual score, randomly selected from a uniform distribution between 0 and 1. Afterward, we selectively keep the point with the smallest score within a restricted circular space defined by the radius D_{\min} and eliminate the others. To elaborate, a given point Q initially acts as the center of a small circular repulsion space with the repulsion radius D_{\min} , i.e., $\mathcal{B}(\mathbf{q}, D_{\min})$, where \mathbf{q} is the position of Q . The concept of the repulsion space is that within this space, if there are multiple candidate nodes, some nodes need to be removed so that only a single candidate node finally remains within a circular repulsion space with a repulsion radius of D_{\min} . Specifically, if there are additional candidate points within $\mathcal{B}(\mathbf{q}, D_{\min})$, their scores are compared with that of Q , and only the point with the smallest score is retained in each repulsion space. This implies that the distance D between every two points is larger than or equal to D_{\min} .

At the end of the second step, we construct the MHCPP, denoted as Φ_A , with the density λ_A which can be mathematically represented as $\lambda_A = \frac{1 - \exp(-\pi D_{\min}^2 \lambda_1)}{\pi D_{\min}^2}$.

B. Terrestrial-Aerial Link Propagation Model

1) *Channel Fading*: The terrestrial-aerial connection commonly relies on LoS transmission [31]. In addition, terrestrial devices are often situated in outdoor environments prone to rich scattering, hence the signals from these devices to aerial nodes often propagate through multiple paths. Due to the versatility of the Nakagami fading model and the fact that it often better matches empirical data, we use it to effectively characterize the signal propagation characteristics of terrestrial-aerial links in complex environments possibly with a mixture of rich scattering and the LoS paths.³ Specifically, the small-scaling

channel fading coefficient h_{TA} of T-A link exhibits Nakagami fading. Consequently, $|h_{TA}|^2$ can be modeled as a random variable that follows a normalized Gamma distribution. The Nakagami fading parameter is denoted by N_{TA} , and for the sake of simplicity, it is assumed to be a positive integer [21].

2) *SINR Model*: The SINR at the AN receiver A of the T-A link from the target transmitter T_m can be expressed as:

$$\text{SINR}_1 = \frac{P_T |h_{T_m A}|^2 (H_A^2 + R_m^2)^{-\frac{\alpha_1}{2}}}{I_T + \sigma_T^2} \approx \frac{P_T |h_{T_m A}|^2 (H_A^2 + R_m^2)^{-\frac{\alpha_1}{2}}}{I_T}, \quad (1)$$

where the interference power

$$I_T = \sum_{T_n \in \Phi_U \setminus T_m} P_T |h_{T_n}|^2 (H_A^2 + R_n^2)^{-\frac{\alpha_1}{2}}, \quad (2)$$

$\Phi_U = \Phi_1 \cap \mathcal{B}(\mathbf{a}, R_A)$, T_n are the interfering TNs, P_T is the transmit power at TNs, R_m and R_n are the distances from the target node T_m and the interference node T_n to the terrestrial projection position \mathbf{a} of the AN A , respectively, while α_1 is the path-loss exponent of the T-A link, and σ_T^2 is the strength of additive white Gaussian noise (AWGN) of the T-A link. The approximation in (1) is due to the fact that the system is interference limited and $I_T \gg \sigma_T^2$.

C. Aerial-Satellite Link Propagation Model

1) *Directional Beamforming Modeling*: We assume that the antenna array on the satellite uses receive BF, and the antenna array on each aerial node uses transmit BF. In principle, the aerial nodes can also use receive BF, but this assumption is not mandatory herein. The physical antenna array is approximated using a sectored antenna model for simplicity. This assumption is justified because we can use specific BF algorithms and corresponding sidelobe suppression techniques to achieve a single mainlobe with a significantly higher gain than the sidelobes [32], [33]. Furthermore, since the satellite has a large coverage area, the signals transmitted by all the aerial nodes within the satellite's coverage area are assumed to be received by the satellite's mainlobe. Meanwhile, we assume that for the target aerial node, it always uses the mainlobe to transmit signals to the satellite, whilst for each interfering aerial node, whether its mainlobe or sidelobe aligns to the satellite is random. In the sectored antenna model, it is assumed that the array gain remains a constant value G for all the angles within the mainlobe, and it is a constant value g within the sidelobe.⁴

Let the overall directional BF gain from an AN A to the satellite S be G_{A-S} , G_r signify the gain of the receiver array mainlobe, and the angular width of the mainlobe of transmitter be θ . Further denote G_t and g_t as the transmitter array gains of the mainlobe and sidelobe, respectively. The target AN A_m and its serving satellite S can estimate the angles of

³The Rician and the Nakagami models behave approximately equivalently near their mean value. This observation has often been used to advocate the Nakagami model as an approximation for situations where a Rician model would be more appropriate.

⁴Although this assumption is not perfectly accurate from theoretic perspective, it is indeed a sufficiently good approximation in most practical applications, as evidenced by the technical specifications of commercial sector antenna products for cellular base stations.

departure and arrival, and then adjust their antenna steering orientations to exploit the maximum directivity gain [21]. We assume that the estimates are perfect. The value of G_{A_m-S} for the A-S link from a given target AN A_m to the satellite S is given by $D_{A_m-S} = G_t G_r$. On the other hand, for the n -th interfering link, we assume that the angle of arrival and the angle of departure of the signal are independently and uniformly distributed in the range $(0, 2\pi]$, which results in a random directivity gain denoted as D_{A_n-S} . Thus, the probability distribution for D_{A_n-S} can be expressed as:

$$G_{A_n-S} = \begin{cases} G_t G_r, & P_{\text{Mb},\text{Mb}} = \frac{\theta}{2\pi}, \\ g_t G_r, & P_{\text{Sb},\text{Mb}} = 1 - \frac{\theta}{2\pi}, \end{cases} \quad (3)$$

where $P_{tx,\text{Mb}}$ denotes the probability of the n -th A-S link in state (tx, Mb) , with $tx \in \{\text{Sb}, \text{Mb}\}$, while Sb and Mb denote the sidelobe and mainlobe.

2) *Channel Fading*: The SR fading model [34] is commonly used to analyze the performance of satellite-terrestrial links in different fixed and mobile satellite services operating in various frequency bands [35]. For the low-altitude nomadic relay UAVs in the CSATN system considered, the presence of abundant shadowing effect due to complex terrain, combined with the predominant LoS propagation path, closely aligns with the characteristics of SR fading. In our analysis, $2c$ denotes the mean power of the multipath component excluding the LoS component, and Ω denotes the mean power of the LoS component, while q is the Nakagami fading parameter. Let the small-scaling channel fading coefficient of the A-S link be h . Then the PDF of $|h|^2$ is represented as [36]:

$$f_{|h|^2}(x) = \kappa \exp(-\beta x) {}_1F_1(q; 1; \delta x), \quad (4)$$

where $\kappa = \frac{(2cq)^q}{2c(2cq+\Omega)^q}$, $\delta = \frac{\Omega}{2c(2cq+\Omega)}$, and $\beta = \frac{1}{2c}$.

3) *SINR Model*: According to the aforementioned model, the SINR at the satellite receiver S originating from the target AN A_m can be expressed as:

$$\text{SINR}_2 \approx \frac{P_m G_{A_m-S} |h_{A_m S}|^2 d_m^{-\alpha_2}}{I_A}, \quad (5)$$

where the interference power

$$I_A = \sum_{A_n \in \Phi_A \setminus A_m} P_n G_{A_n-S} |h_{A_n S}|^2 d_n^{-\alpha_2}, \quad (6)$$

A_n are interfering ANs, P_m and P_n are the transmit power of target AN A_m and interfering ANs A_n , respectively, d_m and d_n are the distances between A_m and S and between A_n and S , respectively, while α_2 is the path-loss exponent of the A-S link, and σ_A^2 is the strength of AWGN of the A-S link. Again owing to the interference limited nature, $I_A \gg \sigma_A^2$.

D. Association Policy

There is a strong repulsion among the points in the MHCPP. We set the ground coverage radius of AN R_A to half of the repulsion radius D_{\min} , i.e., $R_A = \frac{D_{\min}}{2}$. Hence, TNs can establish communication with at most one AN. We further explore an association policy where the links between TNs and ANs as well as between ANs and the satellite are randomly

established. In other words, our target transmitter is randomly selected within the communication range and the T-A link is independent of the A-S link. Therefore, meeting the following criteria indicates the user's ability to successfully establish communication with the satellite: (i) the SINR_1 for the T-A link surpasses a preset threshold denoted as T_{h_1} , and (ii) the SINR_2 for the A-S link surpasses a predefined threshold denoted as T_{h_2} . By defining $P_{\text{cov}}^{\text{T-A}} \triangleq \mathbb{P}(\text{SINR}_1 \geq T_{h_1})$ and $P_{\text{cov}}^{\text{A-S}} \triangleq \mathbb{P}(\text{SINR}_2 \geq T_{h_2})$, the coverage probability can be expressed as

$$P_{\text{cov}} = P_{\text{cov}}^{\text{T-A}} P_{\text{cov}}^{\text{A-S}}. \quad (7)$$

III. DISTRIBUTION OF DISTANCES

In order to derive the coverage probability expressions, it is necessary to firstly characterize the distance distributions arising from the stochastic geometry of the system under consideration. In particular, we present the PDF for the distribution of distances in **Lemma 1** and **Lemma 2**.

As the BPP is employed to model the user distribution, N_0 TNs are scattered independently and uniformly across the circular wireless network centered at \mathbf{u} with radius R_U . Consequently, the PDF describing the user distribution within the region $\mathcal{B}(\mathbf{u}, R_U)$ is given by

$$f(\mathbf{x}_i) = \frac{1}{\pi R_U^2}, \quad \|\mathbf{x}_i - \mathbf{u}\|_2 \leq R_U, \quad (8)$$

where \mathbf{x}_i for $i \in \{1, 2, \dots, N_0\}$ are the locations of users.

