

Testing an unstable cosmic neutrino background*

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I discuss how different cosmological observations can test the possibility that neutrinos might be unstable on cosmological times, resulting into an unstable cosmic neutrino background. I also discuss how actually there are different independent anomalies intriguingly hinting to such a possibility that would clearly point to new physics. I first focus on how the new DESI results place an upper bound on the sum of neutrino masses that starts to be in tension with the lower bound from neutrino oscillation experiments and how this tension could be easily solved assuming unstable relic neutrinos. Then I show how 21 cm cosmology allows to test radiative relic neutrino decays and how these could explain the controversial EDGES anomaly. I also discuss how the excess radio background and in particular the ARCADE 2 data can also be nicely explained by relic neutrino radiative decays. Finally, I point out the difficulties in building a model that does not clash with the upper limits on the effective magnetic moment coming from neutrino-electron scattering experiments and globular cluster stars.

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*Talk based on [1, 2]. Slides can be found at <https://www.southampton.ac.uk/pdb1d08/>

*Speaker

1. Exploring the unknown

Search of new physics is not just simply challenging but, with no evidence of new physics at colliders toward the end of the LHC Run III in 2026, it is becoming more and more clear that this will require in the next years not only formidable efforts but, likely, new ways to explore uncharted territories. High luminosity LHC will only start in 2030 and 100 TeV colliders likely not before 2050. Moreover, new physics might well lie in a region of parameter space, at high energies and/or small couplings, well beyond even the reach of future colliders. In this situation, cosmological observations and neutrino physics provide alternative ways to access such remote regions. On the other hand, the remote regions we can explore are not within our direct control but are somehow scattered in the energy versus couplings plane. It becomes then important to take advantage of all opportunities offered by experimental power and nature itself. Fortunately, many new observational tools became available in the last years or will soon become available. Not only low energy neutrino experiments are making considerable progress but also cosmological and astrophysical observations provide many new avenues. First of all, the discovery of gravitational waves has opened a new way to explore the physics of the early universe. In addition there are new observational tools that are providing new information with potential discoveries on the way: 21 cm cosmology experiments, CMB spectral distortions, the JWST telescope, new galaxy surveys such as DESI. These new observations are not only placing more stringent constraints, but in many cases are hinting to new physics, beyond the standard models of particle physics and cosmology. In my talk I will focus on the constraints from the CMB spectrum, 21 cm cosmology, excess radio background.

2. Constraints from CMB spectrum

The FIRAS instrument of COBE has measured the spectrum of the cosmic microwave background (CMB) in the frequency range (60 – 600) GHz, corresponding approximately to the photon energy range (2.5×10^{-5} – 2.5×10^{-3}) eV and placed very strong upper bounds on deviations from a Planckian spectrum with temperature $T_{\gamma 0} = (2.7255 \pm 0.0006)$ K [3]. These translate into strong constraints in the parameter of any model that predicts some amount of non-thermal radiation in that frequency range today. Interestingly, one can place a lower bound on the lifetime of active neutrinos decaying radiatively into active neutrinos ($\nu_j \rightarrow \nu_i + \gamma$ with $i, j = 1, 2, 3$). If the decaying active neutrinos are assumed to decay non-relativistically (for $m_i \gg T$), then the energy of the photon produced in the decay at the present time is simply given by

$$E_{\gamma 0} \simeq \frac{m_j^2 - m_i^2}{2m_j} \frac{1}{1 + z_D}, \quad (1)$$

where z_D is the redshift at the decay time and if $m_i \simeq m_j$. Since neutrino oscillation experiments measure $m_j^2 - m_i^2$, one can put constraints on the lifetime $\tau(\nu_j \rightarrow \nu_i + \gamma)$ versus the lightest neutrino mass m_1 , assuming normal ordering for definiteness and because current data disfavour inverted ordering. For example, consider the case $\nu_2 \rightarrow \nu_1 + \gamma$. In the hierarchical limit, for $m_1 \lesssim \sqrt{m_2^2 - m_1^2} \sim 10$ meV, one obtains the highest value of $E_{\gamma 0}$, for $z_D = 0$, given by $E_\gamma \simeq 5$ meV, that is beyond the detected FIRAS range. However, for $z_D \gtrsim 2$, there are still non thermal photons

