

# Monitoring observations of SMC X-1's excursions (MOOSE) III. X-ray spectroscopy of a warped, precessing accretion disc

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## ABSTRACT

The MOOSE (Monitoring Observations of SMC X-1's Excursions) program uses the Neutron Star Interior Composition Explorer Mission (NICER) to monitor the high-mass X-ray binary SMC X-1 during its superorbital period excursions. Here, we perform X-ray spectral analyses of 26 NICER observations of SMC X-1, taken at the tail-end of the excursion between 2021-04-01 and 2022-01-05. We use a single spectral model to fit spectra observed in high, intermediate, and low states, using a combination of a partial covering fraction model, a blackbody disc, and a power-law component. We find that the partial covering fraction varies significantly with the superorbital state during superorbital excursion. Our findings suggest that the low/high state in SMC X-1 is caused by a very high obscuration of the accretion disc.

**Key words:** accretion, accretion discs – pulsars: individual: SMC X-1 – X-rays: binaries.

## 1 INTRODUCTION

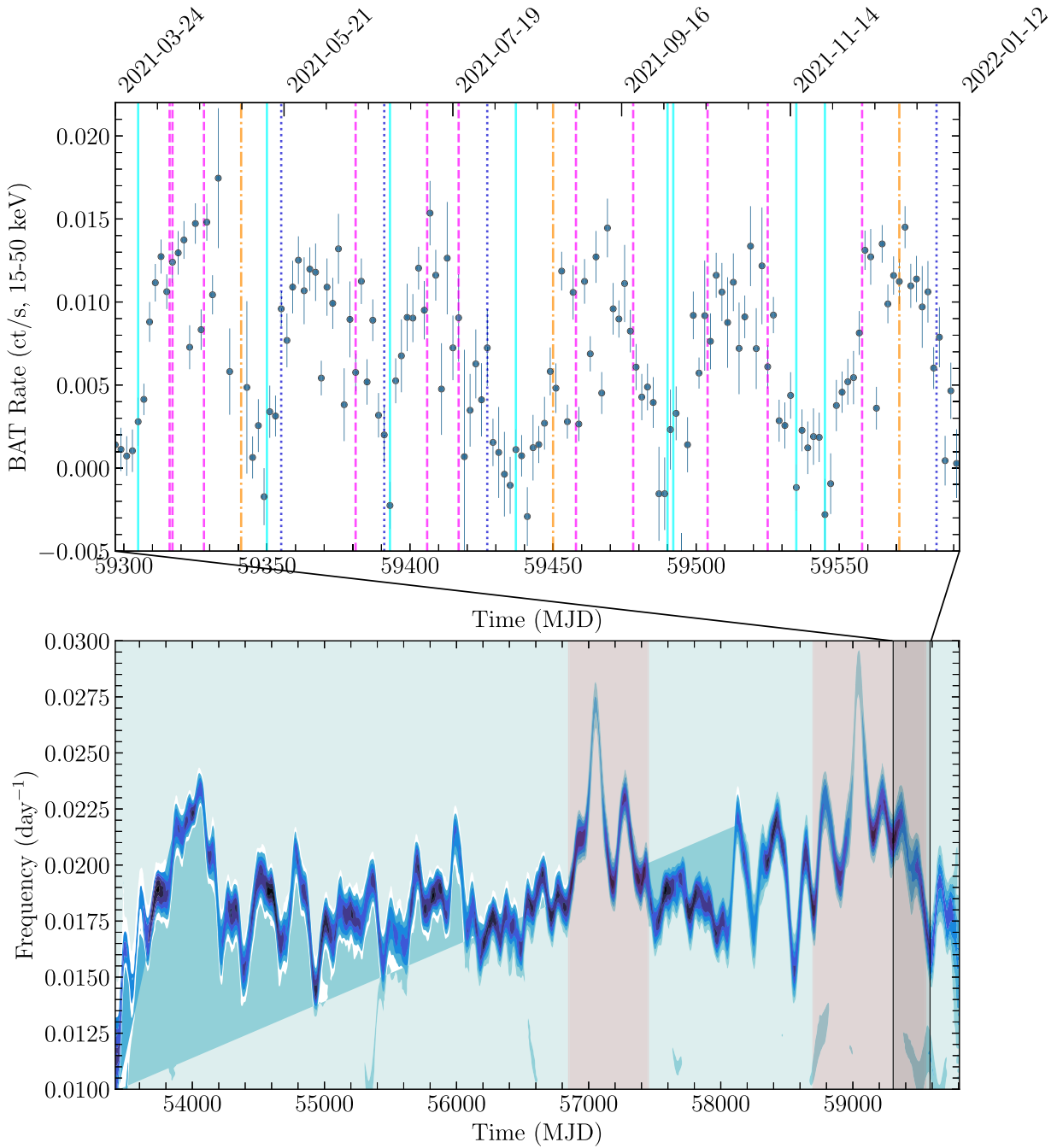
Warped accretion discs challenge our current models and understanding of accretion physics. Many studies now suggest that warped accretion discs are far more ubiquitous than previously thought, and are present in black holes and neutron star systems alike (Townsend & Charles 2020; Thomas et al. 2022). For example, Clarkson et al. (2003) demonstrated that many systems display superorbital periods (detected periods longer than the binary orbit) with varying lengths, which are due to warped accretion discs, where the stability of the warp is determined by properties of the binary system, such as binary separation and binary mass ratio (Ogilvie & Dubus 2001). Smoothed

particle hydrodynamic simulations (e.g. Foulkes, Haswell & Murray 2006) have indicated that the central engine's illumination of the accretion disc can exert non-axisymmetric radiation, which causes tilting or warping on the disc's surface.

The neutron star X-ray binary SMC X-1 is one of the best systems in which to study the physics behind accretion discs due to its well-determined distance, low extinction, and variety of time dependent behaviour. SMC X-1's orbital period is 3.89 d with a pulse period of 0.7 s (Lucke et al. 1976), and it exhibits a superorbital period of 40–60 d (Gruber & Rothschild 1984; Wojdowski et al. 1998). This is likely due to a warped, precessing accretion disc (Clarkson et al. 2003; Hickox, Narayan & Kallman 2004; Brumback et al. 2020). SMC X-1's superorbital period is nominally  $\sim 55$  d, but is observed to change to as low as 45 d (Fig. 1), a so-called superorbital period 'excursion', which occurs when the collimated radiation hits the accretion disc, changing its geometry (Foulkes et al. 2006).