From Fig. 1, it can be seen that the coverage area of each AN is finite-size, impacting the users eligible to establish communication with an AN. Specifically, these users must be situated inside the intersecting region of \mathcal{S}'_A and \mathcal{S}_U . Given the constant vertical separation between ANs and the ground, our focus narrows down to the distribution of the distance r between the user and the AN's projection point on the ground. Let the random variable M be the distance from the projected location of an AN to the center of the user area. In this context, we can analyze the PDF of the distance r conditioned on M equal to m_0 . Based on the geometric relationships, it becomes apparent that when $M > R_A + R_U$, there will be no users within the AN's coverage range. Thus, we assume that the radius R_C of all the ANs' location area, \mathcal{S}_A , is equivalent to the sum of R_A and R_U , i.e., $R_C = R_A + R_U$.

The PDF of the distance distribution from the users to the ground projection point of an AN can be categorized into two scenarios based on the relative spatial relationship between the coverage range of the AN, \mathcal{S}'_A , and the user area, \mathcal{S}_U . These two scenarios are illustrated in Fig. 2. The first scenario arises when the complete area of \mathcal{S}'_A is entirely within \mathcal{S}_U , while the second scenario occurs when these two areas have a partial intersection. Further details can be found in Appendix A.

Lemma 1: The PDF describing the distance r between a given TN and the projected location of the AN within the overlapping area of $\mathcal{S}'_A \cap \mathcal{S}_U$, conditioned on $M = m_0$,

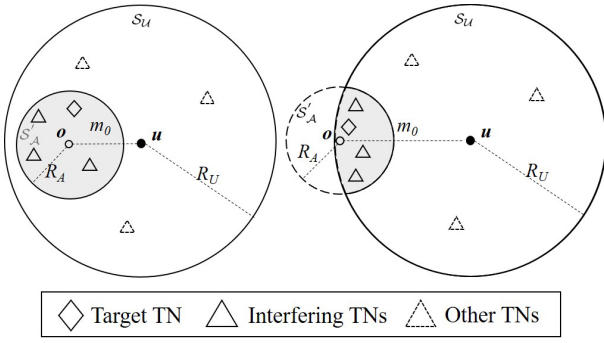


Fig. 2. The positional relationship between S'_A and S_U , where o is the ground projection position of the AN considered.

is expressed as:

$$f_R(r|m_0) = \begin{cases} f_{R^{(1)}}(r|m_0) = \frac{2r}{R_A^2}, & 0 < r < R_A \text{ and} \\ & 0 < m_0 < R_U - R_A, \\ f_{R^{(2)}}(r|m_0) = \frac{2\pi r}{\gamma}, & 0 < r < R_U - m_0 \text{ and} \\ & R_U - R_A < m_0 < R_U, \\ f_{R^{(3)}}(r|m_0), & R_U - m_0 < r < R_A \text{ and} \\ & R_U - R_A < m_0 < R_U, \\ f_{R^{(3)}}(r|m_0), & m_0 - R_U < r < R_A \text{ and} \\ & R_U < m_0 < R_U + R_A, \end{cases} \quad (9)$$

where $f_{R^{(3)}}(r|m_0)$ is given in (10), as shown at the bottom of the page,

$$\gamma = R_U^2 \left(\theta_2 - \frac{1}{2} \sin(2\theta_2) \right) + R_A^2 \left(\varphi_2 - \frac{1}{2} \sin(2\varphi_2) \right), \quad (11)$$

$$\theta_2 = \arccos \left(\frac{m_0 + R_U^2 - R_A^2}{2m_0 R_U} \right), \quad (12)$$

$$\varphi_2 = \arccos \left(\frac{m_0 + R_A^2 - R_U^2}{2m_0 R_A} \right), \quad (13)$$

$$\varphi_3 = \arccos \left(\frac{m_0^2 - R_U^2 + r^2}{2m_0 r} \right). \quad (14)$$

Proof: See Appendix A. \square

Remark 1: Due to the independent and uniform distribution of TNs within the overlapping area, it can be observed that when the distance between the projection point and the center of the user area is $M = m_0$, the distance variables r_m and r_n for the target TN and interference TNs are independently and identically distributed. Specifically, this can be expressed as $f_{R_m}(r_m|m_0) = f_{R_n}(r_n|m_0) = f_R(r|m_0)$.

Lemma 2: The PDF of the distance M from the projection point of the AN to the center of the user area is given by

$$f_M(m_0) = \frac{2m_0}{(R_A + R_U)^2}, \quad 0 < m_0 < R_A + R_U. \quad (15)$$

Proof: Considering that the movement range of the projection point is within $\mathcal{B}(u, R_U)$, the range of the distance m_0 from the projection point to the center of the user area S_U is $0 < m_0 < R_U + R_A$. Thus the CDF of M can be expressed as

$$F_M(m_0) = \frac{m_0^2}{(R_A + R_U)^2}, \quad 0 < m_0 < R_A + R_U. \quad (16)$$

The corresponding PDF can be derived by differentiating (16) with respect to m_0 . This completes the proof. \square

IV. COVERAGE PROBABILITY

In this section, we conduct an analysis on the coverage probabilities for both the T-A link and A-S link, assuming that at least one user is in S'_A . The coverage probability refers to the likelihood that the SINR at the receiver is larger than the minimum SINR threshold necessary for successful data transmission. In other words, if the SINR of the signal at a receiver surpasses a pre-established threshold, the transmitter is deemed to be inside the coverage area of the receiver's communication network.

A. T-A Link

Theorem 1: The coverage probability of a TN communicating with an AN within the coverage range of the AN under the Nakagami fading channel is given by

$$\begin{aligned} P_{\text{cov}}^{\text{T-A}} &\triangleq \mathbb{P}(\text{SINR}_1 \geq T_{h_1}) \\ &= \int \int \sum_{n=1}^{N_{\text{TA}}} (-1)^{n+1} \binom{N_{\text{TA}}}{n} \mathbb{E}_I [\exp(-sI_T)] \\ &\quad \times f_{R_m}(r_m|m_0) f_M(m_0) dr_m dm_0, \end{aligned} \quad (17)$$

where T_{h_1} is the SINR threshold of the T-A link,

$$\mathbb{E}_I [\exp(-sI_T)] = \mathcal{L}_{I_T}(s), \quad (18)$$

is the Laplace transform of the cumulative interference power I_T , $s = \frac{n\eta T_{h_1} (H_A^2 + r_m^2)^{\frac{\alpha_1}{2}}}{P_T}$ with $\eta = N_{\text{TA}}(N_{\text{TA}}!)^{-\frac{1}{N_{\text{TA}}}}$, and N_{TA} is Nakagami fading parameter.

Proof: See Appendix B. \square

Lemma 3: Laplace transform of random variable I_T is

$$\mathcal{L}_{I_T}(s) = \mathbb{E}_{N_I, R_n} \left[\prod_{T_n \in \Phi_U \setminus T_m} \underbrace{\left(1 + \frac{sP_T}{N_{\text{TA}}(H_A^2 + r_n^2)^{\frac{\alpha_1}{2}}} \right)^{-N_{\text{TA}}}}_{D_2} \right], \quad (19)$$

$$\begin{aligned} f_{R^{(3)}}(r|m_0) &= \frac{r \sqrt{4m_0^2 R_U^2 - (m_0 + R_U^2 - r^2)^2}}{m_0^2} + 2r \left(\varphi_3 - \frac{1}{2} \sin(2\varphi_3) \right) \\ &\quad + \frac{(m_0^2 + R_U^2 - r^2) \sqrt{2R_U^2(m_0 + r^2) - R_U^4 - (m_0^2 - r^2)^2}}{2m_0^2 r}. \end{aligned} \quad (10)$$

where the expectation is over the number of interference users N_I and the interfering users' distances R_n .

Proof: See Appendix C. \square

The point distribution of the interference users can be described by a BPP. Therefore, the number of interference users N_I follows a binomial distribution with a certain probability of success. The probability of success can be expressed as

$$P_I = \begin{cases} P_{I_1} = \frac{R_A^2}{R_U^2}, & 0 < m_0 < R_U - R_A, \\ P_{I_2} = \frac{\gamma}{R_U^2}, & R_U - R_A < m_0 < R_U + R_A, \end{cases} \quad (20)$$

where γ is given in (11). Noting the PDF $f_R(r_n|m_0)$ (9), we obtain the three expressions of $\mathcal{L}_{I_T}(s)$ in the three different ranges of $0 < m_0 < R_U - R_A$, $R_U - R_A < m_0 < R_U$ and $R_U < m_0 < R_U + R_A$, which are given in (21), as shown at the bottom of the page, where N_0 is the total number of users,

$D_1 = f_{R^3}(r_n|m_0)$, and $D_2 = \left(1 + \frac{sP_T}{N_{TA}(H_A^2 + r_n^2)^{\frac{\alpha_T}{2}}}\right)^{-N_{TA}}$.