that would be detected and this yields a constraint on the lifetime $\tau(\nu_2 \rightarrow \nu_1 + \gamma) \gtrsim 10^{20}$ s. In the quasi-degenerate case, for $m_1 \gtrsim m_{\text{sol}}$, one has $E_{\gamma 0} \simeq [(m_j - m_i)/2][1/(1 + z_D)]$ and, in particular, one obtains $E_{\gamma 0} \lesssim 2.5 \times 10^{-4}$ eV for $m_1 \gtrsim 0.1$ meV, below the FIRAS frequency range. In this case there would be no constraints but on the other hand the current cosmological upper bound on the sum of the neutrino masses, $\sum_i m_i < 0.12$ eV (95% C.L.) implies $m_1 \lesssim 0.03$ eV (95% C.L.), so that this limit would not be realised.

Radiative neutrino decays $\tau(\nu_j \rightarrow \nu_i + \gamma)$ necessarily imply a non-vanishing effective neutrino magnetic moment μ_{eff}^{ij} and this is true even if ν_i is a sterile neutrino. One has indeed the following general relation connecting radiative neutrino decay rate and effective neutrino magnetic moment [4, 5]

$$\Gamma_{\nu_j \rightarrow \nu_i + \gamma} = \frac{\mu_{\text{eff}}^{ij}}{8\pi} \left(\frac{m_j^2 - m_i^2}{m_j} \right)^3. \quad (2)$$

In this way a lower bound on $\tau(\nu_j \rightarrow \nu_i + \gamma)$ translates into an upper bound on μ_{eff}^{ij} . For example, the lower bound $\tau(\nu_2 \rightarrow \nu_1 + \gamma) \gtrsim 10^{20}$ s valid for $m_1 \lesssim m_{\text{sol}} \simeq 10$ meV, translates into an upper bound $\mu_{\text{eff}}^{ij} \lesssim 5 \times 10^{-8} \mu_B$, where $\mu_B \equiv e\hbar/(2m_e)$ is the Bohr magneton. For other active-to-active neutrino decay channels, one can obtain slightly more stringent upper bound. However, these are in any case three-four orders of magnitude looser than the upper bounds

$$\mu_{\text{eff}}^{ij} \lesssim 3.2 \times 10^{-11} \mu_B, \quad \mu_{\text{eff}}^{ij} \lesssim 3 \times 10^{-12} \mu_B \quad (3)$$

placed, respectively, by neutrino-electron scattering experiments [6] and globular cluster stars [7].

The Primordial Inflation Explorer (PIXIE) experiment will greatly improve FIRAS constraints on CMB spectral distortions and, correspondingly, the lower limits on lifetimes and the upper limit on magnetic moment placed by CMB will improve, respectively, by four and two orders of magnitude. Moreover, the lower frequency threshold will decrease down to ~ 30 GHz. In this way there is a consistency between the upper bound on μ_{eff}^{ij} obtained from CMB spectral distortions and those obtained from neutrino-electron scattering experiments and globular cluster stars.

Notice that, conversely, from Eq. (2) one can also translate the upper bound on the effective magnetic moment into a very stringent lower bound on the lifetime for radiative neutrino decays [2]

$$\tau_{\nu_i \rightarrow \nu_j + \gamma} \gtrsim 2.5 \times 10^{21} \text{ s} \left(\frac{\text{eV}}{\Delta m_{ij}} \right)^3. \quad (4)$$

For values $\Delta m_{ij} \ll 1$ eV, one obtains such long lifetimes that it is difficult to think of any cosmological observational opportunity to test them. Therefore, the upper bounds on the effective magnetic moment, represent a strong constraint on any cosmological application of relic neutrino radiative decays. We will be back on this important point in connection to an explanation of the excess radio background.