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**Figure 1.** Hilbert–Huang transform of SMC X-1 (from Hu et al. 2023) showing three of its superorbital period excursions. The inset at MJD 59 305 shows the *Swift*/BAT light curve of SMC X-1 overlaid with observation times from our NICER monitoring campaign (pink dashed are high state observations, blue dotted lines are intermediate state observations, aqua solid lines are low state observations, and gold dash–dotted lines are pre-eclipse dips), taken during the tail-end of the superorbital period excursion. Our observations span a range of superorbital phases and source luminosity. The grey shaded regions mark the duration of the third and fourth superorbital excursions, respectively. Our observations span the tail end of the fourth excursion and continue after the excursion has finished.

The broad-band X-ray spectrum has been characterized as a cut-off power-law continuum with a low energy blackbody component and iron emission lines by various instruments and studies including *ASCA* (Paul et al. 2002), *Beppo-SAX* (Naik & Paul 2004), *XMM–Newton* and *NuSTAR* (Brumback et al. 2020), and Neutron Star Interior Composition Explorer (*NICER*; Dage et al. 2022).

SMC X-1’s superorbital period has been a long-standing subject of investigation since Gruber & Rothschild (1984), which observed

the variability and spectrum of SMC X-1 with observations from the UCSD/MIT instrument on *HEAO 1* from 1977 to 1979. Their results suggest that SMC X-1 has two states, high or low, and they constructed average spectra separately for each state, which showed that the total emission from SMC X-1 displays a continuum spectrum with a dominant exponential form. More recent studies using *XMM–Newton* and *NuSTAR*’s combined broad-band X-ray coverage reveal that the superorbital high and low states exhibit

different X-ray continua and suggest higher absorption during the low states (Pike et al. 2019; Brumback et al. 2020), consistent with observation from a precessing warped accretion disc. Pradhan, Maitra & Paul (2020) examined archival Suzaku and NuSTAR spectra of SMC X-1 during different superorbital states and noted large changes in the normalization of the power-law component that suggest an additional mechanism may be driving SMC X-1's spectral changes with superorbital phase.

SMC X-1 also exhibits timing behaviours beyond its superorbital period, including an energy-dependent pulse profile and binary eclipses. Beppo-SAX observations of SMC X-1 revealed a single-peaked pulse profile at energies below 1 keV and a double-peaked profile at higher energies (Naik & Paul 2004). These results were confirmed by observations using *Chandra*, *XMM-Newton*, and NuSTAR. Hickox & Vrtilek (2005) and Brumback et al. (2020) performed pulse-phase resolved spectroscopy of SMC X-1 and found that the blackbody component of the X-ray spectrum followed the low-energy pulse profile and the power-law component followed the high-energy power law, similar to ASCA studies by Paul et al. (2002). These studies suggest that the soft component is likely produced by reprocessing of the hard X-ray pulsar beam by the inner accretion disc. They support this claim by using a model of a twisted inner disc illuminated by the rotating X-ray pulsar beam to simulate pulsations in the soft component, thus showing that the precession of an illuminated accretion disc can roughly reproduce the observed long-term changes in the soft-pulse profiles for some disc and beam geometries (Hickox & Vrtilek 2005; Brumback et al. 2020).

Studies of the X-ray orbital light curve of SMC X-1 have revealed it to have pre-eclipse dips in the orbital phase range of 0.6–0.85 (e.g. Woo et al. 1995; Raichur & Paul 2010; Brumback et al. 2022). While not well studied, these dips are thought to be similar to those seen in Her X-1 (Giacconi et al. 1973), and are caused by increased obscuration from the impact of the accretion stream on to the accretion disc.

SMC X-1's superorbital excursions offer a rare chance to study both pulsar behaviour and the accretion disc at the same time. Dage et al. (2019) and Hu et al. (2019) highlighted that the superorbital period and the spin of SMC X-1 may be both correlated with the physics behind the accretion. Hu et al. (2013) applied the Hilbert–Huang transform to analyse the time-frequency properties of the superorbital modulation in SMC X-1 from observations made by the All-Sky Monitor onboard the Rossi X-ray Timing Explorer. The resultant Hilbert spectrum showed that the superorbital modulation period varied between ~40 and ~60 d, providing a robust timing technique that could very closely follow the changes in the superorbital period.

Later analysis of SMC X-1 by Hu et al. (2019) showed that a third observed superorbital period excursion event occurred during 2014–2016 and suggests that this excursion is recurrent and possibly periodic. Brumback et al. (2020) modelled the geometry of SMC X-1 and showed that superorbital period cycles are indeed consistent with a warped accretion disc. However, a similar analysis has not yet been completed for data taken during a superorbital period excursion, and it is not known whether the geometry of the disc changes as the superorbital period changes. Stray-light studies of SMC X-1 with NuSTAR found that SMC X-1's pulse profile did not vary with energy, but did change significantly over time (Brumback et al. 2022).

A study of SMC X-1 by Pike et al. (2019) suggests that its transient pulsations may be due to obscuration of the warped accretion disc. Thus, understanding the physical processes behind accretion is the first step to addressing the superorbital period, and understanding SMC X-1 may help shed light on the more extreme processes

happening in the more distant pulsating ultraluminous X-ray sources, some of which show similar long-term variability (Bachetti et al. 2020; Townsend & Charles 2020).

The first paper in this series, MOOSE I, Dage et al. (2022) introduces the first 26 observations of the MOOSE campaign and provides spectral fits to the high state spectra of SMC X-1 as it exits its fourth epoch of superorbital period excursion (Fig. 1). In these high-state spectral fits, Dage et al. (2022) found very little fluctuation between key spectral parameters like absorption column density, blackbody disc temperature, and photon index. MOOSE II (Hu et al. 2023) studies the excursion phenomenon in SMC X-1 specifically, comparing the properties of the most recent excursion event (2020–2021 or MJD 58700–59550, see Fig. 1) to prior excursions. Their study of the superorbital period finds that the spin-up acceleration and the pulse profiles (the shape of the pulsations emanating from the neutron star) may be connected to the superorbital excursion. These behaviours suggest that SMC X-1 is a complex physical system that requires more than a simple warped disc model (see also Pradhan et al. 2020).