$\mathcal{L}_{I_1}(s)$ for $0 < m_0 < R_U - R_A$ is derived as follows:

$$\begin{aligned} \mathcal{L}_{I_1}(s) &= \sum_{n_I=1}^{N_0-1} \binom{N_0-1}{n_I} (P_{I_1})^{n_I} \left(\int_0^{R_A} D_2 f_{R^1}(r_n|m_0) dr_n \right)^{n_I} \\ &\quad \times (1 - P_{I_1})^{N_0-1-n_I} \\ &= \sum_{n_I=1}^{N_0-1} \binom{N_0-1}{n_I} \frac{R_A^{2n_I} (R_U^2 - R_A^2)^{N_0-1-n_I}}{R_U^{2(n_I+1)}} \\ &\quad \times \left(\int_0^{R_A} D_2 \frac{2r_n}{R_A^2} dr_n \right)^{n_I}. \end{aligned} \quad (22)$$

$\mathcal{L}_{I_2}(s)$ for $R_U - R_A < m_0 < R_U$ is derived as follows:

$$\begin{aligned} \mathcal{L}_{I_2}(s) &= \sum_{n_I=1}^{N_0-1} \binom{N_0-1}{n_I} (P_{I_2})^{n_I} \left(\int_0^{R_U-m_0} D_2 f_{R_2}(r_n|m_0) dr_n \right. \\ &\quad \left. + \int_{R_U-m_0}^{R_A} D_2 f_{R_3}(r_n|m_0) dr_n \right)^{n_I} (1 - P_{I_2})^{N_0-1-n_I} \\ &= \sum_{n_I=1}^{N_0-1} \binom{N_0-1}{n_I} \frac{\gamma^{n_I} (R_U^2 - \gamma)^{N_0-1-n_I}}{R_U^{2(n_I+1)}} \end{aligned}$$

$$\times \left(\int_{R_U-m_0}^{R_A} D_2 \frac{2\pi r}{\gamma} dr_n + \int_{R_U-m_0}^{R_A} D_1 D_2 dr_n \right)^{n_I}. \quad (23)$$

$\mathcal{L}_{I_3}(s)$ for $R_U < m_0 < R_U + R_A$ is derived as follows:

$$\begin{aligned} \mathcal{L}_{I_3}(s) &= \sum_{n_I=1}^{N_0-1} \binom{N_0-1}{n_I} (P_{I_2})^{n_I} \left(\int_{m_0-R_U}^{R_A} D_2 f_{R_4}(r_n|m_0) dr_n \right)^{n_I} \\ &\quad \times (1 - P_{I_2})^{N_0-1-n_I} \\ &= \sum_{n_I=1}^{N_0-1} \binom{N_0-1}{n_I} \frac{\gamma^{n_I} (R_U^2 - \gamma)^{N_0-1-n_I}}{R_U^{2(n_I+1)}} \\ &\quad \times \left(\int_{m_0-R_U}^{R_A} D_1 D_2 dr_n \right)^{n_I}. \end{aligned} \quad (24)$$

By substituting (9), (15) and (21) into (17), we obtain the coverage probability $P_{\text{cov}}^{\text{T-A}}$ of the terrestrial-aerial link given in (25) as shown at the bottom of the next page.

B. A-S Link

The target transmitter A_m has the transmit power P_m , while the power level for other A_n in Φ_A is P_n .

Theorem 2: The coverage probability for an arbitrarily located AN under the SR fading channel is given by

$$\begin{aligned} P_{\text{cov}}^{\text{A-S}} &\triangleq \mathbb{P}(\text{SINR}_2 \geq T_{h_2}) \\ &= 1 - \sum_{k=0}^{\infty} \frac{\Psi(k)}{(\beta - \delta)^{k+1}} \Gamma(k+1) \sum_{t=0}^{k+1} \binom{k+1}{t} \\ &\quad \times (-1)^t \mathbb{E}[\exp(-s' I_A)], \end{aligned} \quad (26)$$

where $\Psi(k) = \frac{(-1)^k \kappa \delta^k}{(k!)^2} (1 - q)_k$, $s' = \frac{t\zeta(\beta - \delta) T_{h_2} d_m^{\alpha_2}}{P_m G_{A_m-S}}$, $\zeta = (\Gamma(k+2))^{-\frac{1}{k+1}}$, and q is Nakagami fading parameter of the SR fading model.

Proof: See Appendix D. \square

To simplify the expression of $P_{\text{cov}}^{\text{A-S}}$, we first note that the expectation of $\mathbb{E}[\exp(-s' I_A)]$ is over the the distance d_m between A_m and S as well as the interference, i.e.,

$$\mathbb{E}[\exp(-s' I_A)] = \mathbb{E}_{d_m, I}[\exp(-s' I_A)]. \quad (27)$$

Compared with the finite-size operational range of ANs, typically spanning only a few kilometers, the spatial separation between the satellite and ANs is considerably larger, extending to hundreds even thousands of kilometers. Hence, the distance

$$\mathcal{L}_{I_T}(s) = \begin{cases} \mathcal{L}_{I_1}(s) = \sum_{n_I=1}^{N_0-1} \binom{N_0-1}{n_I} \frac{R_A^{2n_I} (R_U^2 - R_A^2)^{N_0-1-n_I}}{R_U^{2(n_I+1)}} \left(\int_0^{R_A} D_2 \frac{2r_n}{R_A^2} dr_n \right)^{n_I}, & 0 < m_0 < R_U - R_A, \\ \mathcal{L}_{I_2}(s) = \sum_{n_I=1}^{N_0-1} \binom{N_0-1}{n_I} \frac{\gamma^{n_I} (R_U^2 - \gamma)^{N_0-1-n_I}}{R_U^{2(n_I+1)}} \\ \quad \times \left(\int_{R_U-m_0}^{R_A} D_2 \frac{2\pi r}{\gamma} dr_n + \int_{R_U-m_0}^{R_A} D_1 D_2 dr_n \right)^{n_I}, & R_U - R_A < m_0 < R_U, \\ \mathcal{L}_{I_3}(s) = \sum_{n_I=1}^{N_0-1} \binom{N_0-1}{n_I} \frac{\gamma^{n_I} (R_U^2 - \gamma)^{N_0-1-n_I}}{R_U^{2(n_I+1)}} \left(\int_{m_0-R_U}^{R_A} D_1 D_2 dr_n \right)^{n_I}, & R_U < m_0 < R_U + R_A. \end{cases} \quad (21)$$

disparity between the satellite and ANs is negligible. Therefore, it is postulated that all of the aerial transmitters possess an equal transmission distance to S , i.e., $d_m = d_0$. Since d_m is approximately a constant, (27) depends on the interference only. Consequently, we have

$$\mathbb{E}[\exp(-s' I_A)] = \mathcal{L}_{I_A}(s'), \quad (28)$$

that is, $\mathbb{E}[\exp(-s' I_A)]$ is the Laplace transform of the cumulative interference power I_A .

Lemma 4: Laplace transform of random variable I_A is

$$\mathcal{L}_{I_A}(s') = \exp(\lambda_A S_A (M_2 - 1)), \quad (29)$$

where $\lambda_A = \frac{1 - \exp(-\pi D_{\min}^2 \lambda_1)}{\pi D_{\min}^2}$, $S_A = \pi R_C^2$, and $M_2 = M_1(t_1) \frac{\theta}{2\pi} + M_1(t_2) (1 - \frac{\theta}{2\pi})$ with $M_1(t_l) = \frac{(2cq)^q (1 + 2ct_l)^{q-1}}{[(2cq + \Omega)(1 + 2ct_l) - \Omega]^q}$, $l \in \{1, 2\}$, $t_1 = s' P_n d_0^{-\alpha_2} G_t G_r$ and $t_2 = s' P_n d_0^{-\alpha_2} g_t G_r$.

Proof: See Appendix E. \square

By inserting (28) and (29) into (26), we obtain the closed-form analytical expression of $P_{\text{cov}}^{\text{A-S}}$ for the A-S link in (30), as shown at the bottom of the page.

V. AVERAGE ERGODIC RATE

The average achievable ergodic rate, also known as the Shannon throughput, is measured in bits per second per Hertz (bits/s/Hz). It represents the mean data rate that can be achieved by a communication system using a normalized

frequency resource of 1 Hz. This metric also corresponds to the ergodic capacity of a fading communication link, normalized to a unit bandwidth. Formally, the average ergodic rate is defined as

$$\bar{C} \triangleq \frac{1}{K} \mathbb{E}[\log_2(1 + \text{SINR})]. \quad (31)$$

A. T-A Link

Theorem 3: Under a Nakagami fading channel, the average rate of any arbitrary terrestrial node is given by

$$\bar{C}^{\text{T-A}} = \frac{1}{K} \int \int \int_{t>0} \sum_{n=1}^{N_{\text{TA}}} (-1)^{n+1} \binom{N_{\text{TA}}}{n} \mathbb{E}_{I_{\text{T}}}[\exp(-s_1 I_{\text{T}})] \times f_{R_m}(r_m | m_0) f_M(m_0) dt dr_m dm_0, \quad (32)$$

where $s_1 = \frac{n\eta(2^t - 1)}{P_{\text{T}}(H_{\text{A}}^2 + r_m^2)^{-\frac{\alpha_1}{2}}}$, $\mathbb{E}_{I_{\text{T}}}[\exp(-s_1 I_{\text{T}})]$ is obtained by replacing s in $\mathcal{L}_{I_{\text{T}}}(s)$ of (19) with s_1 , $f_{R_m}(r_m | m_0)$ is shown as (9), and $f_M(m_0)$ is shown as (15).