3. Cosmological tensions

There are different tensions in current data from cosmological observations within the Λ CDM model. The most famous tension is the Hubble tension [8]. The new JWST data seemed to solve the tension [9] but it has been noticed that, actually, they are not yet statistically significant so that the

tension still persists [10]. There is not a clear simple way to solve the Hubble tension. Extensions of the Λ CDM model can ameliorate it but not solve it completely [11]. Systematic uncertainties or local effects also do not seem enough to fully solve the tension. It might then be that this might be the result of a combination of different effects. The new DESI results on baryon acoustic oscillation (BAO) also support some cosmological tensions, though of different nature. While BAO data are compatible with a value of H_0 consistent with the value inferred by *Planck* data from CMB anisotropies, they support a model of dark energy different from a simple cosmological constant, with a dependence of the dark energy equation of state parameter on redshift.

However, there is another important tension emerging from DESI data that is relevant for our discussion. When these are combined with CMB data from *Planck* and ACT, the DESI collaboration obtains the following upper bound on the sum of neutrino masses within the Λ CDM model [12]

$$\sum_i m_{\nu_i} \leq 72 \text{ meV} \quad (95\% \text{ C.L.}) . \quad (5)$$

The best fit is obtained for $\sum_i m_{\nu_i} = 0$ when a prior $\sum_i m_{\nu_i} \geq 0$ is imposed. This upper bound is in clear tension with the lower bound imposed by neutrino oscillation experiments [13]

$$\sum_i m_{\nu_i} \geq 58 \text{ meV} . \quad (6)$$

This upper bound (5) has been revisited taking into account new *Planck* likelihoods resulting into a more relaxed one $\sum_i m_{\nu_i} < 120 \text{ meV}$ at 95% C.L. [14], implying a milder tension. However, even taking into account these different likelihoods for CMB data, new DESI results (DESI DR2 BAO + DR1 Full Shape) make the tension even stronger, since the upper bound on the sum of neutrino masses Eq. (5) gets even more stringent [15, 16]

$$\sum_i m_{\nu_i} \leq 64 \text{ meV} \quad (95\% \text{ C.L.}) . \quad (7)$$

The same DESI data seem to suggest that an extension of the Λ CDM model with an evolving dark energy equation of state parameter would solve the tension. Within a ' $w_0 w_a$ CDM' model the upper bound gets indeed relaxed to

$$\sum_i m_{\nu_i} \leq 163 \text{ meV} \quad (95\% \text{ C.L.}) . \quad (8)$$

However, when SN data are also combined the bound gets more stringent again and the DESI collaboration obtains (suing Pantheon+ data for SN)

$$\sum_i m_{\nu_i} \leq 117 \text{ meV} \quad (95\% \text{ C.L.}) , \quad (9)$$

so that some tension still persists considering that the best fit is still found for vanishing neutrino masses. A possible solution of this tension is to consider unstable relic neutrinos. The cosmological upper bound on the sum of neutrino masses we reported assumes neutrino lifetimes $\tau_{\nu_i} \gg 0.1 t_0$, where $t_0 \simeq 4 \times 10^{17} \text{ s}$ is the age of the universe. If all ordinary neutrinos decay with shorter lifetimes, then their role as hot dark matter can be neglected and the upper bound gets strongly

relaxed [17, 18]. The neutrino lifetimes should anyway be longer than $\sim 10^6 (\sum_i m_{\nu_i}/50 \text{ meV})^5$ not to have a clash with CMB anisotropies observations that support the presence of neutrino free streaming [19]. Moreover, from the CMB spectral distortion constraints we discussed, such short lifetimes necessarily imply that neutrinos have to decay invisibly. For example, if active neutrinos interact with a scalar field ϕ with interactions [17, 18]

$$\mathcal{L}_{\nu-\phi} = \frac{\lambda_{ij}}{2} \bar{\nu}_i \nu_j \phi + \text{h.c.}, \quad (10)$$

one would open the decay channel $\nu_i \rightarrow \nu_j + \phi$ with lifetime

$$\tau_{\nu_i \rightarrow \nu_j + \phi} \simeq 7 \times 10^{17} \text{ s} \left(\frac{0.05 \text{ eV}}{m_{\nu_i}} \right) \left(\frac{10^{-15}}{\lambda_{ij}^2} \right)^2. \quad (11)$$