Dage et al. (2022) studied 11 NICER high-state observations (out of the 26 observations taken during the tail-end of excursion) and found no evidence for significant changes in the spectral shape of the superorbital high state. In this work, we present the first spectral fits to all 26 of the NICER observations to investigate spectral changes between superorbital high, intermediate, and low states and to examine if the spectral shapes change after the end of excursion. We present the data and analysis in Section 2 and discuss the results in Section 3. Our conclusions and recommendations for future work are presented in Section 4.

## 2 OBSERVATIONS AND DATA ANALYSIS

We analysed 26 observations within the MOOSE data set of SMC X-1, taken with the NICER (Gendreau et al. 2016). These observations were taken in random intervals of at least 10 d, spanning different stages of the superorbital cycle (specifically the high, intermediate, and low states), from 2021-04-01 (MJD 59305) until 2022-01-05 (MJD 59584). Most observations were taken towards the end of the 2020–2021 superorbital excursion, defined as the time interval from MJD 58 700 to 59 550 (Hu et al. 2023). The final three observations occurred after this excursion epoch (see Fig. 1 and Table 1).

### 2.1 NICER

The NICER observations were processed with HEASOFT 6.29 NICERL2 task. For each observation, the spectrum was generated with the XSELECT command, with optimal binning implemented (Kaastra & Bleeker 2016). For the background, the spectra were generated with the NIBACKGEN3C50 tool (Remillard et al. 2022). The NICERARF and NICERRMF tasks were used to generate the ancillary response files (ARFs) and response matrix files (RMFs). This data reduction follows the method used in Dage et al. (2022), where it is described in detail. Further information including date, exposure, count rate, and other filtering parameters can be found in Table 1.

### 2.2 X-ray spectral fitting

Working with these spectra, we tested a series of models to fit the 0.3–12 keV energy range for all observations. We used XSPEC v12.12.0 (Arnaud 1996) to model the spectra, using  $\chi^2$  statistics, abundances from Wilms, Allen & McCray (2000), and photoelectric cross-sections from Verner et al. (1996).

**Table 1.** NICER observations log with count rate errors determined by XSPEC. Pre-eclipse dips are marked with †.

ObsID	Date	Duration (s)	Overonly range	Underonly range	Count rate (ct/s)
4509010101	2021-04-01	1006	<11	<200	33 ± 0.2
4509010102	2021-04-12	1362	<3	<200	214 ± 0.4
4509010103	2021-04-13	483	<7	<200	220 ± 0.6
4509010301	2021-04-24	436	<20	<200	195 ± 0.7
4509010401 †	2021-05-07	967	<40	<200	2 ± 0.05
4509010501	2021-05-16	1446	<140	<200	7 ± 0.07
4509010601	2021-05-21	1024	<4	<200	146 ± 0.4
4509010701	2021-06-16	1279	<2	<200	206 ± 0.4
4509010801	2021-06-26	1684	<1.5	<200	139 ± 0.3
4509010802	2021-06-28	796	<20	<200	10 ± 0.2
4509010803	2021-07-11	944	<30	<200	232 ± 0.5
4509010901	2021-07-22	821	<20	<200	179 ± 0.4
4509011001	2021-08-01	1235	<50	<200	72 ± 0.3
4509011101	2021-08-11	1123	<1	<200	9 ± 0.1
4509011201 †	2021-08-24	1327	<20	<200	52 ± 0.3
4509011301	2021-09-01	1898	<0.5	<200	189 ± 0.4
4509011401	2021-09-21	1476	<35	<200	245 ± 0.5
4509011501	2021-10-03	350	<16	<200	9 ± 0.2
4509011601	2021-10-05	1107	<10	<200	10 ± 0.1
4509011701	2021-10-17	2533	<1	<200	195 ± 0.3
4509011901	2021-11-07	1259	<30	<200	176 ± 0.4
4509012001	2021-11-17	955	<75	<200	10 ± 0.2
4509012101	2021-11-27	1513	<100	<200	6 ± 0.07
4509012201	2021-12-10	1476	<11	<200	249 ± 0.4
4509012301 †	2021-12-23	2411	<1	<306	5 ± 0.06
4509012401	2022-01-05	1474	<15	<300	151 ± 0.3

We implemented a model with an interstellar medium absorption component (`tbabs`) and a partial covering component (`pcfabs`) to assess the degree of obscuration from the warped accretion disc (e.g. Neilsen, Hickox & Vrtilek 2004). We set the (`tbabs`)  $N_H$  to the average best-fitting line-of-sight value from Dage et al. (2022) ( $2.5 \times 10^{21} \text{ cm}^{-2}$ ), which is broadly consistent with those found in Neilsen et al. (2004), Pradhan et al. (2020), and Brumback et al. (2023). We freeze this value for all observations, out of concern for degeneracy between the  $N_H$  of the `tbabs` and `pcfabs` models. We also fit a blackbody component (`bbody`), a cut-off power-law (`cutoffpl`), and three Gaussian components for emission lines, with values adopted from Brumback et al. (2020). The  $\Gamma$  cut-off value is capped at 20 keV for all observations, similar to Brumback et al. (2020) and Dage et al. (2022). Our best-fitting model is `tbabs * pcfabs * (bbody + cutoffpl + gauss + gauss + gauss)`.

Except for three pre-eclipse dip observations, the high, intermediate, or low states corresponded to the model-predicted count rate, as follows:

- (i) Low, 10–50 ct/s
- (ii) Intermediate, 50–150 ct/s
- (iii) High, >150 ct/s

We aim to apply the best-fitting model described above to all observations, regardless of superorbital state, to investigate changes in obscuration or covering fraction due to changes in the accretion disc during excursion. However, spectra from the low states of the superorbital cycle, when the source flux was decreased, had a lower signal-to-noise (S/N) than the high state data sets. Hence, to apply a consistent spectral model to all data sets while reducing degeneracy in the `pcfabs` components (see Brumback et al. 2023, for more discussion on model degeneracy), we chose to fix the  $kT$  and  $\Gamma$  values in the low and intermediate state spectra to the high state average values, which were 0.19 keV and 0.79, respectively. In this

way, we are effectively making the assumption that the underlying continuum has a constant spectral shape. This assumption is valid when considering the many historic data sets of this source which consistently produce the same spectral shape of a cut-off power-law and soft blackbody component (e.g. the ASCA observations examined in Paul et al. 2002). More recent spectral studies of SMC X-1 with NICER over a period of several months also suggest that the underlying spectral shape remains constant (Brumback et al. 2023). Assuming a constant spectral shape and freezing the low and intermediate state continuum parameters allows us to test whether this assumption holds for the lower S/N data.