Proof: See Appendix F. \square

B. A-S Link

Theorem 4: Under an SR fading channel, the average rate of any arbitrary aerial node is given by

$$\bar{C}^{\text{A-S}} = \frac{1}{K} \int_{t>0} \left(1 - \sum_{k=0}^{\infty} \frac{\Psi(k)}{(\beta - \delta)^{k+1}} \Gamma(k+1) \sum_{v=0}^{k+1} \binom{k+1}{v} \right)$$

$$\begin{aligned} P_{\text{cov}}^{\text{T-A}} &= \int \int \sum_{n=1}^{N_{\text{TA}}} (-1)^{n+1} \binom{N_{\text{TA}}}{n} \mathcal{L}_{I_{\text{T}}}(s) f_{R_m}(r_m | m_0) f_M(m_0) dr_m dm_0 \\ &= \int_0^{R_U - R_A} \int_0^{R_A} \sum_{n=1}^{N_{\text{TA}}} (-1)^{n+1} \binom{N_{\text{TA}}}{n} \mathcal{L}_{I_1}(s) f_{R^1}(r_m | m_0) f_M(m_0) dr_m dm_0 \\ &\quad + \int_{R_U - R_A}^{R_U} \left(\int_0^{R_U - m_0} \sum_{n=1}^{N_{\text{TA}}} (-1)^{n+1} \binom{N_{\text{TA}}}{n} \mathcal{L}_{I_2}(s) f_{R^2}(r_m | m_0) dr_m \right. \\ &\quad \left. + \int_{R_U - m_0}^{R_A} \sum_{n=1}^{N_{\text{TA}}} (-1)^{n+1} \binom{N_{\text{TA}}}{n} \mathcal{L}_{I_2}(s) f_{R^3}(r_m | m_0) dr_m \right) f_M(m_0) dm_0 \\ &\quad + \int_{R_U}^{R_U + R_A} \int_{m_0 - R_0}^{R_A} \sum_{n=1}^{N_{\text{TA}}} (-1)^{n+1} \binom{N_{\text{TA}}}{n} \mathcal{L}_{I_3}(s) f_{R^3}(r_m | m_0) f_M(m_0) dr_m dm_0. \end{aligned} \quad (25)$$

$$\begin{aligned} P_{\text{cov}}^{\text{A-S}} &= 1 - \sum_{k=0}^{\infty} \frac{\Psi(k)}{(\beta - \delta)^{k+1}} \Gamma(k+1) \sum_{t=0}^{k+1} \binom{k+1}{t} (-1)^t \exp(\lambda_A S_A (M_2 - 1)) \\ &= 1 - \sum_{k=0}^{\infty} \frac{(-1)^k \kappa \delta^k (1 - q)_k}{k! (\beta - \delta)^{k+1}} \sum_{t=0}^{k+1} \binom{k+1}{t} (-1)^t \\ &\quad \times \exp \left(\frac{\pi (R_U + R_A)^2 (1 - \exp(-\pi D_{\min}^2 \lambda_1))}{\pi D_{\min}^2} \left(\frac{(2cq)^q (1 + \frac{2tc P_n G_t G_r \zeta(\beta - \delta) T_{h_2}}{P_m G_{A_m-S}})^{q-1}}{((2cq + \Omega)(1 + \frac{2tc P_n G_t G_r \zeta(\beta - \delta) T_{h_2}}{P_m G_{A_m-S}}) - \Omega)^q} \frac{\theta}{2\pi} \right. \right. \\ &\quad \left. \left. + \frac{(2cq)^q (1 + \frac{2tc P_n g_t G_r \zeta(\beta - \delta) T_{h_2}}{P_m G_{A_m-S}})^{q-1}}{((2cq + \Omega)(1 + \frac{2tc P_n g_t G_r \zeta(\beta - \delta) T_{h_2}}{P_m G_{A_m-S}}) - \Omega)^q} \left(1 - \frac{\theta}{2\pi} \right) - 1 \right) \right). \end{aligned} \quad (30)$$

TABLE II
DEFAULT SIMULATION SYSTEM PARAMETERS

| Notation | Parameters | Values |
|----------------------|---|--------------------|
| H_A | Height of ANs | 0.05 km |
| d_0 | Distance between ANs and the satellite | 400 km |
| R_U, R_A | Radius of S_U and S_A' | 9.5 km, 0.5 km |
| D_{\min} | Minimum distance between every two candidate points | 1 km |
| P_T, P_A | Power of transmitters in TN and AN | 20 dBw, 20 dBw |
| G_t, g_t | Antenna gains of the main and side lobes | 10 dB, -10 dB |
| λ_T | Density of terrestrial nodes | 10^{-4} |
| λ_1 | Density of candidate points | 5×10^{-7} |
| N_{TA} | Nakagami fading parameter | 3 |
| (c, q, Ω) | SR fading model | (0.158, 1, 0.1) |
| α_1, α_2 | Path-loss exponents of T-A and A-S link | 2, 2 |
| T_{h1} | SINR threshold of the T-A link | variable |
| T_{h2} | SINR threshold of the A-S link | -20 dB |

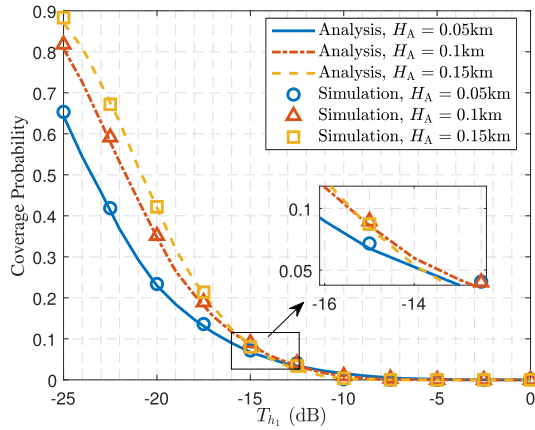


Fig. 3. Coverage probability of the terrestrial-aerial link as the function of SINR threshold T_{h1} given three different H_A .

$$\times (-1)^v \mathbb{E}_{I_A} [\exp(-s'_1 I_A)] \Big) dt, \quad (33)$$

with $s'_1 = \frac{v \zeta(\beta-\delta) (2^t-1) d_m^{\alpha_2}}{P_m G_{A_m-S}}$, and $\mathbb{E}_{I_A}[\exp(-s'_1 I_A)]$ is obtained by replacing s' in $\mathcal{L}_{I_A}(s')$ of (29) with s'_1 .

Proof: See Appendix G. \square

VI. NUMERICAL RESULTS

In this section, we verify the derived analytical expressions using Monte Carlo simulations with 50,000 runs. The results from the analytical derivations of Section IV are indicated in the following figures as ‘Analysis’, while the Monte Carlo results are indicated in the figures as ‘Simulation’. Unless otherwise specifically stated, the default system parameters utilized in the simulations are listed in Table II.

A. Performance of Terrestrial-Aerial Link

In this subsection, we conduct a simulation under various system parameters to verify the analytical coverage probability and average ergodic rate of the terrestrial-aerial link derived in Subsection IV-A, and the results obtained are depicted in Figs. 3 to 8. It can be seen that the analytical results closely match the corresponding simulation results, which supports the validity of our Theorem 1.

Fig. 3 depicts the coverage probability as the function of the SINR threshold T_{h1} , given three different values of the

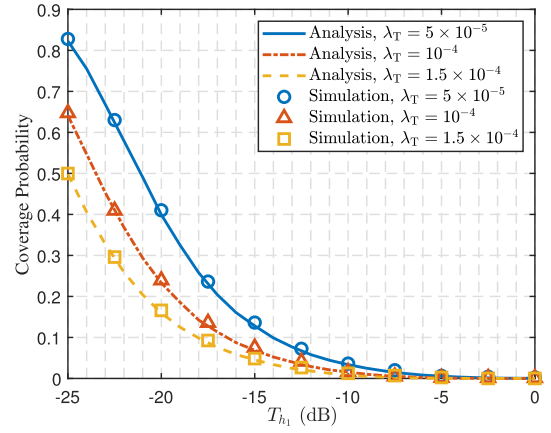


Fig. 4. Coverage probability of the terrestrial-aerial link as the function of SINR threshold T_{h1} given three different λ_T .

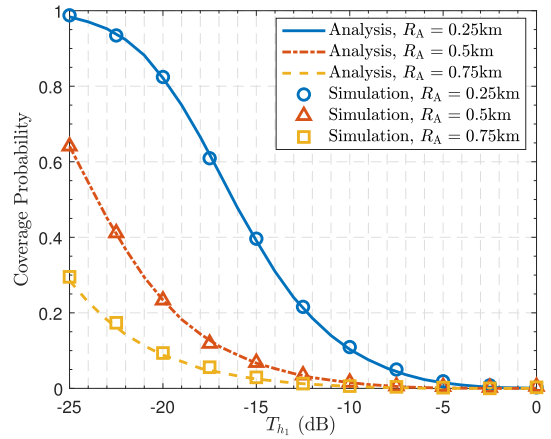


Fig. 5. Coverage probability of the terrestrial-aerial link as the function of SINR threshold T_{h1} given three different R_A .

height of the ANs H_A . It can be seen from Fig. 3 that increasing the SINR threshold T_{h1} decreases the coverage probability, i.e., decreasing the likelihood of experiencing the link coverage. This is expected due to the inverse relationship between T_{h1} and the probability of achieving an SINR that surpasses the given threshold value. Notably, the results of Fig. 3 indicates that increasing the height of ANs enhances the coverage probability of the T-A link. This can be explained by examining the impact of H_A on the SINR. From the SINR (1) of the T-A link and the accumulative interference power (2) of the link, it is clear that the reduction in the MUI is far more than the reduction in the target signal power when increasing H_A . Therefore, increasing H_A increases the link SINR, leading to the enhancement of the coverage probability.

Fig. 4 investigates the impact of the density of terrestrial nodes λ_T on the achievable coverage probability performance. It can be seen from Fig. 4 that increasing the density of terrestrial nodes reduces the achievable coverage probability. This is because a higher λ_T indicates a higher number of terrestrial transmitters concurrently attempting to access the UAV, leading to a higher MUI and consequently a lower coverage probability.