Therefore, the tension between oscillation neutrino experiments and cosmological observations might be interpreted as if it suggests the existence of a low scale dark sector destabilising the cosmic neutrino background.

4. Radiative neutrino decays: specific intensity

We have seen that FIRAS constraints place stringent lower bound on the lifetime of active-to-active radiative neutrino decays since the photon energy necessarily lies within the FIRAS range. However, if the active neutrino ν_i decays into a sterile neutrino ν_0 , then neutrino oscillation experiments do not constraint $m_i^2 - m_0^2$ and the photon energy can be below the FIRAS low threshold energy $E_\gamma^{\text{FIRAS, low}} = 60 \text{ GHz} = 2.5 \times 10^{-4} \text{ eV}$. In this case, as we are going to discuss in next sections, one can consider different constraints coming from 21 cm cosmological global signal and excess radio background.

A quantity that describes non-thermal radiation is the *specific intensity*

$$I_{\gamma_{\text{nth}}}(E, z) \equiv \frac{d\mathcal{F}_E^{\gamma_{\text{nth}}}}{dA dt dE d\Omega} = \frac{1}{4\pi} \frac{d\varepsilon_{\gamma_{\text{nth}}}}{dE} = \frac{E^3}{4\pi^3} [e^{E/T_{\gamma_{\text{nth}}}(E, z)} - 1]^{-1}. \quad (12)$$

In the last expression $T_{\gamma_{\text{nth}}}(E, z)$ is the *effective (radiometric) temperature* of non-thermal radiation, corresponding to the temperature of a thermal (black body) radiation with the same specific intensity at frequency $\nu = E/(2\pi)$. For $E \ll T_{\gamma_{\text{nth}}}$, one obtains a simple linear relation between effective temperature and specific intensity

$$T_{\gamma_{\text{nth}}} \simeq \frac{4\pi^3}{E^2} I_{\gamma_{\text{nth}}}(E, z). \quad (13)$$

In the case of radiative neutrino decay one obtains for the specific intensity [1, 20, 21]:

$$I_{\gamma_{\text{nth}}}(E, z) = \frac{1}{4\pi} \frac{d\varepsilon_{\gamma_{\text{nth}}}}{dE} = \frac{n_{\nu_i}^\infty(z)}{4\pi} \frac{e^{-\frac{t(a_D)}{\tau_i}}}{H(a_D) \tau_i}, \quad (14)$$

where τ_i is the lifetime of the decaying neutrinos and $\varepsilon_{\gamma_{\text{nth}}}$ is the energy density of the non-thermal radiation. The quantities $H(a_D)$ and $t(a_D)$ are, respectively, the expansion rate and the age of the universe calculated at the time of decay of the relic neutrinos that produced photons with energy E

and detected at redshift z . The time of decay $t_D \equiv t(a_D)$ corresponds to a redshift $z_D = a_D^{-1} - 1$ and scale factor $a_D = (E/\Delta m_{0i}) a \leq a$. Finally,

$$n_{\nu_i}^\infty(z) = \frac{6}{11} \frac{\zeta(3)}{\pi^2} T^3(z) \quad (15)$$

is the relic neutrino number density calculated at the time of detection, at redshift z , in the standard stable neutrino case, where T is the standard photon temperature.