To further assess the impact of freezing the blackbody  $kT$  and  $\Gamma$  values on our `pcfabs`/ $N_H$  and covering fraction results, we investigate a representative low state spectrum (ObsID 4509012301). For this fit, we keep the values of  $kT$  and  $\Gamma$  fixed, but vary their values by up to 20 per cent from their average values, in increments of 5 per cent. This was done (1) for  $kT$  only, while keeping  $\Gamma$  constant, (2) for  $\Gamma$  only, while keeping  $kT$  constant, and finally (3) while varying both values simultaneously. In all three cases, variations in the values of  $kT$  and  $\Gamma$  did not result in a change in either `pcfabs`/ $N_H$  or covering fraction of more than 5 per cent. For this reason, we are confident that holding the shape of the spectral continuum constant in the low state data does not induce artificial errors into the `pcfabs` values. This is consistent with the results found in Brumback et al. (2023), where the spectral continuum in SMC X-1 varies little with superorbital period.

The best-fitting parameters for this model are in Table 2, and plotted in Fig. 2. Examplespectra are shown in Fig. 3.

### 3 RESULTS AND DISCUSSION

The first 26 NICER observations in the MOOSE data set span different stages of the system’s superorbital period; that is, its high,

**Table 2.** Best-fitting parameters for our model,  $\text{tbabs}*\text{pcfabs}*(\text{bbody} + \text{cutoffpl} + \text{gauss} + \text{gauss} + \text{gauss})$ , in the 0.3–12 keV band. Observations in the low state (i.e. with a count rate lower than 50 counts/sec) and intermediate state were fit with a model with blackbody temperature and power-law index frozen to the best-fitting values from the high states (see Section 2.2). The  $N_{\text{H}}$  for  $\text{tbabs}$  has been frozen to  $2.5 \times 10^{21} \text{ cm}^{-2}$ . Pre-eclipse dips are marked with †.

ObsID	State	$\text{pcfabs}N_{\text{H}}$ ( $10^{22} \text{ cm}^{-2}$ )	kT (keV)	$\text{pcfabs}$ (percent)	$\Gamma$	Power-law norm.	$F_{0.3-12}$ ( $\text{erg cm}^{-2} \text{ s}^{-1}$ )	$\chi^2/\text{d.o.f}$
4509010101	Low	$3.2 \pm 0.2$	0.19	$0.89 \pm 0.02$	0.79	$0.0158 \pm 0.0007$	$(2.7 \pm 0.1) \times 10^{-10}$	176/130
4509010102	High	$< 0.02$	$0.192 \pm 0.002$	$0.00 \pm 0.05$	$0.73^{+0.03}_{-0.05}$	$0.0572 \pm 0.0008$	$(1.21 \pm 0.02) \times 10^{-9}$	300/161
4509010103	High	$27.3^{+15.6}_{-9.0}$	$0.191 \pm 0.003$	$0.24 \pm 0.08$	$0.9 \pm 0.1$	$0.10 \pm 0.01$	$(1.2 \pm 0.1) \times 10^{-9}$	159/147
4509010301	High	$43.9^{+23.6}_{-15.4}$	$0.192 \pm 0.004$	$0.3 \pm 0.1$	$0.6 \pm 0.1$	$0.08 \pm 0.01$	$(1.1 \pm 0.1) \times 10^{-9}$	143/143
4509010401 †	Low	$26.6^{+10.8}_{-9.3}$	0.19	$0.8 \pm 0.1$	0.79	$0.003^{+0.005}_{-0.001}$	$(1.6 \pm 0.2) \times 10^{-11}$	139/111
4509010501	Low	$17.5^{+6.9}_{-5.2}$	0.19	$0.59 \pm 0.05$	0.79	$0.0036 \pm 0.0006$	$(5.6 \pm 0.9) \times 10^{-11}$	240/124
4509010601	Intermediate	$26.6^{+5.7}_{-4.8}$	0.19	$0.29 \pm 0.07$	0.79	$0.069 \pm 0.008$	$(9 \pm 1) \times 10^{-10}$	177/130
4509010701	High	$32.3^{+8.7}_{-6.7}$	$0.187 \pm 0.002$	$0.28 \pm 0.05$	$0.78 \pm 0.04$	$0.087 \pm 0.008$	$(1.1 \pm 0.1) \times 10^{-9}$	268/162
4509010801	Intermediate	$15.8^{+4.6}_{-4.2}$	0.19	$0.16 \pm 0.05$	0.79	$0.050 \pm 0.004$	$(8.8 \pm 0.7) \times 10^{-10}$	226/160
4509010802	Low	$44.8^{+12.4}_{-10.0}$	0.19	$0.77 \pm 0.05$	0.79	$0.010 \pm 0.002$	$(1.0 \pm 0.2) \times 10^{-9}$	244/126
4509010803	High	$42.8^{+18.4}_{-12.9}$	$0.193 \pm 0.002$	$0.24 \pm 0.07$	$0.71 \pm 0.09$	$0.09 \pm 0.01$	$(1.3 \pm 0.1) \times 10^{-9}$	187/159
4509010901	High	$25.8^{+8.1}_{-6.3}$	$0.182 \pm 0.003$	$0.24 \pm 0.06$	$0.78 \pm 0.09$	$0.071 \pm 0.008$	$(1.0 \pm 0.1) \times 10^{-9}$	171/156
4509011001	Intermediate	$11.3 \pm 2.5$	0.19	$0.35 \pm 0.06$	0.79	$0.038 \pm 0.005$	$(3.9 \pm 0.5) \times 10^{-10}$	189/130
4509011101	Low	$37.5 \pm 14.8$	0.19	$0.66 \pm 0.00$	0.79	$0.005 \pm 0.001$	$(6 \pm 1) \times 10^{-11}$	324/125
4509011201 †	Low	$7.9 \pm 1.2$	0.19	$0.56 \pm 0.02$	0.79	$0.031 \pm 0.003$	$(4.8 \pm 0.5) \times 10^{-10}$	334/130
4509011301	High	$27.5^{+8.1}_{-6.1}$	$0.185 \pm 0.002$	$0.24 \pm 0.05$	$0.68 \pm 0.08$	$0.077 \pm 0.007$	$(1.1 \pm 0.1) \times 10^{-9}$	177/160
4509011401	High	$39.7^{+12.7}_{-9.6}$	$0.190 \pm 0.002$	$0.25 \pm 0.06$	$0.78 \pm 0.07$	$0.097 \pm 0.009$	$(1.3 \pm 0.1) \times 10^{-9}$	254/161
4509011501	Low	$27.9^{+12.2}_{-9.0}$	0.19	$0.77 \pm 0.07$	0.79	$0.007 \pm 0.005$	$(8 \pm 2) \times 10^{-11}$	137/117
4509011601	Low	$26.2^{+6.4}_{-5.6}$	0.19	$0.8 \pm 0.1$	0.79	$0.02 \pm 0.01$	$(4 \pm 3) \times 10^{-11}$	435/130
4509011701	High	$33.3^{+9.0}_{-7.0}$	$0.191 \pm 0.002$	$0.21 \pm 0.05$	$0.70 \pm 0.06$	$0.074 \pm 0.005$	$(1.09 \pm 0.07) \times 10^{-9}$	267/160
4509011901	High	$28.6^{+10.7}_{-7.6}$	$0.188 \pm 0.003$	$0.24 \pm 0.06$	$0.7 \pm 0.1$	$0.071 \pm 0.007$	$(1.0 \pm 0.1) \times 10^{-9}$	170/154
4509012001	Low	$28.9^{+17.0}_{-14.0}$	0.19	$0.6 \pm 0.1$	0.79	$0.005 \pm 0.001$	$(6 \pm 1) \times 10^{-11}$	282/123
4509012101	Low	$19.2^{+17.3}_{-13.8}$	0.19	$0.4 \pm 0.2$	0.79	$0.004 \pm 0.002$	$(3 \pm 2) \times 10^{-11}$	221/126
4509012201	High	$37.6^{+15.1}_{-11.3}$	$0.197 \pm 0.002$	$0.21 \pm 0.06$	$0.77 \pm 0.08$	$0.098 \pm 0.009$	$(1.3 \pm 0.1) \times 10^{-9}$	223/159
4509012301 †	Low	$30.4 \pm 1.9$	0.19	$0.947 \pm 0.004$	0.79	$0.0096 \pm 0.0008$	$(9.4 \pm 0.8) \times 10^{-11}$	441/130
4509012401	Intermediate	$34.4^{+15.8}_{-10.5}$	0.19	$0.16 \pm 0.08$	0.79	$0.056 \pm 0.006$	$(9 \pm 1) \times 10^{-10}$	193/130