Fig. 5 portrays the coverage probability as the function of the SINR threshold T_{h1} , given three different values of the

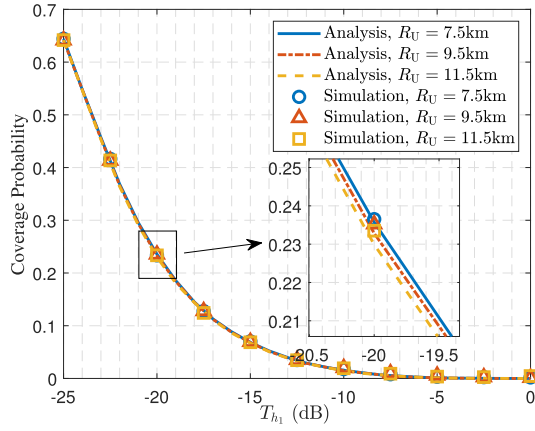


Fig. 6. Coverage probability of the terrestrial-aerial link as the function of SINR threshold T_{h1} given three different R_U .

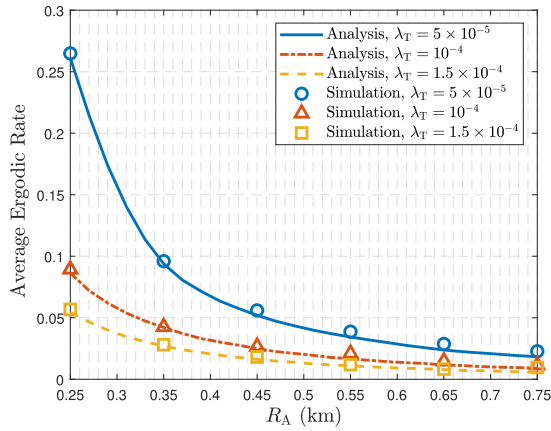


Fig. 7. Average ergodic rate of the terrestrial-aerial link as the function of AN's ground coverage radius R_A given three different values of λ_T .

AN's ground coverage radius R_A , where the influence of R_A on the achievable coverage probability is clearly exhibited. Specifically, increasing the AN's ground coverage radius leads to noticeably reduction in the coverage probability. This is because a larger ground region S_A' covers more terrestrial nodes, which can communicate with the same AN. This results in a higher number of territorial transmitters concurrently attempting to access the AN, leading to a higher MUI and consequently a lower coverage probability.

Fig. 6 studies the influence of the radius R_U on the coverage probability, indicating that impact of R_U on the coverage probability is negligible. Increasing R_U increases the area S_U of terrestrial nodes but this hardly changes the number of the TNs within the AN's coverage area S_A' , given the same user density λ_T . That is, the number of ground nodes connected to the same AN is hardly changed. Consequently, the MUI of the T-A link is hardly changed and the coverage probability is hardly affected, when R_U is changed.

Fig. 7 shows the average ergodic rate as the function of AN's ground coverage radius R_A , given three different values for the density of terrestrial nodes λ_T . As expected, increasing R_A enhances the average ergodic rate. This is because a larger coverage radius results in more interference nodes, given a fixed density. Additionally, a higher density of terrestrial nodes

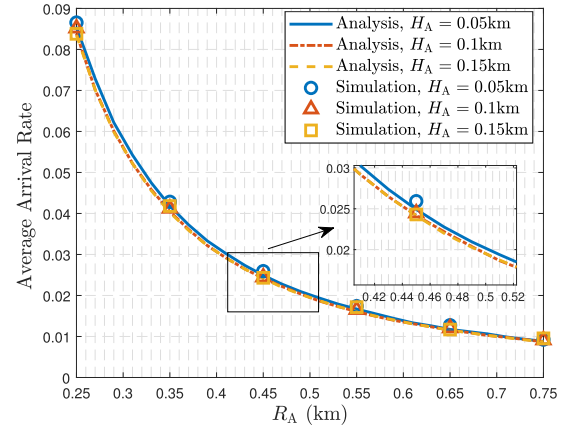


Fig. 8. Average ergodic rate of the terrestrial-aerial link as the function of AN's ground coverage radius R_A given three different values of H_A .

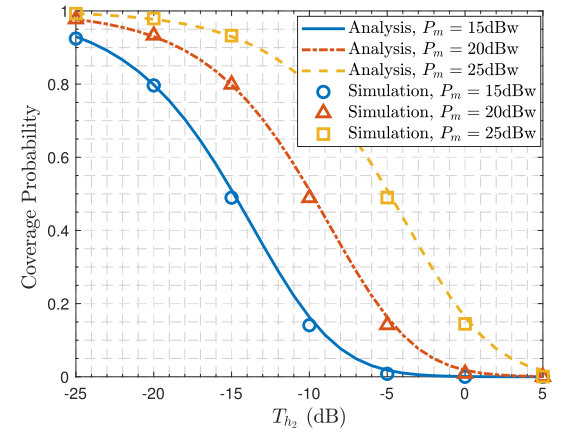


Fig. 9. Coverage probability of the aerial-satellite link as the function of the SINR threshold T_{h2} given three different values of P_m .

λ_T leads to more ground nodes, which increases the MUI of the T-A link, thereby reducing the average ergodic rate.

Fig. 8 demonstrates the impact of the values of the height of the ANs, H_A , on the data transmission rate of the T-A link. As explained for Fig. 8, an increase of the values of H_A reduces the average ergodic rate slightly. This can be explained by examining the impact of H_A on the SINR. However, the increase of H_A has a negligible impact on the SINR, resulting in only minor variations in the average ergodic rate.

B. Performance of Aerial-Satellite Link

Similarly, Monte Carlo simulations are employed to validate the close-form analytical coverage probability of the aerial-satellite link provided by **Theorem 2**. In the simulation, all the interfering ANs have the same transmit power of $P_n = P_A$, while the target AN's transmit power P_m is a variable. The results obtained are presented in Figs. 9 to 15, which confirm that Monte Carlo simulated coverage probability closely matches the analytical theoretical result.

More specifically, in Fig. 9, we analyze the relationship between the coverage probability and the SINR threshold. From Fig. 9, it is evident that there exists an inverse relationship between the threshold value T_{h2} and the coverage probability, whereby an increase of T_{h2} leads to a decrease of

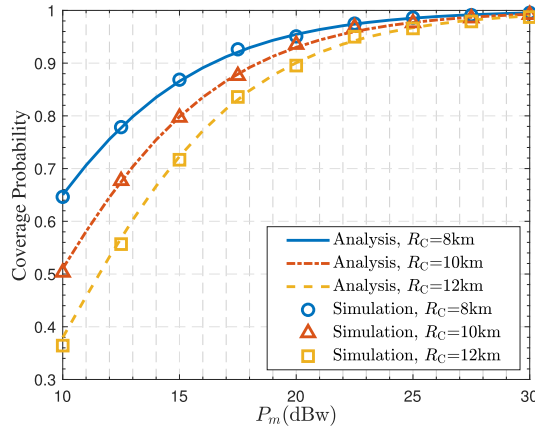


Fig. 10. Coverage probability of the aerial-satellite link as the function of target AN's transmit power P_m given three different values of R_C .

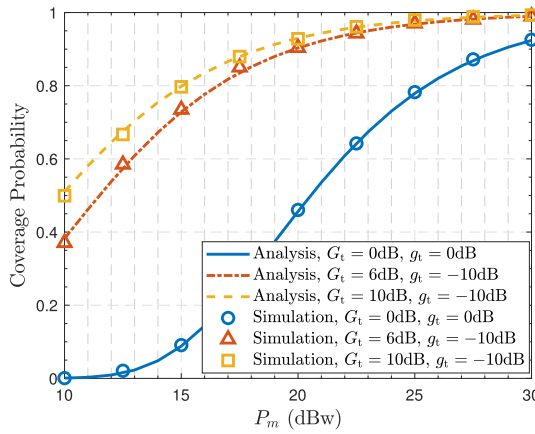


Fig. 11. Coverage probability of the aerial-satellite link as the function of target AN's transmit power P_m given three different combinations of G_t and g_t .

the coverage probability. Furthermore, given the other network parameters unchanged, an increase of the target AN's transmit power P_m leads to an enhanced coverage probability. This is because when the transmit signal strength of the targeted aerial node is enhanced while the interference power from other aerial nodes remain unchanged, the SINR increases, which manifests an increase in coverage probability.

Fig. 10 plots the coverage probability of the A-S link as the function of target AN's transmit power P_m , given three different values for the radius R_C of the circle space \mathcal{S}_A . As expected, increasing P_m increases the coverage probability, since increasing the power of the target transmitter leads to an increase in its SINR and this reduces the risk of communication interruption. In addition, the impact of R_C on the coverage probability is clearly shown in Fig. 10, namely, the expansion of the distribution space of aerial transmitters leads to a worsen coverage probability. This is because the increased availability of space for the MHCPP deployment of air nodes results in a higher number of transmitters concurrently attempting to access the satellite, leading to a higher MUI and consequently a worsen coverage probability.

Fig. 11 investigates the impact of different antenna gains on the coverage probability, and the results indicate that higher

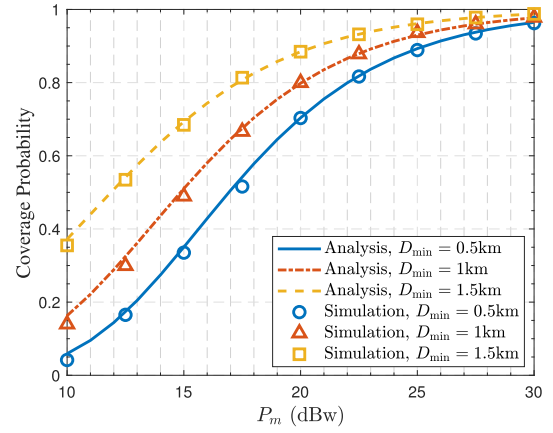


Fig. 12. Coverage probability of the aerial-satellite link as the function of target AN's transmit power P_m given three different values of D_{\min} .