The expansion rate at the decay, $H(a_D)$, can be calculated in the Λ CDM model as

$$H(a_D) = H_0 \sqrt{\Omega_{M0} a_D^{-3} + \Omega_{\Lambda0}} = H_0 \sqrt{\Omega_{M0}} a_D^{-\frac{3}{2}} \left(1 + \frac{a_D^3}{a_{\text{eq}}^3} \right)^{\frac{1}{2}}, \quad (16)$$

where $a_{\text{eq}} \equiv (\Omega_{M0}/\Omega_{\Lambda0})^{1/3} \simeq 0.77$, $\Omega_{M0} \simeq 0.3111$, $H_0 \simeq t_0^{-1}$ and $t_0 \simeq 13.8 \text{ Gyr} \simeq 4.35 \times 10^{17} \text{ s}$ [22]. One can also obtain an analytical expression for the age of the universe at the time of decay, $t(a_D)$ [23]:

$$t(a_D) = \frac{2}{3} \frac{H_0^{-1}}{\sqrt{\Omega_{\Lambda0}}} \ln \left[\sqrt{\left(\frac{a_D}{a_{\text{eq}}} \right)^3} + \sqrt{1 + \left(\frac{a_D}{a_{\text{eq}}} \right)^3} \right]. \quad (17)$$

5. 21 cm cosmology

The 21 cm cosmological global signal represents an important diagnostic tool to test new physics after the recombination era [24]. The 21 cm (emission or absorption) line is produced by hyperfine transitions between the spin-singlet and triplet energy levels of the 1s ground state of Hydrogen atoms. The energy splitting between the two levels is $E_{21} = 5.87 \mu\text{eV}$, corresponding to a rest frequency $\nu_{21}^{\text{rest}} = 1.420 \text{ GHz}$. This transition can be used cosmologically to obtain information on the cosmological history and parameters in a wide redshift range $z \sim 7\text{--}200$. The 21 cm brightness temperature parameterises the brightness contrast between the cosmic radiation and the absorbed or emitted radiation in the 21 cm transitions is usually referred to as the 21 cm cosmological global signal and is approximately given by [25]

$$T_{21}(z) \simeq 23 \text{ mK} (1 + \delta_B) x_{H_I}(z) \left(\frac{\Omega_{B0} h^2}{0.02} \right) \left[\left(\frac{0.15}{\Omega_{M0} h^2} \right) \left(\frac{1+z}{10} \right) \right]^{1/2} \left[1 - \frac{T_\gamma(z)}{T_S(z)} \right], \quad (18)$$

where $T_S(z)$ is the spin temperature describing the triplet-to-singlet state density ratio. In this expression $\delta_B = (\rho_B - \bar{\rho}_B)/\bar{\rho}_B$ is the fractional baryon overdensity, $x_{H_I}(z)$ is the neutral hydrogen fraction. If the spin temperature is equal to the photon temperature ($T_S = T_\gamma$), then photons are absorbed and reemitted with the same intensity and there is no visible signal. Also, if all atoms are ionised so that $x_{H_I} = 0$, there cannot be any signal.

The most prominent feature that is expected within the Λ CDM model in the 21 cm cosmological signal is an absorption signal, corresponding to a negative value of T_{21} , at redshifts in the range $z = 10\text{--}30$. The EDGES collaboration claimed to have detected such absorption feature centred at $z = z_E \simeq 17$ [26], thus within the expected range of redshifts. However, the measured (negative) value of T_{21} is approximately twice the expected one. This anomalous signal can be interpreted in terms of a non-thermal radiation component produced by relic neutrino decays with a temperature,

at $z = z_E$, $T_{\gamma_{\text{nth}}} \simeq 60$ K. We can assume, for definiteness, that the decaying neutrinos are the lightest active neutrinos decaying non-relativistically into quasi-degenerate sterile neutrinos. The Eq. (14) has to be specialised to the case $z = z_E$ and $E = E_{21} = 5.87 \mu\text{eV}$ and imposing $T_{\gamma_{\text{nth}}}(z = z_E) \simeq 60$ K, one obtains

$$(\Delta m_1^{3/2} \tau_1)^{\text{EDGES}} \simeq 4.0 \times 10^{13} \text{ eV}^{3/2} \text{ s}. \quad (19)$$

The EDGES anomaly is controversial and a few studies have suggested that the signal is contaminated by some foreground contribution, for example originating in the ionosphere. The SARAS3 experiment has even rebutted the EDGES claim [27], so we need to wait for more results. In this respect it is exciting that the moon-based experiment LuSEE will soon be able to measure the 21 cm cosmological global signal in absence of Earth foregrounds [28].