low, and, intermediate stages. In this analysis, we closely monitored the variations in the spectral parameters as a function of superorbital period. Our analysis expands upon previous work by Dage et al. (2022), which examined only the high state spectra during excursion and by Pradhan et al. (2020), which did not consider any data taken during excursion.

In Fig. 2, the NICER band flux (Panel E) appears to be directly proportional to the flux of the source (Panel F) and its Swift/BAT count rate (Panel G). Since the power law produces the bulk of our continuum spectral model, it is not surprising that it fluctuates in the same way as the flux of the source.

Fig. 2 demonstrates that certain spectral parameters remain relatively unchanged across different superorbital states. Unsurprisingly, the characteristic disc blackbody temperature (kT) and power-law photon index ( $\Gamma$ ) of the continuum exhibit minimal variation. These results support previous findings that the shape of SMC X-1's high superorbital state X-ray continuum is stable over time (Dage et al. 2022; Brumback et al. 2023). We expand upon these findings by showing that the low and intermediate state spectra are well fit by a similar continuum model, which supports our assumption that the underlying continuum shape does not change. One possible explanation for the apparent stability of SMC X-1's underlying X-ray continuum is that the inner accretion flow is not sensitive to the rotation of the disc. Such a scenario would imply that the X-ray spectrum does not change with flux state, it simply modulates in normalization and absorption.