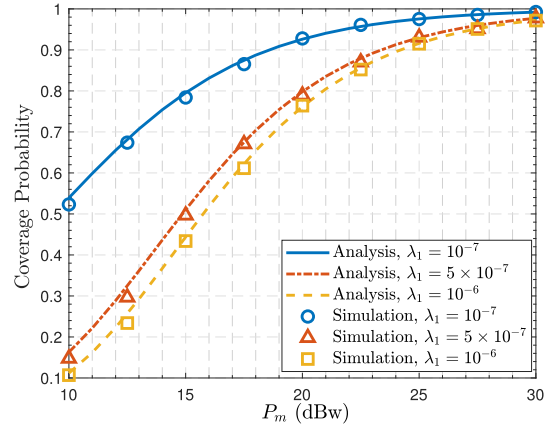


Fig. 13. Coverage probability of the aerial-satellite link as the function of target AN's transmit power P_m given three different values of λ_1 .

mainlobe gain and lower sidelobe gain improve the achievable coverage probability performance. The case of both G_t and g_t being 0dB simulates the scenario without directional BF, while the other two sets of G_t and g_t represent scenarios with different directional BF gains. As expected, the utilization of directional BF yields a notable enhancement in coverage probability, compared with the case of without directional BF. With directional BF, the satellite is in the mainlobe of the target transmitter, while it is randomly in the mainlobe or sidelobe of interfering transmitters. Furthermore, a higher disparity in the strength between the mainlobe and side lobes results in a reduced overall interference on the intended recipient. Consequently, the SINR of the signal received from the target node at the satellite is enhanced, leading to an improvement in the coverage probability.

Fig. 12 studies the impact of the minimum distance D_{\min} between every two candidate points on the coverage probability. Evidently, higher D_{\min} leads to lower aerial transmitters' access to the satellite, thereby resulting in a decrease of the interference towards the intended transmitter. Consequently, the SINR of the target link increases, which enhances the likelihood of coverage.

In Fig. 13, we proceed to compare the coverage probability under various values of λ_1 . The graph illustrates a negative

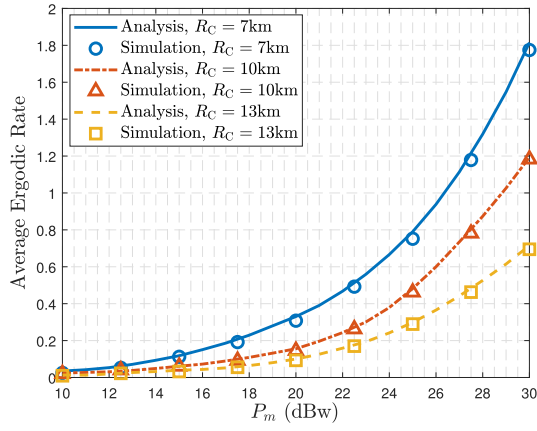


Fig. 14. Average ergodic rate of the aerial-satellite link as the function of target AN's transmit power P_m given three different values of R_C .

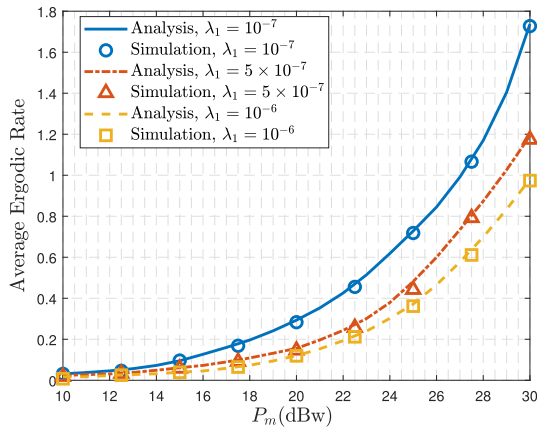


Fig. 15. Average ergodic rate of the aerial-satellite link as the function of target AN's transmit power P_m given three different values of λ_1 .

correlation between the node density and the coverage probability. It can be easily comprehended that an augmented density corresponds to an increased number of nodes, consequently resulting in a greater MUI. This, in turn, contributes to a heightened risk of outage. It may be readily understood that an enhanced density is associated with a higher quantity of nodes, hence leading to an amplified MUI. Consequently, this phenomenon leads to an increased susceptibility to service disruption, manifested as a decrease in the coverage probability.

Fig. 14 depicts the average ergodic rate as the function of the target AN's transmit power P_m , given three different values for the radius R_C of the ANs' deployment area \mathcal{S}_A . As expected, increasing P_m increases the average ergodic rate. In addition, the impact of R_C on the achievable average ergodic rate is clearly shown in Fig. 14. Evidently, increasing the available area of \mathcal{S}_A results in a reduction of the average ergodic rate, because there are more interfering transmitters. Observe that Fig. 14 is consistent with Fig. 10, which is to be expected given the relationship between the coverage probability and the average ergodic rate.

Fig. 15 further investigates the impact of the node density on the average ergodic rate. As expected, increasing λ_1 reduces the average ergodic rate, since increasing λ_1 leads to more

interfering nodes. Obviously, Fig. 15 is entirely consistent with Fig. 13, because a higher coverage probability corresponds to a higher average ergodic rate and vice versa.

VII. CONCLUSION

In this paper, we have proposed a tractable approach for analyzing the coverage probability and the average ergodic rate of T-A links and A-S links in a CSATN system, whose terrestrial terminals are located in a finite-size region. This condition incurs significant challenge for the performance analysis. Utilizing the expressions of coverage probability derived under various conditions, we can input relevant parameter values in analogous scenarios to determine the joint coverage probability of the end-to-end links spanning the terrestrial terminals, the aerial relays, and the satellite. Furthermore, with these theoretical results, we can gain a clear understanding of the impact imposed by critical system parameters, including the coverage area of aerial nodes, the flying altitude of aerial nodes, as well as the terrestrial and aerial nodes' densities, transmission distance, and antenna gain, on the achievable system performance. Therefore, our study offers theoretical guidance and valuable insights on how to conduct CSATN planning, deployment and optimization in practice. Our future work will focus on analyzing the uplink ergodic sum rate for the CSATNs studied here.

APPENDIX

A. Proof of Lemma 1

Proof: In order to facilitate calculations, we provide a two-dimensional Cartesian coordinate system, as depicted in Fig. 16. The AN projection point, denoted as \mathbf{o} , is situated at the origin of the coordinate system. The center point \mathbf{u} of the user area is situated in the positive half of the x-axis. Additionally, conditioned on $M = m_0$, the coordinates of \mathbf{u} is given by $(m_0, 0)$.

1) Given that $0 < m_0 < R_U - R_A$, \mathcal{S}'_A is entirely contained within \mathcal{S}_U , and $0 < r < R_A$. The CDF of r is

$$F_{R^{(1)}}(r|m_0) = \frac{\pi r^2}{\pi R_A^2} = \frac{r^2}{R_A^2}, \quad (34)$$

and the corresponding PDF is given by

$$f_{R^{(1)}}(r|m_0) = \frac{2r}{R_A^2}. \quad (35)$$

Given that $R_U - R_A < m_0 < R_U$, \mathcal{S}'_A and \mathcal{S}_U exhibit partial overlap. It is possible to further categorize this scenario into two distinct situations, dependent on whether the projection point falls inside the area of \mathcal{S}_U . According to Fig. 16(b), it is evident that the region of overlap between \mathcal{S}'_A and \mathcal{S}_U corresponds to the intersection area of two circles: one with a radius of R_A centered at the origin, and the other with a radius of R_U centered at $(m_0, 0)$. Hence, the abscissa x^* at which the two circles intersect can be expressed as

$$x^* = \frac{m_0^2 - R_U^2 + R_A^2}{2m_0}. \quad (36)$$

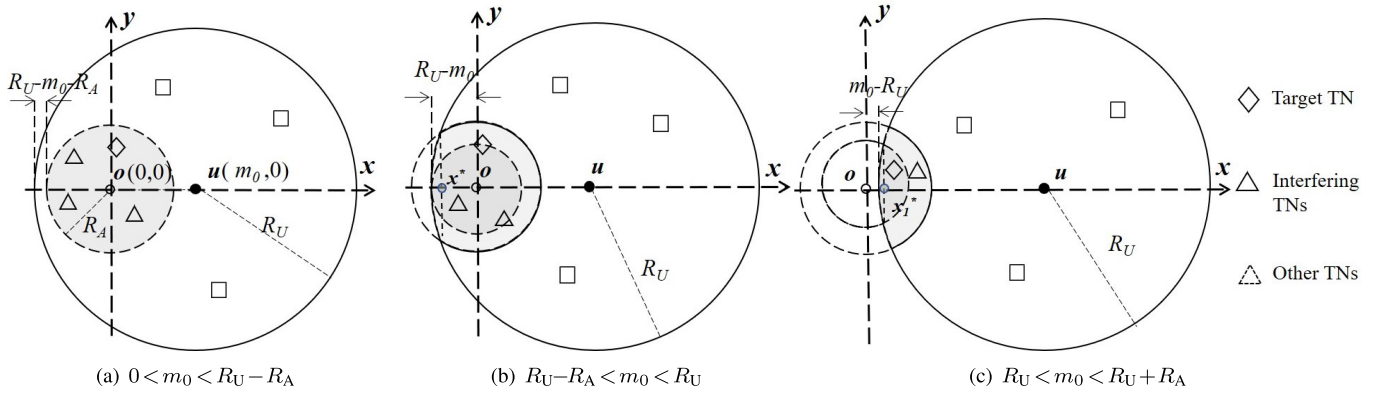


Fig. 16. Illustration of positional relationships under different conditions.