6. Excess radio background

The ARCADE 2 balloon-borne experiment has measured the absolute temperature of sky at frequencies in the range (3–10) GHz [29], well below the FIRAS low threshold, and covering a 8.4% portion of the sky. Only 6 data points gave in the end a meaningful result not dominated by noise. These point clearly show an excess compared to the CMB temperature that is not described by a thermal component (that implies that the temperature changes with the frequency). The excess cannot be explained in terms of a known population of radio sources and different attempts have not detected any anisotropy so that the source of the excess has to be extremely smooth and this seems to suggest that can be better described by a smooth background rather than unknown radio sources. It also disfavours solutions where the signal is somehow correlated with the dark matter distribution, since one would expect some level of anisotropy that is excluded by the observations. It is quite fair to conclude that the ‘nature of the background is still unknown’ [30], and for this reason the excess radio background should be regarded as a mystery.

An intriguing possibility is that the source of non-thermal radiation is given by non-relativistic radiative relic neutrino decays into quasi-degenerate sterile neutrinos, as we discussed in the case of the 21 cm global signal. As for the 21 cm cosmological signal, we can still start from the general expression Eq. (12) and specialise it at the present time and this time, since we have different energies to fit, leave indicated the energy dependence (also contained in a_D), finding

$$T_{\gamma_{\text{nth}}}(E, 0) \simeq \frac{6 \zeta(3)}{11 \sqrt{\Omega_{\text{M}0}}} \frac{T_0^3}{E^{1/2} \Delta m_1^{3/2}} \frac{t_0}{\tau_1} \left(1 + \frac{a_D^3}{a_{\text{eq}}^3} \right)^{-\frac{1}{2}}. \quad (20)$$

When this is used to fit the six data points found by ARCADE 2, one finds as a best fit [1]

$$\tau_1 = 1.46 \times 10^{21} \text{ s}, \quad m_1 - m_s = 4.0 \times 10^{-5} \text{ eV} \quad (21)$$

with a very good $\chi_{\text{min}}^2 \simeq 1$. The curve for the effective temperature for these best fit parameters is shown in the figure with a orange thick solid line. In the vertical axis $T_{\text{ERB}}(E) \equiv T_{\gamma 0}(E) - T_{\text{CMB},0}$ is the effective temperature of the excess radio background. It can be noticed how one of the most clear features of the fit is the existence of an end-point at $E = m_1 - m_s$. These best fit values correspond to $\Delta m_1^{3/2} \tau_1 \simeq 4.0 \times 10^{14} \text{ eV}^{3/2} \text{ s}$, a value about 1 order of magnitude higher than the