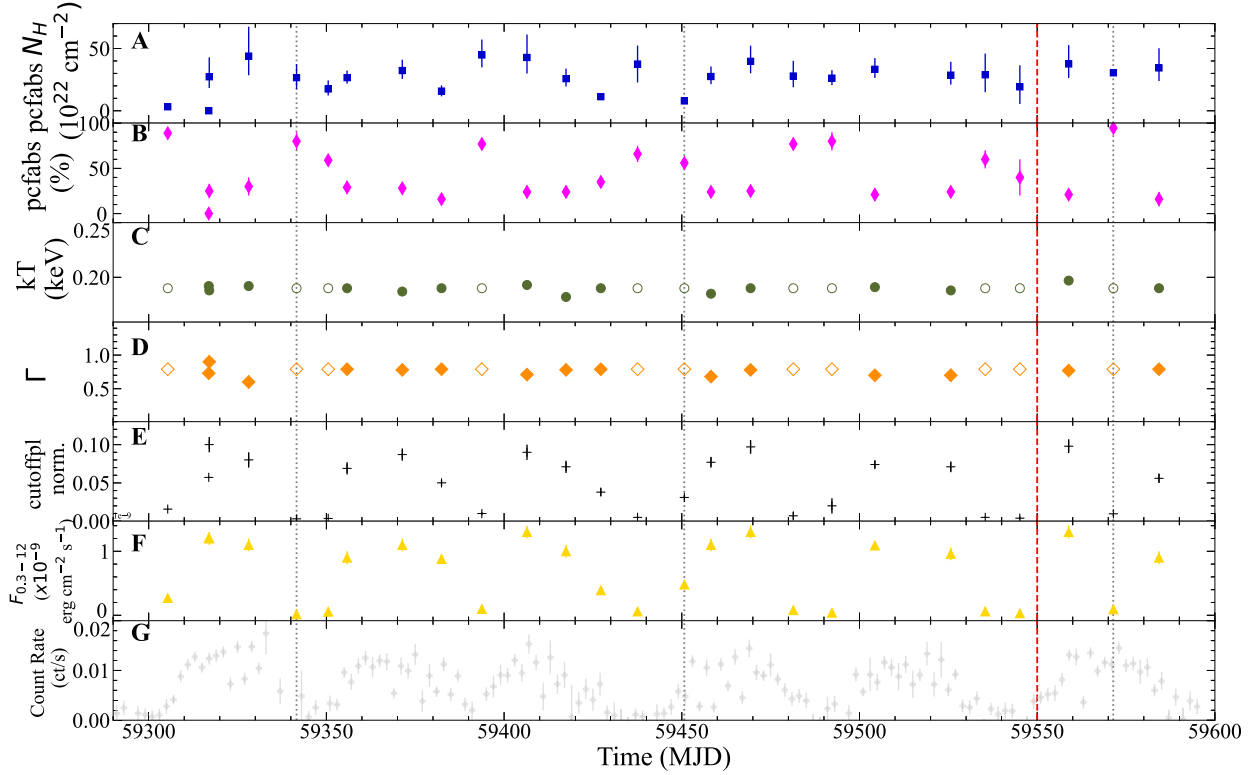
In addition to investigating how SMC X-1's excursion X-ray spectrum varied across superorbital state, we also investigated the differences between spectra taken during excursion and those taken after. In Fig. 2, the red vertical dashed line marks the end of the excursion period, however, there is no abrupt change in the variability of the spectral parameters around this epoch.

### 3.1 Correlation between covering fraction and superorbital phase

The  $\text{pcfabs}$  model parameters  $N_{\text{H}}$  and covering fraction modulate the shape of the soft end of the X-ray spectrum. Fig. 2 shows variability in both of these parameters across the time of our observations, although the  $N_{\text{H}}$  appears to become less variable with time.

Our spectral fitting results indicate a strong negative correlation between  $\text{pcfabs}$  covering fraction and source count rate, thus implying that the partial covering plays a significant role in the shape of the soft spectrum. To investigate the relationship between covering fraction and superorbital state, we plotted the covering fraction as a function of the NICER count rate in Fig. 4. We found that the covering fraction and superorbital state are inversely related, with the high-state observations having the largest count rates and smallest covering fractions and the low states having the smallest count rates and highest covering fractions. This relationship fits with our understanding of the warped accretion disc precession that drives





**Figure 2.** Variation with time (MJD) of the key SMC X-1 X-ray spectral fit parameters: Panel A (blue squares) shows  $pcfabs N_H$ . Panel B (pink diamonds) shows partial covering fraction. Panel C (green points) shows disc blackbody  $kT$ . Due to varying spectral quality between high and low state observations, we fix the  $kT$  in the low and intermediate state spectra to the average high state value of 0.19. The fixed values are plotted with open symbols, while the free values are plotted with filled symbols. Panel D (orange rhombuses) shows the  $\Gamma$  values. As in Panel C, reduced S/N in low state prompted us to fix this value in the low state spectra to the average high state value of 0.79. As before, the fixed points are plotted with open symbols while those where  $\Gamma$  was left variable are plotted with filled symbols. The impact of fixing these  $kT$  and  $\Gamma$  values is discussed in section 2.2. Panel E (black crosses) shows the normalization of the cut-off power law. Panel F (gold triangles) shows the total flux in the NICER band of 0.3–12 keV. Finally, Panel G (grey dots) shows the Swift/BAT light curve during the epoch where these observations were taken. The blackbody  $kT$  and  $\Gamma$  values fluctuate very little with superorbital phase, while the  $pcfabs N_H$  and covering fraction both show variations with superorbital period, and in particular the covering fraction shows a mostly smooth variation that is maximized during the superorbital low states. Table 2 details the spectral fit values. In all panels, the red vertical dashed line represents the end of the latest excursion epoch and the grey dotted lines mark the three observations that took place during pre-eclipse dip.

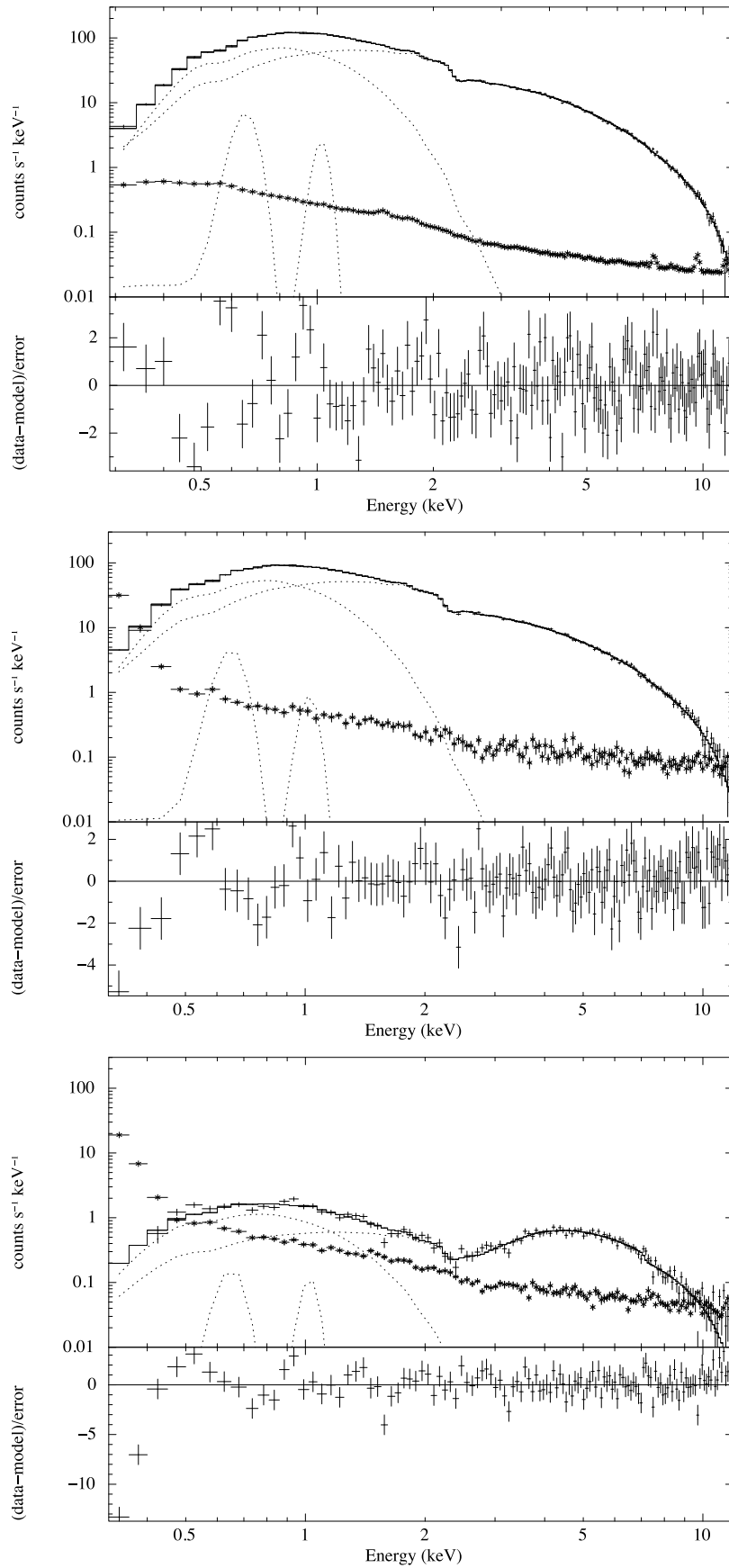
the superorbital period. To investigate the relationship between these two spectral parameters and source count rate in detail, we calculated the Pearson linear correlation coefficient for  $N_H$  against count rate and for  $pcfabs$  against count rate, which provides additional insights.