Then the intersecting area, denoted as γ , can be written as

$$\gamma = \int_{m_0 - R_U}^{x^*} 2\sqrt{R_U^2 - (x - m_0)^2} dx + \int_{x^*}^{R_A} 2\sqrt{R_A^2 - x^2} dx. \quad (37)$$

By setting $\frac{m_0 - x}{R_U} = \cos(\theta)$ and $\frac{x}{R_A} = \cos(\varphi)$, we obtain

$$\gamma = R_U^2 \left(\theta_2 - \frac{1}{2} \sin(2\theta_2) \right) + R_A^2 \left(\varphi_2 - \frac{1}{2} \sin(2\varphi_2) \right), \quad (38)$$

i.e., γ is given in (11) with θ_2 and φ_2 given in (12) and (13).

2) If $0 < r < R_U - m_0$ and $R_U - R_A < m_0 < R_U$, the PDF of r can be expressed as

$$f_{R^2}(r|m_0) = \frac{2\pi r}{\gamma}. \quad (39)$$

3) However, if $R_U - m_0 < r < R_A$ and $R_U - R_A < m_0 < R_U$, the overlapping region contains only a segment of the circle defined by the equation $x^2 + y^2 = r^2$. The abscissa x_1^* , which represents the intersection point between the circle $x^2 + y^2 = r^2$ and the circle $(x - m_0)^2 + y^2 = R_U^2$, is given by

$$x_1^* = \frac{m_0^2 - R_U^2 + r^2}{2m_0}. \quad (40)$$

Thus the CDF of r can be written as

$$\begin{aligned} F_{R^3}(r|m_0) &= \frac{1}{\gamma} \left(\int_{m_0 - R_U}^{x_1^*} 2\sqrt{R_U^2 - (x - m_0)^2} dx \right. \\ &\quad \left. + \int_{x_1^*}^r 2\sqrt{r^2 - x^2} dx \right) \\ &= \frac{1}{\gamma} \left(R_U^2 \left(\theta_4 - \frac{1}{2} \sin(2\theta_4) \right) + r^2 \left(\varphi_3 - \frac{1}{2} \sin(2\varphi_3) \right) \right), \quad (41) \end{aligned}$$

where $\theta_4 = \arccos\left(\frac{m_0 + R_U^2 - r^2}{2m_0 R_U}\right)$ and φ_3 is given in (14). The corresponding PDF $f_{R^3}(r|m_0)$ is then given by (10).

4) Similarly, if $m_0 - R_U < r < R_A$ and $R_U < m_0 < R_U + R_A$, as shown in Fig. 16(c), we can easily obtain the CDF of r as

$$\begin{aligned} F_{R^4}(r|m_0) &= \frac{1}{\gamma} \left(\int_{m_0 - R_U}^{x_1^*} 2\sqrt{R_U^2 - (x - m_0)^2} dx \right. \\ &\quad \left. + \int_{x_1^*}^r 2\sqrt{r^2 - x^2} dx \right) \end{aligned}$$

$$\begin{aligned} &+ \int_{x_1^*}^r 2\sqrt{r^2 - x^2} dx \\ &= \frac{1}{\gamma} \left(R_U^2 \left(\theta_4 - \frac{1}{2} \sin(2\theta_4) \right) + r^2 \left(\varphi_3 - \frac{1}{2} \sin(2\varphi_3) \right) \right), \quad (42) \end{aligned}$$

where $\theta_4 = \arccos\left(\frac{m_0 + R_U^2 - r^2}{2m_0 R_U}\right)$ and φ_3 is given in (14). Thus, the corresponding PDF $f_{R^4}(r|m_0)$ is given in (10). This completes the proof. \square

B. Proof of Theorem 1

Proof:

$$\begin{aligned} P_{\text{cov}}^{\text{T-A}} &= \mathbb{P}(\text{SINR}_1 \geq T_{h_1}) \\ &= \mathbb{E}_{R_m} [\mathbb{P}(\text{SINR}_1 \geq T_{h_1} | R_m = r_m, m_0)] \\ &= \int \int \mathbb{P}(\text{SINR}_1 \geq T_{h_1} | R_m = r_m, m_0) \\ &\quad \times f_{R_m}(r_m|m_0) f_M(m_0) dr_m dm_0. \quad (43) \end{aligned}$$

We note that $\mathbb{P}(\text{SINR}_1 \geq T_{h_1} | R_m = r_m, m_0)$ satisfies:

$$\begin{aligned} &\mathbb{P}(\text{SINR}_1 \geq T_{h_1} | R_m = r_m, m_0) \\ &= 1 - \mathbb{P}\left(|h_{T_m A}|^2 \leq \frac{T_{h_1} I_T (H_A^2 + r_m^2)^{\frac{\alpha_1}{2}}}{P_T}\right) \\ &\stackrel{(a)}{<} 1 - \mathbb{E}\left[\left(1 - \exp\left(\frac{-\eta T_{h_1} I_T (H_A^2 + r_m^2)^{\frac{\alpha_1}{2}}}{P_T}\right)\right)^{N_{\text{TA}}}\right] \\ &\stackrel{(b)}{=} \sum_{n=1}^{N_{\text{TA}}} (-1)^{n+1} \binom{N_{\text{TA}}}{n} \mathbb{E}_I \left[\exp\left(\frac{-n\eta T_{h_1} I_T (H_A^2 + r_m^2)^{\frac{\alpha_1}{2}}}{P_T}\right) \right] \\ &\stackrel{(c)}{=} \sum_{n=1}^{N_{\text{TA}}} (-1)^{n+1} \binom{N_{\text{TA}}}{n} \mathbb{E}_I [\exp(-s I_T)], \quad (44) \end{aligned}$$

where (a) is a tight upper bound when N_{TA} is small [37], that is, for small N_{TA} , $\mathbb{P}(|h|^2 < \psi) < \mathbb{E}[(1 - \exp(-\psi\eta))^{N_{\text{TA}}}]$ with $\eta = N_{\text{TA}}(N_{\text{TA}}!)^{-\frac{1}{N_{\text{TA}}}}$, and (b) is obtained by the binomial theorem, while (c) is obtained by denoting $s = \frac{n\eta T_{h_1} (H_A^2 + r_m^2)^{\frac{\alpha_1}{2}}}{P_T}$. This completes the proof. \square

C. Proof of Lemma 3

Proof: Assumed that the distance denoted as R_n between the interference user and the projection point is equal to r_n . Thus, $\mathcal{L}_{I_T}(s)$ can be written as

$$\begin{aligned}\mathcal{L}_{I_T}(s) &= \mathbb{E} \left[\prod_{T_n \in \Phi_U \setminus T_m} \exp \left(-s P_T |h_{T_n A}|^2 (H_A^2 + r_n^2)^{-\frac{\alpha_1}{2}} \right) \right] \\ &= \mathbb{E}_{N_I, R_n} \left[\prod_{T_n \in \Phi_U \setminus T_m} \mathbb{E}_{|h_{T_n A}|^2} \left[\exp \left(|h_{T_n A}|^2 \right. \right. \right. \\ &\quad \left. \left. \left. \times \left(-s P_T (H_A^2 + r_n^2)^{-\frac{\alpha_1}{2}} \right) \right) \right] \right] \\ &\stackrel{(a)}{=} \mathbb{E}_{N_I, R_n} \left[\prod_{T_n \in \Phi_U \setminus T_m} \underbrace{\left(1 + \frac{s P_T}{N_{TA} (H_A^2 + r_n^2)^{\frac{\alpha_1}{2}}} \right)^{-N_{TA}}}_{D_2} \right],\end{aligned}\quad (45)$$

where (a) is obtained by using the moment-generating function (MGF) of the normalized Gamma random variable. This completes the proof. \square

D. Proof of Theorem 2

Proof: Using the Kummer's transform of the hypergeometric function [38], the PDF of $|h|^2$ (4) can be rewritten as

$$f_{|h|^2}(x) = \sum_{k=0}^{\infty} \Psi(k) x^k \exp(-(\beta - \delta)x), \quad (46)$$

where

$$\Psi(k) = \frac{(-1)^k \kappa \delta^k}{(k!)^2} (1 - q)_k. \quad (47)$$

Then, the CDF of $|h|^2$ can be expressed as

$$\begin{aligned}F_{|h|^2}(x) &= \sum_{k=0}^{\infty} \Psi(k) \int_0^x t^k \exp(-(\beta - \delta)t) dt \\ &= \sum_{k=0}^{\infty} \frac{\Psi(k)}{(\beta - \delta)^{k+1}} \bar{\gamma}(k+1, (\beta - \delta)x).\end{aligned}\quad (48)$$