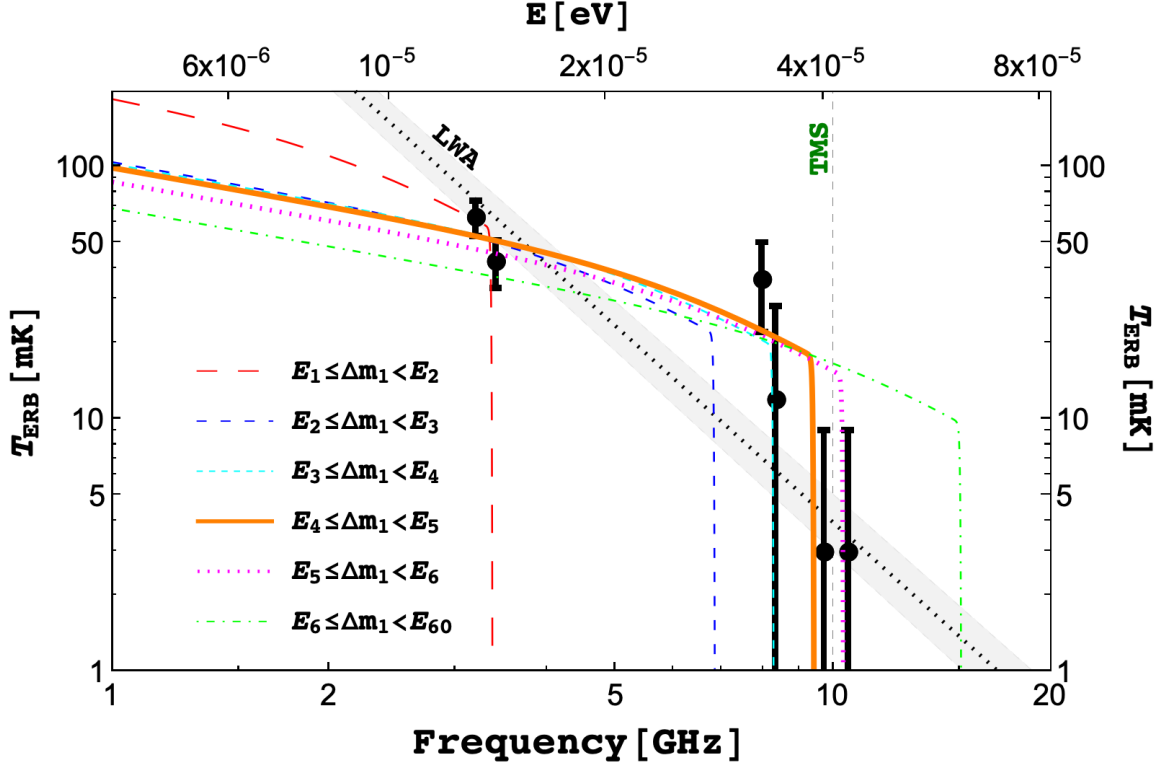


Figure 1: Best fit curves for T_{ERB} obtained with Eq. (20). The thick solid orange curve corresponds to a solution very close to the best global fit ($\Delta m_1 = 4.0 \times 10^{-5}$ eV and $\tau_1 = 1.46 \times 10^{21}$ s). The ARCADE 2 data points are taken from Ref. [29], while the power-law fit $\beta = -2.58 \pm 0.05$ (dotted line with grey shade) is from [31]. The figure is taken from [1].

best fit value Eq. (19) explaining the EDGES anomaly. Even taking into account the errors, there is a $\sim 3\sigma$ tension. However, this is not a problem since as we said the EDGES anomaly might be dominated by foregrounds and the anomalous signal one can predicts from the solution to the excess radio background is much weaker than the one observed by EDGES. Of course, the opposite would have been a problem, since EDGES should have seen such a strong signal.

This result sounds very exciting but there is a clear challenge: it violates the lower limit on the lifetime in Eq. (4) that in our case gives $\tau_i \gtrsim 10^{36}$ s. A model should then be able to circumvent the connection between lifetime and effective magnetic moment enforced by the relation (2).

7. Final remarks

- New exciting cosmological tools allow to explore new physics in regimes, both energy and coupling-wise, inaccessible to colliders;
- At very low scales there are interesting mysteries that might be explained by an unstable relic neutrino background decaying invisibly and radiatively;

- The short requested lifetimes to solve the excess radio background, and possible the EDGES anomaly, are challenging to explain without violating the upper bounds on the effective magnetic moment but this maybe makes things even more exciting;
- We will have soon experiments testing these ideas, both lunar-based radio antennas that will try to detect the 21 cm cosmological global signal and the new Tenerife microwave spectrometer (TMS) that will try to measure the excess radio background at higher frequencies than ARCADE 2.

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