For the relationship between  $N_H$  and count rate, we obtained a correlation coefficient of 0.24 with a null hypothesis probability of 0.23, indicating no significant correlation. To determine the influence of outliers, we performed  $10^4$  bootstrap simulations. The resulting correlation coefficient distribution revealed a peak at  $r = 0.25$  with a standard deviation of 0.19, suggesting a large overlap with the null hypothesis. Additionally, we carried out  $10^4$  Monte Carlo simulations to test the impact of parameter uncertainties on the correlation coefficient. By considering the  $N_H$  0.1 cm uncertainty as the standard deviation in a Gaussian distribution for each simulation, we derived a correlation coefficient of  $-0.02 \pm 0.2$ . This indicates that the correlation between  $N_H$  and the count rate is statistically negligible.

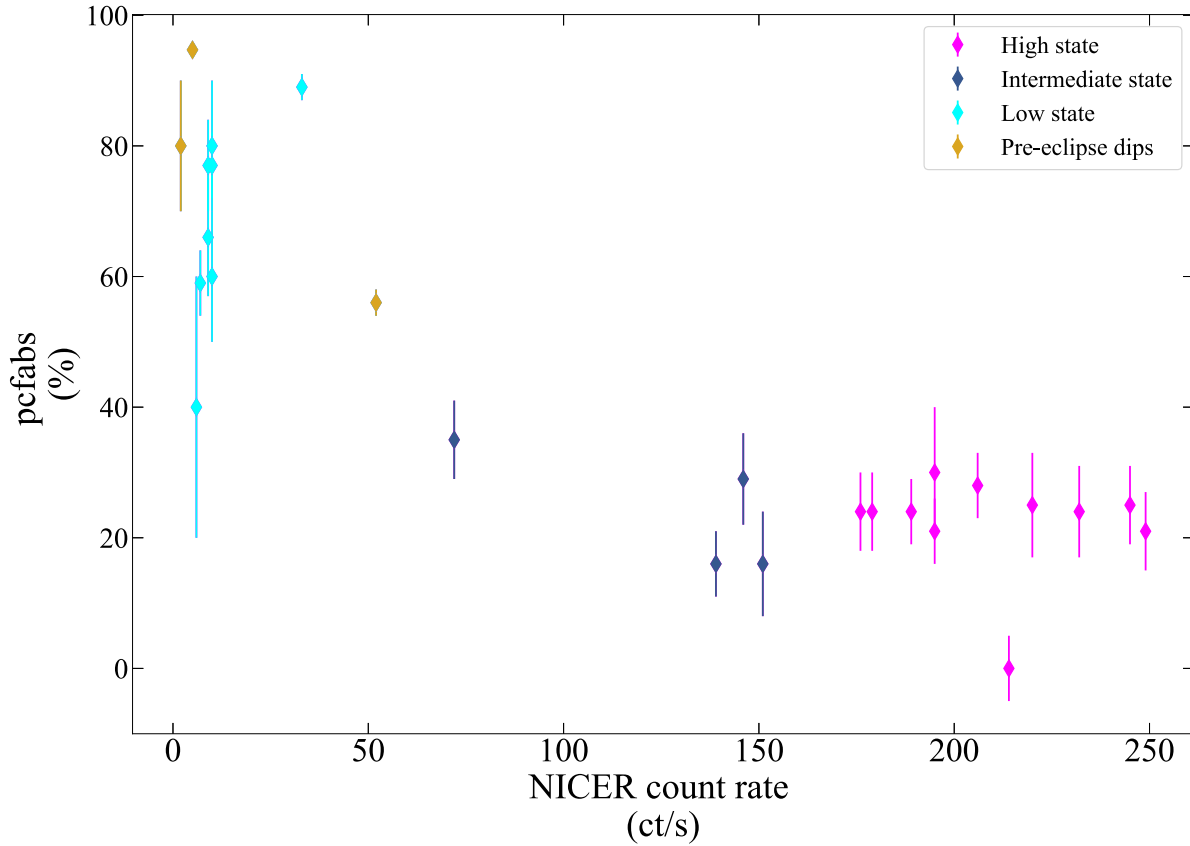
On the other hand, when examining the anticorrelation between  $pcfabs$  and count rate, we found a more substantial negative correlation with a coefficient of  $-0.86$ , with a null hypothesis probability of  $2.3 \times 10^{-8}$ . This implies a consistent inverse relationship between  $pcfabs$  and count rate. Employing the bootstrap method

resulted in a single-peaked distribution of the correlation coefficient, with an average value of  $-0.86$  and a standard deviation of 0.04. Similarly, Monte Carlo simulations produced a correlation coefficient of  $-0.83 \pm 0.04$ , consistent with the bootstrap findings. Thus, the observed anticorrelation between  $pcfabs$  and the count rate is highly significant compared to any relation between  $N_H$  and the count rate.