Therefore, we obtain $P_{\text{cov}}^{\text{A-S}}$ as

$$\begin{aligned}P_{\text{cov}}^{\text{A-S}} &\triangleq \mathbb{P} \left(\frac{P_m G_{A_m-S} |h_{A_m S}|^2 d_m^{-\alpha_2}}{I_A} \geq T_{h_2} \right) \\ &= 1 - \mathbb{P} \left(|h_{A_m S}|^2 \leq \frac{T_{h_2} I_A d_m^{\alpha_2}}{P_m G_{A_m-S}} \right) \\ &= 1 - \mathbb{E} \left[\kappa \sum_{k=0}^{\infty} \frac{\Psi(k)}{(\beta - \delta)^{k+1}} \bar{\gamma} \left(k+1, (\beta - \delta) \frac{T_{h_2} I_A d_m^{\alpha_2}}{P_m G_{A_m-S}} \right) \right] \\ &\stackrel{(a)}{\approx} 1 - \mathbb{E} \left[\sum_{k=0}^{\infty} \frac{\Psi(k)}{(\beta - \delta)^{k+1}} \Gamma(k+1) \right]\end{aligned}$$

$$\begin{aligned}&\times \left(1 - \exp \left(-\frac{\zeta(\beta - \delta) T_{h_2} I_A d_m^{\alpha_2}}{P_m G_{A_m-S}} \right) \right)^{k+1} \Big] \\ &\stackrel{(b)}{=} 1 - \sum_{k=0}^{\infty} \frac{\Psi(k)}{(\beta - \delta)^{k+1}} \Gamma(k+1) \sum_{t=0}^{k+1} \binom{k+1}{t} \\ &\quad \times (-1)^t \mathbb{E} [\exp(-s' I_A)],\end{aligned}\quad (49)$$

where (a) is approximated by using $\bar{\gamma}(k+1, x) < \Gamma(k+1)(1 - \exp(-\zeta x))^{k+1}$ [37], $\zeta = (\Gamma(k+2))^{-\frac{1}{k+1}}$, and (b) is obtained from binomial theorem with $s' = \frac{\zeta(\beta - \delta) T_{h_2} d_m^{\alpha_2}}{P_m G_{A_m-S}}$. This completes the proof. \square

E. Proof of Lemma 4

Proof:

$$\begin{aligned}\mathcal{L}_{I_A}(s') &= \mathbb{E} \left[\exp \left(-s' \sum_{A_n \in \Phi_A \setminus A_m} P_n G_{A_n-S} |h_{A_n S}|^2 d_n^{-\alpha_2} \right) \right] \\ &= \mathbb{E} \left[\prod_{A_n \in \Phi_A \setminus A_m} \mathbb{E}_{|h_{A_n S}|^2} \left[\exp \left(-s' P_n G_{A_n-S} |h_{A_n S}|^2 d_n^{-\alpha_2} \right) \right] \right] \\ &\stackrel{(a)}{=} \mathbb{E}_{N_A} \left[\prod_{A_n \in \Phi_A \setminus A_m} \mathbb{E}_{G_{A_n-S}, |h_{A_n S}|^2} \left[\exp \left(-t_A |h_{A_n S}|^2 \right) \right] \right],\end{aligned}\quad (50)$$

where (a) is obtained because all aerial transmitters have an equal distance to S , and $t_A = s' P_n G_{A_n-S} d_0^{-\alpha_2}$.

As shown in [34], the MGF of the SR fading model is defined as $M_S(x) = \mathbb{E} [\exp(-xS)] = \frac{(2cq)^q (1+2cx)^{q-1}}{((2cq+\Omega)(1+2cx)-\Omega)^q}$. Thus, we further obtain

$$\begin{aligned}\mathcal{L}_{I_A}(s') &= \mathbb{E}_{N_A} \left[\prod_{A_n \in \Phi_A \setminus A_m} \mathbb{E}_{G_{A_n-S}} \left[\underbrace{\frac{(2cq)^q (1+2ct_A)^{q-1}}{((2cq+\Omega)(1+2ct_A)-\Omega)^q}}_{M_1(t_A)} \right] \right] \\ &\stackrel{(b)}{=} \mathbb{E}_{N_A} \left[\prod_{A_n \in \Phi_A \setminus A_m} \underbrace{\left(M_1(t_1) \frac{\theta}{2\pi} + M_1(t_2) \left(1 - \frac{\theta}{2\pi} \right) \right)}_{M_2} \right] \\ &\stackrel{(c)}{=} \sum_{n=0}^{\infty} \frac{(\lambda_A S_A)^n}{n!} \exp(-\lambda_A S_A) (M_2)^n \\ &= \exp(\lambda_A S_A (M_2 - 1)),\end{aligned}\quad (51)$$

where (b) is obtained by denoting $t_1 = s' P_n d_0^{-\alpha_2} G_{I_r}$ and $t_2 = s' P_n d_0^{-\alpha_2} g_{I_r}$, and (c) is obtained by the fact that N_A follows the PPP with the density of λ_A and $S_A = \pi R_C^2$. This completes the proof. \square

F. Proof of Theorem 3

Proof: From (31), we have

$$\begin{aligned}\bar{C}^{\text{T-A}} &\triangleq \frac{1}{K} \mathbb{E} [\log_2(1 + \text{SINR}_1)] \\ &\stackrel{(a)}{=} \frac{1}{K} \iiint_{t>0} \mathbb{E} [\mathbb{P}(\log_2(1 + \text{SINR}_1) > t) | R_m = r_m, m_0] \\ &\quad \times f_{R_m}(r_m | m_0) f_M(m_0) dt dr_m dm_0,\end{aligned}\quad (52)$$

where (a) follows from the fact that if the random variable X involved is positive, $\mathbb{E}[X] = \int_{t>0} \mathbb{P}(X > t) dt$.

We note that $\mathbb{E} \left[\mathbb{P} \left(\log_2(1 + \text{SINR}_1) > t \right) | R_m = r_m, m_0 \right]$ satisfies:

$$\begin{aligned} & \mathbb{E} \left[\mathbb{P} \left(\log_2(1 + \text{SINR}_1) > t \right) | R_m = r_m, m_0 \right] \\ &= \mathbb{E} \left[\mathbb{P} \left(|h_{TmA}|^2 > \frac{I_T(2^t - 1)}{P_T(H_A^2 + r_m^2)^{-\frac{\alpha_1}{2}}} \right) | R_m = r_m, m_0 \right] \\ &\stackrel{(b)}{<} \left(1 - \mathbb{E} \left[\left(1 - \exp \left(\frac{-\eta I_T(2^t - 1)}{P_T(H_A^2 + r_m^2)^{-\frac{\alpha_1}{2}}} \right) \right)^{N_{TA}} \right] \right) \\ &\stackrel{(c)}{=} \sum_{n=1}^{N_{TA}} (-1)^{n+1} \binom{N_{TA}}{n} \mathbb{E}_{I_T} [\exp(-s_1 I_T)], \end{aligned} \quad (53)$$

where (b) is obtained by the tight upper bound when N_{TA} is small [37], that is, $\mathbb{P}[|h|^2 < \psi] < (1 - \exp(-\psi\eta))^{N_{TA}}$ with $\eta = N_{TA}(N_{TA}!)^{-\frac{1}{N_{TA}}}$, and (c) is obtained by the binomial theorem and by denoting $s_1 = \frac{n\eta(2^t-1)}{P_T(H_A^2+r_m^2)^{-\frac{\alpha_1}{2}}}$. This completes the proof. \square

G. Proof of Theorem 4

Proof: Starting from the definition (31), we have

$$\begin{aligned} \bar{C}^{A-S} &\triangleq \frac{1}{K} \mathbb{E} [\log_2(1 + \text{SINR}_2)] \\ &\stackrel{(a)}{=} \frac{1}{K} \mathbb{E} \left[\int_{t>0} \mathbb{P} \left(\log_2 \left(1 + \frac{P_m G_{A_m-S} |h_{A_mS}|^2 d_m^{-\alpha_2}}{I_A} \right) > t \right) dt \right] \\ &\stackrel{(b)}{=} \frac{1}{K} \mathbb{E} \left[\int_{t>0} \left(1 - \mathbb{P} \left(|h_{A_mS}|^2 \leq \frac{I_A(2^t - 1)}{P_m G_{A_m-S} d_0^{-\alpha_2}} \right) \right) dt \right] \\ &\stackrel{(c)}{=} \frac{1}{K} \int_{t>0} \left(1 - \mathbb{E} \left[\sum_{k=0}^{\infty} \frac{\Psi(k)}{(\beta - \delta)^{k+1}} \right. \right. \\ &\quad \left. \left. \times \gamma \left(k+1, (\beta - \delta) \frac{I_A(2^t - 1) d_0^{\alpha_2}}{P_m G_{A_m-S}} \right) \right] \right) dt \\ &\stackrel{(d)}{\approx} \frac{1}{K} \int_{t>0} \left(1 - \mathbb{E} \left[\sum_{k=0}^{\infty} \frac{\Psi(k)}{(\beta - \delta)^{k+1}} \Gamma(k+1) \right. \right. \\ &\quad \left. \left. \times \left(1 - \exp \left(-\frac{\zeta(\beta - \delta)(2^t - 1) I_A d_0^{\alpha_2}}{P_m G_{A_m-S}} \right) \right)^{k+1} \right] \right) dt \\ &\stackrel{(e)}{=} \frac{1}{K} \int_{t>0} \left(1 - \sum_{k=0}^{\infty} \frac{\Psi(k)}{(\beta - \delta)^{k+1}} \Gamma(k+1) \sum_{v=0}^{k+1} \binom{k+1}{v} \right. \\ &\quad \left. \times (-1)^v \mathbb{E} [\exp(-s_1' I_A)] \right) dt, \end{aligned} \quad (54)$$

where (a) follows from the fact that if the random variable X involved is positive, $\mathbb{E}[X] = \int_{t>0} \mathbb{P}(X > t) dt$, (b) is due to the fact that (d) is approximately a constant d_0 , (c) is obtained by substituting (48) into right-hand side expression of (b), (d) is approximated by using $\gamma(k+1, x) < \Gamma(k+1)(1 - \exp(-\zeta x))^{k+1}$ with $\zeta = (\Gamma(k+2))^{-\frac{1}{k+1}}$ [37], and (e) is obtained from the binomial theorem with $s_1' = \frac{v\zeta(\beta-\delta)(2^t-1)d_0^{\alpha_2}}{P_m G_{A_m-S}}$. \square

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