Under a model in which absorption by a warped, precessing disc is responsible for the superorbital modulation, we expect maximum obscuration during the superorbital low states and minimum obscuration during the superorbital high states. The only places where we see deviation from the inverse relationship between partial covering fraction and superorbital period are during pre-eclipse dips (see grey dotted lines in Fig. 2). These dips are orbital in nature and therefore can occur during the orbital high state. Our data set captured three pre-eclipse dips, defined as having an orbital phase higher than 0.8, based on the ephemeris from Falanga et al. (2015). These three observations, ObsIDs 4509010401, 4509011201, 4509012301 all showed high covering fractions, which agrees with the interpretation of similar features in Her X-1 (e.g. Giacconi et al. 1973) as increased obscuration by the ‘splash zone’ where the accretion stream impacts the disc.



**Figure 3.** Representative high state (top panel, ObsID 4509011701), intermediate state (middle panel, ObsID 4509012401), and low state (bottom panel, ObsID 4509012301) spectra fit with our best-fitting model.



**Figure 4.** Best-fitting partial covering fraction versus NICER count rate. The gold points denote pre-eclipse dips, the cyan points are low state observations, the dark blue are intermediate state, and the fuchsia are high state. Overall, the trend between partial covering fraction and superorbital period state appear to be correlated, indicating that the source’s low states coincide with a higher percentage of covering, and vice versa. As seen in Table 1, the observation lengths vary significantly, leading to larger error bars in shorter observations.

Additionally, Brumback et al. (2023) analysed 18 NICER observations of SMC X-1 during four different superorbital high states and found that the continuum parameters (blackbody temperature  $kT$  and  $\Gamma$ ) showed very little change between superorbital high states. Instead, they found that the most significant changes in spectral shape occurred between spectra from the superorbital intermediate state (when the source is increasing in luminosity as the accretion disc moves out of the line of sight) and the high state. Brumback et al. (2023) suggested that the underlying spectral continuum shape is constant, but is sensitive to changes in obscuration caused by the rotation angle of the disc. Our results from this analysis, particularly the inverse relationship between the covering fraction and superorbital period state, support these results and the conclusion that the inner accretion flow in SMC X-1 is insensitive to changes in the outer disc shape, although we are assuming that the underlying model continuum does not change significantly in the high/low state.

While our assumption of a constant spectral state seems well supported by the data, the full picture may be more complex. Pradhan et al. (2020) jointly fit SUZAKU and NuSTAR spectra and found that the power-law normalization (in the hard energy band of both detectors) is variable. From their spectroscopic fits, they conclude that there is evidence for a change in the partial covering fraction of the inner disc region, correlated with the superorbital variation. However, due to the power-law variability in the hard X-ray band, they suggest that there is another mechanism behind the superorbital variation, i.e. a change in the instantaneous accretion rate. We cannot

make a direct comparison to the Pradhan et al. (2020) spectra as our NICER observations do not extend above 12 keV, and do not fully constrain the power-law cut-off (as noted in Dage et al. 2022, the cut-off extends beyond the range to which NICER is sensitive). Like Pradhan et al. (2020), a correlation between the power-law normalization component ( $K$  of `xspec`’s `cutoffpl`) and the 0.3–12.0 keV model flux is apparent in the excursion data (panels E and F of Fig. 2), as expected for any major component of the source emission. However, our fits strongly suggest that the only correlation between the superorbital period and the X-ray spectral shape in the soft band is due to variation in the partial covering fraction of the inner accretion disc.

#### 4 CONCLUSIONS AND FUTURE WORK

We performed X-ray spectroscopy of 26 NICER observations of the neutron star pulsar SMC X-1 to investigate changes in spectral shape across superorbital states within excursion for the first time, and compare to data from outside excursion. Our best-fitting model for these observations is a blackbody and cut-off power-law continuum with several emission lines that is absorbed by a neutral absorber and a partial covering fraction, and we assume that the underlying model continuum does not change significantly in the low state. Our findings are summarized as follows:



- (i) The same spectral model can adequately describe all of the data regardless of superorbital state or excursion status.
- (ii) The partial covering parameter is inversely related to source count rate (a proxy for superorbital state). Pradhan et al. (2020) observed this relationship for non-excursion data, and the trend carries on in excursion. This implies a warped accretion disc is obscuring the source, and the superorbital period is caused by the rotating warped accretion disc covering flux from the neutron star.
- (iii) The spectral parameters show no change in the immediate vicinity of the end of excursion.  $N_H$  potentially shows a transition from an epoch of higher variability to a more stable epoch approximately 70 d before the end of excursion, but the correlation between these behaviours is unclear.

The next step will be to study the later observations in the MOOSE data set, which continue after the end of excursion and could provide more insights into the difference in spectral shape and parameter variability between excursion and non-excursion data.

The presence of soft emission lines in our data is also interesting. These disc-formed emission lines are effective observational tracers of how material in the accretion disc behaves and evolves over time. Throughout a binary orbit, line profile shape/strength will change, carrying within it an imprint of the evolving source of X-rays heating the accretion disc itself. An empirical connection between the line emitting regions, and physical properties of the X-ray source heating the disc, has proved to be an effective observational tool for understanding the structure and geometry of the gas making up accretion discs in low mass X-ray binaries (see Tetarenko et al. 2020; Tetarenko, Shaw & Charles 2023). In the future, a similar technique used for LMXBs could realistically be adapted and applied to SMC X-1, using a suitable model for X-ray irradiation in X-ray pulsar sources (e.g. Hickox & Vrtilek 2005).

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## DATA AVAILABILITY

The NICER observations are publicly available through HEASARC (<https://heasarc.gsfc.nasa.gov/docs/archive.html>).

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